

Technical Note

Detection of Glacier Calving Margins with Convolutional Neural Networks: A Case Study

Yara Mohajerani ^{1*}, Michael Wood ¹, Isabella Velicogna, ^{1,2} and Eric Rignot ^{1,2}

¹ University of California, Earth System Science, Irvine, CA 92617, USA

² Jet Propulsion Laboratory, CA 91109, USA

* Correspondence: ymohajer@uci.edu

Abstract: The continuous and precise mapping of glacier calving fronts is essential for monitoring and understanding rapid glacier changes in Antarctica and Greenland, which have the potential for significant sea level rise within the current century. This effort has been mostly restricted to the slow and painstaking manual digitalization of the calving front positions in thousands of satellite imagery products. Here, we have developed a machine learning toolkit to robustly and automatically detect glacier calving front margins in satellite imagery. The toolkit is based on semantic image segmentation using Convolutional Neural Networks (CNN) with a modified U-Net architecture to isolate the calving fronts from satellite images after having been trained with a dataset of images and their corresponding manually-determined calving fronts. As a case study we train our neural network on a varied set Landsat images with lowered resolutions from Jakobshavn, Sverdrup, and Kangerlussuaq glaciers, Greenland and test the results on novel images from Helheim glacier, Greenland to evaluate the performance of the approach. The neural network is able to identify the calving front in new images with a mean deviation of 96.3 m from the true fronts, equivalent to 1.97 pixels on average, while the corresponding error for manually-determined fronts on the same resolution images is 92.5 m. We find that the trained neural network significantly outperforms common edge detection techniques, and can be used to continuously map out calving-ice fronts with a variety of data products.

Keywords: Calving Front; Image Segmentation; U-Net; Convolutional Neural Network; Machine Learning; Greenland

1. Introduction

In recent decades, tidewater glaciers discharging ice from the Greenland Ice Sheet have been thinning, speeding up and retreating inland [1–6]. The position of glacier ice fronts reflects a delicate balance of advection and ablation processes [7] and hence is an important proxy for the impacts of regional changes in climate and ocean state on the mass balance in the Greenland Ice Sheet. To assess records of ice front retreat over time, ice front positions are typically manually digitized from aerial imagery [4] or satellite imagery [2,5] using geographic information software. Since the launch of Landsat 5 in 1984, the Landsat fleet has captured images of the Greenland Ice Sheet with a repeat cycle of 16 days. However, because the manual ice front digitization process requires a considerable time investment, most current records of calving front retreat are limited to only a few ice front positions per glacier per year, if any. This shortage of data has limited assessments of ice front retreat to an annual basis, yet seasonal factors may be critical to understanding the pattern of long term retreat of Greenland's glaciers [8] or to understand for instance the level above which a glacier may be pushed out of balance compared to its state of seasonal, natural variability [6]. In effect, an automated system to rapidly delineate calving front positions would provide a foundation for understanding regional changes on the periphery of the ice sheet over the past several decades, especially with the emergence

of a new generation of satellites with high data volume, a high number of acquisitions and higher resolution (e.g. [9], [10], [11], [12].)

Detecting glacier calving fronts in images falls under a more general category of problems that deal with image segmentation. Generally, image segmentation techniques focus on either dividing an image into different regions (e.g. clustering, classification, region extraction) or finding the boundaries between regions (i.e. detection of discontinuities, edge detection). A detailed overview of these categories and techniques is given by Fu and Mui [13]. Various techniques have been developed in the past for this class of problems. One of the most prominent of these analytical techniques is the Sobel filter, which uses gradients with a given threshold to detect edges [14]. Other approaches include the "Scale-Space" technique, which, first developed by Witkin *et al.* [15], detects the desired feature at a coarser scale and tracks it continuously at a higher resolution. This approach was further improved by Perona and Malik [16] by using an anisotropic diffusion process to keep the spatial accuracy of the features and detect edges. Applying these techniques to geophysical images such as ice-covered fjords and geologic formations is challenging due to the noisy nature of the data, variable atmospheric conditions (particularly clouds) and temporal changes on the ground. Seale *et al.* [3] analyzed the evolution of calving fronts for 32 glaciers in Greenland using a Sobel filter as well as a brightness profiling technique applied to MODIS data. While achieving reasonable results below the resolution of MODIS (0.25km), this approach relies on the proper selection of subregions around the calving front and heavy use of quality assurance and post-removal of anomalies. Furthermore, analytical techniques relying on brightness gradients in images are dependent on the particular nature of the data. For example, the same gradient thresholds may not be applicable to other instruments and spectral bands. They would also not be applicable to other data types such as radar interferometry (see Massonnet and Feigl [17]). Finally, while this process provides an approximation of overall glacier retreat, it does not yield a digitized-front product which can be used by the glaciological community.

An alternative approach for overcoming these problems is the use of deep neural networks (see LeCun *et al.* [18]) that can be trained on any data type to detect glacier fronts. Image segmentation techniques have improved rapidly in recent years due to the progress in deep learning and semantic image segmentation with convolutional neural networks (e.g. see Krizhevsky *et al.* [19]). Large neural networks with thousands or millions of parameters have allowed much more accurate classification and segmentation of images. In fact, deep neural networks with rectified activation units have already surprised human performance in some visual recognition tasks (see He *et al.* [20]).

The issue with such deep neural networks for image segmentation is the need for very large training datasets where the desired features (in this case calving fronts) have already been determined for thousands of images. For many fields of research the shortage of vast training data limits the use of such tools. However, a recent deep neural network architecture developed for biomedical image segmentation, U-Net [21], has been shown to provide highly accurate image segmentation with minimal training data through the use of data augmentation in a deep convolutional neural network. Here we develop a modified version of the U-Net architecture that can robustly identify and extract glacier calving fronts from optical satellite imagery. We discuss our results for a set of glaciers on the Greenland ice sheet. We compare our trained network with the Sobel filter. We conclude on the application of CNN technology to the detection of ice sheet calving margins.

2. Materials and Methods

We detect and reconstruct glacier calving fronts from Landsat imagery with the use of an image segmentation technique that relies on a deep convolutional neural network using a modified U-Net architecture [21]. The methodology is divided into three overarching areas:

1. Discussion of raw satellite images, production of training data, and pre-processing of images before training
2. Semantic image segmentation and the architecture of the neural network

3. Reconstruction of new calving fronts on new data and the post-processing of the outputs of the neural network

Figure 1 summarizes the steps required to pre-process the data, train the network, make predictions, and get the glacier front positions after post-processing. Each of these steps are discussed in the following sections.

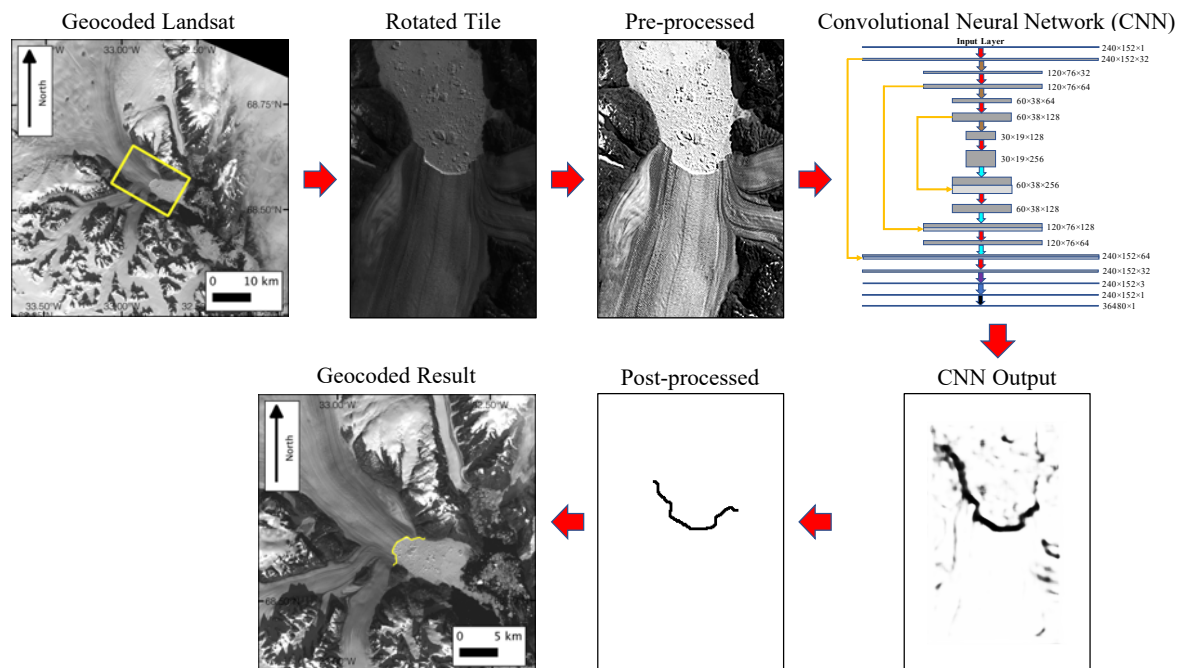


Figure 1. The outline of our methodology: Geocoded Landsat images are trimmed and rotated so that glacier flow is in the y-direction. The images are pre-processed and fed into to a Convolutional Neural Network (CNN) for training (refer to Figure 2 for a zoomed-in version of the CNN panel). The CNN is used to predict new calving front positions, which are post-processed and converted back to geocoded images.

2.1. Data and Pre-Processing

We retrieve Level 1 Landsat Data from the USGS Earth Explorer portal for Landsat 5, Landsat 7, and Landsat 8. For Landsat 5, we utilize the “green” band (0.52–0.60 μm) with a resolution of 30 m, while for Landsat 7 and 8 we utilize the “panchromatic” band (0.52–0.90 μm and 0.503–0.676 μm respectively) with a resolution of 15 m. The scenes are delivered in the UTM projection corresponding to their longitude and latitude to maintain linear and areal distances. We splice the images to the region around the glacier ice front with a buffer of 300 m, an area we define using ice fronts that have previously been digitized manually.

In order to make it easier for the Neural Network (NN) to detect glacier fronts, we perform a series of pre-processing steps on the input images. Firstly, the spliced input images are processed to be of uniform size (200 \times 300 pixels) and oriented such that the glacier ice flow is in the y-direction for consistency, in order to improve the performance of the NN across a variety of images. Because the total retreat distance varies between glaciers, the scale of the 200 \times 300 pixel images will also vary. In effect, the resolution of the image subsets are different for each glacier and the approach described herein does not operate on the native resolution of the Landsat products, but rather provides a benchmark for evaluating the performance of different neural network configurations compared to the analytical filter and manual results. The lower resolution images reduce computational resource and training time requirements for our case study. The pixel resolution varies per fjord based on the span of the retreat distance of each glacier over time. The pixel resolutions are as follows: 61.4 m

for Sverdrup, 57.7 m for Kangerlussuaq, and 88.1 m for Jakobshavn. The pixel resolution of the test images on Helheim glacier is 49.0 m. Note that the test data has the highest resolution, allowing us to test the ability of the NN to be tested on slightly higher resolution images after being trained on a range of various lower resolutions. The corresponding calving front targets, hereinafter referred to as "labels", are rasterized as single-pixel-thick lines for maximal spatial precision. We also further crop the input images to a size of 150x240 pixels with the aim of improving the training time and performance of the neural network while keeping all the calving fronts within the image frame. In addition, the architecture of the NN requires the dimensions to be divisible by the number of downsampling steps. With three downsampling layers, the images are padded to be divisible by 8 (see Figure 2), resulting in 240×152 images.

Furthermore, we apply a series of alterations to the images to make the input more suitable for training the neural network. After a series of experiments with high-pass and low-pass filters, changes of contrast, and application of preliminary edge-detection algorithms, we find the optimal pre-processing steps to be as follows: First, we normalize the image contrasts such that the darkest and lightest points in every image are black and white, respectively. Next we equalize the gray-scale intensities to create a uniform distribution, followed by smoothing and edge-enhancement of the images.

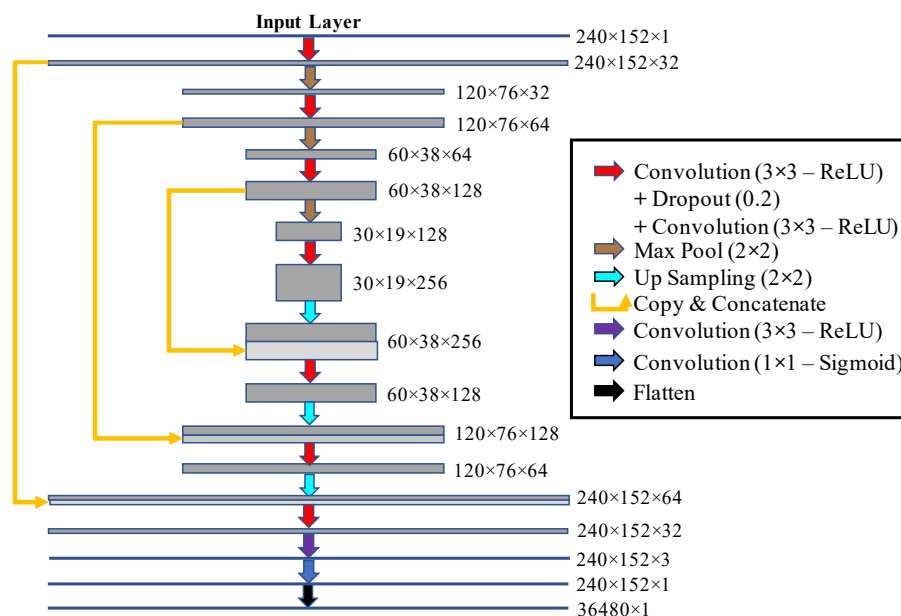
2.2. Semantic Image Segmentation

We develop a Convolutional Neural Network (CNN) [22] with a U-Net architecture [21] with custom sample weights for the segmentation of glacier fronts. U-Net has been very successful for semantic segmentation of biomedical images. It is built based on the architecture of Fully Convolutional Networks (FCN) [23]. The challenge in semantic segmentation is resolving desired features ("what") and their contextual location ("where"). The idea of FCN is to combine fine, detailed features with coarse, contextual information. U-Net is a modification of such an architecture, which can be conceptualized as having two main components: 1) A "down" component that uses convolutional layers to detect desired features in images in progressively smaller layers with higher numbers of filters or "feature channels", and 2) An "up" component that has up-sampling layers to convey contextual information to higher resolution layers and reconstruct output images through convolutional layers. Convolutional layers consist of a series of kernels that are convolved across the input, mapping each group of pixels into single values in a new layer. These kernels act as filters that map out particular features from the image (such as features associated with glacier fronts). See LeCun *et al.* [18] for a discussion of convolutional neural networks. During the "down" component, pooling layers are applied to downsample the output of each set of convolutional layers [18]. This dimensionality reduction is a way of introducing location-invariance by combining similar features and coarsening the output of the convolutional kernels. In our neural network we use 2×2 max-pooling layers, which take the maximum value between each group of 4 pixels, resulting in location invariance within local batches and faster convergence of the network [24]. In the second stage, the images are upsampled by doubling the rows and columns of the previous layer (by repeating the rows and columns) and concatenated with the last convolutional layer with the same dimensions as the upsampled image. Thus, the detailed global features in the last convolutional layer are combined with the contextual information of the previous layer. This combined upsampled layer is then fed to convolutional layers, as before. The reconstructed image by the last convolutional layer will have the same size as the input images and contain the desired segmented features.

The architecture of our neural network is depicted in Figure 2. Our network is composed of 29 total layers, with 3 downsampling steps and 4 sets of convolutional layers going from 32 to 256 feature channels and the corresponding upsampling steps. We apply 3×3 convolutional layers with padding (such that the output of each convolutional layer has the same image size as the input) and a stride of 1. We use Rectified Linear Units (ReLU) [25] as our non-linear activation function, which has been shown to be very successful in convolutional neural networks [18]. In

order to apply regularization and avoid over-fitting to training data, we use Dropout layers [26] between convolutional layers with an elimination fraction of 0.2. This randomly drops some units at each iteration from the neural network in order to minimize over-fitting and excessive reliance on individual units. We find that increasing the dropout fraction significantly increases the “noise” (number of false-positives) in our results. Our downsampling is performed by 2×2 MaxPooling layers with no padding and strides of 2. Therefore, at every step the height and width of the layer is reduced by half while the number of convolutional kernels (also known as feature channels) doubles. The same convolution→dropout→convolution architecture is used in the upsampling stage, where the number of feature channels is halved in each iteration. The 2×2 upsampling is done by repeating the rows of and columns of the previous layer, and concatenating the resulting matrix with the corresponding higher-resolution layer. We get performance improvements by also adding a final 3×3 ReLU convolution to go from the final 32 channels to 3, followed by a Sigmoid convolution layer to get the final reconstructed image. The architecture of the network is also summarized in Table S1.

We use a binary cross-entropy loss function (see Mannor *et al.* [27]) with custom sample weights for each input image. Note that images of glacier fronts pose a severe class imbalance problem, since the vast majority of pixels are not calving fronts. As a result, the NN learns to obtain high accuracy by simply classifying every pixel as not being part of the calving front. To avoid this false-negative classification artifact, we develop custom sample weights such that for every training example the pixels containing calving fronts have much higher penalties in the loss function if misidentified. In order to have an equal contribution from each class of pixels, the weight is determined as the average ratio of the number of non-boundary pixels to pixels including glacier front boundaries, which is 241.15 in our training set with 123 240 \times 152 input images. We also take advantage of data augmentation by mirroring the horizontal orientation of glaciers and inverting the grayscale intensities to mimic different shadows. However, we get accurate results even without the use of augmentation, which speeds up the training process (discussed in the next section).



delineate the fjord walls. Note that these polygons only need to be defined once per glacier and may be used for all additional fronts obtained via the NN. We iterate through pairs of pixels on the fjord boundaries to find a least-cost path through the array, where the weights of each “step” are given by the output of the NN. A 500 m buffer is used from the fjord walls. The extracted path of pixels with the least weight is identified as the ice front, and converted to the geographical coordinates of the original spliced Landsat scene used to generate the subset. The geographical coordinates are stored as both arrays and shapefiles which may be used in geographical information systems.

3. Results

We train the neural network on a set of 123 preprocessed 240×152 input images from Jakobshavn, Sverdrup, and Kangerlussuaq glaciers. Note that while this may seem like a limited number of training instances, one of the advantages of the utilized network architecture used in this study is its ability to perform well with an extremely limited set of training data. In fact, the U-Net architecture used by Ronneberger *et al.* [21] used a training set that consisted of $30\,512 \times 512$ pixel images. Training success with few training images is in part enabled by data augmentation, which plays an important role in reducing our output errors, as discussed below. We leave aside 10% of the images for cross-validation during training. The validation dataset is used to prevent overfitting. The training is halted when the validation loss starts to increase as a result of overfitting. In addition, in order to test the ability of the neural network to predict calving fronts beyond the training set for different glacier geometries, we test the trained network on images of Helheim glacier, whose geometry is unknown to the NN during training. Note that this test dataset is in addition to the cross-validation data used during training. We minimize the custom-weighted binary cross-entropy loss function discussed in Section 2 using the Adam optimizer [28] with batches of 10 images at a time. Furthermore, we use a variable learning rate, which is reduced by half after every 5 epochs without any improvements to the accuracy. We test the performance of a variety of NN configurations (discussed in the next section) and find that training the NN described in Figure 2 with horizontal mirroring augmentation with batches sizes of 10 leads to excellent agreement between the “generated” and “true” fronts. Training the network for 54 epochs leads to an accuracy of 92.4% in the training set and 93.6% in the validation set, after which the validation loss starts to increase as a result of over-fitting. Figure 3 shows the result of the NN network on a particularly noisy test image.

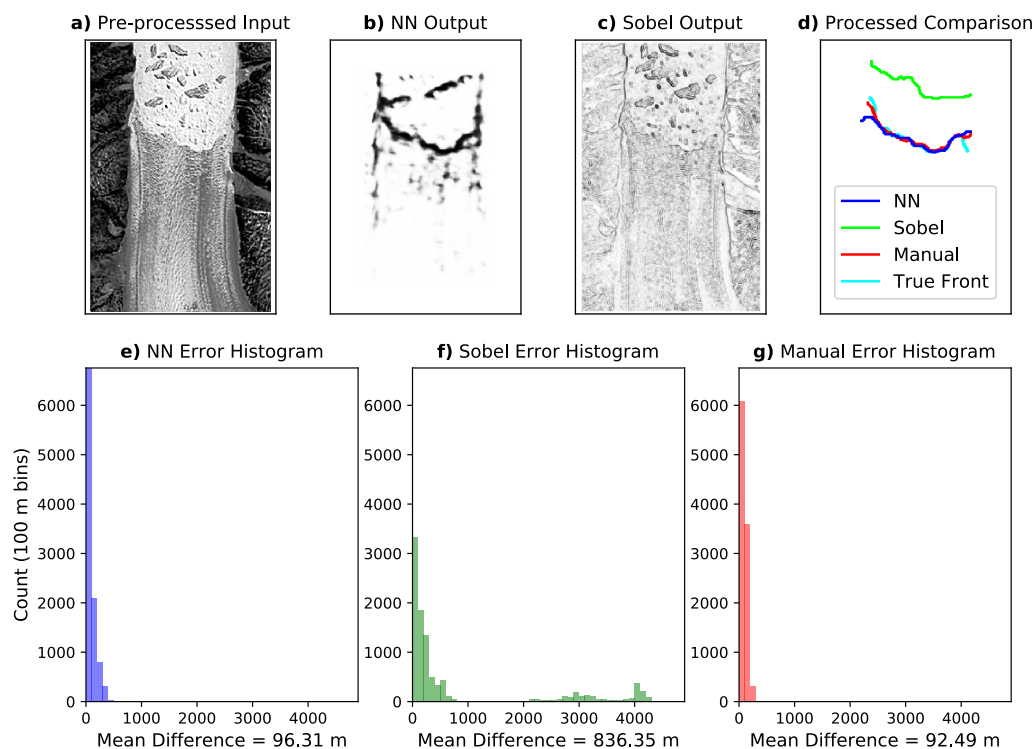


Figure 3. The output of the neural network shown for a sample test image of Helheim Glacier from Landsat 5. The pre-processed input image is shown in Panel (a). Panels (b) and (c) show the raw outputs of the neural network and the Sobel filter, respectively. Panel (d) depicts the corresponding extracted calving fronts compared to the true front, with the addition of the manually-determined front on the same resolution rasterized image used for the NN and Sobel filter. Note that the output of the NN shows remarkable agreement with the true front. Panels (e), (f), and (g) show the distribution of differences between the generated and true fronts across *all* test images, with the corresponding mean differences with the true fronts for the NN, Sobel, and manual results, respectively.

Panel (a) shows the pre-processed input image. Note that we pick this example as an instance of an image that can mislead analytical edge detection filters, but the reported results and errors are drawn from the complete test dataset. The raw output of the NN is shown in Panel (b). It is evident that the neural network is able to extract the calving front from the input image. Figure 3 also compares the output of the NN to the Sobel filter, a common analytic edge detection algorithm that has been used in previous studies (e.g. see Seale *et al.* [3]). It is clear from Panel (c) that the Sobel filter is very sensitive to noise and identifies many gradients in the texture of the glacier, the icebergs, and the surrounding topography as calving boundaries, which could lead to a false identification of the position of the calving front. Panel (d) shows the extracted fronts in post-processing (as discussed in Section 2.3). Note that we have also included a manually-determined front in addition to the “true” front. While the true front has also been determined manually on high resolution geocoded data, the “manual” comparison in Figure 3 refers to hand-drawn fronts on the pre-processed lower resolution rasterized images that are also used for the NN and Sobel processing for an equal comparison of the performances. The neural network performs remarkably well compared with the true boundary. However it is evident that the Sobel filter is not able to extract the calving front as accurately as the NN. Furthermore, the performance of the neural network appears to be comparable to manually-determined front. Results for other test images are provided in the Supplementary Material.

While Panels (a)-(d) of Figure 3 showcase the output of one image, Panels (e) and (f) show the error analysis obtained from the complete set of test images for the NN, Sobel filter, and manual

results. We quantify the errors by breaking the extracted calving fronts of Helheim glacier (which was not used during training) into 1000 smaller line segments and calculating the mean difference between the corresponding segments of the generated and true fronts. Figure 3 shows the distribution of the differences for the NN (e) the Sobel filter (f), and manual results (g). We calculate the total error in the glacier fronts as the mean deviation between all of the line segments in the outputted and true glacier front boundaries. The NN has a mean difference of 96.3 m, equivalent to 1.97 pixels, which is more than 8 times smaller than that of the Sobel filter. The manual output has a mean error of 92.5 m, only slightly below the error of the NN. Most of the error in the NN output is attributed to the edges of the calving front, as can be seen in the Supplementary Material. Furthermore, it appears that the Sobel errors have a multimodal distribution. In other words, when the Sobel filter identifies the correct gradient as the calving front, it is in good agreement with the NN results. However, the filter can be easily misled by other gradients in the image, resulting in a complete mis-identification and large errors for some images, leading to additional peaks in the histogram and larger overall errors. The manual error histogram shows a more narrow distribution of errors, similar to the NN. The results from the NN, Sobel filter, and the manual technique for individual test images, along with the corresponding errors, can be viewed in the Supplementary Material.

Note that the errors are dependent on the resolution of the input images. As noted before, the resolution of our inputs are less than that of the native Landsat images in order to account for the possible span of ice fronts while minimizing image sizes and training time. However, the errors could be improved further by increasing the resolution and the areal extent of the input images, requiring more computational resources and increased training time. Thus, our benchmark analysis shown above is conducted on the same glacier to limit the influence of resolution and image size on the performance comparison of NN configurations and analytical filter and manual results.

4. Discussion

Images of glacier calving fronts are inherently noisy, with a variety of surfaces and boundaries. Therefore, the application of analytical edge detection schemes such as the Sobel filter [14] results in many false-positive predictions, where any sharp gradients on the surface of the glacier, icebergs, valley walls, and surrounding topography are likely to be labeled as glacier calving fronts. In contrast, a convolutional neural network is able to learn the desired features in the images in order to correctly identify the calving front and mostly ignore other boundaries and sharp gradients. As discussed in Figure 3, the glacier fronts extracted from the output of the NN are in very close agreement to the true front and have similar errors as manually-determined fronts on the same resolution. The analytical filter, however, appears to be very sensitive to noise. It returns noisy images of sharp gradients from which the calving front cannot be correctly extracted in some cases. While customized analytical edge-detection schemes may be able to achieve reasonable results (see Seale *et al.* [3]), they often rely on dataset-specific parameterizations and thresholds that are not readily applicable to various imagery solutions. The application of neural networks, on the other hand, does not require analytical customization for different datasets. The NN can be trained on any imagery product with the proper training labels. The applicability of NNs for the detection of calving fronts goes beyond optical imagery, and can be potentially applied to other forms of data such as radar, which will be explored in future studies.

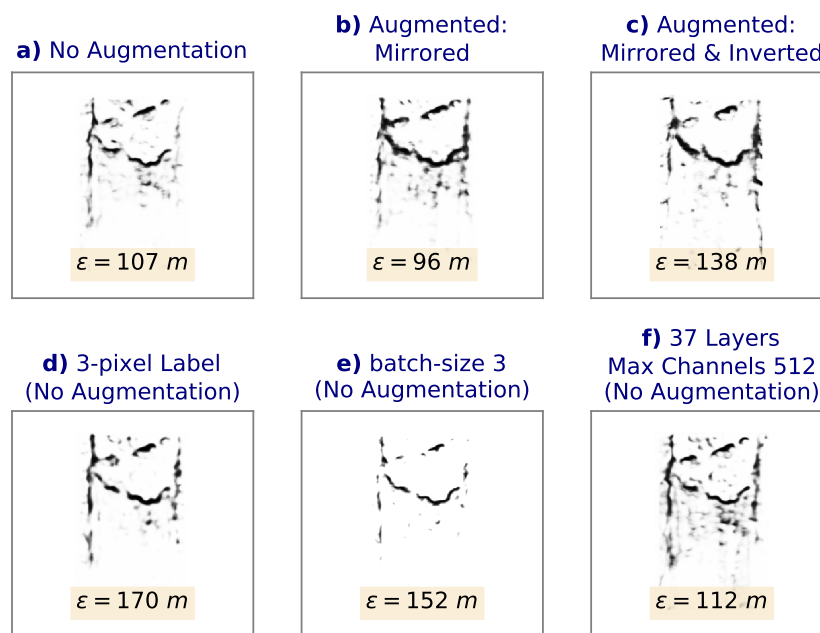


Figure 4. A comparison of raw outputs for various architecture and training configurations of the NN. ϵ represents the mean deviation from the true front for each case. Note the best results presented in the Results section correspond to Panel (b).

The proper configuration and training of the NN can have a significant effect on the accuracy of the generated calving fronts. Figure 4 showcases various alterations to the NN on the same image used in Figure 3. Panels (a)–(c) use the architecture of the NN shown in Figure 2 without any data augmentation (a), horizontally mirroring the images (b), and horizontally mirroring and inverting the colors of the images (c) during training. We find that data augmentation results in more continuous calving fronts while generally reducing the “noise” (number of false-positives). However, color inversion does not seem to contribute further to the performance of the network. In fact, while horizontal mirroring produces a mean deviation error of 96 m, the addition of inversion increases the error to 138 m. Furthermore, note that data augmentation increases the training time by several fold, depending on the number of alterations. As a result, it is desirable to use minimal augmentation while maintaining a low error. Therefore, we restrict the augmentation to horizontal mirroring. Furthermore, Panel (d) shows the effect of increasing the width of the glacier front lines in the training labels from 1 pixel to 3 pixels. While the mean error increases due to the loss of spatial precision, it is interesting to note that the noise, or number of false-positives, also decreases noticeably. This may be a result of the smaller class imbalance and weight ratio in the loss function (which decreases from 241.15 to 82.22), reducing the relative cost for a false classification of the calving fronts compared to background pixels. Therefore, if more pronounced calving front lines with minimal noise are required in post-processing, thicker labels may be desired.

We also find that the number of batches used during training has a significant effect on the results. We use batch sizes of 10 in the chosen NN. On the one hand, using larger batch sizes increases the noise in the output of the neural network, significantly decreasing the accuracy metric in the validation dataset. On the other hand, while using smaller batch sizes reduces the background noise, it also decreases the accuracy, with the mean error changing from 107 m (10 batches) to 152 m (3 batches), as shown in Panel (e). However, smaller batch sizes might be desirable if fewer false-negatives (at the cost of less continuous calving fronts) are required. Note that while smaller

batch sizes increase training time per epoch, fewer iterations are required before overfitting in validation loss becomes evident.

Lastly, we also examine the effect of the depth and size of the neural network on the test results. While increasing the depth leads to smaller errors compared to increasing the width or the number of units in each layer (not shown), there are no improvements with respect to the 29-layer NN, as shown in Panel (f). This may be due to the limited availability of training data for a deeper NN. The 37-layer NN (with one more downsample/upsampling step compared to Figure 2) shows a more noisy output with a mean error of 112 m, slightly larger than the mean error of the corresponding 29-layer output in Panel (a). Note that the same relationship is true with the addition of augmentation. However, in the case of a larger and more varied training dataset, a deeper NN could potentially lead to further improvements.

5. Conclusions

We have used a Convolutional Neural Network (CNN) with a U-Net architecture [21] to automatically detect glacier calving fronts in images obtained from Landsat 5 (“green” band) and Landsat 7 and 8 (“panchromatic” band). After exploring different network architectures and training and augmentation configurations, we find remarkable agreements between the true hand-drawn calving fronts and those obtained by a 29-layer deep neural network with 3×3 ReLU convolutional layers [25], regularization with 0.2 Dropout layers [26], 2×2 downsampling (MaxPooling [24]) and upsampling layers, a sample-weighted loss function based on the ratio of calving-front vs. non-calving-front pixels, and the utilization of data augmentation. We test the performance of the network not only on new images in the validation dataset, but also on an entirely new glacier with higher spatial resolution to test the effect of different fjord geometries and spatial resolutions on the trained network. After training the NN on Jakobshavn, Sverdrup, and Kangerlussuaq glaciers, we test it on Helheim glacier and obtain a mean deviation error of 96.3 m, equivalent to 1.97 pixels on average, which is comparable to the mean error of 92.5 m obtained from hand-drawn results on the same resolution. As a comparison, the Sobel filter [14], a commonly used analytical edge-detection method (e.g. see Seale *et al.* [3]) results in a mean error of 836.3 m on the same dataset.

The success of the neural network (NN) in automatically detecting calving fronts, along with the need for a relatively small training set and short training times, makes this approach highly desirable for the continuous monitoring of numerous glaciers around the globe with the ever-growing wealth of remote-sensing data. The use of more spectral bands from various satellites can potentially improve the performance of the NN in the future. Furthermore, unlike analytical edge-detection techniques, the use of neural networks is not limited to optical imagery and can potentially be extended to many data forms such as radar. Therefore, the use of convolutional neural networks in the detection of calving fronts can be a widely applicable and powerful approach for future studies in order to monitor the retreat of numerous glaciers in real time.

Supplementary Materials: The architecture of the Neural Network (NN), as well as the generated fronts and the associated errors from the NN, Sobel filter, and manual results for sample test images of Helheim Glacier can be found in the Supplementary Material.

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Author Contributions: Y.M. created, trained, and tested various neural network architectures and analytical edge-detection methods, pre-processed the rotated tiles, and wrote most of the manuscript. M.W. provided the input data and the training labels, post-processed the data and geocoded the results, quantified the errors, and wrote some of the manuscript. I.V. and E.R. provided guidance and supervision throughout the project and contributed to the manuscript.

Conflicts of Interest: The authors declare no conflict of interest. The sponsors of this work had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, and in the decision to publish the results.

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