

1 Article

2 Modeling dislocation contrasts obtained by 3 accurate-Electron Channeling Contrast Imaging for 4 characterizing deformation mechanisms in bulk 5 materials

6 Hana KRIAA ¹, Antoine GUITTON ^{1,2} and Nabila MALOUFI ^{1,2,*}

7 ¹ Université de Lorraine - CNRS - Arts et Métiers ParisTech – LEM3, 7 rue Félix Savart, 57070 Metz, France;
8 hana.kriaa@univ-lorraine.fr (H.K.); antoine.guitton@univ-lorraine.fr (A.G.); nabila.maloufi@univ-lorraine.fr
9 (N.M.)

10 ² Laboratory of Excellence on Design of Alloy Metals for low-mAss Structures (DAMAS) – Université de
11 Lorraine, 57073 Metz, France.

12 * Correspondence: nabila.maloufi@univ-lorraine.fr; Tel.: +33 372 747 865

13 Received: date; Accepted: date; Published: date

14 **Abstract:** Electron Channeling Contrast Imaging (ECCI) is becoming a powerful tool in Materials
15 Science for characterizing deformation defects. Dislocations observed by ECCI in Scanning
16 Electron Microscope, exhibit several features depending on the crystal orientation relative to the
17 incident beam (white/black line on a dark/bright background). In order to bring new insights
18 concerning these contrasts, we report an original theoretical approach based on the dynamical
19 diffraction theory. Our calculations led, for the first time, to an explicit formulation of the
20 backscattered intensity as a function of various physical and practical parameters governing the
21 experiment. Intensity profiles are modeled for dislocations parallel to the sample surface for
22 different channeling conditions. All theoretical predictions are consistent with experimental
23 results.

24 **Keywords:** ECCI, dislocation contrast, modeled intensity profiles, invisibility criteria, dynamical
25 theory of electron diffraction.
26

27 1. Introduction

28 The Electron Channeling Contrast Imaging (ECCI) technique is based on the fact that the
29 BackScattered Electrons (BSE) signal is highly dependent on the orientation of the incident beam
30 relative to the lattice planes [1]. Therefore, any slight local distortion of the crystal lattice, produced
31 for instance by a dislocation, leads to a BSE intensity (I_{BSE}) modulation, thus generating several
32 contrasts such as a bright line on a dark background [2] or a black line on a bright background [3].
33 For understanding the origin of the dislocation contrasts obtained by ECCI, the two-beam dynamical
34 diffraction theory was adapted from the Transmission Electron Microscopy (TEM) [4] [5]. Briefly, the
35 electron beams are described, inside the crystal, by a superposition of Bloch waves. The different
36 inelastic scattering events are divided into two categories: those scattered through angles less than
37 90° (forming the forward scattering wave) and those scattered through angles greater than 90°
38 (forming the backscattered wave) [6]. In the multiple scattering model electrons can be removed
39 from the forward scattering wave to the backscattered one and vice-versa. In order to simulate the
40 I_{BSE} profiles for both perfect and imperfect crystal, Spencer *et al.* [7] and Wilkinson *et al.* [6, 8, 9] used
41 this Bloch wave-based model. They showed that for the perfect crystal, the simulated profiles exhibit

42 the main experimental features of the channeling pattern: bright band and dark edges. The same
 43 approach was also used by Reimer [10, 11] for a perfect crystal where the multiple scatterings are
 44 treated as incoherent. These different approaches, were extended to the case of an imperfect crystal
 45 containing a dislocation [6-9] or a stacking fault [12]. Despite their contribution to the theory of
 46 defects electron channeling contrasts [7-12], detailed calculations leading to an analytical expression
 47 of BSE signal as a function of experimental parameters, is still missing. Furthermore, in most cases
 48 [7,8] theoretical results were not compared to the experiments. This can be illustrated from the
 49 dislocation profiles calculated for Bragg condition, which exhibit an extra-pic of I_{BSE} not observed
 50 experimentally [7, 8].

51 To deepen our understanding of the observed channeling contrast of dislocations, we propose an
 52 easier way to model the I_{BSE} as a function of physical parameters either relative to the material or
 53 governing the ECCI experiment. Our theoretical results show a good agreement with the
 54 experiments for several diffraction conditions.

55 In a crystal, the electronic wave function is a solution of the time independent Schrödinger's
 56 equation and is given by [11]:

$$57 \quad \Psi(\mathbf{r}) = \sum_j \varepsilon^{(j)} \sum_g C_g^{(j)} e^{[2\pi i (\mathbf{k}_0^{(j)} + \mathbf{g}) \cdot \mathbf{r}]} e^{[-2\pi q^{(j)} z]} \quad (1)$$

58 The index j refers to the j th wave, $\varepsilon^{(j)}$ are the excitation amplitudes of the Bloch wave $\psi^{(j)}$, $C_g^{(j)}$ are
 59 the amplitudes of the diffracted waves with a wave vector $\mathbf{k}_g^{(j)} = \mathbf{k}_0^{(j)} + \mathbf{g}$, where $\mathbf{k}_0^{(j)}$ is the wave vector
 60 of the j th primary wave and \mathbf{g} is the diffraction vector. \mathbf{r} is the spatial position vector at which the
 61 electron intensity is evaluated. The second factor of equation (1) contains the absorption parameter
 62 $q^{(j)}$ expressing the exponential attenuation of the wave amplitude with increasing depth z .
 63

64 In order to determine the different coefficients of the Bloch wave function, presented in equation (1),
 65 Reimer used the two-beam condition *i.e.* only one set of lattice planes is in channeling condition.
 66 Hence, the total BSE signal of a slice of a thickness dz , located at a depth z is given by [11]:

$$67 \quad \frac{d\eta}{dz} = N\sigma_B \{ \psi\psi^* + (1 - \sum_j |C_0^{(j)}|^2 e^{[-4\pi q^{(j)} z]}) \} \quad (2)$$

68 N is the atom number per unit of volume, σ_B is the backscattering cross-section through angles
 69 larger than 90° and $\psi\psi^*$ is the probability for the Bloch wave to be backscattered at a depth z . The
 70 last terms (in parentheses) in equation (2) describe the electrons that are removed from the Bloch
 71 wave field by scattering before reaching the slice dz .
 72

73 The BSE coefficient $\eta_{0.c.}$ is, then, obtained from the integration of equation (2) in the total interaction
 74 depth from $z=0$ to $z \rightarrow \infty$ (labelled $\Delta\eta$ in Reimer's model). O.C. indicates that only the total BSE
 75 intensity due to orientation contrast is calculated, while the contributions due to atomic number and
 76 to the surface inclination are not considered [11]:

$$77 \quad \eta_{0.c.} = \frac{N\sigma_B}{4\pi} \xi_0' \left(- \frac{s \xi_g + \frac{\xi_0}{\xi_g}}{1 + (s \xi_g)^2 - \left(\frac{\xi_0}{\xi_g}\right)^2} + \frac{s \xi_g}{1 + (s \xi_g)^2 + [(1 + (s \xi_g)^2) \left(\frac{\xi_0}{\xi_g}\right)]^2} \right) \quad (3)^*$$

78 Equation (3) corresponds to the variation of the BSE intensity for a perfect crystal i.e. the intensity
 79 profile of an isolated pseudo-Kikuchi band [7,11,13], where ξ'_0 and ξ'_g are the absorption lengths,
 80 ξ_g is the extinction distance and s the deviation parameter.

81

82 2. Our theoretical approach for BSE intensity calculation for an imperfect crystal

83 If we consider a column located at a position x away from a dislocation, at position $x=0$ and depth
 84 $z=z_D$ (where z_D is the mean depth of the dislocation), the distortion of the lattice planes near the
 85 dislocation does not depend on z but only on x and it is given by $\left(\frac{\partial \mathbf{R}}{\partial z}\right)_{z=z_D}$ (\mathbf{R} is the displacement field
 86 of the crystalline planes) [14].

87 Therefore, for calculating the I_{BSE} in the case of an imperfect crystal containing a dislocation parallel
 88 to the sample surface, independently of the depth z , we take into account a new deviation parameter
 89 s' written by:

$$90 \quad s' = s + s_D \quad \text{where} \quad s_D = \mathbf{g} \cdot \left(\frac{\partial \mathbf{R}}{\partial z}\right)_{z=z_D} \quad (4)$$

91 s is the deviation from the exact Bragg position in the perfect crystal, which can be experimentally
 92 measured [3]. The scalar product $\mathbf{g} \cdot \left(\frac{\partial \mathbf{R}}{\partial z}\right)_{z=z_D}$ represents the supplementary deviation, s_D due to the
 93 variation of the incidence angle between the primary beam and the distorted crystalline planes near
 94 the dislocation core. Far from the dislocation, the crystal is considered perfect. The planes are not
 95 distorted and the deviation s_D becomes zero. Consequently, to take into account the presence of the
 96 defect, we substitute s by s' in the expression of $\eta_{0.c.}$ for a perfect crystal (in equation 3, which does
 97 not depend on z). We obtain:

$$98 \quad \eta_{0.c.} = \frac{N\sigma_B}{4\pi} \xi'_0 \left(- \frac{(s+s_D(x)_{z=z_D}) \xi'_g + \frac{\xi'_0}{\xi_g}}{1 + ((s+s_D(x)_{z=z_D}) \xi'_g)^2 - \left(\frac{\xi'_0}{\xi_g}\right)^2} + \frac{(s+s_D(x)_{z=z_D}) \xi_g}{1 + ((s+s_D(x)_{z=z_D}) \xi_g)^2 + [1 + ((s+s_D(x)_{z=z_D}) \xi_g)^2 \left(\frac{\xi'_0}{\xi_g}\right)^2]} \right) \quad (5)$$

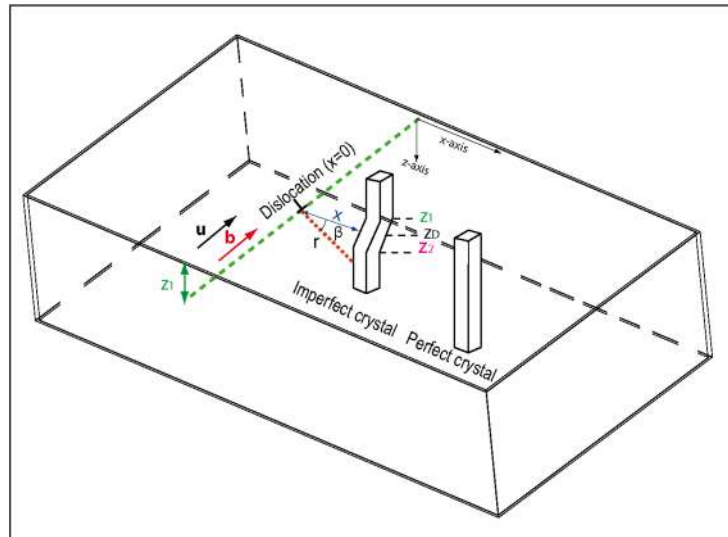
99 This allows us to study the variation of the I_{BSE} as a function of x (distance x away from the
 100 dislocation core). Where, the contrast associated to a dislocation is described by s_D (containing all
 101 the effect of \mathbf{R}).

102 2.1. Screw dislocation

103 Figure 1 shows a screw dislocation parallel to the surface of a bulk sample and located at a depth z_D .
 104 This defect is characterized by a Burgers vector \mathbf{b} and a line direction \mathbf{u} . At a distance x away from
 105 the dislocation core (in $x=0$), the crystal plane is deformed. The displacement field $\mathbf{R}_{\text{screw}}$ is then
 106 defined in polar coordinate (β) as follows [15]:

$$107 \quad \mathbf{R}_{\text{screw}} = \frac{\mathbf{b} \beta}{2\pi} = \frac{\mathbf{b}}{2\pi} \tan^{-1} \left(\frac{z-z_D}{x} \right) \quad (6)$$

108



109

110 **Figure 1.** Schematic of a screw dislocation parallel to the surface and located at a depth z_D . Deformed planes,
 111 perpendicular to the surface, are at a distance x away from the dislocation core.

112

113 The derivative of R_{screw} with respect to the depth z , at a turning point ($z = z_D$), is given by:

$$114 \frac{dR_{\text{screw}}}{dz} \Big|_{z=z_D} = \frac{b}{2\pi x \left(1 + \left(\frac{z-z_D}{x}\right)^2\right)} = \frac{b}{2\pi x} \quad (7)$$

115 Based on this reasoning, the substitution of equation (7) in equation (5) allows us to obtain the
 116 following expression of $\eta_{\text{o.c.}}$:

$$117 \eta_{\text{o.c.}} = \frac{N_{\text{OB}}}{4\pi} \xi_0' \left(- \frac{\left(s + \frac{\mathbf{g} \cdot \mathbf{b}}{2\pi x}\right) \xi_g + \frac{\xi_0'}{\xi_g}}{1 + \left(\left(s + \frac{\mathbf{g} \cdot \mathbf{b}}{2\pi x}\right) \xi_g\right)^2 + \left(\frac{\xi_0'}{\xi_g}\right)^2} + \frac{\left(s + \frac{\mathbf{g} \cdot \mathbf{b}}{2\pi x}\right) \xi_g}{1 + \left(\left(s + \frac{\mathbf{g} \cdot \mathbf{b}}{2\pi x}\right) \xi_g\right)^2 + \left[1 + \left(s + \frac{\mathbf{g} \cdot \mathbf{b}}{2\pi x}\right) \xi_g\right]^2 \left(\frac{\xi_0'}{\xi_g}\right)^2} \right) \quad (8)$$

118 Equation (8) gives the variation of the BSE signal as a function of the distance x and the experimental
 119 parameters such as the deviation s and the diffraction vector \mathbf{g} .

120 It should be noted that in this paper, we show profiles modeled in the case of aluminum, where the
 121 parameters are: acceleration voltage $E=20$ kV, $\mathbf{g} = (220)$, the extinction distance $\xi_g=50$ nm, absorption

122 lengths $\xi_0'=140$ nm and $\xi_g'=600$ nm [11]. It should also be mentioned that in all modeled profiles the

123 background level is taken as reference (at the zero of the ordinate axis). All negative values then
 124 correspond to lower BSE intensities than the background level.

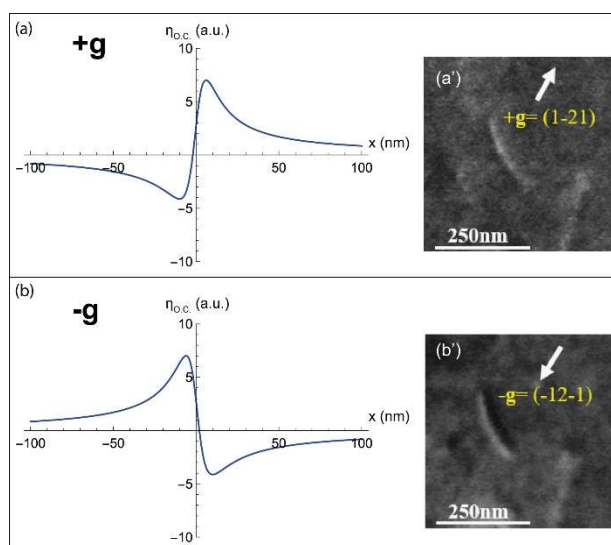
125 2.1.1. Deviation parameter $s=0$

126 The theoretical intensity profiles calculated from equation (8), in the case of a screw dislocation, for
 127 the diffraction conditions $s=0$ and $\pm\mathbf{g}$ are represented in Figure 2. Their corresponding
 128 experimental ECC micrographs are also shown (Figures 2a' and b'). The \mathbf{g} and \mathbf{s} vectors are,
 129 respectively, determined experimentally through the pseudo-band indexation of the HR-SACP
 130 (High Resolution Selected Area Channeling Pattern) assisted by EBSD experiment [2, 3].

131

132 For both $+\mathbf{g}$ and $-\mathbf{g}$ diffractions, the dislocation profiles (Figures 2.a and b) are anti-symmetric: a
 133 hollow and a peak corresponding to the black and white sides of the dislocation respectively

134 (Figures 2a' and b'). Moreover, in the case of $-g$, the extrema are inverted compared to those
 135 observed for $+g$: the peak becomes hollow and vice versa.



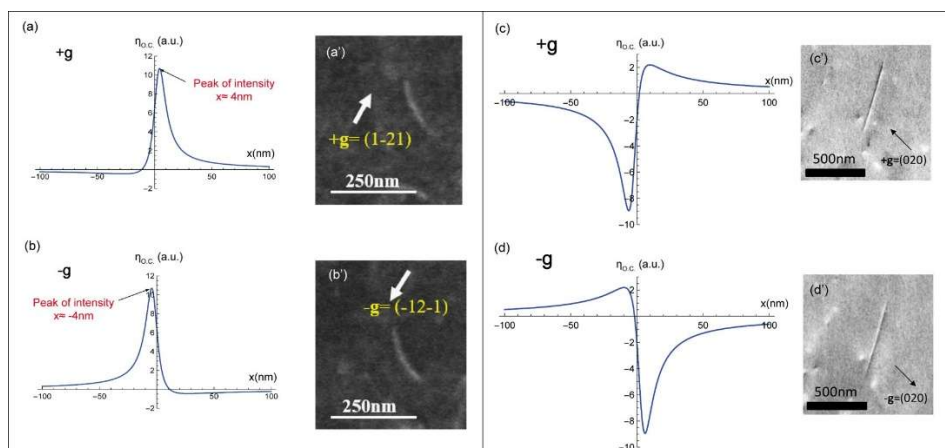
136

137 **Figure 2.** I_{BSE} profiles modeled, for a screw dislocation parallel to the surface, with a deviation parameter $s=0$
 138 for the diffractions (a) $+g$ and (b) $-g$ with their corresponding experimental ECC micrographs (a') and (b').
 139

140 Such theoretical results reveal that at Bragg position, a screw dislocation generates a BSE image with
 141 black/white sides, which reverse with the inversion of the sign of g . Therefore, the variation of I_{BSE}
 142 given by equation (8) is in good agreement with the experimental observations already reported in
 143 literature [3,7].
 144

145 2.1.2. Deviation parameter $s>0$

146 The I_{BSE} profiles calculated by equation (8) with a deviation parameter slightly positive ($s=0.01 \text{ nm}^{-1}$)
 147 are represented in Figures 3a and b for the $+g$ and $-g$ diffractions respectively. In this condition
 148 ($s>0$), both $\pm g$ dislocation profiles present one intensity peak only. This is in agreement with the
 149 experimental ECC micrographs shown in Figures 3a' and b': bright line on dark background. Note
 150 also that the maximum intensity does not coincide with the exact position of the dislocation core
 151 ($x=0 \text{ nm}$) but it is at $x \approx \pm 4 \text{ nm}$: it is displaced from one side of the dislocation position to the other
 152 side when changing from $+g$ to $-g$. This result is analogous to that obtained in TEM and can be
 153 used to characterize a dislocation configuration consisting of two parallel dislocations such as dipole
 154 [3, 16].
 155

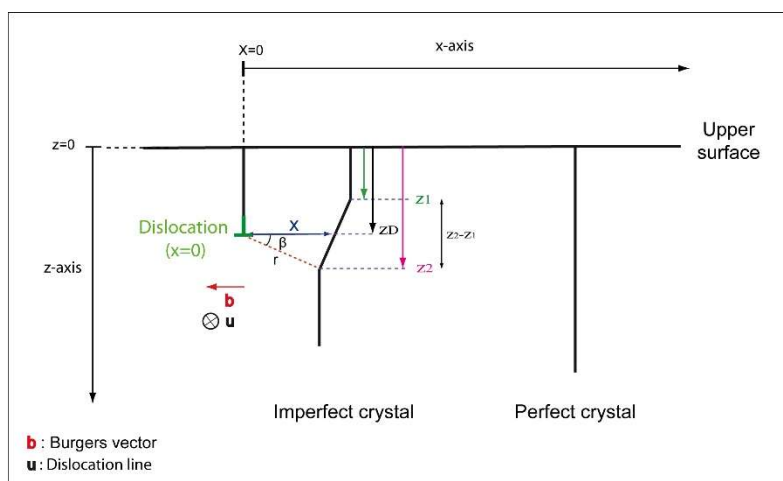


156
157 **Figure 3.** I_{BSE} profiles modeled, for a screw dislocation parallel to the surface, with $s>0$ and $s<0$ for (a) (c) $+g$
158 and (b) (d) $-g$ with their corresponding experimental ECC micrographs (a'), (b'), (c') and (d').

159 2.1.3. Deviation parameter $s<0$

160 The I_{BSE} profiles calculated from our theoretical model for a slightly negative deviation parameters
161 ($s=-0.01 \text{ nm}^{-1}$) and $\pm g$ diffraction conditions are represented in Figure 3c and 3d. For the diffraction
162 $+g$, the curve contains a deep hollow and a peak corresponding to the black and white dislocation
163 sides respectively (Figure 3c'). This contrast is inverted with the inversion of the sign of g (Figures
164 3d and d'). For $s<0$, the BSE signal emitted from the zone of interest is high: bright background.

165 2.2. Edge dislocation



166
167 **Figure 4.** Schematic of an edge dislocation parallel to the surface and located at a depth zD . Deformed planes,
168 perpendicular to the surface, are at a distance x away from the dislocation core.

169 Similar to the screw dislocation, an edge dislocation parallel to the surface and located at a depth zD
170 produces a local deformation of the crystalline planes nearby its core (see Figure 4). Such distortion
171 is described by its displacement field, written in polar coordinate, as follows [15]:

$$172 \mathbf{R}_{\text{edge}} = \frac{\mathbf{b}}{2\pi} \left[\beta + \frac{\sin 2\beta}{2(1-\nu)} \right] + \frac{\mathbf{b} \times \mathbf{u}}{2\pi} \left[\frac{1-2\nu}{2(1-\nu)} \ln|r| + \frac{\cos 2\beta}{4(1-\nu)} \right] \quad (9)$$

173
174 ν is the Poisson's ratio, \mathbf{u} is the dislocation line direction and r is the polar coordinate. Where β
175 and r are given by:

$$176 \quad \beta = \tan^{-1} \left(\frac{z - z_D}{x} \right) \text{ and } r = \frac{x}{\cos \beta} \quad (10)$$

177 From equations (9) and (10), R_{edge} can be expressed as a function of the distance x away from the
178 dislocation. The new deviation parameter s' is then:

$$179 \quad s' = s + \mathbf{g} \cdot \frac{dR_{\text{edge}}}{dz} \Big|_{z=z_D} \quad (11)$$

180

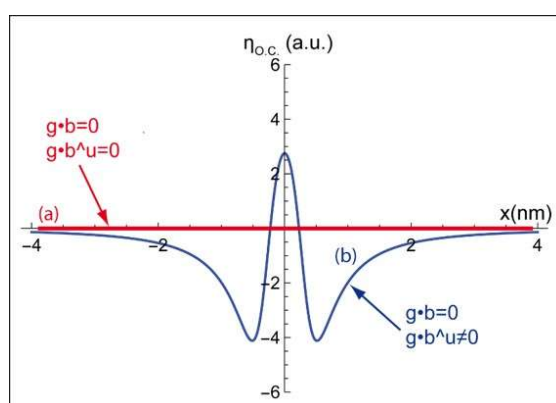
181 The presence of an edge dislocation in the crystal can also be highlighted, analytically, by the
182 insertion of equation (11) in equation (5). The calculated theoretical profiles are similar to that
183 obtained for a screw dislocation. For the diffraction $+\mathbf{g}$, at Bragg condition ($s=0$), the modeled curves
184 are characterized by a maximum and a minimum of I_{BSE} . The edge dislocation generates a
185 white/black contrast. However, for $s > 0$, the profile presents only a single peak consistent with
186 experimental observations. The maximum intensity is situated at a position $x \approx -6$ nm away from
187 the dislocation core. Concerning the case of $s < 0$, the I_{BSE} profile show a hollow with a slight peak. All
188 profiles are also reversed, following the inversion of the \mathbf{g} sign regardless of the deviation
189 parameter s .

190

191 2.3. Extinction criteria

192 Furthermore, for both screw and edge dislocations, considering the extinction criteria $\mathbf{g} \cdot \mathbf{b} = 0$ and
193 $\mathbf{g} \cdot \mathbf{b} \times \mathbf{u} = 0$ in our equation leads to a null BSE yield ($\eta_{0,c} = 0$ a.u in Figure 5a). Regarding the edge
194 dislocation, the $\mathbf{b} \times \mathbf{u}$ term in equation (9) becomes null when $z = z_D$. Nevertheless, the position of the
195 dislocation is located in the $[z_1, z_2]$ range (see Figure 1), therefore the $\mathbf{b} \times \mathbf{u}$ term is not null. For $\mathbf{g} \cdot \mathbf{b} = 0$
196 and $\mathbf{g} \cdot \mathbf{b} \times \mathbf{u} \neq 0$, in the $[z_1, z_2]$ range except z_D , the calculated profile for an edge dislocation displays a
197 low intensity peak $\eta_{0,c} \approx 2,7$ (a.u with respect to the background level) surrounded by two hollows.
198 Such residual contrast (Figure 5b) is characteristic of an edge dislocation observed by TEM under
199 these diffraction conditions [17].

200

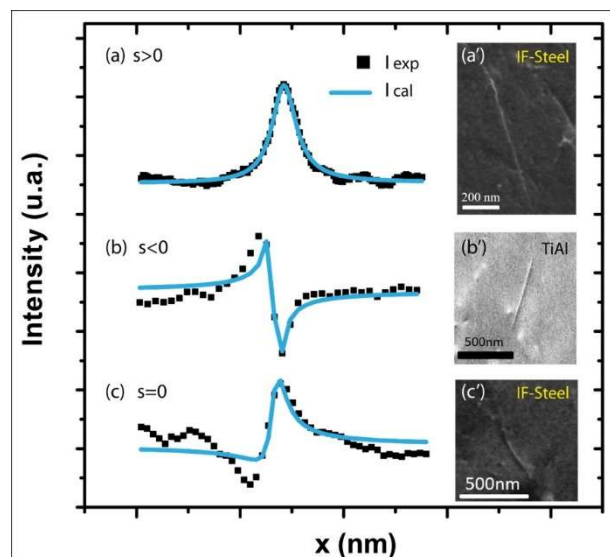


201 **Figure 5.** I_{BSE} profiles modeled for the extinction conditions: (a) $\mathbf{g} \cdot \mathbf{b} = 0$, $\mathbf{g} \cdot \mathbf{b} \times \mathbf{u} = 0$ and (b) $\mathbf{g} \cdot \mathbf{b} = 0$, $\mathbf{g} \cdot \mathbf{b} \times \mathbf{u} \neq 0$.

202

203 2.4. Quantitative comparisons with experimental profiles

204 In this part, for each deviation parameter: $s>0$, $s<0$ and $s=0$, an average profile is calculated from 50
 205 experimental dislocation profiles and fitted by equation (5). The results are illustrated by Figures 6a,
 206 b and c respectively.



207

208 **Figure 6.** Fitted (blue line) and experimental (black squares) I_{BSE} profiles and their corresponding ECC
 209 micrographs obtained for (a, a'): $\mathbf{g}=(01-1)$ and $s>0$, (b, b'): $\mathbf{g}=(020)$ and $s<0$ and (c, c'): $\mathbf{g}=(2-1-1)$ and $s=0$
 210 respectively.

211 As can be seen, the best fits are obtained for $s>0$ (the correlation coefficient $\chi^2=2$) and $s<0$ ($\chi^2=8.7$).
 212 While for $s=0$, the general features of the curve are well modeled, the correlation coefficient is higher:
 213 $\chi^2=16.4$. At Bragg condition because of the strong interaction between the electron beam and the
 214 crystal atoms [18], dynamical effects are magnified and the diffracted intensity is high enough to
 215 excite neighboring reflections. Then the successively and coherently produced beams interfere with
 216 each other. The "n" beam approach must thus be considered to better report the experimental results.
 217 Besides, in our calculations multiple scattering was treated incoherently.

218 Nevertheless, the fitted profiles provide, among other parameters, reasonable orders of magnitude
 219 of the physical parameters ξ_g , ξ'_0 and ξ'_g for different deviation parameters and materials
 220 (interstitial Free (IF)-steel: Figure 5a, a', c and c' TiAl: Figures 6b and b'). Furthermore, the obtained
 221 parameters are in good agreement with the values reported in the literature [11]. Such as the case of
 222 IF-steel: $\xi_g=9,4\pm 1,3$ nm ; $\xi'_0=170,4\pm 36,7$ nm ; $\xi'_g=177,7\pm 38,3$ nm.

223 3. Conclusions

224 In this paper an original theoretical model based on the Bloch wave approach of the dynamical
 225 diffraction theory was developed for modeling I_{BSE} around dislocations without resorting to
 226 numerical methods. An analytical formula of the BSE signal as a function of the different physical
 227 parameters governing the ECCI experiment has been proposed for the first time to our knowledge.
 228 The BSE contrast profiles, produced by screw and edge dislocations parallel to the sample surface,
 229 display the same appearance for the diffraction conditions. For a deviation parameter $s=0$ (Bragg

230 condition) and $s < 0$, the theoretical BSE curves show hollow and peak of intensity corresponding to
231 the black and white dislocation sides respectively. The inversion of \mathbf{g} leads to the profile inversion
232 (hollow becomes peak and vice versa). For $s > 0$, the bright dislocation contrast is envisaged in the
233 modeled profile by the intensity peak. This latter (dislocation image) do not coincide with the exact
234 dislocation position ($x=0$) and it is displaced to the opposite side when \mathbf{g} is reversed. Moreover, our
235 theoretical model confirms the use of the invisibility criteria in ECCI.

236 The good agreement between the theoretical and experimental results was also confirmed by
237 adjusting the BSE intensity profiles. Hence, deduced values for the physical parameters ξ_g , the
238 extinction distance and ξ'_0 and ξ'_g , the absorption lengths are consistent with the literature.

239 Because the use of ECCI is becoming widespread for the defects characterization in bulk material in
240 SEM, we provide a usable formula of the BSE intensity produced by dislocations. Furthermore, our
241 approach can be extended to other defects. ECCI is now mature for exploring new horizons in
242 Materials Science.

243
244 **Author Contributions:** All ECCI observations were performed by H.K. H.K., A.G. and N.M. performed the
245 theoretical interpretations. H.K. wrote the main manuscript text. All the authors participate in the discussion.

246 **Conflicts of Interest:** The authors declare no conflict of interest.

247 References

- 248 1. Booker, G. R.; Shaw, A. M. B.; Whelan, M. J.; Hirsch, P. B. Some comments on the interpretation of the
249 Kikuchi-like reflection patterns observed by scanning electron microscopy. *Phil. Mag.* **1967**, *16*, 1185-1191.
- 250 2. Mansour, H.; Guyon, J.; Crimp, M. A.; Gey, N.; Beausir, B.; Maloufi, N. Accurate electron channeling
251 contrast analysis of dislocations in fine grained bulk materials. *Scripta. Mater.* **2014**, *84-85*, 11-14.
- 252 3. Kriaa, H.; Guitton, A.; Maloufi, N. Fundamental and experimental aspects of diffraction for
253 characterizing dislocations by electron channeling contrast imaging in scanning electron microscope. *Sci.*
254 *Rep.* **2017**, *7*, 9742.
- 255 4. Howie, A.; Whelan, M. J. Diffraction contrast of electron microscope images of crystal lattice defects. II.
256 The development of a dynamical theory. *Proc. Royal. Soc.* **1961**, *263*, 217-237.
- 257 5. Howie, A.; Whelan, M. J. Diffraction contrast of electron microscope images of crystal lattice defects. III.
258 Results and experimental confirmation of the dynamical theory of dislocation image contrast. *Proc.*
259 *Royal. Soc.* **1962**, *267*, 206-230.
- 260 6. Wilkinson, A. J.; Hirsch, P. B. Electron diffraction based techniques in scanning electron microscopy of
261 bulk materials. *Micron.* **1997**, *28*, 279-308.
- 262 7. Spencer, J. P.; Humphreys, C. J.; Hirsch, P. B. A dynamical theory for the contrast of perfect and imperfect
263 crystals in the scanning electron microscope using backscattered electrons. *Phil Mag.* **1972**, *26:1*, 193-213.
- 264 8. Wilkinson, A. J.; Hirsch, P. B.; Czernuszka, J. T.; Long, N. J. Electron channeling contrast imaging of
265 defects in semi-conductors. *Proc. Micros. Semiconduct. Mater.* **1993**, *134*, 755-762.
- 266 9. Wilkinson, A. J.; Hirsch, P. B. The effects of surface stress relaxation on electron channelling contrast
267 images of dislocations. *Phil. Mag. A.* **1995**, *72:1*, 81-103.
- 268 10. Reimer, L.; Heilers, U.; Saliger, G. Kikuchi band contrast in diffraction patterns recorded by transmitted
269 and backscattered electrons. *Scanning.* **1986**, *8*, 101-118.

- 270 11. Reimer, L. Scanning Electron Microscopy. Physics of image formation and microanalysis.
271 Springer-Verlag Berlin Heidelberg GmbH, 2nd edition (1998).
- 272 12. Zeafferer, S.; Elhami, N. N. Theory and application of electron channelling contrast imaging under
273 controlled diffraction conditions. *Acta. Mat.* **2014**, *75*, 20-50.
- 274 13. Clarke, D. R.; Howie, A. Calculations of lattice defect images for scanning electron microscopy. *Phil. Mag.*
275 **1971**, *24* (190), 959-971.
- 276 14. Cockayne, D. J. H.; Ray, I. L. F.; Whelan, M. J. Investigations of dislocation strain fields using weak beams.
277 *Phil. Mag.* **1969**, 20-168, 1265-1270.
- 278 15. Hirth, J. P.; Lothe, J. Theory of dislocations. A Wiley-Interscience Publication, 2nd edition (1982).
- 279 16. Guitton, A. Joulain, A. Thilly, L. Tromas, C. Dislocation analysis of Ti₂AlN deformed at room
280 temperature under confining pressure. *Sci. Rep.* **2014**, *4* (6358), 1-4.
- 281 17. Edington, J. W. Interpretation of Transmission Electron Micrographs. London (1976).
- 282 18. Williams, D.B.; Carter, C. Transmission Electron Microscopy. Springer, New York (1996).
- 283

284