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Visual Inertial Odometry with Robust Initialization and Online Scale Estimation

Euntae Hong 1, Jongwoo Lim 1,*

1 Division of Computer Science and Engineering, Hanyang University, Seoul, 133-791, Korea;
hongeuntae@hanyang.ac.kr, jlim@hanyang.ac.kr
* Correspondence: jlim@hanyang.ac.kr; Tel.: +82-02-2220-2376

Abstract: Visual inertial odometry (VIO) has recently received much attention for efficient and accurate ego-motion estimation of unmanned aerial vehicle systems (UAVs). Recent studies have shown that optimization-based algorithms achieve typically high accuracy when given enough amount of information, but occasionally suffer from divergence when solving highly non-linear problems. Further, their performance significantly depends on the accuracy of the initialization of inertial measurement unit (IMU) parameters. In this paper, we propose a novel VIO algorithm of estimating the motional state of UAVs with high accuracy. The main technical contributions are the fusion of visual information and pre-integrated inertial measurements in a joint optimization framework, and the stable initialization of scale and gravity using relative pose constraints. To handle ambiguity and uncertainty of VIO initialization due to unpredictable motion patterns, a local scale parameter is adopted in the online optimization. Quantitative comparisons with the state-of-the-art algorithms on the EuRoC dataset verify the efficacy and accuracy of the proposed method.

Keywords: visual-inertial odometry; UAV navigation; sensor fusion; optimization

1. Introduction

In robots and Unmanned Aerial Vehicle systems (UAVs), the ego-motion estimation is essential. To estimate the current pose of a robot, various sensors such as GPS, inertial measurement unit (IMU), wheel odometry, and camera have been used. In recent years, the visual-inertial odometry (VIO) algorithm, which fuses the information from a camera and an IMU, has been garnering increasing interest because it overcomes the disadvantages of other sensors and can operate robustly. For example, a GPS sensor can estimate the global position of the device, but it can only operate in outdoors, and cannot get precise positions needed for UAV navigation. An IMU sensor measures acceleration and angular velocity with high frequency, but the pose estimated by integrating the sensor readings easily drift due to the sensor noise and time-varying biases. The visual odometry (VO) is more accurate than other sensors for estimating the device poses because it utilizes the long-term observations of distant visual features. However, it is vulnerable to motion blur from fast motions, lack of scene textures, and abrupt illumination changes. Also monocular VO systems cannot estimate the absolute scale of motion. By fusing IMU and visual information, VIO operates in extreme environments where the VO fails, and achieve higher accuracy with metric scale.

Initially VIO is approached by loosely-coupled fusion of visual and inertial sensors [1,2]. An Extended Kalman Filter (EKF) [3,4] is also used as it can update the current state (e.g., the 3D pose and covariance) by solving a linearized optimization problem for all state variables in a tightly-coupled manner [5–7]. The filtering-based approaches can estimate the current poses fast enough for real-time applications; however they are less accurate than the optimization-based approach because of the approximation in the update step. Recently the optimization-based algorithms [5–8] have been developed for higher accuracy, but they require higher computation cost and suffer from divergence when the observation is poor or the initialization is not correct. Certainly there is a trade-off between
performance and speed, and it is difficult to optimize all the parameters in the initialization and update phase, especially when the information is insufficient.

In this work, we propose a VIO system that uses the tightly-couple optimization framework with a robust initialization method for the scale and gravity. A non-linear problem for visual-inertial system may not have a unique solution depending on the some types of the motions [9], and it makes the initialization task a challenging research. We jointly optimize a relative motion constraint together with other parameters and update by the accuracy of the optimization result rather than waiting for a precise scale to be computable. And we verified that we can estimate the reliable camera pose quantitatively on real scale for EuRoC [10] benchmark dataset including dynamic illumination changes and fast motion. Our main contributions are summarized as follows:

- We propose a novel visual-inertial odometry algorithm using non-linear optimization of tightly-coupled visual and pre-integrated IMU observations with a local scale variable.
- A robust online initialization algorithm for the metric scale and gravity directions is introduced. By enforcing the relative pose constraints between keyframes acquired from visual observations the initial scale and gravity vectors can be estimated reliably.
- To avoid the failure due to the divergent scale variable in optimization, the proposed system determines the initialization window size adaptively and autonomously.
- The experimental results show that the proposed method achieves higher accuracy than the state-of-the-art VIO algorithms on the well-known EuRoC benchmark dataset.

2. Related work

The VIO algorithms focus on highly accurate pose estimation of a device by fusing visual and IMU information. Cameras provide the global and stationary information of the world but the visual features are heavily affected by the external disturbances like fast motion, lighting, etc. IMU sensors generate instantaneous and metric motion cues, but integrating the motions for a long period of time results a noisy and drifting trajectory. As these two sensors are complementary there have been many attempts to combine the two observations.

Recent VIO algorithms can be classified into filtering-based approach which feeds the visual and inertial measurements to filters, and optimization-based approach using non-linear optimization for state estimation. The former approaches use an Extended Kalman Filter (EKF) [11] which represents the state as a normal distribution with the mean and covariance. The EKF-based system are faster than the optimization-based methods since they use linearized motion and observation models. In the multistate constrained Kalman filter (MSCKF) [3], the visual information and IMU data are combined into a filter and the body poses are updated by a 3D keypoints processing with high accuracy. Li and Mourikis [4] proposes the new closed-form representation for the IMU error state transition matrix to improve the performance of MSCKF and the online model with extrinsic calibration. Hesch et al. [12] develop an observability constraint, OC-VINS, that explicitly enforces the system’s unobservable direction, to prevent spurious information gain and reduce discrepancies. The optimization-based methods are more accurate than the filtering-based method; however, it suffers from a high computational cost. To overcome this limitation, optimizing only a small window of poses or running an incremental smoothing is proposed [13,14]. Leutenegger et al. [5] propose to calculate the position and velocity by integrating IMU measurements with VO’s keyframe interval while marginalizing out to old keyframe poses to mitigate complexity. However, these methods use the propagated poses of the IMU measurements for a certain interval, which has the disadvantage of re-integrating the linear acceleration value according to the device orientation changes for the local window. Forster et al. [8] proposed extending the IMU pre-integration method [15] to efficiently update the bias variables by calculating linear approximation IMU biases Jacobian for a very short interval using the IMU pre-integration method. Lupton and Sukkarieh [16] proposed a slide window optimization framework for the IMU pre-integration method and old keyframe marginalization in local window, and Qin and

The optimization methods directly use IMU sensor measurements together with the visual features as the constraints of the pose variables which results a highly non-linear formulation. For accurate and stable pose estimation, the initialization of metric scale and gravity direction is critical because the time-varying IMU biases needs to be calculated from the device poses. If the biases are not estimated accurately the following online pose optimization is likely to diverge. Martinelli [9] demonstrates that there may exist multiple solutions in the visual-inertial structure from motion formulation. Mur-Artal and Tardos [6] proposes closed-form formulation for vision-based structure from motion with scale and IMU biases; however they should wait initialization until 15 seconds to make sure all values are observable. Weiss et al. [18] proposed an initialization method that converges quickly using the extracted velocity and the dominant terrain plane based on the optical flow between two consecutive frames, but it requires aligning the initial pose and the gravity direction at the beginning. We discuss in Section 5 how to calculate the metric scale and gravity using the pose graph optimization (PGO) [19] and IMU pre-integration.

3. System overview

The proposed visual-inertial odometry algorithm consists of visual feature tracking, IMU pre-integration, initialization, and optimization modules. We use the KLT-feature tracker [20] to find the correspondence of feature points for geometric modeling of camera poses and scene structure. Alternatively one can use descriptor matching algorithms [21–24] for this task, which is necessary for visual SLAM systems. We introduce a tightly coupled visual-inertial odometry system, which continuously estimates the motional state with a local scale parameter by minimizing the cost from visual information and IMU measurements (Section 4). We also present a robust initialization algorithm of the metric scale and gravity using pose graph optimization (Section 5).
Figure 2. (a) is the result of proposed system for V1 02 in EuRoC benchmark dataset, blue line is the estimated trajectory, black dots show reconstructed sparse landmarks, and red square represents the current camera pose. (b) shows a captured camera images in the EuRoC, which has experience of challenging environmental changes such as motion blur and illumination changes. Our proposed system has been verified to be able to estimate reliable poses for all sequences in Section 6.

4. Visual inertial optimization

The goal of the visual-inertial odometer is to estimate the current motional state using visual information and inertial measurements at every time. The state $s_t$ at time $t$ is defined as a quadruple

$$s_t = (\omega_d T_t, \omega_v, d_b^a, d_b^\omega_t),$$

where $\omega_d T = [\omega_d R, \omega_d p] \in SE(3)$ is the transformation from the device to the world coordinate system, $\omega_v$ is the velocity of the device, and $d_b^a, d_b^\omega$ are the sensor bias. The coordinate systems are denoted as a prescript on the left side of the symbol, and there are the world ($w$), the device ($d$), and the camera ($c$) coordinate systems. The time is denoted as a subscript ($t$) of the symbol. The world coordinate system is defined so that the gravity direction is aligned with the negative z-axis. We follow the convention that the device coordinate system is aligned with the IMU coordinate system. The transformation from the camera to the device coordinate system is written as $^c_d T$ and it is pre-calculated in the device calibration process [25,26].
4.1. Visual reprojection error

The visual error term of our proposed method uses the re-projection error in the conventional local bundle adjustment. The error is the difference between the projected location $x_{i,l}$ of a 3D landmark $X_l$ and its tracked location $\hat{x}_{i,l}$ at the keyframe $i$. The visual cost $C_{\nu,k}^i$ from the tracked features is defined as:

$$C_{\nu,k}^i = \rho \left( e^{\nu}(i,l)^\top \Lambda_{\nu,i}^{0} e^{\nu}(i,l) \right)$$  
$$e^{\nu}(i,l) = \hat{x}_{i,l} - \pi \left( \frac{d}{c} T^{-1} * w a T^{-1} * w X_l \right),$$  

where $\Lambda_{\nu,i}^{0}$ is the information matrix associated with the tracked feature point at the keyframe, and $\pi$ denotes the camera projection function. $*$ and $^{-1}$ denotes the composition/application and the inversion operators for SE(3) transformations respectively, and $\rho$ is the Huber norm [27], which is defined as:

$$\rho(x) = \begin{cases} 
1, & \text{if } x \geq 1 \\
2\sqrt{x} - 1, & \text{if } x < 1 
\end{cases}$$  

![Figure 3. Visualization of visual error. The green dashed line represents re-projection error $e^{\nu}$ and visual error term optimizes the summation of these errors for local window.](image)

4.2. IMU Pre-Integration

The IMU sensors measure the angular velocity and translational acceleration and in theory the 3D pose (orientation and position) of the device can be calculated by integrating the sensor readings over time. However, the raw IMU measurements contain significant noise and time-varying non-zero bias, and these make the integration-based pose estimation very challenging. The IMU angular velocity $d \hat{\omega}$ and acceleration $d \hat{a}$ measurements at time $t$ are modeled with the true acceleration $w a$ and angular velocity $d \omega$ as

$$d \hat{a}_t = w R^T \left( w a_t - w g \right) + d b a_t + n^a,$$
$$d \hat{\omega}_t = d \omega_t + d b \omega_t + n^\omega,$$

where $w R^T$ is the rotation from the world to the device coordinates (note the transpose), $w g$ is the constant gravity vector in the world, $d b_a$, $d b_\omega$ are the acceleration and gyroscope biases, and $n^a$, $n^\omega$ are the additive zero-mean noise. From the following relations,
position, velocity, and orientation that are not dependent to the biases can be written as follows from measurements to the poses of the consecutive frames by adding IMU factors incrementally as in [7,8].

In the optimization framework. Thus, we follow the pre-integration method, which represents IMU and it is computationally burdensome to re-integrate the values according to the changes of the state orientation of the device can be propagated through the first and second-integration used in [28],

\[
\Delta \mathbf{p}_{i,j} := \mathbf{R}_i \Delta \mathbf{p}_{i,j} = \mathbf{R}_i (\mathbf{d} \mathbf{a}_i - \mathbf{d} \mathbf{b}_{i,j} - \mathbf{n}^a) \Delta t_{i,j+1}^2
\]

\[
\Delta \mathbf{v}_{i,j} := \frac{\mathbf{R}_i \mathbf{v}_{i,j}}{\mathbf{R}_i} = \mathbf{R}_i (\mathbf{d} \mathbf{a}_i - \mathbf{d} \mathbf{b}_{i,j} - \mathbf{n}^a) \Delta t_{i,j+1}^2
\]

\[
\Delta \mathbf{R}_{i,j} := (\mathbf{d} \mathbf{R}_i) \mathbf{R}_i = \prod_{k=i}^{j-1} \mathbf{R}_k (\mathbf{d} \mathbf{a}_k - \mathbf{d} \mathbf{b}_{i,j} - \mathbf{n}^a) \Delta t_{i,k+1}^2
\]

Assuming the acceleration \( \mathbf{d} \mathbf{a}_k \) and the angular velocity \( \mathbf{d} \mathbf{\dot{a}}_k \) are constant between time interval \( t_k \) and \( t_{k+1} \), we can simplify the above equations as follows:

\[
\mathbf{w}_{p_{k+1}} = \mathbf{p}_{k+1} + \mathbf{v}_{k+1} = \mathbf{p}_k + \mathbf{v}_k \Delta t_{k+1} + \int_{t_k}^{t_{k+1}} (\mathbf{w} \mathbf{R}_k (\mathbf{d} \mathbf{a}_k - \mathbf{b}_{i,j} - \mathbf{n}^a) + \mathbf{w} \mathbf{g}) dt^2
\]

\[
\mathbf{w}_{v_{k+1}} = \mathbf{v}_{k+1} + \mathbf{g} \Delta t_{k+1} + \mathbf{R}_k (\mathbf{d} \mathbf{a}_k - \mathbf{d} \mathbf{b}_{i,j} - \mathbf{n}^a) \Delta t_{k+1}^2
\]

\[
\mathbf{w}_{\mathbf{R}_{k+1}} = \mathbf{R}_k \exp \left( \int_{t_k}^{t_{k+1}} (\mathbf{d} \mathbf{\dot{a}}_k - \mathbf{d} \mathbf{b}_{i,j} - \mathbf{n}^a) dt \right)
\]

The measurement rate of the IMU is much faster than that of the camera, as illustrated in Figure 4, and it is computationally burdensome to re-integrate the values according to the changes of the state in the optimization framework. Thus, we follow the pre-integration method, which represents IMU measurements to the poses of the consecutive frames by adding IMU factors incrementally as in [7,8].

For two consecutive keyframes \([i, j]\) where the time between two \((\Delta t_i, \Delta t_j)\) can vary, the changes of position, velocity, and orientation that are not dependent to the biases can be written as follows from the Equations 11-13:
where $\mathbf{R}_i^j$ represents the rotation from the frame $k$ to the time $i$. We can calculate the right side of above equation directly from the IMU measurements and the biases between the two keyframes. However, these equations are the function of the bias $d\mathbf{b}_{t_i}$ and $d\omega_{t_i}$. If the biases $d\mathbf{b}_{a}$ and $d\omega_{a}$ between the keyframes are assumed to be fixed, we can obtain the values of $\Delta\mathbf{p}_{t_i}, \Delta\omega_{t_i}, \Delta\mathbf{R}_{t_i}$ from the IMU measurements without re-integration.

However, in the case of bias, it changes slightly in the optimization window, and we use recent IMU pre-integration described in [7,8] to reflect the bias changes in the optimization by updating delta measurements of bias using the Jacobians which describe how the measurements change due to the estimation of the bias, as

$$ w\mathbf{p}_j = w\mathbf{p}_i + w\mathbf{v}_i\Delta t_{i,j} + \frac{1}{2} w\mathbf{g}\Delta t_{i,j}^2 + \frac{w}{2}\mathbf{R}_i(\Delta\mathbf{p}_{t_i} + J^{\omega}_{\mathbf{b}} d\omega_{t_i} + J^{a}_{\mathbf{b}} d\mathbf{b}_{t_i}) $$

$$ w\mathbf{v}_j = w\mathbf{v}_i + w\mathbf{g}\Delta t_{i,j} + \frac{w}{2}\mathbf{R}_i(\Delta\mathbf{v}_{t_i} + J^{\omega}_{\mathbf{b}} d\omega_{t_i} + J^{a}_{\mathbf{b}} d\mathbf{b}_{t_i}) $$

$$ w\mathbf{R}_j = w\mathbf{R}_i \Delta\mathbf{R}_{t_i} \exp(J^{\omega}_{\mathbf{b}} d\omega_{t_i}), $$

where $J^{\omega}$ and $J^{a}$ are the Jacobians which are first-order approximations of the variation of the IMU biases.

Finally, the local optimization cost of the IMU residual $e^\mu_{t_{ij}}$ for the interval of keyframes $i$ and $j$ using pre-integration is defined as follows:

$$ C^\mu_{t_{ij}} = e^\mu(i,j)^\top \Lambda^\mu_{t_{ij}} e^\mu(i,j) $$

$$ e^\mu(i,j) = \begin{bmatrix} w\mathbf{R}_i^j (w\mathbf{p}_j - w\mathbf{p}_i - w\mathbf{v}_i\Delta t_{i,j} - \frac{1}{2} w\mathbf{g}\Delta t_{i,j}^2 ) - (\Delta\mathbf{p}_{t_i} + J^{\omega}_{\mathbf{b}} d\omega_{t_i} + J^{a}_{\mathbf{b}} d\mathbf{b}_{t_i}) \\ \frac{w}{2}\mathbf{R}_i^j (w\mathbf{v}_j - w\mathbf{v}_i - w\mathbf{g}\Delta t_{i,j}) - (\Delta\mathbf{v}_{t_i} + J^{\omega}_{\mathbf{b}} d\omega_{t_i} + J^{a}_{\mathbf{b}} d\mathbf{b}_{t_i}) \\ \exp(\frac{w}{2}\mathbf{R}_i^j) \exp(J^{\omega}_{\mathbf{b}} d\omega_{t_i}) \right)^\top \frac{w}{2}\mathbf{R}_i^j \\ \frac{w}{2}\mathbf{R}_i^j \exp(J^{\omega}_{\mathbf{b}} d\omega_{t_i}) \right)^\top \frac{w}{2}\mathbf{R}_i^j \\ d\mathbf{b}_{t_i}^\mu - d\mathbf{b}_{t_i}^a \\ d\omega_{t_i}^\mu - d\omega_{t_i}^a \end{bmatrix} $$

where, $\Lambda^\mu_{t_{ij}}$ is the information matrix associated with the IMU pre-integration covariance between the keyframes, reflecting the IMU factor noise. As the IMU biases follow the Brownian motion model, we penalize abrupt changes of the biases between consecutive keyframes with the bias costs at the bottom two entries in Equation 21.
4.3. Online optimization

Considering UAVs, the VIO system should estimate the current pose in real-time using captured visual information and IMU measurement. We use the visual-inertial bundle adjustment framework and solve the optimization problem with the Gauss-Newton algorithm implemented in the ceres-solver [29]. For the state \( s_n \) and the 3D landmarks \( l_m \), the cost function is defined as follows for the optimization window

\[
S_{\text{online}} = (s_0, s_1, \ldots, s_n, l_m) \quad (22)
\]

\[
S^*_{\text{online}} = \arg\min_{S_{\text{online}}} \left\{ C_p + \sum_{k,d} C_{k,j}^p + \sum_{k} C_{k,k+1}^r \right\} \quad k \in [0, n], i \in m \quad (23)
\]

where, \( C_p \) is the prior information from marginalization which is the factor for the states out of the local optimization window.

The scale estimated from initialization is often not observable since it has a dependent on motion. In order to estimate a optimal metric scale, we include the local scale factor into our cost function and optimize it with other variables such as poses. When a new keyframe is added, we assumed that the device experiences the motion changes and perform jointly optimization including local scale \( s \) variable.

\[
e^R(i,j) = \begin{bmatrix}
   d_{R_i}^w \left( \left( w_{p_j} - w_{p_i} \right)s - \left( w_{v_j} - w_{v_i} \right) \Delta t_{ij} - \frac{1}{2} w_{g} \Delta t_{ij}^2 \right) - \left( \Delta p_{ij} + J^w_R \Delta b_{w_i}^d + J^w_R \Delta a_{i}^d \right) \\
   d_{R_j}^w \left( \left( w_{v_j} - w_{v_i} \right)s - \left( w_{g} \right) \Delta t_{ij} \right) - \left( \Delta v_{ij} + J^w_R \Delta b_{w_i}^d + J^w_R \Delta a_{ij}^d \right) \\
   \log((\Delta R_{ij}) \operatorname{Exp}(J^w_R \Delta b_{w_i}^d)) \right)^T d_{R_i}^w \\
   d b_{w_j}^d - d b_{w_i}^d \\
   d b_{w_j}^d - d b_{w_i}^d
\end{bmatrix} \quad (24)
\]

Figure 5 shows the graphical model of our visual inertial local bundle adjustment. We perform local optimization with sufficiently accurate scale variable which is computed through bootstrapping in Section 5, and the optimized reliable local scale is marginalized to prior information along with the pose of the old keyframe.

Figure 6. The difference estimated trajectories with ground truth of MH 01 for the non-scale optimization (left) and the proposed optimization involving scale (right). The proposed method is able to accurately estimate the poses by updating the scale incrementally.
4.4. Marginalization

The optimization-based VIO algorithms need to marginalize out the old information not to slow down the processing speed [5,7]. The marginalization does not eliminate the old information outside of the local optimization window of keyframes, but converts it into a linearized approximate form to the remaining state variables using Schur complement [30]. When a new keyframe is added into the local optimization window and the window size exceeds the preset threshold, the state of the oldest keyframe in the window including the pose, velocity, and bias is marginalized (Figure 7 illustrates keyframe marginalization in a graphical model). On the other hand, if the current frame is not selected as a keyframe, only the visual information is dropped while the IMU measurements are kept for IMU pre-integration. The marginalized factor is applied to be a prior of the next optimization, which helps to find a better solution than simply fixing the keyframe poses outside of the optimization window.

![Figure 7. Old keyframe marginalization with optimized scale. Marginalized measurements are used as prior for the next optimization.](image)

5. Bootstrapping

Unlike the monocular visual odometry where the camera parameters are known and the absolute scale of the map is not recoverable, the visual-inertial odometry needs to find the critical parameters such as the scale of the map and gravity direction to robustly estimate the state. Moreover there are many motion patterns in which the multiple solutions of IMU bias parameters exist, such as constant velocity motions including no motion [9]; thus, optimization involving all state variables without precise initialization may not converge to the true solution. For these reasons, some VIO systems require approximate manual initialization of the gravity vectors or IMU biases, or real scale distance information using different sensors [31]. The map of visual features are constructed starting from the two keyframes with sufficient parallax, and it is continuously updated as more keyframes are observed. However, the IMU measurements for these keyframes may not observe any significant changes in acceleration, and this can cause failure in bootstrapping the VIO system.

In this work, we propose a bootstrapping method that computes the accurate scale and gravity through stepwise optimization using relative pose constraints. Our method consists of vision-only map building, pose graph optimization with IMU pre-integration, convergence check, and IMU bias update.

5.1. Vision-only map building

The first step, vision-only map building, is identical to monocular visual odometry [32,33] and structure from motion algorithms (SFM) [34]. The system finds the first two keyframes $w_c^T_0$ and $w_c^T_1$ with sufficient motion, by checking the numbers of inlier features by a Homography and a unit-translation SE3 motion by the five-point algorithm [35]. Since the absolute scale of motion is not available, the visual map is initialized in an arbitrary scale and the inlier features are triangulated and their 3D positions are registered. The gravity direction is roughly initialized with the average of the first acceleration vectors (we experimentally use the first 30 readings @ 200Hz), and the world coordinate system is set by aligning the gravity to $y$-down. Once the initial map with 3D points is
Algorithm 1: Proposed online VIO algorithm

Data: Images, accelerations and gyro

Result: 6DOF poses and landmarks

Initialization: Select 2 keyframes for visual motion based initialization and perform visual odometry to estimate relative keyframe motion [37]. Then, calculate the metric scale and gravity by PGO with IMU factor. Check the convergence of the optimized parameters and re-propagate the pre-integration factor using the initial bias, scale and gravity;

for $k = 1$ to $K$
do
  Extract and tracking keypoints using KLT [20];
  if $k^{th}$ frame is keyframe then
    Add new landmarks;
    Perform online optimization minimizing cost function with local scale factor Eqn. 24;
    Marginalize old keyframe’s variables with scale.;
  else
    Performs pose optimization by Eqn. 22 with fixed previous keyframe’s poses;
    Marginalize visual information observed on current frame;
  end
end
return optimized 6DOF pose and landmarks involving real scale.

built the pose of later keyframes are computed by the PNP algorithm [36] Local bundle adjustment using Equation 2 is performed initially and whenever a keyframe is added to improve the accuracy of pose and point positions. Until the scale and gravity is reliably measured in the next steps, purely vision-only map building is continued.

5.2. Pose graph optimization with IMU pre-integration

While purely visual mapping is running, we try to estimate the metric scale using the pre-integrated IMU factor. For easy formulation and efficient estimation, we adopt the pose graph optimization (PGO) framework [19,38,39] which constructs a graph of keyframes whose edges represent the relative pose constraints between keyframes, and optimizes the keyframe poses so that the inconsistency of the relative poses and constraints are minimized (note that this is equivalent to marginalizing the landmarks in bundle adjustment). PGO is commonly used in monocular SLAM systems to fix the scale drift in loop closures using Sim(3) relative poses. In contrast we use SE(3) relative poses with a global scale parameter $s$ to the entire map, as the scale drift for a short period of initialization time is not significant. Additional constraints from the pre-integrated IMU and the gravity vector are added to PGO, and the factors in our formulation are illustrated in Figure 8.

Formally we define the state for PGO with all keyframe poses, velocities, the gravity, and the global scale $s$ as

$$S_{pgo} = (wT_0, wT_1, \ldots, wT_n, wv_1, \ldots, wv_n, wg, s).$$

In this section we parameterize an SE(3) transformation with a pair of a translation vector $p$ and a Hamiltonian quaternion [40] $q$, i.e., $T = [R(q), p]$, where $R(\cdot)$ is the function converting a quaternion to a $3 \times 3$ rotation matrix.

While performing visual pose estimation, we calculate IMU pre-integration for keyframes using Equations 17-19, in which bias and noise are initialized as zero. Using Equations 17-18 for consecutive keyframes $i$ and $j$, we obtain the scale error cost $e^s_{ij}$

$$e^s(i,j) = \begin{bmatrix} R(wq_i)^T (wT_j - wT_i)s - wv_i \Delta t_{ij} - \frac{1}{2} wg \Delta t_{ij}^2 - (\Delta p_{ij} + J^e_{\Delta p} d b^w_{ij} + J^d_{\Delta p} d b^s_i) \\ R(wq_i)^T (wv_j - wv_i - wg \Delta t_{ij}) - (\Delta v_{ij} + J^e_{\Delta v} d b^w_{ij} + J^d_{\Delta v} d b^s_i) \end{bmatrix}$$

and $\mathcal{L}^s_{ij} = (e^s(i,j))^T \Lambda^s_{ij} e^s(i,j)$.
Hereby, $\Lambda_{ij}$ denotes the information matrix, and we use the sub-block of $M_{ij}$. Experimentally, the metric scale can be calculated to be zero if the motion is partially small or involve no motion. To prevent this case, the scale factor in the proposed method uses exponential parameterization. For the relative pose between two keyframes $i$ and $j$ is given as $\mathbf{p}_{ij} = \mathcal{R} (\mathbf{q}_i) (\mathbf{w}_{p_j} - \mathbf{w}_{p_i})$ and $\mathbf{q}_{ij} = \mathbf{q}_i^* \mathbf{q}_j$, the relative pose costs in PGO are given as follows:

$$
C_{ij} = e^{rel} (i, j) \Lambda_{ij}^w e^{rel} (i, j)
$$
(28)

$$
e^{rel} (i, j) = \begin{bmatrix}
\mathbf{p}_{ij} - \hat{\mathbf{p}}_{ij} \\
2 * \text{Vec} (\mathbf{q}_{ij} \hat{\mathbf{q}}_{ij}^*)
\end{bmatrix}
$$
(29)

where $(\hat{\mathbf{p}}_{ij}, \hat{\mathbf{q}}_{ij})$ is the relative pose constraint between keyframe $i$ and $j$ in the current map, Vec$(\mathbf{q})$ returns the vector (imaginary) part of the $\mathbf{q}$ and $\Lambda_{ij}^w$ is the information matrix from the keyframe pose covariance.

We define the optimization cost for a new state $\mathbf{S}_{pgo}$ by combining Equations 29 and 26 for whole keyframes $n$ as follows:

$$
\mathbf{S}_{pgo}^* = \underset{\mathbf{S}_{pgo}}{\text{argmin}} \left\{ \sum_{i,j \in k} C_{ij} + \sum_{k} C_{kk+1} \right\}, \quad k \in [0, n].
$$
(30)

Note that, because we know that the magnitude of gravity $\mathbf{g}$ is 9.8, we include the constraint $\mathbf{g}^\top \mathbf{g} = 9.8^2$ when performing the optimization.

5.3. Convergence check

The proposed scale and gravity optimization can be calculated in real-time at the moment of insertion of a new keyframe, and we update the optimized variable at a point sufficient to initialize VIO. We use two ways to measure the accuracy: covariance of $\mathbf{X}^*$ and variance of optimized scale variables. The covariance of $\mathbf{S}_{pgo}^*$ is given by,

$$
\text{C}(\mathbf{S}_{pgo}^*) = \left( J^\top (\mathbf{S}_{pgo}^*) J(\mathbf{S}_{pgo}^*) \right)^{-1}
$$
(31)

where $J(\mathbf{S}_{pgo}^*)$ is the Jacobian of Equation 30 at $\mathbf{S}_{pgo}^*$. We apply the optimized scale and gravity to the system initialization when the largest eigenvalue of the optimized covariance $\lambda_{max}(\text{C}(\mathbf{S}_{pgo}^*))$ is less than the threshold $\tau_{cov}$ and the scale variance is less than the threshold $\tau_{var}$ at the same time. The scale variance is calculated from the optimized scale value during the registration of few keyframes and measures the continuous accuracy of estimates. Experimentally, the scale and gravity initialization in the bootstrapping step are estimated to reliable values within 5 seconds on average for the EuRoC dataset, and then converge to an accurate value through continuous scale optimization in Section 4.
5.4. IMU biases update

After the optimized scale and gravity are applied to state $\mathbf{S}$, we can calculate the initial IMU biases while fixing the pose variables $\langle \mathbf{wT}_0, \mathbf{wT}_1, \ldots, \mathbf{wT}_k \rangle$ in the optimization using Equation 22. The pre-integration factors for the local window keyframes are re-propagated using biases computed through initialization. At this point, the bootstrapping of the VIO is complete and online optimization is performed using the framework presented in Section 4.3.

6. Experiments

We used the EuRoC [10] dataset, which contains various challenging motions, to evaluate the quantitative performance of the proposed algorithm. The dataset was collected from a "Firefly" micro-aerial vehicle equipped with a stereo camera and inertial measurement at high flying speeds. We used only the left images with inertial sensor data. The sensor data in the EuRoC dataset were captured as a global shutter WVGA monochrome image at 20 fps and IMU data at 200 Hz. This dataset consists of five "Machine Hall" sequences and six "Vicon Room" sequences, which are labeled into easy, normal and difficult, depending on the motion speed and illumination environment changes. Both types of datasets measure the ground truth position from the Leica MS50 laser tracker and Vicon motion capture systems and are well calibrated to be used as benchmark datasets in various SLAM applications. We implemented the proposed system in C++ without GPU and was executed it on Intel Core i7 3.0G CPU laptops with 16GB RAM in real-time.

6.1. Comparison

We compared our proposed algorithm with recent state-of-the-art approaches using the same evaluation method as Delmerico and Scaramuzza [31], who evaluated the benchmark VIO performance in advance. They used the recommended parameter settings maintained in all tests of each algorithm and evaluated the RMSE position error over the align trajectory to ground truth pose via SE(3) [42]. Note that, because our proposed method is not a SLAM system, we conducted the comparison evaluation with algorithms that do not include loop closing. We directly compared the RMSE results with OKVIS [5], ROVIO [43], VINS-Mono [17], SVO+MSF [44,45] and SVO+GTSAM [46] using [31].

OKVIS is the open source VIO system that solves the visual re-projection errors for landmarks and IMU measurement with non-linear optimization they use a directly integration model without using the IMU pre-integration method. ROVIO is an EKF based VIO system to update pose state using multi-level patches around feature points with propagated IMU motion and minimization of photometric errors. VINS-Mono algorithm is similar to OKVIS with non-linear optimization based sliding window estimator, but uses the IMU pre-integration error term for relative pose between keyframes. In addition, the author proposed a loop closure using 4DOF pose graph optimization, but we compare it with the results without the module activated. SVO+MSF is an algorithm that combines Semi-Direct Visual Odometry (SVO) [44] which is quickly estimate frame pose based on...
Figure 10. Trajectory result of the proposed method and ground truth. Estimated trajectories are aligned to ground truth pose via $SE(3)$. The green line represents ground truth trajectory and the red dashed line is ours. For overall sequences, the proposed method estimates the accurate poses without any failure cases in tightly coupled optimization framework with a robust initialization method using relative pose constraints.

Visual patches and IMU measurement with EKF framework. Note that, this VIO system needs manual initialization using extra sensors. SVO+GTSM optimize structureless visual reprojection error with IMU pre-integration term performing full-smoothing factor graph optimization by [14]. These several methods differ from visual term (re-projection and photometric error), IMU term (IMU pre-integration and direct integration) and minimization method. Since the VIO system is a pose estimation method in continuous situations that does not involve re-localization, partial pose estimation failures can not be restored in extreme environments changes such as fast motion or dramatic illumination changes (V1 03 (difficult), V2 03 (difficult)).

Table 1 shows the RMSE of our proposed algorithm and the other VIO system results and estimated full trajectories of EoRoC are shown in Figure 10. We propose a robust algorithm that
Table 1. Average distance error on EuRoC dataset (unit: meters).

<table>
<thead>
<tr>
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<tbody>
<tr>
<td>MH 01 (easy)</td>
<td>0.14</td>
<td>0.14</td>
<td>0.16</td>
<td>0.21</td>
<td>0.27</td>
<td>0.05</td>
</tr>
<tr>
<td>MH 02 (easy)</td>
<td>0.13</td>
<td>0.20</td>
<td>0.22</td>
<td>0.25</td>
<td>0.12</td>
<td>0.03</td>
</tr>
<tr>
<td>MH 03 (medium)</td>
<td>0.20</td>
<td>0.48</td>
<td>0.24</td>
<td>0.25</td>
<td>0.13</td>
<td>0.12</td>
</tr>
<tr>
<td>MH 04 (difficult)</td>
<td>0.22</td>
<td>1.38</td>
<td>0.34</td>
<td>0.49</td>
<td>0.23</td>
<td>0.13</td>
</tr>
<tr>
<td>MH 05 (difficult)</td>
<td>0.20</td>
<td>0.51</td>
<td>0.47</td>
<td>0.52</td>
<td>0.35</td>
<td>0.16</td>
</tr>
<tr>
<td>V1 01 (easy)</td>
<td>0.05</td>
<td>0.40</td>
<td>0.09</td>
<td>0.10</td>
<td>0.07</td>
<td>0.07</td>
</tr>
<tr>
<td>V1 02 (medium)</td>
<td>0.07</td>
<td>0.63</td>
<td>0.20</td>
<td>0.10</td>
<td>0.10</td>
<td>0.11</td>
</tr>
<tr>
<td>V1 03 (difficult)</td>
<td>0.16</td>
<td>X</td>
<td>0.24</td>
<td>0.14</td>
<td>0.13</td>
<td>X</td>
</tr>
<tr>
<td>V2 01 (easy)</td>
<td>0.04</td>
<td>0.20</td>
<td>0.13</td>
<td>0.12</td>
<td>0.08</td>
<td>0.07</td>
</tr>
<tr>
<td>V2 02 (medium)</td>
<td>0.11</td>
<td>0.37</td>
<td>0.16</td>
<td>0.14</td>
<td>0.08</td>
<td>X</td>
</tr>
<tr>
<td>V2 03 (difficult)</td>
<td>0.17</td>
<td>X</td>
<td>0.29</td>
<td>0.14</td>
<td>0.21</td>
<td>X</td>
</tr>
<tr>
<td>Overall</td>
<td>0.13</td>
<td>0.23</td>
<td>0.22</td>
<td>0.16</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

works well with the same parameters for whole sequences without any failures. ROVIO, VINS and OKVIS operate robustly in all sequences, but get low accuracy at V2 03, which is difficult to robust initialization due to fast motion and MH 05 which contains night-time outdoor scene. SVO+GTSAM makes a challenging performance in the "Machine Hall" with far features with illumination changes, however it fails to estimate temporal poses on "Vicon Room" including fast motion (V1 03, V2 02-03). Our algorithm performs well in the MH 04-05 and V1-2 03 which are the most difficult dataset with dramatic illumination changes involving motion blur and darkness scene. Accurate scale and gravity initialization can reliably update the bias, and it is also possible to estimate exact pose in unstable feature tracking case through continuous scale updating. We make the best performance for overall without any failure cases in tightly coupled optimization framework with a robust initialization method using relative pose constraints. The most important aspect of the UAVs is to estimate the pose stably for the entire running without other extra sensors. The proposed method suited for this since it uses all the visual observation of the previous state by calculating the global metric scale and gravity while stably estimating the pose using visual information from the start.

7. Conclusions

In this paper, we propose a stable and accurate monocular visual inertial odometry system, which can be applied to UAVs in unknown environments. Even when we do not know the initial motion well, we optimize the relative motion with the IMU pre-integration factor to effectively solve the high non-linear problem and estimate reliable states by performing jointly optimization. We also estimate the local scale and update it into the marginalization to overcome the limitation of the sliding window approach where the observations are reduced. Further, We present that our proposed method makes stable and accurate results for EuRoC benchmark dataset experiencing various environmental changes.

The problem of state estimation of UAVs is a challenging research topic due to various environment changes that have not been unstructured before. Therefore, we are interested in studying the integration of additional sensors for stable operation of real unmanned environment system. Further, we are considering the dense map reconstruction from the reliable device pose estimated from various sensors. The high-density reconstructed environment can be applied to various applications such as obstacle detection, re-localization and 3D object tracking, which will make UAVs a more helpful application.
Author Contributions: E.H. implemented the system and write original draft preparation with validation. And J.L. conceived main methodology and supervise with editing the manuscript. All authors read and approved the final manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.


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