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Scaffolds with a High Surface Area-to-Volume Ratio and Cultured Under Fast Flow Perfusion Result in Optimal O₂ Delivery to the Cells in Artificial Bone Tissues

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Featured Application: Optimization of Scaffold Design And Flow Perfusion Culturing Conditions for Maximal Delivery of Oxygen to the Cells Embedded Deep Inside of Engineered Tissues.

Abstract: Tissue engineering has the potential for repairing large bone defects, which impose a heavy financial burden on the public health. However, difficulties with O₂ delivery to the cells residing in the interior of tissue engineering scaffolds make it challenging to grow artificial tissues of clinically-relevant sizes. This study uses image-based simulation in order to provide insight into how to better optimize the scaffold manufacturing parameters, and the culturing conditions, in order to resolve the O₂ bottleneck. To do this, high resolution 3D X-ray images of two common scaffold types (salt leached foam and non-woven fiber mesh) are fed into a Lattice Boltzmann Method fluid dynamics and reactive Lagrangian Scalar Tracking mass transfer solvers. The obtained findings indicate that the scaffolds should have maximal surface area-to-solid volume ratios, for higher chances of the molecular collisions with the cells. Furthermore, the cell culture media should be flown through the scaffold pores as fast as practically possible (without detaching or killing the cells). Finally, we have provided a parametric sweep that maps how the molecular transport within the scaffolds is affected by variations in rates of O₂ consumption by the cells. Ultimately, the results of this study are expected to benefit the computer-assisted design of tissue engineering scaffolds and culturing experiments.

Keywords: Oxygen Delivery; Optimization; Mass Transfer; Transport; Bone tissue engineering; Computational fluid dynamics; Lattice Boltzmann Method; Scaffold Design; Culturing Protocol; Lagrangian Scalar Tracking

1. Introduction

Incidences of bone disorders constitute a significant economic burden to societies globally. In the United States alone, the total annual cost (direct and indirect) of treating an estimated 126.6 million people affected by musculoskeletal disorders exceeds \$213 billion [1]. Moreover, with an increasingly obese and ageing population, this trend is expected to continue further. Unfortunately, according to U.S Department of Health & Human Services, only ~10% out of the 115,000 people who needed a lifesaving organ transplant in 2018 have actually received it. This is because despite the

overwhelming demand, almost no FDA-approved [2] artificial tissue products are commercially available today.

A major hurdle standing in the way of producing viable engineered bone is product size limitations. These in turn stem from the inability to deliver sufficient amounts of metabolites (e.g., O_2 , nutrients, etc.) to the inner pore spaces of scaffolds, given that the cells consume them in large quantities as they build tissue. Among these, O_2 plays a critical role in the cell growth and proliferation, and thus its high concentrations have been correlated with both increased cellularity [3] and cell viability [4]. Conversely, a deficiency in O_2 can result in a hypoxic cell state, which is commonly associated with decreased metabolic activity and potentially undesirable differentiation behavior [5-7]. Hence, optimal oxygen transport is important in maintaining tissue function and overall survival within the artificial tissues. For that reason, bone tissue engineering scaffolds are typically cultured in perfusion bioreactors, the idea behind which is to facilitate the mass transfer using flow.

However, understanding what scaffold fabrication parameters, and flow culturing conditions, result in the optimal O_2 delivery to the cells is made difficult by the complexity of the pore network architectures in which they reside. This is because most large scaffolds are not transparent enough for microscopy, and it is also difficult to measure the O_2 concentrations at different locations within the scaffolds. Furthermore, the O_2 uptake rate by the cells changes over time [3]. All these complications make the problem even more difficult to solve manually. For these reasons, computer simulation of the O_2 transport and consumption offers itself as a viable alternative for obtaining insight into the microenvironment, which is experienced by the cells seeded on the surfaces of the scaffold pores.

Yet, modeling of mass transport (and specifically of O_2) within scaffolds is uncommon when compared to flow parameters, such as stimulatory fluid shear stress, permeability, and pressure (see Table II in Ref. [8]). Furthermore, Table 1 below summarizes our overview of the few O_2 models that we did find in literature. From it, it can be seen that the studies commonly use idealized geometries for the scaffolds (e.g., a homogeneous porous medium), instead of realistic image-based. In reality, however, the scaffold architectures may be inhomogeneous. Moreover, many of the models either do not take into account specificities of bone tissue engineering: such as the need for flow perfusion, which generates a stimulatory shear environment natural to the bone canaliculi [9,10]. Instead, many models either target tissue engineering in general, or they may be specific to other tissue engineering disciplines: for example, Ferroni et al. [11] modeled a cardiac scaffold, which is cultured under pulsatile flow (not the case for bone). Finally, few of the models take into account O_2 consumption by the cells. And among those that do, the rate is typically assumed to be constant. Thus, we were not able to find a single bone tissue engineering model, which accounted for all of the following: the realistic scaffold structure, O_2 diffusion, convection and variable consumption rates.

Table 1 Literature overview of O₂ simulations in tissue engineering scaffolds, shows that image-based simulation of convection with diffusion and reaction has not yet been done.

Scaffold Type	Simulated Geometry	O ₂ Diffusion	O ₂ Convection	O ₂ Reaction	Varied Parameter	Citation
45S5 Bioglass-PCL Robocast, Bioactive Glass 70S30C Sol-Gel Foamed and Titania Foam Replicated	Micro-computed Tomography	Yes	No	No	Void Fraction	Fiedler et al. [12]
Cardiac Tissue Eng.	Idealized	Yes	Yes	No	Squeeze Pressure	Ferroni et al. [11]
Microchanneled Hydrogel	Idealized	Yes	No	No	Microchannel Configuration	Arrigoni et al. [13]
Periodically Self-Repeated Representative Volume Element	Idealized	Yes	No	Yes	Geometry of the Repeating Element	Li et al. [14]
Bone Tissue Eng. Molded Tantalum	Idealized	Yes	Yes	Yes	Flow rate	Bergemann et al. [4]
Homogeneous Porous Medium	Idealized	Yes	Yes	Yes	Flow rate, Porosity	Yan et al. [15]

Therefore, in this work we aim to shed insight on how scaffold manufacturing parameters, and flow culturing conditions, affect the O₂ transport and uptake by the cells in realistic bone tissue engineering scaffolds. To do this, we use two types of commonly-implemented types: the salt leached foam and the non-woven fiber mesh poly-l-lactic acid (PLLA) scaffolds. Their geometries are scanned in 3D using high resolution micro-computed tomography (μCT), and imported into our image-based Lattice Boltzmann Method (LBM) flow[16-19] and reactive Lagrangian Scalar Tracking (rLST) mass transport [20] solvers. A big advantage of the latter is it can model particles with a range of reactivity, which is informative about how. In this way, a more complete picture of O₂ transport within the different types of BTE scaffolds can be constructed. The overall computational scheme is depicted in Figure 1.

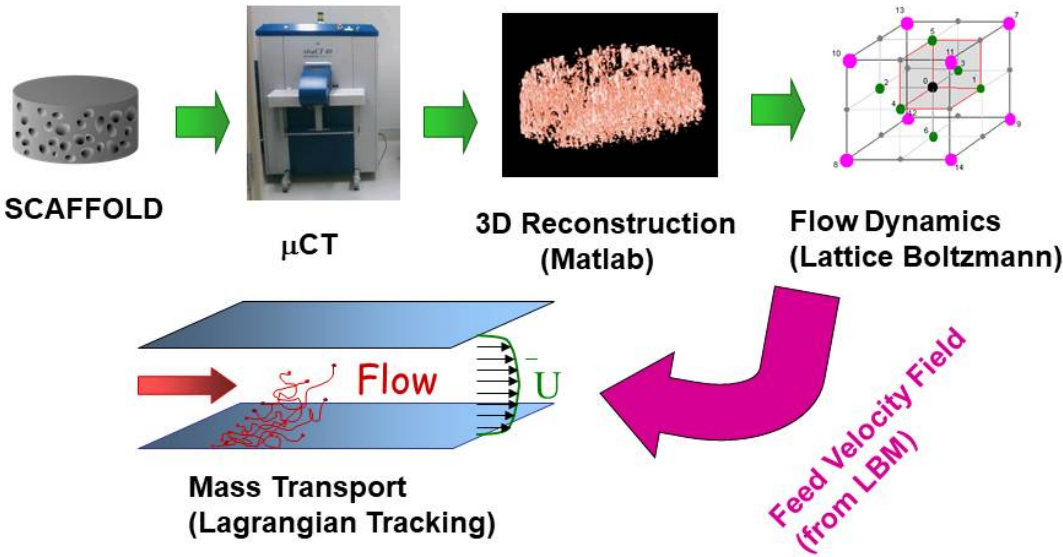


Figure 1 The image-based modeling methodology used in this work: scaffolds are scanned in 3D via high resolution μ CT, reconstructed in silico and the resulting geometries are used by the LBM and rLST solvers.

2. Materials and Methods

2.1 Scaffold Fabrication

The full details of the scaffold preparation protocols can be found in our previous publications [16,17]. Briefly, the scaffolds were non-woven fiber meshes, constructed using polymer micro-fibers produced with spunbonding. The polymer used in the production of fibers was poly-L-lactic-acid (grade 6251D, 1.4% D enantiomer 108,500 MW, 1.87 PDI, NatureWorks LLC). A custom Brabender extruder (19.1 mm (0.75 in.) diameter \times 381 mm length) was used to pressurize and melt the polymer. A manually circulated collection screen was used to collect a random even layering of fibers. Layers of fibers were stacked and measured until the stack reached a mass of 9.0 ± 0.1 g within an area of 162.8 cm^2 . The collected non-woven fiber stack then had a 7cm center cut sheet obtained from it. Finally using an 8 mm diameter die, discs were punched from the layered fiber sheets. The resulting scaffolds used in culturing were 8 mm diameter and ~ 2.3 mm thickness. Average fiber diameter was measured optically, using a Nikon HFX-II microscope.

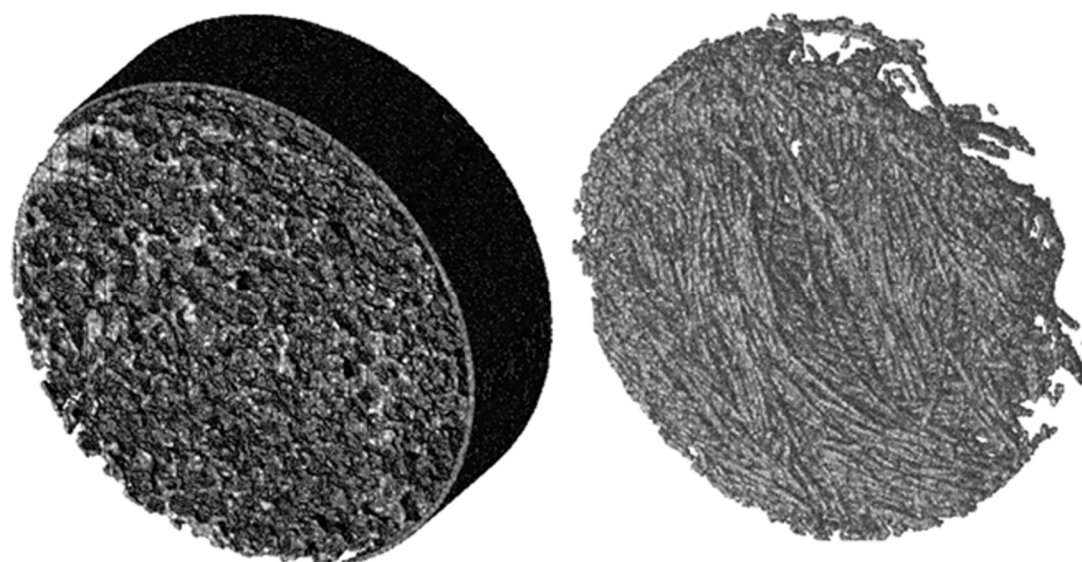
The porous foam scaffolds were prepared using solvent casting/particulate leaching method [21-24]. Briefly, poly(L-lactic acid) (PLLA, 114,500 MW, 1.87 PDI, Birmingham Polymers) was dissolved into chloroform 5% w/v. The solution was then poured over a bed of sodium chloride crystals. Solvent was allowed to evaporate for 24h. The resulting salt-polymer composite was inserted into an 8 mm diameter cylindrical mold and compressed at 500 psi. During compression, the composite was heated to $130\text{ }^\circ\text{C}$ and held at constant temperature and pressure for 30 min. Using a diamond wheel saw (Model 650, South Bay Technology, Inc.), the resulting composite rod was cut into 2.3 mm thick discs. The discs were placed into deionized water (DIH_2O) under agitation for 2 days to leach out NaCl. Entire DIH_2O volumes were replaced twice per day. Leached discs were then removed from DIH_2O and placed under vacuum to remove moisture from the scaffolds. The resulting products were 8 mm diameter, 2.3 mm thick discs. Porosity of scaffolds was determined by measuring the solid volume (mass of the scaffold divided by the density of PLLA) and comparing to the total scaffold volume (assuming a cylindrical scaffold shape.)

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123 *2.2 3D Imaging and Virtual Reconstruction*

124 The full details of our scanning procedure can be found in our previous publication.[16,17,25]
 125 Briefly, scaffolds were then scanned via μ CT using a ScanCo VivaCT40 system (ScanCo Medical,
 126 Bassersdorf, Switzerland) to obtain 10 μ m resolution, 2D intensity image slices at the optimum
 127 settings of 88 μ A (intensity) and 45 kV (energy). The acquired X-ray images were filtered for noise
 128 reduction and assembled into 3D reconstructions of the scaffolds using a custom Matlab code
 129 (MathWorks Inc., Natick, MA). The scans were segmented using global thresholding. Threshold
 130 values were chosen such that the porosity of scaffolds from 3D reconstructions were within 1% of
 131 experimentally calculated porosities. Figure 2 is a typical 3D reconstruction of each scaffold type.
 132 Experimental porosities were obtained by measuring the solid volume (mass of the scaffolds divided
 133 by the density of scaffold materials) and comparing with total scaffold volume (assuming a
 134 cylindrical scaffold) as reported in [16,17,20].

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137

138 **Figure 2** Three dimensional reconstructions of the two scaffold architecture types used in this study. LEFT - Salt-
 139 Leached Porous Foam Scaffold; RIGHT - Non-woven Fiber mesh Scaffold. Both of the scaffolds are made from
 140 PLLA, and their dimensions are 8-mm-diameter and 2.3-mm-thickness. The images were obtained via μ CT
 141 imaging described in our previous works [16,17,25].

142 *2.3 Fluid Flow Modeling: Lattice Boltzmann Method (LBM)*

143 LBM was chosen for the present application, because it is especially appropriate for modeling
 144 pore-scale flow through porous media (such as scaffolds) due to the simplicity with which it handles
 145 complicated boundaries [16-18,20,26-29]. This is because LBM uses structured meshes for complex
 146 geometries, unlike classical CFD approaches which will rather utilize unstructured meshes. Another
 147 advantage of LBM is that it uses a direct method based on first principles at the mesoscopic scale
 148 rather than modeling terms of the fluid flow governing equations at the macroscopic scale. In
 149 addition, the LBM method has gained popularity within the scientific computing community because
 150 of the ease with which it can be parallelized on supercomputers [30].

A previously developed custom-written, in-house code was used in this work [16-18,20,26,29,31]. The D3Q15 lattice [32] in conjunction with the single-relaxation time Bhatnagar, Gross and Krook [33] collision term approximation was used to perform simulations. The no-slip boundary condition was applied at solid faces using the “bounce-back” technique [34]. To take advantage of the inherent LBM parallelizability, domains were decomposed using message passing interface [18,26]. The code has been validated for several flow cases for which analytical solutions are available: forced flow in a slit, flow in a pipe and flow through an infinite array of spheres [16,26].

Each simulation domain was composed of a scaffold placed inside of a pipe. This is meant to mimic the cassette holder that typically fixes the scaffold in the perfusion bioreactors. The pipe's length was taken to be approximately 10 times greater than the scaffold thickness, in order to avoid periodicity artifacts, and to ensure that a uniform parabolic profile is developed before flow reaches the scaffolds. Simulations were performed for a flow rates ranging between 0.15-1 mL/min. This is considered a suitable range for culturing bone tissue in typical perfusion bioreactors. Convergence was defined as when average and highest velocities computed for the simulation domain vary by less than 0.01% for two consecutive time steps.

2.4 Oxygen Transport Modeling: Reactive Lagrangian Scalar Tracking (rLST)

The full details of the rLST code can be found in our prior publications [20,26]. Briefly, the trajectories of the rLST particles are determined by contributions from convection (obtained using the velocity field from the LBM simulations) and diffusion (i.e., Brownian motion obtained from a mesoscopic Monte-Carlo approach). For example, the new X position of a marker at time $t+1$ is calculated from the previous position at time t as follows:

$$\vec{X}_{t+1} = \vec{X}_t + \vec{U}_t^{(LBM)} \Delta t + \Delta \vec{X}_t^{(random)} \quad (1)$$

where \vec{U}_t is the fluid velocity at the particle's location at time t , as obtained from the LBM solver. On the other hand, the random jump has a standard deviation that is given by $\sigma = \sqrt{2D_0\Delta t} = \sqrt{2\nu\Delta t/Sc}$, where D_0 is the *nominal* molecular diffusivity (i.e. the diffusivity that the particles would have if their motion was purely Brownian). It can also be expressed in terms of the dimensionless Schmidt number Sc , which depends on the carrier fluid's viscosity. The molecular diffusivity of O₂ in the cell culture medium (assumed to be an aqueous solution at the physiological temperature of $T = 37^\circ\text{C}$) was $2.62 \times 10^{-5} \text{ cm}^2/\text{s}$, which corresponded to a Schmidt number of 328.14.

The rLST simulations were performed using 1 million particles, which was found to be sufficient to reproduce analytical results from the Taylor-Aris formula, during the validation runs. Their initial positions were distributed uniformly in a release plane at the pipe's entrance. Furthermore, in order to model the O₂ consumption by the cells, each of the rLST particles had a probability 'q' to react upon colliding with the scaffold walls: ranging from $q = 0$ (non-reactive) and $q = 1$ (fully reactive).

It was also assumed that the scaffold's surface was uniformly covered with a monolayer of the cells, each of them capable of consuming the O₂. Since second order reactions (reactions between solute particles) were not considered for this model, any interactions between rLST markers were neglected (i.e. they did not affect each other's path). This approximation is good for a dilute solution. The simulation was allowed to evolve for a total of 10,000-time steps, needed to achieve equilibration.

The 'Mersenne Twister' random number generator with a cycle of length ($2^{19937} - 1$) was used for all random number generation in the rLST code [35].

3. Results

As previously discussed, efficient delivery of O_2 is vital to the cell survival in the 3D bone tissue engineering scaffolds. Yet, choosing the optimal scaffold manufacturing parameters, and the culturing flow conditions is non-trivial, due to the complex transport phenomena occurring in the pore networks of the engineered tissue constructs. For this reason, we have performed image-based simulation of the fluid flow, and of the O_2 transport, occurring within two common types of bone tissue engineering PLLA scaffolds: the salt-leached foam and the non-woven fiber mesh.

Their geometries were varied by controlling the amount and the size of the leached salt grains for the former, and the fiber diameter for the latter. In order to compare the scaffolds on the same scale, here the results are plotted as a function of the "specific surface area" – defined as the ratio of surface area to solid volume. Furthermore, in order to analyze how the transport of O_2 is affected by the rate at which it is consumed by the cells, we considered different probabilities with which its molecules can react upon colliding with the scaffold walls. We examine the condition of a uniform coverage of the scaffold surfaces with O_2 -starved cells. This corresponds to an infinite surface reaction rate (i.e., instantaneous consumption of every O_2 molecule that collides with a scaffold wall); and should be treated as a limiting case scenario, which allows for a comparison of different scaffold structures on an equivalent basis.

Figure 3 is a 3D plot of the O_2 "survival distance" in the stream-wise direction (the X-direction), as a function of the scaffold structure and the cell-culture media perfusion flow rate. The survival distance is defined as the distance that the rLST markers (representing the O_2 molecules) travel on average, until they are "consumed" via a collision with a scaffold wall. From this figure, it is apparent that the survival distance in the stream-wise direction increases as the flow rate goes up. This is consistent with the Taylor-Aris dispersion theory, which states that the effective diffusivity in the stream-wise direction should increase with the square of the Peclet number [20,34]:

$$Pe_m = Re * Sc$$

where Re is the Reynolds number and Sc is the Schmidt Number. Its physical meaning is the ratio of the transport by advection to transport by diffusion. In this study, Sc is fixed for an O_2 molecule in an aqueous cell culture media at $T = 37\text{ }^{\circ}\text{C}$, as was discussed in the methods section. Hence, according to Equation 2, the Peclet number will increase proportionally with the value of Re , which depends on the velocity of the fluid. This leads to a higher effective diffusivity of the solute in the stream-wise direction; and thus, the O_2 can make it further into the scaffold, before it is fully consumed by the cells.

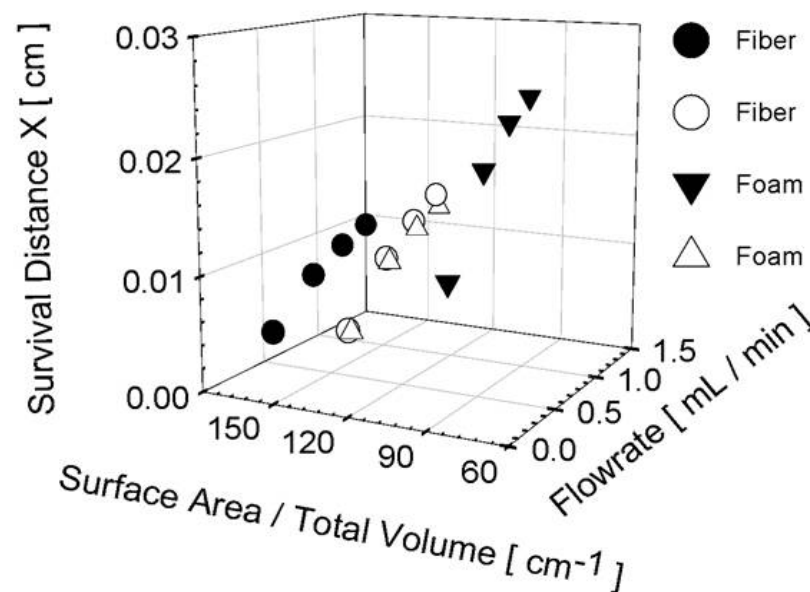


Figure 3 Survival distance in the stream-wise direction, as a function of the scaffold geometry and perfusion flow rate. Data is plotted for the limiting case of the fully reactive rLST particles.

Another trend that is apparent from Figure 3 is that the survival distance of O_2 is also inversely proportional to the specific surface area of the scaffold. This makes sense, because the O_2 molecules have a smaller chance to collide with the scaffold's surface, when it has less area exposed. Furthermore, Figure 3 shows that the foam scaffolds have a lower specific surface area than do the fiber ones. This leads to noticeably longer survival distances of O_2 in the foam scaffolds.

Overall, the result demonstrates that it is plausible to modify the scaffold's geometry in order to increase the efficiency of the O_2 transport within its structure. For example, the specific surface area of a medium composed of cylinders (such as the fiber-mesh scaffold) is given as:

$$S = \frac{4}{D} \quad (3)$$

where D is the fiber diameter. Unfortunately, there is no analytical formula for the salt-leached foam structures, due to their anisotropy resulting from the fabrication procedure. However, in general, their specific surface area goes up with lower porosity (i.e., amount of salt), and with smaller salt grain size used in the leaching.

Interestingly, the survival distances in the Y and Z directions (i.e., perpendicular to the flow) go down with the increasing flow rate (see Figure 4). The reason behind this is likely due to the particles becoming entrained by the carrier fluid. Consequently, they move less in the Y and Z directions per time step, relative to their displacement in the X . As a result, there is a smaller probability of collisions with the walls in the former directions. However, since both the Y and Z survival distances are an order of magnitude smaller than those in the X direction, the *total* survival distance is dominated by the trend displayed by the latter.

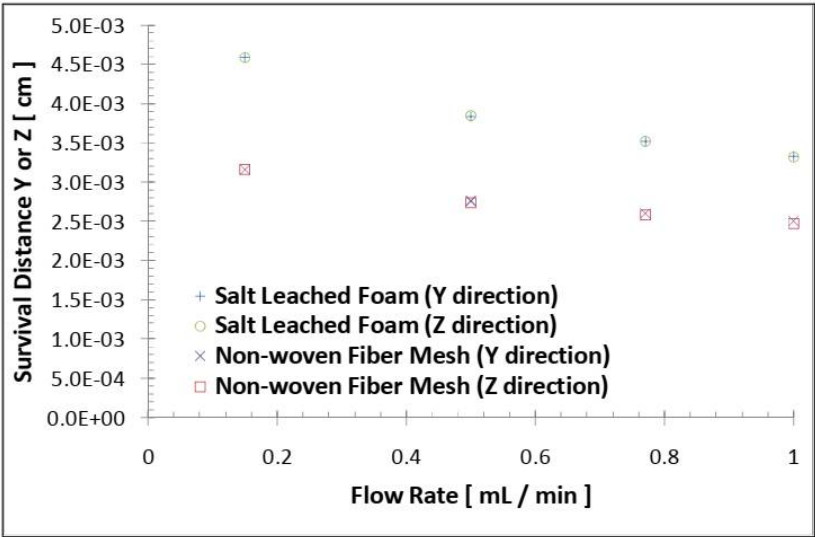


Figure 4 Survival distances in the Y & Z directions, as a function of the scaffold geometry and perfusion flow rate. Data is plotted for the limiting case of the fully reactive rLST particles. Both scaffolds types are chosen to have a similar specific surface area.

Another quantity of interest is the survival time of the O_2 molecules in the scaffolds. Figure 5 plots this quantity as a function of the flow rate and the specific surface area of the scaffolds; for the limiting case of fully reactive rLST particles. Conversely to the survival distance in Figure 3, the survival time in Figure 5 decreases with the flow rate. Though, the effect of the specific surface area remains the same, and the survival time varies inversely-proportionally to it. Combining the results from both of the figures, it becomes apparent that fully reactive molecules get carried to a farther distance by a higher flow rate. However, they take a shorter time to get consumed by the cells on the surface of the scaffolds. This is especially true for the scaffold geometries with a higher exposed surface area.

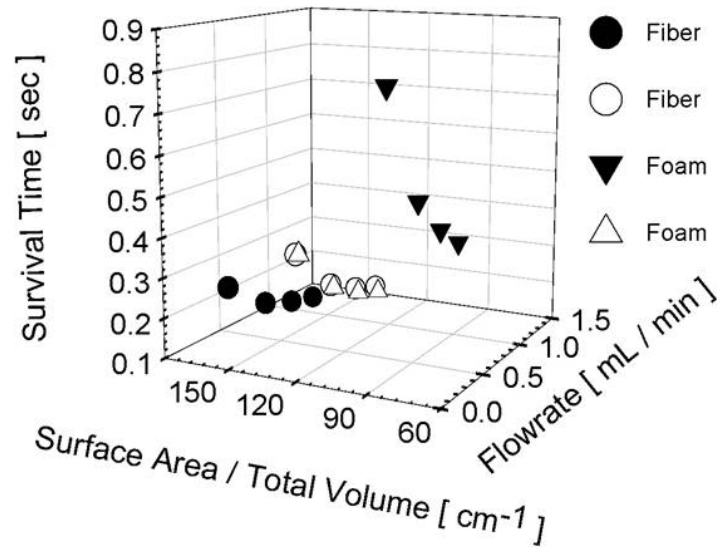


Figure 5 Survival time in the stream-wise direction, as a function of the scaffold geometry and perfusion flow rate. Data is plotted for the limiting case of the fully reactive rLST particles.

Ultimately, it is of interest to measure the *effective* 1st order reaction rate constant k_{eff} , with which the O₂ molecules get consumed in the scaffolds, after accounting for the mass transfer limitations. To that end, Figure 6 is a plot of k_{eff} as a function of the flow rate and specific surface area of the scaffold, for the limiting case of an infinitely fast surface consumption of O₂. It reaffirms the previously observed trends, which show that the O₂ is consumed faster in the scaffold structures with the higher surface area-to-solid volume ratios. Furthermore, it also supports the finding that increasing the cell culture media flow rate through the scaffold leads to a faster O₂ consumption in its pores.

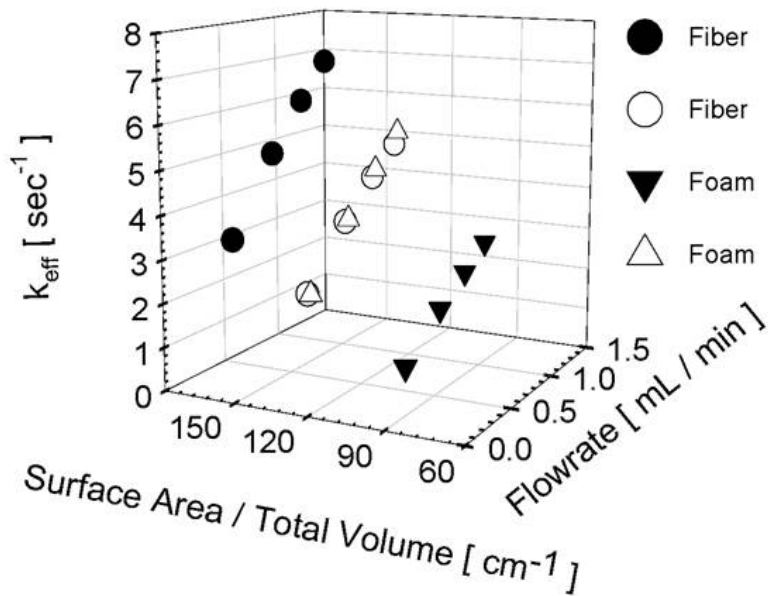


Figure 6 Effective O₂ reaction coefficient k_{eff} , as a function of the scaffold geometry and perfusion flow rate. Data is plotted for the limiting case of the fully reactive rLST particles.

If the cells are not starved for O₂, however, the rLST particles can be made to have a *finite* (as opposed to infinite) probability to become consumed upon collision with the scaffold walls. Thus, Figure 7 explores the role that the different cell affinities for consuming the O₂ have on its transport in the pores. In this case, the rLST particles with the different reactivities are all released simultaneously, and their survival times are compared as a function of the cell culture media flow rate and the scaffold type.

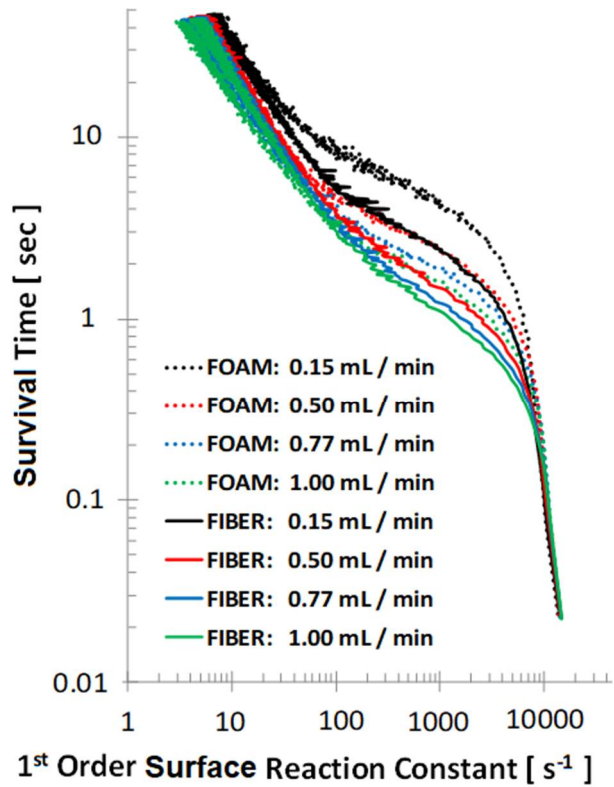


Figure 7 O₂ survival time as a function of the consumption rate by the cells on the scaffold surface. Data is plotted for salt leached foam and non-woven fiber mesh scaffolds at four different flow rates.

Two trends are immediately apparent from Figure 7: 1) the O₂ in the fiber scaffolds (solid lines) has a shorter survival time than in the foam ones (dotted lines), regardless of the cells' affinity for its uptake. This is consistent with the trends in the previous section, which showed that the fiber scaffolds have a higher specific surface area than do the foams. This makes them more efficient at delivering the O₂ molecules to the cells; and 2) the second trend essentially says that for a given surface reaction rate, the consumption of O₂ will take longer at the slower flows. This is again consistent with a similar trend that was shown in Figure 5, where the survival time increased with the slower flow rate.

4. Discussion

In this manuscript, we carried out a study of how the O₂ mass transfer is affected by the scaffold manufacturing and the flow perfusion culturing parameters, in bone tissue engineering scaffolds. The knowledge obtained from the reported results is needed in order to overcome the product-size limitations, which are commonly experienced due to hypoxia and necrosis in the center of large scaffolds. To solve the problem, we used an image-based approach of scanning the true scaffold structures in 3D using a high resolution μ CT, and then feeding the obtained geometries to our in-house parallelized fluid flow (LBM) and mass transport (rLST) solvers. Two scaffolds commonly used in bone tissue engineering, the salt leached foam and the nonwoven fiber mesh, were used for this study. The O₂ transport results were parametrized as a function of the specific surface area of the scaffold, the flow rate in the bioreactor and the affinity to consume the molecule by the cells.

The main conclusions from our work are that the scaffolds with the higher specific area (i.e. surface area-to-solid volume ratio) result in more frequent molecular collisions with the cells. This

increases the chances of the O₂ uptake by them, which results in a higher consumption (i.e., shorter survival times and distances) of the molecules in the scaffold. Furthermore, by increasing the flow rate in the bioreactor, the O₂ transport can be both facilitated (as seen from the shorter survival time in Figure 4) and delivered deeper into the scaffold (as seen from the longer survival distance in Figure 3). Thus, the overall effective O₂ reaction coefficient k_{eff} can be increased by maximizing both the specific surface area of the scaffold and the flowrate through its pores. This is evident from Figure 6.

Interestingly, the conclusion that an increased flow rate improves the O₂ delivery to the cells has also been reported by Bergemann et al. [4]. However, increasing it indefinitely is not an option, because there is a trade-off with the shear forces exerted on the cells by the flow. Specifically, values in the range of 0.1 - 25 dynes/cm² [36-38] are generally considered to be beneficial because they mimic the natural microenvironment in bone canaliculi [9,10] and has been shown to promote tissue regeneration [39-42]. On the other hand, an excessive shear in the range of 26-54 dynes/cm² and higher can cause cell lysing and/or detachment from the scaffold [43,44]. Therefore, there is some optimal flow rate, which was found to be 45 L/min by the Bergemann et al. study [4]. However, this value is specific to their scaffold-and-cell combination, and it could vary for other alternatives. Therefore, both image-based numerical simulations and cell viability assays are necessary for tuning the optimal conditions for other types of cultures. Whereas, at least the physical understanding provided in our study should be applicable across all scaffold types, because they are expressed in terms of the specific surface area.

Finally, Figure 7 in our manuscript provides insight into how the O₂ transport depends on its consumption by the cells. In this case, we are not assuming that the cells are O₂-starved (and as a result take up every oxygen molecule that collides with them). Instead, we vary consumption rate of the O₂ at the scaffold surface, in order to measure how this affects its transport in the scaffold. The results reported in this figure allow other researchers to understand the changes in the scaffold's transport microenvironment over time. They also show how the flowrate and specific surface area trends are affected by the cell-specific O₂ consumption rates.

The limitations of our study are that the cells are assumed to have a uniform coverage on the scaffold surface. In reality, they would likely prefer some areas of the scaffolds more than others. Furthermore, the tissue they lay down and the forces they exert on the scaffold would likely alter the internal structure of the scaffold (and in turn the flow field in its pores). Unfortunately, our model does not account for these types of influences by the cells on the mass transfer of O₂. Additionally, the scaffold's structure in the real experiment could change due to wetting forces, fiber flexibility, and the natural degradation of PLLA. The latter produces acidic byproducts, whose removal is facilitated by the fluid flow [45]. Yet, in our study the scaffold's structure remains static throughout the virtual experiment.

However, the results presented in this manuscript expose qualitative trends that should hold true regardless of the necessary simplifications. Therefore, it is expected that they should contribute significantly to the field of bone tissue engineering scaffold design and experiment optimization.

5. Conclusions

Mass transfer of O₂ in scaffolds cultured in perfusion bioreactors is of interest to the fields of bone, and other types of, tissue engineering. Specifically, understanding how to control it can be instrumental to resolving product size limitations, when it comes to culturing organ-sized scaffolds.

Therefore, we performed an image-based simulation study, in which we showed that the scaffolds with the higher surface area-to-solid volume ratio result in a more efficient transfer of O₂. Additionally, we showed that the effect can be increased further by flowing the cell culture media through the scaffold faster. Serendipitously, this also delivers the O₂ deeper into the scaffold pores, which is key to overcoming the product-size limitations mentioned earlier. Furthermore, we provided a parametric sweep over the rates of O₂ consumption by the cells situated on the scaffold surfaces. This visual aid yields insight into how the different cell affinities for consuming the O₂ can affect the molecule's transport through the biological porous media. Finally, the computational framework presented in this study can serve as a viable tool for optimizing the scaffold design, and experimental culturing protocols, for other types of tissue engineering as well.

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Conflicts of Interest: The authors have no competing financial interests to declare.

References

1. American Academy of Orthopaedic Surgeons, A. One in two Americans have a musculoskeletal condition. Available online: <https://www.sciencedaily.com/releases/2016/03/160301114116.htmEnglish> (accessed on 06/13).
2. Administration, U.S.F.a.D. Approved Cellular and Gene Therapy Products. Available online: <https://www.fda.gov/BiologicsBloodVaccines/CellularGeneTherapyProducts/ApprovedProducts/default.htm> (accessed on 02/20/2018).
3. Simmons, A.D.; Williams, C.; Degoix, A.; Sikavitsas, V.I. Sensing metabolites for the monitoring of tissue engineered construct cellularity in perfusion bioreactors. *Biosensors and Bioelectronics* **2017**, *90*, 443–449.
4. Bergemann, C.; Elter, P.; Lange, R.; Weissmann, V.; Hansmann, H.; Klinkenberg, E.D.; Nebe, B. Cellular Nutrition in Complex Three-Dimensional Scaffolds: A Comparison between Experiments and Computer Simulations. *Int J Biomater* **2015**, *2015*, 584362, doi:10.1155/2015/584362.
5. Gilkes, D.M.; Semenza, G.L.; Wirtz, D. Hypoxia and the extracellular matrix: drivers of tumour metastasis. *Nature Reviews Cancer* **2014**, *14*, 430.
6. Spill, F.; Reynolds, D.S.; Kamm, R.D.; Zaman, M.H. Impact of the physical microenvironment on tumor progression and metastasis. *Current opinion in biotechnology* **2016**, *40*, 41–48.

7. Nguyen, T.D.; Song, M.S.; Ly, N.H.; Lee, S.Y.; Joo, S.W. Nanostars on Nanopipette Tips: A Raman Probe for Quantifying Oxygen Levels in Hypoxic Single Cells and Tumours. *Angew Chem Int Ed Engl* **2019**, *58*, 2710-2714, doi:10.1002/anie.201812677.
8. Zhang, S.; Vijayavenkataraman, S.; Lu, W.F.; Fuh, J.Y. A review on the use of computational methods to characterize, design, and optimize tissue engineering scaffolds, with a potential in 3D printing fabrication. *Journal of Biomedical Materials Research Part B: Applied Biomaterials* **2018**.
9. Verbruggen, S.W.; Vaughan, T.J.; McNamara, L.M. Fluid flow in the osteocyte mechanical environment: a fluid-structure interaction approach. *Biomech Model Mechanobiol* **2014**, *13*, 85-97, doi:10.1007/s10237-013-0487-y.
10. Guyot, Y.; Luyten, F.P.; Schrooten, J.; Papantoniou, I.; Geris, L. A three-dimensional computational fluid dynamics model of shear stress distribution during neotissue growth in a perfusion bioreactor. *Biotechnol Bioeng* **2015**, *112*, 2591-2600, doi:10.1002/bit.25672.
11. Ferroni, M.; Giusti, S.; Nascimento, D.; Silva, A.; Boschetti, F.; Ahluwalia, A. Modeling the fluid-dynamics and oxygen consumption in a porous scaffold stimulated by cyclic squeeze pressure. *Med Eng Phys* **2016**, *38*, 725-732, doi:10.1016/j.medengphy.2016.04.016.
12. Fiedler, T.; Belova, I.V.; Murch, G.E.; Poologasundarampillai, G.; Jones, J.R.; Roether, J.A.; Boccaccini, A.R. A comparative study of oxygen diffusion in tissue engineering scaffolds. *J Mater Sci Mater Med* **2014**, *25*, 2573-2578, doi:10.1007/s10856-014-5264-7.
13. Arrigoni, C.; Bongio, M.; Talò, G.; Bersini, S.; Enomoto, J.; Fukuda, J.; Moretti, M. Rational design of prevascularized large 3D tissue constructs using computational simulations and biofabrication of geometrically controlled microvessels. *Advanced healthcare materials* **2016**, *5*, 1617-1626.
14. Li, E.; Chang, C.; Zhang, Z.; Li, Q. Characterization of tissue scaffolds for time-dependent biotransport criteria—a novel computational procedure. *Computer methods in biomechanics and biomedical engineering* **2016**, *19*, 1210-1224.
15. Yan, X.; Bergstrom, D.J.; Chen, X.B. Modeling of cell cultures in perfusion bioreactors. *IEEE Trans Biomed Eng* **2012**, *59*, 2568-2575, doi:10.1109/TBME.2012.2206077.
16. Voronov, R.; Vangordon, S.; Sikavitsas, V.I.; Papavassiliou, D.V. Computational modeling of flow-induced shear stresses within 3D salt-leached porous scaffolds imaged via micro-CT. *Journal of Biomechanics* **2010**, *43*, 1279-1286, doi:10.1016/j.jbiomech.2010.01.007.
17. VanGordon, S.B.; Voronov, R.S.; Blue, T.B.; Shambaugh, R.L.; Papavassiliou, D.V.; Sikavitsas, V.I. Effects of Scaffold Architecture on Preosteoblastic Cultures under Continuous Fluid Shear. *Industrial & Engineering Chemistry Research* **2011**, *50*, 620-629, doi:10.1021/ie902041v.
18. Papavassiliou, D.V.; Pham, N.H.; Kadri, O.E.; Voronov, R.S. Chapter 23 - Lattice Boltzmann Methods for Bioengineering Applications. In *Numerical Methods and Advanced Simulation in Biomechanics and Biological Processes*, Academic Press: 2018; doi: 10.1016/B978-0-12-811718-7.00023-Xpp. 415-429.
19. Alam, T.A.; Pham, Q.L.; Sikavitsas, V.I.; Papavassiliou, D.V.; Shambaugh, R.L.; Voronov, R.S. Image-based modeling: A novel tool for realistic simulations of artificial bone cultures. *Technology* **2016**, 1-5.
20. Voronov, R.S.; VanGordon, S.B.; Sikavitsas, V.I.; Papavassiliou, D.V. Efficient Lagrangian scalar tracking method for reactive local mass transport simulation through porous media. *International Journal for Numerical Methods in Fluids* **2011**, *67*, 501-517, doi:10.1002/fld.2369.
21. Lu, L.C.; Peter, S.J.; Lyman, M.D.; Lai, H.L.; Leite, S.M.; Tamada, J.A.; Vacanti, J.P.; Langer, R.; Mikos, A.G. In vitro degradation of porous poly(L-lactic acid) foams. *Biomaterials* **2000**, *21*, 1595-1605.

22. Alvarez-Barreto, J.F.; Sikavitsas, V.I. Improved mesenchymal stem cell seeding on RGD-modified poly(L-lactic acid) scaffolds using flow perfusion. *Macromol Biosci* **2007**, *7*, 579-588, doi:DOI 10.1002/mabi.200600280.
23. Mikos, A.G.; Lyman, M.D.; Freed, L.E.; Langer, R. Wetting of poly(L-lactic acid) and poly(DL-lactic-co-glycolic acid) foams for tissue culture. *Biomaterials* **1994**, *15*, 55-58.
24. Liu, X.; Ma, P.X. Polymeric scaffolds for bone tissue engineering. *Ann Biomed Eng* **2004**, *32*, 477-486.
25. Voronov, R.S.; VanGordon, S.B.; Shambaugh, R.L.; Papavassiliou, D.V.; Sikavitsas, V.I. 3D Tissue-Engineered Construct Analysis via Conventional High-Resolution Microcomputed Tomography Without X-Ray Contrast. *Tissue Engineering Part C-Methods* **2013**, *19*, 327-335, doi:10.1089/ten.tec.2011.0612.
26. Voronov, R. Fluid Shear Stress and Nutrient Transport effects via Lattice-Boltzmann and Lagrangian Scalar Tracking Simulations of cell culture media perfusion through artificial bone engineering constructs imaged with microCT[PhD Thesis]. Doctoral Dissertation, University of Oklahoma, 2010.
27. Porter, B.; Zauel, R.; Stockman, H.; Guldberg, R.; Fyhrie, D. 3-D computational modeling of media flow through scaffolds in a perfusion bioreactor. *Journal of Biomechanics* **2005**, *38*, 543-549, doi: 10.1016/j.jbiomech.2004.04.011.
28. Shakhawath Hossain, M.; Bergstrom, D.J.; Chen, X.B. A mathematical model and computational framework for three-dimensional chondrocyte cell growth in a porous tissue scaffold placed inside a bi-directional flow perfusion bioreactor. *Biotechnology and bioengineering* **2015**, *112*, 2601-2610, doi:10.1002/bit.25678.
29. Williams, C.; Kadri, O.; Voronov, R.; Sikavitsas, V. Time-Dependent Shear Stress Distributions during Extended Flow Perfusion Culture of Bone Tissue Engineered Constructs. *Fluids* **2018**, *3*, 25.
30. Wang, J.; Zhang, X.; Bengough, A.G.; Crawford, J.W. Domain-decomposition method for parallel lattice Boltzmann simulation of incompressible flow in porous media. *Physical Review E* **2005**, *72*, 016706, doi:10.1103/PhysRevE.72.016706.
31. Kadri, O.E.; Williams, C., 3rd; Sikavitsas, V.; Voronov, R.S. Numerical accuracy comparison of two boundary conditions commonly used to approximate shear stress distributions in tissue engineering scaffolds cultured under flow perfusion. *Int J Numer Method Biomed Eng* **2018**, *34*, e3132, doi:10.1002/cnm.3132.
32. Qian, Y.H.; Dhumieres, D.; Lallemand, P. Lattice Bgk Models for Navier-Stokes Equation. *Europhysics Letters* **1992**, *17*, 479-484.
33. Bhatnagar, P.L.; Gross, E.P.; Krook, M. A Model for Collision Processes in Gases .1. Small Amplitude Processes in Charged and Neutral One-Component Systems. *Physical Review* **1954**, *94*, 511-525.
34. Sukop, M.C.; Thorne, D.T.; NetLibrary Inc. Lattice Boltzmann modeling an introduction for geoscientists and engineers. Springer: Berlin ; New York, 2006; pp ix, 172 p.
35. Matsumoto, M.; Nishimura, T. Mersenne twister: a 623-dimensionally equidistributed uniform pseudo-random number generator. *ACM Trans. Model. Comput. Simul.* **1998**, *8*, 3-30, doi:10.1145/272991.272995.
36. Stolberg, S.; McCloskey, K.E. Can shear stress direct stem cell fate? *Biotechnology Progress* **2009**, *25*, 10-19, doi:10.1002/btpr.124.
37. Raimondi, M.T.; Moretti, M.; Cioffi, M.; Giordano, C.; Boschetti, F.; Lagana, K.; Pietrabissa, R. The effect of hydrodynamic shear on 3D engineered chondrocyte systems subject to direct perfusion. *Biorheology* **2006**, *43*, 215-222.
38. Kim, K.M.; Choi, Y.J.; Hwang, J.-H.; Kim, A.R.; Cho, H.J.; Hwang, E.S.; Park, J.Y.; Lee, S.-H.; Hong, J.-H. Shear Stress Induced by an Interstitial Level of Slow Flow Increases the Osteogenic Differentiation of

- Mesenchymal Stem Cells through TAZ Activation. *PLOS ONE* **2014**, *9*, e92427, doi:10.1371/journal.pone.0092427.
39. Miyashita, S.; Ahmed, N.E.M.B.; Murakami, M.; Iohara, K.; Yamamoto, T.; Horibe, H.; Kurita, K.; Takano-Yamamoto, T.; Nakashima, M. Mechanical forces induce odontoblastic differentiation of mesenchymal stem cells on three-dimensional biomimetic scaffolds. *Journal of Tissue Engineering and Regenerative Medicine* **2017**, *11*, 434-446, doi:10.1002/term.1928.
40. Zhao, F.; Vaughan, T.J.; McNamara, L.M. Quantification of fluid shear stress in bone tissue engineering scaffolds with spherical and cubical pore architectures. *Biomechanics and Modeling in Mechanobiology* **2016**, *15*, 561-577, doi:10.1007/s10237-015-0710-0.
41. Sikavitsas, V.I.; Bancroft, G.N.; Holtorf, H.L.; Jansen, J.A.; Mikos, A.G. Mineralized matrix deposition by marrow stromal osteoblasts in 3D perfusion culture increases with increasing fluid shear forces. *Proceedings of the National Academy of Sciences* **2003**, *100*, 14683-14688, doi:10.1073/pnas.2434367100.
42. Yourek, G.; McCormick, S.M.; Mao, J.J.; Reilly, G.C. Shear stress induces osteogenic differentiation of human mesenchymal stem cells. *Regenerative medicine* **2010**, *5*, 713-724, doi:10.2217/rme.10.60.
43. Brindley, D.; Moorthy, K.; Lee, J.-H.; Mason, C.; Kim, H.-W.; Wall, I. Bioprocess Forces and Their Impact on Cell Behavior: Implications for Bone Regeneration Therapy. *Journal of Tissue Engineering* **2011**, *2011*, 620247, doi:10.4061/2011/620247.
44. Alvarez-Barreto, J.F.; Linehan, S.M.; Shambaugh, R.L.; Sikavitsas, V.I. Flow Perfusion Improves Seeding of Tissue Engineering Scaffolds with Different Architectures. *Annals of Biomedical Engineering* **2007**, *35*, 429-442, doi:10.1007/s10439-006-9244-z.
45. Agrawal, C.M.; McKinney, J.S.; Lancot, D.; Athanasiou, K.A. Effects of fluid flow on the in vitro degradation kinetics of biodegradable scaffolds for tissue engineering. *Biomaterials* **2000**, *21*, 2443-2452.
46. Towns, J.; Cockerill, T.; Dahan, M.; Foster, I.; Gaither, K.; Grimshaw, A.; Hazlewood, V.; Lathrop, S.; Lifka, D.; Peterson, G.D., et al. XSEDE: Accelerating Scientific Discovery. *Computing in Science & Engineering* **2014**, *16*, 62-74, doi:10.1109/MCSE.2014.80.