

1 Article

2 Microstructure and martensitic transformation 3 behavior in thermal cycled equiatomic CuZr shape 4 memory alloy

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17 **Abstract:** Equiatomic CuZr alloy undergoes a martensitic transformation from the B2 parent phase
18 to martensitic phases ($P2_1/m$ and Cm) below 150 °C. We clarified the effect of the thermal cycling on
19 the morphology and crystallography of martensite in equiatomic CuZr alloy using a transmission
20 electron microscopy. The 10th cycled specimens consisted of different multiple structures at the
21 maximum temperature of DSC measurement: 400 °C and 500°C, respectively. At the maximum
22 temperature 400 °C of DSC measurement, it is composed of the fine plate-like variants, and a
23 lamellar eutectoid structure consisting of $Cu_{10}Zr_7$ and $CuZr_2$ phases on the martensitic variant.
24 Concerning the maximum temperature 500 °C of DSC measurement, it is observed the martensitic
25 structure and the lamellar structure in which the martensitic phase was completely eutectoid
26 transformed. The formation of this lamellar eutectoid structure due to thermal cycling leads to the
27 shift of forward and reverse transformation peaks to low and high temperature side. In addition,
28 new forward and reverse transformation peaks indicating a new transformation appeared by
29 thermal cycling, and the peaks remained around -20 °C. This new martensitic transformation
30 behavior is also discussed.

31 **Keywords:** Shape memory alloys; CuZr alloy; Thermal cycling; Microstructure; Martensitic
32 transformation; Transmission electron microscopy

34 1. Introduction

35 Equiatomic CuZr alloy is expected as a high temperature shape memory material, since it
36 undergoes martensitic transformation point over 100 °C [1-11]. This alloy shows a martensitic
37 transformation from the B2 matrix (space group: $Pm\bar{3}m$) to the two martensitic phases (space group:
38 $P2_1/m$ and Cm) at about 150 °C, and its reverse transformation temperature is around 265 °C [3-5].
39 One of the important characteristics required for practical application of shape memory alloy is a
40 thermal cycling property. Koval *et al.* [3] reported the thermal cycling behavior of equiatomic CuZr
41 alloy is what the transformation peaks shifted significantly, and additional peaks meaning new
42 martensitic transformation appeared by electrical resistivity measurements. In addition, Biffi *et al.*
43 [12] also investigated the thermal cycling property in detail on equiatomic CuZr alloy by differential
44 scanning calorimetry (DSC) measurement as follows. The thermal cycling of equiatomic CuZr alloy

45 provides that the reverse transformation start (A_s) temperature and the martensitic transformation
46 start temperature (M_s) shifted to the high and low temperature sides, respectively. It was also
47 confirmed that the reverse transformation peak A and the martensitic transformation peak M
48 disappear in the 7th cycle [12]. Alternatively, at the 4th cycle, new peaks A^* and M^* different from
49 peaks A and M appeared, and then these new peaks remained around $-20\text{ }^\circ\text{C}$ at the 50th cycle.
50 Although the changes in the macroscopic features and crystal structure accompanying these peaks
51 have been investigated by scanning electron microscopy (SEM) observation and x-ray diffraction
52 (XRD) measurement at varying the temperature, a detail microstructural characterization is not
53 performed in nanoscopic scale. In this study, we aimed to clarify the effect of the thermal cycling on
54 the morphology and crystallography of martensite in equiatomic CuZr alloy using a transmission
55 electron microscopy (TEM).

56 2. Materials and Methods

57 Equiatomic CuZr alloy was prepared from pure copper (99.99%) and zirconium (99.2%) by arc
58 melting in an argon atmosphere. The ingot was remelted for eight times. The samples were
59 homogenized in an argon quartz tube at $850\text{ }^\circ\text{C}$ for 10 h, and annealed at $800\text{ }^\circ\text{C}$ for 1h, followed by
60 water-quenching. After that, the samples were processed to a diameter of 3 mm by ultrasound
61 machining, and DSC measurement was performed ten times using a calorimeter (NETZSCH DSC
62 3500 Sirius). The heating and cooling rates were $20\text{ }^\circ\text{C}/\text{min}$, and the ranges of measurement
63 temperature were $-100\text{ }^\circ\text{C}$ to $550\text{ }^\circ\text{C}$. The constituent phases were examined by using an X-ray
64 diffractometer (XRD, Rigaku Smart Lab) with Ni-filtered Cu $K\alpha$ radiation (combination of $K\alpha_1$ and
65 $K\alpha_2$, removing $K\beta$). For TEM studies, the samples ground to a thickness of $50\text{ }\mu\text{m}$, were dimpled
66 with a GATAN Model 656, and Ar-ion milled with a GATAN model 695 PIPSII. TEM observation
67 was carried out with a JEM- 2100 PLUS, which was operated at 200 kV.

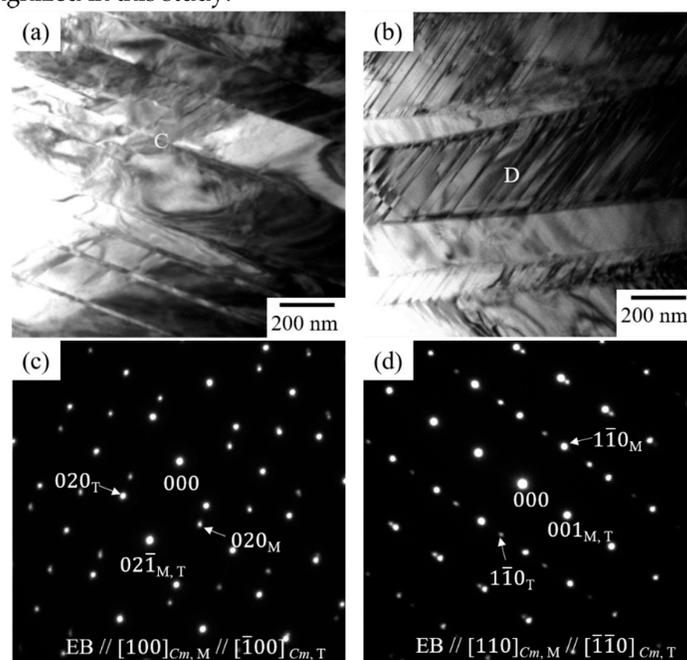
68 3. Results and Discussions

69 3.1. The crystal structure and microstructural feature of the water-quenched equiatomic CuZr alloy

70 In order to determine the lattice constants and the constituent phases in the water-quenched
71 equiatomic CuZr alloy, we performed XRD measurements. The analysis by Reference intensity ratio
72 method [13] using the results of XRD measurement showed that the volume fraction of each phase
73 in water-quenched equiatomic CuZr alloy is CuZr: 84% (Cm : 64%, $P2_1/m$: 20%), $\text{Cu}_{10}\text{Zr}_7$: 8%, CuZr_2 :
74 1%, and $\text{Cu}_2\text{Zr}_4\text{O}$: 7%. The quantitative ratio of CuZr Cm : $P2_1/m$ is about 3: 1, being almost consistent
75 with the previous research [9, 14]. In addition, the refinement of the lattice constants by Pawley
76 method [15] using the results of XRD measurement provides that the lattice constants of CuZr Cm and
77 $P2_1/m$ is $a = 0.6336\text{ nm}$, $b = 0.8589\text{ nm}$, $c = 0.5311\text{ nm}$, $\beta = 105.1\text{ }^\circ$, and $a = 0.3309\text{ nm}$, $b = 0.4209\text{ nm}$, $c =$
78 0.5253 nm , $\beta = 104.2\text{ }^\circ$. It showed good agreement with the previous study [3-5].

79 TEM observations were performed to investigate the microstructural feature and the crystal
80 structure. Figures 1(a) and (b) show the typical bright field images of the water-quenched equiatomic
81 CuZr alloy. Martensitic variants with the plate-like morphology of 250 nm in average width are
82 clearly observed in Figure 1(a). The electron diffraction pattern in Figure 1(c) taken from the
83 boundary C between martensitic variants in (a) consists of two sets of reflections from the $[100]_{Cm}$
84 zone axis that are in mirror symmetry with respect to the $(02\bar{1})_{Cm}$ plane, which is parallel to the
85 interface of alternate plates in (a). This fact indicates that those plates are in $(02\bar{1})_{Cm}$ twin relations. In
86 Figure 1(b), there were also the fine martensitic variants having the width of about 30 nm within the
87 plate-like morphology. The electron diffraction pattern in Figure 1(d) taken from the fine martensitic
88 variant boundary D in (b) consists of two sets of reflections from the $[110]_{Cm}$ zone axis that are in
89 mirror symmetry with respect to the $(001)_{Cm}$ plane, which is parallel to the interface of alternate plates
90 in (b). This indicates that those plates are in $(001)_{Cm}$ twin relations. Those $(02\bar{1})_{Cm}$ and $(001)_{Cm}$ twins
91 are defined as the Type I and compound twins, respectively [4-5, 9]. The lattice constant estimated by
92 electron diffraction patterns showed a value close to the one calculated by XRD. In the TEM

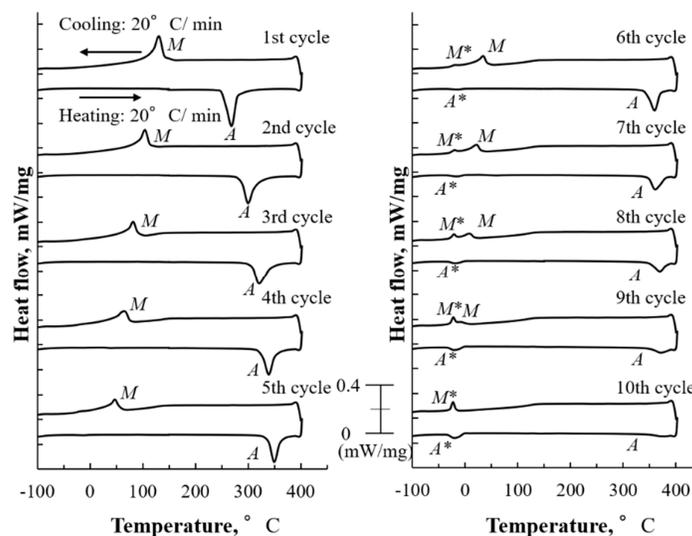
93 observation of the water-quenched equiatomic CuZr alloy, the amount of $P2_1/m$ structure was small
 94 and was not recognized in this study.



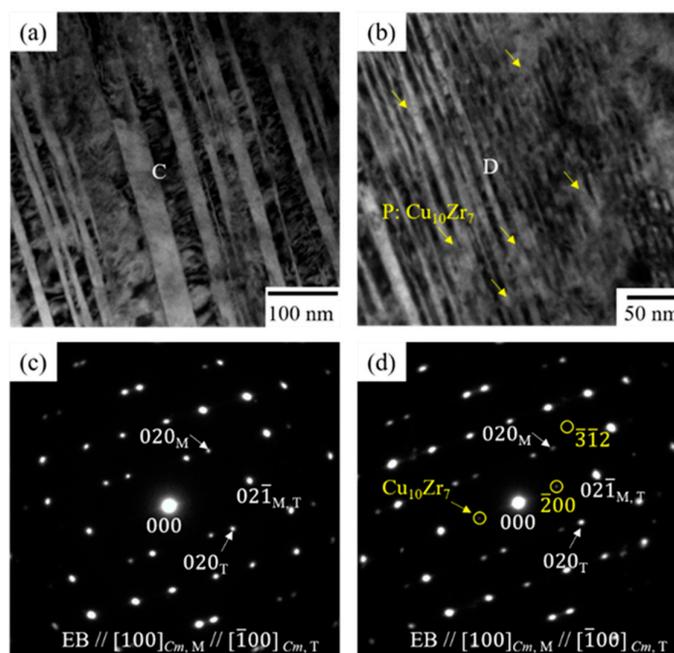
95 **Figure 1.** (a)-(b) Bright field images of water-quenched equiatomic CuZr alloy, and (c)-(d) electron
 96 diffraction patterns taken from the boundary C between martensitic variants in (a), and from the fine
 97 martensitic variants boundary D within the plate-like morphology in (b), respectively.

98 3.2. Effect of thermal cycling on the microstructure in equiatomic CuZr alloy

99 [Figure 2](#) shows the results of thermal cycling test in the water-quenched equiatomic CuZr alloy
 100 by using DSC measurement. The ranges of measurement temperature were -100 °C to 400 °C. In
 101 [Figure 2](#), there are an exothermic peak during cooling and an endothermic peak during heating.
 102 These peaks indicate that M_s and A_s are 135 °C and 261 °C in the water-quenched equiatomic CuZr
 103 alloy, which are almost the same as in the previous reports [3, 12]. As the number of cycles increase,
 104 the peaks A and M shifted toward the high and low temperature side, respectively, as shown in
 105 [Figure 2](#). Also, the areas of both peaks became smaller. At the 6th cycle in [Figure 2](#), a pair of new
 106 endothermic A^* and exothermic M^* peaks appeared that would indicate reverse transformation and
 107 normal transformation, respectively. As the number of cycles increased, the areas of the new peaks
 108 increased, and the areas of A^* and M^* in the 10th cycle were estimated to be -3.01 J/g, and 2.01 J/g,
 109 respectively. In the previous study [12], the new peaks appeared at the 4th cycle, and the areas of
 110 both peaks A^* and M^* were 3.5 J/g, resulting in slightly different from this study. This should be due
 111 to slight differences in the ranges of measured temperature and rates; previous study: -100 to 450 °C,
 112 10 °C/min, present study: -100 to 400 °C, 20 °C/min. There was no significant difference compared
 113 with a shift of the peaks A and M , and the appearance of new peaks A^* and M^* due to the thermal
 114 cycling in the previous study.



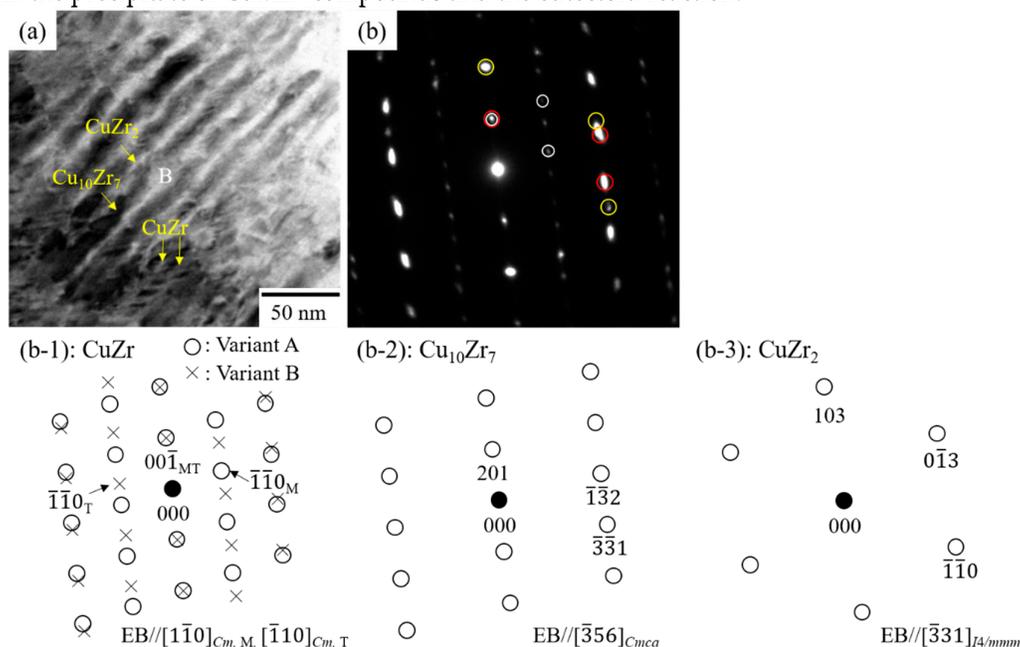
115 **Figure 2.** DSC cooling and heating curves of water-quenched equiatomic CuZr alloy from the first to
 116 10th thermal cycles. (Measured max temperature: 400 °C)



117
 118 **Figure 3.** (a)-(b) Bright field images of 10th cycled equiatomic CuZr alloy, and (c)-(d) electron
 119 diffraction patterns taken from the boundary between martensitic variants in (a) and (b).

120 [Figure 3](#) and [Figure 4](#) show the TEM observation results of the 10th cycled equiatomic CuZr
 121 alloy. In the bright field image of [Figure 3\(a\)](#), many narrow variants with 7- 40 nm in width are
 122 observed. The electron diffraction pattern in [Figure 3\(c\)](#) taken from the boundary C between
 123 martensitic variants in [\(a\)](#) indicates $(02\bar{1})_{Cm}$ type I twins along the $[100]_{Cm}$ zone axis. A large number
 124 of hazy contrasts crossing those variants exist in addition to fine elongated variants in the width of
 125 about 7 nm, as indicated by the yellow arrows in [Figure 3\(b\)](#). The electron diffraction patterns in
 126 [Figure 3\(d\)](#) taken from the area D in [\(b\)](#) indicated another spots combined with ones of $(02\bar{1})_{Cm}$ type
 127 I twins along the $[100]_{Cm}$ zone axis. This corresponds to the diffraction spots taken along $[021]_{Cmca}$
 128 direction of $Cu_{10}Zr_7$ compound, meaning the presence of $Cu_{10}Zr_7$ precipitates. The lattice constant of
 129 $Cu_{10}Zr_7$ shows good agreement with the values described in the reference [\[16-17\]](#): space group: $Cmca$,

130 lattice constant: $a = 1.269$ nm, $b = 0.9314$ nm, $c = 0.9347$ nm. Subsequently, the bright field image of
 131 another region in [Figure 4\(a\)](#) shows the complex contrasts; the lamellar structure with black and
 132 white contrasts and almost horizontal linear contrasts indicated by the arrows. The electron
 133 diffraction pattern of [Figure 4\(b\)](#) taken from the area B in [Figure 4\(a\)](#) consists of four sets of reflections.
 134 A pair of reflections indicated by the white circles of [Figure 4\(b\)](#) is composed of a pattern of $(001)_{Cm}$
 135 compound twins along the $[1\bar{1}0]_{Cm}$ zone axis in CuZr martensite, as shown in [Figure 4\(b-1\)](#). The
 136 remaining diffraction patterns indicated by the red and yellow circles of [Figure 4\(b\)](#) correspond to
 137 the patterns along the $[\bar{3}56]_{Cmca}$ direction of $Cu_{10}Zr_7$ and $[\bar{3}31]_{I4/mmm}$ along the CuZr₂ compounds (space
 138 group: $I4/mmm$, lattice constant: $a = 0.3220$ nm, $b = 0.3220$ nm, $c = 1.118$ nm [18-19]), as shown in [Figures](#)
 139 [4\(b-2\)](#) and [\(b-3\)](#), respectively. Based on the diffraction intensity of each phase and contrasts using the
 140 dark-field imaging, the lamellar structure with black and white contrasts indicates the $Cu_{10}Zr_7$ and
 141 CuZr₂ phases, and almost horizontal linear contrasts indicate the CuZr martensite. This lamellar
 142 structure is considered that CuZr matrix was occurred eutectoid decomposition into $Cu_{10}Zr_7$ and
 143 CuZr₂ phases on the basis of binary Cu-Zr phase diagram [20]. This supports that thermal cycling
 144 causes the precipitate of $Cu_{10}Zr_7$ compounds and the eutectoid reaction. Therefore, a shift of the peaks
 145 A and M toward the high and low temperature side according to the thermal cycling is originated
 146 from the precipitate of $Cu_{10}Zr_7$ compounds and the eutectoid reaction.



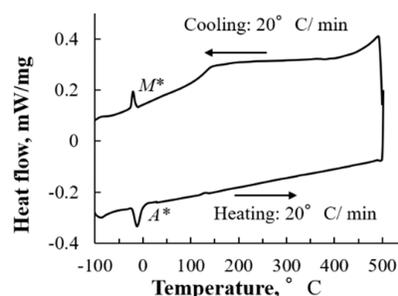
147 **Figure 4.** (a) Bright field images of 10th cycled equiatomic CuZr alloy, (b) electron diffraction patterns
 148 taken from the (a), and (b-1)-(b-3) schematic of electron diffraction patterns in (c).

149 3.3. The martensitic transformation behavior in equiatomic CuZr alloy subjected to thermal cycling

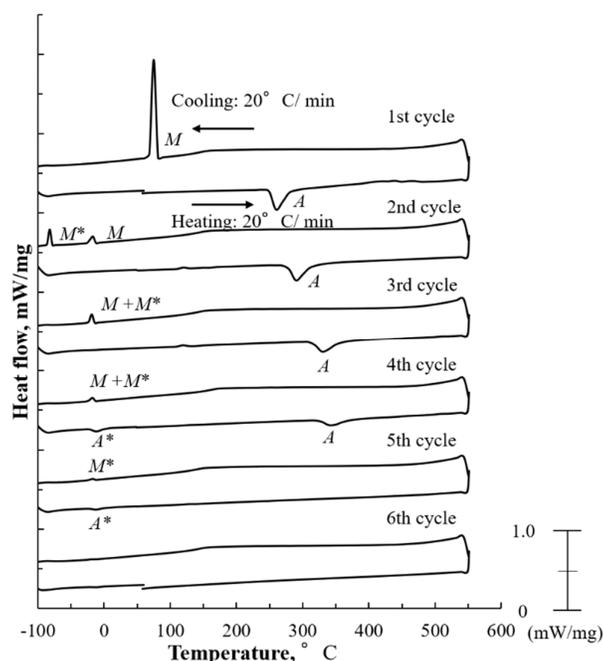
150 The effects of new peaks A^* and M^* on the microstructural feature and crystal structure were
 151 investigated. First, a thermal cycling test was performed on the 10th cycled equiatomic CuZr alloy
 152 according to the following procedure by DSC measurement; R. T. \rightarrow -100 °C \rightarrow R. T. As a result,
 153 the transformation of M^* to A^* similar to the 10th cycle in [Figure 2](#) was confirmed, and it was found
 154 that there was at least no relationship between the new peaks M^* and M which shows from the B2
 155 matrix (space group: $Pm\bar{3}m$) to the two martensitic phases (space group: $P2_1/m$ and Cm). From this, it
 156 is considered that the peak M^* is generated by the transformation from the martensitic phases with
 157 Cm and $P2_1/m$ structure. Firstly, in order to confirm whether Cm structure is transformed by new
 158 peak M^* , in-situ cooling TEM observation was performed at the regions which combined with both
 159 the precipitates and martensitic structure or existed only martensitic structure. As a result, it was
 160 found that there was no difference between the observation at room temperature and -150 °C

161 meaning that the region having the Cm structure was not transformed. From these results, although it
 162 has become clear that the precipitates affects the transformation behavior, the new phase can not be
 163 clearly distinguished by the mixture with the precipitate. Therefore, by changing the temperature
 164 range of the thermal cycling test by DSC measurement, the amount of precipitates is increased, and
 165 we tried to make the microstructure where precipitates and martensite phase were mixed become
 166 perfect eutectoid structure.

167 [Figure 5](#) shows the DSC curves of 10th cycled equiatomic CuZr alloy with the ranges of
 168 measurement temperature were $-100\text{ }^{\circ}\text{C}$ to $500\text{ }^{\circ}\text{C}$. It is apparent that peak A and M disappears
 169 completely, new peak A^* and M^* are existed around $-20\text{ }^{\circ}\text{C}$. Furthermore, [Figure 6](#) shows the DSC
 170 curves until 6th thermal cycles. It is noted that a new peak corresponding to M^* appeared at 2nd
 171 cycle, followed by the combination with the peak M at the 3rd cycle, and then those peaks
 172 disappeared at the 6th cycle. These results supports that martensitic transformation related to each
 173 peak A , M , A^* and M^* are finally inhibited as eutectoid reaction due to thermal cycling proceeds. That
 174 is, the remaining martensite with Cm and $P2_1/m$ structure except for the precipitated and lamellared
 175 regions formed by thermal cycling is considered to be closely associated with the new peak A^* and
 176 M^* . And it was found that the new peak of M^* were kept to around $-20\text{ }^{\circ}\text{C}$ due to the formation of
 177 precipitates accompanying the thermal cycling test.

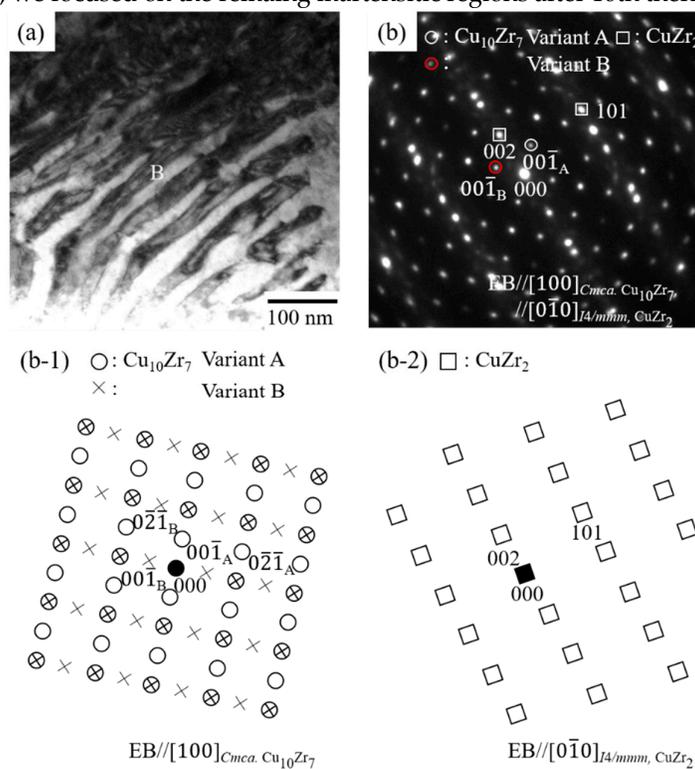


178 **Figure 5.** DSC cooling and heating curves of 10th cycled equiatomic CuZr alloy with maximum
 179 temperature $500\text{ }^{\circ}\text{C}$.

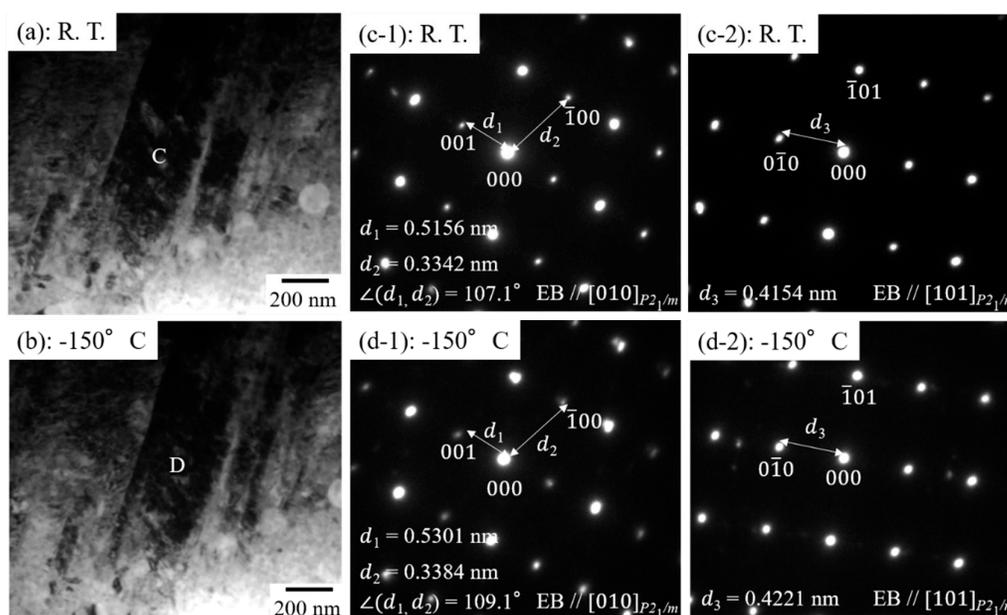


180 **Figure 6.** DSC cooling and heating curves of water-quenched equiatomic CuZr alloy from the first to
 181 6th thermal cycles (Measured max temperature: $550\text{ }^{\circ}\text{C}$).

182 In order to investigate the effect of the thermal cycling test shown in [Figure 5](#) and [Figure 6](#) on
 183 the structure, TEM observation was performed. As a result, there were the structures where eutectoid
 184 decomposition of CuZr phase proceeded and did not. [Figure 7](#) and [Figure 8](#) show the results of TEM
 185 observation after 10 thermal cycling tests in equiatomic CuZr alloy by DSC measurement at a
 186 maximum temperature of 500 °C. In the bright-field images in [Figure 7\(a\)](#) and [Figure 8\(a\)](#), the only
 187 lamellar structure and the only martensitic structure were observed, respectively. The electron
 188 diffraction pattern in [Figure 7\(b\)](#) taken from the lamellar structure in (a) consists of three sets of
 189 reflections. Two sets of reflection shown in [Figure 7\(b-1\)](#) indicates the patterns stemming from two
 190 variants along the $[100]_{Cmca}$ zone axis in $Cu_{10}Zr_7$ phase. The remaining pattern is composed of the
 191 diffraction pattern from the $[0\bar{1}0]_{I4/mmm}$ zone axis in $CuZr_2$, as shown in [Figure 7\(b-2\)](#). The orientation
 192 relationship between $Cu_{10}Zr_7$ and $CuZr_2$ was $[100]_{Cmca} // [010]_{I4/mmm}$; $(011)_{Cmca} // (001)_{I4/mmm}$. In-situ
 193 cooling TEM observation was performed in this fully lamellared structure, providing that no
 194 microstructural change were observed by cooling to -150 °C below peak M^* as expected. In addition,
 195 TEM observation after the thermal cycling test in [Figure 6](#) shows that the eutectoid structure is totally
 196 formed. Therefore, we focused on the remaining martensitic regions after 10th thermal cycling.



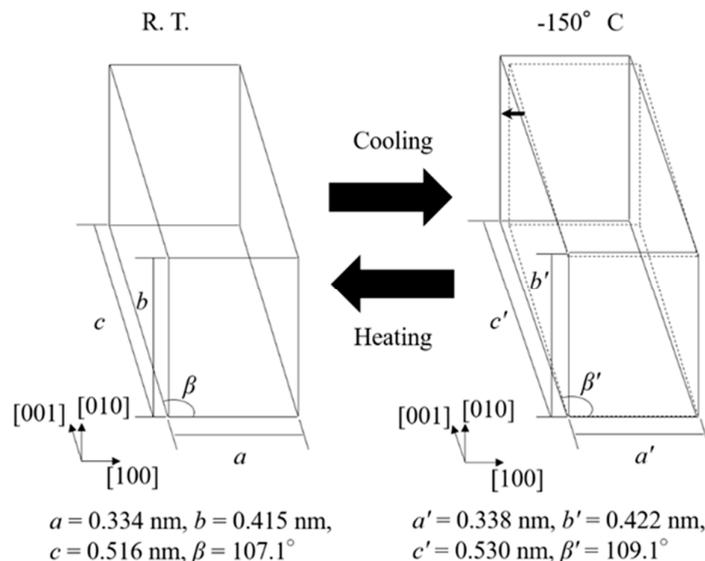
197 **Figure 7.** (a) Bright field image of 10th cycled equiatomic CuZr alloy, (b) electron diffraction pattern
 198 taken from the (a), and (b-1)-(b-2) schematic of electron diffraction patterns in (b). (The measured
 199 maximum temperature at DSC measurement is 500 °C.)



200 **Figure 8.** (a)-(b) Bright field images of 10th cycled equiatomic CuZr alloy at R. T., and -150°C, and (c-
 201 1, 2)-(d-1, 2) electron diffraction patterns taken from the martensitic variants C in (a), and D in (b),
 202 respectively. (The measured maximum temperature at DSC measurement is 500 °C.)

203 **Figure 8** shows the TEM images of in-situ cooling observation from room temperature to -150
 204 °C. The electron diffraction patterns in **Figures 8(c-1)** and **(c-2)** taken from the martensitic variant in **(a)**
 205 indicated the $[010]_{P21/m}$ and $[101]_{P21/m}$ zone axes in CuZr. The lattice constants of $P21/m$ in 10th thermal
 206 cycled specimen are estimated as $a = 0.334$ nm, $b = 0.415$ nm, $c = 0.516$ nm, $\beta = 107.1^\circ$ from electron
 207 diffraction patterns. Compared with those of the water-quenched specimen, which are $a = 0.331$ nm,
 208 $b = 0.421$ nm, $c = 0.525$ nm, $\beta = 104.2^\circ$, these values are a little difference. This should be due to the
 209 difference in the alloy composition of matrix accompanying eutectoid decomposition by thermal
 210 cycling test. **Figure 8(b)** shows the bright field image in the same location as **(a)** in the specimen cooled
 211 until -150 °C. No change of morphology of martensitic variant was observed between R. T. and -150
 212 °C. However, it is noted that d values and angle between planes shown in **Figures 8(d-1)** and **(d-2)**
 213 are much different from those of **Figures 8(c-1)** and **(c-2)**. Based on the electron diffraction patterns
 214 taken from another martensitic variant at -150 °C, the lattice constants of martensite at -150 °C are a'
 215 $= 0.338$ nm, $b' = 0.422$ nm, $c' = 0.530$ nm, $\beta' = 109.1^\circ$. Comparing the change of the lattice constant at
 216 room temperature and -150 °C, the results are $a' = a + 0.004$ nm, $b' = b + 0.007$ nm, $c' = c + 0.014$ nm, β'
 217 $= \beta + 2.0^\circ$. These results indicate that c -axis and β angle move largely, and a - and b - axes hardly move.
 218 **Figure 9** shows the schematic illustration of unit cell showing change of the lattice constant
 219 accompanying with heating and cooling. Usually, the metals are known to shrink during cooling.
 220 However, the change of the lattice constant obtained from present in-situ cooling observation was
 221 not shrinking but expanding of unit cell. From above results, the change of the lattice constant due to
 222 cooling is associated with the new peak M^* , that is, new martensitic transformation around -20 °C.
 223 From the change of the lattice constant, it is clear that the c -axis and β angle largely moved compared
 224 to a - and b -axes through the new martensitic transformation, and it is predicted that the atoms existed
 225 in the $(110)_{B2}$ plane in $B2$ parent phase have moved further, as indicated by the arrows of the
 226 schematic diagram at -150 °C in **Figure 9**. Ti-Ni and Ti-Pt alloys [21-22] which is one of shape memory
 227 alloys have the shear-shuffling mechanism of $(110) [1\bar{1}0]_{B2}$ in general, supporting that this new
 228 martensitic transformation is caused by the further movement of the $(110)_{B2}$ plane in $B2$ parent phase;
 229 that is, the significant change of c -axis and β angle. Furthermore, small transformation strain
 230 evaluated from the change of lattice constants seen in **Figure 9** provides the small thermal hysteresis
 231 of the new peaks M^* and A^* , leading to the no change of morphology in the whole variants compared

232 with Figures 8 (a) and (b). This new martensitic transformation at low temperature is considered to
 233 be closely related to the strain and stress caused by thermal cycling. During this new martensitic
 234 transformation, the $P2_1/m$ structure was transformed instead of the Cm structure. Concerning the
 235 crystal structure of new martensite at low temperature, $P2$ or $P2_1$ which is a subgroup of $P2_1/m$ is
 236 mentioned as an option of the space group. Otherwise, it might indicate a tendency to further
 237 transformation from the $P2_1/m$ structure to Cm structure by strain and stress due to thermal cycling.



238 **Figure 9.** The change of lattice constant in the martensitic phase (R. T.) to the new phase (-150 °C) of
 239 10th cycled CuZr alloy.

240 4. Conclusions

241 In this study, we investigated the microstructure and martensitic transformation behavior in
 242 thermal cycled equiatomic CuZr shape memory alloy using TEM. The obtained results are
 243 summarized as follows.

- 244 (1) In the 10th cycled equiatomic CuZr alloy (the temperature range of DSC measurement: -100 °C
 245 to 400 °C), three structures were observed by TEM; I: the martensitic variant, II: the structure in
 246 which $\text{Cu}_{10}\text{Zr}_7$ precipitates exist inside the martensitic variant, III: the structure in which the
 247 lamellar consisting of $\text{Cu}_{10}\text{Zr}_7$ and CuZr_2 phases and martensitic variants are mixed. TEM
 248 observation of the 10th cycled equiatomic CuZr alloy (the temperature range of DSC
 249 measurement: -100 °C to 500 °C) showed two structures; I: the martensitic variant, II: the lamellar
 250 structure in which the CuZr martensitic phase was completely eutectoid transformed. This fact
 251 indicated that the eutectoid decomposition occurred in equiatomic CuZr alloy during the thermal
 252 cycling.
- 253 (2) When the martensitic variant having $P2_1/m$ (lattice constant: $a = 0.334 \text{ nm}, b = 0.415 \text{ nm}, c = 0.516$
 254 $\text{nm}, \beta = 107.1^\circ$) of 10th cycled equiatomic CuZr alloy was cooled from room temperature to -
 255 150 °C, the change in the crystal structure corresponding to the new peak M^* occurred, and the
 256 lattice constant was $a' = 0.338 \text{ nm}, b' = 0.422 \text{ nm}, c' = 0.530 \text{ nm}, \beta' = 109.1^\circ$. This new martensitic
 257 transformation at low temperature is considered to be closely related to the strain and stress
 258 caused by thermal cycling.

259 **Author Contributions:** S. Hisada, M. Matsuda, and M. Nishida conceived and designed the experiments; S.
 260 Hisada and M. Matsuda performed the experiments, analyzed the data, wrote original draft preparation; M.
 261 Nishida, C. A. Biffi, and A. Tuissi wrote review and editing.

262 **Conflicts of Interest:** The authors declare no conflict of interest.

263

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