

Article

# Self-Tuning Control Techniques for Wind Turbine and Hydroelectric Plant Systems

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1 **Abstract:** The interest on the use of renewable energy resources is increasing, especially towards  
2 wind and hydro powers, which should be efficiently converted into electric energy via suitable  
3 technology tools. To this aim, self-tuning control techniques represent viable strategies that can be  
4 employed for this purpose, due to the features of these nonlinear dynamic processes working over  
5 a wide range of operating conditions, driven by stochastic inputs, excitations and disturbances.  
6 Some of the considered methods were already verified on wind turbine systems, and important  
7 advantages may thus derive from the appropriate implementation of the same control schemes for  
8 hydroelectric plants. This represents the key point of the work, which provides some guidelines  
9 on the design and the application of these control strategies to these energy conversion systems. In  
10 fact, it seems that investigations related with both wind and hydraulic energies present a reduced  
11 number of common aspects, thus leading to little exchange and share of possible common points.  
12 This consideration is particularly valid with reference to the more established wind area when  
13 compared to hydroelectric systems. In this way, this work recalls the models of wind turbine and  
14 hydroelectric system, and investigates the application of different control solutions. The scope is to  
15 analyse common points in the control objectives and the achievable results from the application  
16 of different solutions. Another important point of this investigation regards the analysis of the  
17 exploited benchmark models, their control objectives, and the development of the control solutions.  
18 The working conditions of these energy conversion systems will be also taken into account in  
19 order to highlight the reliability and robustness characteristics of the developed control strategies,  
20 especially interesting for remote and relatively inaccessible location of many installations.

21 **Keywords:** Wind turbine system; hydroelectric plant simulator; model-based control; data-driven  
22 approach; self-tuning control; robustness and reliability

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## 23 1. Introduction

24 The trend to reduce the use of fossil fuels, motivated by the need to meet greenhouse gas  
25 emission limits, has driven much interest on renewable energy resources, in order also to cover global  
26 energy requirements. Wind turbine systems, which now represent a mature technology, have had  
27 much more development with respect to other energy conversion systems, *e.g.* for biomass, solar, and  
28 hydropower [1,2]. In particular, hydroelectric plants present interesting energy conversion potentials,  
29 with commonalities and contrast with respect to wind turbine installations [3–5].

30 One common aspect regarding the design of the renewable energy conversion system concerns  
31 the optimality and the efficiency of its converter. However, as wind and hydraulic resources are free,  
32 the key point is represented by the minimisation of the cost per kWh, also considering the lifetime  
33 of the deployments. Moreover, when the capital, operational and commissioning/decommissioning

34 costs are fixed, the value of the energy sold (*i.e.* the energy receipts) has to be maximised. This  
35 represents a fundamental economic objective, which should be carefully taken into account also  
36 by the design of the control system. Indeed, the design of the device should follow a top-down  
37 development. However, as first step, physicists propose the energy conversion system design, whilst  
38 system engineers investigate the control problem in a subsequent phase, in cooperation with the  
39 discipline-specific experts. This approach is common in most industrial applications of control, but  
40 it can lead to non-optimal solutions.

41 It is worth noting that preliminary works highlighted interactions between the renewable energy  
42 conversion system design and the strategies exploited to control them, see for example, [6]. Moreover,  
43 by taking into account that the cost of control system technology (*i.e.* sensors, actuators, computer,  
44 software) is relatively lower than the one of the renewable energy converter [7], the control system  
45 should aim at increasing the energy conversion capacity of the given plant. However, this strategy  
46 neglects the control system capability and the engineering expertise required for the development  
47 of a suitable control technique. As an example, model-based control design schemes need for  
48 a high-fidelity mathematical model of the process to be controlled, which could have required a  
49 significant number of man-hours to achieve it. On the other hand, increasing efforts are made for  
50 integrating the control technology efficiency and its performances (both technical and economic),  
51 with the reliability and safety features of the controlled system, as discussed *e.g.* in [8]. By considering  
52 these aspects in particular for wind turbine installations and hydroelectric plants, this paper will  
53 analyse different model-based and data-driven control techniques that are more effective than their  
54 baseline governors.

55 Note also that several economic aspects have to be considered when designing control schemes  
56 for renewable energy conversion devices. One important point is that wind turbine processes  
57 and hydroelectric plants can be installed in relatively remote and inaccessible areas, with obvious  
58 implications for operation requirements and maintenance services. To this aim, the control technique  
59 must be designed to be robust and reliable, thus motivating the need for fault-tolerant control features  
60 (also known as 'sustainable') [9].

61 It is quite established that the mathematical descriptions of both wind turbine processes and  
62 hydroelectric plants are represented by nonlinear dynamic processes working over a wide range  
63 of operating conditions and excitations. These systems are also required to operate under specific  
64 physical constraints, such as displacements, velocities, accelerations, torques and forces. Therefore,  
65 these systems can operate effectively with economically attractive and high operational lifetimes only  
66 if their working conditions are carefully fulfilled. With these issues in mind, the paper recalls the  
67 mathematical description of a wind turbine system and a hydroelectric plant, by using a wind turbine  
68 benchmark and a hydroelectric simulator, respectively. The former process was proposed for the  
69 purpose of an international competition started in 2009 and described in detail [10], whilst the latter  
70 system was developed by the same authors, and presented for the first time in [11]. On the other hand,  
71 this work analyses different control strategies for both wind turbines and hydroelectric systems that  
72 can show common and different aspects. Moreover, in general, when considering on-grid plants, the  
73 control system has to consider also the regulation of the voltage and frequency, which will not be  
74 addressed in this work.

75 After these remarks, by means of the analysis of the proposed modelling and control topics, the  
76 work will sketch common and different aspects of wind turbines and hydraulic systems, which will  
77 be exploited for the design of the control technique. On one hand, hydroelectric power plants result  
78 to be more established and even more common than wind turbine processes, but the control aspects  
79 for the latter systems have been examined more in depth in the last decades.

80 With reference to wind turbine systems, it can be observed that modern installations  
81 exploit control techniques and technologies in order to obtain the needed goals and performance  
82 achievements. These plants can implement their regulation via 'passive' control methods, such as  
83 the plants with fixed-pitch, and stall control machines. The blades of these systems are deployed in

84 order to limit their power via the blade stall, when the wind speed exceeds its rated value. These  
85 systems do not need any pitch control mechanism, as addressed *e.g.* in [12]. Moreover, these plants  
86 implement a simple rotational speed control, thus avoiding the inaccuracy problems derived from  
87 the measurement of the wind speed [10]. On the other hand, wind turbine rotors using adjustable  
88 pitch systems are often exploited in constant-speed installations, in order to overcome the limitations  
89 due to the simple blade stall and to improve the converted power [13]. Therefore, in order to increase  
90 the generated power below the rated wind speed, the wind turbine has to modify its rotational speed  
91 with the wind velocity. To this aim, the regulation of the blade pitch is exploited only above the rated  
92 wind speed to control the generated power [14]. Large wind turbines can implement another control  
93 technique modifying the yaw angle, which is used to orient the rotor towards the wind direction. In  
94 this way, a yaw error signal is generated from a nacelle-mounted wind direction sensor, which is thus  
95 exploited to control the yaw motor when the error exceeds certain limits, as described *e.g.* in [15].

96 It is worth noting that a limited number of works have addressed the development of self-tuning  
97 control techniques for hydroelectric plants, as shown *e.g.* in [16]. In fact, a high-fidelity mathematical  
98 description of these processes can be difficult to be achieved in practice. However, some contributions  
99 reported the analytical formulation of hydroelectric plants, together with the design of their control  
100 strategies. Note that these papers took into account the elastic water effects, even if the nonlinear  
101 dynamics are linearised around an operating condition. Moreover, other contributions, see *e.g.*  
102 [17], proposed different mathematical models together with the strategies exploited to control these  
103 systems. In the same way, linear and nonlinear dynamic processes with different water column  
104 effects and regulation strategies are also proposed. For example, [18] considered advanced control  
105 techniques for hydraulic processes.

106 In the light of these considerations, the paper also proposes to analyse those control aspects  
107 that might be similar between wind turbine and hydroelectric systems, with the aim of exploiting  
108 some solutions, developed in the wind turbine domain, and to apply them within the other  
109 concerning hydroplants. This approach could be used to stimulate novel research topics and the  
110 development of innovative techniques in a multidisciplinary control community, and the most  
111 important achievements will be summarised in this paper. In particular, suitable analytical models  
112 of these energy conversion plants should be able to provide the overall dynamic behaviour of the  
113 monitored processes, thus leading important impacts on the development of the control techniques.  
114 Moreover, the work introduces some kind of common rules for tuning the different controllers, for  
115 both wind turbine and hydroelectric plants. Therefore, the paper shows that the parameters of these  
116 controllers are obtained by exploiting the same tuning strategies. This represents one of the key  
117 contributions of the study.

118 Note that some previous studies by the same authors addressed several topics presented in  
119 this paper. For example, the work [19] considered control techniques when applied only to the  
120 hydroelectric simulator, which were not compared to the wind turbine benchmark. On the other  
121 hand, the paper [20] performed an overview of the main modelling and control strategies, in  
122 particular for wind turbines and wave energy devices: the hydroelectric plant benchmark and  
123 the simulations of the proposed control techniques were not addressed. Moreover, the earlier  
124 work [11] presented the hydroelectric simulator, but considered only the design of standard PID  
125 regulator for the optimisation of its time response. Finally, the paper [21] developed a fault tolerant  
126 control methodology by means of differential algebraic tools using a purely nonlinear mathematical  
127 formulation of the wind turbine system. Other more recent control techniques applied to wind  
128 turbine systems were investigated *e.g.* in [22,23].

129 It is worth highlighting the main contribution of the paper, which aims at providing some  
130 guidelines on the design and the application of self-tuning control strategies to two energy  
131 conversion systems. Some of these techniques were already verified on wind turbine systems, and  
132 important advantages may thus derive from the appropriate implementation of the same control  
133 methods for hydroelectric plants. In fact, it seems that investigations related with both wind and

134 hydraulic energies present a reduced number of common aspects, thus leading to little exchange and  
135 share of possible common points. This consideration is particularly valid with reference to the more  
136 established wind area when compared to hydroelectric systems. In this way, the paper summarises  
137 also the most common models used for describing wind turbine and hydroelectric systems. Moreover,  
138 it analyses the application of the different control solutions to these energy conversion systems. The  
139 aim is thus to exploit common points in the control objectives and the achievable results from the  
140 application of different solutions. Another important point of this paper concerns the discussion  
141 of the exploited benchmark models, their control objectives, and the development of the control  
142 solutions. The working conditions of these energy conversion systems will be also taken into account  
143 in order to highlight the reliability and robustness characteristics of the developed control strategies.

144 Finally, the paper has the following structure. Section 2 provides the brief presentation of  
145 the benchmark and simulation models used for describing the accurate behaviour of the dynamic  
146 processes. Section 3 discusses the specific requirements of the control systems exploited to control  
147 these energy conversion plants. Section 3.1 summarises the design of the proposed model-based and  
148 data-driven control techniques, taking into account the control objectives and the available tools.  
149 In Section 4, these self-tuning control strategies are implemented and compared, with respect to  
150 the achievable reliability and robustness features. Section 5 ends the paper summarising the main  
151 achievements of the paper, and drawing some concluding remarks.

## 152 2. Simulator Models and Reference Governors

153 This section recalls the simulators used for describing the dynamic behaviour of the wind turbine  
154 and the hydroelectric processes considered in this paper. Moreover, the baseline control schemes  
155 developed for the regulation of the wind turbine benchmark are also summarised in Section 2.1. On  
156 the other hand, the hydroelectric simulator, together with its reference governor, is recalled in Section  
157 2.2.

### 158 2.1. Wind Turbine System Benchmark

159 Industrial wind turbine installations are normally equipped with large rotors, flexible blades  
160 and light load-carrying structures, which work in uncertain environments, often placed in remote  
161 and inaccessible places [24]. These topics have motivated the use of high-fidelity simulators and  
162 the development of proper control solutions, which could cope with these challenging technologies.  
163 These control strategies should thus be able to obtain prescribed performances, such as decreasing  
164 the produced energy cost, increasing the energy conversion effectiveness, reducing downtimes, and  
165 maximising the installation lifetime [8]. To this aim, the control scheme should also reduce the  
166 structural loads, torques and induced vibrations, thus increasing the lifetime of the overall installation  
167 [25]. These challenging topics will not be considered in this work, which represent recent research  
168 topics in the frameworks of both wind turbine systems and hydroelectric power plants. However,  
169 this paper will consider the design and the application of self-tuning control techniques that are  
170 able to optimise the tracking of a given reference. This reference or set-point signal guarantees the  
171 maximisation of the energy production [6].

172 In particular regarding wind turbines, even if they are designed in both horizontal- and  
173 vertical-axis solutions, this work focuses on a horizontal-axis device, which nowadays represents  
174 the most common type of installation for large-scale deployments. Moreover, the three-bladed  
175 horizontal axis wind turbine model reported in this work follows the principle that the wind power  
176 activates the wind turbine blades, thus producing the rotation of the low speed rotor shaft. In order  
177 to increase its rotational speed generally required by the generator, a gear-box with a drive-train  
178 is included in the system. A more detailed picture of this benchmark that was proposed for an  
179 international competition but with different purposes is given *e.g.* in [10]. The schematic diagram of  
180 this benchmark that helps to recall its main variables and function blocks developed in the Simulink

181 environment is depicted in Fig. 1 (b), while the diagram showing its working principles is sketched  
 182 in Fig. 1 (a).

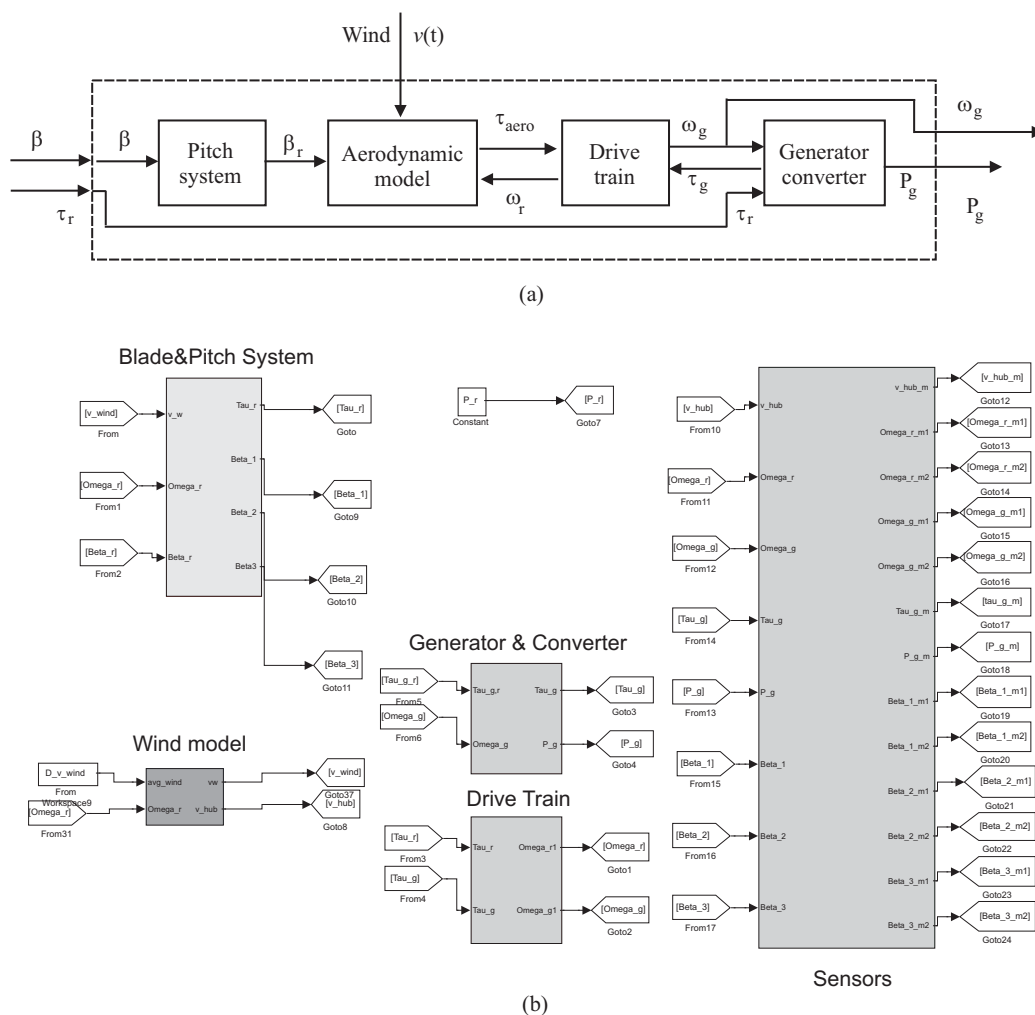


Figure 1. (a)Block diagram of the wind turbine plant, and (b) its benchmark with function blocks.

183 The wind turbine simulator presents 2 controlled outputs, *i.e.* the generator rotational speed  
 184  $\omega_g(t)$  and its generated power  $P_g(t)$ . The wind turbine model is controlled by means of two actuated  
 185 inputs, *i.e.* the generator torque  $\tau_g(t)$  and the blade pitch angle  $\beta(t)$ . The latter signal controls  
 186 the blade actuators, which can be implemented by hydraulic or electric drives. The benchmark  
 187 considered in this work includes a hydraulic circuit actuating the wind turbine blades [10].

Several other measurements are acquired from the wind turbine benchmark: the signal  $\omega_r(t)$  represents the rotor speed and  $\tau_r(t)$  is the reference torque. Moreover, aerodynamic torque signal  $\tau_{aero}(t)$  is computed from the wind speed  $v(t)$ , which is usually available with limited accuracy. In fact, the wind field is not uniform around the wind turbine rotor plane, especially for large rotor systems. Moreover, anemometers measuring this variable are mounted behind the rotor on the nacelle. Therefore, the wind speed measurement  $v(t)$  is affected by the interference between the blades and the nacelle, as well as the turbulence around the rotor plane. Furthermore, when these instantaneous wind fields are considered across the rotor plane, the wind variable  $v(t)$  may change in space and time, and it is especially true in large rotor installations. The alteration of the wind speed measurement  $v(t)$  with respect to its nominal value around the rotor plane represents an uncertainty in the wind turbine model and a disturbance term in control design. On the other hand,

the aerodynamic torque depends on another factor,  $C_p$ , representing the power coefficient, as shown by Eq. (1):

$$\tau_{aero}(t) = \frac{\rho A C_p(\beta(t), \lambda(t)) v^3(t)}{2 \omega_r(t)} \quad (1)$$

$\rho$  being air density,  $A$  the area swept by the turbine blades during their rotation, whilst  $\lambda(t)$  represents an important variable, *i.e.* the tip-speed ratio of the blade, which is given by the relation of Eq. (2):

$$\lambda(t) = \frac{\omega_r(t) R}{v(t)} \quad (2)$$

188 where  $R$  is the rotor radius. The nonlinear static function  $C_p(\cdot)$  represents the power coefficient,  
 189 which is usually modelled via a two-dimensional map (or look-up table), as highlighted *e.g.* in [10].  
 190 The relation of Eq. (1) is exploited to derive the variable  $\tau_{aero}(t)$  assuming an uniform measurement  
 191  $v(t)$ , together with the acquired signals  $\beta(t)$  and  $\omega_r(t)$ . As remarked above, the uncertainty affecting  
 192 the wind speed  $v(t)$  leads to an error in the derivation of the variable  $\tau_{aero}(t)$  [10]. Moreover, the  
 193 overall nonlinear behaviour represented by the relations of Eqs. (1) and (2) is reported in Figure 2.  
 194 The picture is sketched for different values of the variable  $\lambda(t)$ , depending on the signals  $v(t)$  and  
 195  $\beta(t)$ .

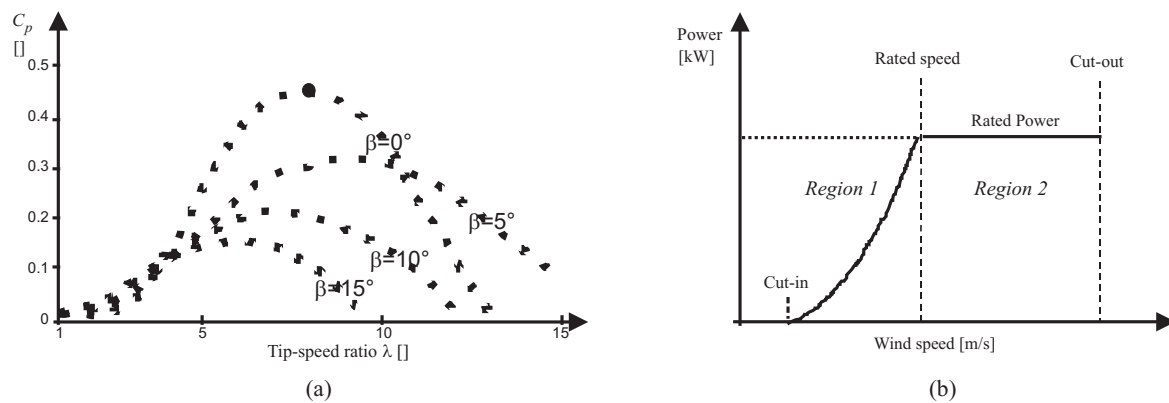


Figure 2. Examples of power coefficient function (a) and power curve (b).

196 It is worth noting that diagram in Figure 2 (b) represents the power curve highlighting the  
 197 working conditions of the wind turbine system, also known as partial load (region 1) and full load  
 198 (region 2) operating situations of the plant [10].

The wind turbine benchmark considered in this work includes a simple two-body linear model of the third order that is exploited to describe the dynamic behaviour of the drive-train. It implements also a simple first-order linear dynamic model of the electric generator and a second order dynamic description of the pitching system, as addressed in more detail in [10]. The overall continuous-time representation of the wind turbine benchmark is represented by the general model in form of Eq. (3):

$$\begin{cases} \dot{x}(t) = f_c(x(t), u(t)) \\ y(t) = x(t) \end{cases} \quad (3)$$

199 with  $u(t) = [\tau_r(t) \beta(t)]^T$  and  $y(t) = [\omega_g(t) P_g(t)]^T$  are the manipulated input signals and the  
 200 controlled output measurements, respectively.  $f_c(\cdot)$  is described by means of a continuous-time  
 201 nonlinear function that will be exploited for representing the complete dynamic behaviour of the  
 202 controlled process. Moreover, since this paper will analyse several data-driven control approaches,  
 203 this system will be used to acquire a number of  $N$  sampled data sequences  $u(k)$  and  $y(k)$ , with



204  $k = 1, 2, \dots, N$ . Furthermore, the variables and parameters of the wind turbine benchmark submodels  
 205 (see e.g. Fig. 1), the static function  $C_p(\beta, \lambda)$ , as well as the errors and uncertain effects affecting  
 206 the input–output measurements were implemented in the simulation code in order to provide a  
 207 high–fidelity wind turbine plant simulator, as highlighted in [10]. In particular, the input and output  
 208 measurements, which are acquired from the wind turbine benchmark, are assumed to be actuated  
 209 and measured by realistic devices introducing additive Gaussian noise processes with zero mean and  
 210 standard deviation values summarised in Table 1 [24].

**Table 1.** Gaussian noise standard deviations of the wind turbine variables.

Variable	$v(t)$	$\omega_r$	$\omega_g$	$\tau_g$	$P_g$	$\beta$
Std. Dev. Value	0.5 m/s	0.025 rad/s	0.05 rad/s	90 Nm	$10^3$ W	0.2 deg

As already highlighted by Fig. 2 (b), the wind turbine control task depends on its working conditions [10]. However, as the wind turbine benchmark recalled in this work operates in nominal conditions, only 2 regions are analysed, as remarked above. In particular, when operating in the working region 1, the turbine is regulated to achieve the optimal power production (below the rated wind speed). On one hand, with reference again to Fig. 2 (b), this is obtained with the blade pitch angle  $\beta$  fixed to 0 degrees. On the other hand, the tip–speed ratio  $\lambda$  of Eq. (2) is settled at its optimal value  $K_{opt}$ . These conditions are obtained according to the peak value of the power coefficient function of the wind turbine, already represented in Figure 2 (a). In this optimal working condition, the reference torque equals the converter one, i.e.  $\tau_g = \tau_r$ , as described by the relation of Eq. (4):

$$\tau_r = K_{opt} \omega_r^2 \quad (4)$$

211 In this situation, the optimal tracking of the power reference is obtained, as soon as the wind speed  
 212  $v(t)$  increases, and the working condition moves to to the control region 2. The control task aims also  
 213 at tracking the power reference  $P_r$ , which is achieved by modifying  $\beta$ , while  $C_p$  is decreasing. The  
 214 advanced control strategies considered in this work tries to maintain the generator speed  $\omega_g$  at its  
 215 nominal value  $\omega_{nom}$  by changing both  $\beta$  and  $\tau_g$ .

Therefore, the control system operating in region 2 exploits the relations in the form of Eqs. (5) when implemented as difference equations [10]:

$$\begin{cases} \beta(k) &= \beta(k-1) + k_p e(k) + (k_i T_s - k_p) e(k-1) \\ e(k) &= \omega_g(k) - \omega_{nom} \end{cases} \quad (5)$$

216 where  $k = 1, 2, \dots, N$  corresponds to the sample indices, and the variable  $\omega_{nom}$  is the given reference  
 217 generator speed, depending on the wind turbine plant. For the case of the wind turbine system  
 218 considered in this work,  $P_r = 4.8\text{MW}$  is the rated power, and  $\omega_{nom} = 162.5\text{rad/s}$ . The standard  
 219 PI governor parameters used for the speed control task were settled to  $k_i = 0.5$  and  $k_p = 3$ , with  
 220 sampling time  $T_s = 0.01$  s [10].

Concerning the regulation of the second input  $\tau_g$ , a further standard PI governor is implemented in the wind turbine benchmark, similarly to the one of Eq. (5), which is described again in its discrete–time formulation of Eqs. (6):

$$\begin{cases} \tau_r(k) &= \tau_r(k-1) + k_p e(k) + (k_i T_s - k_p) e(k-1) \\ e(k) &= P_g(k) - P_r \end{cases} \quad (6)$$

221 This standard PI regulator exploited in the benchmark for the power control task has its parameters  
 222 settled to  $k_i = 0.014$  and  $k_p = 447 \times 10^{-6}$ , as proposed in [10]. Note that the discrete–time regulators

223 of Eqs. (5) and (6) implemented in the wind turbine benchmark and recalled in this study were  
224 simulated with a frequency of 100 Hz, *i.e.* with a sampling interval of  $T_s = 0.01$  s.

225 Finally, Section 4 will consider the performances of these baseline controllers summarised by  
226 the overall laws of Eqs. (4), (5) and (6) proposed in [10] in comparison with the self-tuning control  
227 techniques recalled in Section 3. These methodologies will be applied to both the wind turbine and  
228 the hydroelectric systems, thus highlighting common and different aspects of these solutions with  
229 respect to their working conditions.

## 230 2.2. Hydroelectric Plant Simulator

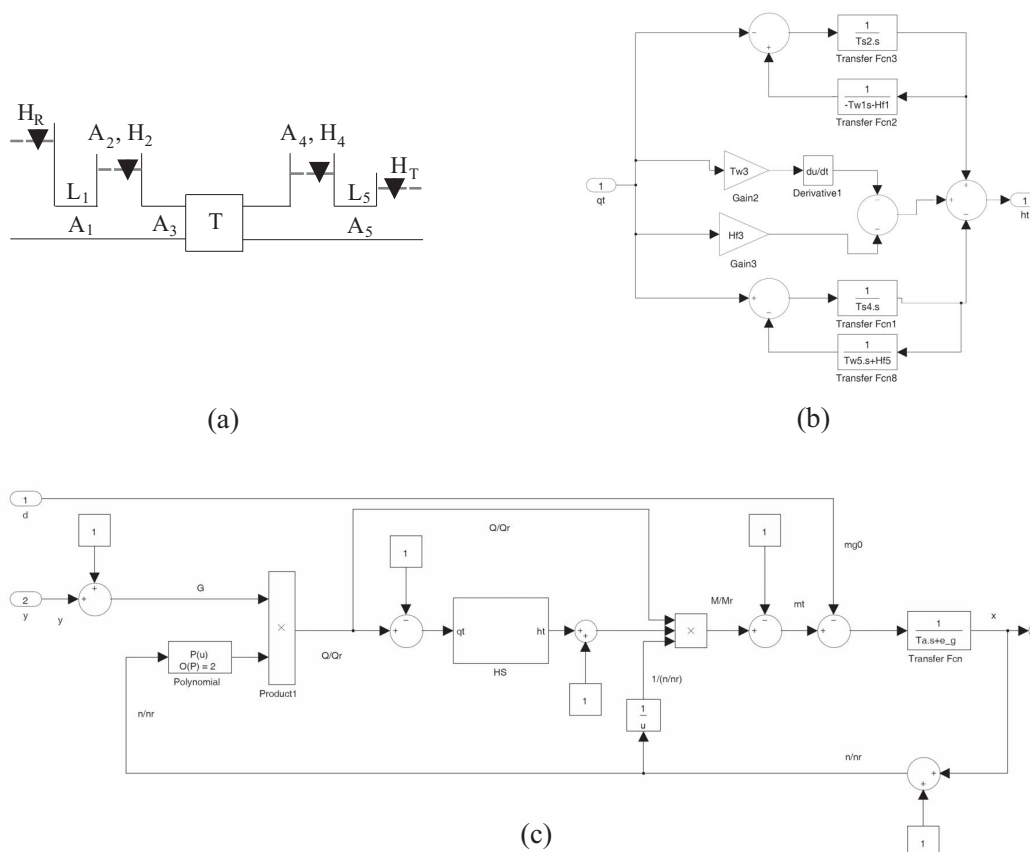
231 It is well-established that hydroelectric systems transform hydraulic renewable source into  
232 useful energies, mostly electric but also mechanical one. However, as for wind turbines, they  
233 must operate according to different load situations. In general, hydroelectric plants must operate  
234 despite of possible variations in the hydropower flow, and in particular in both planned or nominal  
235 conditions and accidental or unplanned situations. Moreover, routine operations such as start-up,  
236 shutdown, load rejection and acceptance may induce important hydraulic transients, possible leading  
237 to dangerous high pressure and sub-pressure variations and oscillations in the hydraulic system.  
238 These situations must be analysed in order to avoid possible mechanical malfunctions and failures.  
239 The same simulation codes already exploited for the development of the wind turbine benchmark  
240 described in Section 2.1, *i.e.* Matlab and Simulink, are the tools exploited for modelling, simulating,  
241 and analysing the behaviour of hydroelectric plants that exhibit important nonlinear dynamics, as  
242 addressed earlier *e.g.* in [26]. More recently, hydropower systems including Pumps as Turbines (PATs)  
243 have been considered by the same authors, since they present challenging aspects in connection  
244 with the control design problem, mainly when implemented for water distribution network and  
245 pipeline applications [27]. In fact, general hydropower plants include special control techniques to  
246 guarantee stable and safe working conditions. Therefore, the same self-tuning control methodologies  
247 already developed for wind turbine systems, as summarised in Section 3, will be considered for the  
248 hydroelectric process described in this paper. Note that, due to the design features of the considered  
249 self-tuning control solutions, they have shown to work properly also when applied to hydroelectric  
250 plants.

251 With reference to the hydroelectric system, which is recalled in this work for analysis and  
252 comparison purposes, consists of a high water head and a long penstock. It includes also upstream  
253 and downstream surge tanks, where a Francis hydraulic turbine is included [28]. This hydroelectric  
254 simulator considered in earlier studies by the same authors, see *e.g.* [11], served to analyse the  
255 transient behaviour of the process with different control schemes. More recent contributions by  
256 the same authors reconsidered the same simulator but for the development of data-driven and  
257 model-based fault diagnosis and fault tolerant control solutions [29]

258 The scheme of this hydroelectric simulator including two surge tanks and the Francis hydraulic  
259 turbine considered in this work is recalled in Fig. 3 [11]. As already remarked, but recalled here  
260 for the readers' convenience, the hydroelectric simulator includes a reservoir with water level  $H_R$ ,  
261 an upstream water tunnel with cross-section area  $A_1$  and length  $L_1$ , an upstream surge tank with  
262 cross-section area  $A_2$  and water level  $H_2$  of appropriate dimensions. A downstream surge tank with  
263 cross-section area  $A_4$  and water level  $H_4$  follows, ending with a downstream tail water tunnel of  
264 cross-section area  $A_5$  and length  $L_5$ . Moreover, between the Francis hydraulic turbine and the two  
265 surge tanks, there is a penstock with cross-section area  $A_3$  and length  $L_3$ . Finally, the right far side  
266 of Fig. 3 (a) highlights a tail water lake with level  $H_T$ . The levels  $H_R$  and  $H_T$  of the reservoir and the  
267 lake water, respectively, are assumed to be constants. Fig. 3 (b) depicts also the scheme of the pure  
268 hydraulic system, and Fig. 3 (c) shows the complete hydroelectric plant simulator.

The mathematical description of the pure hydraulic system, depicted in Fig. 3 (b), which does not include the Francis hydraulic turbine, was proposed earlier in [26] and later in [30]. This model was modified by the authors and presented for the first time in [11]. By considering a pressure water





**Figure 3.** Overall scheme of the hydroelectric process, (b) the hydraulic system, and (c) its complete simulator.

supply system, as addressed in [31], the expressions of the Newton’s second law for a fluid element inside a pipe and the conservation mass law for a control volume can be derived, which take into account the water compressibility and the pipe elasticity. If the penstock is assumed to be relatively short, the water and pipelines are considered incompressible. In this conditions, only the inelastic water hammer effect needs to be considered. Therefore, the simplified and general relation of the penstock has the form of Eq. (7):

$$\frac{h}{q} = -T_w s - H_f \tag{7}$$

as suggested in [31].

Moreover, Eq. (7) represents the transfer function between the flow rate deviation and the water pressure deviation valid for a simple penstock. The variable  $h$  represents the water pressure relative deviation, whilst  $q$  is the flow rate relative deviation. The term  $H_f$  represents the hydraulic loss, with  $s$  the Laplace operator, and  $T_w$  the water inertia time expressed by the relation of Eq. (8):

$$T_w = \frac{L Q_r}{g A H_r} \tag{8}$$

Note that the time variable  $T_w$  of the water inertia described by the relation of Eq. (8) is a function of the hydraulic variable, such as the penstock length  $L$ , the rated flow rate  $Q_r$ , the gravity acceleration  $g$ , the cross-section area  $A$ , and the rated water pressure  $H_r$ . The classic plant represented in Fig. 3 (b) can be separated into 3 subsystems, and namely the upstream water tunnel, the penstock, and the downstream tail water tunnel. The transfer functions between the flow rate deviation and water

pressure deviation transfer functions of the three subsystems are summarised below, by following the approach proposed in [31]. In this hydraulic system, the upstream water tunnel is connected with the reservoir and together with the upstream surge tank. Moreover, taking into account that the upstream water tunnel inlet coincides with the reservoir, and due to the constant value of the inlet water pressure deviation during hydraulic transients, the transfer function between the flow rate and the water pressure deviations of the upstream water tunnel outlet has the form of Eq. (9):

$$\frac{h_1}{q_1} = -T_{w1} s - H_{f1} \quad (9)$$

On the other hand, the downstream tail water tunnel connects the downstream surge tank with the tail water lake. The downstream tail water tunnel outlet is assumed to coincide with the tailwater lake, with constant outlet water pressure deviation. In this way, the transfer function between the flow rate and the water pressure deviations of the downstream tail water tunnel inlet is represented in the form of Eq. (10):

$$\frac{h_5}{q_5} = -T_{w5} s - H_{f5} \quad (10)$$

Usually, the draft tube water inertia is considered within the penstock. Therefore, the transfer function between the flow rate and the water pressure deviations within the penstock are expressed by the relation of Eq. (11):

$$h_t = h_2 - h_4 + h_3 \quad (11)$$

with:

$$\frac{h_3}{q_3} = -T_{w3} s - H_{f3} \quad (12)$$

The relations describing the surge tanks are formulated from the flow continuity at the two junctions, by neglecting the hydraulic losses at surge tank orifices, and represented via the relations of Eqs. (13):

$$\begin{cases} \frac{A_2 H_r}{Q_r} \frac{dh_2}{dt} = q_2 = q_1 - q_3 \\ \frac{A_4 H_r}{Q_r} \frac{dh_4}{dt} = q_4 = q_3 - q_5 \end{cases} \quad (13)$$

In this situation, the surge tank filling time has the form of Eq. (14):

$$T_s = \frac{A H_r}{Q_r} \quad (14)$$

270 Once the description of the hydraulic system of Fig. 3 (b) was developed as proposed in [30], the  
 271 authors included the Francis turbine. Its mathematical model and performance curves summarised  
 272 in this work were obtained in order to describe the dynamic behaviour of a realistic hydroelectric  
 273 process, as addressed in [32]. To this aim, the values of the most important variables the hydraulic  
 274 system and the Francis hydraulic turbine, which represent the overall hydroelectric process simulator  
 275 working at rated conditions are summarised in Table 2:

After these considerations, in the following the procedure for computing the non-dimensional performance curves of the hydraulic turbine considered in this work is briefly recalled. In particular, the non-dimensional water flow rate  $Q/Q_r$  is expressed as a function of the non-dimensional rotational speed  $n/n_r$ , and represented by the second order polynomial of Eq. (15):

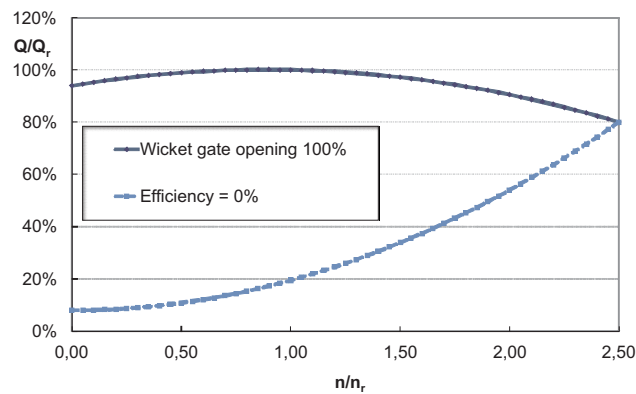
$$\frac{Q}{Q_r} = G \left[ a_1 \left( \frac{n}{n_r} \right)^2 + b_1 \left( \frac{n}{n_r} \right) + c_1 \right] = f_1(n, G) \quad (15)$$

276 Moreover, the relation of Eq. (15) includes the wicket gate opening, described by the  
 277 non-dimensional parameter  $G$ , varying from 0 to 100%. In particular, Fig. 4 represents the curve

**Table 2.** Values of the main parameters of the hydroelectric plant simulator.

Variable	Description	Value
$H_r$	Reservoir water level	400 m
$Q_r$	Water flow rate	36.13 m <sup>3</sup> /s
$P_r$	Hydraulic turbine power	127.6 MW
$n_r$	Turbine rated rotational speed	500 rpm
$\eta_r$	Efficiency rated value	0.90
$M_r$	Turbine-rated torque	2437 kNm

278 derived for  $G = 100\%$ , *i.e.* fully open wicket gate. Moreover, the curve at  $\eta = 0\%$  is also depicted,  
 279 thus defining the operating conditions of the Francis hydraulic turbine. Furthermore, the same  
 280 polynomial curve of Eq. (15) allows the computation of the water flow rate  $Q$  as a function of the  
 281 hydraulic turbine rotational speed  $n$  and its wicket gate opening  $G$  for all working conditions.



**Figure 4.** Representation of the non-dimensional water flow rate  $Q/Q_r$  with respect to the non-dimensional rotational speed  $n/n_r$ .

282 The hydroelectric simulator assumes that the turbine efficiency is constant and equal to its rated  
 283 value  $\eta_r$ , *i.e.* 0.9, as reported in Table 2. Note that the hydroelectric simulator does not include possible  
 284 efficiency variation with the electric load, even if the turbine efficiency  $\eta_r$  could be a function of the  
 285 non-dimensional rotational speed  $n/n_r$ .

On the other hand, the non-dimensional turbine torque  $M$  results a function of the water flow rate  $Q$ , the water level  $H$  and the rotational speed  $n$ , as highlighted by the relation of Eq. (16):

$$\frac{M}{M_r} = \frac{Q}{Q_r} \frac{H}{H_r} \frac{n}{n_r} = f_2(Q, n, G) \quad (16)$$

286 Moreover, the combination of the relations of Eqs. (15) and (16) highlights that the turbine torque  $M$   
 287 is a function of the water flow rate  $Q$ , the rotational speed  $n$  and wicket gate opening  $G$ .

288 Finally, the overall model of the hydroelectric simulator is described by the relations of Eqs. (17)  
289 – (20), which express the non-dimensional variables with respect to their relative deviations:

$$\frac{Q}{Q_r} = 1 + q_t \quad (17)$$

$$\frac{H}{H_r} = 1 + h_t \quad (18)$$

$$\frac{n}{n_r} = 1 + x \quad (19)$$

$$G = 1 + y \quad (20)$$

290 with  $q_t$  is the turbine flow rate relative deviation,  $h_t$  the turbine water pressure relative deviation,  
291  $x$  the turbine speed relative deviation, and  $y$  the wicket gate servomotor stroke relative deviation.  
292 Moreover, the relation of Eq. (20) allows only negative values of  $y$ .

On the other hand, when the generator unit and its network are considered, and in particular the generator unit is connected only to an isolated load, the load characteristic of the the generator unit are described by the dynamic model of Eq. (21):

$$\frac{x}{m_t - m_{g0}} = \frac{1}{T_a s + e_g} \quad (21)$$

293 with  $m_{g0}$  being the load torque,  $T_a$  representing the generator unit mechanical time, whilst the  
294 parameter  $e_g$  is the load self-regulation factor. The variables and parameters of the hydroelectric  
295 model were selected according to the work [30] in order to represent a realistic hydroelectric plant  
296 simulator. Moreover, as for the wind turbine benchmark, the signals that can be acquired from the  
297 actuator and sensors of the hydroelectric plant are modelled as the sum of the actual variables and  
298 stochastic noises, as proposed in [33].

With reference to the control strategies for classic hydroelectric plants, standard PID regulators are used to compensate the hydraulic turbine speed. Therefore, the actuated signal  $u$  is computed as sum of the proportional, integral, and differential terms of the error  $x$  in Eq. (19), expressed in the form of Eq. (22):

$$u = x \left( K_p + \frac{K_i}{s} + \frac{K_d s}{1 + T_n s} \right) \quad (22)$$

299 with  $K_p$  being the proportional gain,  $K_i$  the integral gain, and  $K_d$  the derivative gain.  $T_n$  is the  
300 parameter of the derivative filter time constant. The hydroelectric simulator considered in this work  
301 exploits an electric servomotor that is used as a governor. The same simulator was already proposed  
302 by the authors but with different purposes in [29].

The servomechanism implemented in the hydroelectric simulator is described as a first-order model, which relates the control signal  $u$  with the wicket gate servomotor stroke  $y$  according to Eq. (23) [30]:

$$\frac{y}{u} = \frac{1}{T_y s + 1} \quad (23)$$

303 with  $T_y$  representing the wicket gate servomotor response time.

304 This concludes the description of the complete nonlinear simulator of a typical hydroelectric  
305 plant consisting of two surge tanks and a Francis hydraulic turbine, as represented in Fig. 3.

306 Note finally that the nonlinear behaviour of the Francis hydraulic turbine and the inelastic water  
307 hammer effects were taken into account to compute and simulate realistic hydraulic transients. Due  
308 to its nonlinear characteristics, traditional regulation techniques can rely on conventional controllers  
309 implementing on-off strategies. Standard PID controllers are also considered for their relative  
310 simplicity. However, as remarked *e.g.* in [30] and by the authors in their earlier work [11], classic  
311 control solutions can produce unsatisfactory responses, with high overshoot and long settling time.

312 Moreover, the tuning of the regulator parameters is difficult, as highlighted in [30], since a gain  
313 scheduling of the PID parameters would have been required. Thus, advanced control strategies  
314 that were already proposed for the wind turbine benchmark and recalled in Section 3 will be briefly  
315 summarised and applied to the hydroelectric simulator, as shown in Section 4. Extended simulations,  
316 comparisons, and the sensitivity analysis of the proposed solutions represent one of the key points of  
317 this paper.

318 Finally, it is worth noting that some relations of the hydroelectric system have been linearised, see  
319 *e.g.* Eqs. (7) and (17). However, this simplified model has been considered for comparison purpose,  
320 as the nonlinear parts of the processes under investigation are closer, as highlighted by Eqs. (1) and  
321 (15).

### 322 3. Advanced Control Techniques for Energy Conversion Systems

323 This section revises the main control issues and objectives that can be valid for both wind turbine  
324 and hydroelectric processes, whilst Section 3.1 summarises those self-tuning control methodologies  
325 that will be designed and compared when applied to the considered energy conversion benchmark  
326 and simulator.

327 In general, control systems exploit design algorithms that force a dynamic model to track  
328 prescribed references or set-point, such that fixed objectives or behaviour modes are achieved. In  
329 this way, the classic control problem is formulated as tracking task, where the system output has  
330 to follow the set-point, thus representing the final objective. Tasks expressed in this form are also  
331 present in energy conversion applications, for example the speed control of both wind and hydraulic  
332 turbines. However, it could be useful to improve the problem descriptions and to give a deeper  
333 insight into possible solutions, in order to achieve all potentials of control theory when applied to  
334 energy conversion systems.

335 The complete definition of the control problem usually requires the optimisation of a given  
336 prescribed performance index (such as the maximum energy conversion, the minimum power loss)  
337 subjected to suitable physical constraints (*e.g.* saturations, amplitudes, rates, forces, torques, etc), thus  
338 leading to a constrained minimisation or maximisation problem. The considerations raised here agree  
339 with the aim of a standard controlled system including a feedback loop. In fact, the objective index  
340 usually represents some metrics (the most common is the quadratic one) of the difference between  
341 the reference (*i.e.* the desired value) with respect to the controlled output. This is the well-known  
342 tracking error of the monitored output with respect to the set-point. Therefore, the desired behaviour  
343 of the controlled process in closed-loop is usually defined in several ways, which represent also  
344 the working principles of the control techniques recalled in Section 3.1. First, with reference to the  
345 process output, the desired transient or steady-state responses can be considered, as for the case  
346 of self-tuning PID regulators summarised in Section 3.1.1. On the other hand, if the frequency  
347 behaviour is taken into account, the desired closed-loop poles can be fixed as roots of the closed-loop  
348 transfer function. This represent the design approach used by the adaptive strategy considered in  
349 Section 3.1.3. Moreover, when robust performances are included, the minimisation of the sensitivity  
350 of the closed-loop system with respect to the model-reality mismatch or external disturbances can be  
351 considered. This approach is related for example to the fuzzy logic methodology reported in Section  
352 3.1.2. Furthermore, for the case of optimal control, the trade-off between control energy and tracking  
353 error has to be evaluated. Control issues related to the model-reality mismatch and the disturbance  
354 sensitivity concern the system robustness and reliability. Specific control strategies addressing these  
355 objectives have been proposed since the late 1970's. In general, the proposed design methodologies  
356 lead to explicit solution for the feedback control laws. Some other strategies provide solutions to this  
357 optimisation problem when it is defined at each time step, as for the case of the Model Predictive  
358 Control (MPC) with disturbance decoupling considered in Section 3.1.4. The considered strategy  
359 integrates the advantages of the MPC solution with the disturbance compensation feature. Therefore,  
360 different data-driven and model-based control solutions that may be successfully used for the control



361 of both the wind turbine benchmark and the hydroelectric plant simulator will be recalled in Section  
 362 3.1.

363 Under these considerations, the general control principle followed in this paper is sketched in  
 364 Fig. 5. It consists of the optimal set-point generation and the closed-loop design to achieve the  
 365 reference tracking. These two phases have to take into account of the system physical constraints. For  
 366 example, the wind turbine system relies on a variable speed turbine, which requires the computation  
 367 of the optimal rotational speed ( $\omega_r$  or  $\omega_g$ ) for the regions 1 and 2 of the power curve reported in  
 368 Fig. 2 (b). Moreover, the reference torque  $\tau_r$  and the blade pitch control  $\beta$  are also exploited to  
 369 obtain the needed rotational velocity  $\omega_g$ . On the other hand, the hydroelectric system requires an  
 370 optimal velocity reference  $n_r$  that is obtained for this plant, and the control of  $u$  and  $y$  allows to  
 371 track  $n$  according to the desired value  $n_r$ . Moreover, the relation of Eq. (16) highlights that the  
 372 non-dimensional turbine torque  $M$  depends on the water flow rate  $Q$ , the water level  $H$  and the  
 373 rotational speed  $n$ . Furthermore, by including the relation of Eq. (15), the turbine torque  $M$  results a  
 374 function of the water flow rate  $Q$ , the rotational speed  $n$  and wicket gate opening  $G$ .

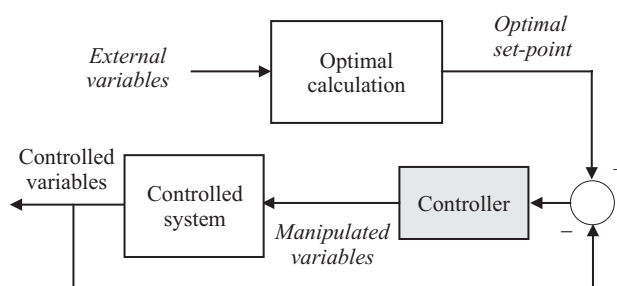


Figure 5. Reference computation for the general closed-loop scheme.

375 Finally, it is worth noting that model-based control designs rely on the mathematical  
 376 descriptions of the process models, in order to derive the control laws. The design of standard PID  
 377 regulators and Model Predictive Control (MPC) methods follows a model-based approach, which  
 378 will be illustrated in Sections 3.1.1 and 3.1.4, respectively. However, the need for these high-fidelity  
 379 mathematical descriptions can require much more effort than the derivation of the controller models.  
 380 Therefore, dynamic system identification methodologies have been successfully proposed in order  
 381 to determine the so-called black-box or gray-box representations, as addressed *e.g.* in [34], which  
 382 is also used for the self-tuning PID design. Usually, these descriptions do not present structural  
 383 relationships to the physical processes. On the other hand, dynamic system identification schemes can  
 384 be also exploited for deriving adaptive controller prototypes, which are thus able to adapt themselves  
 385 with respect to unknown conditions or time-varying systems. By means of this 'self-tuning mode',  
 386 adaptive control strategies relying on linear models of the controlled process are also able to track  
 387 changes of the plant. Examples of these data-driven approaches are represented by the fuzzy logic  
 388 and adaptive controllers recalled in Sections 3.1.2 and 3.1.3, respectively. On the other hand, the  
 389 MPC strategy exploits the proposed disturbance compensation method, which is thus able to cope  
 390 with uncertainty and model-reality mismatch effects. Note however that, in general, the optimal  
 391 regulation of nonlinear systems is achieved via purely nonlinear controllers [35]. The stability and  
 392 convergence properties achieved by the use of adaptive controllers should be carefully analysed over  
 393 all operating conditions, as addressed in [14]

### 394 3.1. Data-Driven and Model-Based Control Methodologies

395 This section describes briefly several control schemes consisting of self-tuning PID controllers,  
 396 and Artificial Intelligence (AI) strategies, such as fuzzy logic and adaptive methods, as well as Model  
 397 Predictive Control (MPC) approach. Some of them were already proposed by the authors for the

398 application to wind turbine and wind park installations, *e.g.* in [34]. These methodologies will be  
 399 applied, compared and discussed in Section 4, when considered for both the wind turbine benchmark  
 400 and the hydraulic plant simulator.

In general, the mathematical formulation of the control law can be provided as linear or nonlinear dynamic function  $\mathcal{F}$  in the form of Eq. (24):

$$u(t) = \mathcal{F}(y(t)) \quad (24)$$

401 with  $y(t)$  being the monitored output, whilst  $u(t)$  is the control input. The control techniques  
 402 proposed for the systems under investigation should lead to the computation of the control law of  
 403 Eq. (24) generating the input  $u(t)$  that allows to track the given reference or set-point  $r(t)$  for the  
 404 controlled output  $y(t)$ .

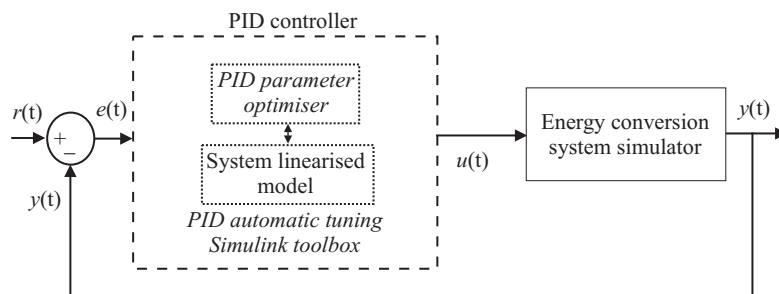
405 Finally, the implementation of the different control techniques is sketched below.

### 406 3.1.1. Autotuning Model-Based PID Control

Industrial processes commonly exploit closed-loop including standard PID controllers, due to their simple structure and parameter tuning [36]. The control law depends on the tracking error  $e(t)$  defined by the difference between the desired and the measured output signals, *i.e.*  $e(t) = r(t) - x(t)$ . This signal is injected into the controlled process after proportional, integral and derivative computations. Therefore, the continuous-time control signal  $u(t)$  is generated by the PID regulator in the form of Eq. (25):

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt} \quad (25)$$

407 with  $K_p$ ,  $K_i$ ,  $K_d$  being the PID proportional, integral, and derivative gains, respectively. The most  
 408 common strategy exploited for the computation of the optimal parameters of the PID governor  
 409 uses proper Ziegler-Nichols formulas, as described in [36]. However, with the development of  
 410 relatively recent automatic software routines, the PID optimal parameters can be easily determined  
 411 by means of direct tuning algorithms implemented for example in the Simulink environment. These  
 412 strategies require the definition of the controlled process as Simulink model, such that they balance  
 413 the input-output performances of the monitored system in terms of response time and stability  
 414 margins (robustness) [36]. In particular, the PID automatic tuning procedure implemented in the  
 415 Simulink toolbox performs the computation of the linearised model of the energy conversion systems  
 416 studied in this paper. The logic scheme of this procedure is sketched in Fig. 6.



**Figure 6.** Block diagram of the monitored system controlled by the PID regulator with automatic tuning.

417 Note finally that the PID block in Fig. 6 performs the computation of a linearised model of the  
 418 controlled system, if required. Therefore, the optimiser included in the PID block and implemented in  
 419 the Simulink environment derives of the PID parameters that minimise suitable performance indices,  
 420 as described in [36].

### 421 3.1.2. Data–Driven Fuzzy Logic Control

422 Fuzzy Logic Control (FLC) solutions are often exploited when the dynamics of the monitored  
 423 process are uncertain and can present nonlinear characteristics. The design method proposed in this  
 424 work exploits the direct identification of rule–based Takagi–Sugeno (TS) fuzzy prototypes. Moreover,  
 425 the fuzzy model structure, *i.e.* the number of rules, the antecedents, the consequents and the fuzzy  
 426 membership functions can be estimated by means of the Adaptive Neuro–Fuzzy Inference System  
 427 (ANFIS) toolbox implemented in the Simulink environment [37]. The authors already suggested to  
 428 employ regulators in the form of TS fuzzy models for designing fault diagnosis and fault tolerant  
 429 control strategies presented *e.g.* in [29].

The TS fuzzy prototype relies on a number of rules  $R_i$ , whose consequents are deterministic functions  $f_i(\cdot)$  in the form of Eq. (26):

$$R_i : \text{IF } x \text{ is } A_i \text{ THEN } u_i = f_i(x) \quad (26)$$

where the index  $i = 1, 2, \dots, K$  describes the number of rules  $K$ ,  $x$  is the input vector containing the antecedent variables, *i.e.* the model inputs, whilst  $u_i$  represents the consequent output. The fuzzy set  $A_i$  describing the antecedents in the  $i$ –th rule is described by its (multivariable) membership function  $\mu_{A_i}(x) \rightarrow [0, 1]$ . The relation  $f_i(x)$  assumes the form of parametric affine model represented by the  $i$ –th relation of Eq. (27):

$$u_i = a_i^T x + b_i \quad (27)$$

430 with the vector  $a_i$  and the scalar  $b_i$  being the  $i$ –th submodel parameters. The vector  $x$  consists of  
 431 a proper number  $n$  of delayed samples of input and output signals acquired from the monitored  
 432 process. Therefore, the term  $a_i^T x$  is an Auto–Regressive eXogenous (ARX) parametric dynamic model  
 433 of order  $n$ , and  $b_i$  a bias.

The output  $u$  of the TS fuzzy prototype is computed as weighted average of all rule outputs  $u_i$  in the form of Eq. (28):

$$u = \frac{\sum_{i=1}^K \mu_{A_i}(x) y_i(x)}{\sum_{i=1}^K \mu_{A_i}(x)} \quad (28)$$

434 The estimation scheme implemented by the ANFIS tool follows the classic dynamic system  
 435 identification experiment. First, the structure of the TS fuzzy prototype is defined by selecting a  
 436 suitable order  $n$ , the shape representing the membership functions  $\mu_{A_i}$ , and the proper number of  
 437 clusters  $K$ . Therefore, the input–output data sequences acquired from the monitored system are  
 438 exploited by ANFIS for estimating the TS model parameters and its rules  $R_i$  after the selection of a  
 439 suitable error criterion. The optimal values of the controller parameters represented by the variables  
 440  $a_i$  and  $b_i$  of (27) are thus estimated [38].

441 The work proposes also a strategy different from ANFIS that can be exploited for the estimation  
 442 of the parameters of the fuzzy controller. This method relies on the Fuzzy Modelling and  
 443 Identification (FMID) toolbox designed in the Matlab and Simulink environments as described in  
 444 [39]. Again, the computation of the controller model is performed by estimating the rule–based  
 445 fuzzy system in the form of Eq. (28) from the input–output data acquired from the process under  
 446 investigation. In particular, the FMID tool uses the Gustafson–Kessel (GK) clustering method [39] to  
 447 perform a partition of input–output data into a proper number  $K$  of regions where the local affine  
 448 relations of Eq. (27) are valid. Also in this case, the fuzzy controller model of Eq. (28) is computed  
 449 after the selection of the model order  $n$  and the number of clusters  $K$ . The FMID toolbox derives the  
 450 variables  $a_i$  and  $b_i$ , as well as the identification of the shape of the functions  $\mu_{A_i}$  by minimising a given  
 451 metric [39].

452 Note that the overall digital control scheme consisting of the discrete–time fuzzy regulator of Eq.  
 453 (28) and continuous–time nonlinear system of Eq. (24) includes also Digital–to–Analog (D/A) and  
 454 Analog–to–Digital (A/D) converters, as shown in Figure 7.

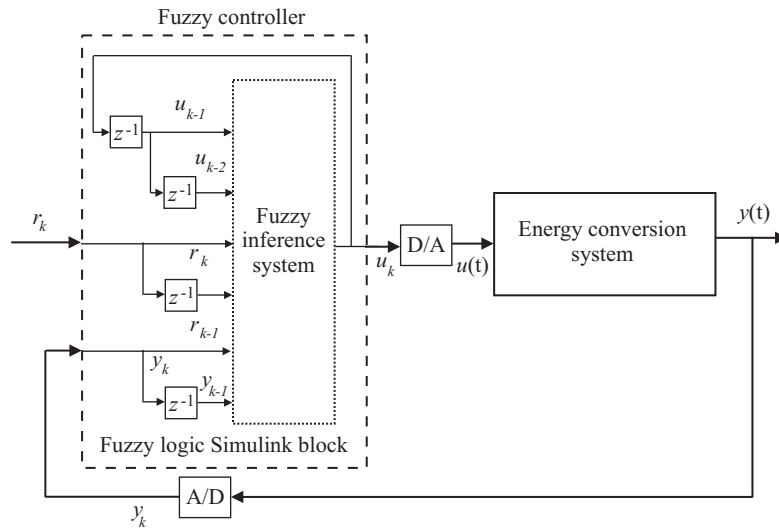


Figure 7. Block diagram of the monitored system controlled by the fuzzy regulator.

455 With reference to Figure 7, note finally that the fuzzy controller block implemented in the  
 456 Simulink environment includes a suitable number  $n$  of delayed samples of the signals acquired from  
 457 the monitored process. Moreover, the fuzzy inference system in Figure 7 implements the TS model of  
 458 Eq. (28). The delay  $n$ , the membership functions  $\mu_{A_i}$ , and the number of clusters  $K$  are estimated by  
 459 the FMID and the ANFIS toolboxes, as described in [39].

### 460 3.1.3. Data-Driven Adaptive Control

The adaptive control technique proposed in this work relies on the recursive estimation of a 2-nd order discrete-time transfer function  $G(z)$  with time-varying parameters described by Eq. (29):

$$G(z) = \frac{\beta_1 z^{-1} + \beta_2 z^{-2}}{1 + \alpha_1 z^{-1} + \alpha_2 z^{-2}} \quad (29)$$

461 where  $\alpha_i$  and  $\beta_i$  are identified on-line at each sampling time  $t_k = kT$ , with  $k = 1, 2, \dots, N$ , for  $N$   
 462 samples, and  $T$  being the sampling interval.  $z^{-1}$  indicates the unit delay operator. A viable and  
 463 direct way for deriving the model parameters in Eq. (29) that is proposed in this work is based on  
 464 the Recursive Least-Square Method (RLSM) with directional forgetting factor, which was presented  
 465 in [40]. Note that the authors suggested to use on-line techniques also for the development of fault  
 466 tolerant control system, as described in [29].

Once the parameters of the model of Eq. (29) have been derived, this paper proposes to compute the adaptive controller in the form of Eq. (30):

$$u_k = q_0 e_k + q_1 e_{k-1} + q_2 e_{k-2} + (1 - \gamma) u_{k-1} + \gamma u_{k-2} \quad (30)$$

with  $e_k$  and  $u_k$  represent the sampled values of the tracking error  $e(t)$  and the control signal  $u_k$  at the time  $t_k$ , respectively. With reference to the description of Eq. (30), by following a modified Ziegler-Nichols criterion,  $q_0$ ,  $q_1$ ,  $q_2$ , and  $\gamma$  represent the adaptive controller parameters, which are

derived by solving a Diophantine equation. As described in [40], by considering the recursive 2-nd order model of Eq. (29), this technique leads to the relations of Eqs. (31):

$$\begin{cases} q_0 = \frac{1}{\beta_1} (d_1 + 1 - \alpha_1 - \gamma) \\ \gamma = \frac{s_1 \beta_2}{r_1 a_2} \\ q_1 = \frac{\alpha_2}{\beta_2} - \frac{s_1}{r_1} \left( \frac{\beta_1}{\beta_2} - \frac{\alpha_1}{a_2} + 1 \right) \\ q_2 = \frac{s_1}{r_1} \end{cases} \quad (31)$$

where:

$$\begin{cases} r_1 = (b_1 + b_2) (a_1 b_2 b_1 - a_2 b_1^2 - b_2^2) \\ s_1 = a_2 ((b_1 + b_2) (a_1 b_2 - a_2 b_1) + b_2 (b_1 d_2 - b_2 d_1 - b_2)) \end{cases} \quad (32)$$

Note that the design technique proposed in this work and represented by the relations of Eqs. (31) and (32) assumes that the behaviour of the overall closed-loop system can be approximated by a 2nd order transfer function with characteristic polynomial represented by Eq. (33):

$$D(s) = s^2 + 2\delta\omega s + \omega^2 \quad (33)$$

with  $\delta$  and  $\omega$  being the damping factor and natural frequency, respectively.  $s$  is the derivative operator. Furthermore, if  $\delta \leq 1$ , the following relations are used [40]:

$$\begin{cases} d_1 = -2e^{-\delta\omega T} \cos(\omega T\sqrt{1-\delta^2}) \\ d_2 = e^{-2\delta\omega T} \end{cases} \quad (34)$$

467 This paper suggested this adaptive control technique since both the recursive estimation procedure  
468 of Eq. (29) and the on-line computation of the control law of Eq. (30) are available from the digital  
469 Self-Tuning Controller Simulink Library (STCSL) described in [40]. According to this solution, the  
470 output  $y_k$  of the time-varying model of Eq. (29) follows the reference signal  $r_k$  when the control law  
471 of Eq. (30) is . The achievable performances depend on the design parameters given by Eq. (33).

472 The on-line control law of Eq. (30) is used for the regulation of the continuous-time nonlinear  
473 system of Eq. (24) by including D/A and A/D converters, as highlighted in the scheme of Figure 8.

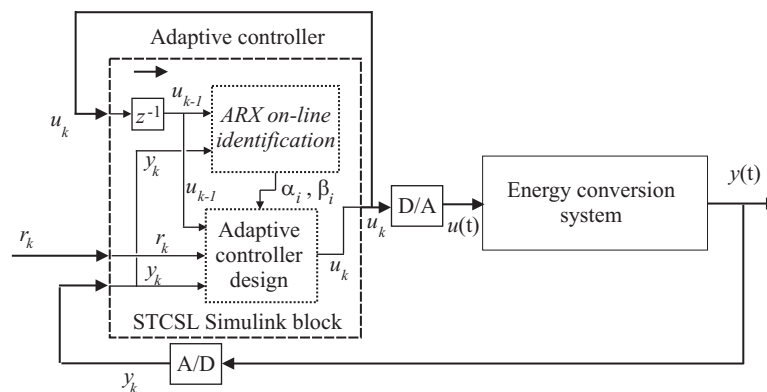


Figure 8. Block diagram of the monitored system controlled by the adaptive regulator.



Note finally that the adaptive control sketched in Figure 8 is implemented via the STCSL block in the Simulink environment. It includes the module performing the on-line identification of the ARX model of Eq. (29), which is used for the adaptive controller design in the form of Eq. (30) [40].

#### 3.1.4. MPC with Disturbance Decoupling

The general structure of the proposed MPC is illustrated in Figure 9, with the MPC managing objectives and constraints of the control inputs. The MPC works as a standard MPC controller when the nominal plant is considered, and generates the reference inputs. In the presence of disturbance or uncertainty effects, the considered solution provides the reconstruction of the equivalent disturbance signal acting on the plant. This represent the key feature of this structure, which compensates the disturbance effect and 'hide' it to the overall system. In this way, it decouples the disturbance effect from the nominal MPC design. Another feature of this structure is the management of the objectives and constraints through the MPC design. These objective and constraints can be the nominal ones. But in case of disturbance or uncertainty, when the nominal performance cannot be achieved, the objectives could be switched to degraded ones and the constraints can also be updated if necessary. The powerful tool to achieve the required fault tolerance characteristic is the optimisation lying in the MPC design itself.

The overall scheme is thus represented aim by the MPC design with disturbance compensation, such that the compensated system has response very similar to the nominal system and the constraints are not violated. The fault compensation problem within the MPC framework is defined as follows. Given a state-space representation of the considered system affected by disturbance or uncertainty has the following form:

$$\begin{cases} \dot{x}_l &= A_l x_l + B_l u + B_d d + w \\ y_l &= C_l x_l + v \end{cases} \quad (35)$$

and its nominal reference model:

$$\begin{cases} \dot{x}_r &= A_l x_r + B_l u_r \\ y_r &= C_l x_r \end{cases} \quad (36)$$

the disturbance compensation problem is solved by finding the control input  $u$  that minimises the cost function:

$$J = \int_t^{t+N_c \Delta t} \left( \|x_l - x_r\|_Q^2 + \|\dot{u}\|_R^2 \right) d\tau \quad (37)$$

given the reference input  $u_r$ .

In Eq. (35) the matrices  $A_l$ ,  $B_l$ ,  $B_d$  and  $C_l$  are of proper dimensions. The vector  $y_l$  represents the output measurements,  $x_l$  is the state of the model with disturbance, whilst  $x_r$  is the reference state, and  $y_r$  the reference output, corresponding to the reference input  $u_r$  of the nominal model. The vectors  $w$  and  $v$  include the model mismatch and the measurement error, respectively.  $d$  represents the equivalent disturbance signal. In Eq. (37)  $t$  is the current time,  $\Delta t$  is the control interval, and  $N_c$  is the length of the control horizon.  $Q$  and  $R$  are suitable weighting matrices. Note that the model of Eq. (35) can be derived by nonlinear model linearisation or identification procedures, as suggested in Sections 3.1.1 and 3.1.3, respectively.

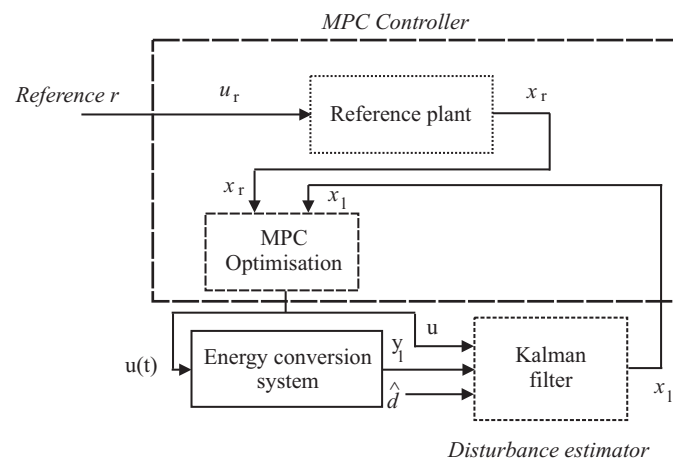
This work proposes to solve the problem in two steps: the reconstruction of the disturbance  $d$ , *i.e.*  $\hat{d}$ , provided by the disturbance estimation module, and the MPC tool. Due to the model-reality mismatch and the measurement error in (35), the Kalman filter (38) is used to provide the estimation of the state vector  $x_l$ , the output  $y_l$  of the system affected by the estimated disturbance  $\hat{d}$ :

$$\begin{cases} \dot{x}_l &= A_l x_l + B_l u - B_l \hat{d} + K_f (y_l - C_l x_l) \\ y_l &= C_l x_l \end{cases} \quad (38)$$

where  $K_f$  is the Kalman filter gain. In this way, based on the estimations  $\hat{d}$  and  $x_l$ , an MPC is designed, which contains the reference model of Eq. (36) and the filtered system of Eq. (38), with  $\hat{d}$  provided by the Kalman filter. Moreover, the MPC has the objective function:

$$\int_t^{t+N_c \Delta t} \left[ (x_l - x_r)^T Q (x_l - x_r) + \dot{u}^T R \dot{u} \right] d\tau \quad (39)$$

499 in which  $x_l$  and  $x_r$  are the states of the filtered and the reference models, respectively. The integrated  
 500 MPC with the Kalman filter solves this general disturbance compensation problem, as long as the  
 501 estimations of both the state and the disturbance are correct. An illustration of the structure of the  
 502 fault compensated MPC is shown in Figure 9.



**Figure 9.** Block diagram of the monitored system controlled via the disturbance compensated MPC scheme.

503 The global estimation and control scheme is a nonlinear MPC problem with the nominal model  
 504 for the considered energy conversion systems of Eq. (35), the disturbance  $d$  with its estimator,  
 505 and the Kalman filter of Eq. (38) as prediction model. The local observability of the model of Eq.  
 506 (35) is essential for state estimation, which is easily verified. The implementation of the proposed  
 507 disturbance compensation strategy has been integrated into the MPC Toolbox of the Simulink  
 508 environment.

509 Note finally that the authors applied the MPC technique to the Fault Tolerant Control (FTC)  
 510 framework in [41].

#### 511 4. Results, Comparisons and Discussions

This work recalled different control techniques as reported in Section 3 that are proposed to compensate the outputs of both the wind turbine benchmark and the hydroelectric plant simulator summarised in Section 2. On the other hand, this section presents the simulations achieved in the Matlab and Simulink environments implementing these control techniques by means of the tools recalled in Section 3.1. The obtained results are evaluated via the percent Normalised Sum of Squared Error (NSSE%) performance function in the form of Eq. (40):

$$NSSE\% = 100 \sqrt{\frac{\sum_{k=1}^N (r_k - o_k)^2}{\sum_{k=1}^N r_k^2}} \quad (40)$$

512 with  $r_k$  being the sampled reference or set-point  $r(t)$ , whilst  $o_k$  is the sampled continuous-time signal  
 513 representing the generic controlled output  $y(t)$  of the process. In particular, this signal is represented

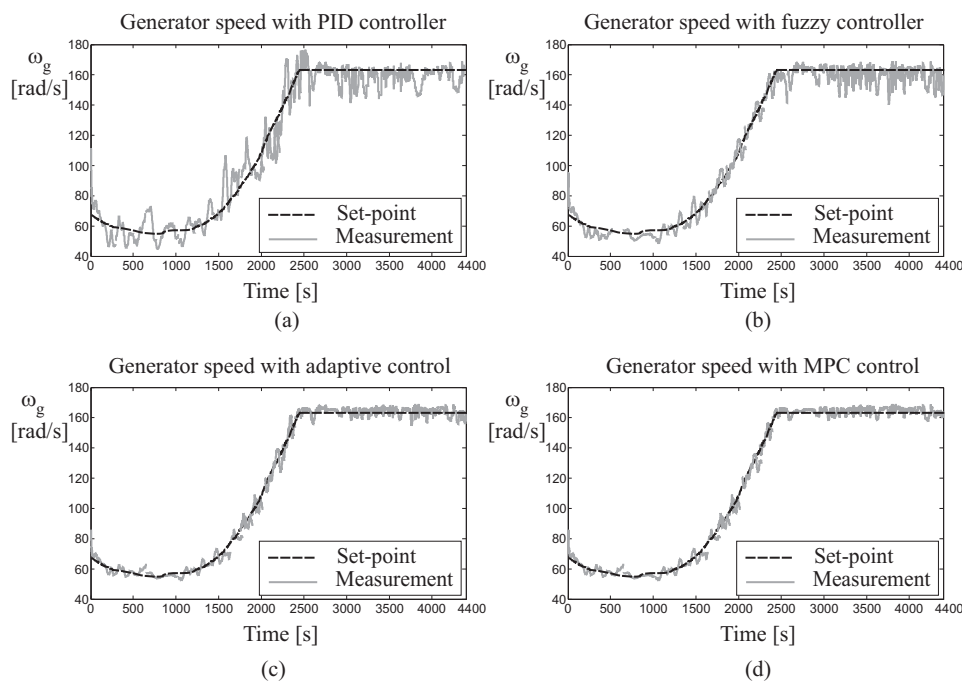
514 by the wind turbine generator angular velocity  $\omega_g(t)$  in Eq. (3), and the hydraulic turbine rotational  
 515 speed  $n$  in Eq. (19) for the hydroelectric plant.

516 Note that the wind turbine benchmark and the hydroelectric plant simulator of Section 2 allow  
 517 the generation of several input–output data sequences due to different wind speed  $v(t)$  effects (see *e.g.*  
 518 (1)) and hydraulic transient under variable loads  $m_{g0}$  (see *e.g.* (21)), respectively. Moreover, in order to  
 519 obtain comparable working situations, the wind turbine benchmark has been operating from partial  
 520 to full load conditions, as highlighted in Figure 2 (b). It is thus considered the similar maneuver  
 521 of the hydroelectric system operating from the start–up to full load working condition. After these  
 522 considerations, Section 4.1 summarises the results obtained from the wind turbine benchmark first.  
 523 Then, the same control techniques will be verified when applied to the hydroelectric simulator.

524 It is worth highlighting that the simulations considered in this work take into account  
 525 disturbance and uncertainty effects. In fact, the hydroelectric plant considers a load disturbance,  
 526 whilst the turbine simulator is driven by wind, which represents the main disturbance source.  
 527 Moreover, the uncertainty effect has been analysed in Section 4.2.

#### 528 4.1. Control Technique Performances and Comparisons

529 Figure 10 reports the results achieved with the control methodologies and the tools summarised  
 530 in Section 3.1. In particular, Figure 10 depicts the wind turbine generator angular velocity  $\omega_g$  when  
 531 the wind speed  $v(t)$  changes from 3 m/s to 18 m/s for a simulation time of 4400s. This simulation time  
 532 is defined by the wind turbine benchmark in [10,42] using a real wind sequence sampled for 4400s.  
 533 Moreover, the initial value of the signal  $\omega_g$  is different from zero since the simulation commences  
 534 when the wind speed has already exceeded the cut–in value highlighted in Figure 2 (b).



**Figure 10.** Wind turbine controlled output compensated by (a) the autotuning PID regulator, (b) the fuzzy controller, (c) the adaptive regulator, and (d) the MPC approach with disturbance decoupling.

535 In detail, with reference to the picture in Figure 10 (a), the parameters of the PID regulator of  
 536 Eq. (25) have been determined using the model–based autotuning tool available in the Matlab and  
 537 Simulink environments. They were settled to  $K_p = 4.0234$ ,  $K_i = 1.0236$ ,  $K_d = 0.0127$ , as described in  
 538 Section 3.1.1. The achieved performances are better than the ones obtained with the baseline control  
 539 laws proposed in [10] and recalled in Section 2.1.

540 Moreover, Figure 10 (b) shows the simulations achieved with the data-driven fuzzy  
541 identification approach recalled in Section 3.1.2. This strategy was proposed here since it represents  
542 a viable and practical way for deriving the models of the controllers by means of the so-called  
543 model reference control approach, as addressed in [43]. According to this strategy, the baseline PID  
544 regulators designed for the nominal wind turbine model were considered as reference controllers for  
545 the generation of the input–output data used by the identification methodology recalled in Section  
546 3.1.2. In this way, the TS fuzzy controller parameters are estimated such that they optimise the  
547 performances in terms of tracking error. In particular, a sampling interval  $T = 0.01\text{s}$  has been  
548 exploited, and the TS fuzzy controller of Eq. (28) has been obtained for a number  $K = 3$  of Gaussian  
549 membership functions, and a number  $n = 2$  of delayed inputs and output. The antecedent vector in  
550 Eq. (27) is thus  $x = [e_k, e_{k-1}, e_{k-2}, u_{k-1}, u_{k-2}]$ . Both the data-driven FMID and ANFIS tools available  
551 in the Matlab and Simulink environments provide also the optimal identification of the shapes of the  
552 fuzzy membership functions  $\mu_{A_i}$  of the fuzzy sets  $A_i$  in Eq. (26).

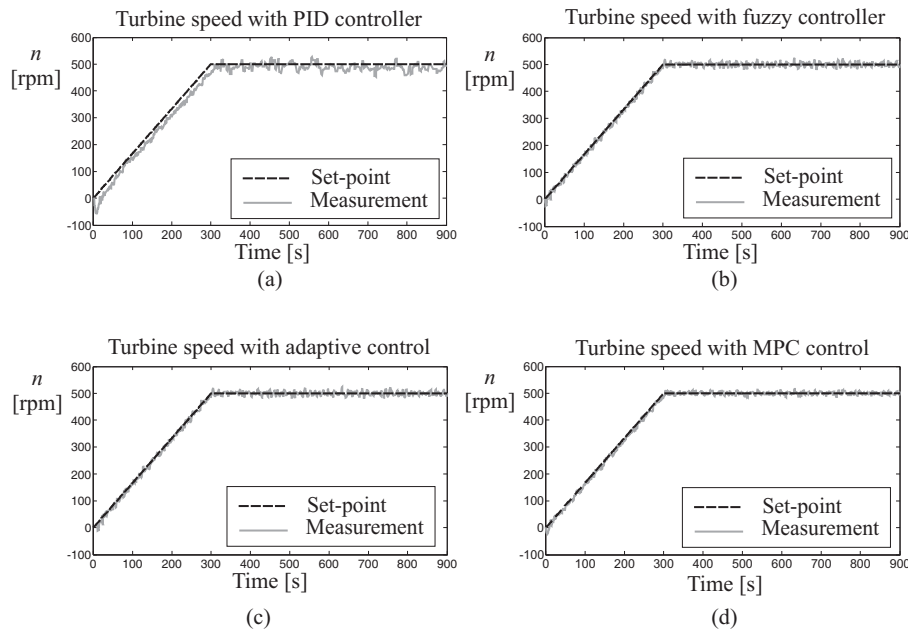
553 On the other hand, the picture in Figure 10 (c) shows the capabilities of the adaptive controller of  
554 Eq. (30). The time-varying parameters of this data-driven control technique summarised in Section  
555 3.1.3 have been computed on-line via the relations of Eqs. (31) with the damping factor and the  
556 natural frequency variables  $\delta = \omega = 1$  in Eq. (33). As already remarked, this work considered this  
557 data-driven adaptive technique since it was already implemented in the Simulink environment via  
558 the Self Tuning Controller Simulink Library (STCSL) [40].

559 Finally, the picture of Figure 10 (d) highlights the results achieved with the MPC technique with  
560 disturbance decoupling recalled in Section 3.1.4. The state-space model of the wind turbine nonlinear  
561 system of Eq. (3) exploited for the design of the MPC and the Kalman filter for the estimation of the  
562 disturbance has order  $n = 5$ , with a prediction horizon  $N_p = 10$  and a control horizon  $N_c = 2$ . The  
563 weighting factors have been settled to  $w_{y_k} = 0.1$  and  $w_{u_k} = 1$ , in order to reduce possible abrupt  
564 changes of the control input. Note that, in this case, the MPC technique has led to the best results,  
565 since it exploits a disturbance decoupling strategy, whilst its parameters have been iteratively adapted  
566 in the Simulink environment in order to optimise the MPC cost function of Eq. (37), as addressed in  
567 Section 3.1.4.

568 The second test case regards the hydroelectric plant simulator, where the hydraulic system with  
569 its turbine speed governor generates hydraulic transients due to the load changes. As already recalled  
570 in Section 2.2, an effective behaviour of a classic PID governor addressed *e.g.* in [30] applied to this  
571 hydroelectric plant would require the scheduling of its gains. In such a way only the performance  
572 of this standard controller could have been improved. In fact, in order to obtain the best dynamic  
573 performance of the hydraulic turbine, the PID governor of the turbine speed in Eq. (22) should  
574 consider different parameters for each working condition. Therefore, in order to consider operating  
575 situations similar to the wind turbine benchmark, the capabilities of the considered control techniques  
576 applied to the hydroelectric simulator have been evaluated during the start-up to full load maneuver.  
577 Moreover, an increasing load torque  $m_{g0}$  in Eq. (21) has been imposed during the start-up to full load  
578 phase, which is assumed to last 300s because of the large size of the considered Francis turbine, and  
579 for a simulation of 900s. This represents one of the different working conditions already addressed  
580 by the authors in [29] but for fault diagnosis applications. It is worth noting that these slow varying  
581 set-points have been considered for comparison purpose. In fact, as shown in [21], the wind turbine  
582 simulator presents similar dynamics, as highlighted in Figure 10.

583 Under these assumptions, Figure 11 summarises the results achieved with the application of  
584 the control strategies recalled in Section 3.1. In particular, for all cases, Figure 11 highlights that the  
585 hydraulic turbine angular velocity  $n$  increases with the load torque  $m_{g0}$  during the start-up to full  
586 working condition maneuver.

587 In more detail, Figure 11 (a) shows the performance of the PID regulator when its parameters  
588 are determined via the model-based autotuning procedure recalled in Section 3.1.1. In particular,  
589 its gains are determined with the algorithm implemented in the Simulink environment. It tries to



**Figure 11.** Hydroelectric system with (a) the autotuning PID regulator, (b) the fuzzy controller, (c) the adaptive regulator, and (d) the MPC approach with disturbance decoupling.

590 compute in an automatic way the optimal parameters of the PID regulator that minimise the step  
 591 response tracking error of the linear model approximating the nonlinear behaviour of the hydraulic  
 592 plant. Furthermore, Figure 11 (a) shows that the PID governor with autotuning is able to keep the  
 593 hydraulic turbine rotational speed error  $n - n_r$  null ( $r(t) = n_r$ , *i.e.* the rotational speed constant) in  
 594 steady-state conditions.

595 Figure 11 (b) reports the results concerning the TS fuzzy controller described by Eq. (28)  
 596 in Section 3.1.2. This fuzzy controller was implemented for a sampling interval  $T = 0.1s$ ,  
 597 with a number  $K = 2$  of Gaussian membership functions, and a number  $n = 3$  of delayed  
 598 inputs and output. The antecedent vector exploited by the relation of Eq. (27) is thus  $x =$   
 599  $[e_k, e_{k-1}, e_{k-2}, e_{k-3}, u_{k-1}, u_{k-2}, u_{k-3}]$ . Moreover, as recalled in Section 3.1.2, the data-driven FMID  
 600 and ANFIS tools implemented in the Simulink toolboxes are able to provide the estimates of the  
 601 shapes of the membership functions  $\mu_{A_i}$  used in Eq. (28).

602 On the other hand, Figure 11 (c) reports the simulations obtained via the data-driven adaptive  
 603 controller of Eq. (30), whose time-varying parameters are computed by means of the relations of  
 604 Eqs. (31). The damping factor and the natural frequency parameters used in Eq. (33) were selected  
 605 as  $\delta = \omega = 1$ . The STCSL tool described in Section 3.1.3 implements this data-driven adaptive  
 606 technique using the on-line identification of the input-output model of Eq. (29) [40].

607 Finally, regarding the MPC technique with disturbance decoupling proposed in Section 3.1.4,  
 608 Fig. 11 (d) reports the simulations obtained using a prediction horizon  $N_p = 10$  and a control horizon  
 609  $N_c = 2$ . Also in this case, the weighting parameters have been fixed to  $w_{y_k} = 0.1$  and  $w_{u_k} = 1$ , in  
 610 order to limit fast variations of the control input, as it will be remarked in the following. Furthermore,  
 611 the MPC design was performed using a linear state-space model for the nonlinear hydroelectric plant  
 612 simulator of Eq. (24) of order  $n = 6$ .

613 After these considerations, it is worth noting that some of the control techniques recalled in this  
 614 paper rely on self-tuning and adaptive methodologies, that are based on data-driven algorithms.  
 615 This means that they do not need for the knowledge of a high-fidelity description of the controlled  
 616 process, thus providing a viable and direct implementation. Some of these strategies were analysed  
 617 in [16] with application to general hydroelectric plant models, but implemented by using different



618 algorithms. Moreover, as an example, the work [44] presented a fuzzy controller that needs for the  
 619 proper design of the membership functions. On the other hand, the paper [17] proposed an advanced  
 620 controller combining four control schemes that rely on adaptive, fuzzy and neural network regulators.

621 In order to provide a quantitative comparison of the tracking capabilities obtained by the  
 622 considered control techniques for the wind turbine benchmark, the first row in Table 3 summarises  
 623 the achieved results in terms of  $NSSE\%$  index.

Table 3. Performance of the considered control solutions.

Simulated system	Working Condition	Standard PID	Autotuning PID	Fuzzy PID	Adaptive PID	MPC Scheme
Wind turbine	From partial to full load	11.5%	7.3%	5.7%	4.1%	2.8%
Hydro plant	From start-up to full load	6.2%	4.9%	3.1%	1.8%	0.9%

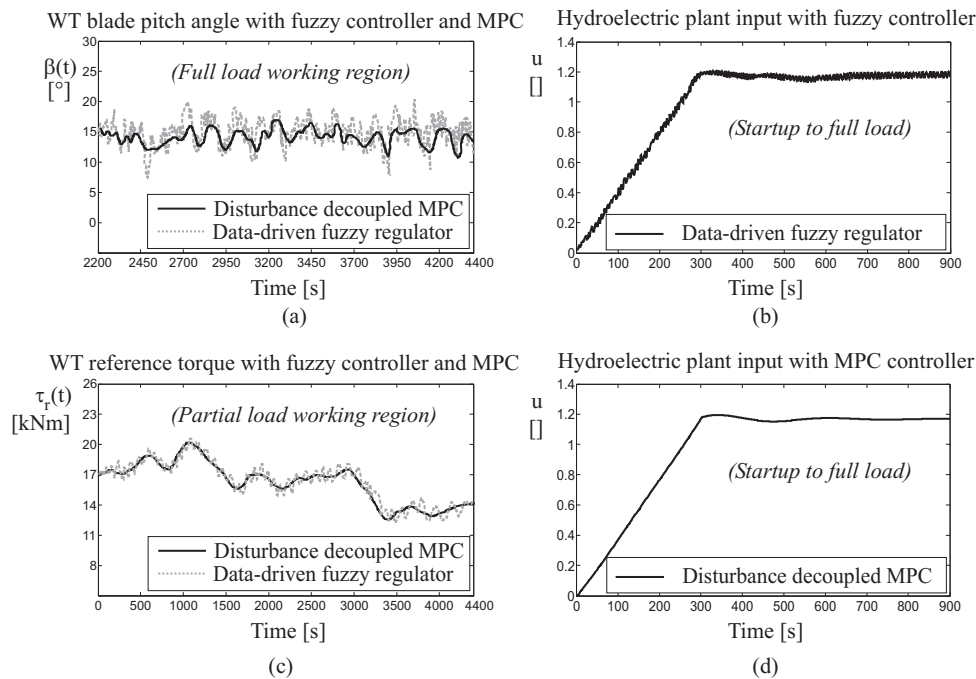
624 In particular, the  $NSSE\%$  values in the first row of Table 3 highlight better capabilities of the  
 625 proposed fuzzy controllers with respect to the PID regulators with autotuning. This is motivated  
 626 by the better flexibility and generalisation capabilities of the fuzzy tool, and in particular the FMID  
 627 toolbox proposed in [39]. A better behaviour is obtained by means of the adaptive solution, due to its  
 628 inherent adaptation mechanism, which allows to track the reference signal in the different working  
 629 conditions of the wind turbine process. However, the MPC technique with disturbance decoupling  
 630 has led to the best results, as reported in the first row of Table 3, since is able to optimise the overall  
 631 control law over the operating conditions of the system, by taking into account future operating  
 632 situations of its behaviour. while compensating the disturbance effects.

633 On the other hand, the results achieved by the validation of the considered control techniques  
 634 to the hydroelectric plant simulator are summarised in the second row of Table 3. In this case, the  
 635 values of the  $NSSE\%$  function are evaluated for the considered conditions of varying load torque  
 636  $m_{g0}$  corresponding to the plant start-up to full load maneuver. According to these simulation results,  
 637 good properties of the proposed model-based autotuning PID regulator are obtained, and they are  
 638 better than the baseline PID governor with fixed gains developed in [30]. In fact, the autotuning  
 639 model-based design implemented in the Simulink environment is able to limit the effect of high-gains  
 640 for the proportional and the integral contributions of the standard PID control law. On the other  
 641 hand, the data-driven fuzzy regulator has led to even better results, which are outperformed by  
 642 the adaptive solution. However, also for the case of the hydroelectric plant simulator, the best  
 643 performances are obtained by means of the MPC strategy with disturbance decoupling. Note that,  
 644 with reference to Table 3, the comparison should be performed by considering the  $NSSE\%$  values  
 645 for a given plant. In fact, even if the  $NSSE\%$  index assumes quite similar values, it refers to control  
 646 techniques implemented and applied to different processes.

647 With reference again to Table 3, some further comments can be drawn in general, concerning  
 648 the key aspects of the considered data-driven and model-based control solutions, with respect to the  
 649 standard PID regulators. The  $NSSE\%$  values obtained here are lower for both the wind turbine and  
 650 the hydroelectric systems. Standard industrial controllers, such the classic PID regulators recalled in  
 651 Section 2, are quite simple and have the benefit of quite straightforward tuning of their parameters.  
 652 Note that these standard regulators are considered here since they were implemented as baseline  
 653 controllers for the considered processes, see e.g. [10,30]. Obviously, when exploited for controlling  
 654 nonlinear dynamic processes, the control laws may lead to limited performances. Therefore, this  
 655 point motivates the use of suitable control solutions, as highlighted by the results summarised  
 656 in Table 3. In particular, when the modelling of the dynamic process can be perfectly achieved,  
 657 model-based control strategies generally represent the best option. However, when modelling

658 errors and uncertainty effects are important, data-driven control schemes relying on adaptation or  
 659 compensation mechanisms can show interesting features.

660 Finally, in order to highlight some further features of the considered, the controlled inputs  
 661 applied to the wind turbine system are depicted and compared in Figures 12 (a) and (c), whilst the one  
 662 feeding the hydroelectric plant in Figure 12 (b) and (d). For the sake of brevity, only the data-driven  
 663 fuzzy controller and the MPC with disturbance decoupling have been summarised here.



**Figure 12.** Wind turbine (a), (c) and hydroelectric plant (b), (d) compensated by the fuzzy controller and the MPC approach with disturbance decoupling.

664 By considering these control inputs, with reference to the data-driven methodologies, and in  
 665 particular to the design of the fuzzy controllers, off-line optimisation strategies allow to reach quite  
 666 good results. However, control inputs are subjected to faster variations. Other control techniques can  
 667 take advantage of more complicated and not direct design methodologies, as highlighted by the MPC  
 668 scheme. In this case, due to the input constraint, its changes are reduced. This feature is attractive  
 669 for wind turbine systems, where variations of the control inputs must be limited. This represents  
 670 another important benefit of MPC with disturbance decoupling, which integrates the advantages of  
 671 the classic MPC scheme with disturbance compensation effects. Therefore, with reference to these two  
 672 control methods, they can appear rather straightforward, even if further optimisation and estimation  
 673 strategies have to be applied.

#### 674 4.2. Sensitivity Analysis

675 This section analyses the reliability and robustness properties of the developed controllers when  
 676 parameter variations and measurement errors are considered. This further investigation relies on  
 677 the Monte-Carlo tool, since the control behaviour and the tracking capabilities depend on both the  
 678 model-reality mismatch effects and the input-output uncertainty levels. Therefore, this analysis has  
 679 been implemented by describing the parameters of both the wind turbine system and hydroelectric  
 680 plant models as Gaussian stochastic processes with average values corresponding to the nominal ones  
 681 summarised in Table 4 for the wind turbine benchmark.

682 Moreover, Table 4 shows that these model parameters have standard deviations of  $\pm 30\%$  of the  
 683 corresponding nominal values [24].

**Table 4.** Wind turbine benchmark parameters for the sensitivity analysis.

<b>Variable</b>	$R$	$\chi$	$\omega_n$	$B_{dt}$	$B_r$
<b>Nominal value</b>	57.5 m	0.6	11.11 rad s <sup>-1</sup>	775.49 N m s rad <sup>-1</sup>	7.11 N m s rad <sup>-1</sup>
<b>Variable</b>	$B_g$	$K_{dt}$	$\eta_{dt}$	$J_g$	$J_r$
<b>Nominal value</b>	45.6 N m s rad <sup>-1</sup>	$2.7 \cdot 10^9$ N m rad <sup>-1</sup>	0.97	390 kg m <sup>2</sup>	$55 \cdot 10^6$ kg m <sup>2</sup>

684 On the other hand, Table 5 reports the hydroelectric simulator model variables with their  
 685 nominal values varied by  $\pm 30\%$  in order to develop the same Monte–Carlo analysis [11].

**Table 5.** Hydroelectric simulator parameters for the sensitivity analysis.

<b>Variable</b>	$a$	$b$	$c$	$H_{f_1}$	$H_{f_3}$	$H_{f_5}$	$T_a$
<b>Nominal value</b>	-0.08	0.14	0.94	0.0481 m	0.0481 m	0.0047 m	5.9 s
<b>Variable</b>	$T_c$	$T_{s_2}$	$T_{s_4}$	$T_{w_1}$	$T_{w_3}$	$T_{w_5}$	
<b>Nominal value</b>	20 s	476.05 s	5000 s	3.22 s	0.83 s	0.1 s	

686 Therefore, the average values of  $NSSE\%$  index have been thus evaluated by means of 1000  
 687 Monte–Carlo simulations. They have been reported in Tables 6 and 7 for the wind turbine benchmark  
 688 and the hydroelectric plant simulator, respectively.

**Table 6.** Sensitivity analysis applied to the wind turbine benchmark.

<b>Standard PID</b>	<b>Autotuning PID</b>	<b>Fuzzy PID</b>	<b>Adaptive PID</b>	<b>MPC Scheme</b>
13.8%	9.2%	7.6%	5.3%	3.9%

**Table 7.** Sensitivity analysis applied to the hydroelectric plant simulator.

<b>Standard PID</b>	<b>Autotuning PID</b>	<b>Fuzzy PID</b>	<b>Adaptive PID</b>	<b>MPC Scheme</b>
9.1%	7.4%	5.6%	3.5%	2.2%

689 It is worth noting that the results summarised in Tables 6 and 7 serve to verify and validate  
 690 the overall behaviour of the developed control techniques, when applied to the considered wind  
 691 turbine benchmark and hydroelectric plant simulator, respectively. In more detail, the values of the  
 692  $NSSE\%$  index highlights that when the mathematical description of the controlled dynamic processes  
 693 can be included in the control design phase, the model–based MPC technique with disturbance  
 694 decoupling still yields to the best performances, even if an optimisation procedure is required.  
 695 However, when modelling errors are present, the off–line learning exploited by the data–driven  
 696 fuzzy regulators allows to achieve results better than model–based schemes. For example, this  
 697 consideration is valid for the PID controllers derived via the model–based autotuning procedures.  
 698 On the other hand, fuzzy controllers have led to interesting tracking capabilities. With reference to  
 699 the data–driven adaptive scheme, it takes advantage of its recursive features, since it is able to track  
 700 possible variations of the controlled systems, due to operation or model changes. However, it requires  
 701 quite complicated and not straightforward design procedures relying on data–driven recursive  
 702 algorithms. Therefore, fuzzy–based schemes use the learning accumulated from data–driven off–line

703 simulations, but the training stage can be computationally heavy. Finally, concerning the standard  
704 PID control model-based strategy, it is rather simple and straightforward. Obviously, the achievable  
705 performances are quite limited when applied to nonlinear dynamic processes. Note that they were  
706 proposed as baseline control solutions for the considered processes. It can be thus concluded that  
707 the proposed data-driven and model-based approaches seem to represent powerful techniques able  
708 to cope with uncertainty, disturbance and variable working conditions. Note finally that the plant  
709 simulators, the control solutions, and the data exploited for the analysis addressed in this paper are  
710 directly and freely available from the authors.

## 711 5. Conclusions

712 The work considered two renewable energy conversion systems, such as a wind turbine  
713 benchmark and a hydroelectric plant simulator. The most important modelling aspects and the  
714 baseline control strategies were also summarised. In particular, the three-bladed horizontal axis wind  
715 turbine benchmark reported in this work consisted of simple models of the gear-box, the drive-train,  
716 and the electric generator/converter. On the other hand, the hydroelectric plant simulator included  
717 a high water head, a long penstock with upstream and downstream surge tanks, and a Francis  
718 hydraulic turbine. Standard PID governors were earlier developed for these processes, which were  
719 rather simple and straightforward, but with limited achievable performances. Therefore, the paper  
720 proposed different control techniques relying on model-based and data-driven approaches. Their  
721 performances were analysed first. Then, the reliability and robustness of these solutions were also  
722 verified and validated with respect to parameter variations of the plant models and measurement  
723 errors, via the Monte-Carlo tool. The achieved results highlighted that data-driven approaches, such  
724 as the fuzzy regulators were able to provide good tracking performances. However, they were easily  
725 outperformed by adaptive and model predictive control schemes, representing data-driven and  
726 model-based approaches that require optimisation stages, adaptation procedures and disturbance  
727 compensation methods. Future investigations will consider the verification and the validation of  
728 the considered control techniques when applied to higher fidelity simulators of energy conversion  
729 systems.

730 **Sample Availability:** The software codes for the proposed control strategies, the simulated benchmarks and the  
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