

1 Article

2 Iterative positioning algorithm of the target node 3 based on distance correction in WSN

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12 Received: date; Accepted: date; Published: date

13 **Abstract:** The node position information is critical in the wireless sensor network (WSN). However,
14 the existing positioning algorithms commonly have low positioning accuracy because of noise
15 interferences in communication. To solve this problem, this paper presents an iterative positioning
16 model based on distance correction to improve the positioning accuracy of the target node in WSN.
17 First, the log-distance distribution model of received signal strength indication (RSSI) ranging is
18 built and the noise impact factor is derived based on the model. Second, the initial position
19 coordinates of the target node are obtained based on the triangle centroid localization algorithm,
20 thereby calculating the distance deviation coefficient under the influence of noise. Then, the ratio of
21 the distance measured by the log-normal distribution model to the median distance deviation
22 coefficient is taken as the new distance between the anchor node and the target node. Based on the
23 new distance, the triangular centroid positioning algorithm is used again to calculate the target
24 node coordinates. Finally, the iterative positioning model is constructed, and the distance deviation
25 coefficient is updated repeatedly to update the positioning result until the set number of iterations
26 is reached. Experiment results show that the proposed iterative positioning model can improve
27 positioning accuracy effectively.

28 **Keywords:** iterative positioning algorithm; distance correction; RSSI; noise impact factor; distance
29 deviation coefficient
30

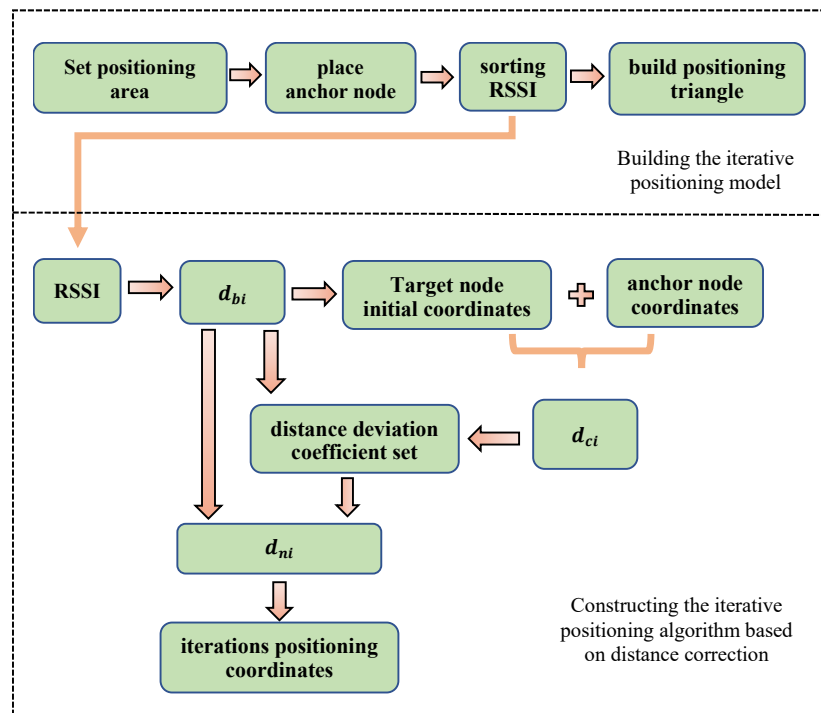
31 1. Introduction

32 Wireless sensor network has been applied widely in various fields of defense, industry and
33 social life due to its advantages of low power consumption, low cost, self-organization and so on. In
34 order to provide effective monitoring services in engineering applications, the nodes own position
35 information must be provided [1,1]. The node position information is the key to whether the
36 information obtained is valuable or not in WSN, especially for the target reconnaissance and
37 tracking in the field of military and anti-terrorism [3,4]. It can be said that perceived data are
38 meaningless if no node position information are provided. However, in the actual physical
39 environment, the wireless signals are inevitably interfered by noises such as multi-path fading [5,6],
40 diffraction [7], antenna gain [8], non-line of sight [9] and so on in the process of propagating, and
41 uncertain propagation loss is produced, which results in inaccuracy in ranging. The maximum
42 ranging error is up to $\pm 50\%$ [10].

43 To solve this problem, the node positioning method in WSN should be explored deeply. An
44 effective node positioning method must consider the following problems. (1) How to construct a
45 mathematical model to fit the nonlinear relationship between the RSSI and the distance? (2) What

46 kind of positioning algorithm should be used to obtain more accurate positioning accuracy? (3)
 47 What are the basic requirements to consider in terms of hardware resources and computational
 48 complexity when building a positioning algorithm?

49 Based on the above three problems, we proposed the target node iterative positioning
 50 algorithm based on distance correction in this paper. The motivation of this paper is reducing the
 51 positioning error of the target node to help users obtain accurate position information. The process
 52 of the target node iterative positioning model based on distance correction is shown as Figure 1.



53

54 **Figure 1.** The process of the target node iterative positioning model based on distance correction

55 In our proposed algorithm, the median of the distance deviation coefficients is used to modify
 56 the measured distance during each iteration. The median of the distance deviation coefficients can
 57 more closely express the overall distance deviation characteristic. The log-distance distribution
 58 model is used to calculate the distance between unknown target nodes and connected anchor nodes
 59 in order to fit the nonlinear relationship between distance and RSSI more accurately, and reduce
 60 computational complexity. The iterative positioning model is constructed to ensure that the target
 61 node is in the area enclosed by the connected anchor nodes, which is also of great help to improve
 62 the positioning accuracy. In addition, the node iterative positioning algorithm based on distance
 63 correction can provide theoretical support for future research. Contributions are included in the
 64 following aspects.

65 (1) Derivation of noise impact factor based on log-normal distribution model

66 The expression of the noise impact factor FN is derived by reconstructing mathematical model,
 67 which is the corresponding numerical relationship between the noise impact factor FN and the
 68 measured distance. The noise impact factor proposed in this paper is used to describe the
 69 influence degree of noise on the measured values of RSSI.

70 (2) The selection of distance deviation coefficient on node measured distance

71 The distance deviation coefficient is used to evaluate the deviation degree of the distances
 72 calculated by the log-distance distribution model and the triangle centroid algorithm
 73 respectively, and a distance deviation coefficients set is established. The median of the distance
 74 deviation coefficient set is selected to characterize the deviation degree of the whole node
 75 measured distances, which can better reflect the overall distance deviation characteristic.

76 (3) Construction of the iterative positioning algorithm based on distance correction

77 The distance deviation coefficient median is used as an iteration factor for the iterative
78 positioning algorithm. In the process of each iteration, the median of the distance deviation
79 coefficients is used to correct the distance from the last positioning, obtaining a distance value
80 closer to the true value. The triangle centroid localization algorithm is iteratively used to reduce
81 the positioning fluctuation error and improve positioning accuracy.

82 The rest of the paper has been organized as follows: Section 2 will demonstrate a brief review of
83 related works. The proposed iterative positioning algorithm will be provided in Section 3. The
84 iterative positioning model will be constructed in Section 4. The experimental results and some
85 analysis will be given in Section 5. Finally, key conclusions and the general discussion will be
86 summarized in Section 6.

87 2. Related works

88 This section reviews two existing works which are the reference foundation theory for
89 positioning of the target node in WSN. First is the measurement of the distance between the target
90 node and the anchor node. Second is to determine the position coordinates of the target node.

91 2.1. The measurement of distance between the target node and the anchor node

92 The measurement of distance between the target node and the anchor node is an important
93 research topic of the node positioning in WSN. Nowadays, most of the existing node positioning
94 algorithms can be divided into two categories according to whether it is necessary to measure the
95 distance or angle. One is the range-based measurement positioning algorithm and the other is
96 range-free measurement positioning algorithm [11]. The distance measurement refers to calculating
97 the distance or orientation between the unknown target node and the anchor node connected thereto
98 through communication between them [12]. The classical distance measurement algorithms include
99 based on signal time of arrival (TOA), signal time difference of arrival (TDOA) [13], Angle of Arrival
100 (AOA) [14] and received signal strength (RSSI) [15,16] algorithms.

101 The first three algorithms need to accurately calculate the distance or angle between the
102 unknown target node and the anchor node, thereby these three algorithms significantly improve the
103 energy consumption of the node and the hardware equipment requirements of the network in the
104 positioning process, and increase the calculation amount and communication cost of the network.
105 The RSSI ranging method is often adopted in practical applications.

106 2.2. The target node positioning algorithm

107 The target node positioning algorithm can be built in several ways. A triangle centroid
108 positioning algorithm based on the distance or relative angle information between the target node
109 and the anchor node has been proposed in the document [17-19]. There are problems of the target
110 node deviating effective locating area and the large positioning error in the positioning algorithm
111 because the node distribution characteristics are not entirely considered. The weighted centroid
112 positioning algorithm has been presented in the document [20-22] by introducing weight factor,
113 which is related to the distance estimation. Therefore, if there is a large deviation in distance
114 estimation, the positioning error will be large. A fingerprint database positioning algorithm has been
115 constructed to improve the positioning accuracy in the document [23-25] by collecting the
116 positioning samples in advance. The positioning algorithm highly relies on the fingerprint database
117 data, if the environment changes, the positioning accuracy will become poor. The positioning
118 algorithm based on the neural network has been put forward in documents [26,27], the input of the
119 algorithm is the value of RSSI and the output is the distance between nodes. Due to the simple
120 learning rules, the output of the neural network cannot be correct when the data is not sufficient. The
121 positioning algorithm based on Bounding-Box has been proposed in the document [28,29]. The
122 positioning accuracy of the algorithm depends on the number of anchor nodes. The positioning
123 accuracy is not high if the number of anchor nodes is not enough.

124 For the above problems, an iterative positioning algorithm based on distance correction is
 125 proposed through correcting the estimated distance between the anchor node and the target node,
 126 and constraining the target node in the sub-triangular positioning area of the iterative positioning
 127 model in this paper. The algorithm calculates the target node coordinates iteratively and improves
 128 positioning accuracy effectively.

129 3. Iterative positioning algorithm for the target node based on distance correction

130 An iterative positioning algorithm for the target node based on distance correction is proposed
 131 in this paper to help users overcome the influence of noise on positioning accuracy. There are three
 132 main key problems presented in this paper for building iterative positioning algorithm based on
 133 distance correction. First, the log-normal distribution mathematical model should be constructed to
 134 measure RSSI, based on which the impact factor of noise on distance detecting can be derived.
 135 Second, a triangle centroid positioning algorithm should be built to determine the initial
 136 positioning coordinates of the target node. Finally, the distance deviation coefficient and its median
 137 can be determined. Therefore, the iterative positioning algorithm for the target node based on
 138 distance correction is constructed according to the median of distance deviation coefficient.

139 3.1. Basic concept

140 **Definition 1.** WSN node positioning. WSN node positioning refers that the position of the unknown target
 141 node is calculated based on the communication between the anchor nodes whose position information are known
 142 in the network by certain techniques, algorithms and schemes [30].

143 **Definition 2.** Anchor node. The anchor node is the node whose coordinates or position information is known in
 144 WSN [31].

145 **Definition 3.** Target node. The target node refers to the node whose coordinates or positioning information is
 146 unknown in the WSN [32].

147 3.2. The preprocessing of iterative positioning algorithm

148 Before the constructions of the iterative positioning algorithm, it is necessary to do some
 149 preprocessing tasks. First of all, the mathematical model of RSSI was constructed and used to
 150 calculate the initial measured distance. Then, analyzing the influence of noise on the measured
 151 distance and constructing the noise impact factor. Finally, the triangle centroid positioning
 152 algorithm is used to obtain the initial positioning coordinates of the target node.

153 3.2.1. RSSI ranging algorithm

154 The basic idea of the RSSI ranging algorithm is to calculate the distance between the
 155 transmitting signal node and the receiving signal node by measuring the received signal strength
 156 because there are varying degrees of losses in the propagation process of wireless signals. Therefore,
 157 it is very important to build an appropriate RSSI ranging model. At present, the model used
 158 commonly is the log-normal distribution model [33-35].

159 P_d is used to indicate the power measurement corresponding to the distance between two
 160 nodes as d , P_{d_0} is used to indicate the power measurement corresponding to the distance between
 161 two nodes as d_0 . The relationship between P_d and d can be expressed as

$$P_d = \frac{P_{d_0}}{\left(\frac{d_0}{d}\right)^n}, \quad (1)$$

162 where n is a signal propagation factor, which is usually obtained by empirical value or actual
 163 calibration.

164 The logarithmic processing is performed on both sides of the formula (1), and after arranging,
 165 the formula (2) can be obtained:

$$\lg Pd = \lg Pd_0 - n \lg\left(\frac{d}{d_0}\right), \quad (2)$$

166 And because the relationship between RSSI value and power can be expressed as:

$$RSSI = 10 \lg p, \quad (3)$$

167 Thus, a mathematical model of RSSI ranging can be obtained:

$$P(d) = P(d_0) - 10n \lg\left(\frac{d}{d_0}\right), \quad (4)$$

168 where $P(d)$ $P(d)$ is the RSSI value when the distance between two nodes is d , and $P(d_0)$ $P(d_0)$ is the
169 RSSI value when the distance between two nodes is d_0 .

170 3.2.2. The effect of noise on RSSI ranging

171 The loss of the wireless signal during propagation has a great influence on the accuracy of the
172 RSSI ranging algorithm and must be considered in practical applications. Next, we will analyze the
173 effect of signal propagation loss on RSSI ranging. In the formula (4), the measurement value $P(d)$ is
174 composed of the true signal strength value and noise signal strength value, denoted as $P_T(d)$ and $P_N(d)$
175 respectively. $P(d_0)$ is the RSSI value when the distance between two nodes is d_0 . To simplify the
176 calculation, d_0 is usually taken as 1, and $P(d_0)$ is denoted as A .

177 Thus, the actual mathematical model of the log-normal distribution model is as follows:

$$P_T(d) - P_T(d) = A - 10n \lg(d), \quad (5)$$

178 From the formula (5), the distance between two nodes can be calculated as follows:

$$d = 10^{\frac{A - [P_T(d) - P_N(d)]}{10n}}, \quad (6)$$

179 Equation (6) can be calculated as follows by further mathematical transformation:

$$d = 10^{\frac{A - P_T(d)}{10n}} 10^{\frac{P_N(d)}{10n}}, \quad (7)$$

180 Assume that $K_1 = \frac{A - P_T(d)}{10n}$, $K_2 = \frac{P_N(d)}{10n}$ $K_1 = \frac{A - P_T(d)}{10n}$ $K_2 = \frac{P_N(d)}{10n}$.

181 Formula (7) can be expressed as

$$d = 10^{K_1} (1 + 10^{K_2} - 1), \quad (8)$$

182 Formula (8) can be expanded further as:

$$d = 10^{K_1} + 10^{K_1} (10^{K_2} - 1), \quad (9)$$

183 Assume that $d_T = 10^{K_1}$, $F_N = 10^{K_2} - 1$ Therefore, the calculation of distance d can be

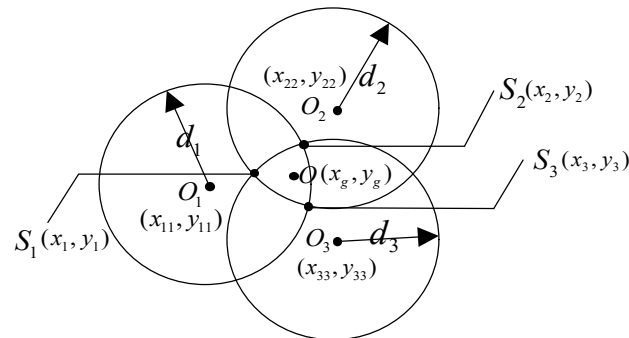
184 simplified as follows:

$$d = d_T + d_T F_N, \quad (10)$$

185 where $d_T = 10^{K_1}$ $d_T = 10^{K_1}$ is the true distance between the anchor node and the target node,
186 $F_N = 10^{K_2} - 1$ $F_N = 10^{K_2} - 1$ is the impact factor of noise on distance measurement. F_N is referred
187 to as noise impact factor in this paper.

188 3.2.3. The triangular centroid positioning algorithm

189 The basic principle of the triangle centroid positioning algorithm is as follows: the three circles
 190 are determined by treating the three anchor nodes as their respective circle centres, by treating the
 191 distances between the anchor nodes and the target node as their respective radii. The
 192 intersection of the three circles can obtain six intersection points, a triangle is constructed by
 193 treating the three closer intersection points as vertexes, the centroid of the triangle is taken as the
 194 coordinates of the node to be positioned. The schematic diagram of triangular centroid positioning
 195 is shown in Figure 2.



196
 197

Figure 2. Schematic diagram of triangular centroid positioning

198 In Fig. 2, and O_1 , O_2 and O_3 are defined as the positions of three anchor nodes with coordinates
 199 of $O_1(x_{11}, y_{11})$, $O_2(x_{22}, y_{22})$ and $O_3(x_{33}, y_{33})$, which radius are d_1 , d_2 , and d_3 respectively. Point $S_1(x_1, y_1)$,
 200 $S_2(x_2, y_2)$ and $S_3(x_3, y_3)$ are the three closer intersection points, that is, the three vertexes of the triangle
 201 centroid positioning algorithm.

202 The intersection point coordinates of the circle O_1 and the circle O_2 can be obtained by equation
 203 (11).

$$\begin{cases} (x - x_{11})^2 + (y - y_{11})^2 = d_1^2 \\ (x - x_{22})^2 + (y - y_{22})^2 = d_2^2 \end{cases} \quad (11)$$

204 In the 2 sets of coordinates solved by equation (11), the intersection $S_3(x_3, y_3)$ closer to the
 205 center of the positioning triangle. The solution of the remaining two points $S_1(x_1, y_1)$ and $S_2(x_2, y_2)$ is
 206 similar to that of point $S_3(x_3, y_3)$.

207 Thus, the initial coordinates $O(x_g, y_g)$ of the target node can be calculated by equation (12).

$$\begin{cases} x_g = \frac{1}{m} \sum_{i=1}^m x_i \\ y_g = \frac{1}{m} \sum_{i=1}^m y_i \end{cases} \quad (m=3), \quad (12)$$

208 where $m=3$, $i = 1, 2, 3$.

209 3.3. The iterative positioning algorithm

210 In the actual physical environment, signals are easily disturbed by noise in the transmission
 211 process. Therefore, there is a large deviation between the distance obtained by the log-normal
 212 distribution model and the real distance value. In order to reduce the positioning error further, a
 213 node iterative positioning algorithm based on distance correction is introduced in the paper.

214 The basic principle of the iterative positioning algorithm based on distance correction is as
 215 follows: the distance deviation coefficient is introduced to evaluate the degree of deviation of the
 216 measurement distance between the log-normal distribution model and based on the triangle
 217 centroid positioning algorithm. The distance between the anchor node and the target node is
 218 recalculated based on the distance deviation coefficient. By constantly updating the distance
 219 between the anchor node and the target node, the target node coordinates are iteratively calculated.

220 3.3.1. The calculation of the distance deviation coefficient

221 The distance between the anchor node and the target node, which is calculated by the
 222 log-normal distribution model, is denoted as d_{bi} . The distance between the anchor node
 223 coordinates and the coordinates, which are calculated by the triangle centroid positioning algorithm,
 224 is denoted as d_{ci} . In order to indicate the deviation of the two distances, the distance deviation
 225 coefficient C_{dev} is defined as equation (13).

$$C_{dev} = \frac{d_{bi}}{d_{ci}} \quad (i=1, 2, 3), \quad (13)$$

226 Many distance deviation coefficients can be solved by the formula (13), and it is important to
 227 determine a characteristic quantity to represent the degree of deviation of the overall node
 228 measurement distance. The two statistical parameters, the average value and the median of distance
 229 deviation coefficients, can both closely be used to express the overall distance deviation
 230 characteristics.

231 The average value of distance deviation coefficients can be expressed the average level of the
 232 overall measurement distance deviation. However, its fatal disadvantage is that if the extremum at
 233 both ends is too low or too high, the final calculation result will greatly deviate from the real
 234 situation.

235 Therefore, the median distance deviation coefficients are usually used to express the overall
 236 distance deviation characteristic. The median is not affected by the extreme values of both ends, and
 237 can better reflect the overall distance deviation characteristics, making the final calculation result
 238 closer to the real situation.

239 The distance deviation coefficients are calculated by the formula (13), the median C_{dev} can
 240 be obtained after sorting.

241 The distance between the anchor node and the target node can be recalculated based on the
 242 median C_{dev} as shown in equation (14).

$$d_{ni} = \frac{d_{bi}}{C_{dev}} \quad (i=1, 2, 3), \quad (14)$$

243 The new distance d_{ni} is obtained by the formula (14), and the triangular centroid positioning
 244 algorithm is iteratively conducted to obtain the positioning result (x_G, y_G) .

245 3.3.2. The iteration termination criteria for algorithm.

246 If the termination condition of the iterative positioning algorithm is set correctly, the higher
 247 positioning accuracy can be obtained with only a small number of iterations, and the algorithm is
 248 prevented from falling into an infinite loop. In general, the iteration termination condition is defined
 249 as:

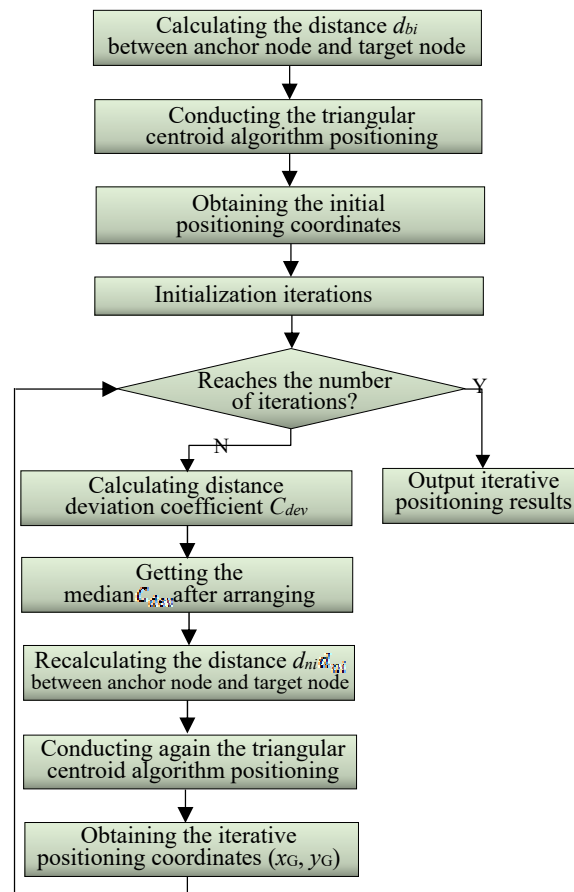
$$P_{\hat{\theta}_n} - P_{\hat{\theta}_{n-1}} < \varepsilon, \quad (15)$$

250 Where $P_{\hat{\theta}_n}$ is the RSSI value between the centroid of the n th iteration and the unknown target
 251 node, ε is the set threshold.

252 Under different environmental conditions, if formula (15) is used as the iterative termination
 253 condition, its computational complexity is very high, even higher than the complexity of the
 254 iterative positioning algorithm itself. In this way, the hardware complexity of the system will
 255 increase significantly and the algorithm become almost infeasible. In practical applications, as the
 256 number of iterations increases, the positioning error has the following cases: fast convergence, slow
 257 convergence, and periodic oscillation. By simulation analysis, it is found that, when the number of
 258 iterations is between 0-10 times, the iteration error varies with different regular pattern, the
 259 iteration error basically unchanged when the number of iterations is between 10-20 times.

260 The flow chart of the iterative positioning algorithm is shown in Figure 3.

261

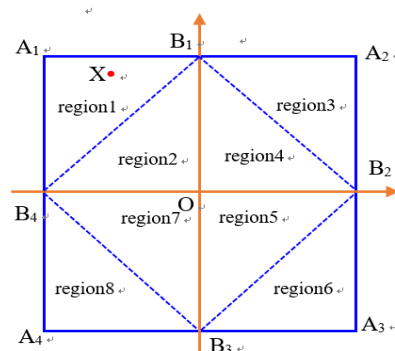


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Figure 3. The flow chart of the iterative positioning algorithm

263 4. The construction of iterative positioning model

264 In the procedure of iterative positioning, whether the target node is in the positioning triangle
 265 area has great influence on its positioning accuracy. The positioning error of the target node located
 266 in the positioning triangle area is much smaller than that of the target node outside the positioning
 267 triangle area. In order to improve the positioning accuracy, an iterative positioning model is
 268 established in the paper, as shown in Figure 4.



269

270

Figure 4. A schematic of the positioning model

271 In Figure 4, the quadrilateral $A_1A_2A_3A_4$ is a square, the point O is its center, the points B_1 , B_2 , B_3
 272 and B_4 are the midpoints of the respective sides. According to the connection shown in Figure 4, the
 273 square $A_1A_2A_3A_4$ is subdivided into eight triangular regions: region 1 to region 8. The anchor nodes
 274 (9 in total) are placed at points A_1 , A_2 , A_3 , A_4 , B_1 , B_2 , B_3 , B_4 and O .

275 There is a target node X in the quadrilateral $A_1B_1OB_4$ in Figure 4, the points closest to the point X
 276 are points A_1 , B_1 , O , B_4 in turn. The node X is included in both $\triangle A_1B_1B_4$ and $\triangle A_1B_1O$. In the $\triangle A_1B_1B_4$,

277 the coordinates (x_{G1}, y_{G1}) is calculated by iterative positioning algorithm. In order to reduce
 278 effectively the positioning error caused by noise, the other coordinate (x_{G2}, y_{G2}) is calculated by
 279 the iterative positioning algorithm in $\triangle A_1B_1O$. The weighted average of these two coordinates can be
 280 taken as the final coordinates (x_{G3}, y_{G3}) . Obviously, the closer the distance between the anchor
 281 node and the target node is, the more reliable the calculation result is. Hence the weight of the
 282 former coordinate should be greater than the weight of the latter coordinate.

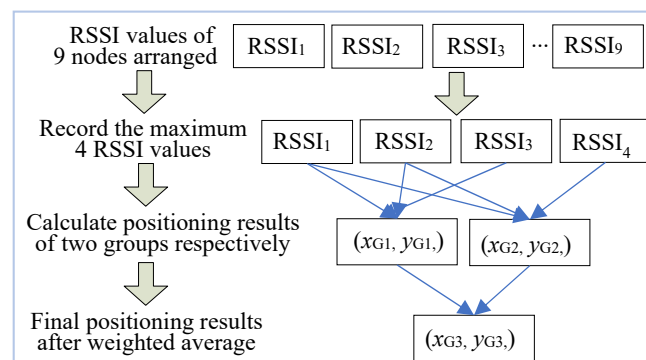
283 The various proportion of weight value are compared by the simulation experiment, the results
 284 show that when the weight of the former coordinate is 0.75 and the weight of the latter coordinate is
 285 0.25, the positioning result better than others.

286 The final positioning results can be expressed as follows in equation (16).

$$\begin{cases} x_{G3} = 0.75x_{G1} + 0.25x_{G2} \\ y_{G3} = 0.75y_{G1} + 0.25y_{G2} \end{cases} \quad (16)$$

287 In actual positioning progress, the RSSI values of the 9 anchor nodes are recorded and arranged
 288 in descending order of their values. The first four larger RSSI values are denoted as $RSSI_1, RSSI_2,$
 289 $RSSI_3$ and $RSSI_4$. The first positioning coordinates (x_{G1}, y_{G1}) is calculated by $RSSI_1, RSSI_2, RSSI_3$ and
 290 their corresponding coordinates. The second positioning coordinates (x_{G2}, y_{G2}) is calculated by $RSSI_1,$
 291 $RSSI_2$ and $RSSI_4$ and their corresponding coordinates. The weighted average of two coordinates
 292 according to the weights mentioned above is the final positioning result (x_{G3}, y_{G3}) .

293 The positioning process of the iterative positioning algorithm is shown in Figure 5:



294

295

Figure 5. The specific implementation process of iterative positioning

296 5. Experiment

297 5.1. The experimental method

298 In order to verify the performance of the algorithm proposed in the paper accurately and
 299 quantitatively, without loss of generality, the positioning experimental area is set as a square of
 300 40m*40m. There are nine anchor nodes in the positioning experimental area, which are located at
 301 the vertices of the square, the middle of each edge and the center of the square. Now, 50 target
 302 nodes are generated in the square area by random, and calculating their positioning results in turn.

303 In the experiment, for different noise impact factors F_N , positioning error is discussed by three
 304 methods of the centroid positioning algorithm, the weighted centroid positioning algorithm and the
 305 iterative positioning algorithm based on distance correction. The value of F_N is taken into account in
 306 two situations: constant value and random value.

307 5.2. Experimental analysis

308 According to the above experimental method, two experiments have been conducted.

309 5.2.1. The first experiment: F_N is constant

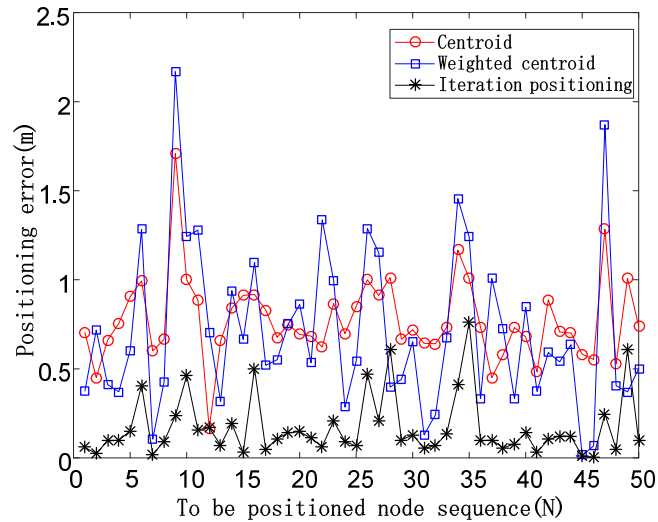
310 When F_N is a constant value, considering the effects of the actual noise on the signal, three

311 typical F_N values are taken for experiments, which are 0.1, 0.2 and 0.3 respectively.

312 The experiments for three parameters are shown as follows:

313 • $F_N=0.1$

314 The positioning error is shown as Figure 6 in the case of the noise impact factor of 0.1.



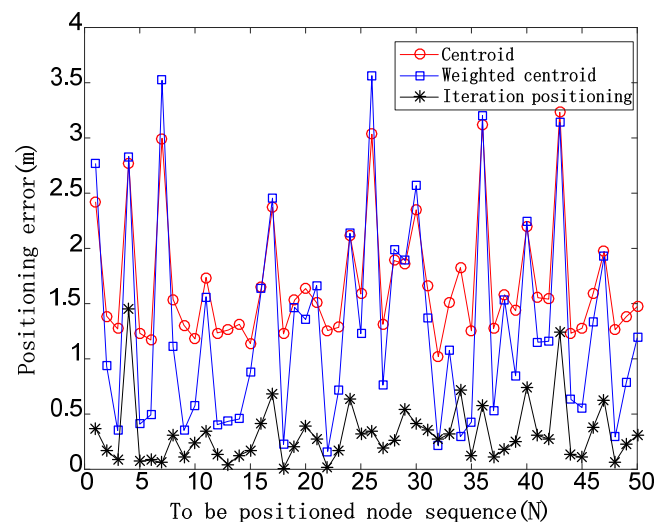
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316 **Figure 6.** The positioning error of the three positioning algorithms in the case of the noise impact
317 factor of 0.1

318 The x -coordinate represents the target node sequence, the unit is the number of nodes. The
319 y -coordinate represents the positioning error, the unit is meter.

320 • $F_N=0.2$

321 The positioning error is shown as Figure 7 in the case of the noise impact factor of 0.2.

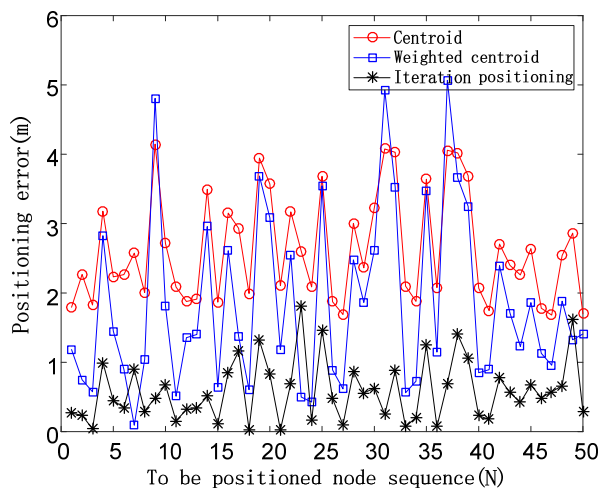


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323 **Figure 7.** The positioning error of the three positioning algorithms in the case of the noise impact
324 factor of 0.2

325 • $F_N=0.3$

326 The positioning error is shown as Figure 8 in the case of noise impact factor of 0.3.



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Figure 8. The positioning error of the three positioning algorithms in the case of noise impact factor of 0.3

330

5.2.2. The second experiment: F_N is a random value

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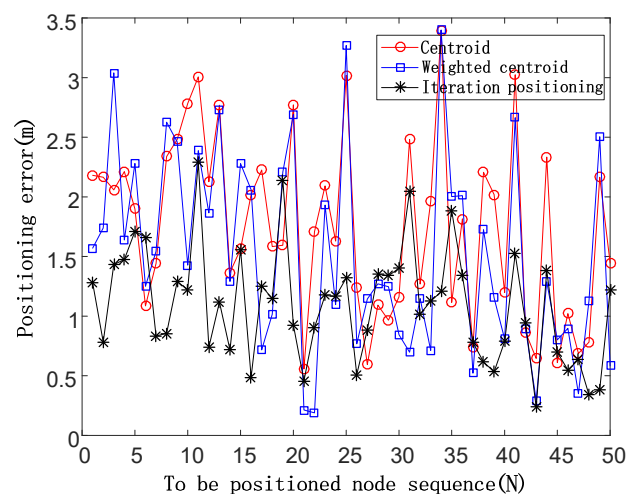
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When F_N is a random value, considering the effect of the actual noise on the signal, the random value is 0.3 times of random function.

333

334

The positioning error is shown as Figure 9 in the case of the noise impact factor of random value.



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336

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Figure 9. The positioning error of the three positioning algorithms in the case of the noise impact factor of random value

338

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In the case of different noise impact factors, the positioning errors of the three positioning algorithms are shown in Table 1.

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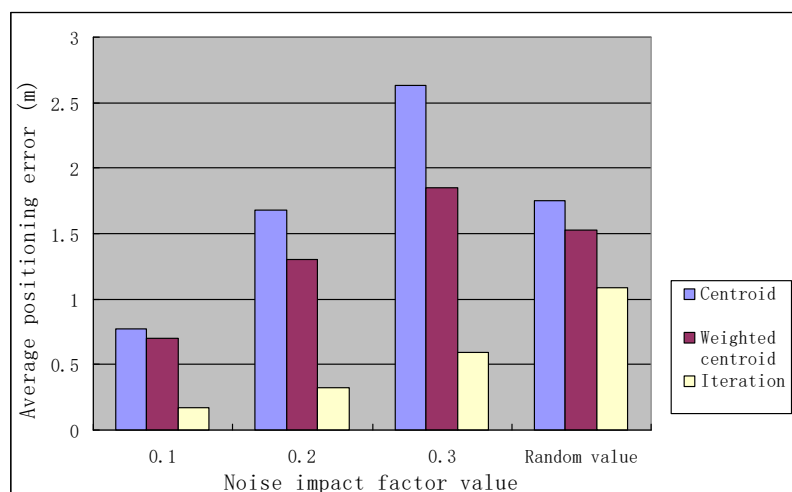
Table 1. The positioning error of the three positioning algorithms in the case of different noise impact factors

Noise impact factor	Average positioning error (m)		
	Centroid	Weighted centroid	Iterative positioning
$F_N=0.1$	0.77	0.70	0.17
$F_N=0.2$	1.68	1.30	0.32
$F_N=0.3$	2.63	1.85	0.59
$F_N=\text{random}$	1.75	1.53	1.09

342 As can be seen from Table 1, when FN is a random value, the positioning accuracy of the
 343 iterative positioning algorithm is improved by 38% compared with the centroid algorithm, and the
 344 positioning accuracy of the iterative positioning algorithm is improved by 29% by comparing with
 345 the weighted centroid algorithm.

346 The positioning error of the three positioning algorithms for different values of noise impact
 347 factors is shown in Figure 10.

348



349 **Figure 10.** The positioning error of the three positioning algorithms under different noise influence
 350 factors

351 As can be seen from Figure 10, the positioning error of the iterative positioning algorithm is
 352 smaller than that of the centroid positioning algorithm and the weighted centroid positioning
 353 algorithm in the case of different noise impact factors F_N .

354 6. Conclusions

355 With the development of wireless communication technology, the position information of data
 356 is playing an increasingly important role. There are errors in node positioning due to various
 357 interferences in the data transmission process. To solve this problem, a node iterative positioning
 358 algorithm based on distance correction is proposed in this paper to help users obtain accurate
 359 position information. Contributions include the following aspects.

360 (1) The noise impact factor FN has been derived on the basis of the original log-distance
 361 distribution model, which is used to describe the corresponding relationship between the noise
 362 impact factor FN and the measured distance. Proposing of noise impact factor provides a novel
 363 method for analyzing the influence of noise on the distance measurement between nodes in WSN.

364 (2) The median of the distance deviation coefficient has been constructed to characterize the
 365 deviation degree of the whole measured distances, and used to correct the distance from the last
 366 positioning. The triangle centroid localization algorithm has been iteratively conducted based on the
 367 corrected new distance value to improve the node positioning accuracy.

368 The experimental results show that the node iterative positioning algorithm based on distance
 369 correction can effectively reduce the positioning error of unknown target nodes in wireless sensor
 370 networks, and help users obtain more accurate node coordinates. In the future, based on the node
 371 iterative positioning algorithm proposed in the paper, we will do some related researches such as
 372 real-time tracking and path planning of moving nodes in WSN.

373 **Author Contributions:** Conceptualization, J.C., S.W., and M.O.; Methodology, all authors; Software, J.C. M.O.,
 374 and Y.C.; Validation, J.C and Y.X.; Formal Analysis, J.C., S.W., and Y.X.; Investigation, J.C, and M.O.; Resources,
 375 J.C., S.W. and Y.C.; Data curation, S.W.,Y.C. and Y.X.; Writing—Original Draft Preparation, J.C. and M.O.;
 376 Writing—Review & Editing, J.C., S.W., and M.O.; Visualization, J.C. and Y.C.; Supervision, J.C. and M.O.;
 377 Project administration, J.C. and M.O.; Funding acquisition, J.C.

378 **Funding:** This research was funded by Natural Science Fundation of Education Department of Anhui province
379 (KJ2018A0087) and Natural Science Foundation of China (51874010).

380 **Conflicts of Interest:** The authors declare no conflict of interest.

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