

1 Numerical Validation of Floating Offshore Wind 2 Turbine Scaled Rotor for Surge Motion

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12
13 **Abstract:** Aerodynamic performance of a floating offshore wind turbine (FOWT) is significantly
14 influenced by platform surging motions. Accurate prediction of the unsteady aerodynamic loads is
15 imperative for determining the fatigue life, ultimate loads on key components such as FOWT rotor
16 blades, gearbox and power converter. The current study examines the predictions of numerical
17 codes by comparing with unsteady experimental results of a scaled floating wind turbine rotor. The
18 influence of platform surge amplitude together with the tip speed ratio on the unsteady
19 aerodynamic loading has been simulated through unsteady CFD. It is shown that the unsteady
20 aerodynamic loads of FOWT are highly sensitive to the changes in frequency and amplitude of the
21 platform motion. Also, the surging motion significantly influences the windmill operating state
22 due to strong flow interaction between the rotating blades and generated blade-tip vortices. Almost
23 in all frequencies and amplitudes, CFD, LR-BEM and LR-uBEM predictions of mean thrust shows a
24 good correlation with experimental results.

25 **Keywords:** CFD, unsteady BEM, Floating Offshore Wind Turbine, Scaled Wind Turbine Rotor
26

27 1. Introduction

28 This paper is an extension and continuation of the earlier work that has been presented in 2018
29 2nd International Conference on Green Energy and Applications of IEEE (ICGEA) [1]. The insatiable
30 demand for the energy and the rising greenhouse gas emissions push the energy sector towards
31 renewable energy. Among the various renewable energy sources, wind energy is one popular form
32 of energy due to its reliability and cost competitiveness. The wind industry has seen a tremendous
33 growth in the past decades [2] leading to the addition of 52.6 GW of power to an existing 539 GW as
34 of 2017. To meet the projected energy demand, the wind industries are pushed to explore
35 technologies beyond conventional land-based installations. Offshore wind turbine is one of the
36 identified potential solutions with significant annual energy output due to high wind speed.

37 Offshore wind technologies are continuously improved by myriad experimental, numerical
38 and field studies. As the water depth increases, the conventional monopile foundation or
39 gravity-based foundation are not economically lucrative. Hence floating wind turbines are proposed
40 as an alternative solution in terms of cost and reliability [3]. Floating wind turbines are an active
41 research topic in recent days with innovative concepts to curtail the installation and maintenance
42 cost. A few concepts have been implemented in prototype turbines in deep waters to demonstrate
43 the feasibility of the concept.

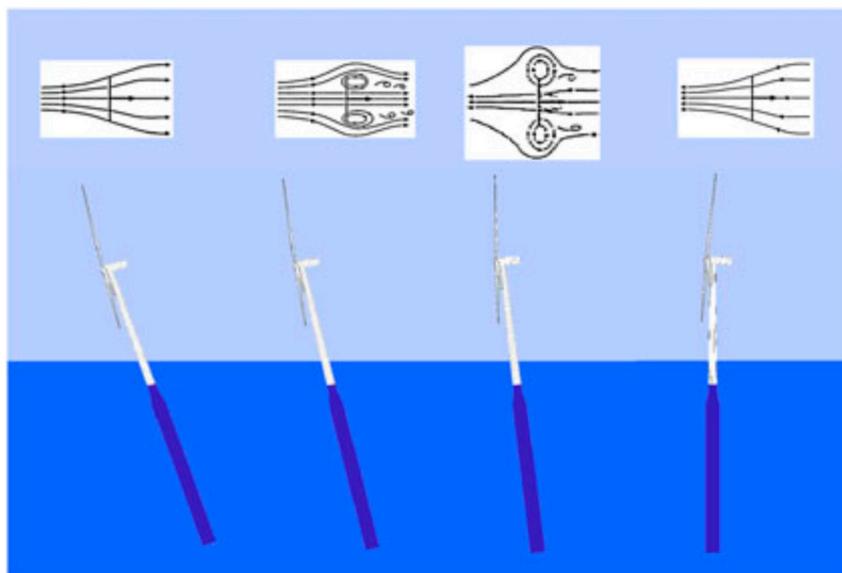
44 The floating offshore wind turbine's capital, Operation and Maintenance (O&M) cost should be
45 significantly reduced in order to be competitive with the fixed bottom wind machines and
46 conventional power sources. Apart from the design considerations of offshore environment, floating
47 offshore wind turbine technology is impaired with other challenges such as application of right

48 floating platform technology and increased O&M cost due to the accessibility of the assets in deep
49 waters. Hence the offshore wind turbines are expected to have improved reliability and should be
50 able to withstand high wind loads to reduce the maintenance cost. Accurate prediction of various
51 forces and combined loading are the important aspects of floating offshore wind turbine systems
52 design.

53 Numerical simulations play important role in every stage of the wind turbine product life
54 cycle development from conceptual design to operation, maintenance and decommissioning to
55 optimize CAPEX and OPEX(O&M). In addition to their significant contribution in predicting the
56 wind loads on the turbine, numerical simulations also help to develop radically new designs. During
57 the design review, compliance and certification process, thousands of simulations are normally
58 performed. Hence, the typical engineering analytic code like NREL FAST, is often used to assess the
59 performance behaviors of the turbine. To compute aerodynamics loads, AeroDyn sub module is
60 integrated with FAST modular framework. Blade Element Momentum (BEM) and Generalized
61 Wake Dynamic (GDW) methods are implemented in AeroDyn.

62 Wind turbine industry has adopted various mathematical models to compute the aerodynamic
63 loads on the onshore turbine rotor. Among the prescribed or free-wake vortex method, acceleration
64 potential method, NREL FAST with AeroDyn sub module, BEM model is preferred for their low
65 computational requirements and well understood [4]. Albeit, the BEM codes include corrections for
66 wake expansion, the pressure due to wake rotation and improved accuracy by accounting for the
67 losses at blade root and tip sections, they are developed for wind turbines with static foundations.
68 Hence the assumptions in BEM are not applicable [5] for floating offshore turbines where the
69 pitching and surging motions [6] of the platform leads to the turbine rotor going through different
70 wake states as shown in Fig 1. Various non-linear effects like rotor-wake interactions, wake-wake
71 interactions, wake meandering etc., are not accounted in BEM theory.

72
73



74

75 **Figure 1** Hypothetical floating wind turbine motions [1]

76 Lloyds Register (LR) has been actively involved in the development of numerical models and
77 experimental modelling. Experiments on scaled rotor provides an insight on the aerodynamic
78 loading of the rotor and to validate the non-linear models. As platform motions of FOWT has greater
79 influence on the unsteady aerodynamic response, a scaled model of the rotor was designed to study
80 the effect [7]. The platform motions significantly affect the power and thrust characteristics of the
81 rotor almost to the same order as the effect of Tip Speed Ratio (TSR) and the blade angle. A scaled
82 down model of the NREL 5MW rotor was designed and tested in the wave tank (immersed in the
83 water) to match the Reynolds number Re , as in field operation. The experiments are conducted with

84 the focus on surge motion [8] and its effects on aerodynamic performances. The BEM based
85 AeroDyn model was modified (LR AeroDyn) to predict the hydrodynamic load on to the scaled
86 rotor. LR has enhanced the BEM code (LR-uBEM) to simulate the unsteady aerodynamic behavior
87 of the rotors. The LR-uBEM model implements the dynamic inflow model based on the elemental
88 aerodynamic loads prediction of individual blades. To gauge the accuracy of engineering numerical
89 codes LR AeroDyn and LR-uBEM, high fidelity CFD model was developed and validated against
90 the experimental simulation.

91 2. Scaled Rotor for unsteady aerodynamic experiments

92 To predict the global loads in well-ordered experimental conditions by scaling down the wind
93 turbine rotor is challenging. This can be attributed to the complexities involved in accomplishing the
94 three scaling laws, which has to be followed to design a scaled rotor that matches the performance of
95 full scale reference rotor [9-12]. It is highly challenging to match the performance of the scaled rotor
96 for the coefficients such as coefficient of power (C_p), coefficient of torque (C_q), and the coefficient of
97 thrust (C_t), to a full scale reference rotor due to the incompatibility of the three primary scaling
98 criteria, the maintenance of geometric, kinematic, and dynamic similarity between model and full
99 scale. Geometric and kinematic similarity are readily achieved by the application of constant
100 geometric scale factor and the maintenance of the tip speed ratio, respectively. However, in doing so
101 the dynamic similarity criteria, defined principally as the maintenance of the Reynolds number for
102 the flow over the blade at model and full scale, is typically not met. In order to address this, a
103 number of researchers have proposed a global performance matching approach for the design of
104 model scale wind turbine rotors where the primarily objective was not the study of the rotor in
105 normal operating conditions [9-12]. Examples of such are the MARIN Stock Wind Turbine for the
106 evaluation of the performance of floating wind turbine foundations scaled down under wind and
107 wave action and the evaluation of advanced control strategies under unsteady operating conditions.
108 In both cases, the design objective was to match the coefficients of the model scale to their respective
109 full scales for a range of operating tip speed ratios. This is achieved by changing the aerofoil profile
110 in the scaled down model along the length of the blade so as to increase the lift coefficient, increasing
111 the chord distribution along the length of the blade by a constant factor, and altering the twist
112 distribution to maximize the lift to drag ratio for the tip speed ratios of primary interest. The criteria
113 for geometric similarity is abandoned, kinematic similarity is maintained, the deficit in the dynamic
114 similitude is corrected for.

115 As is the case for the two rotor designs discussed, the objective of the experiments in this case
116 was the evaluation of the rotor performance subjected to external influence relative to the normal
117 operating state. Specifically, the quantification of the time varying coefficient of thrust resulting from
118 the periodic motion of a rotor at a number of frequencies and amplitudes typical of floating wind
119 turbine system. As such a similar approach to the scaling criteria has been taken. However, in this
120 case, in addition to the global performance matching model scale rotor design objective, additional
121 objectives have been defined in attempt to maintain the critical local performance measures. The
122 model scale rotor requirements are defined as follows:

- 123 1. The coefficient of thrust of the model rotor must be similar to the full scale reference for a range
124 of tip speed ratios,
- 125 2. The chord must be scaled by the same geometric scale factor as the diameter of the rotor,
- 126 3. The twist distribution along the non-dimensional length of the model blade must be same as
127 full scale reference,
- 128 4. The axial induction factor along the non-dimensional length of the model blade must be same
129 as the full scale reference for a range of tip speed ratios.

130 The full scale reference rotor used for this study is the NREL 5MW Reference wind turbine [13],
 131 this has been studied extensively and has been extensively reported in literature. This was also the
 132 basis for the design of the MARIN Stock Wind Turbine. The diameter of the scaled model of the rotor
 133 has been chosen to be 1.0m in order to minimize experimental blockage effects resulting in a
 134 geometric scale factor of 126.0. As aerodynamic coefficients largely influence the rotor
 135 performance, a new methodology has been adopted to match the scaled airfoil Re to the full-scale
 136 airfoil Re. Significant effort has been dedicated to optimize the airfoil profile in order to match the lift
 137 curves even in low Re [7], by retaining the twist of 5 MW NREL rotor blade. As the lift coefficient
 138 heavily influences the non-dimensional rotor thrust and the axial induction factor, the primary
 139 objective is to achieve the required lift coefficients of airfoil sections and in turn complying the
 140 design requirements 1 and 4. Considering the blade length of the scaled rotor, three significant
 141 airfoil profiles are employed in comparison to the six profiles in full scale model. The following
 142 Table.1 indicates the full-scale rotor airfoils and the corresponding airfoils of the scaled rotor. The
 143 shape of SMA (Strathclyde Model rotor Airfoil) series airfoils are shown in comparison to the
 144 full-scale model airfoils in Fig. 2. The methodology followed to accomplish the airfoil profiles and
 145 further analysis on the scaled rotor model performances are described in more detail in [7] and [14].

146 Scaled rotor parameters are shown in Table 1. The designed scaled rotor blades are similar to
 147 full scale rotor following the procedure of Froude scaling. A comparison of the scaled rotor model
 148 and full scale airfoil geometry is shown in Fig 2.

149

Table 1. Scaled rotor airfoil details

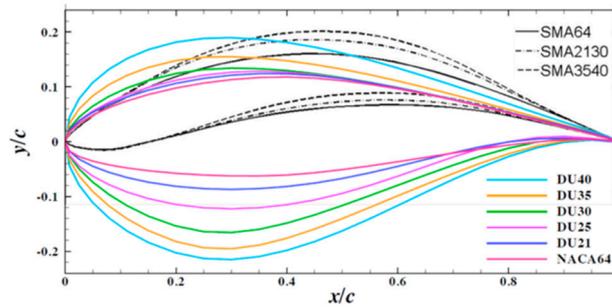
Element/Node	Element center radius (m)	Twist(°)	Element center chord(m)	*Cross-sectional profile
1	0.023	13.308	0.028	Cylinder
2	0.044	13.308	0.031	Cylinder
3	0.066	13.308	0.033	Cylinder
4	0.093	13.308	0.036	DU40 (SMA3540)
5	0.126	11.48	0.037	DU35 (SMA3540)
6	0.158	10.162	0.035	DU35 (SMA3540)
7	0.191	9.011	0.034	DU30 (SMA2130)
8	0.223	7.795	0.032	DU25 (SMA2130)
9	0.256	6.544	0.03	DU25 (SMA2130)
10	0.288	5.361	0.028	DU21 (SMA2130)
11	0.321	4.188	0.026	DU21 (SMA2130)
12	0.354	3.125	0.024	NACA64 (SMA64)
13	0.386	2.319	0.022	NACA64 (SMA64)
14	0.419	1.526	0.02	NACA64 (SMA64)
15	0.446	0.863	0.018	NACA64 (SMA64)
16	0.467	0.37	0.017	NACA64 (SMA64)
17	0.489	0.106	0.011	NACA64 (SMA64)

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Note: * The name in the bracket is scaled rotor airfoil with corresponding airfoil of 5 MW NREL rotor airfoils

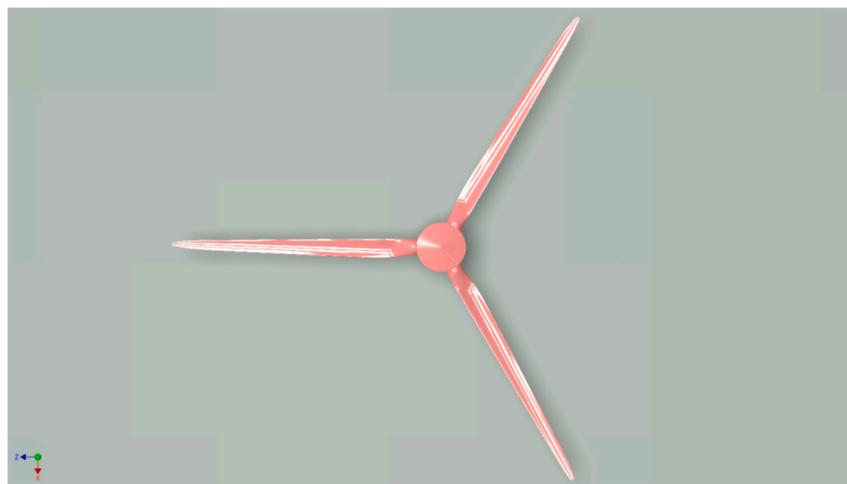


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154 **Figure 2.** Scaled rotor model airfoil shapes in comparison with reference [1]

155 Lift coefficient for the SMA airfoils are computed using Xfoil for the model Re , while for
 156 the full-scale airfoils, the generated lift coefficients from Xfoil are verified through wind tunnel
 157 tests. The Xfoil result compare well with the experimental curves at lower AoA, but at higher
 158 AoA Xfoil overpredicts the coefficients. This can be attributed to the earlier onset of flow
 159 separation in the experimentation. A 3D rendering of the fully assembled rotor is shown in Fig
 160 3. The blades are fixed to the hub at a fixed pitch angle of 0° using a flange machined in the root
 161 end of the blades; as a result the accuracy of the pitch angle is defined by the machining
 162 tolerance of the stainless steel components and not that of the measurement of the pitch angle
 163 itself as would be the case if a locking bearing type fixture was used. Using this approach
 164 requires that the model scale hub is non-dimensionally larger than the full scale reference
 165 to allow for the sufficient space to make the connection from the blade to hub and hub to shaft.
 166 However, the increased diameter of the hub does not require that the blade geometry is altered
 167 in any section other than that defined with a cylindrical section detailed in Table 1 and as such
 168 will have no impact on the aerodynamic performance of the blades.

169



170

171 **Figure 3.** 3D Model of the scaled rotor.

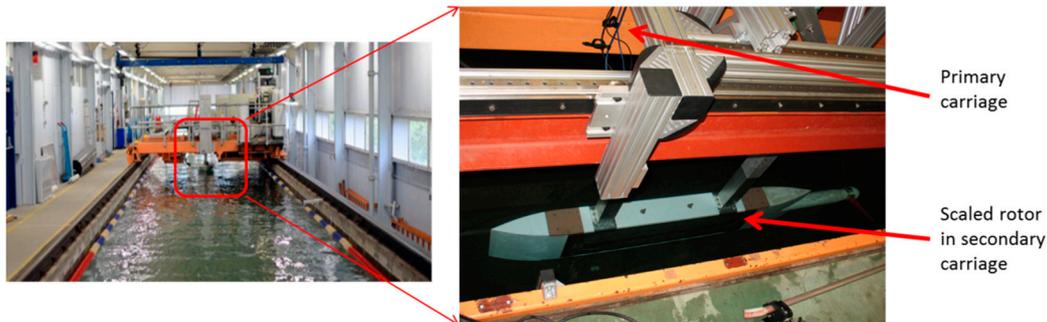
172 During the design stage, the global model rotor performance was compared to the full scale
 173 reference for non-dimensional thrust and torque. The thrust force on the rotor is primarily
 174 influenced by the aerofoil lift and as such the match between the model and reference for this
 175 property is favorable. The increased aerofoil drag at the experimental Reynolds number results in a
 176 reduced torque as compared to the full scale rotor. This was an expected result of implementing this
 177 scaling methodology. The local blade performance was assessed for the model scale rotor by
 178 comparing the axial and tangential Induction factors and the angle of attack along the
 179 non-dimensional length of the blade for different tip speed ratios (TSR) by the authors [7]. The scaled
 180 rotor with its surge motion dual carriage is as shown in Fig. 4.

181



182

183 **Figure 4.** Physical scaled rotor with a rig setup (for surge motion unsteady effects) on the carriage of the
184 towing tank



185

186 **Figure 5.** The tow tank at the Kelvin Hydrodynamics Laboratory and carriage systems

187 In order to achieve Reynold number similarity the model was tested under water at the
188 University of Strathclyde's Kelvin Hydrodynamics Laboratory towing tank (76 m length, 2.5 m
189 depth and 4.6 m in width). The cross-sectional area of the tow tank was sufficiently large compared
190 to the rotor diameter under investigation assuring minimum blockage. The prescribed steady and
191 periodic flow speeds were imparted into the rotor by pulling the rotor through the stationary water
192 using a dual carriage system (primary carriage was for constant motion and secondary carriage for
193 surge cyclic motion) as in Fig.5. The rotor speed was controlled using a DC motor and PID controller
194 directly coupled to the rotor through a shaft fixed to a stiff bedplate using three low-friction
195 bearings. The torque and thrust forces are measured in-line with the shaft using a bi-directional force
196 transducer at a frequency of 137Hz.

197 2. 1. Experimental Design of Surge Motion

198 The surge motion of the rotor does not represent a specific floating wind turbine system, but
199 rather a generalized matrix of operating points, from which conclusions can be drawn regarding the
200 rotor thrust loading. The three variables under investigation were the rotor tip speed ratio, the surge
201 amplitude, and the surge frequency. Similar to the static analysis of the rotor, the tow speed was
202 constant and the rotor speed was varied to alter the tip speed ratio. The operating range of values for
203 these parameters were specified such that they mimic the full-scale rotor operating conditions
204 limited to the experimental setup and surge carrier motion.

205 Three prior studies have been conducted with the objective of studying the aerodynamic
206 performance with the surge motion. The initial values for the parameters were set according to these
207 studies for the current unsteady experimentation of the model scale rotor. Liu et al [15] studied the

208 NREL 5MW baseline wind turbine at three different wind speeds, surge velocities, and surge
 209 frequencies numerically using a BEM based aerodynamic model with a dynamic inflow correction.
 210 DeVaal et al [16] compared the aerodynamic performance of the NREL 5MW turbine subjected to the
 211 a surging motion using four different numerical approaches; a quasi-static BEM model, a BEM
 212 model with an integrated Pit-Peters dynamic inflow correction, a BEM model with an integrated Stig
 213 Oye dynamic inflow correction, and a CFD based actuator disc model. Similarly, Micallef and Sant
 214 [17] studied the NREL 5MW rotor in surge using a quasi-static BEM model, a generalised dynamic
 215 wake model, and a CFD based actuator disk model. The valuable conclusion that has been arrived
 216 from these studies is that the wake induced effects of the rotor thrust as a result of the rotor surging
 217 into the flow depends upon the tip speed ratio, surge frequency, and surge displacement amplitude.

218 The experimental surge operational points considered are drawn primarily from the work of
 219 Liu et al [15] and deVaal et al [16], the surge frequency considered by Micallef and Sant [17],
 220 although representative of a full scale operational condition which would be experienced by a
 221 floating wind turbine system, is out with the operational envelope of the experimental apparatus
 222 when scaled to the model scale. The surge frequencies studied by Liu et al and deVaal et al were 0.1,
 223 0.2, and 0.3rad/s, and between 0.127 and 1.0rad/s, respectively; the corresponding surge
 224 displacement amplitudes were, 3.0, 6.0, and 9.0m, and between 2.0 and 16.0m. deVaal considers only
 225 the rotor operating at its rated wind speed ($V = 11.2\text{m/s}$), Liu et al and Micallef and Sant both
 226 consider this same rotor operation in addition to off design points.

227 The investigated rotor operational states, defined by Liu et al and Micallef and Sant in terms of
 228 inflow wind speed and tip speed ratio, respectively, were 8.0, 11.2 and 16.0m/s and 4.0, 7.0, and
 229 11.0. The tip speed ratio of the NREL 5MW Baseline Wind Turbine at its rated wind speed of
 230 11.2m/s, as defined by Jonkman et al [13], is 7.0.

231 The model scale surge motion displacement and frequency were derived from the studies
 232 discussed by Liu et al [15] and deVaal et al [16] by applying a suitable scaling methodology. This
 233 was achieved by following the scaling relationships defined by Jain et al [18] for the experimental
 234 analysis of the combined effect of aerodynamic and hydrodynamic force components on a model
 235 floating wind turbine rotor and foundation in a wind and wave basin. The model scale surge
 236 frequency and displacement were scaled following the relationships defined in equations 1 and 2,
 237 respectively.

$$238 \omega(\text{surge}, \text{model}) = \omega(\text{surge}, \text{full}) * \sqrt{\lambda} \quad (1)$$

$$239 A(\text{surge}, \text{model}) = \frac{A(\text{surge}, \text{full})}{\sqrt{\lambda}} \quad (2)$$

242 where A is amplitude, ω is the angular frequency and λ is the geometric scaling factor, 126.0 for the
 243 present set of experiments. A comprehensive static and unsteady test matrix was performed. The
 244 dimensionless parameters Ct and Cq that determine the amount of momentum and energy extracted
 245 from the water was computed for static cases. The coefficient of thrust is defined by equation 3:

$$246 Ct = \frac{T}{0.5 \rho AV^2} = 4a(1 - a) \quad (3)$$

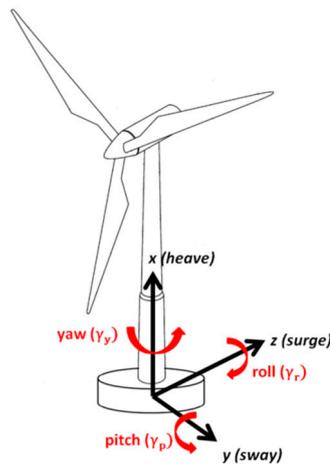
247 where T is the rotor thrust force, ρ is the fluid density, A is the rotor plane area and V is the
 248 fluid velocity. The coefficient of torque is defined by equation 4:

$$249 Cq = \frac{Q}{0.5 \pi \rho R^3 V^2} \quad (4)$$

250 where Q is the torque and R is rotor radius. The torque is measured when the scaled rotor is at
 251 constant rotational speed, constant tow speed of primary carriage for the static test as in Table 2.
 252 Time history of thrust and torque are captured in unsteady surge motion test scenario cases (as in
 253 Table 3). During the unsteady test scenario, secondary carriage oscillates while primary carriage is
 254 at constant speed.

255 3. Numerical Methodology

256 Due to wind shear between ground or sea level to tip of the rotor blade, gust, turbulence, flow
 257 field around the rotor and near wake regions are highly complex even in land-based installations. In
 258 FOWT, the complexity is further compounded by the additional motions at the rotor plane induced
 259 by the floating platform subjected to the three translational (heave, sway, and surge) and three
 260 rotational (yaw, pitch, and roll) motions as shown in the Fig. 6. Among these six motions, surge
 261 motion and pitch motion are responsible for pushing the rotor to interact with its own wake. This
 262 interaction significantly modifies the wind turbine's operating state and in turn varying the axial
 263 induction velocity field and unsteadiness. As the BEM theory is constructed based on the axial
 264 induction factor range, it has to be validated to gain sufficient confidence before applying to FOWT.
 265 In the current study, scaled rotor surge motion experimental results were exploited for validating
 266 the numerical codes.

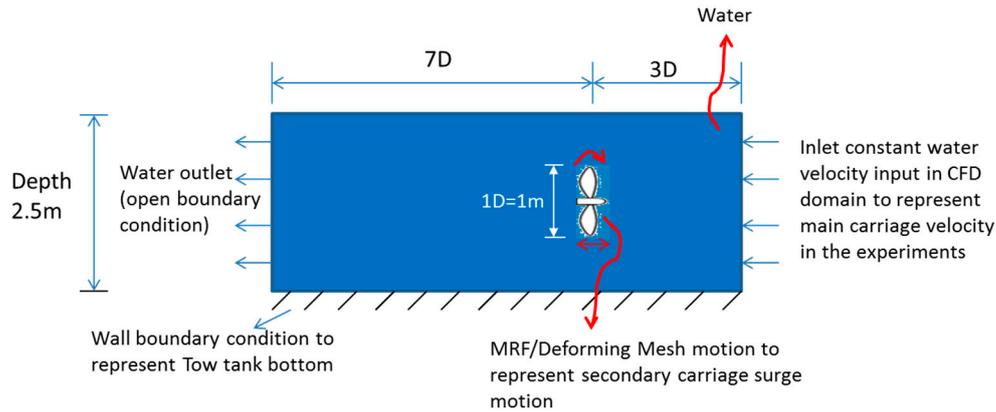


267
 268 **Figure 6.** Floating platform motions (3 linear and 3 rotational).
 269

270 CFD, LR-AeroDyn and LR-uBEM has been chosen for the validation study. CFD simulations
 271 are carried out with reasonable accuracy to gain insight on surge motion's flow field and wake
 272 interactions. As AeroDyn is widely employed in industry for its accuracy, Marine and Hydrokinetic
 273 code is modified to incorporate the surge motion scenarios (LR-AeroDyn). LR's research on
 274 unsteady aerodynamics of FOWT resulted in the development of LR-uBEM code accounting
 275 dynamic in flow model with other unique features. The following sections discuss in detail on these
 276 methodologies.

277 3.1. CFD Model

278 The tow tank is defined in the CFD numerical environment as in Fig.7 to solve the unsteadiness
 279 on the rotor due to surge motion. The primary or main carriage motion (constant) of the rotor is
 280 represented as uniform inlet water boundary condition and the secondary carriage surge motion is
 281 represented as MRF (Multiple Reference Frame) and sliding mesh motion on the rotor domain.



282

283 **Figure 7.** Schematic representation of tow tank in CFD computational domain.284 **3.1.1. CFD Mesh Model**

285 As shown in Fig .8, the scaled rigid 3D rotor blade geometry was generated through commercial
 286 meshing software Ansys ICEM CFD (Version 16.2) by sweeping through all the 17 aero profiles of
 287 the scaled model. The hub is modelled to the dimensions used in the tow tank to eliminate any
 288 inaccuracies introduced due to the flow variation near the blade root.

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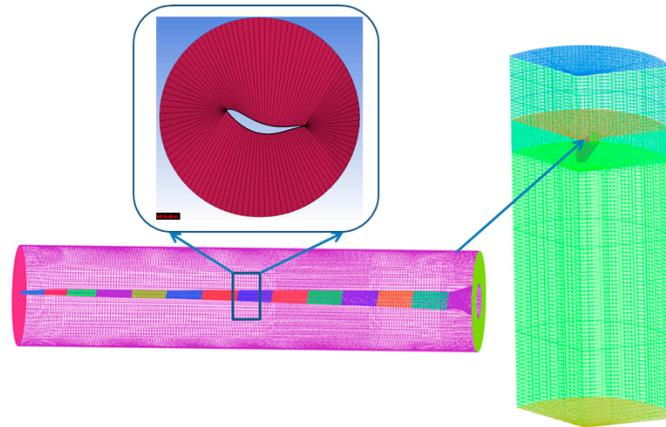


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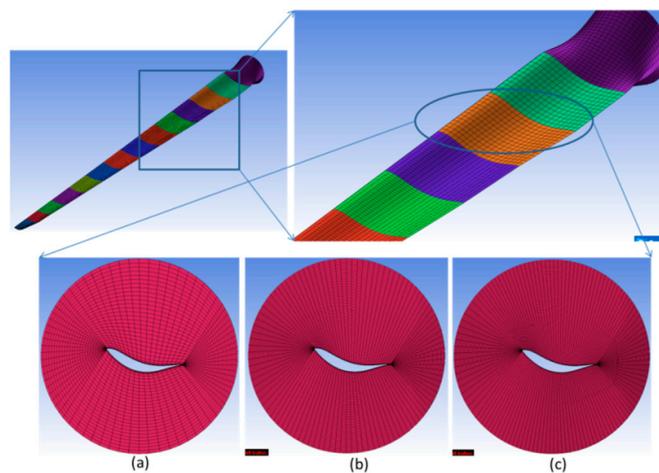
291 **Figure 8.** Scaled rotor 3D model generated in Ansys ICEM CFD environment

292 A multi-block meshing strategy has been employed to create hexahedral mesh in the outer
 293 domain. 'O-grid' type mesh is chosen for the blade domain. A hexahedral structured mesh around
 294 the scaled rotor of one blade and the surrounding water of turbine rotor was generated and for other
 295 blades mesh was generated using periodicity option. As shown in Fig. 9-10, the 3D model of the
 296 scaled rotor model and three kinds of mesh clustering methods (log scale change in near wall and
 297 linear towards perpendicular direction) around the rotor were used in the mesh sensitivity study as
 298 the thrust force is more sensitive to method of mesh clustering.

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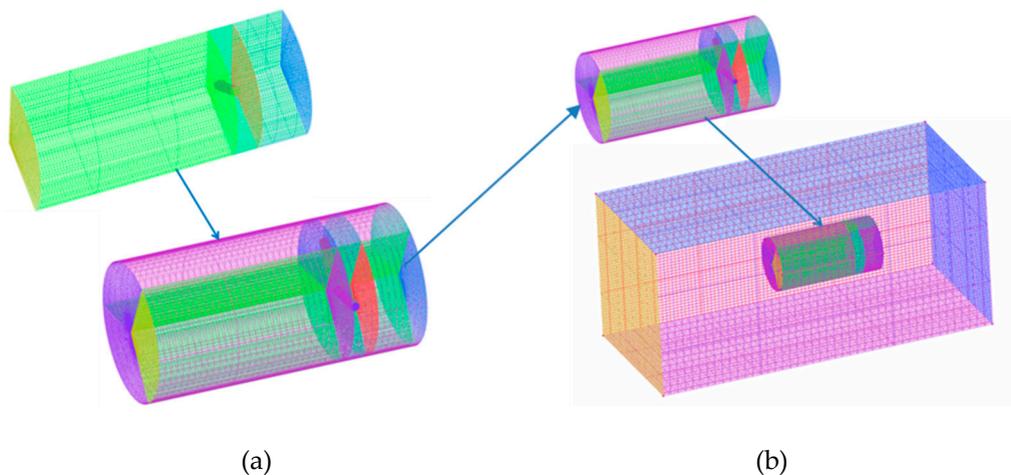
301 **Figure 9.** Scaled rotor mesh model and 1/3rd model of rotating domain with single rotor

302

303 **Figure 10.** Mesh sensitivity study (a). coarse with 0.59million nodes (b) medium with 1.65million nodes
 304 (c) fine with 2.38million nodes-from left to right).

305 The entire computational domain is shown in Fig. 11. The mesh was sufficiently discretized to
 306 capture the near wake and far wake field reasonably. The scaled rotor was refined to yield an y^+ of
 307 ~ 1 near the tip and less than 2 for the rest of the domain as shown in Fig. 12.

308



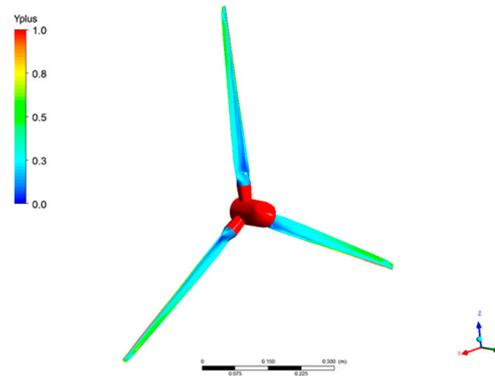
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311

312 **Figure 11.** CFD computational domain (a) 1/3rd rotor model is swept for 360 deg with near wake
 313 domain (b) the complete near wake region mesh model inside the global model

314



315
316 **Figure 12.** Scaled rotor - y+ contour.

317 3.1.2. CFD Numerical Solver

318 The mesh mathematical model is imported in to Ansys CFX CFD solver (Version 16.2) to simulate
319 experimental scenario cases of the rigid 3D scaled rotor. The K-Omega SST (Shear Stress Transport)
320 turbulence scheme was employed without transition modeling. A high order advection scheme and
321 first order numerical method were chosen for turbulence modelling. The k- ω based SST model
322 employs the k- ω model for the near surface treatment and the k- ϵ model in the free-shear layers. In
323 this methodology a blending function is adopted to bridge these two models. The SST k- ω model
324 accounts the transportation of the turbulent shear stress and capable of accurately predicting the
325 onset and the magnitude of flow separation under adverse pressure gradients in the rotor blade,
326 near wake and far wake regions.

327 For the aforementioned reasons, the two-equation SST k- ω model is widely exploited in wind
328 industry for their accurate predictions of flow over blunt body.

329 The K-Omega SST model has a similar form to the standard K-Omega model:

330

$$331 \quad \frac{\partial}{\partial x} (\rho \kappa) + \frac{\partial}{\partial x_i} (\rho \kappa u_i) = \frac{\partial}{\partial x_j} \left(\Gamma_\kappa \frac{\partial \kappa}{\partial x_j} \right) + \tilde{G}_\kappa - Y_\kappa + S_\kappa \quad (5)$$

332

333 And

334

$$335 \quad \frac{\partial}{\partial x} (\rho \omega) + \frac{\partial}{\partial x_i} (\rho \omega u_i) = \frac{\partial}{\partial x_j} \left(\Gamma_\omega \frac{\partial \omega}{\partial x_j} \right) + \tilde{G}_\omega - Y_\omega + D_\omega + DS_\omega \quad (6)$$

336

337 G_κ in the Equations 5 and 6 represents the generation of turbulence kinetic energy due to mean
338 velocity gradients. G_ω represents the generation of ω . Γ_κ and Γ_ω represents the effective diffusivity
339 of κ and ω respectively. Y_κ and Y_ω represent the dissipation of κ and ω due to turbulence. D_ω
340 represents the cross-diffusion term. S_κ and S_ω are user-defined source terms.

341 3.1.3. Mesh sensitivity study, static case simulation and validation

342 The CFD simulations were carried out with uniform water velocity at the inlet boundary for the
343 static case scenarios (without surge motion) as shown in Table 2 before carrying out the unsteady
344 test case simulations. For mesh sensitive study, the rotor thrust co-efficient was compared against
345 the chosen case of 14 rad/s with 7 TSR and 1 m/s water speed, which is the representative of 1m/s
346 tow speed of the carriage mounted with scaled physical rotor as in Table 2 and the results were

347 published by the authors [1]. Medium size mesh model was used in CFD for the validation purposes
 348 of static and unsteady test experimental cases due to the reasonable accuracy and computational
 349 time. Thrust force alone was considered for comparison as the scaled rotor was developed based on
 350 the thrust force related parameter function used in the optimization function [7]. The overall
 351 medium mesh model domain had 7.32 million nodes. The chosen mesh model yielded the y^+ of
 352 less than 1 near the tip and less than 2 everywhere else as shown in Fig. 10. Multiple Reference
 353 Frame (MRF) and sliding mesh simulation methodology was used in the CFD simulations to
 354 validate the thrust and torque predictions of the scaled rotor model. The CFD predicted values were
 355 then validated against the measured values of the experiments as in the Table 2.

356
 357

Table 2. Static state test condition

Tow speed, m/s	TSR	Rotational Speed (rad/s)
1.000	3.000	6
0.931	4.500	9
1.000	7.000	14
0.822	8.519	14
0.735	9.522	14

358 The static runs were carried out to obtain the C_t and C_q in relation to TSR as benchmark values
 359 to compare the rotor subjected to static test case conditions. In order to allow the rotor to rotate at
 360 different TSR, the rotor was subjected to various tow speeds and rotational speeds (rad/s) facilitating
 361 a smooth distribution over the operating range. The TSR of the rotor was allowed to vary from 3 to
 362 9.5 though a constant TSR should be achieved for static scaling. The model rotational speed of 14
 363 rad/s corresponds to the rated rotational speed of the NREL 5MW of 12.10 rpm. Other model
 364 rotational speeds linearly correspond to full-scale rpm. Thus, for a model rotational speed of Ω_m in
 365 rad/s, the full scale rotational speed Ω_f in rpm is given by Equation 7:

366
 367

$$\Omega_f = \frac{\Omega_m}{14 \left(\frac{\text{rad}}{\text{s}}\right)} * 12.1 \text{ rpm} \quad (7)$$

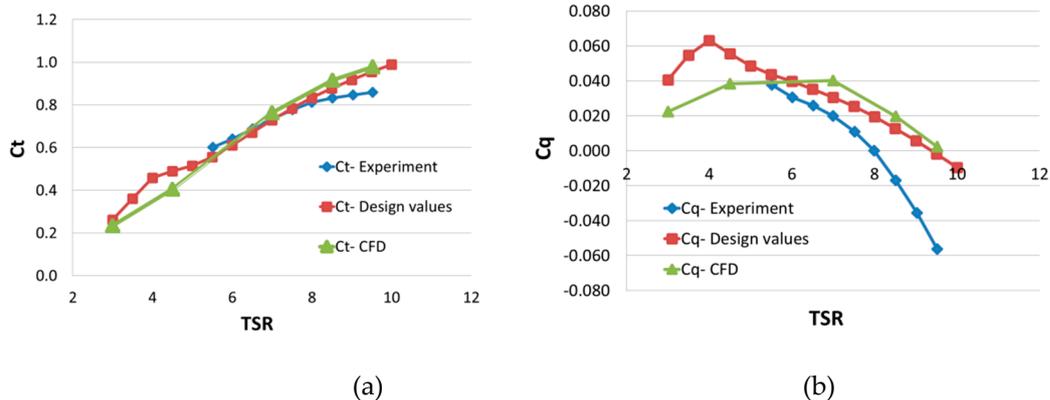
368 The full-scale wind speed, V_f is found from the TSR of the experiment:

$$V_f = \frac{63\pi\Omega_f}{30 \text{ TSR}} \quad (8)$$

370 since the rotor radius is 63m. The rated conditions of 12.10 RPM and 11.4m/s wind speed were
 371 modelled at a rotational speed of 14.0 rad/s and a tow speed of 1m/s. It is aimed to validate the
 372 static state conditions. Hence, the coefficient of thrust C_t and the coefficient of torque C_q in relation
 373 to the TSR are computed analytically (designed values), numerically (CFD) and experimentally. The
 374 results are plotted as shown in the Fig. 13.

375 The thrust coefficients from all the three methods were comparable and difference was within
 376 10%, while the torque coefficient displays a notable difference in analytical prediction (design
 377 values) from the well correlated experimental and CFD results. Xfoil predictions of lift coefficient
 378 C_l and drag coefficient C_d would have contributed significantly to the deviation. It was
 379 experimentally verified that the Xfoil over predicts the drag in the low Re range as the flow over the
 380 airfoil is extremely complex and nonlinear to compute the drag by panel method. The over
 381 prediction is exacerbated by the extrapolation for higher angle of attack from the initial set of lift and

382 drag coefficients computed at lower angle of attack. A possible way of curtailing the error is to
 383 experimentally obtain the initial set of C_l and C_d from the wind tunnel test and extrapolate by
 384 Viterna or Montgomerie method. Considerable effort has been dedicated in refining the mesh for
 385 improved near wall treatment to compute the boundary layer separation and to achieve accurate
 386 rotor drag. Since optimization of the airfoil for the operating Re of the scaled rotor is not in the scope
 387 of the current study, the effect of low Re are anticipated. The discrepancies due to drag is inevitable
 388 especially for the scaled prototype due to premature flow separation on airfoils induced by low Re
 389 because of smaller chord length.



390

391

392 **Figure 13.** static state validation curves for CFD (a) Comparison of thrust co-efficient (b) Comparison of
 393 torque co-efficient.

394 3.1.4. CFD model for unsteady experimental scenarios

395 The surge motion methodology was developed in Ansys-CFX (Version 16.2) software. Medium
 396 size with 7.32 million node mesh model was used for the unsteady simulations. The unsteady runs
 397 include sinusoidal surging motions of the rotor from low to extreme frequencies (3 - low, medium,
 398 and high) and amplitudes (2 - lower and higher), to demonstrate the effect on the rotor unsteady
 399 aerodynamics as experimentally simulated. Simulations were carried out with MRF and deforming
 400 mesh setup in the CFD environment, constant water velocity from the inlet (with a turbulence
 401 intensity of 5%) of the computational domain represented constant primary carriage motion. The
 402 deforming mesh was setup up such that the mesh in the blade and near-wake regions was given a
 403 high rigidity, so that deformation is limited to the outer region with bigger cells, so negative
 404 volumes would not occur. A high resolution scheme was used for advection and turbulence
 405 numerics, a second order backward Euler scheme was used for time stepping. Pressure-velocity
 406 coupling was solved using a fourth order Rhie-Chow interpolation. The surge motion is defined by
 407 the Equation 9:

408

$$409 \quad -A + A \cos 2\pi f \quad (9)$$

410

411 where A is the amplitude of motion and f is the frequency

412 The entire blade and near-wake regions were set to oscillate as defined by Equation 9. The
 413 equation assumes that the mesh starts at the forward-most position, since there are more cells
 414 downstream of the rotor, thus it would facilitate smoother deformation. As per the Table 3,
 415 simulations are carried out to compare against the experimental values.

416

417

418
419**Table 3.** Unsteady experimental test case scenarios chosen for numerical validation at the rotor rotational speed of 14 rad/sec.

TSR	Tow speed, m/s	Surge frequency(f), rad/s	Amplitude(A), M	Scenario name for reference
8.5	0.824	1.12 (0.18Hz)	0.0238	SFA1
		1.12(0.18Hz)	0.1190	SFA2
		3.37(0.54Hz)	0.0238	SFA3
		3.37(0.54Hz)	0.1190	SFA4
		5.61(0.89Hz)	0.0238	SFA5
		5.61(0.89Hz)	0.0952	SFA6
7.0	1.000	1.12(0.18Hz)	0.0238	SFA7
		1.12(0.18Hz)	0.1190	SFA8
		3.37(0.54Hz)	0.0238	SFA9
		3.37(0.54Hz)	0.1190	SFA10
		5.61(0.89Hz)	0.0238	SFA11
		5.61(0.89Hz)	0.0952	SFA12
6.0	1.167	1.12(0.18Hz)	0.0238	SFA13
		1.12(0.18Hz)	0.1190	SFA14
		3.37(0.54Hz)	0.0238	SFA15
		3.37(0.54Hz)	0.1190	SFA16
		5.61(0.89Hz)	0.0238	SFA17
		5.61(0.89Hz)	0.0714	SFA18

420

421 For unsteady test cases, the sinusoidal surging motions for the model rotor were designed to be
422 based on the work by [15] and [16]. As the surge motion is predominant in floating offshore wind
423 turbine applications [17], a detailed surge motion experiments were carried out with scaled rotor.
424 The scenarios were chosen carefully to validate the effects of unsteadiness by the various numerical
425 simulations. Mean thrust and torque values were considered for validation purposes initially. For
426 each of the three different TSRs, three different surge frequencies and two amplitudes (minimum
427 and maximum) were chosen to capture the unsteady behavior. For the scenarios given in the Table
428 2, the steady state MRF simulations were first carried out with the rotational speed of the rotor and
429 towing speed as water inlet velocity in CFD simulations. The results of the steady state calculations
430 were used to initialize the solutions for a complete transient case involving the surge motion of the
431 scaled rotor unsteady test case scenario. The domains were structured in such a way that both the
432 blade rotations and rotor surging motions could be handled smoothly by the solver. The rotor
433 domain had a sliding mesh interface for blade rotations and the mesh motion (deforming mesh)
434 applied for surging motion had an extremely high stiffness in this domain which was relaxed
435 gradually towards the outer domain to preserve the fine boundary layer mesh. This high stiffness
436 ensured that the mesh in the rotor domain had almost no relative nodal displacement, as the mesh
437 on the blade had the first node on the order of microns to yield a $y^+ \sim 1$.

438 3.2. LR –AeroDyn Model for unsteady experimental scenario

439 AeroDyn (V15.04) is an open source (NREL) time-domain wind turbine aerodynamics module
440 [19] that has been tailored for Marine Hydorkinetic Turbines (MHT). MHT AeroDyn module is
441 customized for scaled rotor performance prediction of unsteady experimental test case runs as
442 shown in Table 3 as the model was refined to cover the whole scenario.

443

444 FAST model settings:

445 AeroDyn calculates aerodynamic loads on both the blades and tower. Aerodynamic
 446 calculations within AeroDyn are based on the principles of actuator lines, where the
 447 three-dimensional (3D) flow around a body is approximated by local two-dimensional (2D) flow at
 448 17 cross sections. The distributed pressure and shear stresses are approximated by lift forces, drag
 449 forces, and pitching moments lumped at a node in a 2D cross section. Analysis of 17 nodes are
 450 distributed along the length of each blade, the 2D forces and moment at each node are computed as
 451 distributed loads per unit length, and the total 3D aerodynamic loads are found by integrating the
 452 2D distributed loads along the length.

453 The MHK based model customized for the scaled rotor calculates the influence of the wake via
 454 induction factors based on the quasi-steady Blade-Element/Momentum (BEM) theory, which
 455 requires an iterative Brent's method to nonlinear equation. By quasi-steady or equilibrium wake
 456 (EQUIL) model, it is meant that the induction reacts instantaneously to loading changes. The
 457 induction calculation, and resulting inflow velocities and angles, are based on flow local to each
 458 analysis node of each blade, based on the relative velocity between the fluid and structure (including
 459 the effects of local inflow skew, shear, and turbulence). This method has no time lag which means no
 460 dynamic inflow. The Glauert's empirical correction (with Buhl's modification) is used in the linear
 461 momentum balance at high axial induction factors. In the BEM solution, Prandtl tip-loss, Prandtl
 462 hub-loss models are applied.

463 Angle-of-attack calculations in AeroDyn assume that the axial induction factor(a) only applies
 464 to the free-stream wind velocity(V_α). To calculate the total relative wind speed(V_{rel}) normal to the
 465 rotor disc, each blade element's structural velocity is added to the free-stream wind velocity at the
 466 rotor disc, as shown below.

$$467 \quad V_{rel} = V_\alpha(1 - a) + V_{rotor} \quad (10)$$

468 V_{rotor} , is the structural velocity of the blade element normal to the disc (measured positive
 469 when pointing upwind).

470 The assumption in AeroDyn is that the structural velocities are the product of structural
 471 vibrations at high frequencies, which would results in relatively small induced velocities. However,
 472 when considering floating offshore wind turbines (FOWT), low-frequency motions, particularly, in
 473 surge, pitch and yaw degrees of freedom, which induce change in the free-stream velocity, could
 474 lead to high induced velocities. In low-frequency motion, a better way of expressing the relative
 475 wind speed normal to the rotor disc would be:

$$476 \quad V_{rel} = (V_\alpha + V_{rotor})(1 - a) \quad (11)$$

478 3.3. LR –u BEM Model for unsteady experimental scenario

479 The LR uBEM code was developed to address the issue of uncertainty in predicting the
 480 aerodynamics of floating offshore wind turbines. The development of the uBEM code included
 481 several features vital to an accurate assessment of floating offshore wind turbine aerodynamics.
 482 These include:

- 483 1. An improved tip-loss model which accounts for changes in tip speed ratio and changes in loss
 484 distributions in different wake states.
- 485 2. An unsteady airfoil model including a modified Beddoes-Leishman model which models the
 486 unsteady circulation using the suction surface shape-dependent time constants
- 487 3. A combined unsteady airfoil and stall delay model, accounting for changes in stall delay due
 488 to changes in wind and rotational velocities in real-time.
- 489 4. An extension of the Glauert correction by Buhl to the propeller and propeller-brake wake
 490 states.
- 491 5. A dynamic wake model to account for the time-lag between aerodynamic forces on the rotor
 492 and wake velocities

493 In addition, uBEM predicts the forces on each blade section separately, taking into account local
 494 velocity changes at any position on each blade. The development of the code was based on CFD
 495 simulations of the NREL 5MW virtual wind turbine, used for code comparison studies in OC3, OC4,
 496 and OC5. The CFD simulations were carried out for a static wind turbine and for a surging wind
 497 turbine under various surge conditions, with a fixed rotor RPM. The code was developed completely
 498 in MATLAB, and is modularized to allow for changes to the various corrective models implemented.

499 The unsteady blade element momentum method (uBEM) used in the present study, is based on
 500 the method presented in [20]. The relative velocity vector is given by:

$$501 \quad \mathbf{V}_{rel} = \mathbf{V}_0 + \mathbf{W} + \begin{pmatrix} 0 \\ -\Omega r \cos(\theta_c) \\ 0 \end{pmatrix} \quad (12)$$

502 where V_0 is the blade-specific wind speed at the blade element including relative speed due to rotor
 503 motion, Ω is the rotor rotational speed in rad/s, r is the local blade segment radius. The flow angle,
 504 ϕ , is the angle between the relative velocity and the normal of the rotor plane.

$$505 \quad \phi = \arctan\left(\frac{V_{rel,y}}{V_{rel,z}}\right) \quad (13)$$

506 The normal (z) and tangential (y) induced velocities are then given by:

$$507 \quad \mathbf{W}_z = \frac{-|V_{rel}|^2 C_l \cos(\phi) cB}{8F \left| (V_0 + A) + f_g \begin{pmatrix} 0 \\ 0 \\ W_z \end{pmatrix} \right| \pi r} \quad (14)$$

508

$$509 \quad \mathbf{W}_y = \frac{-|V_{rel}|^2 C_l \sin(\phi) cB}{8F \left| (V_0 + A) + f_g \begin{pmatrix} 0 \\ 0 \\ W_z \end{pmatrix} \right| \pi r} \quad (15)$$

510 Where B is the number of blades, F is the tip-loss factor, f_g is the Glauert correction for high axial
 511 induction factors and C_l is the coefficient of lift computed using the Du & Selig stall-delay model [21]
 512 and the shape-specific modified Beddoes-Leishman model with the angle of attack equal to the flow
 513 angle less the blade twist [22]. W_x is set to 0. At every time step, for each blade element in each
 514 blade, equations (1) to (2) are iterated until there is no change in the induced velocity vector. When
 515 the steady-state induced velocity vector is computed, it is corrected for the dynamic wake effect
 516 using the dynamic wake model [23]. The force coefficients are then recomputed to determine the
 517 unsteady forces at each blade element. The LR-uBEM model is customized and simulated for scaled
 518 rotor model unsteady simulations as per the experimental scenarios.

519 4. Results and discussion of unsteady test cases

520 Comprehensive static and unsteady experimental scenarios were performed and results were
 521 obtained for numerical evaluation and validation. For the unsteady experimental scenario cases, the
 522 last two cycles of six cycle surge motion simulation results were extracted for comparison and
 523 further analysis. This is to ensure that all the initial transient factors were eliminated. Results of CFD,
 524 LR-AeroDyn and LR-uBEM model computations were compared against the experimental results to
 525 comprehend their ability in predicting the aerodynamic forces due to unsteady effects. The variation
 526 in time mean thrust values of different numerical simulation methods would determine the
 527 capability and limitation to predict the unsteady aerodynamic loads on the scaled rotor. Albeit,
 528 thrust is the only significant parameter for the comparison between the numerical methods in this
 529 case (as the scaled rotor is designed against lift curve or thrust of full scale reference rotor), torque
 530 comparisons will further establish their capabilities.

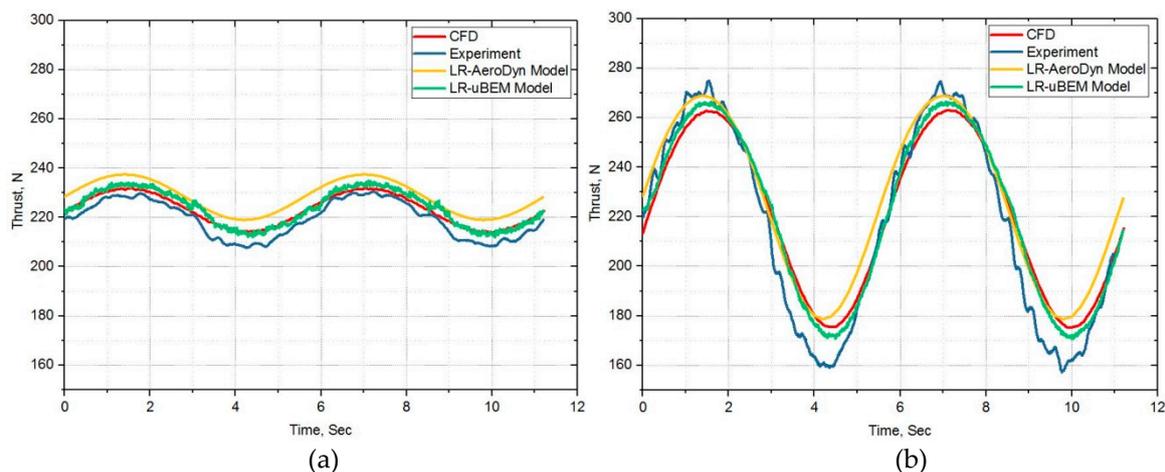
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532 4.1. Hydrodynamic thrust

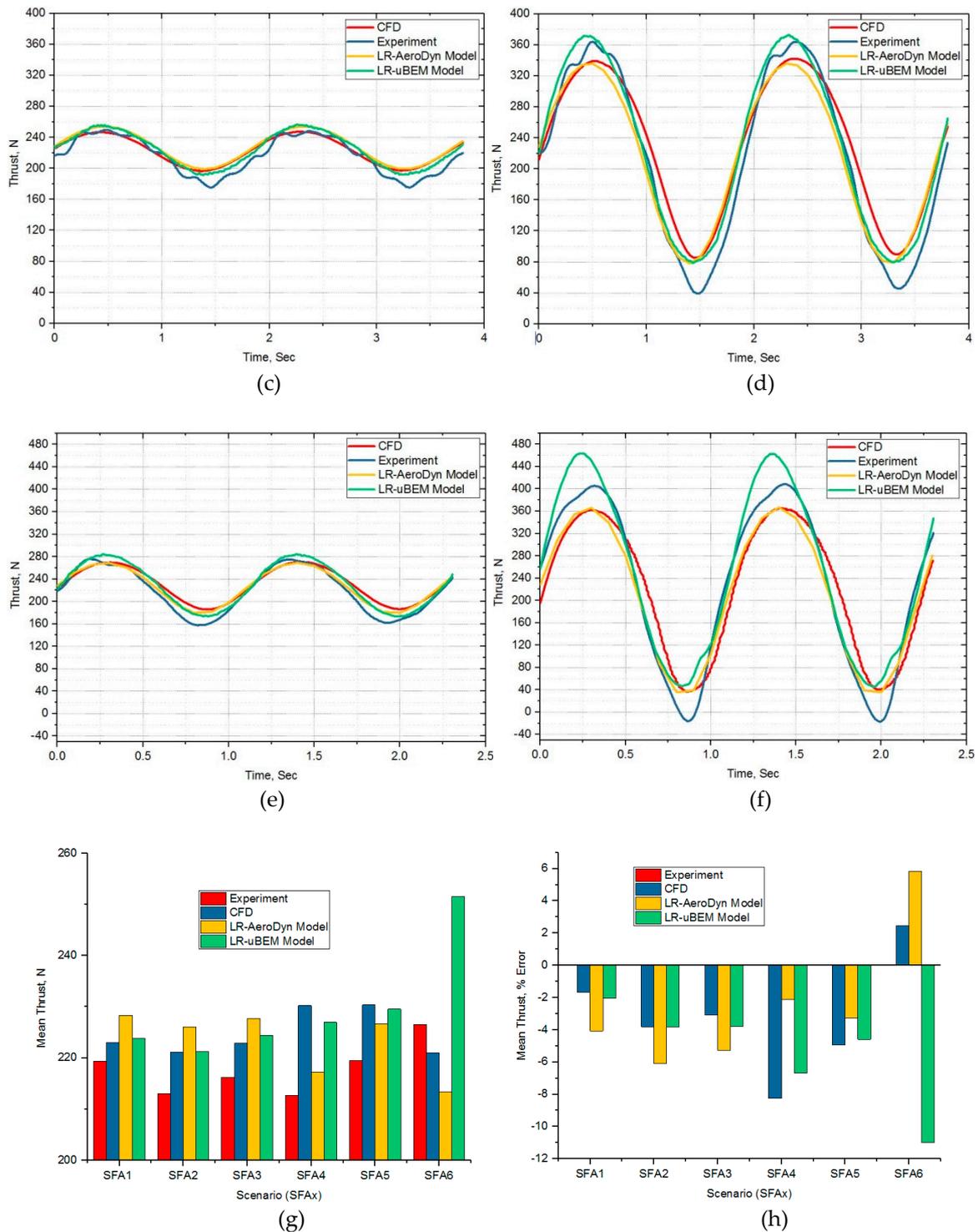
533 One of the main aerodynamic performance parameters is thrust force which is used for axial
 534 induction factor computation in BEM and unsteady based BEM methodologies. Hence, thrust force
 535 was chosen for the model evaluation and validation purposes. Moreover, the axial induction factor
 536 was used to predict the type of the wind turbine operating wakes states as well. Validity of BEM
 537 models are pretty much depending on wind turbine operating wake states and appropriate
 538 correction factors involved. A detailed investigation on thrust force prediction by numerical codes
 539 and comparison is made against the experimental prediction for 8.5, 7.0 and 6.0 TSR unsteady
 540 scenarios. For numerical simulation of the unsteady scenarios with LR-AeroDyn and LR-uBEM are
 541 typically taking a few minutes to complete each scenario, whereas it take 34 hours for the each CFD
 542 simulation cases with 36 core parallel processing computing workstation .

543 4.1.1. TSR 8.5 Scenario

544 In order to understand the unsteady flow behavior at the below rated wind speed which is
 545 about 16% lower than the rated wind speed (11.4m/s) of full scale FOWT, scaled rotor was
 546 subjected to experimental and numerical simulations at 8.5 TSR. With a constant angular speed of 14
 547 rad/s for the different prescribed surge amplitude frequency motions the experiments were carried
 548 out at a constant primary carriage motion of 0.824m/s. Owing to the unsteadiness triggered by
 549 prescribed surge motion, both thrust and torque fluctuate with time. Lower amplitude surge motion
 550 based numerical models were over predicting mean thrust force within 5% error against
 551 experimental results as shown Fig.14 h. Higher amplitude surge motion based numerical models
 552 were predicting mean thrust within 10% error except at the high surge frequency motion. Mean
 553 thrust slightly increases as surge motion frequency and amplitude increases. As in Fig 14 a-f,
 554 backward and forward motions in surge oscillations causing the maximum thrust to vary from
 555 almost 8-100% higher than the mean value while the minimum thrust is about 8-100% lower at TSR
 556 8.5. Its essential to consider the large difference between the extremes for structural stress and
 557 related fatigue issues during full scale design of wind turbines rotor and its pitching control for
 558 floating applications. The possible source of errors: 1) Experiments – It is estimated to be around
 559 2-4% error from various sources of uncertainties from measurement system, random error and
 560 systematic error as the model is very similar to [24] and yet to be quantified in detail 2) CFD –
 561 numerical discretization, error due to mesh deformation techniques and time step selection for high
 562 frequency and larger amplitude motions 3) LR-AeroDyn and LR-uBEM – Load computations are
 563 completely based on the design data of scaled 2D airfoil airfoil lift and drag data, not with scaled 2D
 564 airfoil experimental data and 3D correction errors. A detailed investigation is needed to quantify the
 565 uncertainties of these methods.
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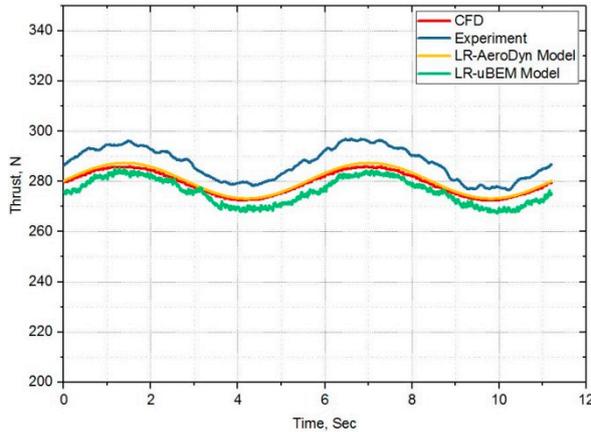
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579 **Figure 14.** TSR 8.5 Cases: (a) SFA1-Low f & lower A ; (b) SFA2-Low f & higher A ; (c) SFA3-Medium f &
 580 lower A ; (d) SFA4-Medium f & higher A ; (e) SFA5-High f & lower A ; (f) SFA6-High f & higher A ; (g) Mean
 581 trust-comparison for all TSR 8.5 cases; (h) Mean trust-percentage error comparison for all TSR 8.5 cases.

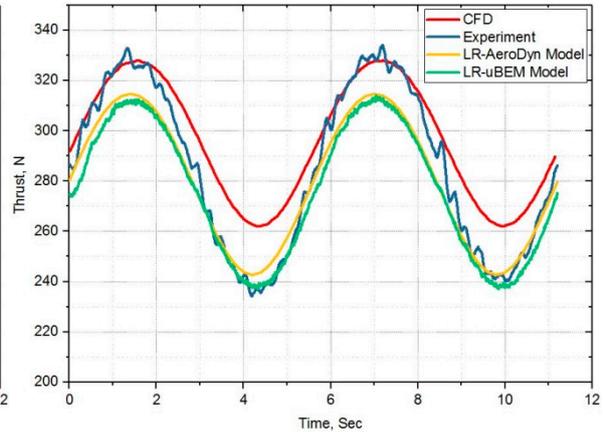
582 4.1.2. TSR 7 Scenario

583 In order to understand the unsteady flow behavior at the rated wind speed of full scale FOWT,
 584 scaled rotor is subjected to different prescribed surge amplitude frequency motions at 7.0 TSR, 14
 585 rad/s inside the tow tank water experimentally when the primarily carriage constant motion is 1m/s.
 586 The same scenario is simulated for all three chosen numerical simulation tools. Lower amplitude
 587 surge frequency motion based numerical models were predicting mean thrust force within 5% error
 588 against experimental results as shown Fig 15 h. Higher amplitude surge frequency motion based

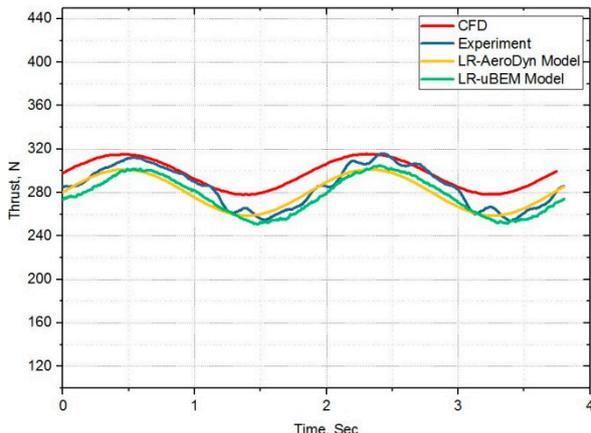
589 numerical models were predicting mean thrust within 5 % error except at the high frequency surge
 590 motion and close to 10 % error at higher amplitude scenario. In experiments, mean thrust gradually
 591 reduces as surge motion frequency and amplitude increases whereas mean thrust gradually
 592 increases in LR-uBEM. Mixed trend is found in both LR-AeroDyn and CFD. As in Fig 15 a-f,
 593 backward and forward motions in surge oscillations causing the maximum thrust to vary between
 594 4-110% higher than the mean value while the minimum thrust is about 4-110% lower at TSR 7.0.
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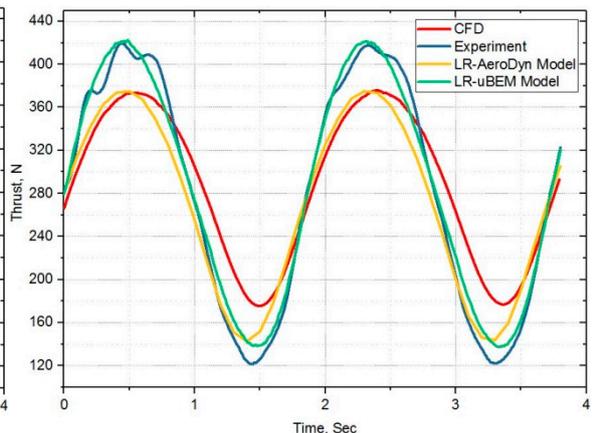
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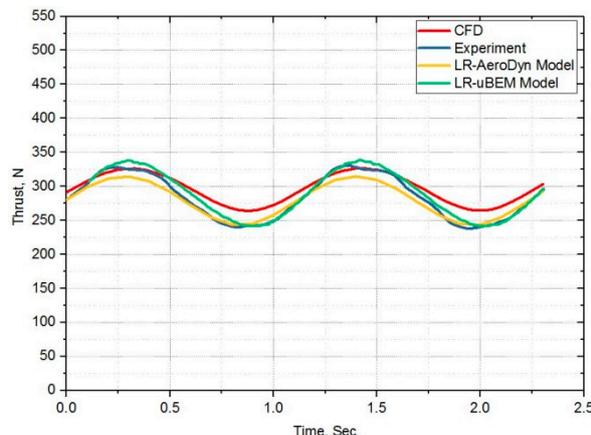
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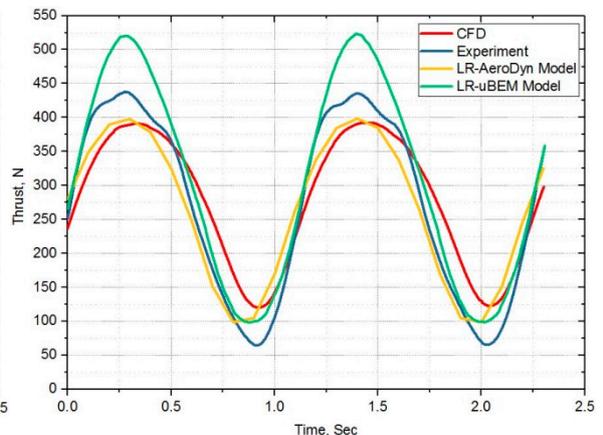
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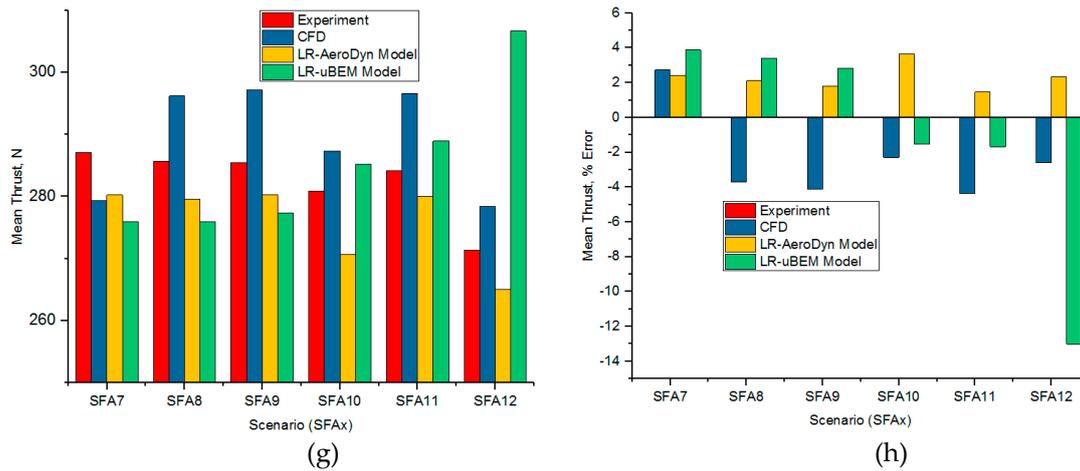


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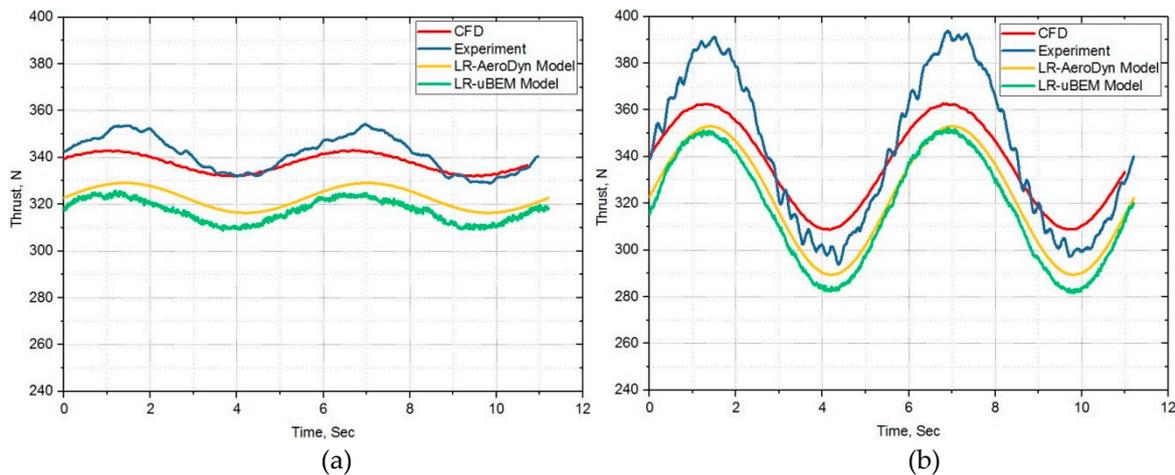
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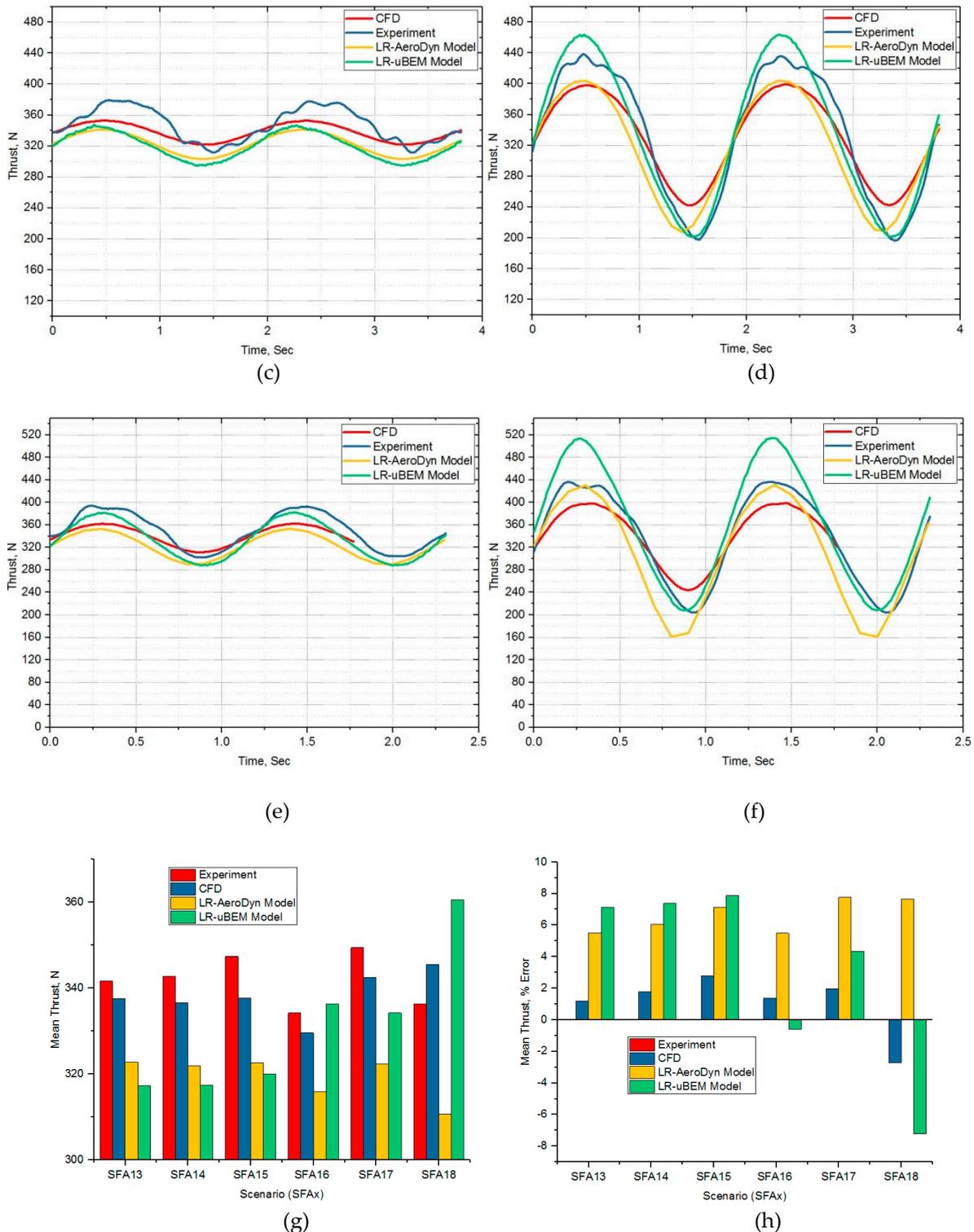
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610 **Figure 15.** TSR 7 Cases: (a) SFA7-Low f & lower A ; (b) SFA8-Low f & higher A ; (c) SFA9-Medium f & lower
 611 A ; (d) SFA10-Medium f & higher A ; (e) SFA11-High f & lower A ; (f) SFA12-High f & higher A ; (g) Mean
 612 thrust - comparison for all TSR 7 cases; (h) Mean thrust - percentage error comparison for all TSR 7 cases.

613 4.1.3. TSR 6 Scenario

614 In order to understand the unsteady flow behavior above the rated wind speed (13.2m/s), which
 615 is 16 % higher than the rated wind speed of full scale FOWT, scaled rotor is subjected to
 616 experimental and numerical simulations at 6.0 TSR, 14 rad/s for the different prescribed surge
 617 amplitude frequency motions when the primary carriage velocity is 1.167m/s. As shown Fig 16 h, all
 618 surge frequency motions were under predicting the mean thrust force within 8% error against
 619 experimental results except at the high frequency motion for higher amplitude scenario. Mean thrust
 620 slightly increases as surge motion frequency and amplitude increases. As in Fig 16 a-f, backward
 621 and forward motions in surge oscillations causing the maximum thrust to vary between 5-60%
 622 higher than the mean value while the minimum thrust is about 5-60% lower at TSR 6.0.

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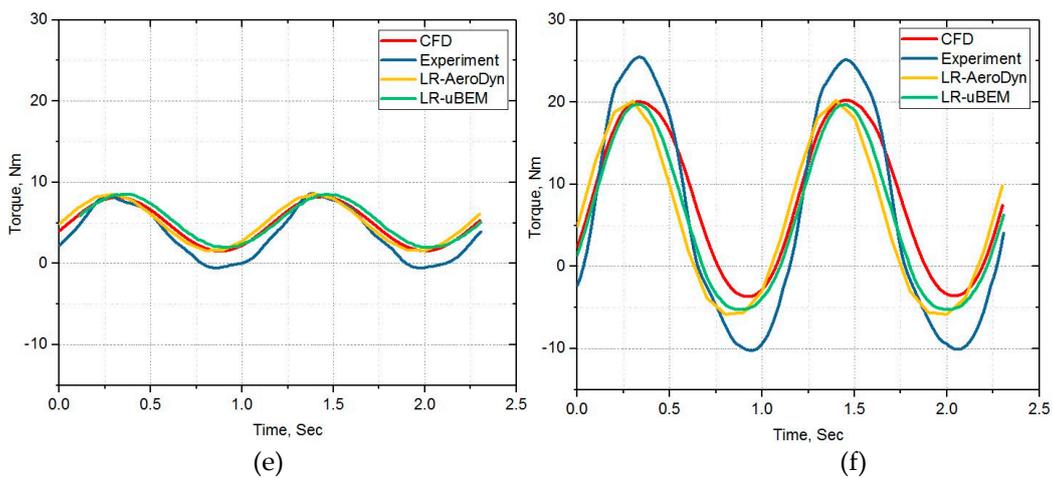
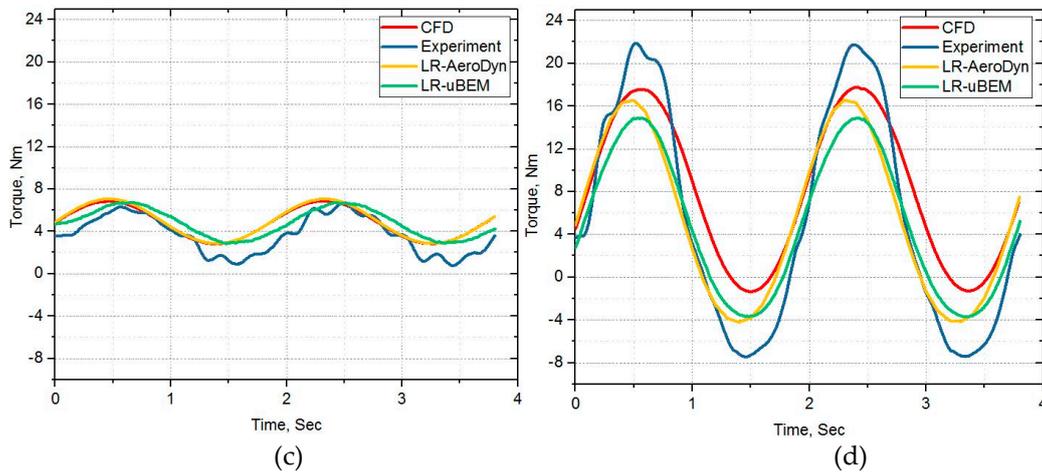
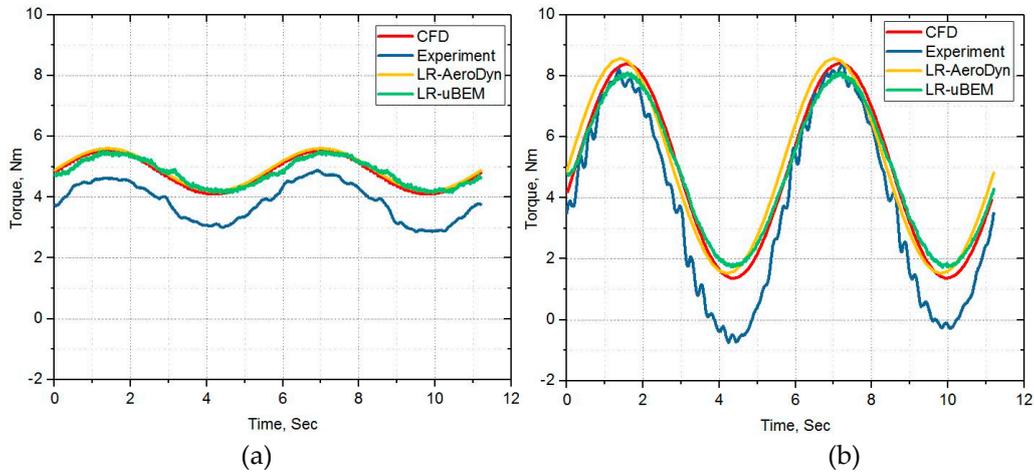
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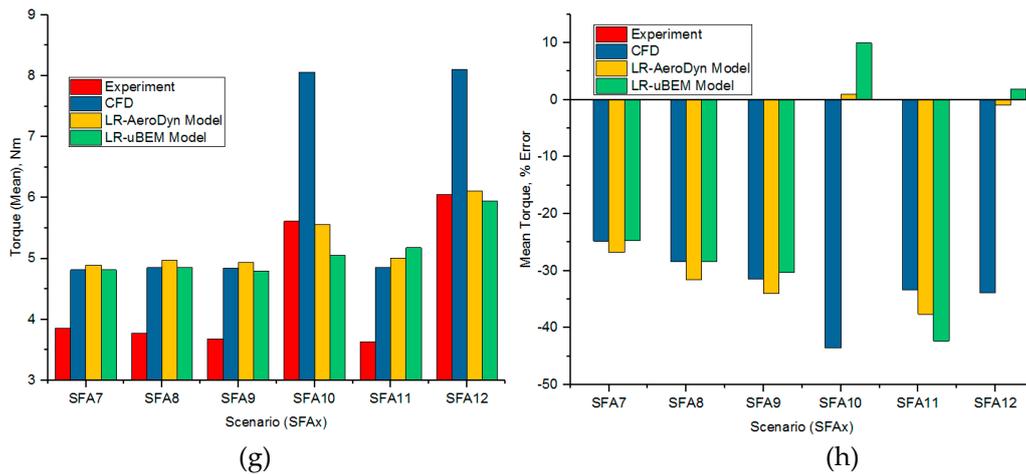
637 **Figure 16.** TSR 6 Cases: (a) SFA13-Low f & lower A ; (b) SFA14-Low f & higher A ; (c) SFA15-Medium f &
 638 lower A ; (d) SFA16-Medium f & higher A ; (e) SFA17-High f & lower A ; (f) SFA18-High f & higher A ; (g)
 639 Mean thrust-comparison for all TSR 6 cases; (h) Mean thrust-percentage error comparison for all TSR 6 cases.

640 4.2. Hydrodynamic torque comparison

641 As power is calculated from the torque values, the torque predictions are compared between
 642 the numerical models, though the scaled rotor design is based on the lift curve. In order to
 643 understand the torque characteristics at the operating wind speed (11.4m/s) of full scale FOWT,
 644 scaled rotor experimental and numerical model results were compared for the prescribed surge
 645 amplitude frequency motions at 7.0 TSR , 14 rad/s rotational speed at primary carriage constant

646 motion of 1m/s. Mean torque value predictions by all numerical models are close to each other, but
 647 differs by maximum of 45% error compared with experimental measurement. As in Fig 17 a-f,
 648 backward and forward motions in surge oscillations causing the maximum torque to vary between
 649 10-150% higher than the mean value while the minimum torque is about 10-150% lower at TSR 7.0.
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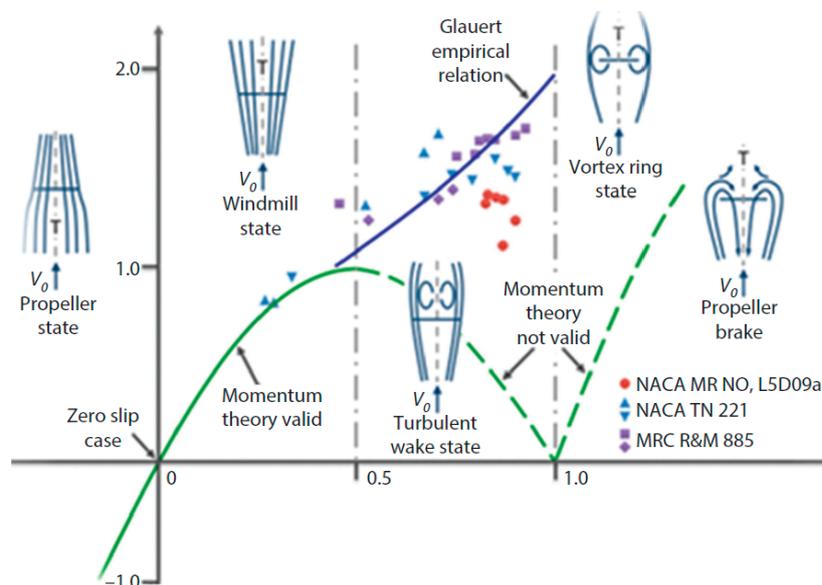
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662 **Figure 17.** TSR 7 Cases: (a) SFA7-Low f & lower A ; (b) SFA8-Low f & higher A ; (c) SFA9-Medium f & lower
663 A ; (d) SFA10-Medium f & higher A ; (e) SFA11-High f & lower A ; (f) SFA12-High f & higher A ; (g) Mean
664 torque - comparison for all TSR 7 cases; (h) Mean torque - percentage error comparison for all TSR 7 cases.

665 4.3. Evaluation of wind turbine operating state

666 As shown in Fig. 18, when the axial induction factor exceeds 0.4, the turbine rotor will no longer be in
667 wind mill state and will be operating in turbulent wake state until the induction factor exceeds 1. Two wake
668 states are predominantly developed during normal wind turbine operation based on the drop of the wind
669 speed in the wake. The primary state is the windmill state during medium to high winds, in which the rotor
670 follows the momentum theory with coefficient of thrust as indicated in the equation 9.

671



672

673 **Figure 18.** Axial induction factor Vs Thrust/thrust coefficient [25].

674 At lower wind speeds, the wind velocity between the freestream wind and the wake differs by a higher
675 magnitude. This leads to the low energy wake with recirculation leading to the turbulent wake state. The free
676 shear layer between the wake and freestream is unstable, producing eddies that carry momentum from the
677 freestream into the wake. Hence the BEM theory following the idealized momentum principle is not able to
678 predict the drop in the thrust force. As rated wind speed differs for each turbine, the occurrence of the turbulent
679 wake state can be represented by using an axial induction factor. Based on the experimental data shown in Fig
680 18, Glauert recommended an equation to model the relationship between C_t and axial induction factor in the
681 turbulent wake state.

682

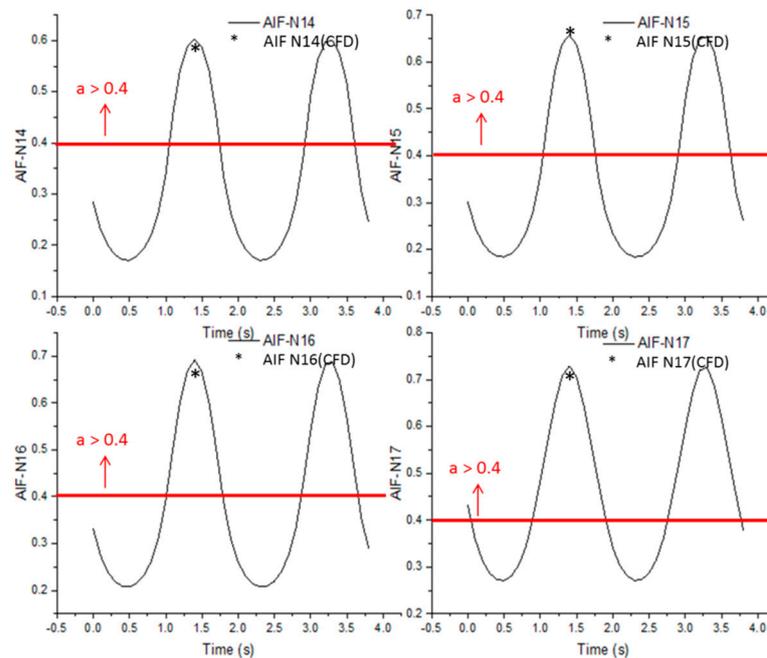
$$C_t = 4aF \left(1 - \left(\frac{1}{4} \right) (5 - 3a)a \right), a > \frac{1}{3} \quad (16)$$

683 where F is the tip-loss factor.

684 Even with the inclusion of F in (16), discontinuities nonetheless existed at $a = 0.4$ between the momentum theory
 685 and Glauert equation, at values of F other than 1. Correction has to be introduced as suggested by Buhl [26], in
 686 an equation 16, that can eliminate the discontinuities at $a = 0.4$ and have a value of $C_t = 2$ when $a = 1$, for all
 687 values of F .

$$688 \quad C_t = \left(\frac{8}{9}\right) + (4F - \left(\frac{40}{9}\right)a + \left(\frac{50}{9} - 4F\right)a * a \quad (17)$$

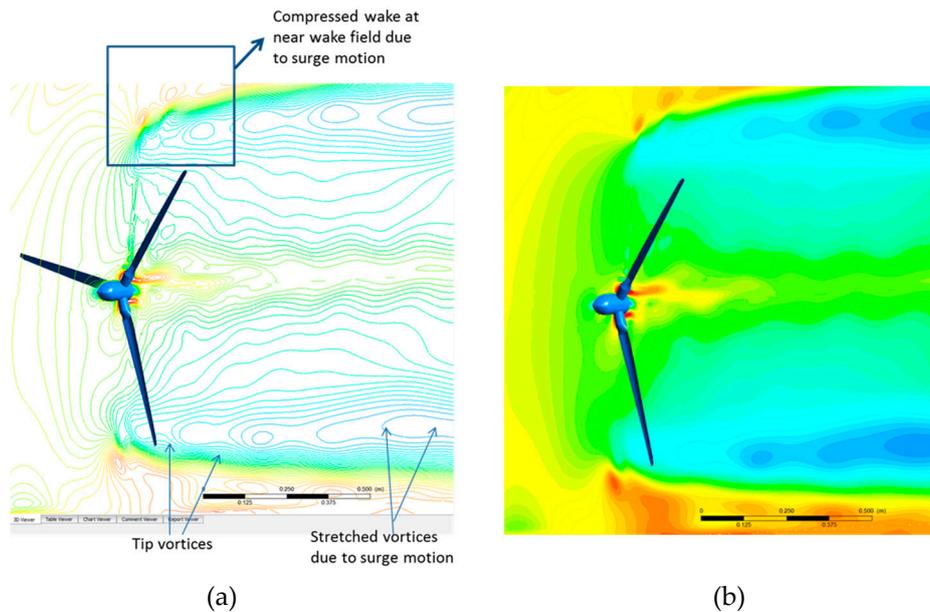
689
 690 The current study bolsters the fact that the surge cyclic motions are pushing the rotor under investigation
 691 to the turbulent wake state of SFA10 scenario as depicted in Fig. 19. From the scaled rotor blade element
 692 number 14 to 17 (the last four elements upto scaled rotor tip of total 17 elements as in Table 1), the turbulent
 693 wake state is clearly identified by the axial induction factor, a . CFD based induction factor derivation [6]
 694 is obtained at 1.25 sec of the last 2 cycles and compared against LR-AeroDyn model prediction as shown in Fig.19.
 695 LR-AeroDyn prediction is within 6% error on these elemental nodes when compared to CFD predictions.
 696 Hence, BEM based engineering models like LR-AeroDyn and LR-uBEM are able predict the surge motion
 697 responses on the rotor loading reasonably well.



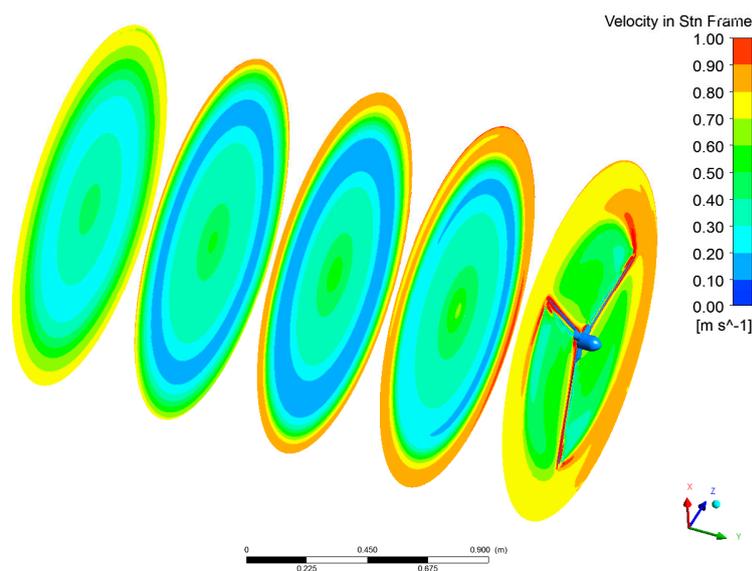
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 699 **Figure 19.** Axial induction factor of element 14-17 of the scaled rotor for the SFA10 scenario with LR-AeroDyn
 700 model simulation and corresponding point wise CFD based axial induction factor comparison at 1.25sec.

701
 702 CFD simulation results are exported to Ansys CFD Post (V16.2) to visualize the velocity and
 703 vorticity contour profiles. These profiles are plotted in Matlab, which clearly demonstrates how the
 704 scaled rotor is interacting with its own wake and the near wake distortion by surge motion
 705 frequencies. The Fig 20-21 show the velocity contour profiles. In addition, these contours display the
 706 surge oscillations behavior and corresponding rotor loading.

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710 **Figure 20.** SFA10 mean rotor position at the end of 6th cycle of surge motion, velocity (a) Line plot; (b)
711 contour plot showing tip vortices and compressed and elongated wake in the near wake field by CFD



712

713 **Figure 21.** SFA10 mean rotor position at the end of 6th cycle of surge motion, near wake field velocity
714 contour plots at 0.5m intervals from rotor plane in the rotating domain by CFD

715 5. Conclusion

716 The flow characteristics on a FOWT is a highly complex phenomenon as it is simultaneously subjected to
717 aerodynamic and hydrodynamic forces from wind and ocean waves. The study on sensitivity of the
718 aerodynamic behavior with respect to the changes in platform motion is indispensable, as small changes in
719 platform motion will be amplified due to the tower height. The current study focused on the investigation of
720 unsteady aerodynamic loading due to surge motion through various numerical codes. A scaled floating rotor
721 has been successfully designed with necessary instrumentation and imparted with hydrodynamic motions,
722 similar to a FOWT operating conditions. The experimental outcome is compared with CFD model results in
723 addition to the selected engineering simulation codes, LR-AeroDyn and LR-uBEM. Almost in all the selected
724 unsteady scenarios, numerical codes predict mean thrust values within 10% error level against the experimental
725 results. Backward and forward motions in surge oscillations leading to the maximum and minimum thrust
726 variation in the range of 4% to 110% from mean thrust. The detailed CFD visualization of complex flow field
727 around the rotor unfolded the fact that the windmill changes its operating state due to the strong interaction of

728 rotor with its own wake instantaneously at higher amplitudes and surge frequencies. Though LR-AeroDyn is
729 equipped with quasi-steady state BEM method, utmost care has to be dedicated when using for higher surge
730 frequencies and amplitudes. LR-uBEM code predicts comparatively well at higher surge frequencies and
731 amplitudes as it is based on dynamic in flow modeling methods, yet variation of 10-15% do exist in some cases.
732 Turbulent wake state of wind turbine operation is identified and compared against CFD based induction factor
733 derivation.

734 6. Future work

735 The computational mesh quality will be further refined around near wake regions with smaller time steps
736 for accurate predictions of unsteady rotor loading results at higher frequency surge motions. Time history of
737 velocity and vorticity data from CFD will be exported to Matlab for enhanced visualization of wake
738 interactions. Lift and drag co-efficient of scaled rotor airfoils will be experimentally obtained to improve the
739 LR-AeroDyn and LR-uBEM model accuracy. A detailed investigation will be performed to quantify the
740 uncertainty analysis for these methods. The numerical models will be further refined for full scale 5MW NREL
741 turbine at its operating conditions of TSR, surge frequencies and amplitude and will be compared with scaled
742 rotor results. The computed results will be used in digital twin approach, in which the remaining useful life of
743 key components such as power converters will be predicted. The proposed approach will curtail the
744 maintenance and inventory cost especially for FOWT.

745 **Author Contributions:** “CFD and LR-AeorDyn, Krishnamoorthi Sivalingam; Scaled Rotor Design,
746 Development and Tow Tank Steady and Unsteady Experiments, Steven Martin.; LR-uBEM, Abdulqadir Aziz
747 Singapore Wala”.

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751 **Conflicts of Interest:** Declare

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