

1 Article

## 2 Influence of Circle of Willis Configuration on the 3 Rupture of Cerebral Aneurysms

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13 **Abstract: Background:** Formation and rupture of cerebral aneurysms may be related to certain types  
14 of configuration of the circle of Willis. Analysis of their interdependence can be of great importance.  
15 **Methods:** A group of 114 patients treated operatively for the cerebral aneurysm rupture and a group  
16 of 56 autopsied subjects were involved in the study. Four basic types of the circle of Willis  
17 configurations were formed—two symmetric types A and C, and two asymmetric types B and D.  
18 **Results:** A statistically significantly higher presence of asymmetry of the circle of Willis in the group  
19 of surgically treated subjects ( $p=0.006$ ) with a significant presence of asymmetric Type B in this  
20 group ( $p=0.017$ ) were determined. The presence of changes in the A1 segment in the group of  
21 subjects with solitary aneurysms on the anterior communicating artery showed a statistically  
22 significant presence in the group of autopsied subjects ( $p=0.0004$ ). Analyzing the presence of  
23 symmetry of the circle of Willis between the two groups, that is, the total presence of symmetric  
24 types A and C indicated their statistically significant presence in the group of autopsied patients  
25 ( $p=0.043$ ). **Conclusion:** Changes such as hypoplasia or aplasia of A1 and the resulting asymmetry of  
26 the circle of Willis directly affect the possibility of the rupture of cerebral aneurysms. Detection of  
27 the corresponding types of the circle of Willis after diagnostic examination can be the basis for the  
28 development of a protocol for monitoring such patients.

29 **Keywords:** Cerebral aneurysms; circle of Willis

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### 31 1. Introduction

32 Intracranial aneurysms are on average asymptomatic until the moment of rupture. Intracranial  
33 hemorrhage caused by aneurysm rupture occurs in almost 10% [1,2]. However, the presence of  
34 cerebral aneurysms is much more common and ranges between 3.6-9% depending on the series [3-  
35 7].From these data it is clear that there is a big difference between the incidence of cerebral  
36 aneurysms and frequency of their rupture. All this leads us to think about the causes of cerebral  
37 aneurysm rupture.

38 Locations of cerebral aneurysms are typically the sites of arterial junctions on the blood vessels  
39 of the base of the brain. The interconnected blood vessels at the base of the brain form a specific  
40 ring-like configuration, named after Willis who first described them. There are various forms of  
41 interconnected blood vessels within the circle of Willis itself [8]. The perfusion characteristics of  
42 each configuration of the circle of Willis directly depend on its anatomical characteristics i.e. the  
43 presence of normoplastic, hypoplastic or aplastic parts [9,10]. Basically, all configurations of the  
44 circle of Willis can be divided into symmetric and asymmetric. Connecting the appropriate circle of  
45 Willis configurations with its perfusion characteristics can indicate which configuration has an

46 increased perfusion load in certain parts [11,12]. This plays a key role in understanding the  
47 hemodynamic mechanism for the creation and rupture of cerebral aneurysms.

48 Linking the presence of aneurysmal changes with the corresponding configuration of the  
49 circulation ring at the base of the brain can indicate the predisposition of some types of  
50 configurations for the formation and rupture of cerebral aneurysms. An analysis of their association  
51 can be very important for making the right decisions on therapeutic approaches and monitoring of  
52 unruptured cerebral aneurysms.

## 53 2. Material and methods

54 The presence of morphological variations in the blood vessels of the base of the brain was  
55 monitored in two groups of subjects. The first group was made up of 114 patients who underwent  
56 surgical treatment for ruptured aneurysmal changes in the cerebral blood vessels. The second  
57 group was formed from 56 subjects who were subjected to autopsy after a fatal outcome that was  
58 not caused by hemorrhagic intracranial disease.

59 The subjects in the first group were subjected to MSCT and angiographic imaging of the  
60 cerebral blood vessels. A preoperative analysis of angiographic images was made and the existence  
61 of corresponding configurations of the circle of Willis was established. A dominant flow was  
62 determined in relation to the position of aneurysm. The corresponding blood vessel diameters were  
63 compared to the symmetric blood vessel diameters on the opposite side. Reduction of the blood  
64 vessel diameter by 1/3 to 2/3 in relation to the diameter of the blood vessel on the opposite side was  
65 marked as hypoplasia, and a decrease in the blood vessel diameter below 1/3 of the thickness of the  
66 opposite vessel was marked as pronounced hypoplasia. The presence of hypoplasia determined the  
67 symmetry or asymmetry of the circle of Willis. Intraoperatively, the relationship between visualized  
68 parts of the circle of Willis and aneurysm was analyzed, and then compared with the angiographic  
69 finding.

70 The second group consisted of subjects who underwent clinical or postmortem autopsy and  
71 who did not die due to some intracranial haemorrhagic disease. The subjects were selected by  
72 random sample method. During the autopsy, the brain was taken out from the cranial fossa  
73 together with the blood vessels of the base of the skull using a precise technique, and those at the  
74 entrance to the cranial cavity were resected. By precise preparation all blood vessels were separated  
75 from the base of the brain and distributed on a homogeneous flat surface with the formation of the  
76 typical configuration of the circle of Willis. The thickness of the blood vessels, the presence of  
77 anomalies, their arrangement and the symmetry of the present changes were observed. After  
78 such preparation, the circles of Willis were photographed by a digital camera, and then analyzed on  
79 a computer for a possible update of the original finding (Figure1).

80 For the purpose of comparing and analyzing the presence of the corresponding  
81 configurations of the circle of Willis, 4 basic types of configuration and one sub-type were formed.

82 **Type A** represents a symmetric circle of Willis with different variations at the level of the  
83 anterior communicating artery (ACoA).

84 **Type B** is an asymmetric circle of Willis with hypoplasia/aplasia of the A1 segment of the  
85 anterior cerebral artery (ACA).

86 **Type C** represents a symmetric circle of Willis with varying degrees of the hypoplasia/aplasia  
87 of the posterior communicating artery (PCoA) bilaterally, or the presence of a bilateral fetal PCoA  
88 type.

89 **Type D** is an asymmetric circle of Willis with single-sided PCoA hypoplasia or a single-sided  
90 fetal PCoA type

91 **Subtype B/D** represents an asymmetric circle of Willis with hypoplasia/aplasia of the A1  
92 segment of the anterior cerebral artery, in combination with changes in the posterior segment (due  
93 to hypoplasia of PCoA or PCA)(Figure 2).

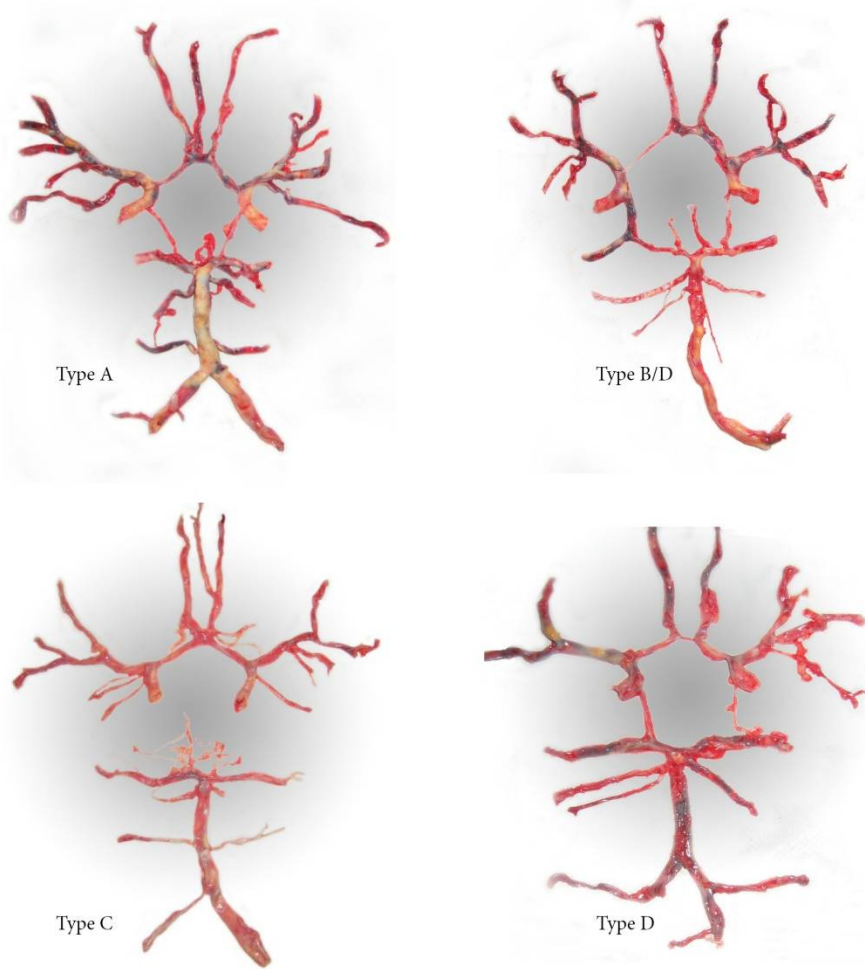


Figure 1.Preparations of the circle of Willis

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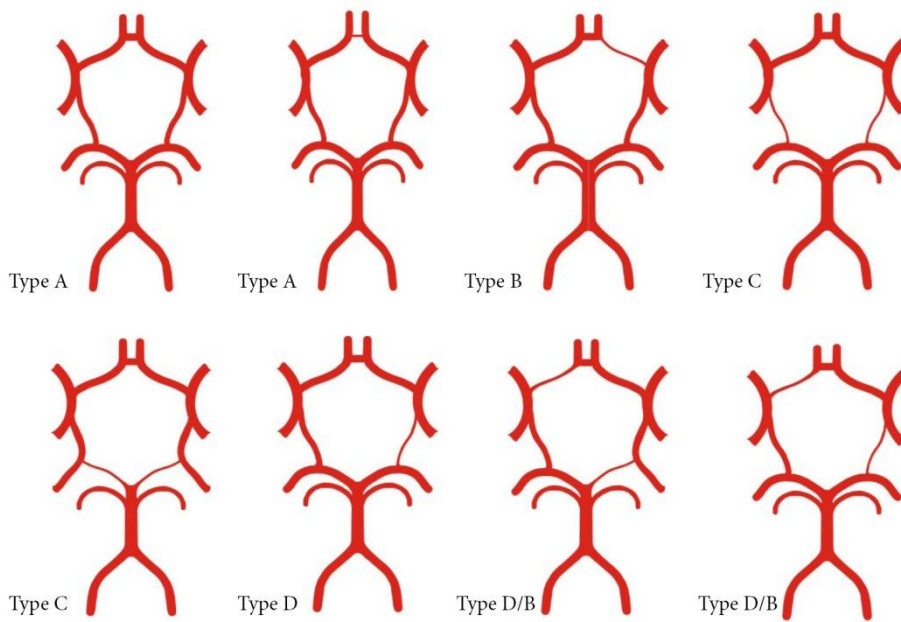


Figure 2.Basic types of configuration of the circle of Willis.

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100 The study complies with the Declaration of Helsinki. The study protocol (No CLI-1000) form  
 101 was approved by the Ethics Committee of the Clinical Center Niš, Serbia (01-2016-03). The  
 102 autopsies were done in accordance with the health care law and the bylaws of the Ministry of  
 103 Health. The patients undergoing surgery gave verbal consent that the results of their angiographic  
 104 recording and surgery findings can be used in the study.

### 105 *Statistical Analysis*

106 All the findings were numerically processed, tabulated and subjected to statistical analysis of  
 107 the existing differences between the groups. Student's t-test was used (if there was a normal  
 108 distribution of frequencies within the group) or non-parametric Mann-Whitney Rank Sum Test, if  
 109 the frequency distribution was unequal. A p-value of <0.05 was selected as statistically significant.

### 110 **3. Results**

111 In the group of autopsied patients, there was a total of 15 (26.8%) asymmetries of the circle of  
 112 Willis, while 73 (64%) of asymmetric configurations were found in the group of surgically treated  
 113 patients. Of these, 9(16%) findings were with asymmetry due to changes in the anterior segment of  
 114 the autopsied patients, while in surgically treated subjects the asymmetry of the anterior segment  
 115 was found in 50 (43.9%) cases. The incidence of asymmetry in the group with multiple aneurysms is  
 116 somewhat higher than in the group with solitary aneurysms (Table 1,2).

117 **Table 1.** Configuration of the circle of Willis – the group of autopsied patients.

Configuration of the circle of Willis		$\Sigma$
Symmetric Willis		<b>41(73.2%)</b>
Asymmetric Willis	Changes in the A1 segment	9(16%)
		15(26.8%)
Asymmetric Willis -	Changes in the posterior segment	6(10.8%)
$\Sigma$		56(100%)

118

119 **Table 2.** Configuration of the circle of Willis – the group of surgically treated patients.

	Asymmetric Willis		Symmetric Willis	$\Sigma$
	Changes in the A1 segment	Other changes		
Solitary aneurysms	33	15	33	81
Multiple aneurysms	17	8	8	33
	<b>50 (43.9%)</b>	23(20.1%)		
$\Sigma$	73 (64%)		<b>41(36%)</b>	114(100%)

120

121 By comparing the presence of asymmetry of the circle of Willis among the groups, the  
 122 significantly higher presence of asymmetry was determined in the group of surgically treated  
 123 subjects (p=0.006). The presence of changes in the A1 segment in the group of subjects with solitary  
 124 aneurysms on the anterior communicating artery showed a statistically significant presence in the  
 125 group of autopsied patients (p=0.0004).

126 In the group of surgically treated patients there were 23 (20.2%) changes in the posterior  
 127 segment in terms of unilateral hypoplasia or fetal type PCoA, and 6 (10.8%) changes in the posterior

128 segment were present in the group of autopsied subjects. By comparing the relationship between  
 129 the representation of changes in the posterior segment and PCoA and its impact on the occurrence  
 130 of asymmetry of the circle of Willis, no statistically difference was found between the group of  
 131 subjects undergoing surgery and the group of autopsied subjects.

132 The presence of the corresponding configurations of the circle of Willis in the group of  
 133 autopsied patients is shown in Table 3.

134 **Table 3.** Types of configuration the circle of Willis – the group of autopsied subjects.

Type Circle of Willis	
Type A	27 (48.2%)
Type B	4 (16%)
sub type B/D	5
Type C	14 (25%)
Type D	6 (10.8%)
$\Sigma$	56 (100%)

135 The presence of the corresponding types of the circle of Willis configuration was examined in  
 136 the group of surgically treated patients with solitary aneurysms separately from patients with  
 137 multiple aneurysms (Table 4,5).

138 **Table 4.** Types circle of Willis configuration – group of patients with solitary aneurysms.

Type Willis	Locations of ruptured solitary aneurysms						$\Sigma$
	ACoA	MCA	ICA	PCoA	perA	VBA	
Type A	9	5	2	2	1	1	20(24.7%)
Type B	24	3	2	/	3	/	34(42%)
subtype B/D	/	/	/	2	/	/	
Type C	/	8	2	2	/	1	13(16%)
Type D	/	/4	24	6	/	/	14(17.3%)
$\Sigma$	33	20	10	12	4	2	81(100%)

ACoA- anterior communicative artery, MCA- medial cerebral artery, ICA- internal carotid artery  
 PCoA- posterior communicative artery, perA- pericalosis artery, VB- vertbrobasilar artery

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140 Comparison of the presence of symmetric Type A in the group of autopsied patients and in the  
 141 group of patients with solitary aneurysms shows that there is a statistically significant presence of  
 142 symmetric Type A in the group of autopsied subjects ( $p=0.048$ ). Statistical differences in the  
 143 presence of symmetric Type C between the groups of surgically treated and autopsied subjects  
 144 were not found. Analyzing the presence of symmetry of the circle of Willis between the groups, i.e.,  
 145 total presence of symmetric types A and C, indicated their statistically significant presence in the  
 146 group of autopsied patients ( $p=0.043$ ).

147 The presence of asymmetric Type B is significantly higher in the group of surgically treated  
 148 patients with solitary aneurysms ( $p=0.017$ ). A statistically significant presence of asymmetric Type B  
 149 compared to the group of autopsied subjects was seen by observing the entire group of patients  
 150 undergoing surgery. ( $p=0.009$ )

151 The presence of asymmetric Type D did not show any statistical differences between the  
152 groups.

153 **Table 5.** Circle of Willis configuration types – group of patients with multiple aneurysms.

Types Willis	Multiple aneurysms						$\Sigma$
	Locations of ruptured aneurysms						
	ACoA	MCA	ICA	PCoA	perA	VBA	
<b>Type A</b>	/	3	1	1	/	/	5(15.2%)
<b>Type B</b>	12	/	3	/	/	/	17(51.5%)
Sub type B/D	/	/	/	2	/	/	
<b>Type C</b>	/	1	2	/	/	/	3(9%)
<b>Type D</b>	/	6	/	2	/	/	8(24.3%)
<b><math>\Sigma</math></b>	12	10	6	5			33(100%)

ACoA-anterior communicative artery, MCA-medial cerebral artery, ICA-internal carotid artery  
PCoA- posterior communicative artery, perA-pericalosis artery, VBA-vertbrobasilar artery

154 In the group of patients with multiple aneurysms there was a greater presence of asymmetric  
155 Type B than in the group with solitary aneurysms, but without statistical significance (Table4,5).

157 The presence of asymmetric type B in the group of patients operated on was observed in 50  
158 (43.9%) patients. Of these, 31 (62%) patients were with right-sided hypoplasia of the A1 segment,  
159 and 19 (38%) with left-sided A1 hypoplasia. Thirty-six (72%) ruptured aneurysms which were  
160 associated with hypoplasia of the A1 segment were localized on the ACoA. If we consider only the  
161 correlation between A1 hypoplasia and rupture of the aneurysm on ACoA, it can be seen that 70%  
162 of cases show the presence of right-sided hypoplasia (Table 6). Fourteen (28%) ruptured aneurysms  
163 associated with A1 hypoplasia were at other locations (MCA, ICA, PCoA, perA), with 12 of them  
164 being positioned on the side of the hypoplastic segment.

165  
166 **Table 6.** Correlation between hypoplasia of A1 and location of the ruptured aneurysm.

Locations ruptured aneurysms	Hypoplysia A1 right	Hypoplysia A1 left	$\Sigma$
<b>ACoA</b>	25	11	36(72%)
<b>MCA</b>	1	2	3(6%)
<b>ICA</b>	1	4	5(10%)
<b>PCoA</b>	2	1	3(6%)
<b>perA</b>	2	1	3(6%)
<b><math>\Sigma</math></b>	31(62%)	19(38%)	50(100%)

ACoA-anterior communicative artery, MCA-medial cerebral artery, ICA-internal carotid artery  
PCoA- posterior communicative artery, perA-pericalosis artery

167 In the group of 114 surgically treated patients, the presence of right-sided A1 hypoplasia was  
168 recorded in 27.2% (31) of patients, and of left-sided hypoplasia in 16.7% (19), while in the group of  
169 56 autopsied subjects 4 (7.1%) were with left-sided hypoplasia of the A1 segment and 5 (8.9%) with  
170

171 right-sided hypoplasia. By comparing these findings, we obtained statistically significant  
172 representation of A1 segment hypoplasia in the group of patients undergoing surgery compared to  
173 the group of autopsied patients ( $p = 0.027$ ).

#### 174 4. Discussion

175 Our results suggest that asymmetric configuration of the circle of Willis was much more  
176 frequent in the patients operated on after the rupture of an aneurysm than in subjects from autopsy.  
177 In addition, it has been established that there is a statistically significant presence of  
178 hypoplastic changes on the A1 segment in the group of patients undergoing surgery, which  
179 correlates with other studies [13-15]. The obtained results on the high prevalence of type B  
180 configuration with A1 segment hypoplasia in the ruptured aneurysm group indicate its high  
181 haemodynamic instability. In addition, the type B configuration is in the greatest correlation with  
182 the rupture of aneurysm on ACoA.

183 This finding clearly indicates that the morphological characteristics of the type of hypoplasia or  
184 aplasia in the anterior segment lead to an increase in blood flow from the opposite side, and a  
185 compensatory increase in flow through ACoA [9,16]. Increasing intramural pressure on the  
186 connective parts of the ACoA complex can initiate the process of remodeling the blood vessel  
187 resulting in the formation of an aneurysmal sac and then to its rupture [17].

188 Unlike the anterior segment, changes in the posterior segment of the circle of Willis have not  
189 shown significant association with the formation of cerebral aneurysms. During embryogenesis and  
190 with the development and differentiation of the carotid and basilar basin, the posterior  
191 communicating artery has a tendency for regression and decrease of blood flow [18]. Its functioning  
192 at the level of zero flow [19] indicates that stress at its exit from the carotid artery is not caused by  
193 blood redistribution, but by other haemodynamic disorders. This is also suggested by the fact that  
194 despite identical characteristics of the PCoA junction with ICA and PCA, aneurysms occur  
195 primarily on the carotid portion of PCoA. The dependence of the formation of aneurysms on PCoA  
196 from hemodynamic relationships in the ICA itself is clearly noticed in cases of the fetal type of the  
197 PCoA, the existence of which has not shown significant association with the formation of  
198 aneurysms. If we observe the point of separation of PCoA in relation to ICA, as a point of  
199 bifurcation angle, then we can apply the principle of optimal distribution of flow for the given angle  
200 [10]. Any increase in this angle leads to a direct increase in stress on the site of separation of PCoA,  
201 so that the formation of aneurysm on PCoA is due to the geometry itself and the course the ICA  
202 takes in that part of PCoA [20,21].

203 The significant prevalence of symmetric Type A in the group of autopsied subjects (in  
204 correlation with other studies) [22,23] and the statistically significant presence of asymmetric Type  
205 B in the group of subjects operated on due to cerebral aneurysm rupture clearly points to the direct  
206 influence of the configuration of the circle of Willis on the formation and rupture of cerebral  
207 aneurysms.

208 The presence of C and D configurations in the tested groups did not show significant effect on  
209 the formation and rupture of cerebral aneurysms. All this indicates that the presence or absence of  
210 PCoA changes cannot be associated with the onset or rupture of cerebral aneurysms.

211 The significant presence of the right-sided hypoplastic A1 in the group of patients undergoing  
212 surgery is interesting. The tendency of the types B and D to right-sided positioning of the  
213 morphological variants of A1 segment can be considered as part of the embryologic development of  
214 the vascular network and perfusion needs of the corresponding brain hemispheres.

215 Rupture of an aneurysm on MCA, ICA, PCoA perA, with the presence of the B type  
216 configuration (hypoplasia of A1), was in 90% on the side of the hypoplastic segment. This in turn  
217 indicates that the flow through the ICA and MCA on the side of hypoplasia has been significantly  
218 increased due to reduced flow through the hypoplastic A1.

219 In an experimental study with rabbits Ersin et al. demonstrated the hemodynamic effect of  
220 increased perfusion requirements in the formation of aneurysms [24], and Guangyu Zhu and al.

221 pointed to the significance of collateral circulation within the various anatomical variations of the  
222 circle of Willis [16].Ren and al. mathematically proved the influence of different anatomical  
223 variations as well as their perfusion characteristics [25]. Just like in our study, in a study conducted  
224 by Rojj et al. the configuration of the circle of Willis was identified as a risk factor for the rupture of  
225 cerebral aneurysm, suggesting that ruptures are also influenced by the direction of blood flow and  
226 the shape of aneurysms[28].

227 All this demonstrates that the hemodynamic load of asymmetric configurations directly  
228 influences the development of the process of remodeling certain parts towards achieving the  
229 appropriate perfusion, which can also affect the formation of cerebral aneurysms. Basically,  
230 asymmetric configuration has increased perfusion requirements in certain parts, which in turn can  
231 lead to the process of blood vessel remodeling in the part of permanent increase of the perfusion  
232 flow. Remodeling can be directed towards achieving an appropriate expansion of collateral  
233 circulation and achieving appropriate perfusion while reducing existing stress in the area of the  
234 burdened parts. Any further increase in perfusion requirements can lead to the continuation of the  
235 cascade of remodeling the blood vessel wall towards dilatation at the site of the greatest stress and  
236 to the gradual formation of an aneurysmal sac.

## 237 5. Conclusion

238 Asymmetric configuration basically has increased perfusion requirements in certain parts,  
239 which in turn can initiate the process of blood vessel remodeling in the part of permanent increased  
240 perfusion flow. Remodeling can be directed towards achieving an appropriate expansion of  
241 collateral circulation and achieving the appropriate perfusion, while reducing the existing stress in  
242 the area of the loaded parts. Any further increase in perfusion requirements can lead to the  
243 continuation of the cascade of remodeling the blood vessel wall in the direction of dilatation at the  
244 site of the greatest stress and to the gradual formation of an aneurysmal sac, followed by its rupture

245 Hypoplasia of the A1 segment entails significantly disturbed perfusion relationships in the  
246 AcomA area and the stress burden of the junction angle between A1 and A2, which in turn prompts  
247 the formation of an aneurysmal sac. In addition, there is a high correlation of AcoA aneurysm  
248 rupture with the asymmetric circle of Willis configuration

249 Formation of the basic circle of Willis configuration types and association with their  
250 susceptibility to cerebral aneurysm rupture can be used to make a protocol for monitoring  
251 unruptured aneurysms that are detected after MSCT or NMR angiography.

252

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254 Methodology; RM Investigation; BL Formal Analysis;R.M. Methodology

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