Flow-induced stresses and displacements in jointed concrete pipes, installed by pipe jacking method

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Abstract: Transient flows result in unbalanced forces and high pressure in pipelines. Under these conditions, the combined effects of flow-induced forces along with sudden pipe displacements can create cracks in the pipeline, especially at the junctions. This situation consequently results in water leakage and reduced operational efficiency of the pipeline. In this study, displacements and stresses in a buried pressurized water transmission pipe installed by pipe jacking method are investigated using numerical modeling and considering interactions between fluid, pipe, and soil. The analyses were performed consecutively under no-flow, steady flow, and transient flow conditions, in order to investigate the effects of flow conditions on displacements and stresses in the system. Analyses of the results show that displacements and stresses in the jointed concrete pipes are significant under transient flow conditions. Moreover, because of pressure transient effects, maximum tensile stresses exceed the tensile strength of concrete at the junctions, leading to cracks and consequent water leakage.

Keywords: Fluid-Structure Interaction, Soil-Structure Interaction, Transient Flow, Pipe Jacking, Numerical Modeling, Abaqus FEA

1. Introduction

Pipe failures are usually a complex function of different circumstances, including pipe properties, internal and external loadings, and environmental factors. Generally, when applied forces exceed the bearing capacity of the pipe materials, failure occurs [1]. Among pipe damage and causes, several failures have been reported due to pressure transient effects [2,3,4]. Transient pressure in pipe networks is generally formed due to factors such as sudden changes in valve operations, starting or stopping of pumps, the sudden change in reservoir level, and changes in the demand conditions. In such cases, the kinetic energy of the fluid is reduced significantly, and pressure waves are transmitted along the pipeline. This high-pressure build-up can damage the pipeline by creating sudden pipe displacements and excessive stresses in the pipe wall [5]. Figure 1 and 2 show stress distribution in a pressurized pipe, and stresses acting on the pipe wall.
In Figure 1, \( P_{\text{out}} \) is the soil overburden pressure on the pipe, \( P \) is the transient pressure of the fluid, \( R \) is the internal radius, and \( e \) is the thickness of the pipe.

According to Figure 2, by considering the existence of two-dimensional axially symmetric stresses in a circular ring subjected to the internal pressure \( P \) and external pressure \( P_{\text{out}} \) (soil pressure), the pipe displacements can be described by Equation 1 and 2, as:

\[
\rho_r \frac{\partial \bar{u}_z}{\partial t} = \frac{\partial \sigma_z}{\partial z} \tag{1}
\]

\[
\rho_r \frac{\partial \bar{u}_r}{\partial t} = \frac{1}{r} \frac{\partial (r \sigma_r)}{\partial r} - \frac{\sigma_r}{r} \tag{2}
\]

By solving Equation 1 and 2, the hoop and radial stresses can be calculated using Equation 3 and 4, as:

\[
\sigma_r = \frac{A}{r^2} + 2C \tag{3}
\]

\[
\sigma_r = \frac{A}{r^2} + 2C \tag{4}
\]

A and C are determined by satisfying the following boundary conditions:

\[
\sigma_r \bigg| \frac{r=R}{r=R} = -P(z,t) \tag{5}
\]

\[
\sigma_r \bigg| \frac{r=R+e}{r=R+e} = -P_{\text{out}} \tag{6}
\]

It follows that:
\[ A = \frac{R^2 (R + e)^2 (P_{\text{out}} - P)}{2(R + 0.5e)e} \]

\[ C = \frac{R^2 P - (R + e)^2 P_{\text{out}}}{4(R + 0.5e)e} \]

Finally, the averaged values of \( \sigma_\phi \) and \( \sigma_r \) are presented in Equation 9 and 10, as:

\[ \sigma_\phi = \frac{1}{e} \int_R^{R+e} \sigma_\phi dr = \frac{R}{e} P - \frac{R + e}{e} P_{\text{out}} \]

\[ \sigma_r = \frac{1}{2\pi(R + 0.5e)e} \int_R^{R+e} 2\pi r \sigma_r dr = -\frac{3}{4} P - \frac{1}{4} P_{\text{out}} \]

In recent years, the use of underground structures such as pressurized water pipes for the distribution of water has increased. Trenched and trenchless drilling are two methods commonly used for the construction of buried pipelines [6]. In the trenched method, the soil is removed to form a trench in the ground, and as the pipes are installed, the trench is filled with soil again. In this method, issues such as reduced enclosing tensions around the pipe, due to lack of proper soil compaction can occur, which can consequently result in inadequate safety and instability of the structure, in the event of pressure transient conditions and pipe displacements [1]. Whereas in trenchless drilling, soil compaction and stresses within the soil are not significantly affected. Pipe jacking is a trenchless drilling technique, used for the installation of underground structures such as pipelines, ducts, and culverts. In this method, powerful hydraulic jacks are used to push concrete or steel pipes through the ground at the same time as drilling is taking place within the shield [7]. In this method, the end connection of a fitting that is to be assembled into another fitting is called “the spigot”, and the female connection of the pipe fitting is referred to as “the socket”. The spigot end of a fitting is inserted into the socket. Spigot and socket joint pipes are joined and sealed using a rubber ring (Figure 3).

Figure 3. The spigot and socket ends of a concrete pipe in pipe jacking method [8]

1.1. Literature Review and Motivation

Kyriakides and Babcock [9] studied the propagation of internal pressures in circular pipes. They concluded that transient pressures cause significant stresses in the pipes. In another effort, Milligan et al. [10] investigated the pipe-soil interactions in the pipe jacking method and proposed a theoretical model for the interactions. Using numerical modeling, Valiente [11] evaluated failures in concrete pipes due to internal pressures. He presented equations to estimate maximum stresses in the pipe. Gysling [12] conducted an experimental study on vibrations and displacements around unburied
pipes due to dynamic flows. He used sensors to measure displacements, and concluded that unsteady pressures could be damaging to the pipeline.

Wasmer et al. [13] investigated the crack growth in straight and bent unburied cast iron pipes under steady internal pressures, and proposed an analytical model. Meis et al. [14] conducted a research study to determine the static and dynamic behavior of some typical restrained and unrestrained underground pipe joints due to internal pressure and earthquakes. Gou [15] studied a pipeline under oblique loading. He demonstrated the effect of pipe burial depth on displacements around the pipe. Schmitt et al. [16] investigated pipeline failure due to dynamic pressure effects in a case study in Tunisia. They used numerical modeling to investigate damages in the pipe. Tijsseling [5] investigated the impact of dynamic pressures in a pressurized pipe, considering fluid-structure interactions. He presented equations for determining tensions and displacements in unburied pipes. Using the finite element method, Lydell and Riznic [17] conducted a survey on the damages to pipes in various projects. They categorized various factors, including internal pressures in the pipe.

More recently, Vazouras et al. [18] investigated the mechanical behavior of buried steel pipelines crossing an active strike-slip fault. They studied the effects of fault displacements and evaluated the critical strain in the pipeline. Wu et al. [19] used a three-dimensional finite element analysis to study the effects of load and displacement-controlled bending on the plastic collapse of pressurized pipes. Rezai et al. [1] studied the impact of transient hydraulic conditions on pipe failures by analyzing historical records and investigating different case studies. Wang [20] used the finite element method to study damages in underground pipes as a function of soil overburden and surface loads. He proposed a method to evaluate the magnitude of damage in pipes within a short period of time as a result of an impact load on the surface. Xu et al. [21] studied the effects of soil overburden and traffic loads on a concrete pipeline. The results indicated that applied loads had considerable impacts on damages to the pipe.

The literature review indicates that flow-induced stresses and displacements in buried pressurized water transmission pipes installed using trenchless drilling (pipe jacking method) have not been investigated. Therefore, this study aims to fill this gap in the literature.

2. Materials and Methods

In this research, a typical water transmission concrete pipe in a soil environment is numerically studied using the Abaqus FEA (Finite Element Analysis) under three scenarios: a) drilling and pipe installation (no-flow condition); b) steady flow in the pipe; c) transient flow in the pipe. General steps for setting up the model are presented in the following sub-sections.

2.1. Model Geometry

Geometries of the soil mass, pipe cross-section, and model boundaries are shown in Figure 4. A long concrete pipe, with internal and external radii of 45 and 50 cm, respectively, was modeled. Model boundaries were determined by trial and error in a way that they show the least impact on analysis results.
2.2. Soil and Material Properties

The geomechanical properties of the soil mass were selected based on the characteristics of normally consolidated clay in urban areas [22]. Moreover, the properties of the pipe were selected based on the characteristics of typical water transmission concrete pipes [23]. Table 1 presents soil and material properties used in the model.

<table>
<thead>
<tr>
<th>Material</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Soil</td>
<td>Log. of Bulk Modulus</td>
<td>0.026</td>
</tr>
<tr>
<td></td>
<td>Poisson’s Ratio</td>
<td>0.4</td>
</tr>
<tr>
<td></td>
<td>Tensile Limit</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>The angle of Internal Friction</td>
<td>23</td>
</tr>
<tr>
<td></td>
<td>Log. of Plastic Bulk Modulus</td>
<td>0.174</td>
</tr>
<tr>
<td></td>
<td>Density (Kg/m³)</td>
<td>1800</td>
</tr>
<tr>
<td></td>
<td>Stress Ratio</td>
<td>0.94</td>
</tr>
<tr>
<td></td>
<td>Initial Yield Surface Size (Pa)</td>
<td>4884</td>
</tr>
<tr>
<td></td>
<td>Wet Yield Surface Size</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>Flow Stress Ratio</td>
<td>0.778</td>
</tr>
<tr>
<td>Concrete</td>
<td>Young’s Modulus (GPa)</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>Compressive Strength (MPa)</td>
<td>28.3</td>
</tr>
<tr>
<td></td>
<td>Tensile Strength (MPa)</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Poisson’s Ratio</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>Density (Kg/m³)</td>
<td>2500</td>
</tr>
<tr>
<td>Water</td>
<td>Density (kg/m³)</td>
<td>1000</td>
</tr>
<tr>
<td></td>
<td>Bulk Modulus (GPa)</td>
<td>2.7</td>
</tr>
</tbody>
</table>

2.3. Flow Characteristics

Internal pressure and flow velocity in the pipe under steady flow condition were selected to be 0.5 MPa (72.52 psi) and 4 m/s, respectively, as typical values in urban water transmission pipes.

2.4. Modeling Procedure

In the present study, the general assumptions that were necessary to model the FSI (fluid-structure interaction) problem are as follows:

- The surrounding soil is monolithic.
- The concrete lining behavior is considered as non-linear.
- A damage plasticity behavior is considered in the concrete lining.
- The CPE8R (8-node plane strain quadrilateral, biquadratic displacement, reduced integration) elements are used for the simulation of the concrete pipe.
- Based on the Cam-Clay criterion, the soil is considered as a plastic material.
- Dynamic explicit method is applied to solve the finite element equations in the Abaqus FEA.

2.4.1. Acoustic Environment

Inside a pressurized water pipe, the only degree of freedom in nodes of the finite element model of the fluid is pressure. In Abaqus FEA, acoustic environments and acoustic materials possess this feature. An acoustic environment is an elastic environment where no shear stress is present (assuming non-viscous fluid), and the pressure is proportional to volumetric strain. Acoustic environments consider the effects of inertia and fluid compressibility. Pressure wave propagation can also be simulated in these environments [24]. Therefore, in this study, acoustic elements were
implemented to simulate fluid motion in the pipe, in order to investigate the impact of transient pressures on pipe displacements and the distribution of stresses in the pipe wall.

2.4.2. Interactions Between Model Components and Meshing

As stated above, the only variable in the acoustic environment is pressure. The value of this variable was applied to each node by applying initial conditions using a quasi-static wave method [25]. The interactions between the pipe and fluid were introduced to the model by coupling displacement matrixes of the inner pipe surface with displacement matrixes of the fluid boundary elements. Moreover, the interactions between the pipe and soil were introduced to the model by defining cohesive elements between the soil and the outer pipe surface. Figure 5 shows the meshing of the soil, pipe, and fluid environments in a 3D view.

Figure 5. Finite element model mesh – 3D View

2.4.3. Transient Flow in The Pipe

To create transient flow in the pipe, it was assumed that 90% of a valve on the path was closed. In this condition, based on hydraulic analysis using the method of characteristics (MOC) [26], flow velocity upstream of the valve will reach 1 m/s, and pressure waves will form in the pipe. Figure 6 shows the change in flow velocity as a result of the relative valve closure percentage and the closure time. The flat lines in the figure continue until the end of the simulation time.

Figure 6. Flow velocity upstream of the valve and relative valve closure
If the time it takes to close the valve is less than wave travel time, the change in pressure head can be obtained using Equation 11 [27]. According to Figure 6, the time it takes to close 90% of the valve is about 15 s, while the wave travel time is about 59 s. Therefore, Equation 11 is applicable.

\[
\Delta H = \frac{a \Delta V}{g}
\]

\[
a = \sqrt{\frac{1}{\rho_w \left( \frac{1}{k_w} + \frac{d}{E e} \right)}}
\]

In Equation 11, \( \Delta H \) (m) is the change in pressure head, \( a \) (m/s) is the pressure wave velocity, \( g \) is the acceleration of gravity, and \( \Delta V \) (m/s) is the change in water velocity in the pipe. In Equation 12, \( \rho_w \) (kg/m³) is the specific mass of water, \( k_w \) (GPa) is the bulk modulus of water, \( d \) (m) is the pipe diameter, \( E \) (GPa) is the modulus of elasticity of concrete, and \( e \) (m) is the thickness of the pipe [28].

The calculated values for \( a \) and maximum pressure under the transient flow condition are presented in Table 2.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( a ) (m/s)</td>
<td>854</td>
</tr>
<tr>
<td>Max. Pressure (MPa)</td>
<td>2.61 (378.55 psi)</td>
</tr>
</tbody>
</table>

The calculated maximum transient pressure was applied to fluid elements in the model as impact load. The transient pressure from fluid elements transfers to pipe elements, leading to pipe displacements and stresses in the pipe wall.

3. Results

In the following sections, displacements in the soil environment and stresses in the pipe wall are presented. Displacements under all scenarios are measured relative to their position right after drilling and pipe installation (before reaching a new equilibrium). The location where displacements and stresses are analyzed is near the valve, and the displacements in each stage are cumulative.

3.1. No-Flow Condition

Figure 7 and 8 show vertical (\( U_2 \)) and horizontal (\( U_1 \)) displacements in the soil environment, respectively, and Figure 9 shows stresses in the pipe wall under no-flow condition. In Figure 9, as well as in other figures showing stress distribution contours in the following sections, the blue color shows areas in compression, while red shows areas in tension.

Figure 7. Displacements in the vertical direction under the no-flow condition
After drilling and pipe installation, distribution of stresses in the soil will change, and eventually, due to the stress release phenomenon, the soil mass will reach a new equilibrium. Figure 7 shows that soil at the bottom of the section has become swollen. The amount of this uplift at the bottom (5 mm) is greater than the amount of displacement in the crown (1 mm). According to Figure 8, horizontal displacements on the top and bottom sides are quite symmetrical and uniform, with a maximum of 3 mm on the sides. Therefore, under the no-flow condition and due to unloading and inflation of the soil, among all displacements, the greatest occurs at the bottom.

Stress distribution contours mostly show compression (blue) at the top and tension (red) at the bottom of the pipe (Figure 9). Under this condition, the highest tensions occurred at the bottom of the pipe with a maximum value of 2.69 MPa (390.15 psi) at the junction.

### 3.2. Steady Flow Condition

Figure 10 and 11 show vertical (U2) and horizontal (U1) displacements in the soil environment, respectively, and Figure 12 shows the stresses in the pipe wall under steady flow condition.
As mentioned earlier, in this scenario, the pressurized pipe is operating under a steady flow with 0.5 MPa (72.52 psi) of pressure. Due to this pressure, as well as the fluid weight, the concrete pipe moves, and this displacement transfers to the surrounding soil. As a result, displacements that took place under no-flow condition will change. The figures show that the maximum displacement under the steady flow condition is 1 mm, both in vertical and horizontal directions. This value is obtained from the maximum vertical pipe displacement difference in Figure 7 and 10. The same value is obtained by comparing horizontal displacements in Figure 8 and 11.

Similar to the no-flow condition, stress distribution contours mostly show compression at the top, and tension at the bottom of the pipe (Figure 12). Under this condition, due to the addition of the...
internal pressure, the highest tensions occurred at the bottom of the pipe, with a maximum value of 3.86 MPa (559.85 psi) at the junction.

3.3. Transient Flow Condition

Figure 13 and 14 show vertical ($U_2$) and horizontal ($U_1$) displacements in the soil environment, respectively, and Figure 15 shows the stresses in the pipe wall under transient flow condition.

![Figure 13. Displacements in the vertical direction under transient flow condition](image1)

![Figure 14. Displacements in the horizontal direction under transient flow condition](image2)

![Figure 15. Stresses in the pipe wall under transient flow condition (MPa)](image3)

According to Figure 13 and 14, relative to steady flow condition, displacements in the soil have increased under the influence of transient pressures in the pipe. The results obtained at this stage indicate that maximum displacements occurred at the upper portions of the section, with a maximum value of 3.1 mm in the crown.
Similar to the two previous conditions, stress contours show areas under compression at the top and areas under tension at the bottom of the pipe. In the event of a transient flow, the maximum tension remained at the bottom of the pipe, with a maximum value of 8.1 MPa (1174.81 psi) at the junction.

4. Discussion

In Figure 16, the absolute value of total displacements (resultant of vertical and horizontal displacements) under each scenario are shown. $U_{\text{no-flow}}$, $U_{\text{steady}}$, and $U_{\text{transient}}$, refer to total displacements under no-flow, steady flow, and transient flow conditions, respectively.

![Figure 16. Total displacements under: no-flow, steady flow, and transient flow conditions](image)

Figure 16 shows that under the no-flow condition, maximum displacements occurred at the bottom of the section, which can be attributed to soil inflation, as a result of unloading the soil, soil overburden, soil type, and distribution of loads in the drilled environment. Under steady flow condition, the greatest displacement occurred at the bottom of the section, which can be attributed to the internal pressure, fluid weight, and soil overburden. Finally, under transient flow condition, the entire section of the pipe moved upward, and the maximum displacement occurred in the crown.

Concerning stresses, junctions were the most critical points. In all cases, the maximum compressive and tensile stresses were formed at the junction.

Table 3 summarizes the maximum displacements along with the maximum compressive and tensile stresses in the pipe wall under each scenario.

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Max. Displacements (mm)</th>
<th>Max. Stresses (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Vertical</td>
<td>Horizontal</td>
</tr>
<tr>
<td>No-flow condition</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>Steady flow</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Transient flow</td>
<td>4</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure 16 shows that under the no-flow condition, maximum displacements occurred at the bottom of the section, which can be attributed to soil inflation, as a result of unloading the soil, soil overburden, soil type, and distribution of loads in the drilled environment. Under steady flow condition, the greatest displacement occurred at the bottom of the section, which can be attributed to the internal pressure, fluid weight, and soil overburden. Finally, under transient flow condition, the entire section of the pipe moved upward, and the maximum displacement occurred in the crown.

Concerning stresses, junctions were the most critical points. In all cases, the maximum compressive and tensile stresses were formed at the junction.

Table 3 summarizes the maximum displacements along with the maximum compressive and tensile stresses in the pipe wall under each scenario.

Considering the range of 2.2 to 4.2 MPa for the tensile strength of concrete, under transient flow condition, the tensile stress in the concrete pipe wall exceeds this range. High tensile stresses will cause cracks in the pipe wall, especially at the junctions, and consequently result in water leakage, soil wash, and generally reduced operational capacity of the pipeline.

5. Conclusions

A concrete water transmission pipe installed underground in ordinary compacted clay soil using trenchless drilling (pipe jacking method) was modeled in Abaqus FEA. The purpose of this study was to investigate flow-induced stresses in the pipe wall and displacements in the soil environment, under no-flow, steady flow, and transient flow conditions in the pipe. The following are the key findings of this study:
• Under the no-flow condition, the most significant displacements occurred at the bottom of the section. This can be attributed to the soil inflation phenomenon, as a result of drilling and alteration of stress distribution in the soil environment.

• Under steady flow condition, the soil environment showed small displacements, due to the internal pressure and fluid weight in the pipe.

• By the occurrence of transient pressure due to the event of transient flow in the pipe, the displaced region was enlarged, and the pipe and surrounding soil showed an upward movement.

• Under all scenarios, maximum compressive and tensile stresses were formed at the junction. The maximum value was observed under the transient flow condition, where the tensile stress exceeded the allowable tensile capacity of the concrete. This situation will cause cracks in the pipe wall and consequently leads to water leakage and reduced operational capacity of the pipeline.

Future work can be done on optimizing the valve closure pattern, considering the internal pressure in the pipe, existing soil overburden on the pipe, and soil type, in order to minimize transient pressures and resultant pipe displacements. Moreover, a comprehensive parametric study can be performed on different model components to investigate the impact of each parameter on the model results.

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