

1 *Type of the Paper (Article)*

2 **Optical constants of rare-earth substituted ferrite- 3 type amorphous garnets and nanoscale garnet-oxide 4 layers**

5 **Mohammad Nur-E-Alam*, Mikhail Vasiliev and Kamal Alameh**

6 Affiliation: Electron Science Research Institute, School of Science, Edith Cowan University, 270 Joondalup
7 Drive, Joondalup 6027, WA, Australia; m.nur-e-alam@ecu.edu.au (MNA); m.vasiliev@ecu.edu.au (MV);
8 k.alameh@ecu.edu.au (KA).

9 * Correspondence: m.nur-e-alam@ecu.edu.au

10

11 **Abstract:** Amorphous ferrite-type rare-earth (RE) substituted garnets and garnet-oxide
12 nanocomposite layers are prepared on clear glass substrates by using RF magnetron sputter-
13 deposition process. By using a combination approach employing custom-built spectrum-fitting
14 software in conjunction with Swanepoel's envelope method, the spectral dispersion function of
15 optical constants and the layer thicknesses are derived accurately from the transmission spectra of
16 the as-deposited samples. The effects of excess metal-oxides added to the base material systems
17 during the co-deposition process are found to affect the refractive index and the optical absorption
18 coefficients of garnet-oxide composites. A number of optical constant datasets are presented,
19 enabling the experimentalists to design nanophotonic or integrated-optics devices employing these
20 functional materials.

21 **Keywords:** rare-earth garnets; optical constants; envelope method; nano-composites; magneto-
22 optics.

23

24 **1. Introduction**

25 Rare-earth substituted ferrite garnet-type thin-film materials are in high demand in modern
26 magneto-optics (MO) and nano-scale devices for use in various applications. During the last couple
27 of decades, many researchers and engineers worldwide have conducted a significant amount of work
28 in the field of MO garnet thin film materials. These works have their origins from the days of bubble-
29 domain magnetic disk memory development, when the substitution of rare-earth ions (e.g. Bi^{3+} , Ce^{3+}
30 and others) into the Yttrium Iron garnet (YIG) material system was found to significantly enhance
31 the Faraday rotation properties. The rare-earth ions substitution into the dodecahedral sublattice sites
32 of garnet mainly affects the structural (lattice constant), optical (refractive index and absorption
33 coefficient), and also the magnetic and magneto-optic properties of iron garnet thin film materials.
34 More recently, other non-magnetic (e.g. Ga or Al) ions have been introduced to the ferrite garnet
35 systems, which tend to occupy the octahedral and tetrahedral garnet sublattices, also affecting
36 magnetic and MO properties. A huge variety of rare-earth and other metal dopants have been
37 introduced into different garnet-type systems, and their properties studied extensively to overcome
38 the practical difficulties of using these ferrite-type garnets in various new and existing technologies
39 [1-14], e.g. to increase the specific Faraday rotation simultaneously with reducing the annealing
40 process temperature. The demand for application-specific MO garnets is still growing, since the need
41 for on-chip integration of MO/MPC non-reciprocal photonic devices is rapidly becoming imperative
42 day by day [15-20].

However, the development of high-quality thin-film garnet materials requires a significant amount of characterization and investigation of all material properties of interest. Most of the previous reports of substituted iron-garnet films include optical absorption, Faraday rotation, MO figure of merit, and magnetic hysteresis loop measurement results for either a single wavelength or within a narrow spectral range [7-14, 21-25]. Despite the growing interest in using garnet films, to the best of our knowledge, there are no comprehensive reports on the easy determination of optical constants data of garnet thin films. Moreover, the detailed reports in which the refractive index dispersion functions of MO garnets have been presented, are relatively scarce. Therefore, determination of the optical constants (complex refractive index) by a non-destructive and cost-effective method is an important part of material characterization, which is necessary whenever any new garnet composition is developed. The accurate determination of optical constants data across a wide spectral range for each particular rare-earth-substituted garnet material is crucial for the design and optimization of any MO or MPC-based modern devices operating at different wavelengths e.g. active displays, image sensors, magneto-optic sensors and imagers, and magneto-plasmonic biosensors. Spectroscopic ellipsometry and profilometry are well-known technologies used to determine the physical thickness and/or refractive index of thin-film materials, but these are often very complex, and costly equipment is required. However, based on both the transmission and reflection spectra, several calculation methods have been reported to derive the refractive index (mainly, its real part) and the film thickness [26-31]. All of these methods are applicable (within certain limitations) to determine the refractive index of thin films using the optical interference fringes of the transmission and reflection spectra. Measurement accessories for spectrophotometers capable of measuring the reflection spectra are costlier and less accessible compared to equipment measuring transmission spectra only. In this work, we derive accurately the optical constants data for multiple rare-earth doped iron garnets simultaneously with the garnet film thicknesses from the optical transmission spectra by means of a combinatorial approach of employing custom-built spectrum-fitting software in conjunction with Swanepoel's envelope method [32]. We apply the measurement methodology described in subsequent section to a very broad spectral range between 400 nm to over 2000 nm to generate optical property datasets for multiple MO garnet compositions of interest to future device developers.

2. Theory and equations used to process transmission fringes and derive the refractive index and film thickness data

75 Swanepoel's envelope method (SWEM) [26-28, 30-32] can be used to calculate an approximate
 76 value of the refractive index of semitransparent and weakly-absorbing thin film media. Amorphous
 77 garnet-type nanoscale layers grown on clear glass substrates represent an appropriate medium to
 78 apply SWEM to determine their optical constants. The basic equation given below can be used to
 79 calculate the approximate refractive index values of garnet films by using the spectral locations of the
 80 transmission maxima and minima:

$$n_1 = \left[N + (N_2 - S_2)^{1/2} \right]^{1/2} \quad \dots \dots \dots \quad (1)$$

84 where the value of N can be determined from the following expression: $N = 2S\{(T_M - T_m)/(T_M \cdot T_m) +$
 85 $(S^2 + 1)/2$; here T_M and T_m denote the maximum and minimum transmittance at a given wavelength,
 86 respectively. Parameter S represents the refractive index of used glass substrate (averaged across the
 87 spectral range of interest), which is 1.47 for the Corning glass substrates used in this work.

Figure 1 shows an example of typical transmission spectrum of a garnet film presenting the envelopes transmission maxima (T_M) and minima (T_m) intensities.

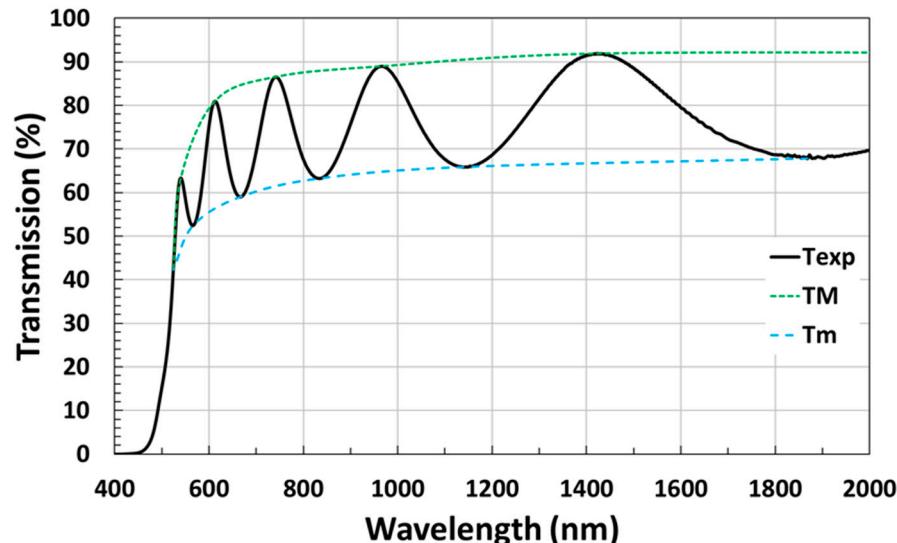


Figure 1. Example of a typical transmission spectrum of a garnet thin film sample of composition type $\text{Bi}_{2.1}\text{Dy}_{0.9}\text{Fe}_{3.9}\text{Ga}_{1.1}\text{O}_{12}$ (the garnet composition characterized within Ref [33]); where T_{exp} is the measured transmission of the sample, T_M and T_m are the maxima and minima of the envelopes.

Using the primary refractive index (approximate n_1 , derived from equation 1 at all wavelengths of interest) values into the basic equation of the interference fringes, $2nd = m_0\lambda$, the order number (m_0 , which is an integer for maxima and a half-integer for minima) of interference fringes, and the first-approximation value of the film thickness (d_1 , as shown in Table 1) can be determined by using the expression:

$$d_1 = \frac{\lambda_1 \lambda_{21}}{2(n_2 \lambda_1 - n_1 \lambda_2)}. \quad \dots \quad (2)$$

where, n_1 , and n_2 , are the refractive indices at two adjacent maxima (or minima) at λ_1 and λ_2 .

Table 1: Example of calculated results for a typical garnet thin film material deposited on a glass substrate (transmission spectrum is shown in Fig. 1).

1	2	3	4	5	6	7	8	9	10	
Sample	Wavelength	T _M	T _m	n ₁ =[N +	d ₁	=	m ₀ =2n	M	d ₂ =Mλ/2	n ₂
	(nm)			(N ² -	λ ₁ λ ₂ /2(n ₂ λ ₁ -	1d/λ		n ₁ (nm)	=Mλ/2	
				S ²) ^{1/2}] ^{1/2}	n ₁ λ ₂) (nm)				d ₂ (ave)	
A	typical	1868	0.92	0.6779	2.239	-	1.5	1.5	626	2.226
garnet type		1430	0.9187	0.6675	2.269	627	2.0	2.0	630	2.272
thin film		1140	0.9056	0.6585	2.276	641	2.5	2.5	626	2.264
		966	0.8895	0.647	2.286	638	3.0	3.0	634	2.302
		834	0.88	0.6323	2.318	630	3.5	3.5	630	2.319
		740	0.8650	0.619	2.338	589	4.0	4.0	633	2.351
		666	0.85	0.5899	2.417	585	4.5	4.5	620	2.381
		612	0.8090	0.56	2.457	671	5.0	5.0	623	2.431
		566	0.745	0.5244	2.475	781	5.5	5.5	629	2.473
		540	0.6333	0.46	2.513	-	-	-	-	-

d_1 (ave) = 626 nm, δ_1 = 24.8 nm (3.96%), d_2 (ave) = 629 nm, δ_2 = 4.82 nm (0.76%), $d_{(mpcmf)}$ = 630 nm

110 The detailed explanations of relevant theory are available from Refs [26-28, 32]. The same Refs. Also
 111 discuss the reasons for having some inaccuracies in the refractive index and the first-approximation
 112 film thickness calculations, and also the ways of reducing the deviations obtained in first-
 113 approximation film thickness calculations to obtain an acceptable film thickness values (with a
 114 smaller numerical dispersion). After examination of the calculated n and d values, a simple
 115 complementary graphical method can be applied to derive the first-order number m_1 and the film
 116 thickness d , by modifying the interference fringe expression ($2nd = m_0\lambda$) as given below, for the
 117 successive maxima and minima, starting from the long-wavelength end:

where m_1 is the first-order value, which equals an integer for a maximum and a half-integer for a minimum, and $l = 0, 1, 2, 3, \dots$. Therefore, by plotting $(l/2)$ versus (n/λ) (as shown in Fig. 2(a)), a straight line with slope value $2d$ and cut-off on the Y-axis at $(-m_1)$, the more precise physical thickness d of each thin film sample can be obtained using parameter d_2 ($d = d_2 = 0.5 \times \text{slope value}$).

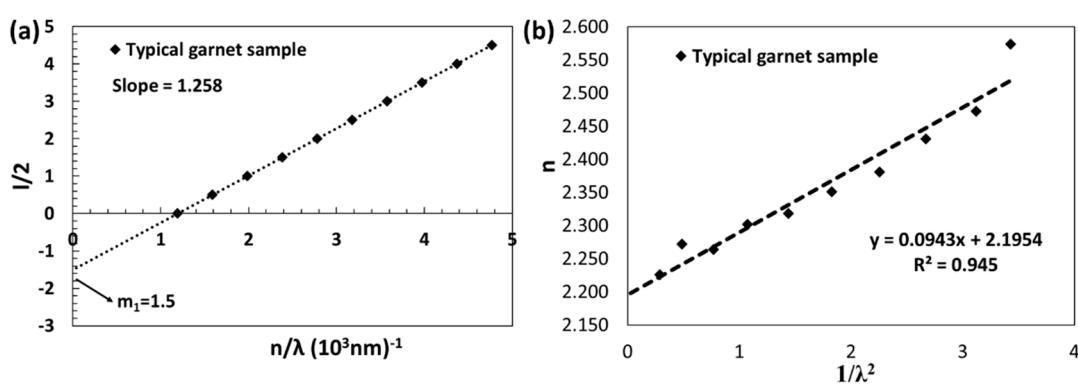


Figure 2. Plots of $(l/2)$ versus (n/λ) (a), and n vs λ^{-2} (b) used to determine the physical film thickness and the first-order value m_1 , and also the Cauchy's constants, respectively.

It is also reported that the Cauchy's dispersion formula can be used to derive the values of refractive index over the spectral range between 300-2500 nm, if only the Cauchy's constants are known [27, 28, 30, 32]. By using the calculated values of the final refractive index (from envelope method), in conjunction with least-square fitting (Fig. 2b), the refractive index dataset can be derived using the following expression:

where a and b are Cauchy's constants, which can be determined from the intercept and slope of the n -versus- λ^{-2} linear plot, respectively.

In our previous work, we demonstrated the computational spectral fitting method of film thickness and absorption coefficient derivation using an in-house-built magnetic photonic crystal (MPC) software using the refractive index dispersion data obtained from Cauchy's formula [32].

3. Methodologies and calculation results for the optical constants of several garnet and garnet-oxide composite thin films

In this work, we have carried out the following steps to investigate and determine the film thicknesses and the refractive index datasets from their measured transmission spectra only:

Part (1): Calculate the refractive index data and film thickness by using the SWEM method.

152 Step (1). The spectral position of the transmission maximum and minimum peaks were
153 determined in the transmission spectrum and listed as shown in the columns 2, 3 and 4 in Table
154 1.

155 Step (2). Calculate the approximate values of refractive index and the primary film thickness
156 estimates using the values of transmission maxima and minima and listed (column 5 and 6).

157 Step (3). The estimated interference fringes order numbers were determined by substituting n_1
158 values in equation (2), as shown in column 7. Later, the refined interference fringes order
159 numbers (either integer or half-integer) were identified, as listed in column 8.

160 Step (4). Recalculate the film thickness using the correct interference fringe numbers and listed
161 the film thickness values (with less deviation) in column 9.

162 Step (5). The final refractive index of the film was recalculated by substituting the correct
163 interference fringe number and the film thickness values in equation 2 as listed in column 10.

164
165 Part (2). By using a simple graphical method based on the modified interference fringes equation, the
166 physical film thicknesses were determined and re-checked. The acceptable film thickness (with better
167 accuracy) was found.

168
169 Part (3). By using the calculated values of the final refractive index (from envelope method), in
170 conjunction with least-square fitting (derived from n vs λ^2 plot), the real parts of refractive index of
171 the films were derived, at each wavelength, using Cauchy's dispersion formula $n(\lambda) = a + b/\lambda^2$, where
172 a, b are the Cauchy's constants.

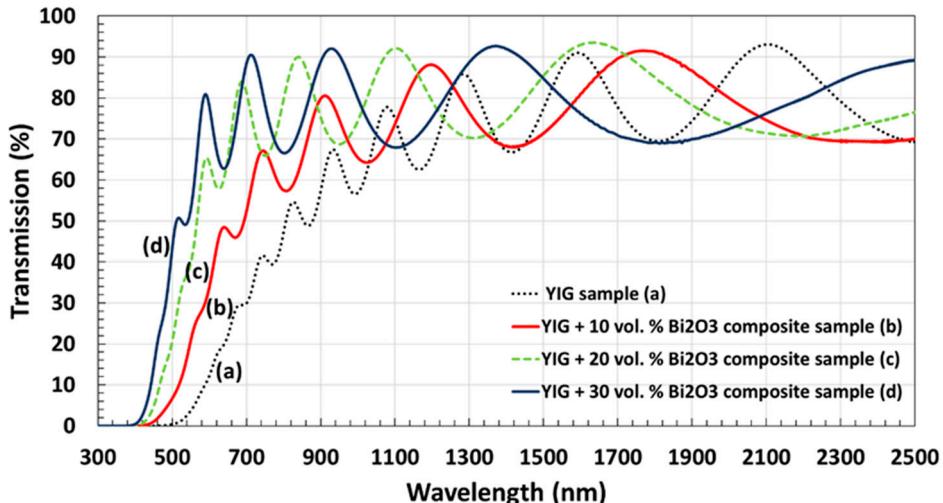
173
174 Part (4). Using the refractive index (derived from Cauchy's dispersion formula) data in MPC
175 spectrum-fitting software, we fitted the transmission spectra with the modeled transmission spectra
176 and re-calculated the film thicknesses. From this fitting process, we then derived the absorption
177 coefficient spectra for all samples using the MPC software, which relied on sufficiently accurate data
178 for both the physical thickness, refractive index dispersion function, and the measured transmission
179 spectrum.

180

181 3.1. Optical study of $Y_3Fe_5O_{12}$ and $Y_3Fe_5O_{12}:Bi_2O_3$ (10-30 vol.%) composites

182 $Y_3Fe_5O_{12}$ (YIG) is one of the most widely known ferrimagnetic garnet crystals among all rare-
183 earth iron garnets that are used in various microwave-range and optical devices such as circulators,
184 isolators, filters, and switches [8, 9, 25]. YIGs do not possess giant Faraday rotation properties in the
185 visible and near-infrared ranges. Various Bi-substituted YIG-derived garnet compositions can
186 possess giant specific Faraday rotations and large MO figures of merit in the visible range, together
187 with narrow ferromagnetic resonance (FMR) linewidths (at about 6.1 Oe at 9.77 GHz[25]) in sputtered
188 nanocomposite-type films with bismuth oxide dilution, which is of significant interest for various
189 modern microwave-range applications and advanced technologies. The methods of synthesis and the
190 measured characteristics for a range of optimized YIG-bismuth oxide ($Y_3Fe_5O_{12}-Bi_2O_3$) composites
191 have been described in detail within the Ref [25]. In this subsection, we present the results of the
192 optical constants study of as-deposited (amorphous) YIG and YIG : Bi_2O_3 (10-30 vol. % of excess oxide)
193 composite nano-scale layers.

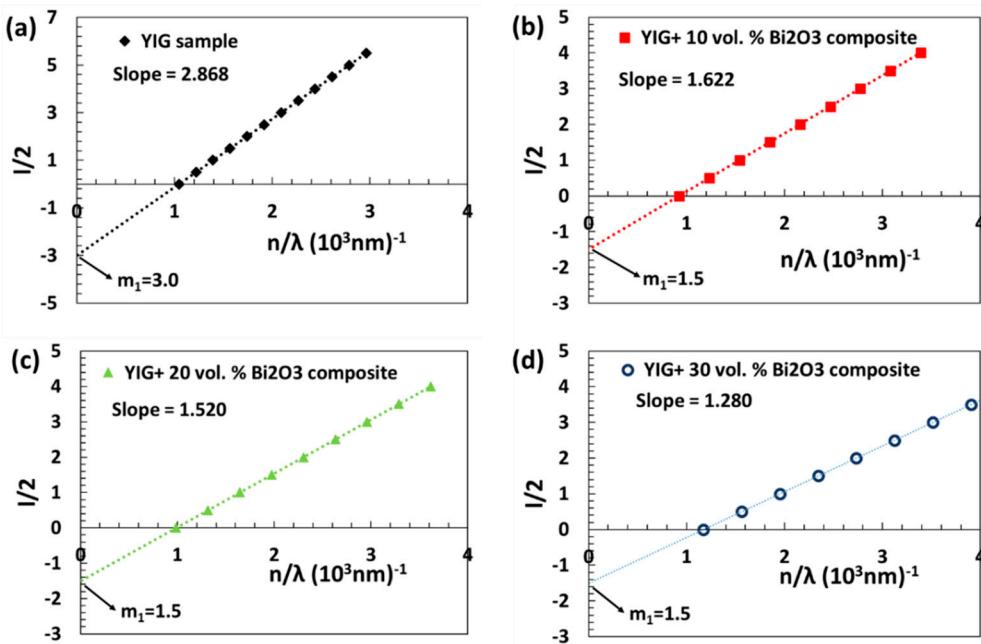
194 Figure 3 shows the measured transmission spectra of as-deposited YIG and YIG : Bi_2O_3
195 composite garnet layers. All samples showed an adequate number of interference fringes to reliably
196 calculate the film thicknesses and their refractive index data using these transmission fringes. It is
197 well known that thicker films show more fringes of transmission [34]. It can be noticed that the
198 addition of Bi_2O_3 content from a separate metal-oxide target during the co-sputtering deposition
199 process helps shift the optical absorption edge in garnet-oxide composite layers towards the shorter
200 wavelengths. Increasing the volumetric content of Bi_2O_3 added into the composite system improves
201 the optical transmittance in the shorter wavelength region.



202

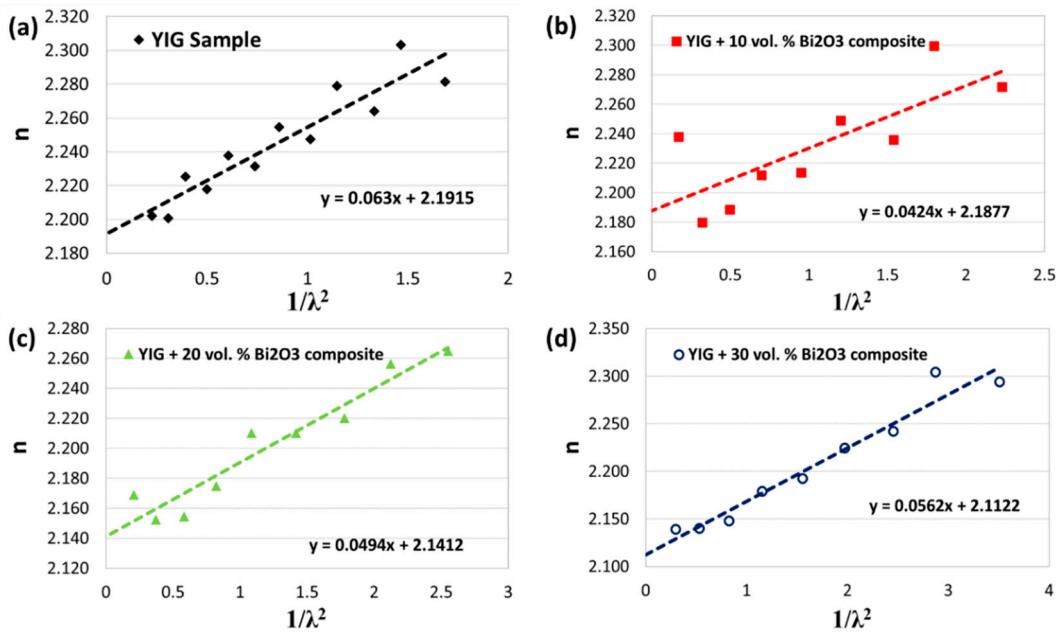
203 **Figure 3.** Transmission spectra of as-deposited $\text{Y}_3\text{Fe}_5\text{O}_{12}$ and $\text{Y}_3\text{Fe}_5\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films deposited on
 204 glass substrates. Curve (a) represents a 1434 nm thick $\text{Y}_3\text{Fe}_5\text{O}_{12}$ garnet layer;
 205 (b) represents a 811 nm thick $\text{Y}_3\text{Fe}_5\text{O}_{12}$: 10 vol. % Bi_2O_3 composite film;
 206 (c) represents a 760 nm thick $\text{Y}_3\text{Fe}_5\text{O}_{12}$: 20 vol. % Bi_2O_3 composite film,
 and (d) represents a 640 nm thick $\text{Y}_3\text{Fe}_5\text{O}_{12}$: 30 vol. % Bi_2O_3 composite film.

207 Figure 4 shows the presentation of simple complementary graphical method ($l/2$ versus n/λ plots)
 208 that we applied to derive film thickness with better accuracy (close to 1% deviation). The
 209 determination of accurate film thickness is one of the important key factors for reliable calculation of
 210 the real part of the refractive index for any type of semi-transparent thin-film materials. The plots
 211 ($l/2$) versus (n/λ) give a straight line of slope equal to twice of the actual film thickness, which
 212 intersects the Y axis at ($-m_1$) values for all samples. From this slope value, the actual film thickness
 213 value for each as-deposited sample was found to be close to the calculated values (calculated using
 214 SWEM, as mentioned in the in Table S1 in the Supplementary section).
 215



216

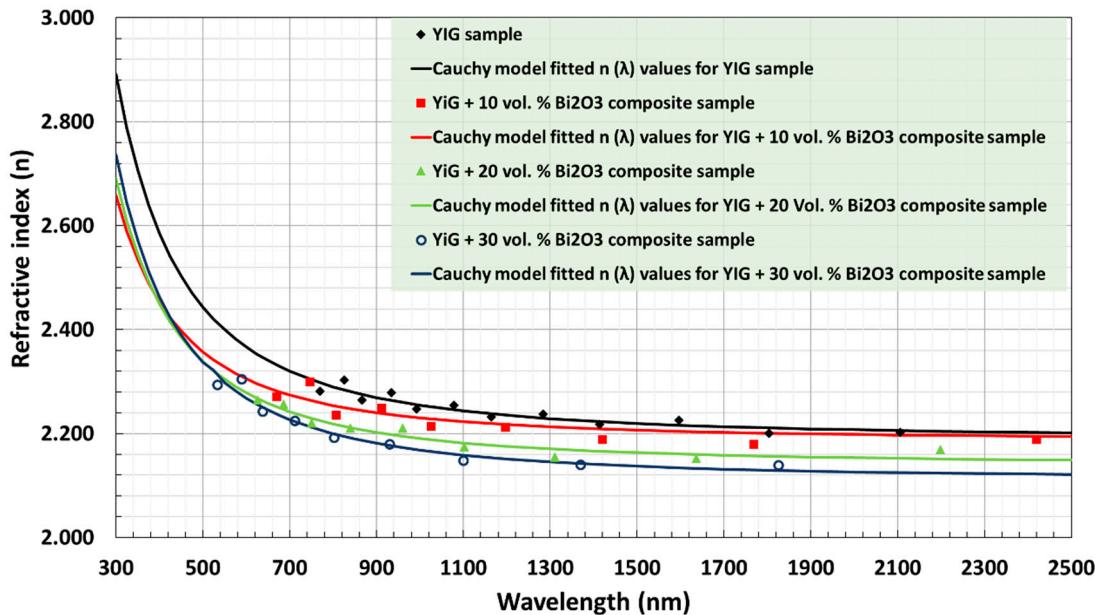
217 **Figure 4.** Plots of ($l/2$) versus (n/λ) used to determine the film thickness and the first-order value m_1 for
 218 $\text{Y}_3\text{Fe}_5\text{O}_{12}$ and $\text{Y}_3\text{Fe}_5\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films. The Y-axis cut-off (m_1) and the slope values for each sample
 219 are illustrated in the graphs.



220

221 **Figure 5.** Least-square fits of the calculated refractive index (n_2) values for $\text{Y}_3\text{Fe}_5\text{O}_{12}$ and $\text{Y}_3\text{Fe}_5\text{O}_{12}:\text{Bi}_2\text{O}_3$ 222 composite-type co-sputtered thin films.

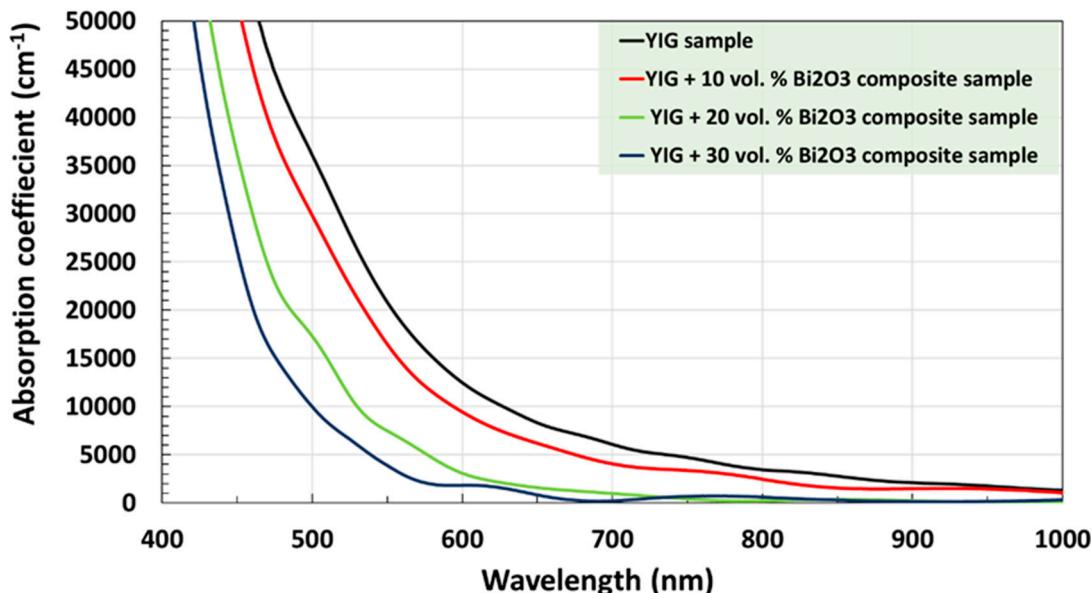
223 Figure 5 shows linear plots of least-square fits (n vs λ^{-2}), from where the values of Cauchy's 224 constants (a, and b) were determined. By substituting the a and b values into Cauchy's dispersion 225 formula Equation (Eq. 4), the values of the refractive index were derived over the whole spectral 226 range of measurement, between 300–2500 nm, as shown in Figure 6. In Figure 6, the data points of n_2 227 values are represented as solid large points, while n values derived by using Cauchy's dispersion 228 relation for the corresponding sample are plotted as solid lines. From this figure, one can note that 229 the increasing volumetric fraction of Bi_2O_3 introduced into the YIG material system helps to reduce 230 to refractive index of the films across the spectrum, thus improving the optical transparency. The 231 transparency has also been improved substantially due to obtaining lower absorption coefficients in 232 nanocomposites, compared to the pure YIG sample. It is likely that, in the nanocomposite materials 233 system, an increased substitution of Bi^{3+} ions occurs within the dodechedral sublattice sites of YIG, 234 thus increasing the specific Faraday rotation. At the same time, diluting the highly-absorbing garnet 235 phase and residual iron oxides with a high-transparency oxide material (Bi_2O_3) leads to reduced 236 optical absorption [22, 25].



237

238 **Figure 6.** Refractive index dispersion spectra of $\text{Y}_3\text{Fe}_5\text{O}_{12}$ and $\text{Y}_3\text{Fe}_5\text{O}_{12}$: Bi_2O_3 composite thin films. The solid
 239 curves were determined according to Cauchy dispersion relationship.

240 Figure 7 shows the absorption coefficient datasets of YIG and YIG: Bi_2O_3 composite films. These
 241 datasets were derived by confirming the film thicknesses using the peak-to-peak fitting of
 242 transmission spectra according to the method described in Refs [22–25, 32]. It was found that
 243 absorption coefficient is substantially dependent on the added excess Bi_2O_3 content. The higher the
 244 bismuth oxide content addition to the nano-composite material system, the lower the absorption
 245 coefficients across visible range, which leads to possibilities to engineer these nanomaterial systems
 246 according to the required applications.



247

248 **Figure 7.** Derived optical absorption coefficient datasets of $\text{Y}_3\text{Fe}_5\text{O}_{12}$ and $\text{Y}_3\text{Fe}_5\text{O}_{12}$: Bi_2O_3 composite samples,
 249 obtained with ECU MPC fitting software (across the spectral range 400–1000 nm) by using the measured
 250 transmission spectrum data of the samples. The physical film thickness used in fitting was obtained from line
 251 slopes (Fig. 4), and the refractive index dispersion function from the Cauchy formula with coefficients obtained
 252 from least-squares fitting (Fig. 5).

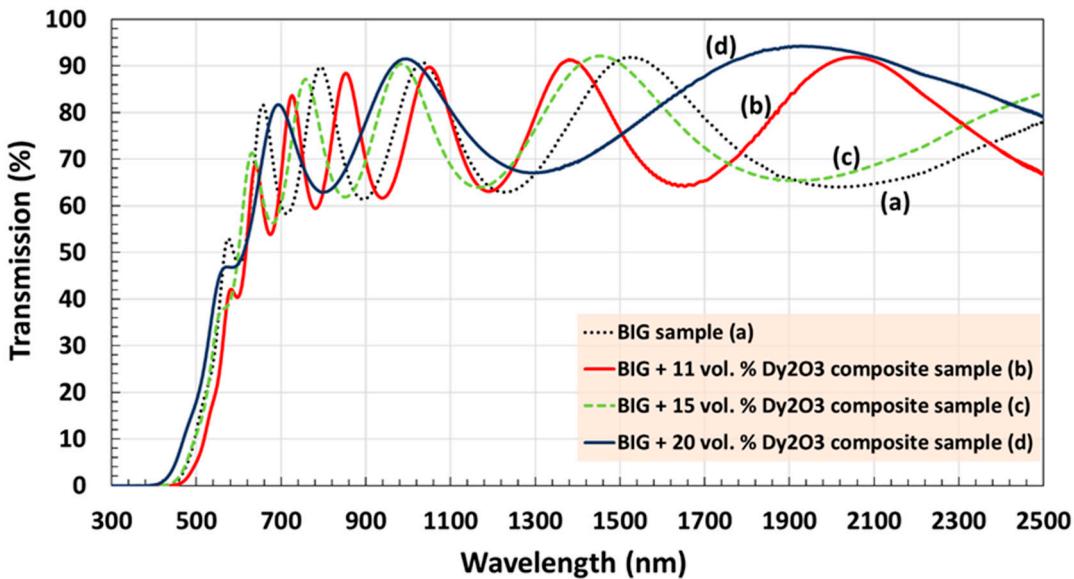
253 These optical constants results can add value to the previously published MO dataset properties
254 of similar garnet-type composites, by way of re-confirming the calculations of MO quality factors or
255 the validity of some MPC designs. Overall, the methodologies and results presented can be of interest
256 for the designers of new semitransparent thin-film compositions of all types.

257

258 *3.2. Optical study of $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ (11-20 vol. %) composites*

259 Bismuth-substituted metal-doped iron garnets of different composition types having high
260 volumetric fraction of the garnet phase together with giant Faraday rotation and good microstructure
261 quality are very suitable for use as functional materials in applied magneto-optics [10-12, 21-25]. The
262 properties of these types of garnet materials are strongly dependent on the level of bismuth
263 substitution as well as on the synthesis process parameters. The higher the number of bismuth atoms
264 substituted into the garnet system (to replace rare-earth atoms, such as Y, Dy, Lu, or Sm), the greater
265 is the potential to have higher Faraday rotation. So far, garnet films approaching the maximum Bi
266 substitution of three atoms per formula unit, e.g. $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ (BIG) and $\text{Bi}_3\text{Fe}_4\text{Ga}_1\text{O}_{12}$, prepared by pulsed
267 laser deposition (PLD) process, demonstrated very large Faraday rotations in the green light [35, 36].
268 According to our knowledge, there are no reports on RF sputtered films of similar composition type
269 (containing 3 bismuth atoms per formula unit, or deposited from an oxide-mix-based garnet-
270 stoichiometry targets containing more than four iron atoms per f. u. such as $\text{Bi}_3\text{Fe}_5\text{O}_{12}$) that possessed
271 good magneto-optic (MO) performance. However, a co-sputtering process successfully led our group
272 to synthesise a garnet composition stoichiometrically as close as possible to $\text{Bi}_3\text{Fe}_5\text{O}_{12}$, which
273 contained some dysprosium (Dy) dilution. The detailed characteristics of $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ composite
274 films containing different amounts of added dysprosium oxide showing excellent combinations of
275 the optical and magneto-optical properties were reported in Ref [23]. Here, we present the results of
276 the optical constants study of RF sputtered thin films of composition type $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and
277 $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ (11-20 Vol. %) composite nano-scale layers.

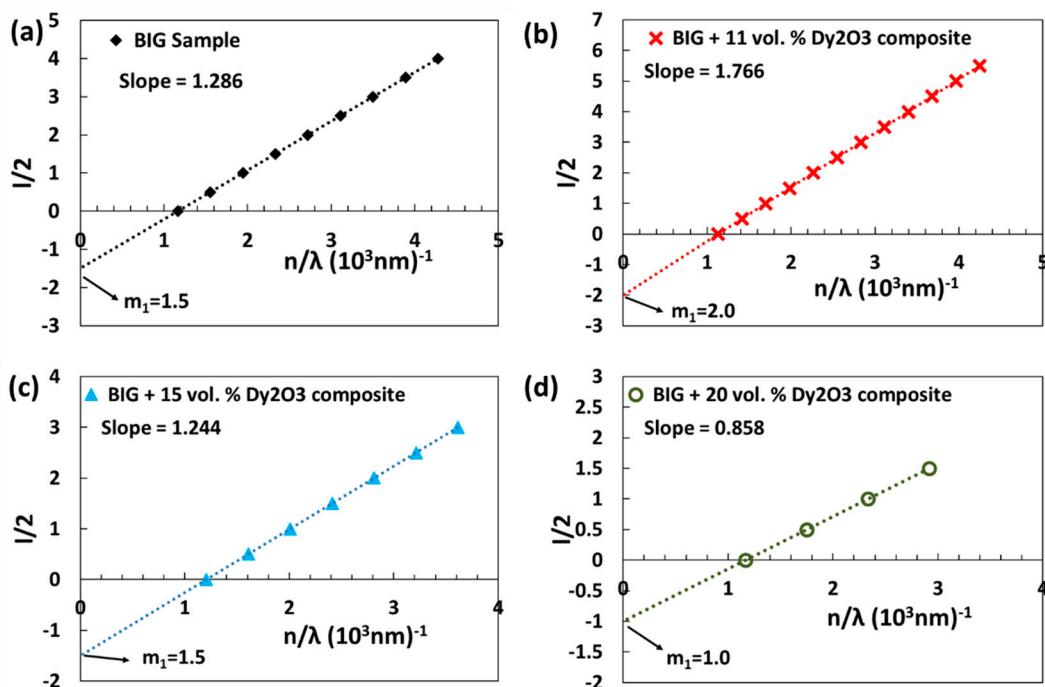
278 Figure 8 shows the measured transmission spectra of as-deposited $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ garnet and
279 $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ (11-20 vol. %) composite thin film layers. All samples show distinct interference
280 fringes with relatively high wave intensity over a wide range of wavelengths (especially from 600 nm
281 to 2500 nm). It can be noticed that below 600 nm, there is a small number of weak transmission peaks,
282 indicating the higher-wavelength absorption edge, compared to results presented in Section 3.1. A
283 limited number of interference fringes are observed (about five fringes, Fig. 8, curve d) for a
284 composite sample of type $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ (20 vol. %), indicating that the sample was possibly thinner.
285 Our calculated data confirmed that the film thickness for this particular batch of samples was less
286 than 500 nm, as can be seen in Fig. 8d, (slope value 0.858). The detailed calculated values of refractive
287 index at multiple wavelength points and the film thickness data for each sample from these batches
288 are summarised in the Supplementary section (Table S2).



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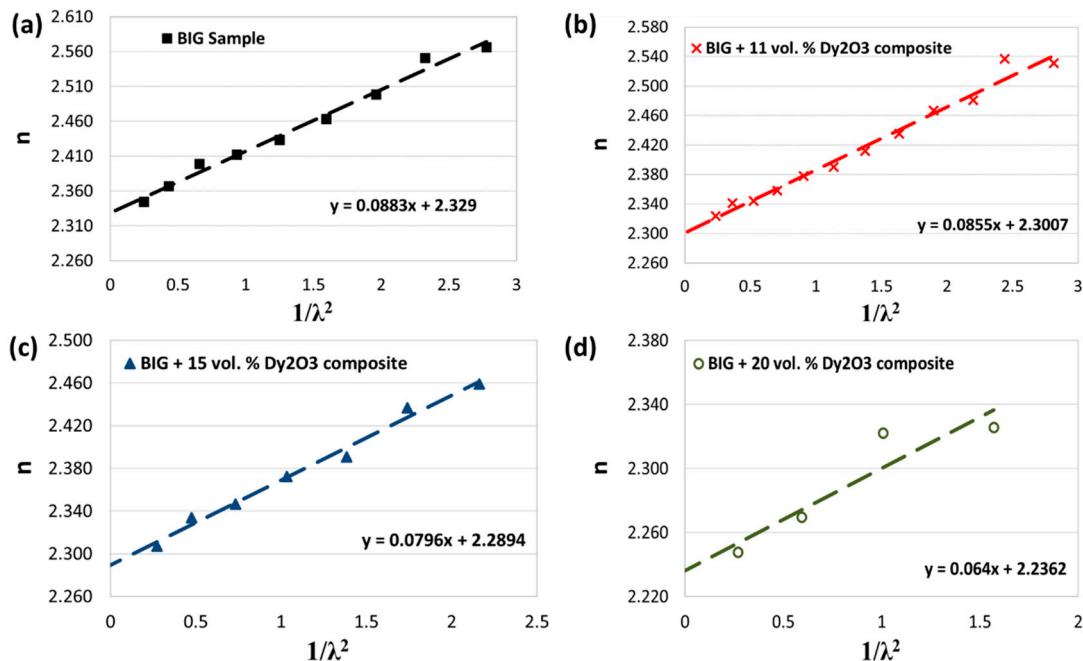
290 **Figure 8.** Transmission spectra of $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ composite thin films.

291 Figure 9 shows the plots of $(l/2)$ versus (n/λ) for all as-deposited BIG and BIG: Bi_2O_3 composite
 292 garnet layers, from which the film thicknesses were recalculated, and then the physical thickness
 293 values were found with a relatively small error. The perfectly straight lines of well-defined slopes
 294 confirmed the accuracy of the calculated values for each of the samples (as listed in Table S2, in the
 295 Supplementary section), and this also validated the modified interference fringes equation (Eq. 3).
 296 With the help of the calculated refractive index values (n_2 at each fringe point), from the least-square
 297 fitting, the wavelength-dependent refractive index data for each sample were extrapolated across a
 298 broad spectral range. Figure 10 shows the least-square fit of the calculated refractive index (n_2) values,
 299 and Figure 11 represents the derived refractive index values (from Cauchy model) for the broad
 300 spectral range, between 300–2500 nm, for all garnet samples.



301

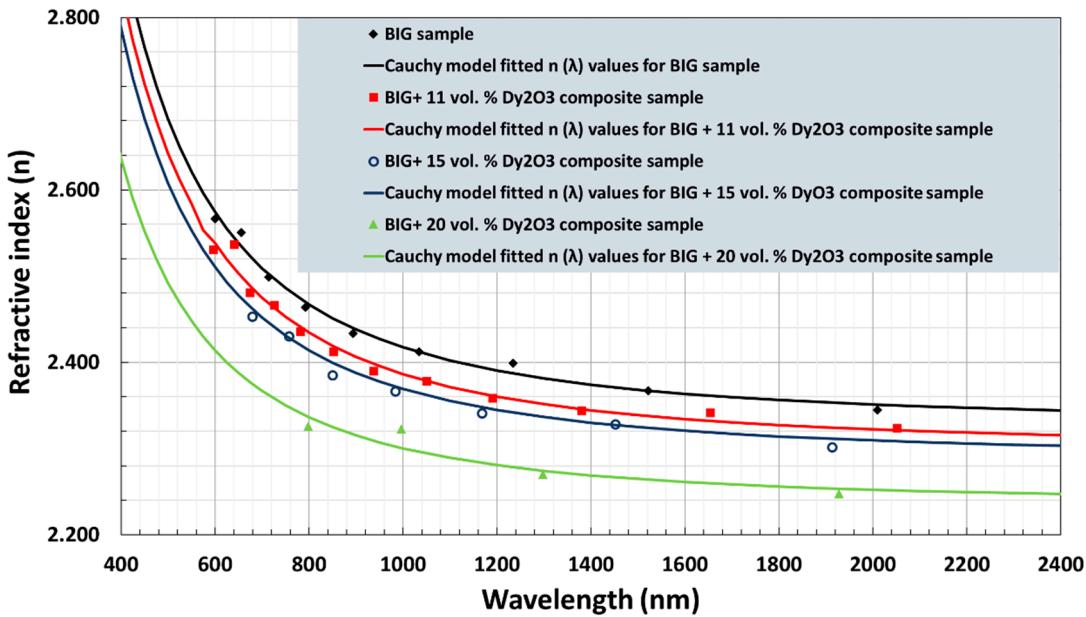
302 **Figure 9.** Plots of $(l/2)$ versus (n/λ) used to determine the film thickness and the first-order value m_1 for
 303 $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ composite thin films.



304

305 **Figure 10.** Least-square fit of the calculated refractive index (n_2) values for $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$
306 composite-type thin films.

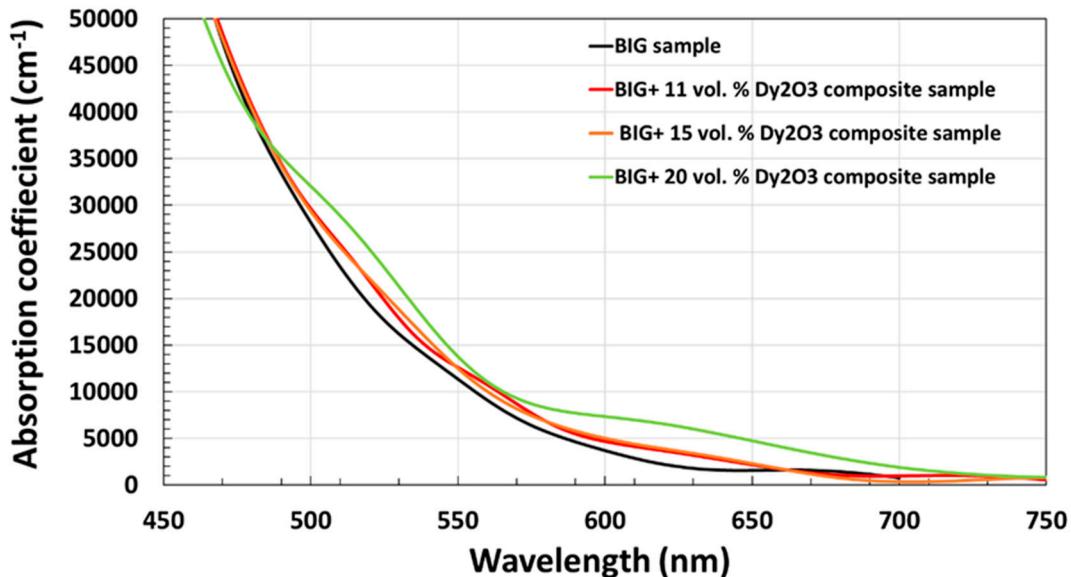
307 It can be seen that the refractive index values gradually decrease noticeably with the increase in
308 the wavelength, up to about 1600 nm, and these remain decreasing with a negligible variance
309 (asymptotically) above that wavelength. The effects of Dy_2O_3 addition to the base material system are
310 quite clear. The refractive index values decreased as the number of excess metal-oxide content
311 increased in the film layer volumes. All of the composite samples exhibited a much lower refractive
312 index values, compared to these of pure BIG sample, which indicated that the dysprosium oxide
313 diluted the oxide mix sputtered from the $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ target. This could be expected to lead, after running
314 the annealing crystallization process, to forming an incompletely-substituted dysprosium iron
315 garnet composition, volume-diluted by extra dysprosium oxide in a solid-solution-type phase. We
316 know from experiments that many metal oxides (including Dy_2O_3) dissociate during sputtering
317 deposition in pure-argon plasma, since the as-deposited metal oxide layers often require a high-
318 temperature annealing process to regain their expected optically-clear appearance. The absorption
319 coefficient values for all samples deposited were also found to be quite promising (as shown in Fig.
320 12).



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322 **Figure 11.** Refractive index dispersion spectra for $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ composite thin films. The
 323 solid curves were determined according to Cauchy dispersion relationship and the marked data points represent
 324 the calculated n_2 values for each of the samples.

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327 **Figure 12.** Derived absorption coefficient datasets for $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ and $\text{Bi}_3\text{Fe}_5\text{O}_{12}:\text{Dy}_2\text{O}_3$ composite
 328 samples.

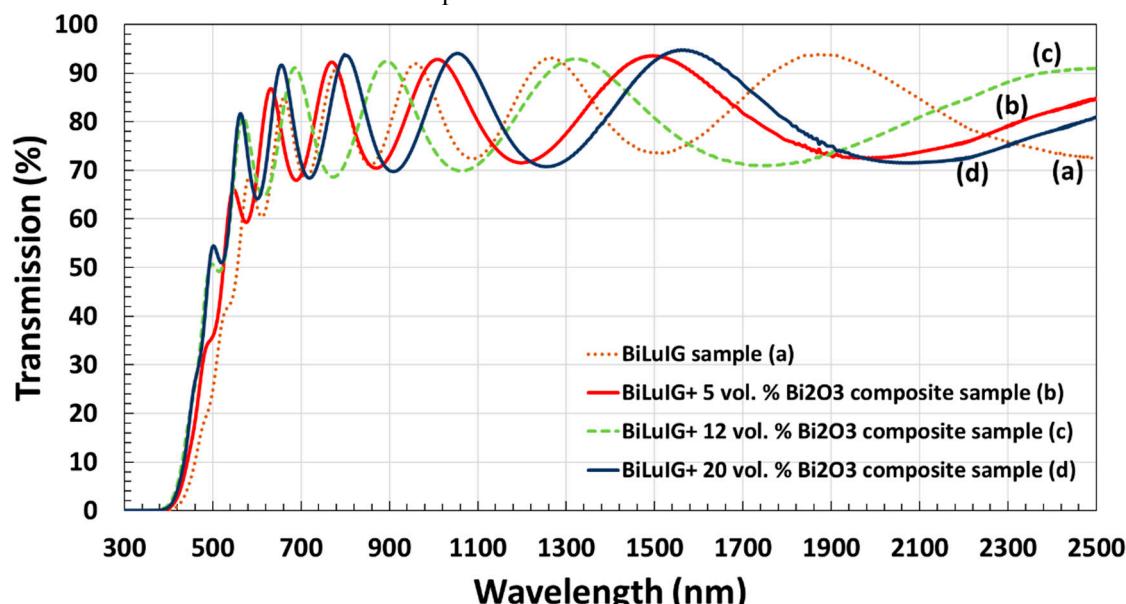
329 The MPC software-based fitting procedure derived the absorption coefficients almost across the
 330 entire visible range for all garnet samples, and these data are plotted in Fig. 12. The effects of Dy_xO_y
 331 dilution are also noticeable, manifesting as rather small changes in the nanocomposite absorption
 332 spectra. The higher the oxide dilution, the higher was the absorption coefficient in the as-deposited
 333 samples. It can be expected that in crystallized (annealed) garnet-type samples, an opposite trend will
 334 be observed: the more Bi atoms in dodecahedral sites replaced by Dy, the small absorption
 335 coefficients.

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337 3.3. Optical study of $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ (5-20 vol. %) composites

338 Highly Bi-substituted lutetium iron garnet thin films of composition type $(\text{BiLu})_3(\text{FeAl})_5\text{O}_{12}$ are
 339 a wonderful subclass of MO garnet materials that features strong in-plane magnetization component
 340 with magnetically-soft switching behaviour suitable for various magneto-optical applications in
 341 nonreciprocal integrated optics, magneto-photonic crystals and waveguides, as well as magnetic field
 342 imaging and sensing devices. Liquid-phase epitaxy (LPE) grown monocrystalline films of a similar
 343 composition type $(\text{BiLu})_3(\text{FeAl})_5\text{O}_{12}$ possessed in-plane magnetic anisotropy suitable for magnetic
 344 flux visualization in high- T_c superconductors [37]. However, LPE technique has some limitations in
 345 terms of achieving high bismuth substitution levels in the films. RF magnetron sputtering is one of
 346 the ideal alternatives to produce high-quality, highly Bi-substituted iron garnet films. A garnet
 347 material with a composition type $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ (BiLuIG) is expected to have a lattice parameter
 348 of 12.384 Å, very close to that of gadolinium gallium garnet (GGG) substrates (12.383 Å), imperative
 349 for the high-quality material growth as well as for the development of practical on-chip MO devices.
 350 Previously, we have reported on the optimization of sputter-deposition process parameters and the
 351 characterization of MO properties in garnet layers of composition type $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$. We have
 352 also experimentally confirmed that the co-sputtering approach ($\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$) improved
 353 the MO quality of these types of garnet materials and allowed to adjust the lattice parameter values
 354 as well [24]. This subsection is intended to provide the experimentally obtained results of the optical
 355 constants study of RF sputtered thin film garnet layers of composition type $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and
 356 also $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ (5-20 Vol. %) composites.

357 Thickness-dependent number of interference fringes has been observed in the transmission
 358 spectra of BiLuIG and $\text{BiLuIG}:\text{Bi}_2\text{O}_3$ garnet composite layers. Figure 13 shows the plots of
 359 transmission spectra of thin garnet layers on glass, for a wide spectral range of 300-2500 nm. The high
 360 amplitude transmission fringes confirmed the achievement of both the good optical homogeneity,
 361 substrate interface quality, and the excellent film surface quality. It can be noticed that all samples
 362 exhibited multiple transmission fringes with large amplitude with high optical transparency. In the
 363 long-wavelength region (especially after 1100 nm), the fringes are found to be much wider spectrally,
 364 compared to those in the short-wavelength region (about 500-1100 nm). The reason is "normal"
 365 refractive index dispersion function (lower index in the long-wavelength range). The very sharp
 366 fundamental absorption edge values are observed in between 400-500 nm. The addition of Bi_2O_3
 367 content pushes the absorption edge towards the shorter wavelength, as can be seen in Fig. 13. The
 368 results of the optical constants study for these material types are summarized in Table S3 (in the
 369 Supplementary section), followed by tabulating the transmission maxima (T_M) and minima (T_m)
 370 values from the obtained transmission spectra.



371
 372 **Figure 13.** Transmission spectra of $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films.

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Figure 14 illustrates the plots of $(l/2)$ versus (n/λ) for all as-deposited BiLuIG and BiLuIG: Bi_2O_3 composite garnet layers, which were found to form straight lines, indicating that relatively high-accuracy film thickness values were obtained. From these simple and appealing graphical presentations, the values of film thicknesses and correct interference order numbers for each sample were calculated, as listed in Table S3, in the Supplementary section. On the other hand, Figure 15 shows the least-square fit of the calculated refractive index (n_2) values, which helped determine the broad-range spectrally-dependent refractive index Cauchy's dispersion model parameters.

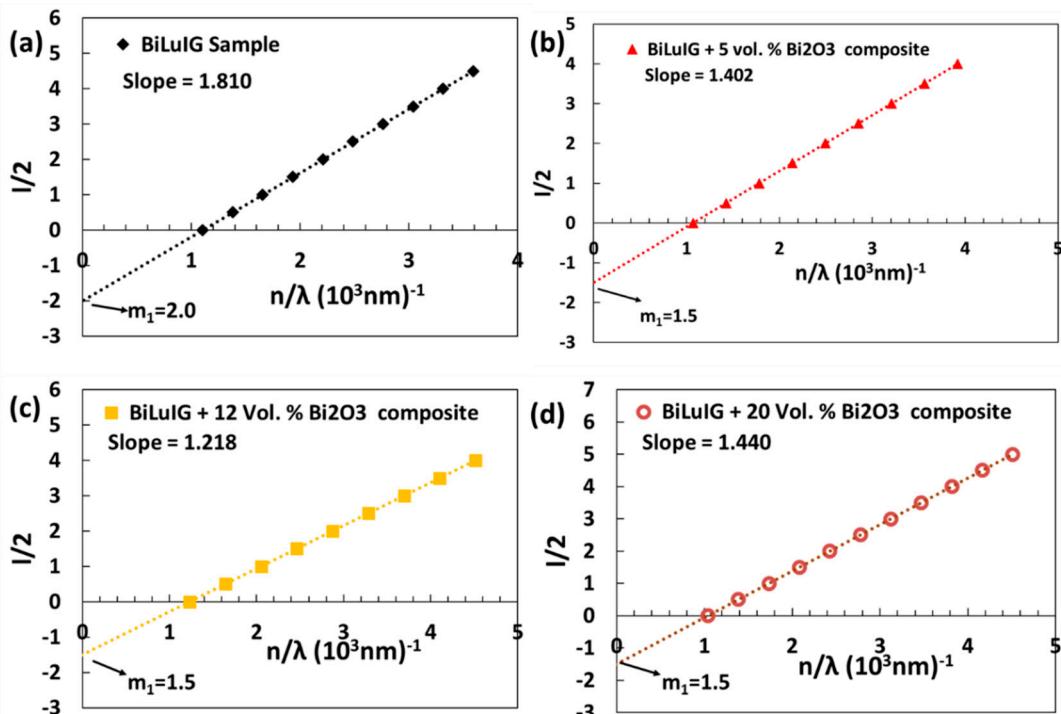
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Figure 14. Plots of $(l/2)$ versus (n/λ) used to determine the film thickness and the first-order values m_1 for $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films.

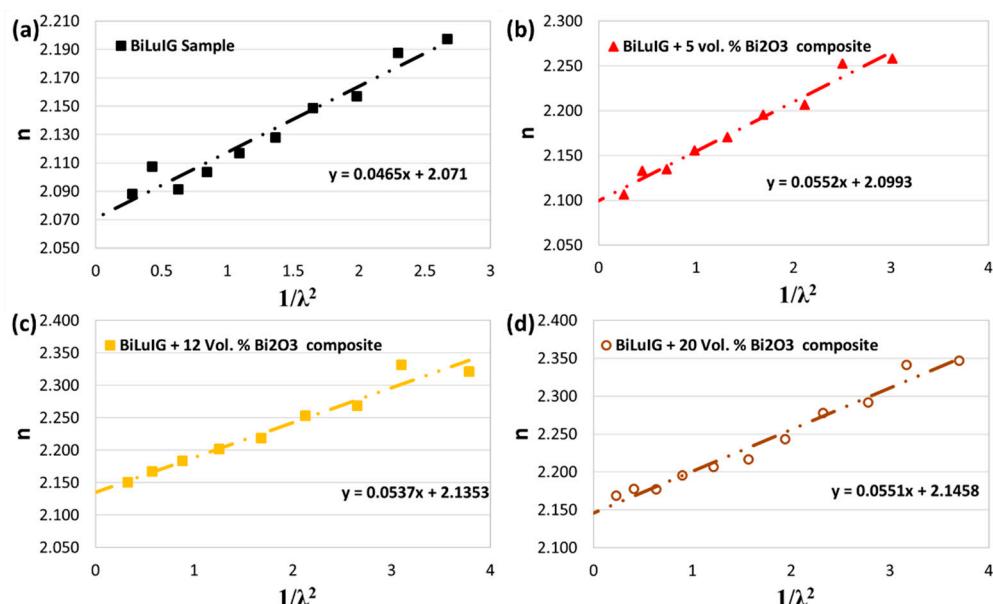
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Figure 15. Least-square fit of the calculated refractive index (n_2) values for $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films.

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The calculated refractive indices at different wavelengths derived from Cauchy's relation as well as the calculated refractive index data points (n_2 values obtained using T_m and T_m) are plotted in Fig. 16. It can be noted that the refractive index (n) is in the range of 2.1-2.5 in the visible region and decreases with increasing wavelength, up to a certain extent. In the long-wavelength region (above 1600 nm), the refractive index seems to be asymptotically approaching a constant value. The volumetric fraction of Bi_2O_3 introduced into the BiLuIG system helps increase the refractive index of the composite films, however, it shifts the absorption edge towards the shorter wavelength region (as seen in Fig. 13). This is expected, in both the as-deposited and also in crystallized samples with high Bi substitution. It can be seen that much lower absorption coefficient has been observed in composite films compared to that of $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ garnet layer as shown in Fig. 17.

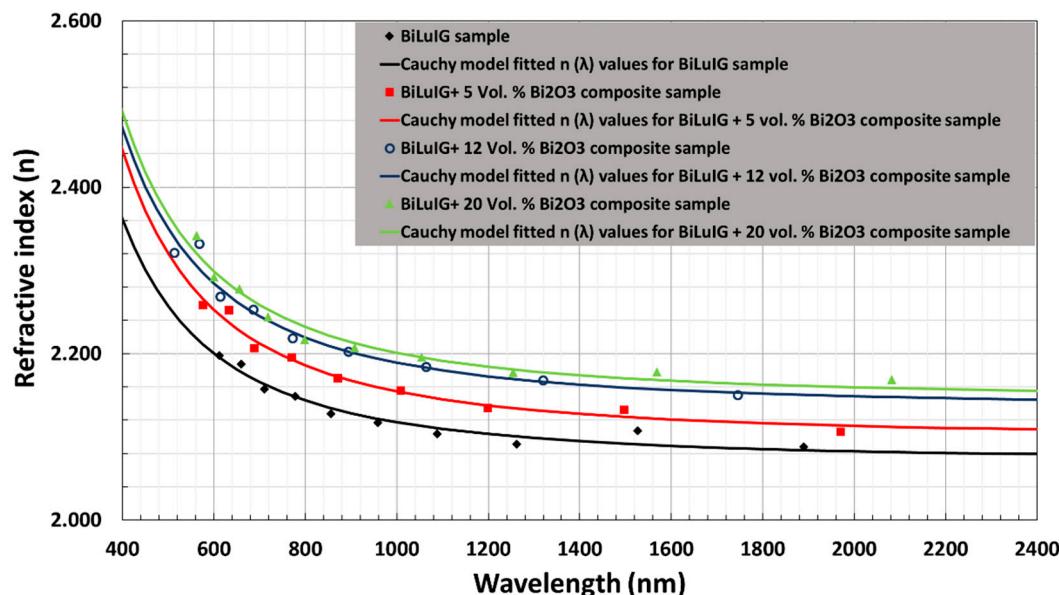
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Figure 16. Refractive index dispersion spectra for $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite thin films. The solid curves were determined according to Cauchy dispersion relationship.

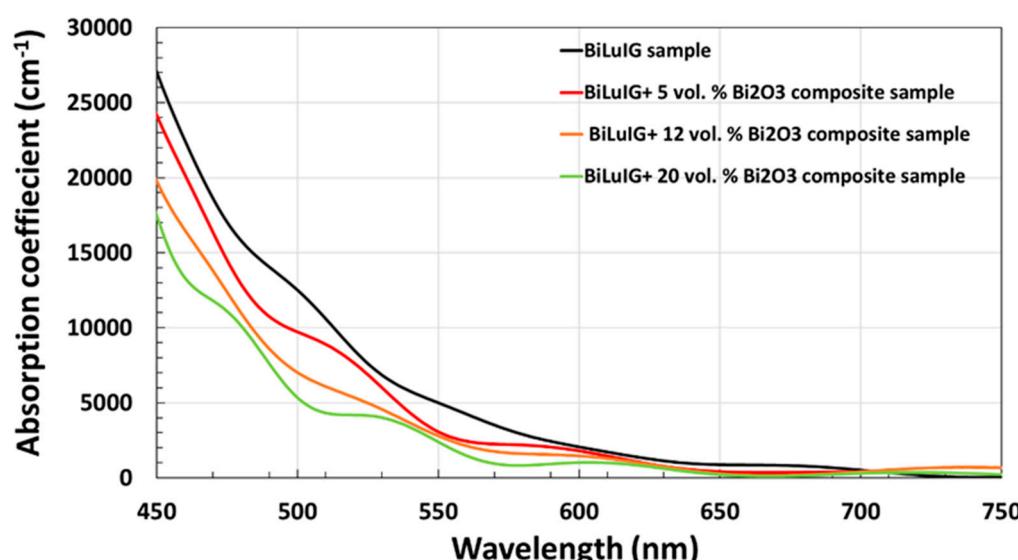
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Figure 17. Derived absorption coefficient and extinction coefficient datasets for the as-deposited $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}$ and $\text{Bi}_{1.8}\text{Lu}_{1.2}\text{Fe}_{3.9}\text{Al}_{1.1}\text{O}_{12}:\text{Bi}_2\text{O}_3$ composite samples.

411 Figure 17 represents the plots of absorption coefficient across most of the visible range for all
412 samples, where the effects of Bi_2O_3 addition can be noticed. The absorption coefficient values decrease
413 with the increasing excess bismuth-oxide content, as expected. Since the as-deposited
414 nanocomposite-type layers are composed of a solid-solution-type mix of several oxides (some of
415 which are metal-rich due to sputtering-induced oxygen loss), the wave-like variations in the spectra
416 are observed (these are not a fitting process artefact). After running composition-optimized annealing
417 crystallization processes, the bulk of film layers will be dominated by garnet phase, partially diluted
418 by the excess oxide. In these layers, strong Faraday rotation is observed, and the “waves” in the fitted
419 absorption coefficient spectra disappear [24].

420 4. Conclusions

421 We have successfully evaluated the optical constants (spectral dependencies of the refractive
422 index for wavelengths between 400 nm to over 2000 nm) for several rare-earth substituted ferrite-
423 type iron garnets and garnet-oxide nanocomposites by using only the transmission spectra datasets.
424 The methodologies used for the derivation of these optical constants datasets have been described.
425 Whilst the datasets have been evaluated in amorphous-phase (as-deposited) RF sputtered films only,
426 a wide range of garnet compositions containing different rare-earth substituting ions have been
427 characterised.

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430 **Supplementary Materials:** The datasets summarized in tables (S1, S2 and S3) are also provided.
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433 **Author Contributions:** M.N.-E.A. performed the experiments and analyzed the data; M.N.-E.A. and
434 M.V. discussed the data and prepared the manuscript; K.A. reviewed and improved the manuscript.
435

436 **Funding:** Electron Science Research Institute, Edith Cowan University, Australia.
437

438 **Conflicts of Interest:** The authors declare no conflict of interest.
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