

Comparative Study on Constitutive Models for 21-4N Heat Resistant Steel During High Temperature Deformation

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Abstract: The Gleeble-1500D thermal simulation test machine was used to conduct the isothermal compression test on 21-4N at the strain rate ($\dot{\epsilon}$) of 0.01-10s⁻¹, the deformation temperature (T) of 1273-1453K and the maximum deformation is 0.916. The data of the stress-strain ($\sigma - \epsilon$) were obtained. Based on the $\sigma - \epsilon$ data, the Johnson-Cook (J-C), modified J-C, Arrhenius and Back-

Propagation Artificial Neural Network (BP-ANN) models were established. The accuracy of four models were verified, analyzed and compared. The results show that J-C model has a higher accuracy only under reference deformation conditions. When the deformation condition changes greatly, the accuracy of J-C model is significantly reduced. The coupling effect of T and $\dot{\epsilon}$ of modified J-C model is considered, and the prediction accuracy is greatly improved. The Arrhenius model introduces Zener-Hollomon (Z) to represent the coupling effect of T and $\dot{\epsilon}$, it has a fairly high prediction accuracy. And it can predict flow stress (σ) accurately at different conditions. The accuracy of BP-ANN model is the highest, but its learning rate is low, the learning and memory are unstable. It has no memory for the weights and thresholds of the completed training. So, there are certain limitations of it in use. Finally, a FEM of the isothermal compression experiment for four models were established, and the distribution of the equivalent stress field, equivalent strain field and temperature field with the deformation degree of 60% were obtained.

Keywords: 21-4N; High temperature deformation; Constitutive models; Numerical simulation

1. Introduction

21-4N is an austenitic heat-resistant steel with good mechanical properties at high temperature and strong chemical stability. It can be used in various extreme environments and widely used in the manufacture of various valves [1-2]. Its hot deformation behavior is an extremely complex dynamic process accompanied by changes in microstructure, including work hardening, grain growth, dynamic recrystallization and so on [3-5]. The flow stress is one of the important indexes for evaluating the deformation ability of metals. The constitutive model is the key to the relationship between reaction the rheological behavior and parameters of metals and alloys. It is an important

prerequisite to establish high-precision constitutive model for simulating the deformation process of metals and alloys by finite element method, and also an important means to optimize production process and achieve high-efficiency and high-quality production [6-8].

In the past few decades, many scholars at home and abroad have done a lot of studies on the constitutive models of different materials. The J-C model is the first used to predict the σ of metals due to its simple form, small amount of calculation and significant reduction in the number of experiments [9-10]. Sahu et al [11] established the J-C model of AA1100 aluminum alloy and simulated and analyzed it by finite element software, the results show that the prediction results have a better accuracy. Limbadri et al [12-13] predicted the effect of deformation conditions on the stress by using J-C model. Buzyurkin et al [14] calculated the parameters of J-C model of VT6, OT4 and OT4-0 titanium alloys, and established J-C model to calculate stress. Jia et al [15] predicted the $\sigma - \varepsilon$ curves of 7A52 aluminum alloy by using J-C model, which proves that the model can meet the accuracy requirements only under the reference deformation conditions. Wang et al [16] predicted the rheological behavior of Ti-6Al-4V by J-C model. The finite element simulation was used to verify the accuracy. However, J-C model has limitations because it ignores the mutual coupling between T and $\dot{\varepsilon}$, so that it has better accuracy only under reference deformation conditions. In this regard, some scholars have improved J-C model. Zhao et al [17] established J-C model and modified J-C model of FeCr alloy, and compared the accuracy of them. Zhang et al [18] predicted the hot rheological behavior of 7075-T6 aluminum alloy by using modified J-C model, and a higher prediction accuracy was obtained. Tan et al [19] observed the mechanical behavior of 7050-T7451 aluminum alloy by using J-C model and modified J-C model. The stress of 7050-T7451 aluminum alloy was predicted by two models. The prediction results show that the accuracy of modified J-C

model has been significantly improved. Wang et al ^[20] studied the dynamic behavior of Inconel718, established modified J-C model with $\sigma - \varepsilon$ data, and verified the prediction accuracy. He et al ^[21] integrated the coupling effect between T and $\dot{\varepsilon}$, established modified J-C model of 10%Cr steel, and proved that modified J-C model has a better predictive ability. Although modified J-C model has been improved significantly in accuracy compared to J-C model, it is also limited by deformation conditions. Its prediction accuracy will gradually decrease as the difference that between deformation condition and reference condition increases. The Arrhenius model compensates for this defect by introducing the Z parameter. No matter how the deformation condition changes, its prediction accuracy can achieve the desired effect. Chen et al ^[22] studied the hot mechanical behavior of Al-12Zn-2.4Mg-1.2Cu alloy, established Arrhenius model by using the $\sigma - \varepsilon$ data. And used the average relative error (AARE) and correlation coefficient (R) to evaluate the accuracy, which proves that Arrhenius model has an accurate predictive ability. Abbasi-Bani et al ^[23] studied the high temperature deformation behavior of Mg-6Al-1Zn, and established J-C model and Arrhenius model. Li et al ^[24] established Arrhenius model of V-5Cr-5Ti alloy by regression analysis, and used it to calculate and analyze the stress. And a better prediction result was obtained. Quan et al ^[25-26] studied the hot mechanical behavior of 42CrMo and Ti-6Al-2Zr-1Mo-1V, and established Arrhenius models of two materials to describe hot rheological behavior, obtained accurate prediction results. Samantaray et al ^[27] used J-C model and Arrhenius model with strain compensation to characterize the high temperature mechanical properties of 9Cr-1Mo alloy. The results show that J-C model has limitations and cannot well describe the high temperature mechanical behavior of 9Cr-1Mo alloy. The Arrhenius model can accurately predict the stress. Li et al ^[28] established Z-A model and Arrhenius model of 7050 aluminum, and the accuracy of the two

models were compared by AARE and R. Yan et al ^[29] predicted the residual stress distribution of Ti-6Al-4V by using Arrhenius model, and obtained accurate predicted results. Li et al ^[30] established Z-A model, J-C model, and Arrhenius model of 28CrMnMoV alloy. The results show that the Arrhenius model can show high prediction accuracy under the whole deformation condition. Compared with Arrhenius model, the accuracy of BP-ANN model is higher. It is one of the widely used ANN models. Yan et al ^[31] studied the hot deformation behavior of Al-6.2Zn-0.70Mg-0.30Mn-0.17Zr alloy at 623-773K and 0.01-20s⁻¹, established its Arrhenius model and BP-ANN model. and compared the accuracy of two models. Han et al ^[32] studied the constitutive relation of as-cast 904L, compensated the $\sigma - \varepsilon$ data with friction factor and temperature, established Arrhenius model and BP-ANN model of it, and compared the accuracy of models. Peng et al ^[33] calculated AARE and R of Arrhenius model and BP-ANN model of the as-cast Ti60, compared the accuracy of two models. Vignesh et al ^[34] established BP-ANN model of AA1100 aluminum alloy and obtained 99% prediction accuracy. At present, there are few studies on the constitutive relation of 21-4N. As the preferred material for engine valves, it is necessary to conduct a comprehensive study on the constitutive relation.

In this paper, based on the hot deformation behavior of 21-4N, the parameters of four models were calculated by using $\sigma - \varepsilon$ data. The J-C, modified J-C, Arrhenius and BP-ANN model of 21-4N were established respectively, and the accuracy of four models were verified. And then, the distribution of the equivalent stress field, equivalent strain field and temperature field with the deformation degree of 60% is obtained by using four models for finite element simulation. The results can provide theoretical basis to predict the rheological behavior of 21-4N.

2. Experiment

In this study, 21-4N was selected as the material, the composition of which is as follows: Cr: 20-22%, Mn: 8-10%, Ni: 3.25-4.5%, Si: $\leq 0.35\%$, C: 0.48-0.58%, N: 0.35-0.5%, P: $\leq 0.04\%$, S: $\leq 0.03\%$, Bal: Fe. The size of the sample is $\phi 8\text{mm} \times 15\text{mm}$. T were set at 1273, 1333, 1393, 1453K, $\dot{\varepsilon}$ were set at 0.01, 0.1, 1, 10s^{-1} , the maximum deformation was 0.916. Fig.1 shows the heating process of the test. The sample was heated to 1453K at 10K/s and holding for 3min. Finally, the sample was compressed at high temperature with different ε and $\dot{\varepsilon}$. After test, water quenching immediately [35-36].

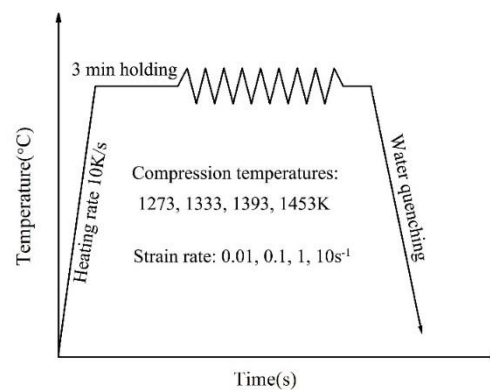


Fig.1 Process flow diagram of the heating process.

3. Result and discussion

3.1 J-C Model

In the 1980s, J-C model was proposed by Johnson and Cook to describe the σ - ε relationship of metals and alloys under high T, high $\dot{\varepsilon}$ and large ε [37-39]. When applied, J-C model assumes materials stress conforms to yield criterion and isotropic strain hardening criterion, and its expression is shown as Eq. (1):

$$\left\{ \begin{array}{l} \sigma = (A + B\varepsilon^n) \left(1 + C \ln \dot{\varepsilon}^* \right) \left(1 - T^{*m} \right) \\ \dot{\varepsilon}^* = \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \\ T^* = \frac{T - T_r}{T_m - T_r} \end{array} \right. \quad (1)$$

In the equation: A - The yield stress, MPa; n - Strain hardening index; C - Strain rate sensitivity coefficient; $\dot{\varepsilon}^*$ - Dimensionless plastic strain rate; T^* - Dimensionless temperature; m - Temperature sensitivity coefficient; $\dot{\varepsilon}_0$ - Reference strain rate, s⁻¹; T_r - Reference temperature, K; B - Strain hardening parameter, MPa; T_m - Melting temperature, K. Therefore, J-C model can be converted as:

$$\sigma = (A + B\varepsilon^n) \left[1 + C \ln \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \right] \left[1 - \left(\frac{T - T_r}{T_m - T_r} \right)^m \right] \quad (2)$$

From Eq. (2), the J-C model contents three parts ^[40-42]: strain hardening effect part - $(A + B\varepsilon^n)$, strain rate enhancement effect part - $\left[1 + C \ln \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \right]$ and temperature effect part - $\left[1 - \left(\frac{T - T_r}{T_m - T_r} \right)^m \right]$; a total of five material parameters: A, B, n, C and m.

The J-C model of 21-4N with ε of 0.1, 0.15, 0.2, 0.25, 0.3, 0.35, 0.4, 0.45, 0.5, T of 1273, 1333, 1393, 1453K and $\dot{\varepsilon}$ of 0.01, 0.1, 1, 10s⁻¹ was studied. The T_r was 1273K, and the $\dot{\varepsilon}_0$ was 0.01s⁻¹. Under this condition, the yield stress of 21-4N is 107MPa (A=107 MPa). The melting temperature of 21-4N is 1727K ($T_m=1727K$).

3.1.1 Determination of parameters n and B

When $T=T_r=1273K$ and $\dot{\varepsilon} = \dot{\varepsilon}_0=0.01s^{-1}$, the $\left[1 + C \ln \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \right]$ and $\left[1 - \left(\frac{T - T_r}{T_m - T_r} \right)^m \right]$ in Eq.

(2) are 1. Therefore, the Eq. (2) can be written as:

$$\sigma = A + B\varepsilon^n \quad (3)$$

Converting and taking the logarithm of Eq. (3), and Eq. (4) can be obtained:

$$\ln(\sigma - A) = \ln B + n \ln \varepsilon \quad (4)$$

From Eq. (4), $\ln(\sigma - A)$ is linear with $\ln \varepsilon$. Fig.2 shows the linear relationship of $\ln(\sigma - A)$ and $\ln \varepsilon$ under different ε . The slope is n , and the intercept is $\ln B$. By calculation, n and B were obtained: $n = -0.3642$, $B = 37.3238 \text{ MPa}$.

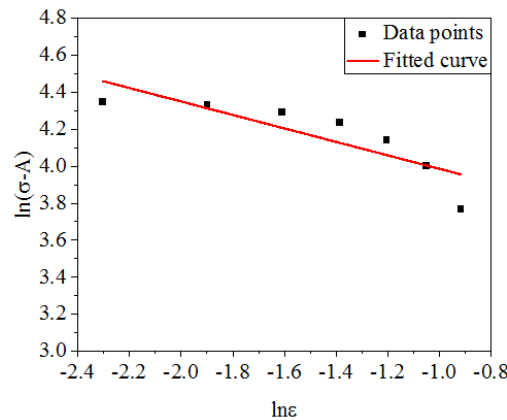


Fig.2 The linear relationship between $\ln(\sigma - A)$ and $\ln \varepsilon$.

Taking A , n and B into Eq. (3):

$$\sigma = 107 + 37.3238\varepsilon^{-0.3642} \quad (4)$$

3.1.2 Determination of parameter C

When $T = T_r = 1273 \text{ K}$, the $\left[1 - \left(\frac{T - T_r}{T_m - T_r}\right)^m\right]$ is 1. That is, the effect of the temperature effect

part on the σ is neglected. Therefore, the Eq. (2) can be converted as Eq. (6):

$$\sigma = (A + B\varepsilon^n) \left[1 + C \ln \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \right] \quad (6)$$

Converting the Eq. (6):

$$\frac{\sigma}{A+B\varepsilon^n} = 1 + C \ln\left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}\right) \quad (7)$$

From Eq. (7), $\frac{\sigma}{(A+B\varepsilon^n)}$ is linear with $\ln\left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}\right)$, the slope is C and the intercept is 1. Fig.3

shows the linear relationship of $\frac{\sigma}{(A+B\varepsilon^n)}$ and $\ln\left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}\right)$ under different ε and $\dot{\varepsilon}$. By

calculation, C was obtained: C=0.1449.

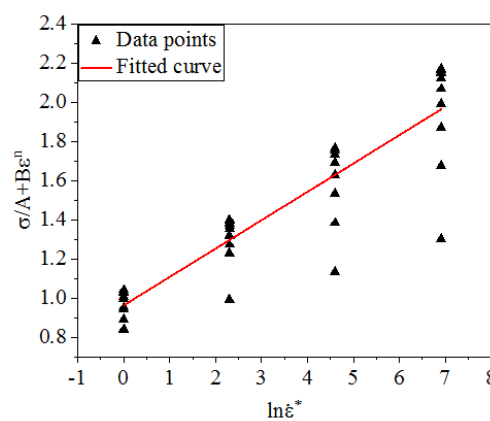


Fig.3 The linear relationship between $\frac{\sigma}{(A+B\varepsilon^n)}$ and $\ln\left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}\right)$.

3.1.3 Determination of parameter m

When $\dot{\varepsilon} = \dot{\varepsilon}_0 = 0.01 \text{ s}^{-1}$, the Eq. (2) can be converted as Eq. (8):

$$\sigma = (A+B\varepsilon^n) \left[1 - \left(\frac{T-T_r}{T_m-T_r} \right)^m \right] \quad (8)$$

Converting the Eq. (8):

$$\ln\left(1 - \frac{\sigma}{A+B\varepsilon^n}\right) = m \ln\left(\frac{T-T_r}{T_m-T_r}\right) \quad (9)$$

From Eq. (9), $\ln\left(1 - \frac{\sigma}{A+B\varepsilon^n}\right)$ is linear with $\ln\left(\frac{T-T_r}{T_m-T_r}\right)$, the slope is m. Fig.4 shows

the linear relationship of $\ln\left(1 - \frac{\sigma}{A + B\dot{\varepsilon}^n}\right)$ and $\ln\left(\frac{T - T_r}{T_m - T_r}\right)$ under different $\dot{\varepsilon}$ and T. By

calculation, m was obtained: m=0.4223.

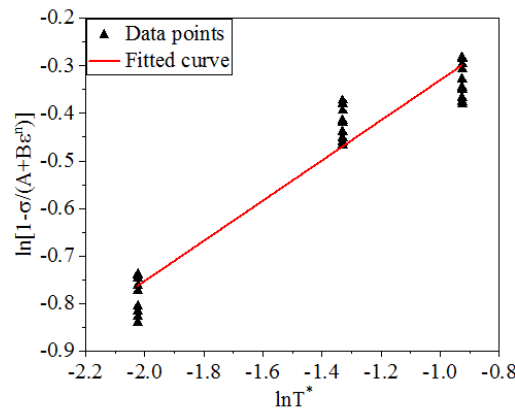


Fig.4 The linear relationship between $\ln\left(1 - \frac{\sigma}{A + B\dot{\varepsilon}^n}\right)$ and $\ln\left(\frac{T - T_r}{T_m - T_r}\right)$.

The J-C model of 21-4N is obtained by substituting the above calculated parameters into Eq.

(2):

$$\sigma = \left(107 + 37.3238\dot{\varepsilon}^{-0.3642}\right) \left(1 + 0.1449 \ln \frac{\dot{\varepsilon}}{0.01}\right) \left[1 - \left(\frac{T - 1273}{454}\right)^{0.4223}\right] \quad (10)$$

3.2 Modified J-C model

Obviously, J-C model ignores the influence of $\dot{\varepsilon}$, $\dot{\varepsilon}$, T. And it does not consider other factors.

However, it is found that J-C model has a higher accuracy only under the reference deformation condition by comparing the stresses which were obtained by the Eq. (10) with the experimental stresses (Fig. 11). When the deformation condition is more and more different from the reference deformation condition, the prediction accuracy will be lower and lower. For the purpose of improving the accuracy of J-C model, Lin, Mirza, Li, Hou et al [43-48] studied and modified J-C

model. By comparison, it is found that the values of σ were obtained by the one-dimensional quadratic or cubic equation are closer to the experimental values than the values obtained by the power function. Therefore, the strain hardening effect part of J-C model was replaced, and other two parts were also adjusted accordingly, as shown in Eq. (11):

$$\sigma = (A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*) \exp[(\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*)(T - T_r)] \quad (11)$$

In the equation: $A_1, B_1, B_2, B_3, C_1, \lambda_1, \lambda_2$ are all parameters related to the material, and other physical quantities have the same meaning as in J-C model.

Similar to the solution process for solving the J-C model, the T_r is 1273K, the $\dot{\varepsilon}_0$ is $0.01s^{-1}$, and the T_m is 1727K.

3.2.1 Determination of parameters A_1, B_1, B_2, B_3

When $T=T_r=1273K$ and $\dot{\varepsilon} = \dot{\varepsilon}_0=0.01s^{-1}$, the Eq. (11) can be converted as Eq. (12):

$$\sigma = A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3 \quad (12)$$

The σ under the condition of ε range of 0.05-0.8 are taken as the research object, and the coefficients in Eq. (12) are solved. Fig.5 shows the $\sigma - \varepsilon$ data in the ε range of 0.05-0.8 and the curve fitted by Eq. (12). The values of A_1, B_1, B_2 and B_3 in Eq. (12) can be obtained by calculation (As shown in Table 1).

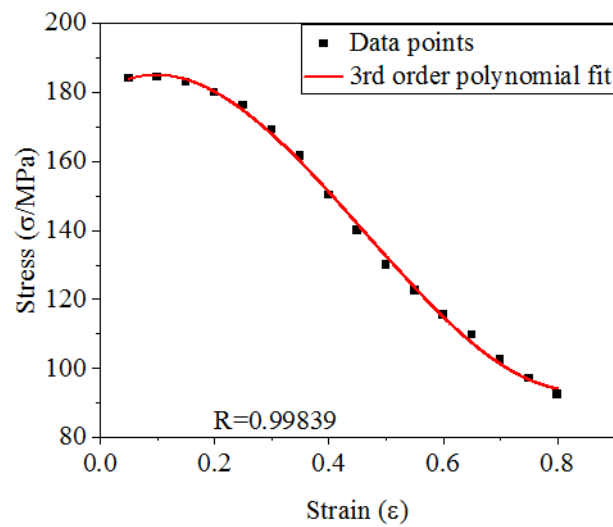


Fig.5 The σ - ε relationship with ε range of 0.05-0.8.

Table.1 The values of A_1 , B_1 , and B_2 in Eq. (12).

| A_1 | B_1 | B_2 | B_3 |
|------------|------------|-------------|------------|
| 179.67 MPa | 113.27 MPa | -647.79 MPa | 465.55 MPa |

3.2.2 Determination of parameter C_1

When $T=T_r=1273K$, the Eq. (11) can be written as:

$$\sigma = (A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*) \quad (13)$$

Converting the Eq. (13):

$$\frac{\sigma}{A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3} = 1 + C_1 \ln \dot{\varepsilon}^* \quad (14)$$

From Eq. (14), $\frac{\sigma}{A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3}$ is linear with $\ln \dot{\varepsilon}^*$, the slope is C_1 . Fig.6 shows

the linear relationship of $\frac{\sigma}{A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3}$ and $\ln \dot{\varepsilon}^*$ under different ε and $\dot{\varepsilon}$. By

calculation, C_1 was obtained: $C_1=0.2002$.

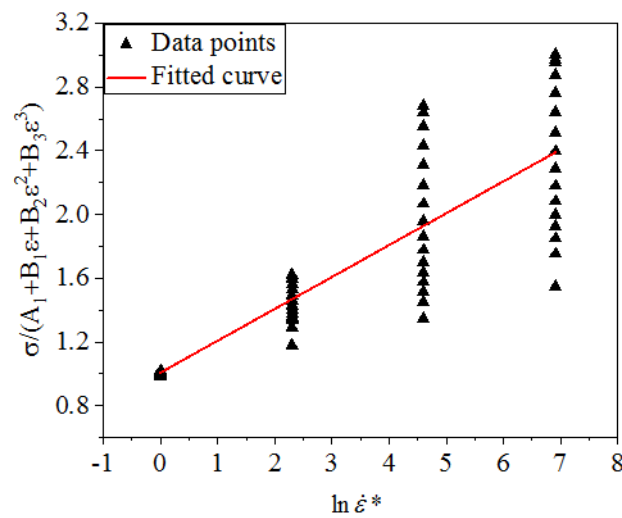


Fig.6 The linear relationship between $\frac{\sigma}{A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3}$ and $\ln \dot{\varepsilon}^*$.

3.2.3 Determination of parameters λ_1 , λ_2

Converting the Eq. (11):

$$\frac{\sigma}{(A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*)} = \exp\left[(\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*)(T - T_r)\right] \quad (15)$$

Taking the logarithm:

$$\ln \frac{\sigma}{(A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*)} = (\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*)(T - T_r) \quad (16)$$

Fig.7 shows the linear relationship of $\ln \frac{\sigma}{(A_1 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*)}$ and

$T - T_r$ under different $\dot{\varepsilon}$. By calculation, $\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*$ were obtained in different $\dot{\varepsilon}$ (As shown in Table.2).

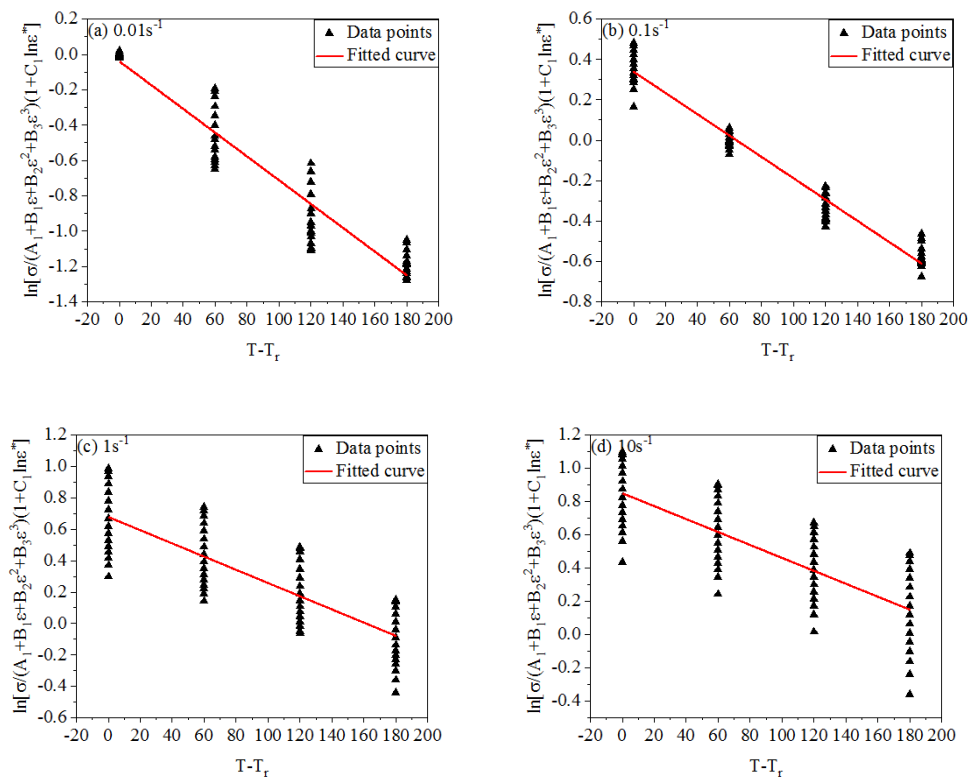


Fig.7 The linear relationship between $\ln \frac{\sigma}{(A_1 + B_1 \varepsilon + B_2 \varepsilon^2 + B_3 \varepsilon^3)(1 + C_1 \ln \dot{\varepsilon}^*)}$ and $T - T_r$ under different $\dot{\varepsilon}$.

Table.2 The values of $\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*$ under different $\dot{\varepsilon}$.

| $\lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*$ | $\dot{\varepsilon}$ | | | |
|---|---------------------|----------|----------|----------|
| | 0.01 | 0.1 | 1 | 10 |
| | -0.00673 | -0.00528 | -0.00420 | -0.00389 |

Let $\lambda = \lambda_1 + \lambda_2 \ln \dot{\varepsilon}^*$, then λ is linear with $\ln \dot{\varepsilon}^*$. Where λ_1 is intercept and λ_2 is slope. Fig.8 shows the linear relationship of λ and $\ln \dot{\varepsilon}^*$, the values of λ_1 and λ_2 can be obtained by calculation: $\lambda_1 = -0.00647$, $\lambda_2 = 0.00042$.

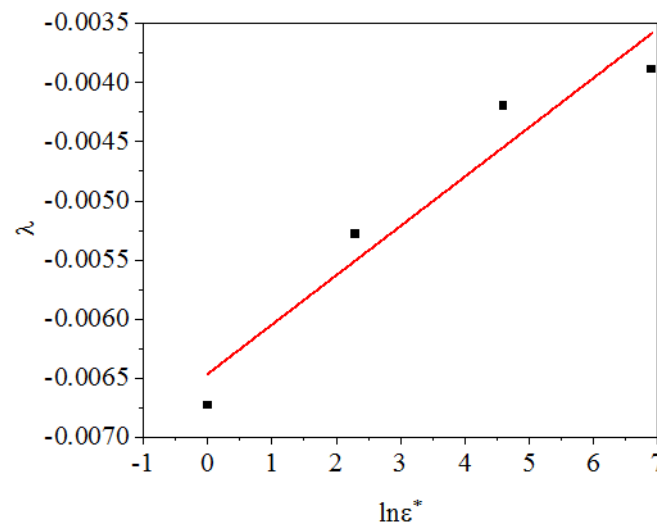


Fig.8 The linear relationship between λ and $\ln \dot{\epsilon}^*$.

Taking $A_1, B_1, B_2, C_1, \lambda_1, \lambda_2$ obtained from above calculation into Eq. (11) to obtain the modified J-C model of 21-4N:

$$\sigma = (179.67 + 113.27\epsilon - 647.79\epsilon^2 + 465.55\epsilon^3) \left(1 + 0.2002 \ln \dot{\epsilon}^*\right) \exp \left[(-0.00647 + 0.00042 \ln \dot{\epsilon}^*) (T - T_r) \right] \quad (17)$$

3.3 Arrhenius model

There is a relationship between σ and T , $\dot{\epsilon}$, ϵ in hot deformation of metals and alloys. It can be expressed by Arrhenius model which proposed by Sellers and Tegart [49-52]:

$$\dot{\epsilon} = f(\sigma) \exp(-Q/RT) \quad (18)$$

Among them:

$$f(\sigma) = \begin{cases} A\sigma^m & (\alpha\sigma < 0.8) \\ B \exp(\beta\sigma) & (\alpha\sigma > 1.2) \\ C [\sinh(\alpha\sigma)]^n & (\text{For all } \sigma) \end{cases} \quad (19)$$

α, β, m meets the following relationship:

$$\alpha = \beta / m \quad (20)$$

In the equation: $\dot{\varepsilon}$ - Strain rate, s^{-1} ; T - Absolute temperature, K ; R - Gas parameter, $8.3145 J / (mol \cdot K)$; Q - Deformation activation energy, kJ / mol ; A, B, C - Material parameter; m, n - Stress index; α, β - Stress level parameter.

There is a certain functional relationship between $\dot{\varepsilon}$, Q and T during hot deformation. Z parameters can be introduced to express this relationship [53-56]:

$$Z = \dot{\varepsilon} \exp(-Q / RT) \quad (21)$$

Taking the flow stress function under full pressure in Eq. (19) into Eq. (18):

$$\dot{\varepsilon} = C [\sinh(\alpha\sigma)]^n \exp(-Q / RT) \quad (22)$$

Combining Eq. (21) with Eq. (22), the Arrhenius constitutive equation can be described with Z parameters. As shown in Eq. (23):

$$\sigma = \frac{1}{\alpha} \ln \left\{ \left(\frac{Z}{C} \right)^{1/n} + \left[\left(\frac{Z}{C} \right)^{2/n} + 1 \right]^{1/2} \right\} \quad (23)$$

The three expressions in Eq. (19) were respectively taken into Eq. (18), then taking the logarithm of the equations. The linear relationships between $\ln \dot{\varepsilon}$ and $\ln \sigma$, σ , and $\ln [\sinh(\alpha\sigma)]$, $\ln [\sinh(\alpha\sigma)]$ and $1/T$, $\ln Z$ and $\ln [\sinh(\alpha\sigma)]$ were obtained. The values of m , β , n , n_1 and $\ln C$ were obtained. The values of α and Q can be obtained by calculation. The results were shown in Table.3.

Table.3 Parameter values of 21-4N under different strains.

| Parameter | ε | | | | | | | |
|-----------|---------------|----------|----------|----------|----------|----------|----------|----------|
| | 0.05 | 0.1 | 0.15 | 0.2 | 0.25 | 0.3 | 0.35 | 0.4 |
| m | 9.571 | 8.144 | 7.505 | 7.059 | 6.670 | 6.288 | 6.137 | 5.852 |
| β | 0.0665 | 0.0545 | 0.0495 | 0.0465 | 0.0441 | 0.0425 | 0.0417 | 0.0415 |
| α | 0.00694 | 0.00669 | 0.00660 | 0.00659 | 0.00660 | 0.00676 | 0.00679 | 0.00708 |
| n | 6.819 | 5.797 | 5.356 | 5.025 | 4.752 | 4.475 | 4.355 | 4.188 |
| n_1 | 12547.3 | 12957.7 | 12549.5 | 12985.7 | 13055.1 | 13255.2 | 13463.4 | 12806.4 |
| Q | 711389. | 624550.2 | 558860.1 | 542547.2 | 515813.5 | 493191.3 | 487504.9 | 445933.2 |

| | 08 | 1 | 2 | 5 | 8 | 6 | 7 | 7 |
|----------------|---------------|----------|----------|----------|----------|----------|----------|----------|
| lnC | 59.087 | 52.144 | 46.428 | 45.129 | 42.896 | 40.948 | 40.548 | 36.900 |
| Parameter | ε | | | | | | | |
| | 0.45 | 0.5 | 0.55 | 0.6 | 0.65 | 0.7 | 0.75 | 0.8 |
| m | 5.577 | 5.404 | 5.321 | 5.238 | 5.187 | 5.112 | 5.068 | 5.046 |
| β | 0.0405 | 0.0404 | 0.0406 | 0.0409 | 0.0414 | 0.0418 | 0.0423 | 0.0432 |
| α | 0.00726 | 0.00748 | 0.00763 | 0.00780 | 0.00798 | 0.00818 | 0.00835 | 0.00856 |
| n | 3.988 | 3.876 | 3.822 | 3.775 | 3.744 | 3.697 | 3.677 | 3.682 |
| n ₁ | 13504.1 | 13429.8 | 13384.9 | 13221.8 | 13063.5 | 12831.4 | 12541.5 | 12421.2 |
| Q | 447772. | 432802.1 | 425345.6 | 414995.7 | 406660.0 | 394420.6 | 383423.9 | 380262.4 |
| | 0 | 9 | 1 | 8 | 7 | 4 | 6 | 8 |
| lnC | 37.188 | 35.935 | 35.350 | 34.497 | 33.799 | 32.752 | 31.831 | 31.691 |

Fig.9 shows the relationships between m , β , α , n , Q , $\ln C$ and ε .

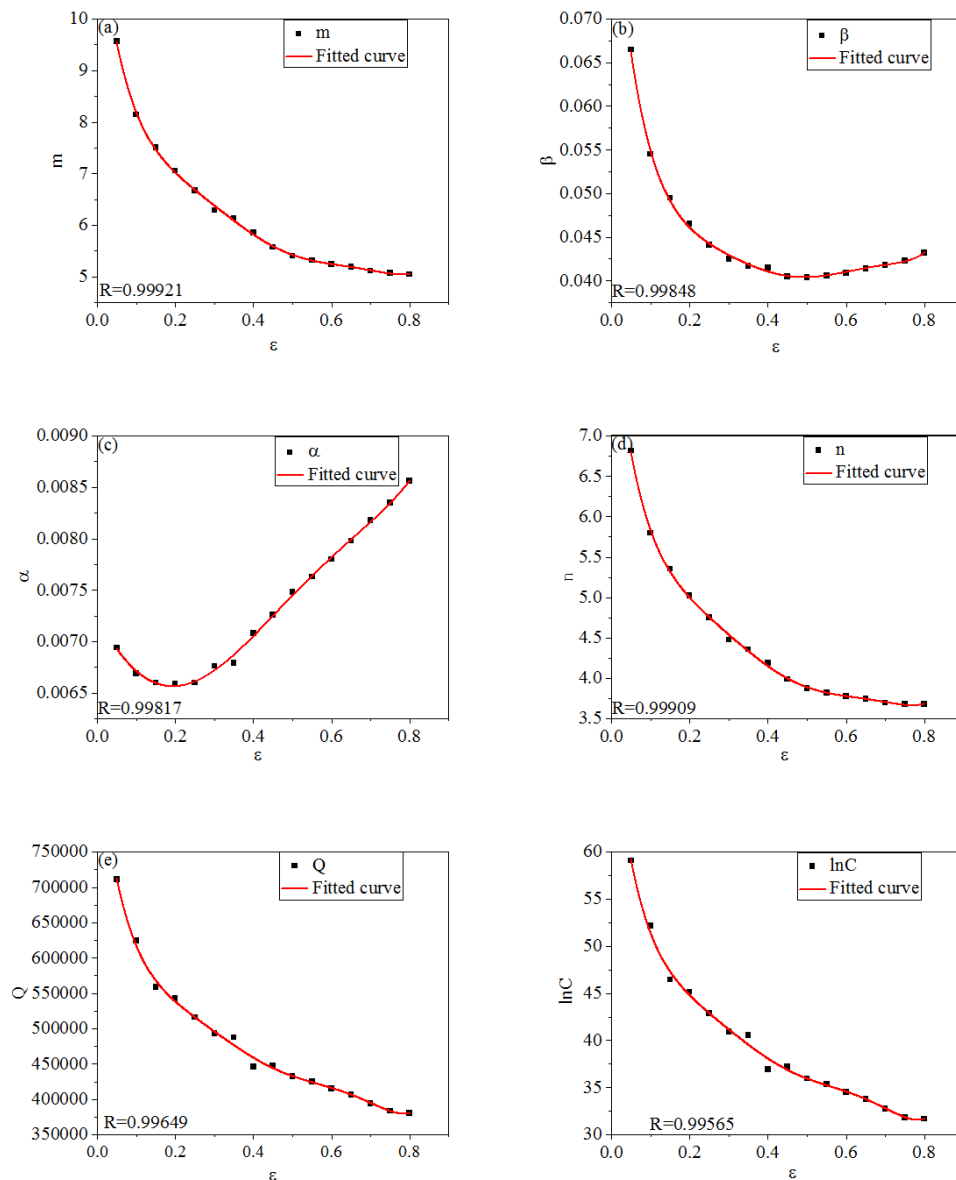


Fig.9 The relationships between m , β , α , n , Q , $\ln C$ and ε .

The curves in the figure were respectively fitted by the sixth-order polynomial form shown by the Eq. (24), and the fitting results were shown in Table. 4^[57-58]. Taking the data in Table. 4 into Eq. (24) to obtain function relationships between m , β , α , n , Q , $\ln C$ and ε . The values of m , β , α , n , Q , and $\ln C$ under different strains can be calculated by the Eq. (24), and the σ under different strains can be obtained correspondingly.

$$\left\{ \begin{array}{l} m = A_{00} + A_{11}\varepsilon + A_{22}\varepsilon^2 + A_{33}\varepsilon^3 + A_{44}\varepsilon^4 + A_{55}\varepsilon^5 + A_{66}\varepsilon^6 \\ \beta = B_{00} + B_{11}\varepsilon + B_{22}\varepsilon^2 + B_{33}\varepsilon^3 + B_{44}\varepsilon^4 + B_{55}\varepsilon^5 + B_{66}\varepsilon^6 \\ \alpha = C_{00} + C_{11}\varepsilon + C_{22}\varepsilon^2 + C_{33}\varepsilon^3 + C_{44}\varepsilon^4 + C_{55}\varepsilon^5 + C_{66}\varepsilon^6 \\ n = D_{00} + D_{11}\varepsilon + D_{22}\varepsilon^2 + D_{33}\varepsilon^3 + D_{44}\varepsilon^4 + D_{55}\varepsilon^5 + D_{66}\varepsilon^6 \\ Q = E_{00} + E_{11}\varepsilon + E_{22}\varepsilon^2 + E_{33}\varepsilon^3 + E_{44}\varepsilon^4 + E_{55}\varepsilon^5 + E_{66}\varepsilon^6 \\ \ln C = F_{00} + F_{11}\varepsilon + F_{22}\varepsilon^2 + F_{33}\varepsilon^3 + F_{44}\varepsilon^4 + F_{55}\varepsilon^5 + F_{66}\varepsilon^6 \end{array} \right. \quad (24)$$

Table. 4 The values of parameter in Eq. (24).

| m | β | α | n | Q | $\ln C$ |
|-------------------|------------------|-------------------|-------------------|------------------|--------------------|
| $A_{00}=12.05$ | $B_{00}=0.087$ | $C_{00}=0.00725$ | $D_{00}=8.57$ | $E_{00}=8.92E5$ | $F_{00}=73.81$ |
| $A_{11}=-65.87$ | $B_{11}=-0.550$ | $C_{11}=-0.00737$ | $D_{11}=-46.54$ | $E_{11}=-4.78E6$ | $F_{11}=-388.15$ |
| $A_{22}=377.37$ | $B_{22}=3.092$ | $C_{22}=0.01941$ | $D_{22}=266.35$ | $E_{22}=2.84E7$ | $F_{22}=2291.91$ |
| $A_{33}=-1227.28$ | $B_{33}=-9.605$ | $C_{33}=0.01259$ | $D_{33}=-870.35$ | $E_{33}=-9.51E7$ | $F_{33}=-7712.90$ |
| $A_{44}=2143.97$ | $B_{44}=16.401$ | $C_{44}=-0.06592$ | $D_{44}=1533.55$ | $E_{44}=1.72E8$ | $F_{44}=14044.30$ |
| $A_{55}=-1882.28$ | $B_{55}=-14.312$ | $C_{55}=0.05639$ | $D_{55}=-1359.92$ | $E_{55}=-1.57E8$ | $F_{55}=-12928.66$ |
| $A_{66}=652.95$ | $B_{66}=4.985$ | $C_{66}=-0.01197$ | $D_{66}=476.78$ | $E_{66}=5.68E7$ | $F_{66}=4707.99$ |

3.4 BP-ANN model

The BP model is an artificial network that is calculated and trained according to error back propagation. Its Schematic diagram is shown in Fig.10. The working process includes the information forward propagation and error back propagation. That is, the information is input from the input layer through the transfer function, propagated in the forward direction, and output by the output layer. When the error between the output information and the expected information exceeds

the normal range, the error signal will be returned in the original way (That is, error back propagation). And the weight of each layer of neurons will be modified through the training network, and thus repeated until the output information error reaches a reasonable range, the training is completed [59-61].

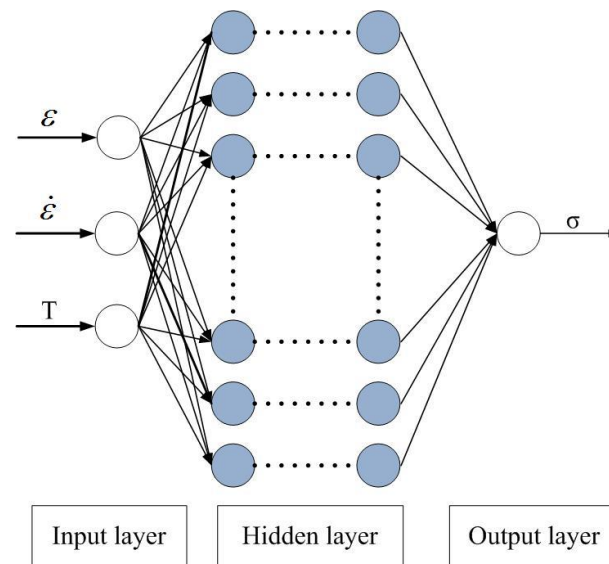


Fig.10 Schematic diagram of artificial neural network model.

When 21-4N undergoes high temperature degeneration, its constitutive relationship can be expressed as:

$$\sigma = \sigma(\varepsilon, \dot{\varepsilon}, T) \quad (25)$$

From Eq. (25), the σ is a function of ε , $\dot{\varepsilon}$ and T . Therefore, there are three input components and one output component in the BP-ANN model.

Since the components of the input layer have large differences in numerical values, for the purpose of data concentration on one or more neurons which causes the low accuracy of the model.

It is necessary to normalize the input data. In general, the Eq. (26) is often used to normalize T and σ [62-63]:

$$Y = \frac{X - 0.95X_{\min}}{1.05X_{\max} - 0.95X_{\min}} \quad (26)$$

In the equation: X - Raw data obtained from the experiment; X_{\min} , X_{\max} - The extreme values of X ; Y - X normalized vector value.

Eq. (27) is often used to normalize the $\dot{\varepsilon}$:

$$\dot{\varepsilon} = \frac{3 + \ln \dot{\varepsilon} - 0.95(3 + \ln \dot{\varepsilon}_{\min})}{1.05(3 + \ln \dot{\varepsilon}_{\max}) - 0.95(3 + \ln \dot{\varepsilon}_{\min})} \quad (27)$$

In this paper, the MATLAB software was used for programming calculation, and the BP-ANN model was trained by using the normalized data. The training function is TRAINLM, the learning function is LEARNGD. The activation function from input layer to hidden layer is TANSIG, and the returned is PURELIN. The $3 \times 10 \times 10 \times 1$ four-layer BP-ANN structure was selected for training, and the error target was set located 10^{-3} . Fig.11 shows the training results. After 47 iterations, the training results reach the error target, the established model converges rapidly and the training is completed.

Best Validation Performance is 0.0025428 at epoch 47

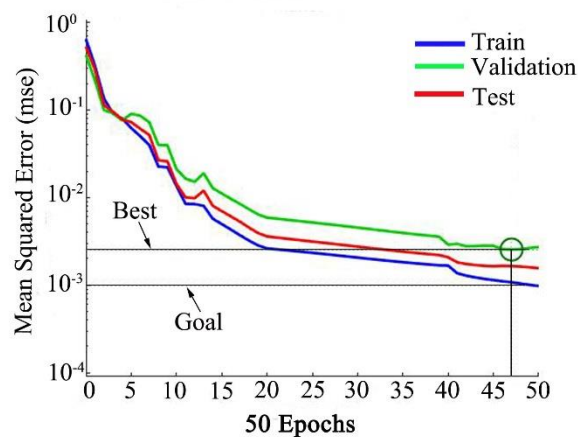


Fig.11 Artificial neural network model training convergence curve.

3.5 Analysis of constitutive equation accuracy

The comparison of stresses between experimental and predicted of four models are shown in

Fig.12-15.

From Fig.12, J-C model has a higher accuracy only at T_r and $\dot{\varepsilon}_0$. The predicted stresses are greatly different from the experimental stresses under other conditions. At low $\dot{\varepsilon}$ and low T, J-C model has a higher accuracy than that at high $\dot{\varepsilon}$ and high T. It indicates that J-C model is suitable for predicting σ at low $\dot{\varepsilon}$ and low T. The T and $\dot{\varepsilon}$ have an effect on the σ and also affect each other. With the increase of T and $\dot{\varepsilon}$, this effect is more obviously.

Modified J-C model improves strain hardening effect part, considers the coupling effect between the T and $\dot{\varepsilon}$. From Fig.13, the accuracy of modified J-C model is significantly higher than that of J-C model, which indicates that the coupling effect between the influencing factors needs to be considered when predicting σ . Modified J-C model is also not suit to predict σ at high $\dot{\varepsilon}$ [64-65].

Arrhenius model introduces the Z parameter in the calculation process. The Z parameter combines the coupling effect of T and $\dot{\varepsilon}$. Fig.14 shows the stresses obtained by Arrhenius model. The predicted stresses are highly consistent with experimental data, indicating that it has high prediction accuracy at the experimental conditions. It shows that the model has a wide range of application [66-67].

Fig.15 shows BP-ANN model of 21-4N. The predicted data are evenly distributed on the σ - ε curves, indicating that the BP-ANN model has a high accuracy under the experimental conditions. Moreover, the BP-ANN model has only two hidden layers in this study, and the precision has reached 99.769%, which indicates that when the hidden layers is more than two layers, the accuracy of the it will be infinitely close to 100%. The predicted stresses obtained by the BP-ANN model are basically identical to that of the experimental [68-69].

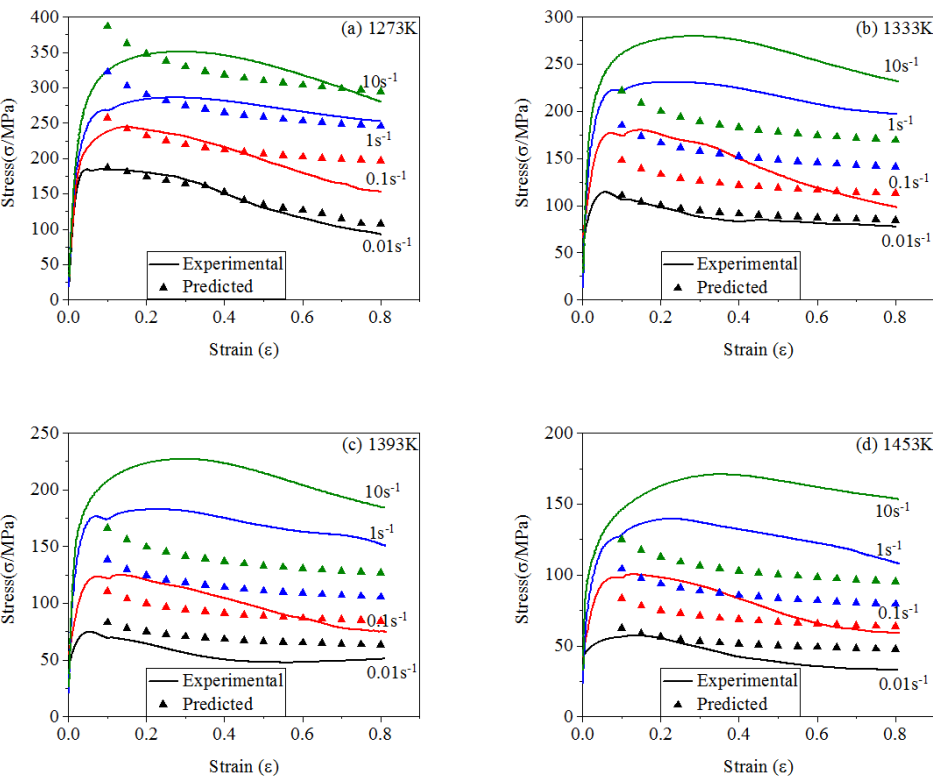


Fig.12 The comparison of stresses between experimental and predicted of J-C model.

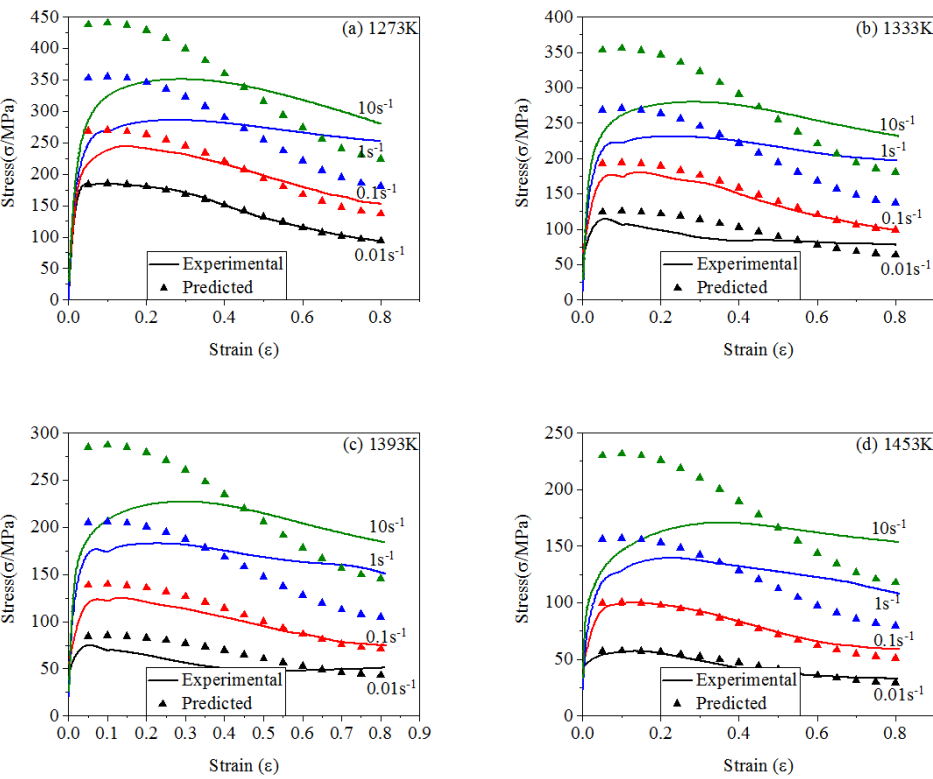


Fig.13 The comparison of stresses between experimental and predicted of modified J-C model.

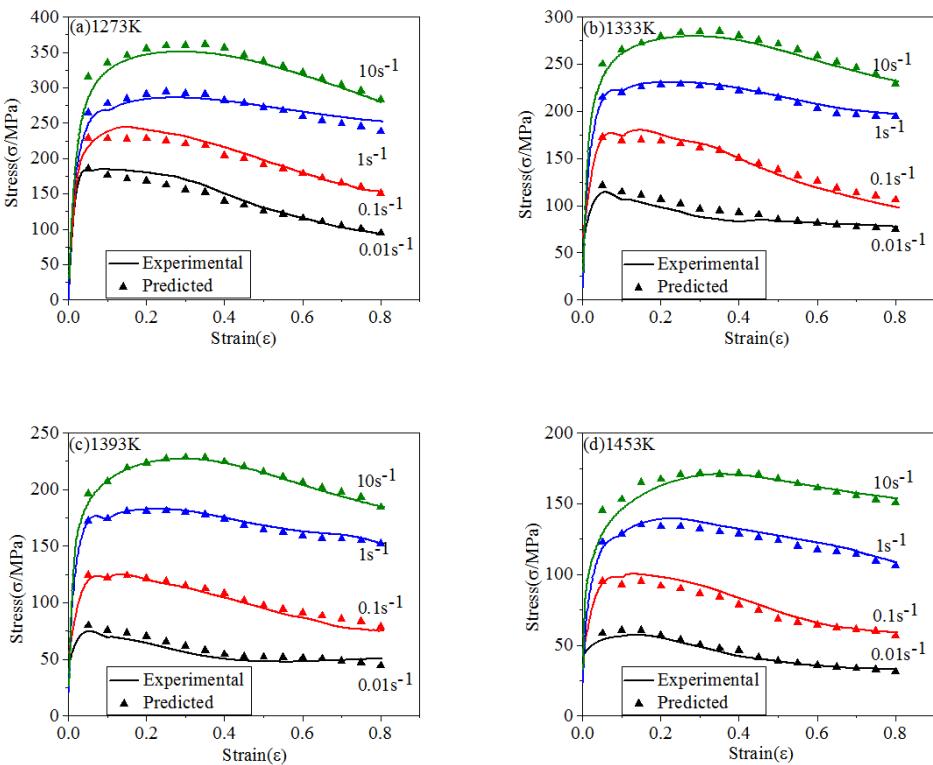


Fig.14 The comparison of stresses between experimental and predicted of Arrhenius model.

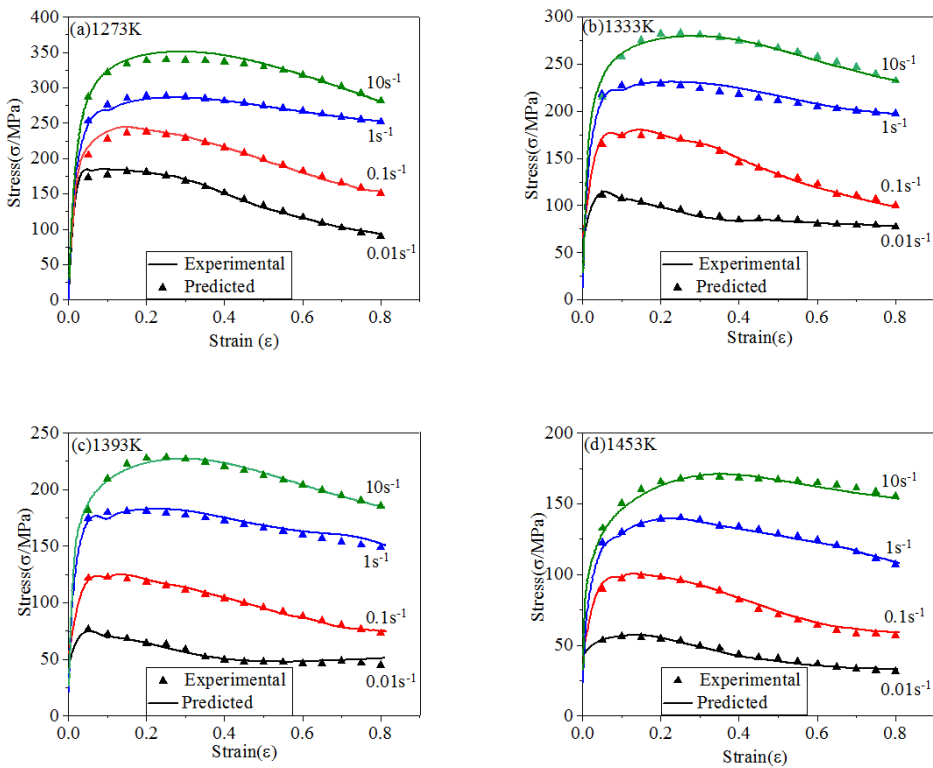


Fig.15 The comparison of stresses between experimental and predicted of BP-ANN model.

The AARE and R is introduced to verify the accuracy of four models. The values of AARE and

R more accurately reflect the linear relationship and effective information between experimental and predicted. Eq. (28) and Eq. (29) show the expressions of AARE and R:

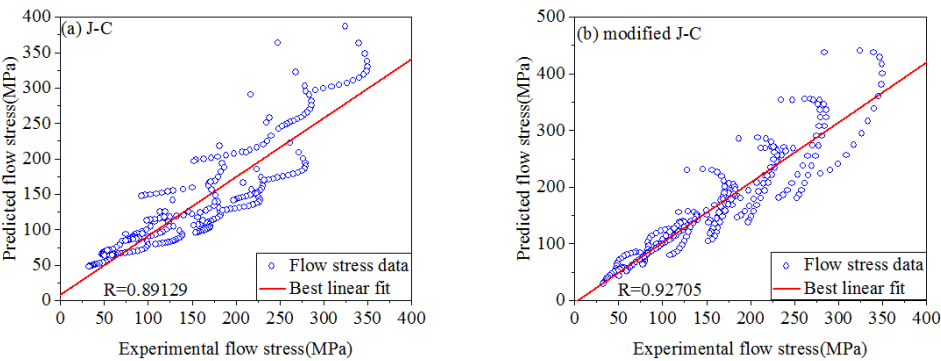
$$AARE(\%) = \frac{1}{N} \sum_{i=1}^N \left| \frac{E_i - P_i}{E_i} \right| \times 100\% \tag{28}$$

$$R = \frac{\sum_{i=1}^n (E_i - \overline{E})(P_i - \overline{P})}{\sqrt{\sum_{i=1}^n (E_i - \overline{E})^2 \sum_{i=1}^n (P_i - \overline{P})^2}} \tag{29}$$

Fig.16 shows the comparison of stresses between experimental and prediction of four models. These R and AARE of four models are calculated by using Eq. (28) and Eq. (29). Table 5 shows the results. From Table 5, the accuracy of modified J-C model is significantly higher than J-C model. And the accuracy of the BP-ANN model is the highest.

Table.5 R and AARE of the four models.

| Types of models | J-C | modified J-C | Arrhenius | BP-ANN |
|-----------------|----------|--------------|-----------|---------|
| AARE | 19.4704% | 13.7428% | 3.3774% | 1.7634% |
| R | 0.83255 | 0.92705 | 0.99452 | 0.99769 |



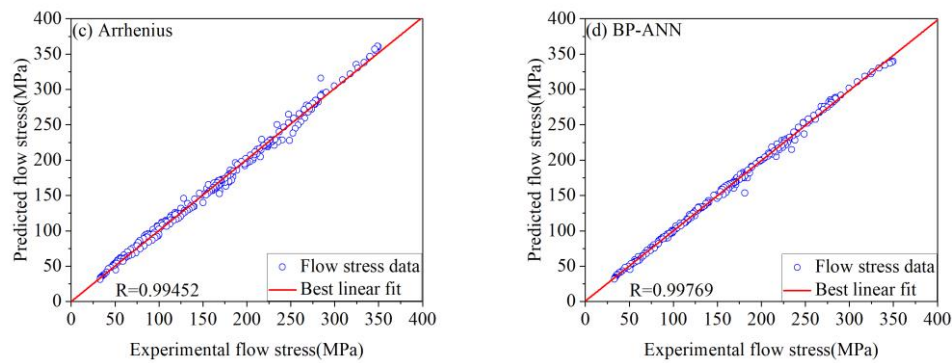


Fig.16 The comparison of experimental and predicted stresses of four models.

3.6 Finite element simulation of four models

In order to verify the practicability of the four models, the Deform-3D software was used to simulate the isothermal compression process. Taking the deformation temperature of 1393K and strain rate of 10s^{-1} as an example, the four established models were input into Deform-3D software for numerical simulation. Fig.17 shows the 3D mesh geometric model simulated by finite element method and the compression process of the simulated sample. The simulated deformation is consistent with the actual compression test. There is no interruption or error report in the simulation process, which indicates that the four established models are correct and can be input into the simulation software for simulation and the simulation accuracy is acceptable.

Fig.18 shows the equivalent stress field, equivalent strain field and temperature field of the samples simulated by four models. It can be seen from the figure that the equivalent stress field, equivalent strain field and temperature field of the samples obtained by the simulation of the four models are all symmetrical structures, indicating that the samples are under uniform stress in the compression process. The maximum stress values all appear in the place where the sample and the mold contact, indicating that the contact surface between the sample and the mold is the main stress area. The equivalent strain field is divided into three or more regions, indicating that the deformation

of the sample is not uniform. The maximum strain appears in the center of the sample, because the center part of the sample is the main deformation area, and it is subject to the common pressure of the upper die and the lower die, and the friction force is smaller than the upper and lower contact surfaces of the sample, so the deformation degree is the maximum. The temperature of the upper and lower surfaces of the sample is the lowest because of the heat transfer between the sample and the mold part. The temperature in the center of the sample is the highest, because in the compression process, the sample will generate a lot of heat due to deformation, and the center part only transfers heat with the surrounding environment, the heat dissipation is far less than the heat transfer between the sample and the mold, so the temperature is the highest.

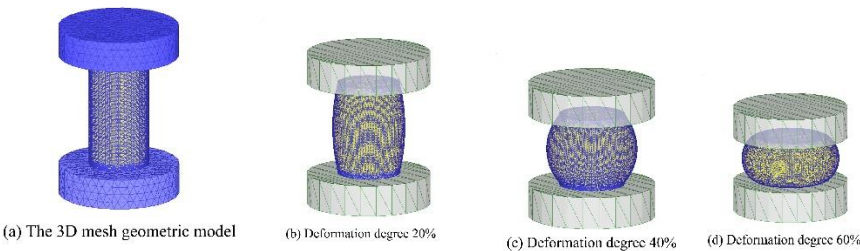
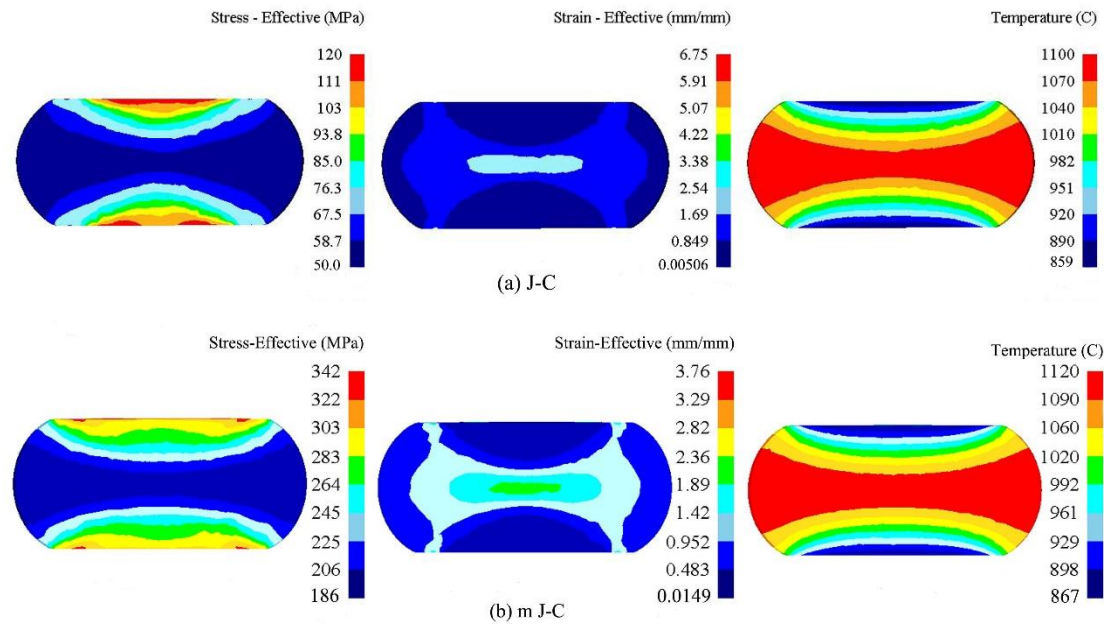


Fig.17 The 3D mesh geometric model and compression process of the simulated sample.



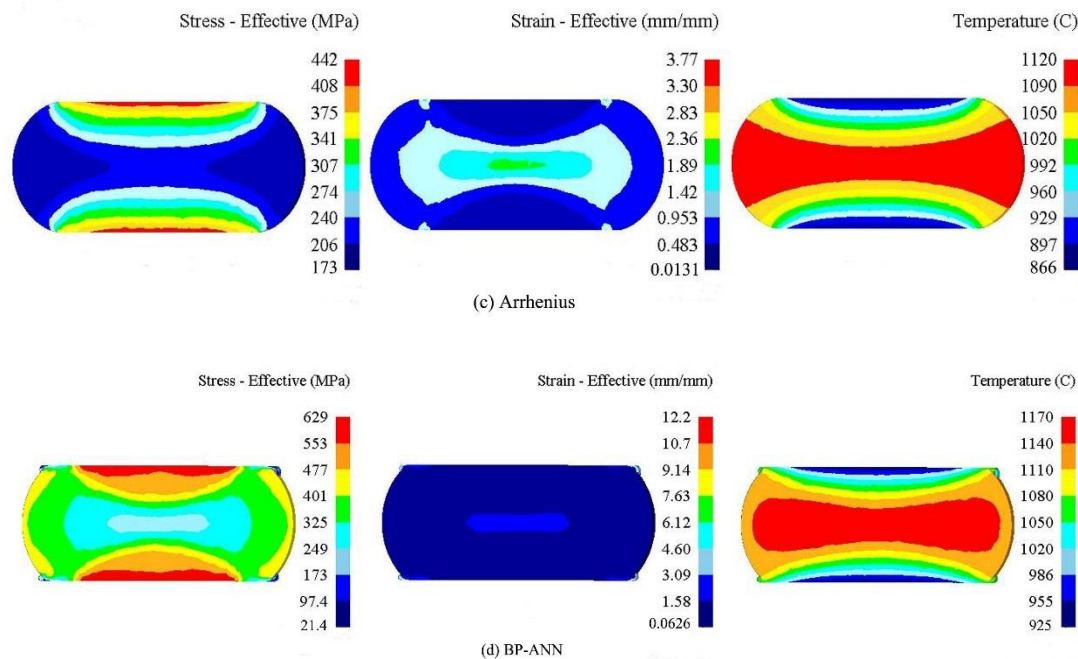


Fig.18 The equivalent stress field, equivalent strain field and temperature field of Four models.

4. Conclusions

1. The T and $\dot{\epsilon}$ are the main influencing factors of $21-4N$ during hot deformation, and they have a coupling effect on σ .
2. J-C model ignores the coupling effect of the $\dot{\epsilon}$ and T . As a result, when the deformation condition changes greatly, the accuracy decreases obviously.
3. Modified J-C model considers the coupling effect of T and $\dot{\epsilon}$. The parameter compensation is carried out on the basis of J-C model. The prediction accuracy has been greatly improved. When the deformation condition changes greatly, the accuracy of it is still within a reasonable range.
4. Arrhenius model uses the Z parameter to express the coupling effect of T and $\dot{\epsilon}$. The prediction accuracy is higher than modified J-C model. It is suitable for the σ prediction under the reasonable deformation conditions.

5. The established BP-ANN model has two hidden layers, which is $3 \times 10 \times 10 \times 1$ topology, and the training is completed after 47 iterations. And it has a very high accuracy under the conditions allowed by the deformation conditions.

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Compliance with ethical standard

The authors declare no conflict of interest.

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