

1 (Article)

2 Precision Permittivity Measurement for Low-Loss 3 Thin Planar Materials Using Large Coaxial Probe 4 from 1 to 400 MHz

5 Kok Yeow You^{1,*} and Man Seng Sim¹

6 ¹School of Electrical Engineering, Faculty of Engineering, Universiti Teknologi Malaysia, 81310, Skudai, Johor,
7 Malaysia; kyyou@fke.utm.my

8
9 * Correspondence: kyyou@fke.utm.my; Tel.: +(6)017-9529948

10

11 **Abstract:** This paper focuses on the non-destructive dielectric measurement for low-loss
12 planar materials with a thickness of less than 3 mm using a large coaxial probe with an outer
13 diameter of 48 mm. The aperture probe calibration procedure required only to make a
14 measurement of the half-space air and three offset shorts. The reflection coefficient for the
15 thin material is measured using a Keysight E5071C network analyzer from 0.3 MHz to 650
16 MHz and then converted to a relative dielectric constant and tangent loss via closed form
17 capacitance model and lift-off calibration process. Measurement error of dielectric constant,
18 $\Delta\epsilon_r$ is less than 2.5 % from 1 MHz to 400 MHz and the resolution of loss tangent, $\tan \delta$
19 measurement is capable of achieving 3×10^{-3} .

20 **Keywords:** large coaxial probe, thin planar materials, low-loss materials, relative permittivity, reflection
21 coefficient, calibration.
22

23 1. Introduction

24 The introduction should briefly place the study in a broad context and highlight why it is
25 important. It should define the purpose of the work and its significance. The current state of the
26 research field should be reviewed carefully and key publications cited. Please highlight
27 controversial and diverging hypotheses when necessary. Finally, briefly mention the main aim of the
28 work and highlight the principal conclusions. As far as possible, please keep the introduction
29 comprehensible to scientists outside your particular field of research. References should be
30 numbered in order of appearance and indicated by a numeral or numerals in square brackets, e.g., [1]
31 or [2,3], or [4–6]. See the end of the document for further details on references. Sensitivity,
32 sustainability and simplicity in operations are important requirements for sensing devices in
33 large-scale material processing industries. To reduce the uncertainty of the measurements, the
34 sensors should have large sensing area, high concentration of sensing field and high sensitivity to
35 the slight changes in material under test (MUT). The operating frequency of the permittivity, ϵ_r
36 measurements in most of the material processing industries are up to a few hundred MHz [1]-[3].

37 Open-ended coaxial probe technique is a simple, broadband and non-destructive way to
38 measure the relative permittivity, ϵ_r of a material. Coaxial probes have been commercialized and
39 used commonly since 1990 [4]. Recently, several probes have produced by manufacturers such as
40 SPEAG Inc. [5], KEYCOM [6], and APREL Inc. [7]. However, coaxial probes (N-type's or SMA's
41 diameter size) are less sensitive to small changes in the MUT especially for thin and low-loss
42 materials in permittivity, ϵ_r measurement at MHz frequency. This causes the measurement results
43 for low-loss materials at low frequencies to be highly scattered and less precise [8]. In fact, most

44 coaxial probe is only suitable for half-space infinite lossy material with $\epsilon_r' > 5$ and $\tan \delta > 0.05$
 45 [4]-[11].

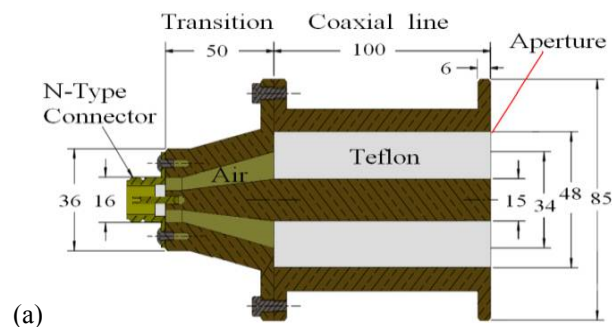
46 In this study, a large open-ended coaxial probe was designed to overcome those issues, which is
 47 capable of measuring the ϵ_r of low-loss materials having thickness of 1 mm precisely from 1 to 400
 48 MHz. The probe design of the probe and its performance were analyzed in detail. An explicit
 49 formulation for the prediction of ϵ_r , which does not involve numerical inversion routines (iterative
 50 method) as in [8]-[11],[13] is used. The differences in this study compared with previous works are
 51 summarized in Table 1.

52 2. Large Coaxial Probe Design

53 2.1. Dimensions and Structure

54 The designed coaxial probe as shown in Figure 1 (a) is made of brass, since the material is
 55 relatively low cost and has slower surface oxidation process when it is exposed to the moisture in the
 56 air. The dimensions of the coaxial probe with outer radius of inner conductor, $a = 7.5$ mm and inner
 57 radius of outer conductor, $b = 24.0$ mm, were designed based on the characteristic impedance, $Z_o =$
 58 $[60 \times \ln(b/a) / \sqrt{\epsilon_c}] = 50 \Omega$. The maximum limit of the operating frequency, f_{max} propagating in the
 59 coaxial line of the probe is determined using TE₁₁ cut-off as: $f_{max} = (3 \times 10^8) / [\pi(b+a)\sqrt{\epsilon_c}] \approx 2.1$ GHz. The
 60 symbol ϵ_c (Air: $\epsilon_c = 1$, Teflon: $\epsilon_c = 2.06$) represents the relative permittivity of material filling in the
 61 coaxial line in between the inner and outer conductor. The total weight of the coaxial probe is 2.6 kg.
 62 It has been divided into three sections: **(I)** N-type connector, which is used to connect the coaxial probe
 63 with the network analyzer via cable. **(II)** Transition section, which is a 50 mm of air-filled
 64 conical taper. The radius a and b of the conductors are increased along the transition length with a
 65 constant ratio, $b/a = 2.3$. Ratio, $b/a = 2.3$ is required to maintain $Z_o = 50 \Omega$ along the transition length
 66 to achieve low return loss and the lowest standing wave ratio (SWR) during the transformation from
 67 small to large coaxial line. **(III)** Large coaxial line section, which is a 100 mm length of 50 Ω teflon-filled
 68 coaxial line with $b/a = 3.3$. The Teflon isolation block is used to prevent the MUT from getting into the
 69 coaxial line. In addition, Teflon has high flexural strength, excellent chemical resistance, and high
 70 stability over a wide temperature range.
 71

72



73



74

(b)



(c)

75 **Figure 1.** (a) Cross-sectional side view and dimensions (in millimeter) of the coaxial sensor. (b) Side
 76 view of the large coaxial sensor. (c) Internal configuration of the coaxial sensor.

77

78

Table 1. Comparative study of large probe.

Ref.	Probe size (cm)	f (MHz)	Transition section	Sample contact	Sample size/shape	Calibration standards	Measured ϵ_r' range	Inverse method
[8]	$2a = 1.00$ $2b = 3.25$ $L = 5.00$	100 – 900	without	Aperture probe	Half-space infinite	Air, short, NaCl solution.	~5-80	Iterative
[9]	$2a = 1.00$ $2b = 3.25$ $L = 5.00$	1 – 10 or 10–3000	without	Aperture probe	Half-space infinite	Short cavity or Air, short, short cavity	~30-80 (Lossy)	Iterative
[10]	$2a = 1.18$ $2b = 4.00$ $L \approx 13.0$	200 – 1500	with	Aperture probe	Half-space infinite	Air, copper plate, Teflon plate.	~5 - 35 (Lossy)	Iterative
[11]	$2a = 4.50$ $2b = 10.3$ $L \approx 41.0$	50 – 1000	with	Filled in coaxial line	Toroid-shaped	3 positions short-circuit along the coaxial line	~7-80 (Lossy)	Iterative
This study	$2a = 1.50$ $2b = 4.80$ $L = 15.0$	1 – 400	with	Aperture Probe	Thin planar backed by metal plate	Air, 3 offset shorts	1 - 20 (Lossless)	Non-iterative

79

* L is the coaxial length of the probe.

80

81

2.2. Probe Characterization Test

82

83

84

85

The complex reflection coefficient, $\Gamma_{AA'} = |\Gamma_{AA'}| \exp(j\phi_{AA'})$ at plane AA' for four MUTs were measured using Keysight E5071C network analyzer in the frequency ranging from 0.3 MHz to 650 MHz at 25 °C. Calibration was done at the AA' plane, as shown in Figure 2, using Keysight 85032F kit.

86



87

88

Figure 2. Experimental set-up and measurement.

89

90

91

92

93

94

95

The sensing distance, h of the probe is 30 mm, which was estimated based on the distance at which the measured phase shift, $\phi_{AA'}$ (rad) as shown in Figures 3 (a) and (b) starting to become constant when the metallic plate was being moved away from the probe aperture in air. Figure 4 shows the time-domain measurements of the coaxial probe, which is operated with minimum windowing and bandpass mode. Clearly, coaxial probe of 15 cm length is sufficient to avoid the interference between plane- AA' and $-BB'$ for the frequency-domain $\Gamma_{AA'}$ measurement.

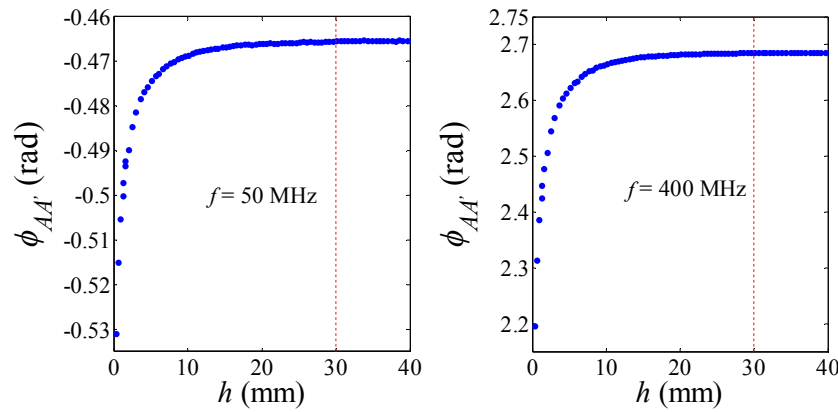


Figure 3. Variation in phase shift $\phi_{AA'}$ with air thickness, h backed by metal plate at (a) 50 MHz and (b) 400 MHz.

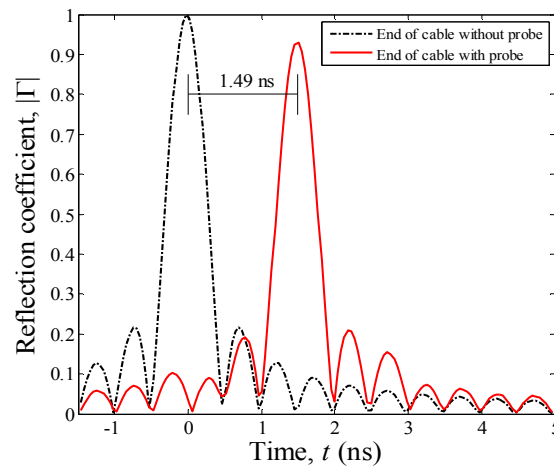


Figure 4. The time-domain response for the end of cable at plane-AA' with and without probe.

3. Calibrations

3.1. Probe Aperture Calibration

The actual normalized admittance, \tilde{Y}_{meas} , was measured with the aperture of the probe placed on a two-layer media, in which the first layered medium was a thin sample to be tested with thickness, h and the second layered medium was the conducting plate. The value of the \tilde{Y}_{meas} of the thin sample is obtained after de-embedding using (2). The effective relative permittivity, ϵ_{eff} of the sample can be estimated as:

$$\epsilon_{eff} = \left(\frac{Y_o}{j\omega C} \right) \tilde{Y}_{meas} - \frac{C_f}{C} \quad (1)$$

where

$$\tilde{Y}_{meas} = \tilde{Y}_{AA'} \left(\frac{\tilde{Y}_{BB'_{Air}}}{\tilde{Y}_{AA'_{Air}}} \right) \quad (2)$$

where $\tilde{Y}_{AA'_{Air}}$ is the measured admittance for air at plane AA', and $\tilde{Y}_{BB'_{Air}}$ is the simulated standard value of admittance for air at aperture probe (plane BB') using the COMSOL simulator. The relationship between $\Gamma_{AA'}$ and $\tilde{Y}_{AA'}$ is given as:

$$\tilde{Y}_{AA'} = \frac{1 - \Gamma_{AA'}}{1 + \Gamma_{AA'}} \quad (3)$$

117

118

119 Symbol $Y_0 = 0.02 \text{ S}$, $C = 2.38\epsilon_0(b-a)$ [11], C_f , and ω are the characteristic admittance, aperture probe
120 capacitance, fringing field capacitance, and the angular frequency, respectively.

121 3.2. Effective Permittivity Calibration

122 For thin solid planar material measurements, the scattering of the wave from probe's aperture
123 would penetrate the thin planar material and impinge on the other layer-interface media. In this
124 situation, the effective permittivity, ϵ_{eff} of the thin specimen will be measured, but not the actual
125 permittivity, ϵ_r of the material [10]. In this study, the relationship between the actual relative
126 permittivity, ϵ_r and effective relative permittivity, ϵ_{eff} for a finite thickness planar specimen was
127 empirically expressed as:

$$\epsilon_r = \epsilon_{eff} (a_1 + a_2 e^{-h/M} + a_3 e^{-2h/M}) \quad (4)$$

128

129 where h is the thickness of the specimen. The empirical coefficient, M was found to suite the large
130 probe, which can be roughly represented by single value as 0.006 [10]. The unknown complex
131 coefficients (a_1 , a_2 , and a_3) values in (4), were found by using three offset-short terminators ($\epsilon_r = 1$),
132 yield:

$$1 = \epsilon_{eff1} (a_1 + a_2 e^{-h_1/M} + a_3 e^{-2h_1/M}) \quad (5a)$$

133

$$1 = \epsilon_{eff2} (a_1 + a_2 e^{-h_2/M} + a_3 e^{-2h_2/M}) \quad (5b)$$

134

$$1 = \epsilon_{eff3} (a_1 + a_2 e^{-h_3/M} + a_3 e^{-2h_3/M}) \quad (5c)$$

135

136

137 The unknown values of a_1 , a_2 , and a_3 in equations (5a)-(5c) were explicitly determined using Cramer's
138 rule as:

$$a_1 = \frac{\left\{ \begin{array}{l} (1/\epsilon_{eff1})(e^{-(h_2+2h_3)/M} - e^{-(2h_2+h_3)/M}) - (1/\epsilon_{eff2})(e^{-(h_1+2h_3)/M} - e^{-(h_3+2h_1)/M}) \\ + (1/\epsilon_{eff3})(e^{-(h_1+2h_2)/M} - e^{-(h_2+2h_1)/M}) \end{array} \right\}}{D} \quad (6a)$$

139

$$a_2 = \frac{\left\{ \begin{array}{l} (1/\epsilon_{eff2})e^{-2h_3/M} - (1/\epsilon_{eff3})e^{-2h_2/M} - (1/\epsilon_{eff1})e^{-2h_3/M} + (1/\epsilon_{eff3})e^{-2h_1/M} \\ + (1/\epsilon_{eff1})e^{-2h_2/M} - (1/\epsilon_{eff2})e^{-2h_1/M} \end{array} \right\}}{D} \quad (6b)$$

140

$$a_3 = \frac{\left\{ \begin{array}{l} (1/\epsilon_{eff3})e^{-h_2/M} - (1/\epsilon_{eff2})e^{-h_3/M} - (1/\epsilon_{eff3})e^{-h_1/M} + (1/\epsilon_{eff1})e^{-h_3/M} \\ + (1/\epsilon_{eff2})e^{-h_1/M} - (1/\epsilon_{eff1})e^{-h_2/M} \end{array} \right\}}{D} \quad (6c)$$

141

142

143 The determinant, D of the equations (6a)-(6c) are given as:

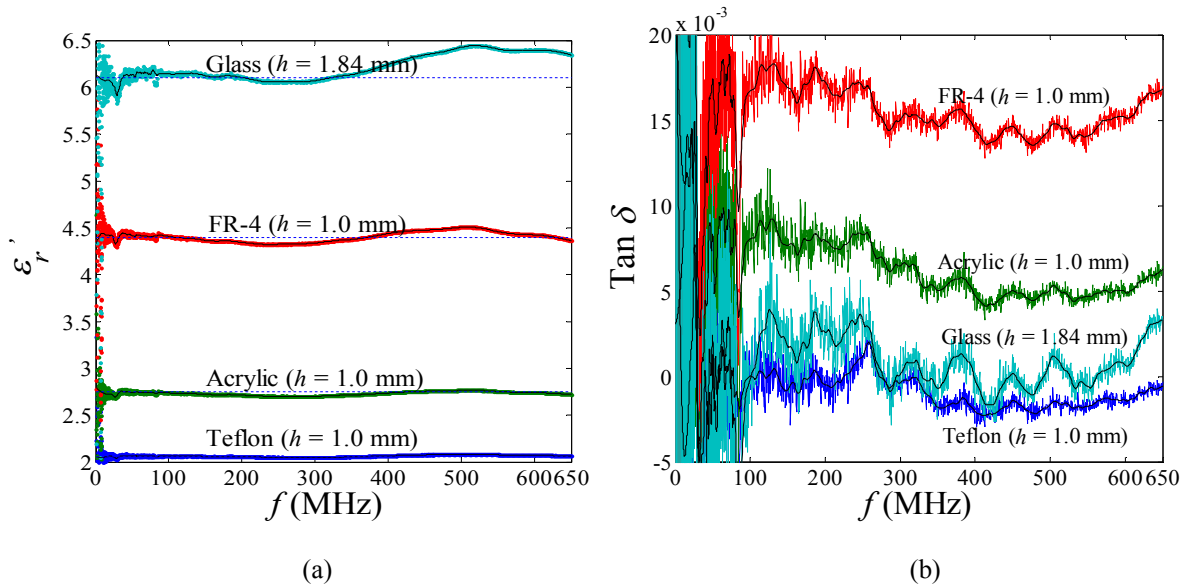
144

$$D = \left\{ e^{-(h_2+2h_3)/M} - e^{-(2h_2+h_3)/M} - e^{-(h_1+2h_3)/M} + e^{-(h_3+2h_1)/M} + e^{-(h_1+2h_2)/M} - e^{-(h_2+2h_1)/M} \right\} \quad (7)$$

145

146 **4. Results and Discussion**

147 Figures 5 (a) and (b) show the measured ϵ_r' and $\tan \delta$ of four thin low-loss MUTs which are in
 148 good agreement with expected values as tabulated in Table 2. The measured scattered data in
 149 Figures 5 (a) and (b) have been smoothed by Local Polynomial Regression (Loess) algorithm, which
 150 is available in built-in MATLAB "smooth" command. The smoothed data are represented by the
 151 black solid lines in Figures 5 (a) and (b).
 152



155 **Figure 5.** Variation in (a) measured ϵ_r' and (b) measured $\tan \delta$ with frequency for the MUTs at
 156 room temperature.
 157

158

Table 2. Expected values for ϵ_r' and $\tan \delta$.

MUT	ϵ_r' (Typ)	$\tan \delta$ (Max)
Teflon	2.06	0.0004
Acrylic	2.75	0.019
FR-4	4.4	0.022
Glass	6.1	0.0036

159

160 Figure 6 shows the percentage of the relative error between the smoothed values of ϵ_r' in Figure
 161 5 (a) and the expected values of ϵ_r' in Table 2. The relative errors are less than 2.5 % for overall
 162 measurements from 1 MHz to 400 MHz. In addition, the resolution for measurement $\tan \delta$ is capable
 163 of achieving 3×10^{-3} .
 164

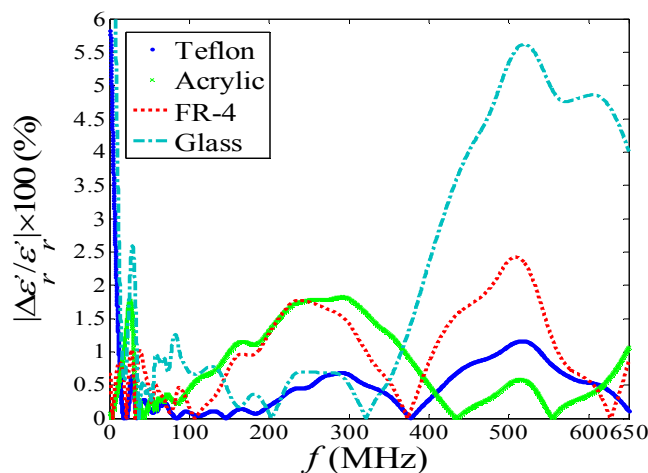


Figure 6. Variation in % relative error of ϵ_r' .

165
166

167 5. Conclusion

168 One-port measurement using a large coaxial probe is an easy, durable and cost effective
169 measurement method in large-scale material processing industries. In this study, the dielectric
170 properties for thin low-loss materials (a few millimeter thickness) at very low frequencies (below 400
171 MHz) have been precisely measured using the open-ended coaxial probe techniques. This accuracy
172 level of the measurement is rarely achieved by previous studies, which used the same technique for
173 low-loss material at very low frequencies.

174

175 **Author Contributions:** Conceptualization, K.Y.Y.; Methodology, K.Y.Y.; Software, K.Y.Y.; Validation, M.S.S.,
176 and K.Y.Y.; Formal Analysis, K.Y.Y. and M.S.S.; Investigation, K.Y.Y. and M.S.S.; Resources, K.Y.Y.; Data
177 Curation, K.Y.Y.; Writing—Original Draft Preparation, K.Y.Y.; Writing—Review and Editing, K.Y.Y.;
178 Visualization, K.Y.Y.; Supervision, K.Y.Y.; Project Administration, K.Y.Y.; Funding Acquisition, K.Y.Y.

179 **Funding:** This research was funded by i-Stone Technology and Research University Grant (GUP) from
180 Universiti Teknologi Malaysia under project number Q.J130000.2523.15H30 and the Ministry of Higher
181 Education of Malaysia (MOHE).

182 **Acknowledgments:** Authors would like to thank to Kok-San Chan, Shau-Lim Ooi, Tze-Lok Eng, Cha-Heng Toh
183 for their invaluable support in probe fabrication.

184 **Conflicts of Interest:** The authors declare no conflict of interest.

185 References

- 186 1. Bakhshiani, M.; Suster, M. A.; & Mohseni, P. A Broadband Sensor Interface IC for Miniaturized Dielectric
187 Spectroscopy from MHz to GHz. *IEEE Journal of Solid-State Circuits* **2014** 49(8), 1669-1681, DOI:
188 10.1109/CICC.2013.6658444.
- 189 2. Hegde, V. J.; Gallot-Lavallée, O.; Heux, L.. Dielectric study of Polycaprolactone: A biodegradable polymer.
190 In, 2016 *IEEE International Conference on Dielectrics (ICD)*, 3-7 July 2016 (Vol. 1, pp. 293-296). IEEE:
191 Montpellier, France, 2016.
- 192 3. Noh, J.; Kim, S. M.; Heo, S.; Kang, S. C.; Kim, Y.; Lee, Y. G.; ... & Lee, B. H. Time Domain Reflectometry
193 Analysis of the Dispersion of Metal–Insulator–Metal Capacitance. *IEEE Electron Device Letters* **2017** 38(4),
194 521-524, DOI: 10.1109/LED.2017.2671367.
- 195 4. Hewlett-Packard. User's Manual: HP 85070B Dielectric Probe Kit. USA, 1997; Hewlett-Packard Company.
- 196 5. SPEAG. High Precision Dielectric Measurements: DAK. Switzerland, 2018; Schmid & Partner Engineering
197 AG.
- 198 6. KEYCOM. Open Mode Probe Method Dielectric Constant and Dielectric Loss Tangent Measurement
199 System. Japan. KEYCOM Characteristic Technologies.
- 200 7. APREL. Dielectric Probe Kit ALS-PR-DIEL. Canada, 2014; APREL Inc.

- 201 8. Filali, B.; Boone, F.; Rhazi, J.; Ballivy, G. Design and Calibration of a Large Open-ended Coaxial Probe for
202 the Measurement of the Dielectric Properties of Concrete. *IEEE Transactions on Microwave Theory and*
203 *Techniques* **2008** 56(10), 2322–2328, DOI: 10.1109/TMTT.2008.2003520.
- 204 9. Otto, G. P.; Chew, W. C. Improved Calibration of a Large Open-Ended Coaxial Probe for Dielectric
205 Measurements. *IEEE Transactions on Instrumentation and Measurement* **1991** 40(4), 742–746, DOI:
206 10.1109/19.85345.
- 207 10. Damme, S. V.; Franchois, A.; Zutter D. D.; Taerwe, L. Nondestructive Determination of the Steel Fiber
208 Content in Concrete Slabs with an Open-Ended Coaxial Probe. *IEEE Transactions on Geoscience and Remote*
209 *Sensing* **2004** 42(11), 2511–2521, DOI: 10.1109/TGRS.2004.837332.
- 210 11. Huang, Y. Design, Calibration and Data Interpretation for a One-port Large Coaxial Dielectric
211 Measurement Cell. *Measurement Science Technology* **2001** 12(2001), 111–115, DOI:
212 10.1088/0957-0233/12/1/315.
- 213 12. Bobowski, J. S.; Clements, A. P. Permittivity and Conductivity Measured Using a Novel Toroidal
214 Split-Ring Resonator. *IEEE Transactions on Microwave Theory and Techniques* **2017** 65(6), 2132–2138, DOI:
215 10.1109/TMTT.2016.2645147.
- 216 13. Shehab, F.; Myers, M. T.; Ott, H.; Dolan, S.; Dietderich, J.; Bayazitoglu, Y. Uniaxial Complex Relative
217 Permittivity Tensor Measurement of Rocks From 40 Hz to 4.5 GHz. *IEEE Transactions on Geoscience and*
218 *Remote Sensing* **2017** 55(2), 1125–1139, DOI: 10.1109/TGRS.2016.2620078.
- 219 14. Gajda, G. B.; Stuchly, S. S. Numerical Analysis of Open-Ended Coaxial Lines. *IEEE Transactions on*
220 *Microwave Theory and Techniques* **1983** 31(5), 380–384, DOI: 10.1109/TMTT.1983.1131507.