

Article

# Diamagnetism of bulk graphite revised

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**Abstract:** Recently published structural analysis and galvanomagnetic studies of a large number of different bulk and mesoscopic graphite samples of high quality and purity reveal that the common picture assuming graphite samples as a semimetal with a homogeneous carrier density of conduction electrons is misleading. These new studies indicate that the main electrical conduction path occurs within 2D interfaces embedded in semiconducting Bernal and/or rhombohedral stacking regions. This new knowledge incites us to revise experimentally and theoretically the diamagnetism of graphite samples. We found that the  $c$ -axis susceptibility of highly pure oriented graphite samples is not really constant but can vary several tens of percent for bulk samples with thickness  $t \gtrsim 30 \mu\text{m}$ , whereas by a much larger factor for samples with smaller thickness. The observed decrease of the susceptibility with sample thickness resembles qualitatively the one reported for the electrical conductivity and indicates that the main part of the  $c$ -axis diamagnetic signal is not intrinsic of the ideal graphite structure but it is due to the highly conducting 2D interfaces. The interpretation of the main diamagnetic signal of graphite agrees with the reported description of its galvanomagnetic properties and provides a hint to understand some magnetic peculiarities of thin graphite samples.

**Keywords:** graphite; diamagnetism; thickness dependence; susceptibility; interfaces; conductivity; graphene

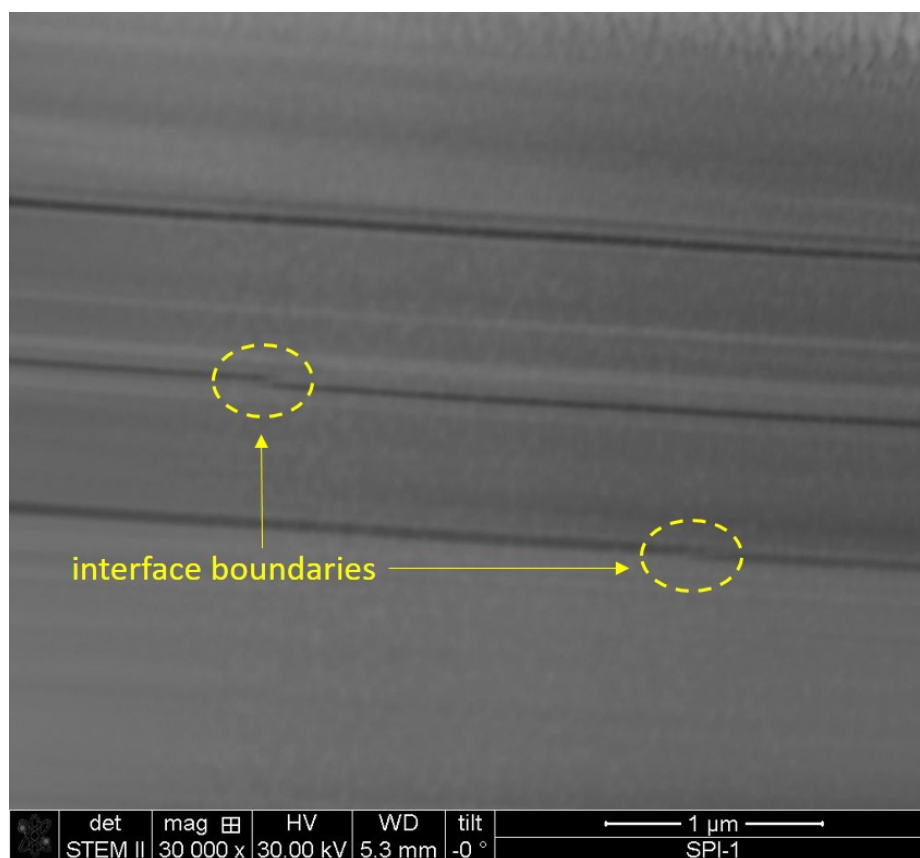
## 1. Introduction

The  $c$ -axis diamagnetic susceptibility of graphite is very large and anisotropic [1–3]. According to the literature of the last 50 years there is consent to interpret this large diamagnetism as due to the Landau diamagnetic contribution of a certain density of free conduction electrons within the graphene planes of graphite. The relatively low density of conduction electrons in graphite arises from the overlap of the  $2p_z$  electronic orbitals, normal to the graphene planes. Whereas the overlap between those orbitals from the carbon atoms at neighbouring graphene layers, in both Bernal and rhombohedral stacking orders, remains very weak, i.e. Van der Waals coupling, as the huge anisotropy of the resistivity and magnetization indicates.

The calculations of the conduction-electrons magnetic susceptibility have been done in the past taking into account an electronic band structure inferred from electric transport and magnetic measurements [4–6]. In particular using the quantum oscillations in the electrical resistance, Hall effect and magnetization, the Shubnikov-de Haas (SdH) and de Haas-van Alphen effects. All theoretical models as well as the interpretation of the measured diamagnetism of graphite in those publications assumed that high quality and pure graphite samples are homogeneous, structurally as well as electronically. All free parameters of the band structure models were obtained from a comparison with experimental data of different graphite samples [7]. Nowadays one may doubt about the accuracy of the used models in particular because no electron-electron or spin-orbit coupling interactions were

35 included explicitly, plus the difficulties those calculations have to model the Van der Waals interaction  
36 between the graphene layers.

37 The main problem those models and interpretation have, however, is directly related to the  
38 misleading assumption that the experimental magnetic and electrical data correspond to homogeneous  
39 bulk graphite samples. First experimental hints at odd with this assumption were obtained from the  
40 magnetic field dependence of the Hall coefficient of kish graphite samples of different thickness [8,9].  
41 Namely, the amplitude of the SdH oscillations decreases the smaller the thickness of the samples.  
42 For example, for a sample with thickness of 18 nm (which corresponds to a stacking of more than  
43 50 graphene layers) one can barely recognize the field oscillations in the Hall coefficient, in clear  
44 contrast to thicker flakes; for a review and discussion on these and other experimental results on  
45 this issue see [10]. Moreover, a nonlinear increase of the resistance of graphite samples the smaller  
46 their thickness was reported [11], which can be described as an anomalous increase in the estimated  
47 absolute resistivity [12] the thinner the sample. Surprisingly, none of those studies [8,9,11] tried to  
48 correlate the obtained results with the internal structure of the samples.



**Figure 1.** STEM picture of a commercial HOPG (SPI) graphite lamella ( $\sim 400$  nm thick) cut from a bulk sample measured also in this work. The electron beam is applied parallel to the graphene layers and normal to the main  $c$ -axis of the graphite structure. The different grey colours indicate crystalline regions with different stacking order (Bernal or rhombohedral) or regions twisted around the  $c$ -axis by a certain angle respect to the neighbouring regions. Well defined two-dimensional interfaces are located between regions with different grey colors at the middle of the picture, which includes also interface boundaries (yellow ellipsoids). More STEM pictures (also with much higher resolution) obtained from different commercial HOPG samples and natural graphite can be seen in [10].

49 Experimental evidence obtained in graphite bulk samples and thin flakes the last 10 years reveals  
50 that the observed thickness dependence of the magneto-electric properties of graphite has its origin  
51 in the internal microstructure of the samples [10,12–14]. In particular scanning transmission electron

52 microscopy (STEM) studies, as example see Figure 1, reveal the existence of two-dimensional (2D)  
53 interfaces between regions with different stacking order and/or between regions with similar stacking  
54 order but twisted around a common  $c$ -axis [10]. The presence of two stacking orders, identified as the  
55 majority phase called Bernal (ABABA...) and the rhombohedral (ABCABCA...) stacking order, has  
56 been measured by high resolution x-rays diffraction (XRD) [15] of different samples including natural  
57 graphite crystals, highly oriented pyrolytic graphite (HOPG) or kish graphite [10,16], in agreement  
58 with previous reports [7,17]. It is important to note that these two stacking orders are not semimetals,  
59 but semiconductors with energy gaps of  $38 \pm 8$  meV (Bernal) and  $110 \pm 20$  meV (rhombohedral),  
60 obtained from the fits to the temperature dependence of the resistance between 2 K to 1100 K of a large  
61 number of different samples of different origins [13].

62 The galvanomagnetic results obtained for samples of different thickness indicate that a highly  
63 conducting path in graphite samples is localized at the 2D interfaces [12–14,18], which upon twist  
64 angle [10] or stacking order [19,20] they can even show superconducting properties [15,21–23]. The  
65 origin of the SdH oscillations in the electrical resistance is related to the 2D interfaces, as recent detailed  
66 electrical measurements clearly revealed [14]. All these recent results motivated us to study more  
67 carefully the magnetization of graphite samples with smaller thickness than the usually reported  
68 samples in the literature. Since the two stacking order phases are semiconducting, it is clear that  
69 the diamagnetic signal of graphite cannot be intrinsic of the graphite structure, otherwise we would  
70 have large changes of the  $c$ -axis susceptibility with temperature, which is not the case [7]. If the  
71 large diamagnetic moment measured in large bulk samples of graphite is mainly due to the highly  
72 conducting interfaces, taking into account STEM studies (see section 2) we expect then to observe a  
73 non systematic variation of the diamagnetic response in bulk samples, even if the samples have similar  
74 volumen and cut from the same sample. Also we would expect to see a decrease in the absolute value  
75 of the diamagnetic susceptibility the smaller the interface number, i.e. the smaller the sample thickness.

76 In clear contrast to the technical requirements needed to study the electrical resistance of graphite  
77 samples with thickness down to a single graphene layer, the measurement of the diamagnetic moment  
78 of thin graphite samples with a commercial SQUID magnetometer is difficult or even impracticable.  
79 For example, assuming one wants to measure the diamagnetic  $c$ -axis magnetic moment of a graphite  
80 flake of thickness  $\times$  width  $\times$  length equal to  $1 \mu\text{m} \times 0.2 \text{ mm} \times 0.2 \text{ mm}$  with an expected diamagnetic  
81  $c$ -axis susceptibility  $\chi \sim -2 \times 10^{-5}$  emu/g Oe, the expected diamagnetic moment at a field of  $10^4$  Oe  
82 applied parallel to the  $c$ -axis would be  $m \lesssim -2 \times 10^{-8}$  emu, a value of the order of the error of  
83 commercial SQUIDs nowadays. The expected small magnetic moment added to a not-easy handling  
84 of such small thin flakes for that kind of measurements (without large backgrounds from substrates,  
85 etc.) put already hard restrictions to perform such magnetization measurements.

86 In this work and besides the SQUID we have used a torque magnetometer that allowed us to  
87 measure with high resolution the susceptibility of well ordered graphite flakes with thickness to  
88  $\sim 1 \mu\text{m}$  and larger. The obtained results of the magnetic moment of highly oriented samples of  
89 different sources and with both magnetometers show that the absolute value of the diamagnetic  
90 susceptibility decreases the smaller the sample thickness. Our results can be considered as a first  
91 experimental hint that agrees qualitatively with the thickness dependence of the conductivity of similar  
92 samples. Our results suggest that the largest contribution to the diamagnetic susceptibility measured  
93 in bulk samples is not intrinsic of the ideal graphite structure.

94 The manuscript is organized as follows: In the next section we discuss the density of interfaces  
95 following the information of a STEM picture obtained from one of the measured samples. Section 3 is  
96 divided in three more sections where we discuss: (A) The temperature dependence of the diamagnetism  
97 of graphite samples, (B) the angle dependence of the torque magnetometer, and (C) the thickness  
98 dependence of the diamagnetic susceptibility. In section 4 we discuss the results and propose a  
99 simple model to understand at least semiquantitatively the thickness dependence of the diamagnetic  
100 susceptibility of graphite samples. Section 5 describes the characteristics of the selected samples and

101 details of the used magnetometers. The conclusion is given in section 6. Further supplementary  
102 information can be seen at <http://www.mdpi.com/2312-7481/xx/1/5/xx>.

## 103 2. Internal structure of graphite samples

104 The 2D interfaces appear between crystalline regions with different stacking orders or twisted by a  
105 certain angle around the common  $c$ -axis. Whereas ideal Bernal and rhombohedral stacking orders are  
106 low-energy gap semiconductors [18,24–26], twisted crystalline graphite regions reveal angle-dependent  
107 moire patterns at their interface with a much higher and position-dependent electronic density of states,  
108 as scanning tunneling microscopy revealed [10,27–30]. The 2D interfaces are located at the boundaries  
109 of the regions with different grey colours in Fig. 1. This STEM picture tells us that: (a) The density of  
110 interfaces is not homogeneous within the observed region of  $\sim 3 \mu\text{m}$  parallel to the  $c$ -axis. (b) We can  
111 recognize clearly only some of the interfaces because of the relatively large thickness of  $\sim 350 \text{ nm}$  of  
112 the lamella. Note that some of the 2D interfaces from in-depth regions of the lamella do not appear  
113 with clear boundaries in the STEM picture. (c) The length of the interfaces is in general much less than  
114 the length of the graphene planes due to grain boundaries. Two regions with cut and shifted interfaces  
115 are indicated by the yellow ellipsoids in Fig. 1. This means that only due to the internal microstructure  
116 of the graphite samples the effective weight to the total diamagnetic response of each single interface  
117 we recognize in the rather small part of a sample through the STEM picture, is in general less than one.  
118 In other words we expect that for mesoscopic and macroscopic graphite samples the ratio between the  
119 effective number of interfaces  $N_{int}$ , contributing similarly in shielding the applied field within a region  
120 of  $N$  graphene layers, can have non-integer values. Therefore, the ratio  $N_{int}/N$  can be considered  
121 as an effective parameter in the model we present in section 4. (d) Which of the observed interfaces  
122 provides the highest diamagnetic response, i.e. magnetic field shielding, remains still unknown. It  
123 may be that most of the interfaces between twisted regions react similarly under a magnetic field due  
124 to the existence of similar high density of states at the hexagonal paths observed in the moire patterns  
125 with different diameters (see [10] and refs. therein).

126 We may conclude that neither the area nor the density or the electronic characteristics of  
127 the interfaces are homogeneously distributed within each bulk sample, making cumbersome the  
128 interpretation of different properties that depend on the response of these interfaces. For example, if  
129 we would measured the diamagnetic response of the lamella of Fig. 1 as it is, and after removing the  
130 interface-free region at the bottom, we will calculate for the lamella with less mass (but with the same  
131 amount of interfaces) an enhanced diamagnetic susceptibility respect to the original sample before. In  
132 other words, a normalization of the measured magnetic moment by the total sample mass is, strictly  
133 speaking, incorrect.

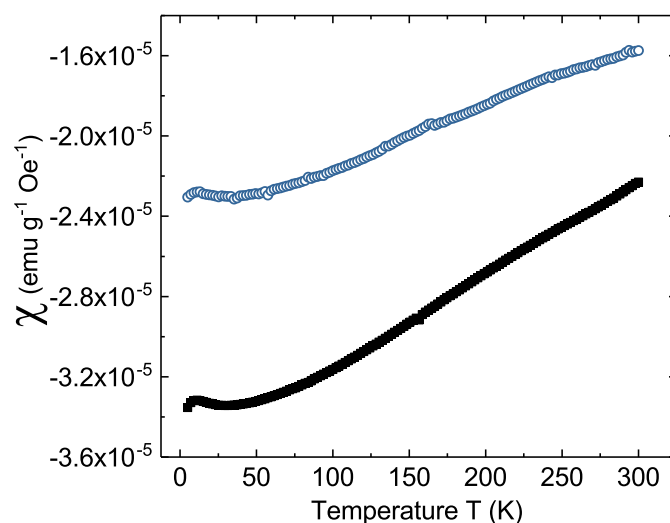
134 We note that in general the diamagnetic  $c$ -axis magnetization of different graphite samples  
135 is not straightforward to understand, even qualitatively. For example, early reports showed a  
136 non-monotonous behavior on the degree of graphitization and its absolute value is  $\sim 30\%$  smaller  
137 for the highest oriented than for less oriented samples [31]. We believe that at least part of this behavior is  
138 related to internal interfaces.

139 In order to fix ideas and provide a semiquantitative estimate of the  $c$ -axis susceptibility due  
140 to the internal interfaces, from Fig. 1 and other STEM studies we estimate between  $\sim 16$  and  $\sim 20$   
141 interfaces in  $\sim 3 \mu\text{m}$  parallel to the  $c$ -axis. Taking into account the distance between graphene planes  
142 in graphite, the interface density would be of the order of  $N_{int}/N \sim (1.6 \dots 2) \times 10^{-3}$ . If the main  
143 contribution to the total diamagnetic susceptibility of graphite would be directly proportional to this  
144 ratio, as our estimates suggest (see section 4), one expects a decrease of this effective ratio the thinner  
145 the sample, below a certain thickness that depends on the internal structure of the graphite sample.

## 146 3. Results

147 (A) *Temperature dependence of the diamagnetism of graphite:* The temperature dependence of the  
148 susceptibility of HOPG samples was obtained using samples of thickness  $201 \mu\text{m}$  and  $27 \mu\text{m}$ . A

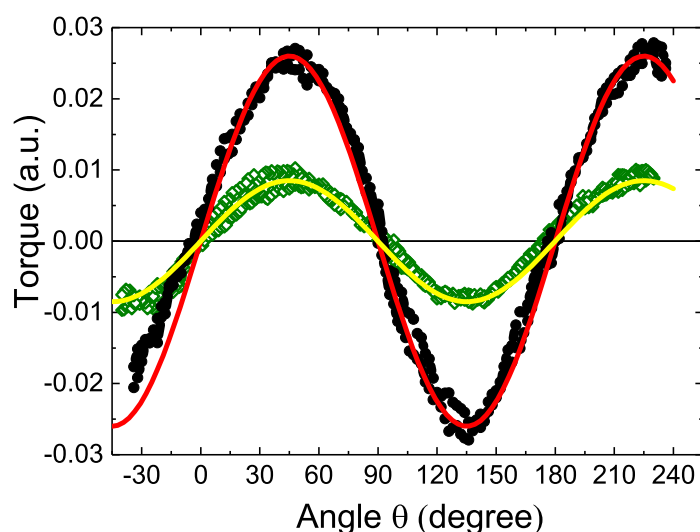
149 magnetic field of 10 kOe parallel to the  $c$ -axis was applied at 300 K and the samples were cooled to  
 150 5 K in the sweep mode with 2K/min rate. The results are shown in Figure 2.



**Figure 2.** Temperature dependence of the mass susceptibility of two HOPG samples from the same source with thicknesses of 201  $\mu\text{m}$  (bottom curve) and 27  $\mu\text{m}$  (upper curve) measured with a SQUID magnetometer.

151 As already reported in the literature, the change of the diamagnetic  $c$ -axis susceptibility with  
 152 temperature is rather weak, having a maximal diamagnetic response at  $\sim 50$  K with a slight increase at  
 153 lower temperatures, as Figure 2 shows. The presented result of the bulk sample is similar to published  
 154 results (see, e.g., Fig. 6 in [32]). The results shown in Figure 2 indicate that the absolute value of the  
 155 magnetic susceptibility of the thinner sample is  $\simeq 25\%$  smaller than samples with thickness of 30.6  
 156  $\mu\text{m}$  or 201  $\mu\text{m}$  at 300 K. Having the samples similar areas and prepared from the same bulk sample,  
 157 this difference is not due to an error in the measurement or because the quality of the sample has  
 158 been changed through handling. These variations of the susceptibility for similar samples of different  
 159 thickness (see also Fig. 4) already suggest a non-intrinsic origin of the main diamagnetic signal.

160 (B) *Angle dependence of the torque:* The torque magnetometer can be used to obtain the magnetic  
 161 moment for one field direction if the sample is strong magnetically anisotropic, i.e.  $\chi_{\parallel} \gg \chi_{\perp}$ , where the  
 162 two susceptibilities mean for fields parallel and perpendicular to the  $c$ -axis. According to published  
 163 results the ratio between the two susceptibilities is  $\chi_{\parallel}/\chi_{\perp} \gtrsim 10$  [1,2,31,33]. This means that the torque  
 164 signal is basically given by the magnetic moment component parallel to the  $c$ -axis.

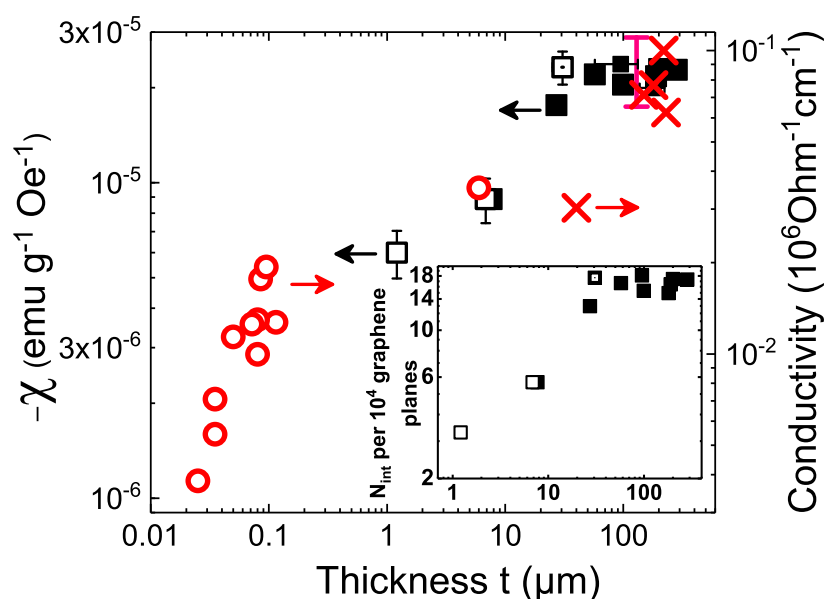


**Figure 3.** Torque signal of two natural graphite flakes vs. angle  $\theta$  between the applied field  $H = 2$  kOe and the  $c$ -axis of the graphite structure. The thickness of the samples was  $1.2 \mu\text{m}$  ( $\diamond$ ) and  $6.9 \mu\text{m}$  ( $\bullet$ ). The lines are fits to a  $\sin(2\theta)$  function. The magnetic moment of the thinnest sample is of the order of  $\sim -2 \times 10^{-9}$  emu.

165 Figure 3 shows as an example the angular dependence of the measured torque signal under a  
 166 constant magnetic field of 2 kOe at room temperature performed on two different pieces of a natural  
 167 graphite sample of thickness  $1.2 \mu\text{m}$  and  $6.9 \mu\text{m}$ . The measurements were done in the two field sweep  
 168 directions and, as can be seen in the figure, a good reproducibility was achieved with negligible  
 169 hysteresis. The magnetic moment obtained from the torque signal depends on the angle  $\theta$  between the  
 170 applied magnetic field  $H$  and the  $c$ -axis of the samples, as shown in Figure 3.

171 (C) Thickness dependence of the diamagnetic susceptibility:

172 Figure 4 shows the results of the  $c$ -axis susceptibility of all graphite samples we have measured  
 173 at 300 K as a function of their thickness and with the two experimental methods. In the same figure we  
 174 included the thickness dependence of the conductivity of graphite obtained at the same temperature  
 175 (right  $y$ -axis) taken from [13,34]. Our data basically agree with the published susceptibility data of  
 176 highly ordered samples of thickness of the order or larger than  $100 \mu\text{m}$ . However, note the variations  
 177 of  $\pm \sim 25\%$  (vertical bar in the upper right in the figure) even for similar samples. We observe that  
 178 when the thickness of the samples is less than  $\sim 50 \mu\text{m}$ , dimensional effects begin to appear on the  
 179 electrical as well as in the magnetic susceptibility of graphite. For  $t < 50 \mu\text{m}$  the experimental trend  
 180 suggests a change of a factor of ten in the susceptibility within a change of  $\sim 3$  orders of magnitude  
 181 in thickness. This means roughly a change of  $\sim 30\%$  in one decade of thickness. Note that all measured  
 182 susceptibility points have a constant, practically thickness independent background contribution  
 183 coming from the rest of the graphene (mainly Bernal stacking) layers, see section 4. In Appendix A  
 184 of the supplementary information we show also the behaviour of the resistivity at 4 K as a function  
 185 of the sample thickness. In Appendix B we demonstrate that the observed decrease of the measured  
 186 susceptibility with thickness is not related to a decrease of the total or lateral sample area.



**Figure 4.** *c*-axis susceptibility of different graphite samples vs. their thickness at 300K measured by a torquemeter (□) and a SQUID magnetometer (■). The samples were obtained from pre-characterized bulk natural graphite [15] as well as HOPG samples of grade ZYA [13,15,35]. The HOPG sample with a thickness 30.6  $\mu\text{m}$  was measured with the SQUID as well as with torque magnetometer (□, see Appendix D in the supplementary information for details of the calibration of the torque magnetometers). The vertical error bar at the top right indicates the values at 300K reported of different oriented samples in the literature [32,36–41]. Right *y*-axis: thickness dependence of the conductivity of several bulk and thin graphite samples at 300K from (○) [13] and (×) [34], calculated using the given geometry in those publications. The inset shows the estimated effective number of interfaces (per  $10^4$  graphene layers) that contribute to the diamagnetic signal as a function of the sample thickness, obtained using Equation (1).

187 The observed behavior strongly suggests that the observed internal microstructure of the graphite  
 188 samples plays a mayor role in those properties. The transport [10,13,14] and structural studies [15]  
 189 indicate that graphite samples have to be considered, electronically speaking, not as homogeneous but  
 190 as a heterostructure. In other words, each sample with thickness  $\gtrsim 20$  nm may start showing three  
 191 contributions to the conductivity as well as to the susceptibility: two semiconducting-like phases with  
 192 Bernal and rhombohedral stacking orders and some of the interfaces between the semiconducting  
 193 phases or twisted by a certain angle within the same stacking order [10], with metallic and/or  
 194 superconducting character [10,13,14,22,23,42]. These three contributions conduct in parallel when the  
 195 current is applied parallel to the graphite layers. Decreasing therefore the thickness of the sample below  
 196 a certain thickness, the diamagnetic contribution to the magnetization, given in first approximation by  
 197 the simple addition of the three magnetic contributions in series, would decrease because the largest  
 198 contribution proportional to the diamagnetic response of the interfaces would also decrease.

#### 199 4. Discussion

200 The decrease of the absolute value of the susceptibility decreasing the thickness of the ordered  
 201 graphite samples does not appear to be related to extra defects one may introduce through handling or  
 202 sample preparation (see also Appendix B and C in the supplementary information). Neither the error  
 203 in the misalignment between the *c*-axis and the applied field direction nor the error in the sample  
 204 dimensions or mass can provide changes of  $\pm 25\%$  observed in thicker samples or a factor of five in the  
 205 susceptibility of thinner samples, see Figure 4. It should be clear that due to the heterostructure of most  
 206 of the graphite samples, i.e. the existence of highly conducting (or superconducting) interfaces and the

207 semiconducting character of the two stacking orders, the magnetic properties of graphite cannot be  
 208 explained with the models proposed in the literature [4–6] and new approaches are needed.

209 To understand at least semiquantitatively the observed behavior we take a simple approach,  
 210 which main aim is to estimate the order of magnitude of the total measured magnetic moment of the  
 211 sample  $m$  assuming that it is due to the direct sum of the independent moments from the 2D interfaces  
 212  $m_{\text{int}}$ , the Bernal ( $m_{\text{B}}$ ) and the rhombohedral ( $m_{\text{RH}}$ ) stacking orders as:  $m = m_{\text{int}} + m_{\text{B}} + m_{\text{RH}}$ . The  
 213 estimates done below provide the order of magnitude and an explanation for the thickness dependence  
 214 of the total susceptibility.

215 We note that there are neither high-resolution band structure measurements nor calculations  
 216 especially for the Bernal stacking orders that provide the obtained small energy gap. This is necessary  
 217 to get the dispersion relation, the Fermi velocity and the effective carrier mass at low enough energy,  
 218 which eventually can be used to estimate the susceptibility of each of the stacking orders. Therefore,  
 219 we shall assume that each of those contributions is given by the 2D susceptibility of the graphene  
 220 layers in each stacking order, similarly for the 2D highly conducting interfaces, multiplied by their  
 221 corresponding densities. The measured  $c$ -axis susceptibility  $\chi$ , with the magnetic field  $H$  applied  
 222 normal to the graphene and interface planes, is estimated as:

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$$\chi = a \left( \chi_{\text{int}} \frac{N_{\text{int}}}{N} + \chi_{\text{B}} \frac{N_{\text{B}}}{N} + \chi_{\text{RH}} \frac{N_{\text{RH}}}{N} \right), \quad (1)$$

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225 where the parameters  $N_i$  ( $i = \text{int}, \text{B}, \text{RH}$ ) refer to the effective number of interfaces, and the number of  
 226 graphene layers that belong to the Bernal and rhombohedral phases in a given sample;  $N$  is the total  
 227 number of layers in a given sample of thickness  $t$ . The prefactor  $a$  in Equation (1) is a normalization  
 228 factor inversely proportional to the 2D mass density. It can be roughly calculated or obtained directly  
 229 from a comparison with the measured  $\chi$  at large enough thickness.

To estimate the  $c$ -axis magnetic susceptibility of the two semiconducting phases with energy  
 gaps  $\sim 38$  meV and  $\sim 110$  meV we take the formula for the orbital diamagnetic susceptibility of a  
 graphene layer with a band gap  $\Delta$  given by (in cgs units) [43]:

$$\chi_{\Delta} = -g_v g_s \frac{e^2 v_F^2}{6\pi c^2} \frac{1}{2\Delta}, \quad (2)$$

where  $g_s = 2$  and  $g_v = 2$  represent the degrees of freedom associated with spin and valley, respectively,  
 and  $c$  the light velocity. We estimate the electron velocity  $v_F$  for a 2D electron system as:

$$v_F = \frac{\hbar \sqrt{2\pi n}}{m^*}, \quad (3)$$

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231 where  $m^*$  is the effective mass of electrons. From experiments one can obtain a carrier concentration at  
 232 room temperature  $n \sim 10^{10} \text{ cm}^{-2}$  [10,18,22]. With this we estimate a carrier velocity  $v_F \sim 3 \times 10^5 \text{ cm/s}$   
 233 assuming that for these semiconducting phases the effective mass is equal to the free electron mass  
 234 with a quadratic dispersion relation. Future measurements should clarify the value of the effective  
 235 mass at least for the majority Bernal phase (without interfaces). The 2D diamagnetic susceptibilities are  
 236  $\chi_{\text{B}} \sim -4 \times 10^{-17} \text{ emu/cm}^2 \text{Oe}$  and  $\chi_{\text{RH}} \sim -10^{-17} \text{ emu/cm}^2 \text{Oe}$ , where we used the same  $n$  for both  
 237 stacking orders. We expect that  $\chi_{\text{RH}}$  should be even smaller than the estimate above.

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239 The 2D diamagnetic susceptibility of the internal interfaces is obtained from the expression  
 240 for the Landau diamagnetism of a 2D gas of free electrons, taking from experiments the effective  
 241 mass  $m^* \sim 0.05 m_e$  [44,45] ( $m_e$  is the free electron mass). Note that the SdH oscillations in the  
 242 magnetoresistance are related to the carriers at the interfaces and not to the semiconducting layers.  
 This is the reason why the SdH oscillations amplitude vanishes the smaller the sample thickness



243 [8–10]. This is obvious because the thinnest, semiconducting samples without interfaces should have a  
 244 negligible amount of conduction electrons at low enough temperatures [10,14].

The Landau diamagnetic susceptibility of the interfaces is therefore:

$$\chi_{\text{int}} = -\frac{e^2}{12\pi m^* c^2} \sim -2 \times 10^{-13} \text{ emu/cm}^2 \text{Oe}. \quad (4)$$

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From STEM studies we know that the ratio of the number of interfaces and of the graphene planes with one or other stacking orders depend on sample and on the position on the same sample, see e.g. [10,15]. Furthermore, although each interface is parallel to the graphene layers, they do not cover all the mesoscopic sample area; they are limited at least within the single crystalline regions with a length and width within a range of  $\sim 1 \dots 20 \mu\text{m}$ , as electron backscattering diffraction pictures indicate [46,47]. This means that a single interface covers in general an area much smaller than the one of the graphene planes. As the thickness of the sample decreases, the probability of having similar diamagnetic response due to the effective distribution of 2D interfaces also decreases. In other words, the relative weight of each single interface is in general less than 1 compare to the graphene layers that cover the whole sample area.

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To estimate the total susceptibility vs. thickness, with the knowledge of the typical thickness of the Bernal and rhombohedral crystalline regions and the number of embedded interfaces obtained from the STEM images, one can roughly estimate an effective ratio of the number of interfaces in a given sample to the number of graphene layers  $\frac{N_{\text{int}}}{N}$ . For example and to fix ideas, the following trends are rather general  $\frac{N_{\text{int}}}{N}(t \lesssim 50 \text{ nm}) \rightarrow 0$  and  $\frac{N_{\text{int}}}{N}(t > 50 \mu\text{m}) \sim 1.6 \times 10^{-3}$ . The range of the ratio of graphene planes of the Bernal phase is  $\frac{N_{\text{B}}}{N} \sim 0.8 \dots 1$  and of the rhombohedral  $\frac{N_{\text{RH}}}{N} \sim 0.2 \dots 0$ .

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This estimate indicates that in real ordered graphite samples with thickness  $t \gtrsim 30 \mu\text{m}$  and for a typical ratio of the number of interfaces, the total susceptibility is given mainly by the conducting interfaces. Moreover and in first approximation the rhombohedral contribution to the total susceptibility can be neglected. With the estimates given above, using the measured value of the susceptibility  $\chi(t > 50 \mu\text{m}) \sim -2 \times 10^{-5} \text{ emu/gOe}$  we obtain  $a \sim 6 \times 10^{10} \text{ cm}^2/\text{g}$ . From the experimental data and using Equation (1) we estimate the ratio  $N_{\text{int}}/N$  vs. the sample thickness, shown as inset in Figure 4.

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Future experiments should try to measure the susceptibility of graphite samples with smaller thickness down to  $\sim 10 \text{ nm}$  and area  $\lesssim 1 \mu\text{m}^2$ , because the probability to have the contribution of interfaces is evidently smaller. If these measurements are achieved successfully one can obtain the susceptibility of the Bernal phase and compare with the theoretical model. This susceptibility represents a rather constant background of the experimental points shown in Fig. 4. However, the technical difficulties to measure such small samples with the systems available nowadays are difficult to overwhelm.

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Finally, we would like to pay attention to an actually common observation in the laboratories, when one tries to leave a thin graphite flake completely or partially levitating under an inhomogeneous magnetic field from a permanent magnet. We observed that not all thin flakes react similarly to the same field distribution, even when they have similar mass and shape. Even several of them do not react at all to the magnetic field, independently of how small their mass is. This simple observation already indicates that our simple assumption of a homogeneous diamagnetic response of graphite samples cannot be correct. Within our interpretation these observations can simply indicate that the selected thin samples have different amount of conducting interfaces.

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Furthermore, an interesting observation was included a year ago in the YouTube internet channel. Namely: large, thin and flat pieces of pyrolytic graphite that levitate on North-South chessboard grid of neodymium magnets can be moved, tilted or shifted by the application of a strong enough laser beam [48]. This observation can be related to an increase in the temperature of the interfaces; the

provoked movement is due to a local decrease of the diamagnetic response in the sample. It would be interesting to measure the temperature of the sample during heating and observe changes in its levitation behavior after crossing a temperature around  $\sim 400$  K, which is of the order of the critical temperature of the superconducting-like response reported in [15,49].

## 5. Materials and Methods

### Samples

In order to investigate the magnetization of graphite samples with different thickness, several well-ordered graphite samples were selected taking into account previous characterization with STEM, XRD, magnetotransport and particle induced x-ray emission (PIXE) measurements. The bulk samples were natural graphite samples from Sri Lanka and Brazil [15] as well as HOPG samples of grade A (ZYA) (Union Carbide, Advanced Ceramic and SPI) of very high purity [12,35,50]. The total magnetic impurities concentration of the selected samples was below 3 ppm. See Appendix C in the supplementary information for more details on the results of this characterization as well as the arguments against the speculation that impurities or sample edges are the reason for the observed behavior of the susceptibility.

The embedded interfaces can be well recognized through STEM picture on Figure 1 (see also [10]) and the existence of the two well-ordered stacking orders by XRD [13,15].

To check for the quality of our samples and the reliability the used experimental setup, we measured the diamagnetic response of bulk samples of thickness  $t > 50 \mu\text{m}$  with the SQUID and the torque magnetometer. The measured  $c$ -axis mass susceptibility at 300 K of all bulk samples was  $\chi \simeq -(2.2 \pm 0.3) \times 10^{-5} \text{ emu/g Oe}$ , in good agreement with previously reported values for highly oriented bulk samples [3,31,37,51]. The mass of the graphite samples was measured with a Mettler Toledo AG245 balance. The size of the samples with thickness larger than  $100 \mu\text{m}$  were measured with an optical microscope, otherwise using a SEM.

### SQUID measurements

We have used two different magnetometers, a SQUID and a torque magnetometer; details of this last are given below. The SQUID measurements were done with a SQUID from Quantum Design. The samples were prepared as follows: Precharacterized bulk samples were selected, i.e. HOPG ZYA and natural graphite samples from Sri Lanka and Brazil mines. The HOPG ZYA samples were glued with a small amount of cryogenic varnish to a thin silicon substrate ( $4 \times 4 \times 0.18 \text{ mm}^3$ ). In Appendix E of the supplementary information we describe further the influence of the substrate on the SQUID measurements. The natural graphite samples obtained from a bulk sample were attached to a long, highly pure quartz rod using a small amount of varnish with the  $c$ -axis of the sample parallel to the applied field. The selected samples were exfoliated with a scotch tape in such a way that the surface of the graphite flake was as flat as possible. The background magnetic signals of the silicon substrate, varnish as well as of the quartz rod were previously characterized. They are much smaller (absolute value) than the signal of the samples, see Appendix E in the supplementary information.

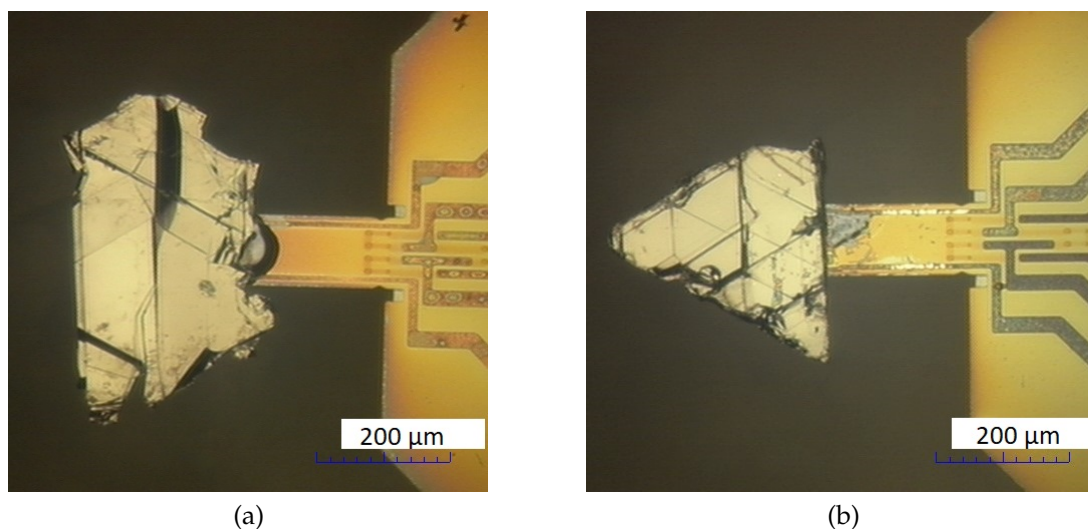
Finally, the graphite samples with their substrates were placed in a plastic straw keeping the magnetic field direction parallel to the  $c$ -axis of the graphite structure within  $\pm 2^\circ$ . Before each measurement, we left the superconducting solenoid with a remanence below 0.1 Oe, using the oscillating mode option of the SQUID. The magnetization was measured at different fixed fields at 300 K. Afterwards the whole measuring process was repeated. All susceptibility values shown and discussed in this manuscript were obtained at fields  $H \leq 10^4 \text{ Oe}$ .

### Torque measurements

Since graphite is a strong anisotropic material [31], its magnetic properties can be also investigated with a torque magnetometer. The torque measurements were realized using a system, which includes

335 a vacuum system with a water-cooled rotating magnet for the generation of fields up to 4 kOe,  
336 an AC Resistor Bridge AVS-47 with preamplifier, a Lake Shore Model 325 Cryogenic Temperature  
337 Controller and the torque magnetometer itself. It consists of a piezo-resistive cantilever PRSA-L300  
338 from SCL-Sensor. Tech. Fabrication GmbH. The cantilever has 4 piezoresistors in a Wheatstone bridge  
339 circuit increasing the sensitivity to magnetic moments of the order of  $m \sim 5 \times 10^{-10}$  emu at 1 kOe.  
340 The Wheatstone bridge is also used to compensate the magnetic field influence on the piezoresistors.  
341 Two resistors are placed at the edge of the cantilever for torque measurements and further two on the  
342 cantilever base for current compensation. A picture of the cantilever tip of the two magnetometers  
343 with the samples can be see in Figure 5.

344 The bulk natural samples were cleaned in ethanol and in an ultrasonic bath for 5 to 7 minutes  
345 for purification and a further fragmentation of the bulk piece. Ethanol droplets containing graphite  
346 flakes dropped onto a silicone substrate covered by 150 nm silicon nitride layer ( $\text{Si}_3\text{N}_4$ ). Afterwards  
347 the samples were dried on the substrates for more than one day and were attached at the edge of the  
348 cantilever as shown in Figure 5. Before starting the measurements we waited for a stable vacuum and  
349 temperature (300 K) for two days. Since the diamagnetic response at fields parallel to the  $c$ -axis of  
350 highly oriented graphite does not depend strongly on temperature, see Figure 2, we restricted the  
351 torque measurements to 300 K.



**Figure 5.** Natural graphite flakes on the tip of the cantilevers. The sample thickness was (a)  $1.2 \mu\text{m}$  and (b)  $6.9 \mu\text{m}$ . The other samples dimensions can be taken from the pictures using the scale bar that indicates  $200 \mu\text{m}$ . The bent seen in picture (a) does not represent a large portion of the graphite flake but it comes from a small part just at the sample surface. It represents an insignificant contribution to the total sample mass (or volume) affecting less than 1% the absolute value of the susceptibility. This is estimated through side pictures.

352 A simple way to check the calibration of the torque magnetometers used is to measure sample big  
353 enough so that one can measure them also with the SQUID. This has been done with one sample. We  
354 have checked the calibration through estimates of the strength factors for each cantilever following [52].  
355 After calibration of the torque signal the susceptibility was calculated dividing the magnetic moment  
356 field slope by the mass of the samples. Further details of the original experimental data, calibration  
357 procedure and estimates of the spring constant of the cantilevers necessary to calculate the magnetic  
358 moment can be read in Appendix D of the supplementary information. To check for the magnetic  
359 anisotropy and simultaneously the quality of the samples, the angle dependence of the torque has  
360 been measured using an applied field of 2 kOe and within a range of  $270^\circ$ , see Fig. 3.

## 361 6. Conclusion

362 Our results show that the absolute value of the diamagnetic susceptibility of highly ordered  
363 graphite is not constant, as assumed in the literature, but it depends on the sample even for samples of  
364 the same batch and volume. Below a certain thickness, our results indicate a decrease of the absolute  
365 value of the diamagnetic susceptibility with the sample thickness. Although more experimental data for  
366 thinner samples are needed to completely assure the observed trend, the behavior is compatible with  
367 recent studies of the galvanomagnetic properties of graphite. These as well as our results indicate the  
368 existence of a non-uniform heterostructure in real graphite samples strongly affecting their magnetic  
369 and electrical properties. The presented results stress the need of a reconsideration of previously  
370 published models used to understand the magnetic and electrical properties of graphite samples.

371 **Supplementary Materials:** The following are available online at <http://www.mdpi.com/2312-7481/xx/1/5/s1>:  
372 Appendix A (Comparison between the thickness dependence of the susceptibility and of the electrical conductivity  
373 at 4 K and 300 K) with one figure, Appendix B (Surface to volume ratio) with two figures, Appendix C (Particle  
374 induced x-ray emission (PIXE) characterization of the samples impurities), Appendix D (Original experimental  
375 data and the calibration curve) with two figures and Appendix E (Influence of substrate on SQUID measurements).

376 **Author Contributions:** B.S. performed all the magnetic measurements and data curation; P.D.E. performed the  
377 supervision of the experimental work; B.S. and P.D.E. conceived and designed the experiments and analyzed the  
378 data, and wrote the paper together.

379 **Funding:** B.S. was supported by Erasmus Mundus Webb project. P.E. was partially supported by the Mincyt from  
380 Argentine with the Milstein fellowship during his stay at the Instituto Balseiro in Bariloche, the University of  
381 Buenos Aires and the University of Tucumán, where part of the manuscript was written.

382 **Acknowledgments:** We acknowledge A. Champi and H. Beth for providing us with the natural graphite samples  
383 from Brazil and Sri Lanka, and W. Böhlmann for the STEM pictures. B.S. greatly thanks the support of A.  
384 Deutschinger, B. C. Camargo, J. Barzola-Quiquia, A. Setzer, V. Zviagin and M. Stiller.

385 **Conflicts of Interest:** The authors declare no conflict of interest. The funders had no role in the design of the  
386 study; in the collection, analysis and interpretation of data; in the writing of the manuscript and in the decision to  
387 publish the results.

## 388 Abbreviations

389 The following abbreviations are used in this manuscript:

390	2D	two dimensional
	HOPG	Highly Oriented Pyrolytic Graphite
391	SEM	Scanning Electron Microscopy
	STEM	Scanning Transmission Electron Microscopy
	SQUID	Superconducting Quantum Interference Device

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