Article

Forecast horizon and Solar variability influences on the performances of Multiscale Hybrid Forecast Model (MHFM)

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Abstract: In this paper, the forecast horizon and solar variability influences on MHFM model based on multiscale decomposition, AR and NN models, are studied. This article follows the works published in [1] showing the performance of the MHFM using 3 multiscale decomposition methods and a forecast horizon equal to 1 hour. Several forecast horizon strategies and its influence on the MHFM performances are investigated. We show that the best strategy for a rRMSE varying from 4.43% to 10.24% is obtained for forecast horizons from 5 minutes to 6 hours. In a second part, the solar variability influence on the MHFM is studied. A classification based on a shows that the best performance of MHFM is obtained for clear sky days with a rRMSE of 2.91% and worst for cloudy sky days with a rRMSE of 6.73%.

Keywords: Hybrid Forecast Model; Forecast Horizon; Daily Global Solar Radiation Clustering; Fuzzy c-means; Variability Characterization

1. Introduction

The electrical output from solar resources is a major issue, particularly for island such as Guadeloupe Archipelago due to its non-interconnected electrical network. To improve the integration of this kind of energy in the electric network, in the proceeding work [1], a hybrid forecast model based on multiscale decomposition methods, AR and NN models is proposed. Three multiscale decomposition methods have been tested (Empirical Mode Decomposition EMD, Ensemble Empirical Mode Decomposition EEMD and Wavelet Decomposition WD). This previous study aimed to demonstrate the robustness and the efficient of the model and had been performed only for a 1h forecast horizon. Our objective here is to pursue this work evaluating the MHFM performances versus the forecast horizon strategy and the solar variability. Classically the forecast horizons can be divided in 3 categories [2] from 5 minutes to 2h intra-hour horizon, from 1h to 6h intra-day horizon and from 1 day to 3 days day-ahead horizon. Whatever the forecast models or the methods presented in the literature, the results are often established for several horizons and generally, the RMSE error increases with the horizon. This article makes an additional study by lingering over the way we determine the forecast horizon. Indeed, two strategies for the forecast horizon determination, are proposed. We show that following to the strategy adopted the results change. In addition, the solar variability influence on the model performances, is studied. For that, a classification of GHI measurements is proposed. Several classification techniques are devoted to global solar radiation data: Soubdhan et al. [3] used the k-means method on the clearness index PDF and found 4 classes, Badosa et al. [4] used the k-means algorithm to solar radiation classification based on 3 parameters (clearness index, Total Accumulated Relative Change and Total Relative Change) they found 5 classes. Soubdhan et al.[5] used the Dirichlet Distribution on the clearness index computed with Global solar radiation measured in Guadeloupe. They found 4 classes. Muselli et al.[6] applied Ward aggregation classification method...
on daily global irradiation on horizontal and tilted plane in Corsica and found 3 classes. Maafi and Harrouni[7] used fractal dimension and clearness index on 2 sites in Algeria and find 3 classes. Fuzzy c-means algorithm was recently used by Bennouiza et al [8] to hourly solar radiation classification. In this study, this Fuzzy C-Means (FCM) classification technique is used. FCM algorithm is a powerful tool which presents more precise results comparing with k-means algorithm [8,9]. It has been also chosen because it introduces the fuzziness for the belongingness of each object and can retain more information of the data set than the hard k-means clustering algorithm [10]. Fuzzy c-means algorithm was recently used by Bennouiza et al [8] to hourly solar radiation classification. Furthermore, to confirm the obtained classification a variability study based on metric of variability is given. Several studies and methods of variability characterization were carried out [11–16]. The paper is built as follows: section 2 describes the dataset considered and the data pre-processing, section 3 presents briefly the MHFM methodology (see [1] for a full description) and section 4 gives the metrics used to evaluate the MHFM performances. Section 5 describes the two strategies applied to determine the forecast horizon influence on the MHFM, the results obtained are presented in section 6. Then, the section 7 presents the FCM algorithm used to establish the influence of variability on the MHFM. Section 8 relates results of the daily classification, the study of the GHI variability according to the classes obtained and the GHI variability influence on the MHFM.

2. Data Set description

The global solar radiation \( GHI_{mes} \) data were measured at Petit-Canal (16°23' N latitude and 61°24' W longitude) located at Guadeloupe Island. The data are sampled at 1 second continuously during the year 2012 from January to December. Guadeloupe is subject to many passing clouds resulting in high variability of global solar radiation measured.

The original solar radiation series is not stationary, to perform the hybrid model a detrended time series must be used. Traditionally, the temporal trend is removed in \( GHI_{mes} \) considering clear sky index [17,18]. The detrended time series are obtained by clear sky index described by the following equation:

\[
K_c = \frac{GHI_m}{GHI_{clear}}
\]

where \( GHI \) is the Global Horizontal Irradiance, index \( m \) refers to the measured GHI index and \( clear \) refers to theoretical clear sky irradiance computed by the Kasten clear sky model[19].

3. Hybrid Forecast Model methodology

The hybrid model presented in [1] is based on a multiscale decomposition method. The hybrid model is performed to the Global solar radiation forecasting and its process is divided in several steps. We recall brief these steps :

- Step 1 : detrend the data estimating the clear sky index.(section 2)
- Step 2 : decompose the \( K_c \) signal using a multiscale decomposition method (Empirical Mode Decomposition, Ensemble Empirical Mode Decomposition or Wavelet Decomposition). The decomposition components obtained will be forecast separately using AR or NN model according to the time scale of component considered. Components with slow fluctuations (representing long time) scale are predict using the AR model and the components with fast fluctuations (representing short time scale) with the NN model [1].
- Step 3 : Forecast the short time scales components with a NN model and the long time scales components with a AR model. Each multiscale decomposition component was predicted.
- Step 4 : Summing all the component forecasting to obtain the predicted \( K_c \) time series.
- Step 5 : rebuild the Global solar radiation signal using the Kasten Clear sky model.
4. Evaluation of Forecast Performances

The Hybrid forecast model performance can be evaluated using the following classical statistical performance indicators

- **Relative Mean Bias Error (rMBE)**

\[ r_{MBE} = \frac{1}{N} \sum_{i=1}^{N} \hat{p}_i - o_i \]  

- **Relative Mean Absolute Error (rMAE)**

\[ r_{MAE} = \frac{1}{N} \sum_{i=1}^{N} |\hat{p}_i - o_i| \]  

- **Relative Root Mean Square Error (rRMSE)**

\[ r_{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (\hat{p}_i - o_i)^2} \]  

where \( o_i \) is the observed value of GHI and \( \hat{p}_i \) is the forecast value of GHI and \( N \) the number of point in the dataset for the considered period.

- **Skill \( s \)**: compare the model performance with a reference model [20]. In this study we compare the proposed model with the persistence model applying the skill parameter proposed by Coimbra et al.[21]:

\[ s = (1 - \frac{RMSE_{model}}{RMSE_{SC_{pers}}}) \times 100 \]  

where index \( SC_{pers} \) refers to the scaled persistence reference model define by Eq. 6.

\[ K_c(t + h) = K_c(t) \]  

The corresponding GHI forecast is obtained using Eq. 7:

\[ \hat{GHI}(t + h) = GHI(t) \times \frac{GHI_{clear}(t + h)}{GHI_{clear}(t)} \]  

5. Forecast horizon Influence on Hybrid Forecast Model Performances

In [1] the MHFM performances are studied only for a forecast horizon corresponding to \( \tau = 1 \) hour. In this work, the forecast horizon influence on the propose hybrid model, is studied. According to categorization given in [2] we focus on intra-hour and intra-day forecast horizons i.e. from 5 minutes to 6 hours. Two strategies based on the data rich in order to evaluated the MHFM performances, are implemented.

5.1. Strategy 1 : sampling data \( T_r = \text{forecast horizon} \ \tau \)

The first strategy consists to resampling the data in order to time sampling \( T_r \) equal to the time horizon \( \tau \). In this case the model predicts directly the next point. Classically, this strategy is used in the solar forecasting field. Figure 1 illustrates the MHFM flowchart including the resampling step before the multiscale decomposition step. Figure 2 briefly illustrates the individual components forecasting process for example, \( T_r = \tau = 1 \) hour. This strategy is operated as follows for each decomposition components after resampling the data set with time sampling \( T_r = \tau \):

- To determine during the AR and NN learning phase, the number of input data selected with the AIC and BIC criterion for the AR model and the mutual information for the NN model [1,18]. The learning phase concerns the half of dataset, i.e 6 months.
MHFM flowchart adapted to the strategy 1, the fuchsia case indicates the step added.

Figure 1

- To provide a forecasting at $t + \tau$ of 6 months data test (different from data of learning phase) according to this strategy it consists in predicting the next point.
- To repeat the process for each $\tau$ value.

5.2. Strategy 2: sampling data $T_r \neq$ forecast horizon $\tau$

In the second strategy, the time sampling is different to the time horizon ($T_r \neq \tau$). Generally, in statistics, the quantity of data can be of great importance, for representative results. This can be considered, in part, having a long period of measurements or in other part, having data with high frequency sampling. The goal, here, is to verify data rich on the MHFM performances; intuitively, we could think that the kind of data (with high frequency sampling) may cause an impact to the model performance. The second strategy consists to verify this assumption. Unlike the first strategy there is no additional step, the data sampling $T_r = 5$ minutes is the same for all the considered forecast horizon $\tau$. Figure 3 illustrates the MHFM flowchart with the second strategy and Figure 4 briefly represent an example of the individual components forecasting phase for a $\tau = 1$ hour. This strategy is operated as follows for each decomposition components:
AR and NN diagram used in the strategy 1: example for $T_r = \tau = 1h$

Figure 2

- To select the number of input data determined with the AIC and BIC criterion for the AR model and the mutual information for the NN model [1,18] using 6 months data set with sampling time $T_r = 5$ minutes. The number of input found will be valid for all the considered forecast horizon $\tau$.
- To provide a forecasting at $t + \tau$ of 6 months data test, the data test sampling time is also 5 minutes and the model allows us to obtain every 5 minutes the forecast at $t + \tau$.

In summary, this approach performs the AR and NN learning phase with 5 minutes data sampling and provides a forecasting at $t + \tau$, with the time horizon $5 \leq \tau \leq 360$ min (6h).

6. Results-Discussion

In this section, the results obtained for each strategy proposed in the preceding section, are presented. Considering the two strategies set out in order to obtain forecasts for several horizons, we apply decomposition methods on data with different sampling. In the strategy 1 the sampling time is equal to the forecast horizon, for example, for a horizon of 5 minutes, data sampled at 5 minutes are used and for a horizon of 2 hours, data are sampled at 2 hours. The initial dataset is sampled at 1 second. Moreover the time horizon is longer the smaller the dataset. This will reduce the number of decomposition components. Indeed the longer the dataset is, the greater the number of components of the decomposition. In the EMD case the number $N$ of intrinsic mode functions (IMF) is proportional to the length of the data set [22]:

$$N = \frac{T}{n\Delta t} \quad (8)$$

where $T$ represents the total data length, $\Delta t$ represents the digitizing rate and $n$ represents the minimum number of $\Delta t$ needed to define the frequency accurately.

In this work, time horizons of 5, 10, 15, 30 minutes, 1h, 2h, 4h and 6h, are tested.

6.1. Results: Strategy 1: Sampling Data = Forecast Horizon

Table 1 shows the Hybrid model forecasting performances using the first strategy. We can note that whatever the Multiscale decomposition-hybrid model chosen the rRMSE error increases with the forecast horizon as illustrated in Figure 5. This increase is nonlinear and seems follow a logarithmic tendency. As shown in [1], the best results are obtained with the WD-Hybrid model (rRMSE varying between 4.41% and 11.42%). The skill parameters which allow to compare the hybrid model performances to the persistence model varying between 78.58% and 85.54%, highlighting the best performances of proposed model (comparatively to the persistence model), for all the forecast horizons.
Hybrid model flowchart adapted to the strategy 2, the fuchsia case indicate the Step undergoing a modification

Figure 3

AR and NN flowchart used in the strategy 2 predicting directly the considered forecast horizon

Figure 4
Table 1. The MHFM performances according to the Forecasting Horizon (Strategy 1).

<table>
<thead>
<tr>
<th>Models</th>
<th>Forecast Horizon</th>
<th>5 min</th>
<th>10 min</th>
<th>15 min</th>
<th>30 min</th>
<th>1h</th>
<th>2h</th>
<th>4h</th>
<th>6h</th>
</tr>
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<tbody>
<tr>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>EMD-Hybrid Model</td>
<td>rMBE (%)</td>
<td>0.17</td>
<td>-0.25</td>
<td>0.23</td>
<td>0.12</td>
<td>-0.32</td>
<td>1.36</td>
<td>1.03</td>
<td>1.99</td>
</tr>
<tr>
<td></td>
<td>rMAE (%)</td>
<td>7.42</td>
<td>7.73</td>
<td>8.30</td>
<td>8.54</td>
<td>11.43</td>
<td>9.00</td>
<td>9.87</td>
<td>13.16</td>
</tr>
<tr>
<td></td>
<td>rRMSE (%)</td>
<td>11.49</td>
<td>11.38</td>
<td>12.24</td>
<td>12.54</td>
<td>16.03</td>
<td>12.91</td>
<td>15.32</td>
<td>20.93</td>
</tr>
<tr>
<td></td>
<td>Skill (%)</td>
<td>44.54</td>
<td>50.22</td>
<td>46.82</td>
<td>51.43</td>
<td>56.30</td>
<td>77.24</td>
<td>79.43</td>
<td>70.45</td>
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<td>rMBE (%)</td>
<td>-0.02</td>
<td>-0.12</td>
<td>-0.27</td>
<td>0.25</td>
<td>-0.60</td>
<td>0.23</td>
<td>0.63</td>
<td>0.12</td>
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<td>8.20</td>
<td>8.56</td>
<td>8.45</td>
</tr>
<tr>
<td></td>
<td>Skill (%)</td>
<td>58.83</td>
<td>59.72</td>
<td>57.10</td>
<td>59.21</td>
<td>61.45</td>
<td>78.15</td>
<td>83.31</td>
<td>81.91</td>
</tr>
<tr>
<td>WD-Hybrid Model</td>
<td>rMBE (%)</td>
<td>0.12</td>
<td>0.01</td>
<td>-0.04</td>
<td>0.11</td>
<td>0.074</td>
<td>0.38</td>
<td>0.29</td>
<td>0.42</td>
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<tr>
<td></td>
<td>rMAE (%)</td>
<td>2.84</td>
<td>3.02</td>
<td>3.04</td>
<td>3.62</td>
<td>4.17</td>
<td>6.11</td>
<td>8.14</td>
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<tr>
<td></td>
<td>rRMSE (%)</td>
<td>4.43</td>
<td>4.41</td>
<td>3.04</td>
<td>5.27</td>
<td>6.42</td>
<td>8.82</td>
<td>11.42</td>
<td>10.24</td>
</tr>
<tr>
<td></td>
<td>Skill (%)</td>
<td>78.58</td>
<td>80.69</td>
<td>80.73</td>
<td>79.57</td>
<td>82.50</td>
<td>84.45</td>
<td>85.18</td>
<td>85.54</td>
</tr>
</tbody>
</table>

Figure 5. Strategy 1 RMSE error (dotted line) and an attempt of modeling by a logarithmic regression (solid line); in the logarithmic regression equation $y$ refers to the RMSE and $x$ refers to the forecast horizon $\tau$.

6.2. Results: Strategy 2: Sampling Data $T_{r} \neq$ Forecast Horizon $\tau$

We have seen that the previous strategy added an additional stage in the hybrid model process for each horizon considered. The objective of the second strategy is to verify if the hybrid model forecast performances are also good by using data high frequency sampling ($T_{r} = 5$ minutes for all the horizons). This approach uses 5 minutes data sampling to forecast the GHI at several horizon $\tau$. The AR and NN model learning phase perform with 5 minutes data sampling and the forecast is directly obtained every 5 minutes at $t + \tau$. With this approach we remark that the WD-Hybrid Model obtain the best results (rRMSE varying from 4.43% to 22.33% and skill parameter varying from 78.58% to −7.81%). Figure 6 represents the rRMSE versus the forecast horizon compared to the associated logarithmic regression. We had make the assumption that enrich the learning data set would improve the model performance but the WD-hybrid model errors obtained using the second strategy are higher than those obtained by the first strategy. Finally, To verify if the hybrid model become more complexe with the strategy 2 we use it with a sampling data varying from 5 to 15 minutes. This complexity would arise from the fact that it is supplied with data high frequency sampling data whatever the chosen horizon. Figure 7 represents the rRMSE versus the forecast horizon for different data sampling and shows that the learning data set sampling has an influence on the hybrid model performances and suggests that the first strategy is the more efficient. Indeed, High frequency data doesn’t seem

Figure 6: Logarithmic regression equation $y = 0.11\ln(x) + 2.38$, $y = 0.10\ln(x) + 2.18$, $y = 0.24\ln(x) + 1.33$.
improve the MHFM performances. These lower performances are certainly due to the fact that we impose the model to predict phenomena observed at small scale (via decomposition components) while these ones are not observable on the chosen time horizon. Use data sampling close or equal to the time horizon (strategy 1) allows to consider only the observable phenomenon for this horizon and thus to obtain better results.

Table 2. Forecasting performance of the Hybrid model according to the Forecasting Horizon with a data sampling = 5min (Strategy 2)

<table>
<thead>
<tr>
<th>Models</th>
<th>Forecast Horizon</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>5 min</td>
<td>10 min</td>
<td>15 min</td>
<td>30 min</td>
<td>1h</td>
<td>2h</td>
<td>4h</td>
<td>6h</td>
</tr>
<tr>
<td>EMD-Hybrid Model</td>
<td>rMBE (%)</td>
<td>0.17</td>
<td>0.013</td>
<td>0.07</td>
<td>-0.33</td>
<td>0.48</td>
<td>-0.14</td>
<td>1.36</td>
</tr>
<tr>
<td></td>
<td>rMAE (%)</td>
<td>7.12</td>
<td>9.39</td>
<td>10.12</td>
<td>11.52</td>
<td>13.51</td>
<td>15.66</td>
<td>17.61</td>
</tr>
<tr>
<td></td>
<td>rRMSE (%)</td>
<td>11.49</td>
<td>14.30</td>
<td>15.53</td>
<td>17.65</td>
<td>20.30</td>
<td>22.95</td>
<td>25.74</td>
</tr>
<tr>
<td></td>
<td>Skill (%)</td>
<td>44.54</td>
<td>30.85</td>
<td>24.91</td>
<td>14.68</td>
<td>1.86</td>
<td>-10.95</td>
<td>-24.29</td>
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<tr>
<td>EEMD-Hybrid Model</td>
<td>rMBE (%)</td>
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<td>-0.38</td>
<td>-0.53</td>
<td>0.31</td>
<td>-1.15</td>
<td>-0.49</td>
<td>0.27</td>
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<tr>
<td></td>
<td>rMAE (%)</td>
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<td>7.59</td>
<td>8.20</td>
<td>9.92</td>
<td>11.78</td>
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<tr>
<td></td>
<td>rRMSE (%)</td>
<td>8.53</td>
<td>12.38</td>
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<td>18.10</td>
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<tr>
<td></td>
<td>Skill (%)</td>
<td>58.83</td>
<td>40.16</td>
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<tr>
<td>WD-Hybrid Model</td>
<td>rMBE (%)</td>
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<td>0.24</td>
<td>-0.22</td>
<td>0.17</td>
<td>0.26</td>
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<tr>
<td></td>
<td>rMAE (%)</td>
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<tr>
<td></td>
<td>rRMSE (%)</td>
<td>4.43</td>
<td>6.95</td>
<td>8.49</td>
<td>14.02</td>
<td>16.30</td>
<td>18.36</td>
<td>21.46</td>
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<tr>
<td></td>
<td>Skill (%)</td>
<td>78.58</td>
<td>66.38</td>
<td>58.98</td>
<td>32.20</td>
<td>21.20</td>
<td>11.24</td>
<td>-3.67</td>
</tr>
</tbody>
</table>

Afterward, we decide to study the influence of another parameter on the MHFM performances. Guadeloupe island is located in the intertropical zone and is subject to many passing clouds, what entails a GHI high variability. In the following section, we study the influence of the GHI variability on the MHFM performances through a classification of the type of days.

7. Solar variability Influence on MHFM performances

7.1. Clearness index

To evaluate the solar variability influence on the performances of the MHFM, a classification of daily Solar is proposed. Each defined day class allows to highlight a type of variability. To perform the classification, the clearness index noted \( K_t \) is used. This parameter removes the effect of daily solar trend and normalizes variability to unity. The clearness index \( K_t \) usually employed for solar radiation clustering [3–5,23].

Figure 6. Strategy 2 rRMSE error (dotted line) and their logarithmic regression (solid line), in the logarithmic regression equation \( y \) refers to the RMSE and \( x \) refers to the forecast horizon \( \tau \)
Figure 7. WD-Hybrid model rRMSE over the forecast horizon for different data sampling

\[ K_t = \frac{GHI_{mes}}{GHI_{extra}} \]  

(9)

Where \( GHI_{mes} \) refers to measured global solar radiation and \( GHI_{extra} \) refers to extraterrestrial radiation estimated according to the Kasten model [19,24]. We notice that the values of \( K_t \) are bounded between 0 and 1. This characteristic allows a uniform classification of all daily sequences of data.

Figure 8. (a) 7 days GHI data and the corresponding theoretical extraterrestrial model (GHI\(_{extra}\)). (b) \( K_t \) signal obtained

7.2. Fuzzy-C means clustering algorithm

The Fuzzy C-means clustering is an iterative method to classify individuals (or samples) in \( C \) classes. It was introduced by Ruspini [25], and later extended by Dunn and Bezdek [26,27]. It determines the centers of the classes and generates the matrix to estimate the membership of individuals, to one of the predefined classes. The main purpose of this method is to minimize a cost function, which is usually chosen to be the total distance between each sample to the center of each class [27,28].

\[ J(U, V) = \sum_{k=0}^{n} \sum_{i=1}^{C} \mu_{ik}^m ||x_{ik} - v_i|| \]  

(10)

With \( n \) the total number of samples, \( C \) is the predefined number of classes, \( x_k \) is the vector representing the \( k^{th} \) individual, \( v_i \) is the vector representing the center of the \( i^{th} \) class and \( \mu_{ik} \) is the degree of membership of the \( k^{th} \) individual in the \( i^{th} \) class. The matrix \( U \) contains the coefficients \( \mu_{ik} \).
V is the matrix containing the center of the C classes \( v_i \) and \( m \) is a constant greater than 1 (generally \( m = 2 \)). By differentiating the function \( J(U, V) \) according to \( v_i \), keeping \( U \) constant and according to \( \mu_{ik} \), keeping \( V \) constant, the following equations are obtained [27]:

\[
\mu_{ik} = \frac{1}{\prod_j \sum_c \left( \frac{\|x_k - v_j\|}{\|x_k - v_i\|} \right)^{(m-1)}} \quad (11)
\]

\[
V_i = \frac{\sum_j (\mu_{ik})^m x_k}{\sum_j (\mu_{ik})^m} \quad (12)
\]

In Eq.10 and Eq.11 the symbol \( \| . \| \) represent the Euclidian distance.

Figure 9. Fuzzy-C-means algorithm flowchart

Validity Criterion

We use a validity criterion to determine the optimal numbers of classes and "fuzzy factor value". It was defined as a fuzzy clustering validity function noted \( S \), which measures the overall average and the separation of a fuzzy-C partition [29]. \( S \) can be explicitly written as :

\[
S = \frac{\sum_i \sum_j (\mu_{ij})^m \|V_i - X_j\|^2}{n * (d_{min})^2} \quad (13)
\]

where \( d_{min} \) represents the minimum euclidian distance between cluster centroids i.e:

\[
d_{min} = \min_{i,j} \|V_i - V_j\| \quad (14)
\]

The class number (or "fuzzy factor value") is optimal for the smallest value of \( S \).
8. Results-Discussion

In this section, we present the results of the fuzzy-c means clustering, then we perform a variability analysis for each identified class of days and finally we determine the MHFM performances for each class of days.

8.1. Daily solar radiation classification results

In this study, the classification method is applied to 366 days of Global solar radiation sampled at 5 minutes. The clearness index $K_t$ defines in Eq. 9 is computed for each day in order to estimate the $K_t$ histograms. These histograms are considered as the fuzzy c-means algorithm inputs. The fuzzy C means clustering algorithm was tested for several numbers of classes $C = 2, 3, 4, 5, 6$. The validation criterion, given in Eq. 13, allows to define that the optimum number of classes is 4: the $S$ value corresponding to each number of cluster, is drawn up in Table 3. Soubdhan et al. [5] also made a classification of the GHI measured in Guadeloupe. This classification method permitted to classify the $K_t$ histograms using a Dirichlet Mixture PDF. Our results have highlighted 4 classes, in agreement with those obtained by Soubdhan et al. in [5].

<table>
<thead>
<tr>
<th>Number of Cluster</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Validity Criteria $S$</td>
<td>0.43</td>
<td>0.37</td>
<td><strong>0.33</strong></td>
<td>0.51</td>
<td>0.57</td>
</tr>
</tbody>
</table>

The 4 classes obtained are clear sky day, intermittent clear sky day, cloudy sky day and intermittent cloudy sky day.

<table>
<thead>
<tr>
<th>Table 4. Allocation of days according to their classes in 2012</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clear Sky</td>
</tr>
<tr>
<td>Number of day</td>
</tr>
<tr>
<td>In percentage</td>
</tr>
</tbody>
</table>

![Figure 10]( figure)

Figure 10. Class representing clear sky day event: a) Clearness index of 109 clear sky days b) Average $K_t$ histogram of the 109 clear sky days c) a clear sky day GHI example

- Clear sky day (CS)

In 2012 clear sky day events represent 29% GHI days of the year (Table 4). This type of day have
Figure 11. Class representing Intermittent clear sky day event: a) Clearness index of 84 intermittent clear sky days b) Average $K_t$ histogram of the 84 intermittent clear sky days c) a intermittent clear sky day GHI example.

Figure 12. Class representing cloudy sky day event: a) Clearness index of 62 cloudy sky days b) Average $K_t$ histogram of the 62 cloudy sky days c) a cloudy sky day GHI example.

very few cloudy passages (Figure 10.c). The clear sky day $K_t$ distribution having a maximum of occurrence value (44%) around $K_t = 0.8$ (Figure 10.a). Figure 10.b show that around 86% of $K_t$ values $\in [0.5; 1]$.

• Intermittent clear sky day (ICS)

This second class represent 24% of events (Table 4). This type of day have an important solar radiation but the cloudy passages are frequent (Figure 11.c). The $K_t$ distribution having a maximum occurrence value (47%) around $K_t = 0.7$ and around 80% of $K_t$ values $\in [0.5; 1]$ (Figure 11.b).

• Cloudy Sky day (CLS)

The cloudy sky day have important slow cloudy passages (Figure 12.c). This is the class is the least represented with 17% of the 2012 year days (Table 4). The $K_t$ distribution having a maximum occurrence (20%) around $K_t = 0.3$ and around 73% of $K_t$ values $\in [0; 0.5]$ (Figure 12.b).

• Intermittent cloudy sky day (ICS)

For an intermittent cloudy sky day, important cloudy passages are observed (Figure 13.c). In this class we have 111 days or 30% of the 2012 year (Table 4). The $K_t$ distribution having a maximum occurrence (25%) around $K_t = 0.7$ and around 63% of $K_t$ values $\in [0.5; 1]$ (Figure 13.b).
In the next section we study the global solar radiation variability. We analyse the fluctuation behavior at different time scale using the Validity Score (VS) parameter [15]. This parameter is based on the amplitude of fluctuations.

8.2. Variability characterization

The objective is to study the amplitude of fluctuations for different timescales to characterize the dynamic of each class of days. To achieve this we used the variability score. Lave et al.[15] define the variability score as the maximum value of ramp rate magnitude \( RR_0 \) times ramp rate probability (Eq.15). The variability score is determined using the cumulative distribution function of ramp rates using a given timescale [16].

\[
VS(\Delta t) = 100 \times \max(RR_0, P(|RR_{\Delta t}| > RR_0))
\]

where \( \Delta t \) represents the time scale, \( RR_0 \) and \( RR_{\Delta t} \) are a percent of Standard Test Conditions (STC) irradiance = 1000W.m\(^{-2}\). The probability \( P(|RR_{\Delta t}| > RR_0) \) represents the fraction of time where the absolute value of \( RR_{\Delta t} \) is higher than \( RR_0 \). Like in [15] we choose to use the moving averages definition of ramp rates \( RR_{\Delta t} \) given by Kleissl [30]:

\[
RR_{\Delta t}(t) = \frac{1}{\Delta t} \left( \sum_{t}^{t+\Delta t} GHI - \sum_{t-\Delta t}^{t} GHI \right)
\]

Firstly we present in Figure. 14 the \( \Delta t \)-cumulative distribution of GHI ramp rate for each class. These figures allow to have an information on the amplitude of the fluctuations and their probability for each type of days. In Figure. 14.a) we can see that 35% of ramp rates for the clear sky days were larger than 50W.m\(^{-2}\). This probability achieve 40% for the intermittent clear sky days, 50% for the cloudy sky days and 55% for the intermittent cloudy sky days. When we increases \( \Delta t \) the probability to be larger than 50W.m\(^{-2}\) increase too (Figure. 14.b, Figure. 14.c and Figure. 14.d). We also noticed that when \( \Delta t \) increase the behavior of the Cloudy Sky cumulative distribution of GHI ramp rate change, its achieve the lowest probability to have an amplitude of fluctuations higher than 50W.m\(^{-2}\) when \( \Delta t \) = 20 min. That means the cloudy sky days have a low dynamic. Whatever the observed amplitude of fluctuations, the intermittent cloudy sky days always have the highest probability to be higher than \( RR_0 \). For \( \Delta t \) = 15 and 20 min, when \( RR_0 \) reach 25% of STC (250W.m\(^{-2}\)), the cloudy sky day and intermittent cloudy sky days cumulative distribution (respectively clear sky days and intermittent clear sky days cumulative distribution) eventually have the same behavior.
Then we present the Variability Score over timescale $\Delta t$ (Figure 15). We show that for each class VS increase over $\Delta t$. The intermittent cloudy sky days is the most variable and the clear sky day the less variable. In [15] Lave et al. made the same observation. They determine the VS over $\Delta t$ for 10 sites in USA, chose to considerate $\Delta t= 1$s, 10s, 30s, 60s and 3600s and demonstrate that VS increase over $\Delta t$.

This variability characterization will have allowed to approve the robustness of the clustering method. Indeed, we found 4 type of days with 4 different variability whether in term of amplitude of the fluctuations that of dynamics of day. In the next section we presents the MHFM performances according to the type of days.

8.3. Variability influence on Hybrid forecast model performances

We applied the first strategy presented in section 5-1. We used 6 months the data available for the learning phase of the hybrid model then predicted 6 other months. The errors were calculated for every day predicted independently. Then, through the classification made beforehand we grouped the
days of the same class and established an average of the error obtained. These errors are summarized in Table 5 for a forecast horizon of 5 minutes. The best performances are obtained with the WD-Hybrid model. The clear sky days are the best predicted ($rRMSE = 2.91\%$), their low variability facilitate their forecast by the model. We note in the previous section that the most variable days is the intermittent cloudy sky days but the MHFM performances for this type of days ($rRMSE = 5.48\%$) is better than this obtained for cloudy sky days ($rRMSE = 6.73\%$). The variability of GHI signal is not the only factor being able to influence the forecast error. The cloudy sky days is the second type of days the most variable and the only type of days which have a very low GHI (generally $< 600 W.m^{-2}$). Moreover, the cloudy sky day $rMBE$ obtained with the WD-Hybrid Model is the highest ($rMBE = 0.32\%$). The 3 others type of day being the most represented (Table 4), during NN and AR the learning phase the hybrid model rarely meet the cloudy sky days GHI signal and finally overestimate their forecasts. All these observations show that it is the combination of high variability and low GHI value which could justify the least good performances of the model on the cloudy sky days class. Nevertheless, the robustness of MHFM allows to limit their effects on the quality of the forecast to obtain a rRMSE lower than 7%.

**Table 5.** Forecasting performances of MHFM for the 4 specific class of days

<table>
<thead>
<tr>
<th></th>
<th>EMD-Hybrid Model</th>
<th>EEMD-Hybrid Model</th>
<th>WD-Hybrid Model</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Clear Sky</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$rMBE$ (%)</td>
<td>0.21</td>
<td>-0.20</td>
<td>0.02</td>
</tr>
<tr>
<td>$rMAE$ (%)</td>
<td>5.14</td>
<td>3.70</td>
<td>2.00</td>
</tr>
<tr>
<td>$rRMSE$ (%)</td>
<td>7.47</td>
<td>5.84</td>
<td>2.91</td>
</tr>
<tr>
<td><strong>Intermittent Clear Sky</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$rMBE$ (%)</td>
<td>0.07</td>
<td>-0.51</td>
<td>0.08</td>
</tr>
<tr>
<td>$rMAE$ (%)</td>
<td>6.00</td>
<td>4.39</td>
<td>2.35</td>
</tr>
<tr>
<td>$rRMSE$ (%)</td>
<td>8.76</td>
<td>6.95</td>
<td>3.35</td>
</tr>
<tr>
<td><strong>Cloudy Sky</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$rMBE$ (%)</td>
<td>0.11</td>
<td>-0.21</td>
<td>0.32</td>
</tr>
<tr>
<td>$rMAE$ (%)</td>
<td>10.14</td>
<td>7.71</td>
<td>4.72</td>
</tr>
<tr>
<td>$rRMSE$ (%)</td>
<td>14.81</td>
<td>11.76</td>
<td>6.73</td>
</tr>
<tr>
<td><strong>Intermittent Cloudy Sky</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$rMBE$ (%)</td>
<td>0.15</td>
<td>-0.19</td>
<td>0.17</td>
</tr>
<tr>
<td>$rMAE$ (%)</td>
<td>9.32</td>
<td>7.42</td>
<td>3.81</td>
</tr>
<tr>
<td>$rRMSE$ (%)</td>
<td>13.36</td>
<td>11.16</td>
<td>5.48</td>
</tr>
</tbody>
</table>

**9. Conclusion**

The goal of this study concerns the influence of time sampling combined to the forecast horizon and the solar variability on the hybrid forecast model performances. Two strategies for the forecast at several horizon are proposed, the first based on the resampling data in order that the data sampling equal to the forecast horizon and the second on order that all the horizon are obtained with the same data sampling (5 minutes). Like in [1] we tested the hybrid model for 3 multiscale decomposition methods (EMD, EEMD and WD). With the first strategy, whatever the Multiscale decomposition-hybrid model chosen the rRMSE error increases with the forecast horizon and the best results are obtained with the WD-Hybrid model (rRMSE varying between 4.41% and 11.42 %). With the second strategy the AR and NN learning phase performs with 5 minutes data sampling and provides a forecasting at $t + \tau$. The rRMSE error increases with the forecast horizon and the WD-Hybrid Model obtain a rRMSE varying from 4.43% to 22.33%. Like demonstrated by Monjoly et al. in [1] the best results are obtained with the WD-Hybrid model. The forecast horizon strategy based on the resampling data (first strategy) is the most efficient. Solar variability influence are determined using a daily classification of the GHI based on clearness index and fuzzy c-means algorithms. We obtain 4 classes according to previous studies : clear sky day, intermittent clear sky day, cloudy sky and intermittent cloudy sky. Then we describe the variability characterization of each class based on the variability score : as expected, the intermittent cloudy sky days is the most variable and the clear sky day the less variable for exemple 35% of ramp rates for the clear sky days were larger than $50 W.m^{-2}$. This
probability achieve 40% for the intermittent clear sky days, 50% for the cloudy sky days and 55% for the intermittent cloudy sky days. Nevertheless the hybrid forecast performances obtained with the most variable class (Intermittent cloudy sky) aren’t the worst this reveals the weakness of the hybrid model for these cases qualified to extreme events. Consequently, in future works, the hybrid model should be improve in this way.. We note that the variability of GHI signal is not the only parameter being able to influence the forecast, the daily GHI profile is an other one. Indeed, the cloudy sky day is the only class with a low GHI profile, its the second class the most variable and it’s the type of day having the highest rRMSE (6.73%).

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**Sample Availability:** Samples of the compounds ...... are available from the authors.