

Article

Unification of Thermo Field Kinetic and Hydrodynamics Approaches in Theory of Dense Quantum–Field Systems

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Abstract: A formulation of nonequilibrium thermo field dynamics has been performed using the nonequilibrium statistical operator method by D.N.Zubarev. Generalized transfer equations for a consistent description of kinetics and hydrodynamics of the dense quantum-field system with strongly coupled states are derived.

Keywords: nonequilibrium thermo field dynamics, kinetics, hydrodynamics, kinetic equations, transport coefficients, coupled states, quark-gluon plasma

1. Introduction

A problem of accounting for the bound states (clusters) [15,16] formed by particles is particularly important in the development of the theories of nonequilibrium processes of temperature quantum-field systems, such as nuclear matter [1–14]. Kinetic and hydrodynamic processes in a hot, compressed nuclear matter, which appears after ultrarelativistic collisions of heavy nuclei [5,12,14,17–21] are mutually connected, and, therefore, the coupled states between nucleons should be considered. This is of great importance for the analysis and correlation of final reaction products. Obviously, a nucleon interaction investigation based on a quark-gluon plasma is a sequential microscopic approach to the dynamical description of reactions in a nuclear matter. The problems of a dense quark-gluon matter were discussed in detail in [2,3,10,11,23–27].

In his recent works [15,16,19] G. Röpke noted the importance of constructing a nonequilibrium theory in which along with hydrodynamic parameters a cluster distribution function are taken into account, similarly to the case of the classical theory of non-equilibrium processes of dense gases and liquids [28–31].

In modern theoretical studies of the nonequilibrium properties of quark-gluon plasma [10,11,23,24], which is one of the states of nuclear matter, one of the most widely used statistical concept is the entropy of Tsallis and Renyi [32–41]. At the same time, the important problem of the construction of kinetic and hydrodynamic equations for nuclear matter of high density and high temperature is not sufficiently addressed for these systems. However, within the framework of the Gibbs statistics, the equations of hydrodynamics and thermodynamics were already considered in many papers using the method of the Zubarev's nonequilibrium statistical operator [42–51], the projection operator method [52,53] and kinetic equations [54–57]. Thus, we propose an approach to solve these problems based on the nonequilibrium thermofield dynamics [58–60] in the formulation of the method of nonequilibrium statistical operator [61–63]. Below, in the second section of this paper, we consider the nonequilibrium thermo field dynamics in the formulation of the nonequilibrium statistical operator method [64–66] in Renyi statistics. Next, in the third section, generalized equations for the consistent description of kinetic and hydrodynamic processes which take into account the bound states that emerge in the temperature quantum-field system will be presented.

2. Nonequilibrium Statistical Operator in Thermo Field Space

We use the nonequilibrium statistical operator method in the thermofield formulation [61,62], where the mean values corresponding to the observables can be found using the nonequilibrium thermovacuum state vector $|\varrho(t)\rangle\rangle$:

$$\langle A \rangle^t = \langle\langle 1 | A \varrho(t) \rangle\rangle = \langle\langle 1 | \hat{A} | \varrho(t) \rangle\rangle, \quad (1)$$

where \hat{A} is a superoperator acting on the state $|\varrho(t)\rangle\rangle$. The nonequilibrium thermovacuum state vector $|\varrho(t)\rangle\rangle$ satisfies the Schrödinger equation [61]:

$$\frac{\partial}{\partial t} |\varrho(t)\rangle\rangle - \left| \frac{1}{i\hbar} [H, \varrho(t)] \right\rangle\rangle = 0, \quad (2)$$

OR

$$\frac{\partial}{\partial t} |\varrho(t)\rangle\rangle - \frac{1}{i\hbar} \hat{H} |\varrho(t)\rangle\rangle = 0. \quad (3)$$

Here, the total Hamiltonian \hat{H} takes the form:

$$\hat{H} = H - \tilde{H}, \quad (4)$$

where $\langle\langle 1 | \hat{H} = 0$, and $H = H(\hat{a}^+, \hat{a})$, $\tilde{H} = H^{(*)}(\tilde{a}^+, \tilde{a})$ are superoperators constructed from the creation and annihilation of superoperators of the thermal Liouville space [61,68,69]. The superoperators H and \tilde{H} are defined in [61].

In the nonequilibrium statistical operator method in the thermofield formulation [61,62], the nonequilibrium thermovacuum state vector as a solution of the Schrödinger equation (3) with a source $-\varepsilon(|\varrho(t)\rangle\rangle - |\varrho_{\text{rel}}(t)\rangle\rangle)$, with the projection taken into account can be found in the form

$$|\varrho(t)\rangle\rangle = |\varrho_{\text{rel}}(t)\rangle\rangle + \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} T(t, t') [1 - \mathcal{P}_{\text{rel}}(t')] \frac{1}{i\hbar} \hat{H} |\varrho_{\text{rel}}(t')\rangle\rangle. \quad (5)$$

Here $T(t, t') = \exp_+ \left\{ \int_{t'}^t dt' [1 - \mathcal{P}_{\text{rel}}(t')] \frac{1}{i\hbar} \hat{H} \right\}$ is the evolution operator with the projection taken into account, where \exp_+ is the ordered exponential, $\varepsilon \rightarrow +0$ after the thermodynamic limit transition.

$$\begin{aligned} \mathcal{P}_{\text{rel}}(t)(|\dots\rangle\rangle) = |\varrho_{\text{rel}}(t)\rangle\rangle &+ \sum_n \frac{\delta |\varrho_{\text{rel}}(t)\rangle\rangle}{\delta \langle\langle 1 | \hat{p}_n | \varrho_{\text{rel}}(t) \rangle\rangle} \langle\langle 1 | \hat{p}_n | \dots \rangle\rangle \\ &- \sum_n \frac{\delta |\varrho_{\text{rel}}(t)\rangle\rangle}{\delta \langle\langle 1 | \hat{p}_n | \varrho_{\text{rel}}(t) \rangle\rangle} \langle\langle 1 | \hat{p}_n | \dots \rangle\rangle \langle\langle 1 | \dots \rangle\rangle \end{aligned} \quad (6)$$

is the Kawasaki-Ganton projection operator, which acts only on the state vectors $|\dots\rangle\rangle$ and has the operator properties $\mathcal{P}_{\text{rel}}(t)|\varrho(t')\rangle\rangle = |\varrho_{\text{rel}}(t)\rangle\rangle$, $\mathcal{P}_{\text{rel}}(t)|\varrho_{\text{rel}}(t')\rangle\rangle = |\varrho_{\text{rel}}(t)\rangle\rangle$, $\mathcal{P}_{\text{rel}}(t)\mathcal{P}_{\text{rel}}(t') = \mathcal{P}_{\text{rel}}(t)$. The relevant thermovacuum state vector $|\varrho_{\text{rel}}(t)\rangle\rangle = \hat{\varrho}_{\text{rel}}(t)|1\rangle\rangle$, is normalized in accordance with the relation $\langle\langle 1 | \varrho_{\text{rel}}(t) \rangle\rangle = \langle\langle 1 | \hat{\varrho}_{\text{rel}}(t) | 1 \rangle\rangle = 1$, where $\hat{\varrho}_{\text{rel}}(t)$ is the relevant statistical superoperator. The relevant thermovacuum state vector of the system can be defined as follows. We assume that $\langle p_n \rangle^t = \langle\langle 1 | \hat{p}_n | \varrho(t) \rangle\rangle$ is the set of observed variables describing the nonequilibrium system state, where p_n are the operators constructed on the respective creation and annihilation operators a_i^+ and a_i . The relevant statistical operator $\varrho_{\text{rel}}(t)$ is determined from the extremum of the Renyi entropy functional

$$L_R(t) = \frac{1}{1-q} \ln \langle\langle 1 | (\varrho'(t)) \rangle\rangle^q - \alpha \langle\langle 1 | \varrho'(t) \rangle\rangle - \sum_n F_n^*(t) \langle\langle 1 | \hat{p}_n | \varrho'(t) \rangle\rangle$$

under the additional condition that the mean values $\langle p_n \rangle^t$ are given with the normalization condition $\langle\langle 1 | \hat{\rho}(t) | 1 \rangle\rangle = 1$ preserved. The Lagrange parameters α and $F_n^*(t)$ are determined from the respective normalization condition and self-consistency conditions:

$$\langle \dots \rangle_{\text{rel}}^t = \langle\langle 1 | \dots | \rho_{\text{rel}}(t) \rangle\rangle, \quad \langle p_n \rangle^t = \langle p_n \rangle_{\text{rel}}^t = \langle\langle 1 | \hat{p}_n | \rho_{\text{rel}}(t) \rangle\rangle. \quad (7)$$

The relevant statistical operator $\rho_{\text{rel}}(t)$ then becomes

$$\rho_{\text{rel}}(t) = \frac{1}{Z_R(t)} \left[1 - \frac{q-1}{q} \sum_n F_n^*(t) \delta \hat{p}_n(t) \right]^{\frac{1}{q-1}}, \quad (8)$$

where q is the Renyi parameter, $\delta \hat{p}_n(t) = \hat{p}_n - \langle\langle 1 | \hat{p}_n | \rho(t) \rangle\rangle$, and

$$Z_R(t) = \langle\langle 1 | \left[1 - \frac{q-1}{q} \sum_n F_n^*(t) \delta \hat{p}_n(t) \right]^{\frac{1}{q-1}} | 1 \rangle\rangle, \quad (9)$$

is the partition function. The sum over n can denote the summation over the wave vector \mathbf{k} , the kind of particles and a whole series of quantum numbers, such as spin. From (8) at $q = 1$, we obtain the relevant statistical operator corresponding to Gibbs statistics [61]:

$$\rho_{\text{rel}}(t) = \exp \left\{ -\Phi(t) - \sum_n F_n^*(t) p_n \right\}, \quad (10)$$

where $\Phi(t) = \ln \text{Sp} \exp \{ -\sum_n F_n^*(t) p_n \}$ is the Massieu-Planck functional. Substituting (8) in (5), we now obtain the nonequilibrium thermovacuum vector

$$|\rho(t)\rangle\rangle = |\rho_{\text{rel}}(t)\rangle\rangle + \sum_n \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} T(t, t') \left| \int_0^1 d\tau \rho_{\text{rel}}^\tau(t') J_n(t') \rho_{\text{rel}}(t)^{1-\tau}(t') \right\rangle\rangle F_n^*(t'), \quad (11)$$

where $J_n(t) = [1 - \mathcal{P}(t)] \frac{1}{q} \psi^{-1}(t) \hat{p}_n$ are the operators of the generalized flows describing the dissipative processes $\dot{\hat{p}}_n = -\frac{1}{i\hbar} \hat{H} \hat{p}_n$ in the system. The projection operator $\mathcal{P}(t)$ acts on operators and has the structure

$$\begin{aligned} \mathcal{P}(t)(\dots) = & \langle\langle 1 | \dots | \rho_{\text{rel}}(t) \rangle\rangle + \sum_m \delta \left[\int_0^1 d\tau \rho_{\text{rel}}^\tau(t) \psi^{-1}(t) (F_m(t) \right. \\ & \left. + \sum_n f_{mn}^{-1}(t) \delta \hat{p}_n) \rho_{\text{rel}}^{-\tau} \right] \langle\langle \dots | \int_0^1 d\tau \rho_{\text{rel}}^\tau(t) \delta \hat{p}_n \rho_{\text{rel}}^{-\tau}(t) \rho_{\text{rel}}(t) \rangle\rangle, \end{aligned} \quad (12)$$

where $\delta[\dots] = [\dots] - \langle\langle 1 | [\dots] | \rho_{\text{rel}}(t) \rangle\rangle$ and $f_{mn}(t) = \frac{\delta \langle\langle 1 | \hat{p}_m | \rho(t) \rangle\rangle}{\delta F_n(t)}$. The operator $\psi(t)$ has the form $\psi(t) = 1 - \frac{q-1}{q} \sum_n F_n^*(t) \delta \hat{p}_n(t)$. Using the nonequilibrium thermovacuum state vector $|\rho(t)\rangle\rangle$ given by (11), we obtain the transport equations for the nonequilibrium means $\langle\langle 1 | \hat{p}_n | \rho(t) \rangle\rangle$ in the thermofield representation. For this, we use the identity

$$\frac{\partial}{\partial t} \langle\langle 1 | \hat{p}_n | \rho(t) \rangle\rangle = \langle\langle 1 | \dot{\hat{p}}_n | \rho(t) \rangle\rangle = \langle\langle 1 | \dot{\hat{p}}_n | \rho_{\text{rel}}(t) \rangle\rangle + \langle\langle J_n(t) | \rho(t) \rangle\rangle. \quad (13)$$

Averaging the last term in the right-hand side with $|\rho(t)\rangle\rangle$ given by (11), we obtain the transport equations for the means $\langle\langle 1 | \hat{p}_n | \rho_{\text{rel}}(t) \rangle\rangle$

$$\begin{aligned} \frac{\partial}{\partial t} \langle\langle 1 | \hat{p}_n | \rho(t) \rangle\rangle &= \langle\langle 1 | \dot{\hat{p}}_n | \rho_{\text{rel}}(t) \rangle\rangle \\ &+ \sum_{n'} \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} \langle\langle \hat{p}_n T(t, t') \Big| \int_0^1 d\tau \rho_{\text{rel}}^{\tau}(t') J_{n'}(t') \rho_{\text{rel}}^{1-\tau}(t') \rangle\rangle F_{n'}^*(t'). \end{aligned} \quad (14)$$

Transport equations (14) take the memory effects into account and can be used to describe nonequilibrium processes in quantum Bose and Fermi systems in concrete cases in the framework of the nonequilibrium thermofield dynamics of nonextensive statistics. In particular, a system of relativistic transport equations for a consistent description of the kinetic and hydrodynamic processes in a quark-gluon system was derived in [62] using the nonequilibrium statistical operator method in the thermofield representation in Gibbs statistics. The advanced approach in terms of Renyi statistics can be generalized to the case of relativistic systems, and this observation is important [32,34–41]. This subject will be described in forthcoming works.

3. Thermo field transport equation with taking into account coupled states

We will consider a quantum field system in which coupled states can appear between the particles. Let us introduce annihilation and creation operators of a coupled state ($A\alpha$) with A -particle:

$$\begin{aligned} a_{A\alpha}(\mathbf{p}) &= \sum_{1, \dots, A} \Psi_{A\alpha\mathbf{p}}(1, \dots, A) a(1) \dots a(A), \\ a_{A\alpha}^+(\mathbf{p}) &= \sum_{1, \dots, A} \Psi_{A\alpha\mathbf{p}}^*(1, \dots, A) a^+(1) \dots a^+(A), \end{aligned} \quad (15)$$

where $\Psi_{A\alpha\mathbf{p}}(1, \dots, A)$ is a self-function of the A -particle coupled state, α denotes internal quantum numbers (spin, etc.), \mathbf{p} is a particle momentum, the sum covers the particles. Annihilation and creation operators $a(j)$ and $a^+(j)$ satisfy the following commutation relations:

$$[a(l), a^+(j)]_{\sigma} = \delta_{lj}, \quad [a(l), a(j)]_{\sigma} = [a^+(l), a^+(j)]_{\sigma} = 0, \quad (16)$$

where σ -commutator is determined by $[a, b]_{\sigma} = ab - \sigma ba$ with $\sigma = \pm 1$: +1 for bosons and -1 for fermions.

The Hamiltonian of such a system can be written in the form:

$$\begin{aligned} H &= \sum_{A, \alpha} \int \frac{d\mathbf{p}d\mathbf{q}}{(2\pi\hbar)^6} \frac{p^2}{2m_A} a_{A\alpha}^+(\mathbf{p} - \frac{\mathbf{q}}{2}) a_{A\alpha}(\mathbf{p} + \frac{\mathbf{q}}{2}) \\ &+ \frac{1}{2} \sum_{A, B} \sum_{\alpha, \beta} \int \frac{d\mathbf{p}d\mathbf{p}'d\mathbf{q}}{(2\pi\hbar)^9} V_{AB}(\mathbf{q}) a_{A\alpha}^+(\mathbf{p} + \frac{\mathbf{q} - \mathbf{p}'}{2}) \hat{n}_{B\beta}(\mathbf{q}) a_{A\alpha}(\mathbf{p} - \frac{\mathbf{q} - \mathbf{p}'}{2}), \end{aligned} \quad (17)$$

where $V_{AB}(\mathbf{q})$ is interaction energy between A - and B -particle coupled states, \mathbf{q} is a wavevector. Annihilation and creation operators $a_{A\alpha}(\mathbf{p})$ and $a_{A\alpha}^+(\mathbf{p})$ satisfy the following commutation relations:

$$\begin{aligned} [a_{A\alpha}(\mathbf{p}), a_{B\beta}^+(\mathbf{p}')]_{\sigma} &= \delta_{A, B} \delta_{\alpha, \beta} \delta(\mathbf{p} - \mathbf{p}'), \\ [a_{A\alpha}(\mathbf{p}), a_{B\beta}(\mathbf{p}')]_{\sigma} &= [a_{A\alpha}^+(\mathbf{p}), a_{B\beta}^+(\mathbf{p}')]_{\sigma} = 0. \end{aligned} \quad (18)$$

$\hat{n}_{B\beta}(\mathbf{q})$ in (17) is a Fourier transform of the B -particle density operator:

$$\hat{n}_{B\beta}(\mathbf{q}) = \int \frac{d\mathbf{p}}{(2\pi\hbar)^3} a_{\mathbf{p}-\frac{\mathbf{q}}{2}}^+ a_{\mathbf{p}+\frac{\mathbf{q}}{2}}.$$

As parameters of a reduced description for the consistent description of the kinetics and hydrodynamics of a system, where coupled states between the particles can appear, let us choose nonequilibrium distribution functions of A -particle coupled states in thermo field representation

$$\langle\langle 1|\hat{n}_{A\alpha}(\mathbf{r}, \mathbf{p})|\varrho(t)\rangle\rangle = f_{A\alpha}(\mathbf{r}, \mathbf{p}; t) = f_{A\alpha}(x; t), \quad x = \{\mathbf{r}, \mathbf{p}\}, \quad (19)$$

102 here $f_{A\alpha}(x; t)$ is a Wigner function of the A -particle coupled state where

$$\hat{n}_{A\alpha}(\mathbf{r}, \mathbf{p}) \equiv \hat{n}_{A\alpha}(x) = \int \frac{d\mathbf{q}}{(2\pi\hbar)^3} e^{-\frac{1}{\hbar}\mathbf{q}\cdot\mathbf{r}} \hat{a}_{A\alpha}^+(\mathbf{p} - \frac{\mathbf{q}}{2}) \hat{a}_{A\alpha}(\mathbf{p} + \frac{\mathbf{q}}{2}) \quad (20)$$

103 is the Klimontovich density operator; and the average value of the total energy density operator

$$\langle\langle 1|\hat{H}(\mathbf{r})|\varrho(t)\rangle\rangle = \langle\langle 1|H(\mathbf{r})\varrho(t)\rangle\rangle. \quad (21)$$

104 By this $\int d\mathbf{r} H(\mathbf{r}) = H$, $\hat{H}(\mathbf{r})$ is a superoperator of the total energy density which is constructed on
 105 annihilation and creation superoperators $\hat{a}_{A\alpha}(\mathbf{p})$ and $\hat{a}_{A\alpha}^+(\mathbf{p})$. The latter satisfy commutation relations
 106 (18). Following [61], one can rewrite relevant statistical operator $\hat{\varrho}_{rel}(t, |\varrho_{rel}(t)\rangle\rangle = \hat{\varrho}_{rel}(t)|1\rangle\rangle$ and
 107 with (8) from $q = 1$ for the mentioned parameters of a reduced description in the form:

$$\hat{\varrho}_{rel}(t) = \exp \left\{ -\Phi^*(t) - \int d\mathbf{r} \beta(\mathbf{r}; t) \left(\hat{H}(\mathbf{r}) - \sum_{A,\alpha} \int \frac{d\mathbf{p}}{(2\pi\hbar)^3} \mu_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right) \right\}, \quad (22)$$

108 where Lagrange multipliers $\beta(\mathbf{r}; t)$ and $\mu_{A\alpha}(x; t)$ can be found from the self-consistency conditions,
 109 correspondingly:

$$\langle\langle 1|\hat{H}(\mathbf{r})|\varrho(t)\rangle\rangle = \langle\langle 1|\hat{H}(\mathbf{r})|\varrho_{rel}(t)\rangle\rangle, \quad (23)$$

$$\langle\langle 1|\hat{n}_{A\alpha}(x)|\varrho(t)\rangle\rangle = \langle\langle 1|\hat{n}_{A\alpha}(x)|\varrho_{rel}(t)\rangle\rangle, \quad (24)$$

110 $\Phi^*(t)$ is the Massieu-Planck functional and it can be defined from the normalization condition :

$$\Phi^*(t) = \ln \left\langle\left\langle 1 \left| \exp \left\{ - \int d\mathbf{r} \beta(\mathbf{r}; t) \left(\hat{H}(\mathbf{r}) - \sum_{A,\alpha} \int \frac{d\mathbf{p}}{(2\pi\hbar)^3} \mu_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right) \right\} \right| \right\rangle\rangle. \quad (25)$$

111 Using now the general structure of nonequilibrium thermo field dynamics (14), one can obtain a
 112 set of generalized transport equations for A -particle Wigner distribution functions and the average
 113 interaction energy:

$$\begin{aligned} \frac{\partial}{\partial t} \langle\langle 1|\hat{n}_{A\alpha}(x)|\varrho(t)\rangle\rangle &= \langle\langle 1|\dot{\hat{n}}_{A\alpha}(x)|\varrho(t)\rangle\rangle \\ &+ \int d\mathbf{r}' \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} \varphi_{nH}^{A\alpha}(x, \mathbf{r}'; t, t') \beta(\mathbf{r}'; t') \\ &+ \sum_{B,\beta} \int dx' \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} \varphi_{nn}^{A\alpha B\beta}(x, x'; t, t') \beta(\mathbf{r}'; t') \mu_{B\beta}(x'; t'), \end{aligned} \quad (26)$$

$$\begin{aligned} \frac{\partial}{\partial t} \langle \langle 1 | \hat{H}(\mathbf{r}) | \varrho(t) \rangle \rangle &= \langle \langle 1 | \dot{\hat{H}}(\mathbf{r}) | \varrho_q(t) \rangle \rangle \\ &+ \int d\mathbf{r}' \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} \varphi_{HH}(\mathbf{r}, \mathbf{r}'; t, t') \beta(\mathbf{r}'; t') \\ &+ \sum_{B, \beta} \int d\mathbf{x}' \int_{-\infty}^t dt' e^{\varepsilon(t'-t)} \varphi_{Hn}^{B\beta}(\mathbf{r}, \mathbf{x}'; t, t') \beta(\mathbf{r}'; t') \mu_{B\beta}(\mathbf{x}'; t'), \end{aligned} \quad (27)$$

114 where $x' = \{\mathbf{r}', \mathbf{p}'\}$, $dx' = (2\pi\hbar)^{-3} d\mathbf{r}' d\mathbf{p}'$. Here

$$\varphi_{nn}^{A\alpha}(x, x'; t, t') = \left\langle \left\langle 1 \left| \hat{J}_{n_{A\alpha}}(x, t) T(t, t') \right| \int_0^1 d\tau \varrho_{rel}^\tau(t') J_{n_{B\beta}}(x'; t') \varrho_{rel}^{1-\tau}(t') \right\rangle \right\rangle, \quad (28)$$

$$\varphi_{nH}^{A\alpha}(x, \mathbf{r}'; t, t') = \left\langle \left\langle 1 \left| \hat{J}_{n_{A\alpha}}(x, t) T(t, t') \right| \int_0^1 d\tau \varrho_{rel}^\tau(t') J_H(\mathbf{r}'; t') \varrho_{rel}^{1-\tau}(t') \right\rangle \right\rangle, \quad (29)$$

$$\varphi_{Hn}^{B\beta}(\mathbf{r}', x'; t, t') = \left\langle \left\langle 1 \left| \hat{J}_H(\mathbf{r}, t) T(t, t') \right| \int_0^1 d\tau \varrho_{rel}^\tau(t') J_{n_{B\beta}}(x'; t') \varrho_{rel}^{1-\tau}(t') \right\rangle \right\rangle, \quad (30)$$

$$\varphi_{HH}(\mathbf{r}, \mathbf{r}'; t, t') = \left\langle \left\langle 1 \left| \hat{J}_H(\mathbf{r}, t) T(t, t') \right| \int_0^1 d\tau \varrho_{rel}^\tau(t') J_H(\mathbf{r}'; t') \varrho_{rel}^{1-\tau}(t') \right\rangle \right\rangle \quad (31)$$

115 are generalized transport cores which describe dissipative processes. In these formulae

$$\begin{aligned} J_H(\mathbf{r}; t) &= (1 - P(t')) \dot{H}(\mathbf{r}), \\ J_{n_{A\alpha}}(\mathbf{r}, \mathbf{p}; t) &= (1 - P(t')) \dot{n}_{A\alpha}(x) \end{aligned} \quad (32)$$

116 are generalized flows, $\dot{H}(\mathbf{r}) = -\frac{1}{i\hbar} [H, H(\mathbf{r})]$, $\dot{n}_{A\alpha}(\mathbf{r}, \mathbf{p}) = -\frac{1}{i\hbar} [H, n_{A\alpha}(x)]$, $P(t)$ is a generalized Mori
117 projection operator in thermo field representation. It acts on operators

$$\begin{aligned} P(t)P &= \langle \langle 1 | \hat{P} | \varrho_{rel}(t) \rangle \rangle + \int d\mathbf{r} \frac{\delta \langle \langle 1 | \hat{P} | \varrho_{rel}(t) \rangle \rangle}{\delta \langle \langle 1 | \hat{H}(\mathbf{r}) | \varrho(t) \rangle \rangle} \left(H(\mathbf{r}) - \langle \langle 1 | \hat{H}(\mathbf{r}) | \varrho(t) \rangle \rangle \right) \\ &+ \sum_{A, \alpha} \int \frac{d\mathbf{r} d\mathbf{p}}{(2\pi\hbar)^3} \frac{\delta \langle \langle 1 | \hat{P} | \varrho_{rel}(t) \rangle \rangle}{\delta \langle \langle 1 | \hat{n}_{A\alpha}(x) | \varrho(t) \rangle \rangle} \left(n_{A\alpha}(x) - \langle \langle 1 | \hat{n}_{A\alpha}(x) | \varrho(t) \rangle \rangle \right) \end{aligned} \quad (33)$$

118 and has all the properties of a projection operator:

$$\begin{aligned} P(t)H(\mathbf{r}) &= H(\mathbf{r}), \quad P(t)P(t') = P(t), \\ P(t)n_{A\alpha}(\mathbf{r}, \mathbf{p}) &= n_{A\alpha}(\mathbf{r}, \mathbf{p}), \quad (1 - P(t))P(t) = 0. \end{aligned}$$

119 The obtained transport equations have the general meaning and can describe both weakly and
120 strongly nonequilibrium processes of a quantum system with taking into consideration coupled states.

121 In the next step we will construct such annihilation and creation superoperators, for which
122 the relevant thermo vacuum state vector is a vacuum state. Analysing the structure of relevant
123 statistical superoperator (22), one can mark out some part which would correspond to the system of
124 noninteracting quantum A -particles. Let us write $\hat{\varrho}_{rel}(t)$ in an evident form and separate terms which
125 are connected with the interaction energy between the particles:

$$\hat{Q}_{rel}(t) = \exp \left\{ -\Phi^*(t) - \int d\mathbf{r} \beta(\mathbf{r}; t) \right. \quad (34)$$

$$\left. \times \sum_{A,\alpha} \int \frac{d\mathbf{r} d\mathbf{p}}{(2\pi\hbar)^3} \left[\frac{\mathbf{p}^2}{2m_A} \hat{n}_{A\alpha}(x) - \mu_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right] - \int d\mathbf{r} \beta(\mathbf{r}; t) \hat{H}_{int}(\mathbf{r}) \right\}.$$

126 Using operator equality (A and B are some operators)

$$e^{A+B} = \left[1 + \int_0^1 d\tau e^{\tau(A+B)} B e^{-\tau(A+B)} \right] e^A,$$

127 the relation for $\hat{Q}_{rel}(t)$ can be rewritten in the following form:

$$\hat{Q}_{rel}(t) = \left[1 - \int d\mathbf{r} \beta(\mathbf{r}; t) \int_0^1 d\tau \hat{Q}_q^\tau(t) \hat{H}_{int}(\mathbf{r}) (\hat{Q}_{rel}(t))^{-\tau} \right] \hat{Q}_{rel}^0(t), \quad (35)$$

128 where

$$\hat{Q}_{rel}^0(t) = \exp \left\{ \Phi(t) - \int d\mathbf{r} \beta(\mathbf{r}; t) \sum_{A,\alpha} \int \frac{d\mathbf{r} d\mathbf{p}}{(2\pi\hbar)^3} \left[\frac{\mathbf{p}^2}{2m_A} \hat{n}_{A\alpha}(x) - \mu_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right] \right\}, \quad (36)$$

129 OR

$$\hat{Q}_{rel}^0(t) = \exp \left\{ \Phi(t) - \int d\mathbf{r} \beta(\mathbf{r}; t) \sum_{A,\alpha} \int \frac{d\mathbf{p}}{(2\pi\hbar)^3} b_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right\}, \quad (37)$$

130 where $b_{A\alpha}(x; t) = \left[\frac{\mathbf{p}^2}{2m_A} \hat{n}_{A\alpha}(x) - \mu_{A\alpha}(x; t) \hat{n}_{A\alpha}(x) \right]$. Relevant statistical superoperator $\hat{Q}_{rel}^0(t)$ is
 131 bilinear on annihilation and creation superoperators $\hat{a}_{A\alpha}(\mathbf{P})$ and $\hat{a}_{A\alpha}^+(\mathbf{P})$, as well as on the
 132 non-perturbed part of Hamiltonian \bar{H}_0 . One can write the total relevant superoperator as some
 133 non-perturbed part of $\hat{Q}_{rel}^0(t)$ and the part which describes interaction of quantum particles in the
 134 relevant state. Further, we introduce the following designation:

$$\hat{Q}_{rel}(t) = \hat{Q}_{rel}^0(t) + \hat{Q}'_{rel}(t), \quad (38)$$

135 where

$$\hat{Q}'_{rel}(t) = - \int d\mathbf{r} \beta(\mathbf{r}; t) \int_0^1 d\tau \hat{Q}_{rel}^\tau(t) \hat{H}_{int}(\mathbf{r}) (\hat{Q}_{rel}(t))^{-\tau} \hat{Q}_{rel}^0(t). \quad (39)$$

136 Relevant (relevant) thermo vacuum states $|\hat{Q}_{rel}(t)\rangle\rangle$ and $|\hat{Q}_{rel}^0(t)\rangle\rangle$ are not vacuum states for annihilation
 137 and creation superoperators $\hat{a}_{A\alpha}(\mathbf{P})$, $\hat{a}_{A\alpha}^+(\mathbf{P})$, $\tilde{a}_{A\alpha}(\mathbf{P})$, $\tilde{a}_{A\alpha}^+(\mathbf{P})$. But for $|\hat{Q}_{rel}^0(t)\rangle\rangle$ one can construct new
 138 superoperators $\hat{\gamma}_{A\alpha}(\mathbf{P})$, $\tilde{a}_{A\alpha}^+(\mathbf{P})$, $\tilde{\gamma}_{A\alpha}(\mathbf{P})$, $\tilde{\gamma}_{A\alpha}^+(\mathbf{P})$ as a linear combination of superoperators $\hat{a}_{A\alpha}(\mathbf{P})$,
 139 $\hat{a}_{A\alpha}^+(\mathbf{P})$ and $\tilde{a}_{A\alpha}(\mathbf{P})$, $\tilde{a}_{A\alpha}^+(\mathbf{P})$ in order to satisfy the conditions:

$$\begin{aligned} \hat{\gamma}_{A\alpha}(\mathbf{P}; t) |\hat{Q}_{rel}^0(t)\rangle\rangle &= 0, & \langle\langle 1 | \tilde{a}_{A\alpha}^+(\mathbf{P}; t) &= 0, \\ \tilde{\gamma}_{A\alpha}(\mathbf{P}; t) |\hat{Q}_{rel}^0(t)\rangle\rangle &= 0, & \langle\langle 1 | \tilde{\gamma}_{A\alpha}^+(\mathbf{P}; t) &= 0. \end{aligned} \quad (40)$$

140 To achieve this let us consider an action of annihilation superoperators $\hat{a}_{A\alpha}(\mathbf{P}; t)$, $\tilde{a}_{A\alpha}(\mathbf{P}; t)$ on relevant
 141 state $|\hat{Q}_{rel}^0(t_0)\rangle\rangle$:

$$\begin{aligned}\hat{a}_{A\alpha}(\mathbf{P};t)|\varrho_{rel}^0(t_0)\rangle &= f_{A\alpha}(\mathbf{P};t-t_0)\tilde{a}_{A\alpha}^+(\mathbf{P};t)|\varrho_{rel}^0(t_0)\rangle, \\ \tilde{a}_{A\alpha}(\mathbf{P};t)|\varrho_{rel}^0(t_0)\rangle &= \sigma f_{A\alpha}(\mathbf{P};t-t_0)\hat{a}_{A\alpha}^+(\mathbf{P};t)|\varrho_{rel}^0(t_0)\rangle,\end{aligned}\quad (41)$$

142 where superoperators $\hat{a}_{A\alpha}(\mathbf{p};t)$, $\hat{a}_{A\alpha}^+(\mathbf{p};t)$, $\tilde{a}_{A\alpha}(\mathbf{p};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{p};t)$ are in the Heisenberg representation

$$\begin{aligned}\hat{a}_{A\alpha}(\mathbf{P};t) &= e^{-\frac{1}{i\hbar}H_0t}\hat{a}_{A\alpha}(\mathbf{P})e^{\frac{1}{i\hbar}H_0t}, & \tilde{a}_{A\alpha}(\mathbf{P};t) &= e^{-\frac{1}{i\hbar}H_0t}\tilde{a}_{A\alpha}(\mathbf{P})e^{\frac{1}{i\hbar}H_0t}, \\ \hat{a}_{A\alpha}^+(\mathbf{P};t) &= e^{-\frac{1}{i\hbar}H_0t}\hat{a}_{A\alpha}^+(\mathbf{P})e^{\frac{1}{i\hbar}H_0t}, & \tilde{a}_{A\alpha}^+(\mathbf{P};t) &= e^{-\frac{1}{i\hbar}H_0t}\tilde{a}_{A\alpha}^+(\mathbf{P})e^{\frac{1}{i\hbar}H_0t},\end{aligned}$$

143 and satisfy commutation relations:

$$\begin{aligned}\left[\hat{a}_{A\alpha}(\mathbf{P};t), \hat{a}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} &= \delta_{A,B}\delta_{\alpha,\beta}\delta(\mathbf{P}-\mathbf{P}'), \\ \left[\tilde{a}_{A\alpha}(\mathbf{P};t), \tilde{a}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} &= \delta_{A,B}\delta_{\alpha,\beta}\delta(\mathbf{P}-\mathbf{P}'), \\ \left[\hat{a}_{A\alpha}(\mathbf{P};t), \tilde{a}_{B\beta}(\mathbf{P}';t)\right]_{\sigma} &= \left[\hat{a}_{A\alpha}^+(\mathbf{P};t), \tilde{a}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} = 0.\end{aligned}$$

144 It is necessary to note that superoperators $\hat{H}(\mathbf{r})$, $\hat{h}_{A\alpha}(x)$ are built on superoperators $\hat{a}_{A\alpha}(\mathbf{p} + \frac{\mathbf{q}}{2})$,
145 $\hat{a}_{A\alpha}^+(\mathbf{p} - \frac{\mathbf{q}}{2})$, $\tilde{a}_{A\alpha}(\mathbf{p} + \frac{\mathbf{q}}{2})$, $\tilde{a}_{A\alpha}^+(\mathbf{p} - \frac{\mathbf{q}}{2})$. Therefore, for convenience here a unit denotation was introduced
146 for arguments like $\mathbf{P} = \mathbf{p} \pm \frac{\mathbf{q}}{2}$. This should be taken into account in further calculations where obvious
147 expressions are needed.

148 According to general relations of [61,62], we can introduce new operators $\hat{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$,
149 $\tilde{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{\gamma}_{A\alpha}^+(\mathbf{P};t)$ via superoperators $\hat{a}_{A\alpha}(\mathbf{P};t)$, $\hat{a}_{A\alpha}^+(\mathbf{P};t)$, $\tilde{a}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$:

$$\begin{aligned}\hat{\gamma}_{A\alpha}(\mathbf{P};t) &= \sqrt{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} \left[\hat{a}_{A\alpha}(\mathbf{P};t) - \frac{n_{A\alpha}(\mathbf{P};t, t_0)}{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} \tilde{a}_{A\alpha}^+(\mathbf{P};t) \right], \\ \tilde{\gamma}_{A\alpha}^+(\mathbf{P};t) &= \sqrt{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} [\tilde{a}_{A\alpha}^+(\mathbf{P};t) - \sigma \hat{a}_{A\alpha}(\mathbf{P};t)].\end{aligned}\quad (42)$$

150 Relations (42) satisfy conditions (40). Here

$$\begin{aligned}n_{A\alpha}(\mathbf{p}, \mathbf{q}; t, t_0) &= n_{A\alpha}(\mathbf{P}; t, t_0) = \langle\langle 1 | \tilde{a}_{A\alpha}^+(\mathbf{P}; t) \tilde{a}_{A\alpha}(\mathbf{P}; t) | \varrho_{rel}^0(t_0) \rangle\rangle \\ &= \langle\langle 1 | \tilde{a}_{A\alpha}^+(\mathbf{p} - \frac{\mathbf{q}}{2}; t) \tilde{a}_{A\alpha}(\mathbf{p} + \frac{\mathbf{q}}{2}; t) | \varrho_{rel}^0(t_0) \rangle\rangle,\end{aligned}$$

151 is a relevant distribution function of A -particle coupled states in momentum space \mathbf{p} , \mathbf{q} , which is
152 calculated with the help of relevant thermo vacuum state vector $|\varrho_{rel}^0(t_0)\rangle$ (37). Function $f_{A\alpha}(\mathbf{P}; t - t_0)$
153 in formulae (41) is connected with $n_{A\alpha}(\mathbf{P}; t, t_0)$ by the relation

$$f_{A\alpha}(\mathbf{P}; t - t_0) = \frac{n_{A\alpha}(\mathbf{P}; t, t_0)}{1 + \sigma n_{A\alpha}(\mathbf{P}; t, t_0)}.$$

154 Superoperators $\hat{\gamma}_{A\alpha}(\mathbf{P};t)$ and $\tilde{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$ and $\tilde{\gamma}_{A\alpha}^+(\mathbf{P};t)$ satisfy the ‘‘canonical’’ commutation
155 relations:

$$\begin{aligned}\left[\hat{\gamma}_{A\alpha}(\mathbf{P};t), \tilde{a}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} &= \delta_{A,B}\delta_{\alpha,\beta}\delta(\mathbf{P}-\mathbf{P}'), \\ \left[\tilde{\gamma}_{A\alpha}(\mathbf{P};t), \tilde{\gamma}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} &= \delta_{A,B}\delta_{\alpha,\beta}\delta(\mathbf{P}-\mathbf{P}'), \\ \left[\hat{\gamma}_{A\alpha}(\mathbf{P};t), \tilde{\gamma}_{B\beta}(\mathbf{P}';t)\right]_{\sigma} &= \left[\tilde{a}_{A\alpha}^+(\mathbf{P};t), \tilde{\gamma}_{B\beta}^+(\mathbf{P}';t)\right]_{\sigma} = 0.\end{aligned}\quad (43)$$

156 Inversed transformations to superoperators $\hat{a}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$ are easily obtained from (42):

$$\begin{aligned} \hat{a}_{A\alpha}(\mathbf{P};t) &= \sqrt{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} \left[\hat{\gamma}_{A\alpha}(\mathbf{P};t) + \frac{n_{A\alpha}(\mathbf{P};t, t_0)}{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} \tilde{\gamma}_{A\alpha}^+(\mathbf{P};t) \right], \\ \tilde{a}_{A\alpha}^+(\mathbf{P};t) &= \sqrt{1 + \sigma n_{A\alpha}(\mathbf{P};t, t_0)} [\tilde{\gamma}_{A\alpha}^+(\mathbf{P};t) + \sigma \hat{\gamma}_{A\alpha}(\mathbf{P};t)]. \end{aligned} \quad (44)$$

157 $\hat{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$, $\tilde{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{\gamma}_{A\alpha}^+(\mathbf{P};t)$ could be defined as some operators of annihilation and creation
158 of A -quasiparticle coupled states, for which relevant thermo vacuum state $|\varrho_{rel}^0(t_0)\rangle\rangle$ (37) is a vacuum
159 state. In such a way, we obtained relations of dynamical reflection of superoperators $\hat{a}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$,
160 $\tilde{a}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$ to new superoperators of "quasiparticles" $\hat{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{a}_{A\alpha}^+(\mathbf{P};t)$, $\tilde{\gamma}_{A\alpha}(\mathbf{P};t)$, $\tilde{\gamma}_{A\alpha}^+(\mathbf{P};t)$.

161 A set of transport equations (26), (27) together with dynamical reflections (42), (44) of
162 superoperators in the thermo field space constitute the basis for a consistent description of the kinetics
163 and hydrodynamics of a dense quantum system with strongly coupled states. Both strongly and
164 weakly nonequilibrium processes of a nuclear matter can be investigated using this approach, in which
165 the particle interaction is characterized by strongly coupled states, taking into account their nuclear
166 nature [1–4].

167 Weakly nonequilibrium processes can be described when the fluctuations of the parameters
168 $\delta\beta(\vec{r};t) = \beta(\vec{r};t) - \beta$, $\delta\mu_{A\alpha}(x;t) = \mu_{A\alpha}(x;t) - \mu_{A\alpha}$ are small, where β and $\mu_{A\alpha}$ are equilibrium values
169 for temperature and chemical potential respectively. In this case, the system of equations (26), (27)
170 will have a similar structure, but is closed with respect to $\langle\langle 1|\delta\hat{n}_{A\alpha}(x)|\varrho(t)\rangle\rangle$, $\langle\langle 1|\delta\hat{H}(\mathbf{r})|\varrho(t)\rangle\rangle$, where
171 $\delta\hat{n}_{A\alpha}(x) = \hat{n}_{A\alpha}(x) - \langle\langle 1|\hat{n}_{A\alpha}(x)|\varrho_0\rangle\rangle$, $\delta\hat{H}(\mathbf{r}) = \hat{H}(\mathbf{r}) - \langle\langle 1|\hat{H}(\mathbf{r})|\varrho_0\rangle\rangle$, $|\varrho_0\rangle\rangle$ is the equilibrium thermo
172 vacuum state vector of the systems.

173 In addition, by designing a system of equations on moments 1, \mathbf{P} of distribution function we
174 obtain, respectively, the equation of the thermo field hydrodynamic for the dense quantum - field
175 systems.

176 These questions require separate consideration and will be investigated in future work.

177 4. Conclusions

178 We generalized the nonequilibrium thermo field dynamics in the frames of Zubarev's
179 nonequilibrium statistical operator method [61] within the framework of Reniy statistics. Based
180 on this approach and Gibbs statistics the generalized equations of consistent description of kinetics
181 and hydrodynamics for dense quantum field systems with strongly bound states were obtained. Using
182 this approach, one can investigate both strongly and slightly nonequilibrium processes of nuclear
183 matter, when the interaction between particles of the latter is characterized by strongly bound states of
184 internucleon nature [2,3].

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