

1 Article

2 Development of Lumped Parameter Model for an 3 Aeronautic Hybrid-Electric Propulsion System

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13

14 **Abstract:** This paper describes a case study for applying of hybrid-electric propulsion system for a
15 general aviation aircraft. The work was performed by a joint team of CIRA and the Department of
16 Industrial Engineering of the University of Naples "Federico II". Electric and hybrid electric
17 propulsion for aircraft has gained widespread and significant attention over the past decade. The
18 driver for industry interest has principally been the need to reduce emissions of combustion engine
19 exhaust products and noise, but increasingly studies revealed potential for overall improvement in
20 energy efficiency and mission flexibility of new aircraft types. The project goal was to demonstrate
21 feasibility of aeronautic parallel hybrid-electric propulsion for a Light aircraft varying the mission
22 profiles and the electric configuration. Through a creation, and application, of a global model, with
23 software AMESim[®], in which it can be represented everything about the components chosen by the
24 industrial partners, some interesting considerations are carried out.

25 In particular, it was confirmed that with the only integration of state of the art technologies, for some
26 particular missions, the advantages of aircraft hybrid-electric propulsion, for light aircraft, are
27 notable.

28 **Keywords:** lumped parameter simulation; aircraft hybrid propulsion; fuel economy; propulsion and
29 propellant systems.

30

31 1. Introduction

32 The aviation industry is responsible for 12% of the total transportation impact of CO₂ while
33 awareness, for decreasing the total carbon footprint, is rising. Both the aerospace and the automotive
34 industry are facing an increasing pressure from society to make the transportation sector more
35 sustainable. Within the automotive industry slowly an increase in electric vehicles can be noticed
36 (<1%). Also in the aerospace industry, a rise in electrification can be seen, with small aircraft as the E-
37 Star and E-Fan [1] (two seaters) as commercial examples. Electrification of the transportation sector
38 could further result in a decrease in noise and an increase in lifespan of parts as vibrations are
39 decreased.

40 This research is focused on the study of aeronautical hybrid-electric propulsion to analyze the
41 consumption and emissions saving compared to a benchmark ICE. The request of greener
42 propulsive systems for a/c is dictated by near future target in terms of air pollution and noise.
43 Currently, aviation is responsible of a considerable part of CO₂ introduced in the atmosphere with

44 about 12% as clear reported by National Geographic on 2015 [2]. The aircrafts emitted about 700
45 million tons of the CO₂, during the 2013. [2] estimated that, without any changes, this number will be
46 tripled by 2050. Another interesting study has been carried out by the British Airways [3]. The local
47 quality of air near airports presents a high concentration of NO_x and CO, this concentration is
48 regulated by the UE Directive. The aircrafts electrification would represent the best option to reach
49 the ideal “clean” and high efficiency mobility. For this reason, during the recent years, the electric
50 traction has been applied to achieve noise and emission reductions. The electrical technology has
51 developed new systems to improve the velocity and autonomy, however, the electrification of
52 aircrafts has many obstacles due essentially to the battery pack and them density of energy. The target
53 of many studies is focused on the buildup of the specific density of the batteries to support the
54 modern electric machines for a greater endurance in the time.

55 Hence, the full replacement of the fossil fuel with green energies is impossible in the near future
56 and, consequently, different technological solutions to reduce the environment impact due to
57 emissions must be applied. For this reason, the European Union has established a program called
58 Clean Sky which is the largest European research program to develop innovative cutting-edge
59 technology aimed on the reduction the environmental and noise emissions due to the aeronautic
60 vehicles.

61 On this scenario, the hybrid propulsion technology represents a great solution for the near
62 future. Hybridization consists of a mechanical coupling, in series or in parallel, of an internal
63 combustion engine with an electric machine connected to a battery system; where the ICE is the
64 principal powering engine. The use of two different type of propulsions allows to benefit of the
65 advantages and to compensate eventually issues of each engine. In this way, the power-unit get a
66 higher efficiency. The hybrid propulsion systems are claiming themselves in the transportation sector
67 with a great success by exploiting the best of the thermal power with the integration of electrical
68 power causes a consequently reduction the total pollution. This reduction, however must be
69 maximize if compared with the normal propulsion system.

70 It is known that the specific energy of liquid fossil fuel is fifty times more than batteries.
71 Therefore, in the study of a hybrid architecture this aspect must be considered.

72 M. Cui et al. [4] have modelled, simulated and optimized the operation of an aeronautic hybrid-
73 electric system close to our project. The electric machine is located on the same shaft of the internal
74 combustion engine; therefore, both rotate at the same speed. Then the shaft is connected to the
75 propeller. In the 2012, Joseph K. Ausserer and Frederick G. Harmon [5] have simulated and
76 prototyped a hybrid-electric system for a small airplane remotely piloted. The little airplane is
77 powered by the ICE of Honda GX 35 (of 35 cm³), with a power of 0.97 kW at 7000 rpm and the electric
78 motor AXI 4130/20, with a power of 0.64 kW, powered by the battery 6xTP3300-4S (Lithium polymer,
79 0.248 kWh). In the 2014, C. Friedrich e P.A. Robertson [6] have also simulated and prototyped a
80 hybrid-electric system for an ultra-light aircraft. The plane is the SONG, developed by Gramex Ltd,
81 usually equipped with a Bailey V5 (of 200 cm³) capable of delivering up to 15 kW. The Bailey engine
82 has been replaced with the Honda GX160 (of 7,5 kW at 7000 rpm in 12 kg) connected with a DC
83 brushless JM1 of the Joby Motors (of 12 kW in 2,8 kg), able to work also as generator to recharge the
84 battery.

85 This paper is focused on the hybridization of an ultra-light aircraft the “Tecnam P2010” [7]. The
86 Tecnam P2010 is usually equipped with the engine IO-360-M1A (powered by AVGas 100LL), built
87 up by AVCO Lycoming [8]. The engine has four opposing cylinders, air cooled, with a maximum
88 power of 130 kW and a displacement is of 5900 cm³. The total weight when installed on the ultra-light
89 aircraft is of 190 kg. The Tecnam P2010 has been completely modified in the hybridization process,
90 replacing the Lycoming engine with CMD 22 that has a reduced weight and size and adding an
91 electrical machine, which can also function as generator, and a battery pack [9-10]. The CMD 22, has
92 four cylinders in a boxer configuration with a displacement of 2200 cm³, a maximum power of 102
93 kW and a total weight is 82 kg [11].

94 The sizing and the choice of each component has been done using a numerical approach with
95 the commercial code AMESim®, developed by Siemens®. Then the model results have been compared

96 with the performance of the baseline configuration. For this reason, a model of the baseline
 97 propulsion system has been also built up. The simulations highlight a fuel saving over the 12% for
 98 the training profile and amount the 6% for the cruise profile.

99 2. The hybrid-electric propulsion system description

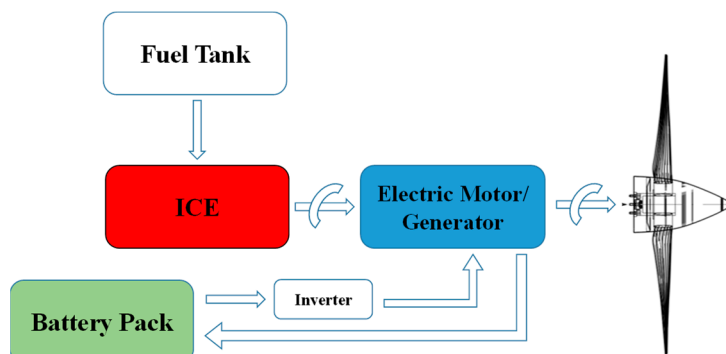
100 Since the aim of the research is to demonstrate the feasibility of hybrid electric propulsion for an
 101 ultra-light aircraft the study has been conducted on an aircraft already available on the market and
 102 powered by a conventional internal combustion engine. The research carried out shows that a hybrid-
 103 electric solution is optimal for this aircrafts category to reduce both emissions and fuel consumption.

104 The analyzed ultra-light aircraft is, as said in the introduction, the Tecnam P2010 that is usually
 105 equipped with the IO-360-M1A (powered by AVGas 100LL), built up by AVCO Lycoming. The IO-
 106 360-M1A has four opposing cylinders, air cooled with a maximum power of 130 kW and a
 107 displacement is of 5900 cm³. The total weight is of 135 kg while when installed the weight becomes
 108 of 190 kg. Therefore, the hybrid-electric motor must have the same power and the same weight to be
 109 proposed as alternative to the ICE.

110 The hybridization of the engine consists on the introduction of a smaller ICE combined with an
 111 electric machine an inverter and a battery pack

112 2.1. The hybrid-electric configuration, system propulsion scheme and hybridization grade

113 A parallel hybrid-electric architecture has been chosen after an accurate analysis of the various
 114 configuration alternative. With a parallel architecture the internal combustion engine is chosen to
 115 ensure the power required for cruise, while the electric motor intervenes at the stage where maximum
 116 power is required (take-off and climb). The internal combustion engine, in this way, can operate at
 117 minimum specific consumption (maximum efficiency) during the cruise, using the electric machine
 118 as generator to recharge the battery pack. The layout of the chosen architecture is presented in figure
 119 1.



120
 121 **Figure 1.** Layout of hybrid propulsion system.

122 As shown in figure 1, the electric motor/generator and the internal combustion engine are linked
 123 to the same shaft, working at the same speed. The rotating speed of both motors is reduced with ratio
 124 of 2:1 before the propeller. This configuration allows a remarkable saving of weight, because both
 125 motors are located in a one single block.

126 Each component of the system has been accurately chosen considering that the hybrid-electric
 127 solution must cover the aircraft requests and replace the original propulsion, the Lycoming IO-360-
 128 M1A.

129 The internal combustion engine chosen in this research is the CMD 22, manufactured by and
 130 Italian company CMD-engine. The CMD 22 is a positive ignition engine for ultra-light aircraft
 131 (Maximum Take-Off Mass of 1200 kg), powered by an automotive fuel with four cylinders in boxer
 132 configuration; the displacement is of 2200 cm³ while the maximum power is of 102 kW. The total
 133 weight is of only 82 kg.

134 The injection system (direct injection) is made by two electric injectors, placed on the aspiration
 135 manifold of each cylinder, and by two ignition candles. Cylinders are opposite horizontally, closed

136 in one block in which the camshaft manages the four intake and exhausts valves for each cylinder. In
 137 figure 2, the main features of the CMD 22 are listed.



Architecture	4 Cylinder Box
Bore	100 [mm]
Stroke	70 [mm]
Displacement	2200 [cm ³]
Compression Ratio	10.5
Naturally Aspirated	
Valves\Cylinder	4
Fuel Injection System	Indirect Electronic Injection System Multi Point
Fuel	Gasoline
EECS	SINGLE FADEC EDU
Alternator	14 [V]
Cooling System	Air/Oli
Dry Weight	82 [kg] - with Gearbox
Dimension L*W*H	638*328*372 [mm] - with Gearbox
Take Off Power	90 [kW] - At the Propeller Shaft (122 Hp)
Continuous Power	74 [kW] - At the Propeller Shaft
Min. BSFC	285 [g/kWh] - At the Propeller Shaft

138

139

Figure 2. Features of the internal combustion engine: CMD22.

140 Since the propeller must work at 2700 rpm, both engines will run at about 5500 rpm. At this
 141 rotation speed the internal combustion engine CMD 22 gives 90 kW while the other 35 kW comes
 142 from the electric, replacing the performance of the original propulsion.

143 Another important aspect is, as said, the overall weight of the entire system that must be below the
 144 135 kg, weight of the Lycoming IO-360-M1A engine. For this reason, since the engine CMD 22 has a
 145 weight of 82 kg, the total weight of the electric machine, the battery and the control systems have to
 146 be of about 65 kg.

147 Today, there are in production some ultra-light motors with the kW/kg ratio equal to 5. In any
 148 way, considering a little motor of 6-8 kg the control systems and the auxiliaries, the maximum weight
 149 for the battery pack is of 55 kg.

150 The total weight of the aircraft can be reduced of about 15 kg by using the electric machine also
 151 as starter motor. Another important aspect that must be considered in the choice of the EM is its
 152 capacity to run under several operative conditions, as indicated in the table 1.

Table 1. Starter torque in function of different temperature conditions

Temperature [°C]	Starting Torque [Nm]
-10	216
-20	523
-25	761
-30	1047
-40	1593

153 EMs for the aeronautical application must respect many other peculiarities. There are in
 154 literature examples of a full-electric aircraft [12-13] where it has been demonstrated the real
 155 applicability of HTS (High Temperature Superconducting). HTS motors have, in fact, high density of
 156 power and lower dimension respect to the traditional motors. On the other hand, it is requested, for
 157 these electric machines, to work at low temperature (of about 50 K), to operate at the best
 158 performance. Therefore, their application requests an efficient cooling system. Despite the cooling
 159 system, the motor has been installed with a cryocooler of 60 kg, but in general the weight has been
 160 reduced. The cryocooler can produce cryogenic gas able to maintain the superconductor temperature
 161 low. This weight saving can be used to grow up the aircraft's autonomy with many batteries.

162 There are available on the market many motors that fit with our project. The final choice is the
 163 EMRAX 208 [10] manufactured by ENSTROJ. This EM is an axial flux synchronous permanent
 164 magnet motor/generator, sinusoidal three phases motor.

165 Main features of the EMRAX 208 motor are listed in table 2.

Table 2. Technical data - EMRAX 208

Technical data - EMRAX 208 High Voltage	
Air cooled	AC
Air Flow = AF, Ambient Air = AA	AF=20m/s; AA=25°C
Weight	9,1 [kg]
Diameter \varnothing / width	208 / 85 [mm]
Maximal battery voltage and full load/no load RPM	470 [Vdc] (5170/7050 RPM)
Peak motor power at max RPM	80 [kW]
Continuous motor power	20 – 32 (at 3000-5000 RPM)
Maximal rotation speed	6000 (7000 peak) [RPM]
Maximal motor current	200 [Arms]
Continuous motor current	100 [Arms]
Maximal peak motor torque	150 [Nm]
Continuous motor torque	80 [Nm]
Motor efficiency	92-98%
Internal phase resistance at 25 °C	12,0 [m Ω]
Wire connection star Induction Ld/Lq	125/130 [μ H]
Controller / motor signal	sine wave
AC voltage between two phases	0,0487 [Vrms/1RPM]
Magnetic flux – axial	0,0393 [Vs]
Number of pole pairs	10
Rotor Inertia (d=160mm; m=4,0kg)	256 [kg*cm ²]

166

167 The hybridization factor (HF) of the hybrid-electric propulsion under investigation has been
 168 defined after the choice of the ICE and the EM. As know, there are three categories of hybridization:

- 169 • Full Hybrid (also called full hybridization): the electric system is able to move the aircraft by
 170 itself on a normalized guide cycle, without the battery support ($HF > 0.38$),
- 171 • Mild Hybrid (also called light hybridization): the full-electric is not able to follow all the
 172 guide cycles ($0.23 < HF < 0.38$),
- 173 • Minimal Hybrid: lower distance done in pure electrical mode ($HF < 0.23$).

174 The HF is obtained by the following expression:

$$HF = \frac{P_{EM}}{P_{ICE} + P_{EM}} = \frac{P_{EM}}{P_{TOT}} \quad (1)$$

175 Where P_{EM} is the power coming from the electrical system and P_{ICE} is the rate from the internal
 176 combustion system. The HF follows in the range [0 ÷ 1] where respectively zero indicates a
 177 conventional endothermic vehicle and one is a full-electric vehicle. In our case, the HF assumes a
 178 value of 0.26 because 32 kW of power comes for the electric motor and 90 kW from the internal
 179 combustion engine. For this reason, the system falls in the light hybridization category since the
 180 electric motor cannot operate alone at any stage of a normalized cycle.

181 The main components of the proposed hybrid-electric propulsion system have been selected
 182 mainly for their performance and weight. In the next paragraph, a numerical model of the entire
 183 propulsion system is described. The model has been built up using the lumped parameter code

184 AMESim LMS® (developed by Simerics®) [14]. The numerical model has been then used for predicting
 185 the performance of the overall system to allow the assessment and the validation of the control
 186 strategies. Each part of the propulsion has been included in the model divided in: mechanical
 187 elements, signals, propeller, mission profiles, EM and ICE.

188 3. Lumped parameter model/ Model assumption

189 The structure of the lumped parameter numerical model used for the simulation of the hybrid-
 190 electric propulsion system is shown in figure 3. The hybrid propulsion of the ultra-light aircraft has
 191 been modelled splitting the system in five units:

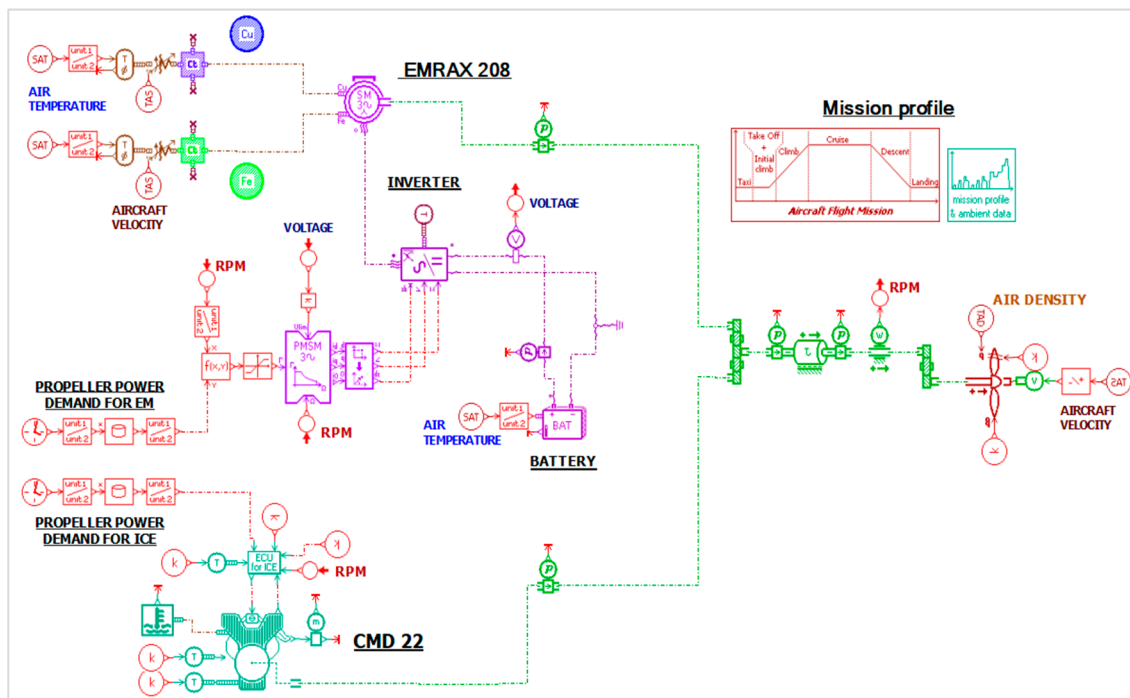
- 192 - The internal combustion engine,
- 193 - The electrical components. This sub-model includes the electrical machine.
- 194 - The cooling system,
- 195 - The propeller
- 196 - Mission profiles.



197

198 **Figure 3.** Structure of the lumped parameter model of the Hybrid-Electric Propulsion System.

199 Each unit, of figure 3, has been modelled using the commercial code AMESim® developed by
 200 Siemens®. The entire model of the hybrid-electrical propulsion system is shown in figure 4.



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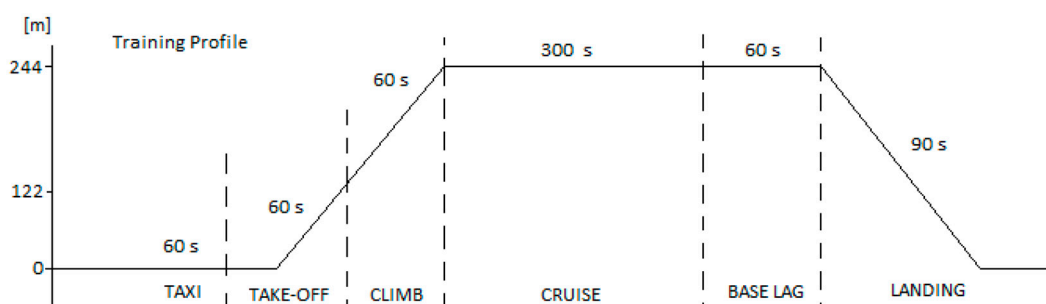
Figure 4. The complete model of the Hybrid-Electric propulsion system.

203 Form figure 4, the five sub-systems of the entire propulsion unit are clearly shown. Before
 204 running simulation, the input parameters to the numerical model have been defined. Two important
 205 parameters are the mission profiles (training and cruse) and the flight speed.

206 The main goal of the modeling task is to build a tool able to estimate performances of the hybrid
 207 system for each mission profile. Mission profiles and the flight speed assigned are described by
 208 following in this paragraph.

209 3.1 Training profile

210 As said, before describing the model result, the input to the model must be defined. Input are
 211 the mission profiles and the flight speed of the aircraft. The "training" is one of the mission profiles
 212 analyzed in this paper. It is composed by segments repeated more times. In fact, excluding take-off
 213 and the taxi segments that happen just one time, the others are repeated interspersed with "touch
 214 and go" phases for climbing again. For this reason, this mission profile is also called "touch and go"
 215 profile. The training profile is clearly shown in figure 5.



216

217

Figure 5. Training Profile.

218 Depending on the battery energy storage capability, the aircraft can do several "touch and go"
 219 as show in the table 3.

Table 3. Training Profile

Phase	Time [s]	Altitude [m]	Power at propeller [kW]
Take-off	60	122	122 (90 ICE + 32 EM)
Climb	60	244	103 (80 ICE + 23 EM)
Cruise	300	244	68 (60 ICE + 8 EM)
Base leg	60	244	23 (35 ICE – 12 GEN)
Landing	90	0	23 (35 ICE – 12 GEN)

220 In the table 3, the power available at the propeller has been split in the contribution of the internal
 221 combustion engine and of the electric machine. During the take-off both motors must work at the
 222 maximum power with consequently less power from the EM during the climb and a little bit during
 223 the cruise (with just 8 kW). Only during the base leg and the landing phases, the internal combustion
 224 engine is the one drives the propeller; part of the ICE power goes also to recharge the battery. As
 225 said, the internal combustion engine gives 35 kW this means that, during the base leg and the landing
 226 were only 23 kW are requested, the other 12 kW goes to the generator (1/3 of its maximum power).

227 The last parameter requested for the simulation is the flight velocity during the training mission
 228 profile. Speed values for each phase of the mission profile are listed in table 4. These data have been
 229 given by company Tecnam, the manufacturer of the aircraft under investigation.

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232

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Table 4: Flight velocity during the training profile

Phase	V_0
Take-Off	45(m/s) = 88 knots
Climb	41.15(m/s) = 80 knots
Cruise	61.7(m/s) = 120 knots
Base Lag	31(m/s) = 60 knots
Landing	36(m/s) = 70 knots

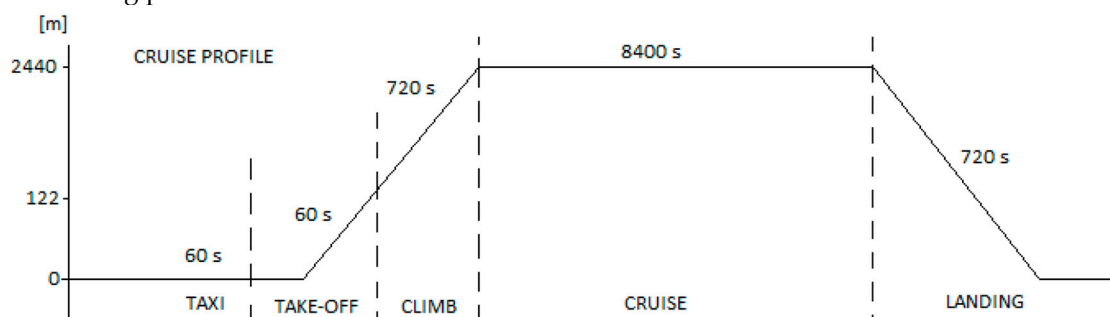
234 3.2 Cruise Profile

235 The cruise profile is completely different from the training. In fact, there is a single cycle during
 236 which the maximum power has to be guaranteed from the internal combustion engine for all the
 237 cruise phase and a minimum recovery goes to the electric machine that works like generator.

Table 5 Cruise Profile

Phase	Time [s]	Altitude [m]	Power at propeller [kW]
Take-off	60	122	122 (90 ICE + 32 EM)
Climb	720	2440	93 (70 ICE + 23 EM)
Cruise	8400	2440	88.5 (90 ICE – 1.5 EM)
Base leg	720	0	23 (25 ICE – 2 GEN)
Landing	60	122	122 (90 ICE + 32 EM)

238 The cruise profile, as shown in both table 5 and figure 6, consists of four segments. The first one
 239 is the take-off that last 60 s, then the climb with 720 s and the main part the cruise segment (8400 s).
 240 By the end, the landing (duration of 720s); therefore, for this profile, there are no touch and go as for
 241 the training profile.



242

243

Figure 6. Cruise Profile.

244 As done for the training profile, also for the cruise the flight speed need to be insert as input to
 245 the numerical model. Data have been supplied by company Tecnam, [7] the manufacturer of the
 246 aircraft. During the take-off segment the aircraft has a speed of 88 knots, then, during the climb the
 247 speed is of 88 knots and becomes 120 knots in the Cruise segment. Landing, the last phase, last 70 s
 248 at 70 knots.

Table 6. Flight velocity during the cruise profile

Phase	V_0
Take-Off	45(m/s) = 88 knots
Climb	41.15(m/s) = 80 knots
Cruise	61.7(m/s) = 120 knots
Base Lag	31(m/s) = 60 knots
Landing	36(m/s) = 70 knots

249 As said, the entire numerical model of the propulsion includes five sub-parts. One of them
 250 concerns the electrical part where the battery is one of the main components. Therefore, before
 251 running simulation an accurate study has been performed to choose the best battery pack for the
 252 specific application.

253 3.3 Battery

254 The choice of the battery pack is crucial in this project because it has to satisfy several
 255 requirements imposed by the mission profiles already described. However, there are other two
 256 important aspects to consider: the weight and volume limits [15-16].

257 The battery must be able to deliver current (at a specific intensity and voltage) to the electric
 258 motor for giving the power required. Therefore, the choice of cells number does not depend only on
 259 the weight but also on the current that can be delivered and on the reduction of the voltage. Several
 260 typologies of cells available on the market, and for this project the lithium-polymer has been chosen
 261 for the great specific energy. A great specific energy means that, with the same energy required, these
 262 batteries have minor mass. As said the battery pack would be able to guarantee two different mission
 263 profiles (training and cruise). Where, the energy that the battery has to storage for only one training
 264 profile is of 1.58 kWh while for the cruise profile is of 5.13 kWh.

265 The battery capacity for the training profile, has been defined considering the maximum voltage
 266 that the electric motor can accept by the battery, namely 500V. Therefore, it assumes the value of
 267 almost 16 Ah.

268 The final choice for the battery pack were the Superior Lithium Polymer Battery SLPB78205130H
 269 of KOKAM, South Korea's leading manufacturer of lithium-polymer.

270 The feature of the Kokam battery cells are listed in table 7.

Table 7: Summary table of battery chosen

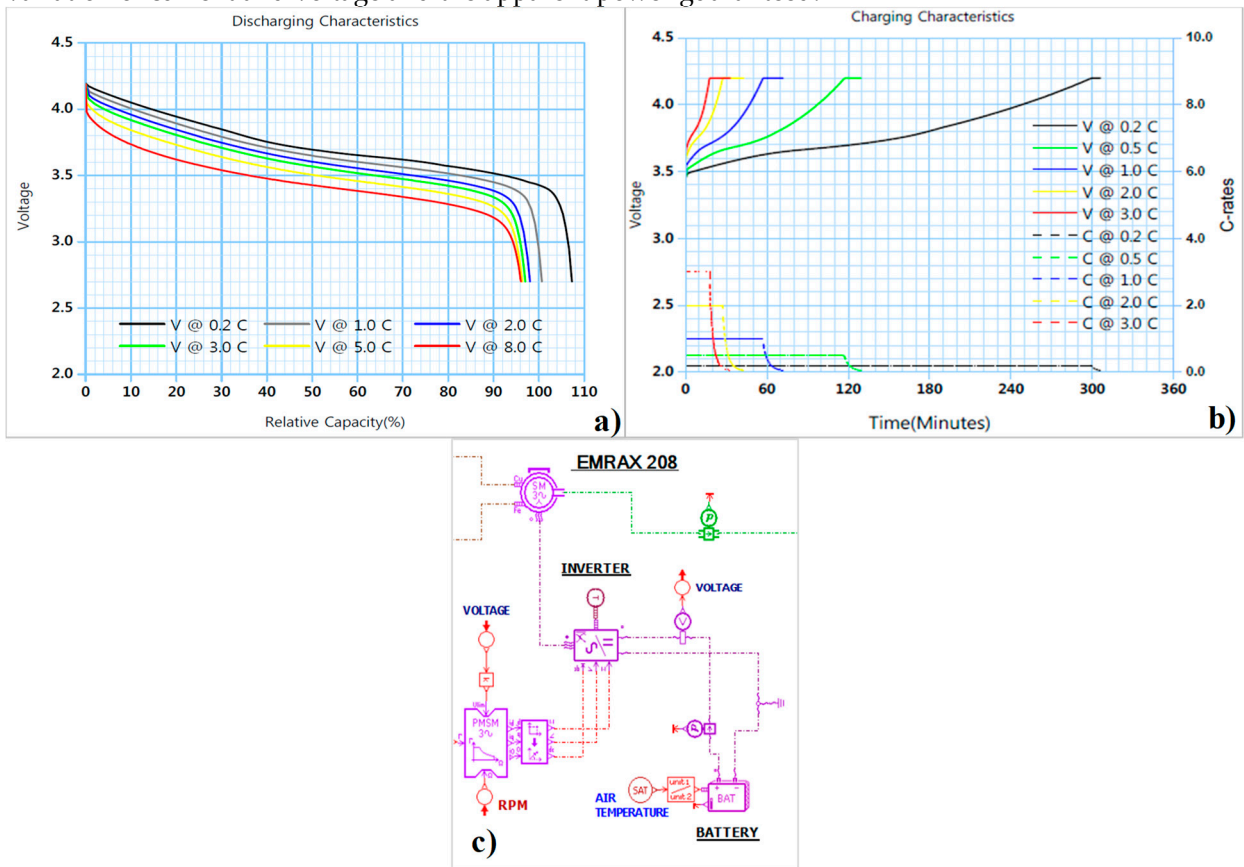
Items	Specification		Remarks
Rated Capacity	16 Ah		Charge @0,2C, 23 ± 3 °C Discharge@0,2C, 23±3 °C
Energy Density	Gravity	146 Wh/kg	Excluded tab and seal
	Volume	359 Wh/l	
Internal Resistance	Max. 1,1 mW		AC @ 1kHz
Weight	Max. 406g		
Cell Dimension [Maximum]	Width	217 mm	Unfolded
	Length	137 mm	Excluded tab length
	Thickness	7,5 mm	3,7 ± 0,1V
	Average	3,7 V	
Voltage	Lower Limited	2,7 V	
	Upper Limited	4,2 V	
Current [Maximum]	Charge	Cont. 48,0 A (3C)	23±3 °C
	Discharge	Cont. 128,0 A (8C)	23±3 °C
		Peak 240,0 A (15C)	< 10s, > SOC 50%
Cycle Life to 80% of Remaining Capacity	1C/1C	1,4	100% DOD or 3,0~4,2 V (@23±3 °C)

271 Kokam battery cells have weight is of 0.406 g with a density of energy of 146 Wh/kg; therefore,
 272 to reach the 8 kWh requested by the electrical motor, the final weight is of 55 kg. This confirms that
 273 both the 5 cycles of the training and the cruise profile could be possible with this battery pack.

274 The model of the battery pack is shown in figure 7.

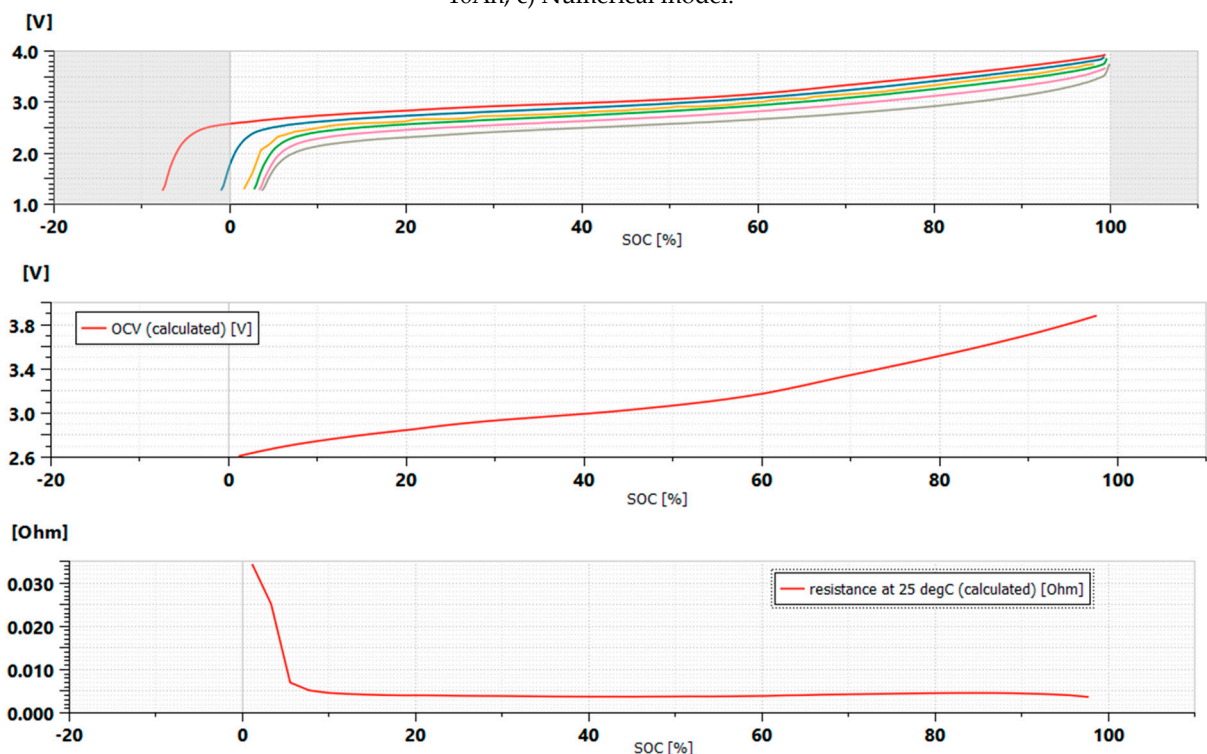
275 All the inputs to the numerical model have been implemented as the number, the disposition
 276 and the capacity of the cells, resistance and the open circuit voltage as function of the state of charge.
 277 The resistance and the open circuit voltage, as function of the state of charge, have been valued
 278 including the discharge curves in figure 7b). Those trends have been plotted as function variation of
 279 C-rate. In the numerical model the battery pack's input (shown in figure 8a) have been obtained for

280 the datasheet of the chosen battery pack. The numerical model, as output, evaluates the OCV (Open
 281 Circuit Voltage) and the resistance at 25 °C for the variation of state of charge, figure 8a). All the
 282 evaluated information are enough to calculate the true state of charge during the simulation, the
 283 variation of current and voltage and the apparent power guaranteed.



284
 285
 286

Figure 7. a) Discharging characteristics of the kokam 16Ah, b) Charging characteristics of the kokam 16Ah, c) Numerical model.



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 288

Figure 8. OCV and the resistance at 25°C at the variation of state of charge.

289 4. Study of the battery pack

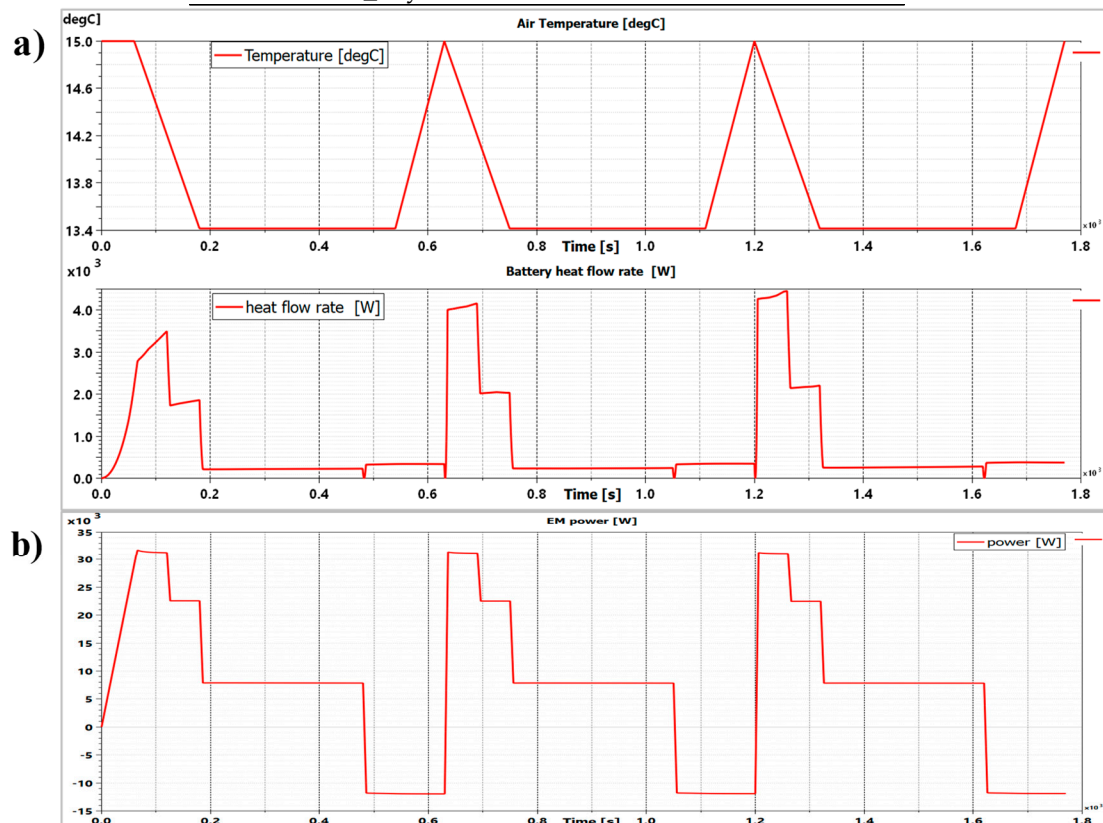
290 The entire model of the hybrid system has been already presented (figure 4). In this section of
 291 the paper, it has been run the numerical model in order to verify the battery pack choice. For this
 292 reason, simulation have been run for both mission profiles considering the weight constrain (55-60
 293 kg). A first test called "test 1" has been run with the training mission profile doing from 3 to 5 touch-
 294 and-go cycles. The second test, called "test 2", instead, is referred to the cruise mission profile.

295 4.1 Test 1: Training Profile

296 The first test is the "Test 1" where the numerical model has been run considering the
 297 performance requested during the training profile and listed in table 3. Table 8 summarizes all the
 298 information of the chosen battery pack. The cell used is, as said, are the Kokam 16 Ah with the total
 299 weight is of 53.6 kg. With this solution, three touch-and-go are guaranteed. First model results are
 300 shown in figure 9 a) where the temperature trend as function of the altitude and the battery heat
 301 exchange are represented. In the figure 9 b), the maximum heat exchange is relative to the phases in
 302 which the maximum electric power is required (Climb segment of the training profile). Figure 9 c)
 303 shows the voltage and current trends of the battery.

Table 8. Training profile characteristics

Training Profile	
Battery type	16 Ah
N_° cells in series	66
N_° branches in parallel	2
Total cells	132
Cell weight	0.406 kg
Total weight	53.6kg
SoC @ end	38.3%
Simulation time	1770 s
N_° cycles	3



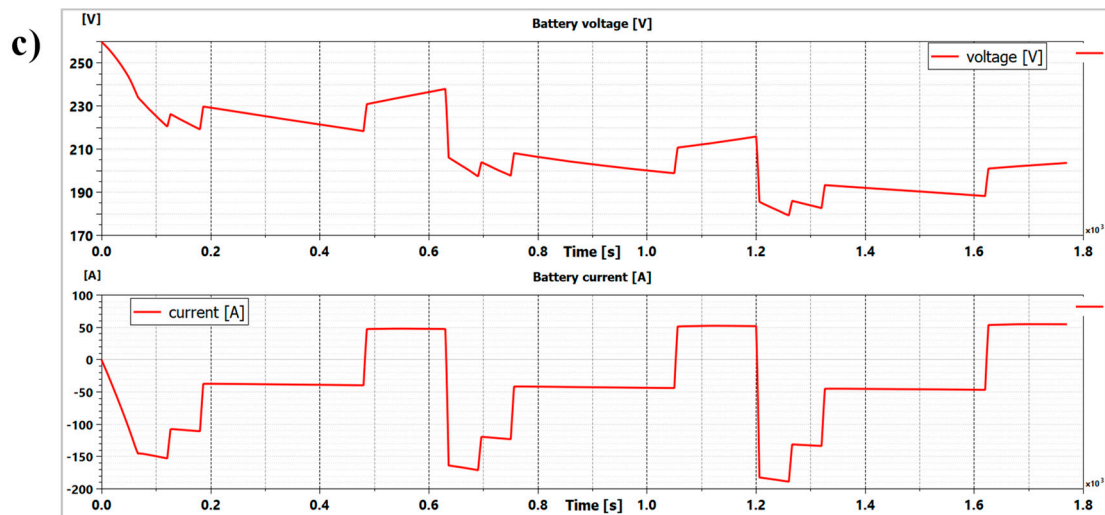


Figure 9. (a) Air temperature vs Battery heat flow rate, (b) Electric machine power, (c) Battery voltage and current – Training profile.

Analyzing data in figure 9, it is clear that the voltage tends to decrease with time while the current tends to increase as a consequence; this is true for all the phases. It is important to understand that, in figure 9 c), the current is negative when the battery is powering the motor, while it is positive when the electric machine works as a generator and recharges the battery.

By the end, another important output of the numerical model is shown in figure 10. The graph presents the state of charge of the battery pack in the training profile as a function of the electric power required during the simulation time.

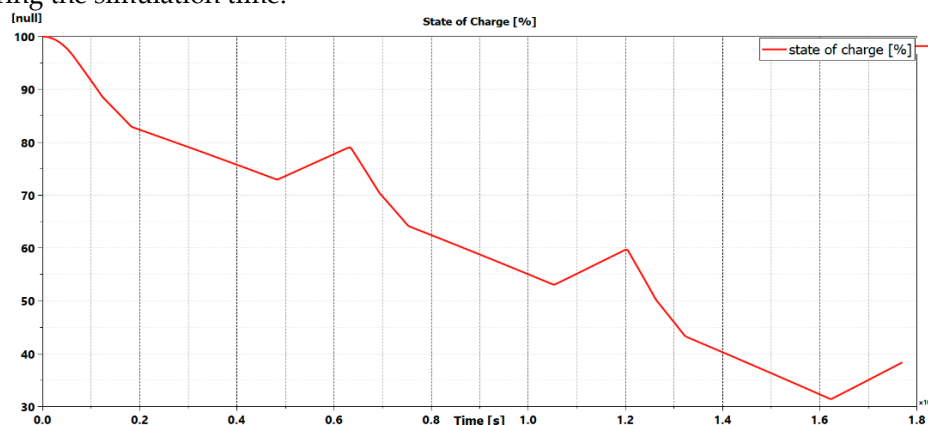


Figure 10. State of charge of the battery pack – Training profile.

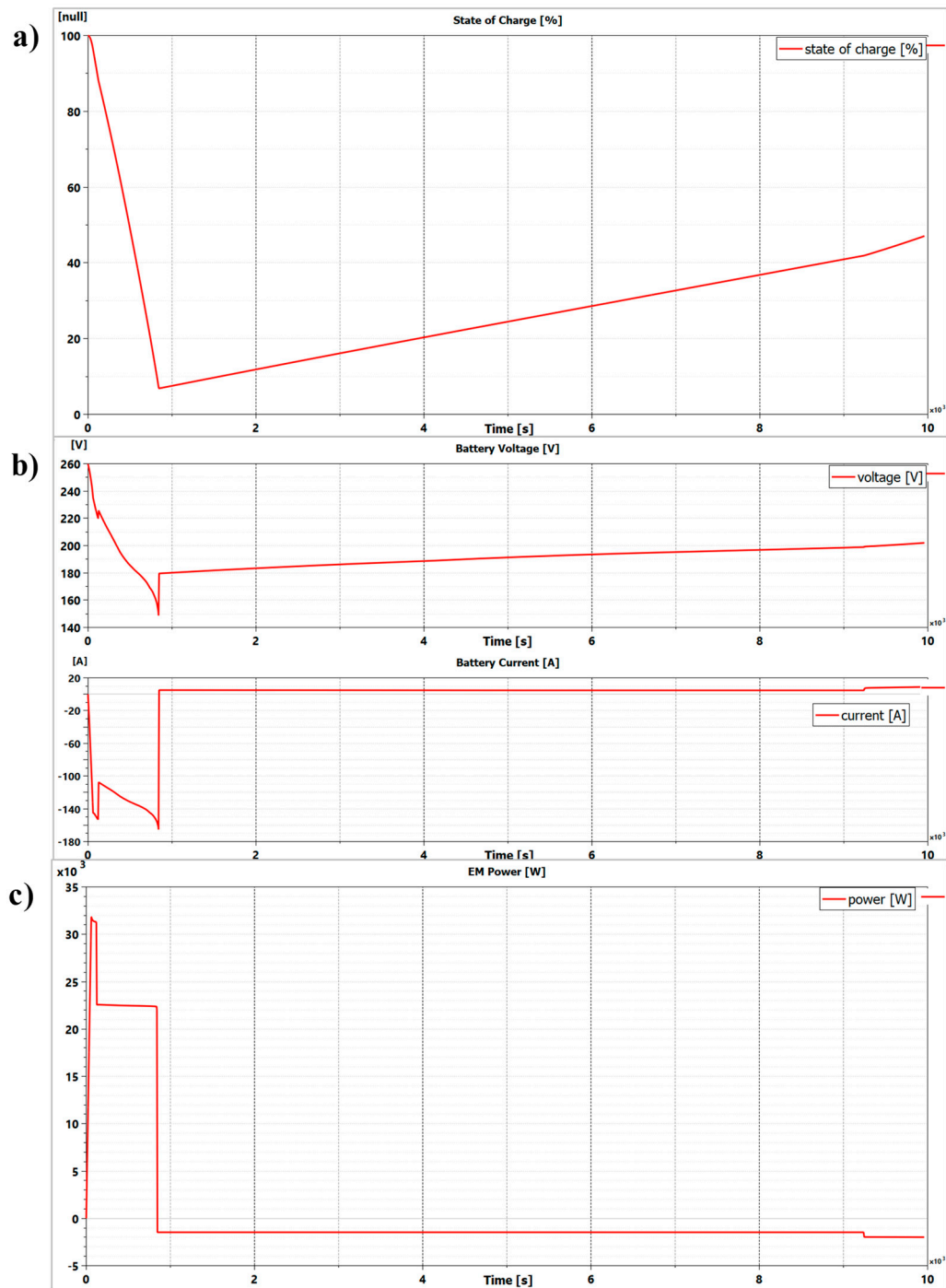
Looking at figure 10, it is clear that the system works in a fully electric configuration during the taxi phase (1 minute), in fact the slope of the curve is greater in the first phase. The electric machine, as said, works also as a generator; in these phases the battery's state of charge increases. By the end, after 3 cycles, the battery still has 38.3% of charge. Even if the battery has a state of charge close to 40% at the end of the third cycle, this percentage is too low to allow the fourth cycle.

It is important to underline that the chosen battery pack configuration respects the weight limits, guarantees the power demand, and respects the actual standards on maximum voltage and the security between two branches in parallel.

4.2 Test 2: Cruise Profile

The project expected the simulation of two different mission profiles. After representing the possible configurations for the training profile; by following the numerical results obtained during the simulation in the cruise profile have been reported. The boundary conditions set in the model for the cruise mission profile are the same as table 7 except for the number of cycles (in the cruise profile consist of a single cycle).

331 Looking at figure 11a) the SoC at the end of the profile mission is of 47% (the overall simulation
 332 time is of 9960 s). The chosen battery pack is able to guarantee this flight profile (of 9960 s) ensuring
 333 a final cycle level of SoC of 47%. The power demand is also perfectly guaranteed as shown in figure
 334 11). Hence, the choice of the Superior Lithium Polymer Battery SLPB78205130H of KOKAM has been
 335 numerically demonstrated to be good for both mission profiles, allowing also three touch-and-go
 336 for the training one. As said, state of charge at the end of the cruise mission profile is of 47%. This can
 337 be justified looking at the lower peak of the trend in the figure 11 a) where after the taking-off and
 338 the climb phases. At that time, the state of charge of the battery is of around 5-8%. Then, thanks to
 339 the cruise mission phase, the electric machine works as generator and consequently the state of charge
 340 increases and goes until the 47%.
 341



342
 343
 344 **Figure 11.** (a) The state of charge, (b) The battery voltage and current, (c) The electric machine power – Cruise profile.

345 The numerical model has been used, as demonstrated in this paper section, to be a good
 346 methodology to approach at the choice of a new component in the hybrid-propulsion system. In the
 347 following paragraph the numerical methodology has been adopted in order to investigate on the real
 348 improvement on the environmental emissions achieved with hybrid-electric solution.

349 5. Numerical model results

350 The numerical model described in the previous paragraph has been run following both mission
 351 profiles to evaluate the overall performance of the hybrid propulsion system.

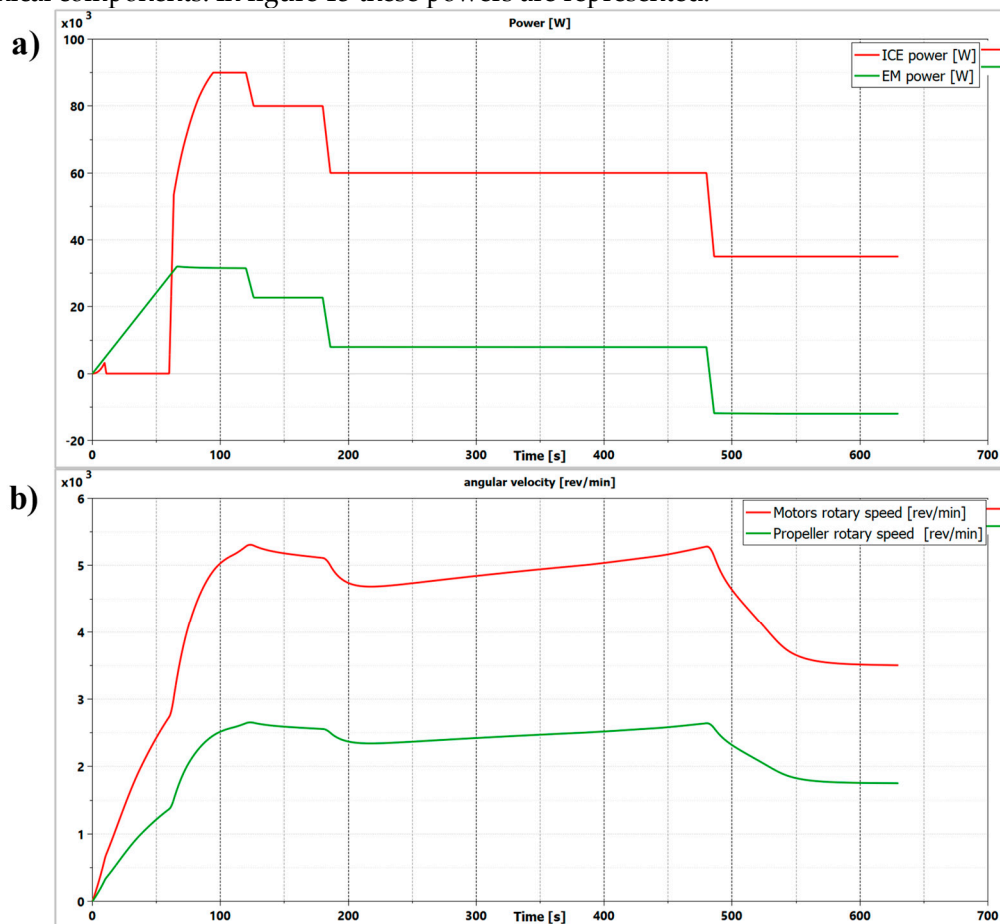
352 A. Model results: Training Profile

353 The entire numerical model shows in figure 4 has been run for three consequent cycles.
 354 However, since the trend of the magnitudes are the same for each graft in the following figures only
 355 one cycle has been reported. Figures 12 a) and b) represent the power and rotary speed of the internal
 356 combustion engine ICE (red) and the electric machine EM (green) as function of the simulation time
 357 for one cycle.

358 In the figure 12 a), the powers comparison shows that the line green, related to the electric
 359 machine, becomes negative when it works as generator. In figure 12 b) represents the speed of both
 360 motors and the propeller speed, that is, as said, half of the motor speed.

361 The overall efficiency of the engine depends on the efficiencies of the; combustion, mechanical
 362 and thermodynamic cycle.

363 These parameters are function of the power loss due to the combustion, the exhaust and the
 364 mechanical components. In figure 13 these powers are represented.



365
 366 **Figure 12.** (a) ICE power and EM power, (b) Motor speed vs Propeller speed (Training).

367 Considering a maximum power of 122 kW at 100 s, the table 9 presents the values of the fuel
 368 power, exhausts power, friction power losses and mechanical power. These values allow calculating
 369 the efficiencies at maximum mechanical power. The engine performance relative to the maximum
 370 mechanical power are instead show in table 10.

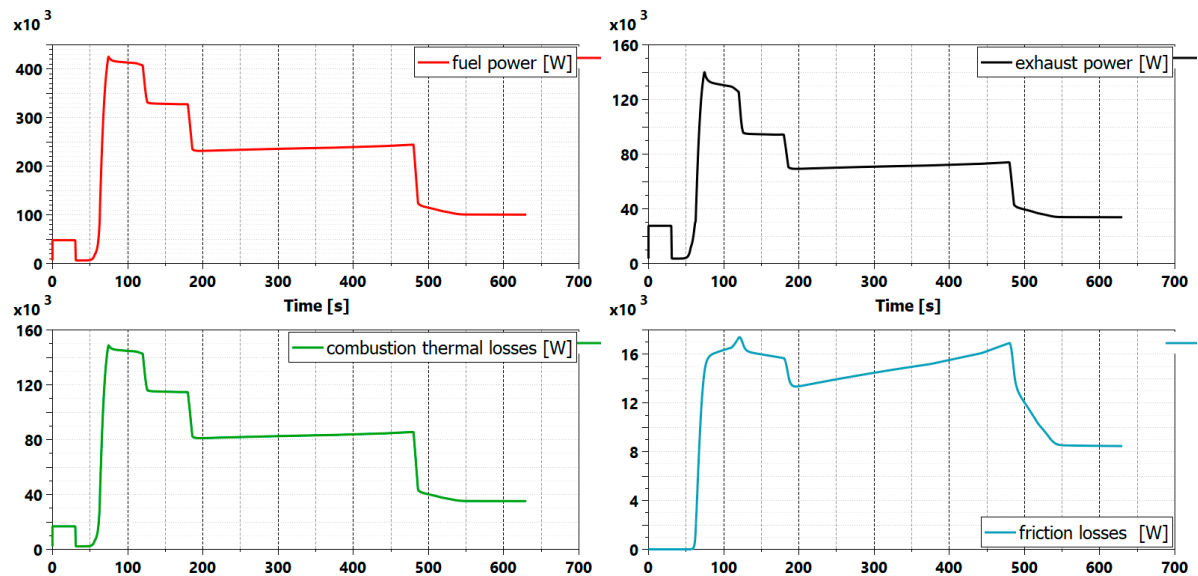
Table 9. Power Type at Propeller (Training)

Power Type at the Max-Power at Propeller	[kW]
Fuel Power	324
Exhausts Power	106.8
Friction losses Power	13.9
Mechanical Power	122

371

Table 10. Performance @ Max-Power before Gearbox (Training)

Performance at the Max-Power before Gearbox (2:1)	
Hybrid: CMD22 + EMRAX208	
Mechanical Power [kW]	122
Torque [Nm]	230.67
Engine speed [rpm]	5053
Specific consumption [g/kWh]	293.21
Global Efficiency [-]	0.27
BMEP [bar]	9.75
IMEP [bar]	11.28



372

373

Figure 13. CMD22 power losses (Training).374 *5.1 Model results: Cruise Profile*

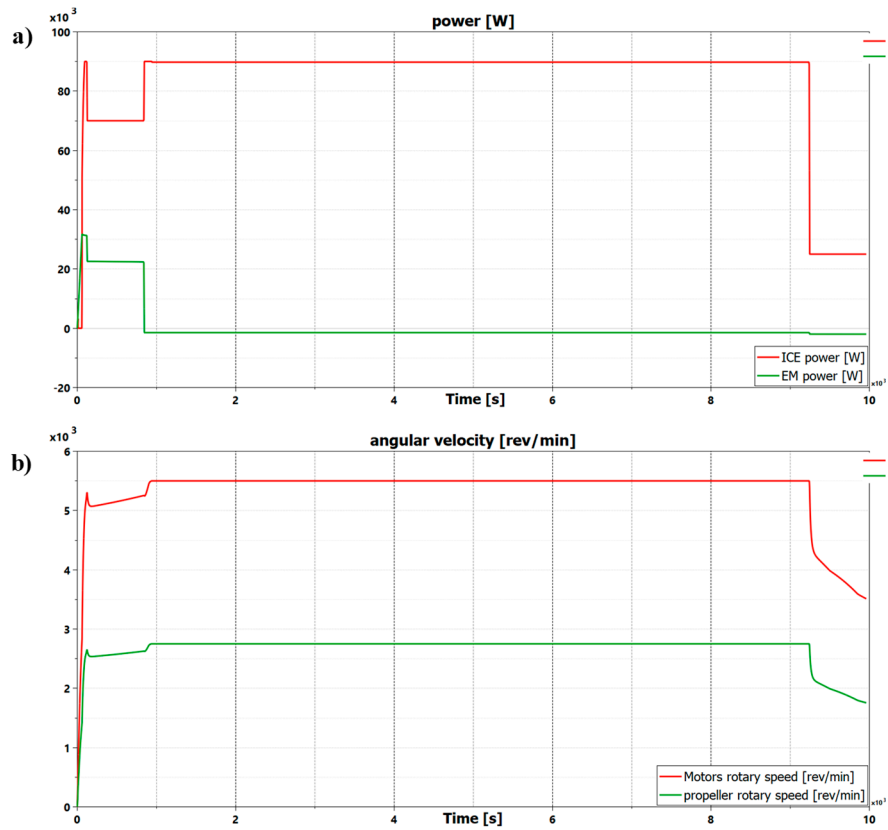
375 At the same way, the cruise profile has been deeply investigated. Model results related to power,
 376 torque, engine speed, specific consumption, pressure, efficiency, power losses and relative
 377 efficiencies, relative to the cruise profile, have been reported in the figures below.

378 Also for the cruise mission profile, considering a maximum power of 122 kW the fuel power, the
 379 exhausts power, the friction of losses power and the mechanical power at 100 s are listed in table 11.
 380 Instead, in table 12 the engine performance relative to the maximum mechanical power in a
 381 determinate time instant are presented.

382

383

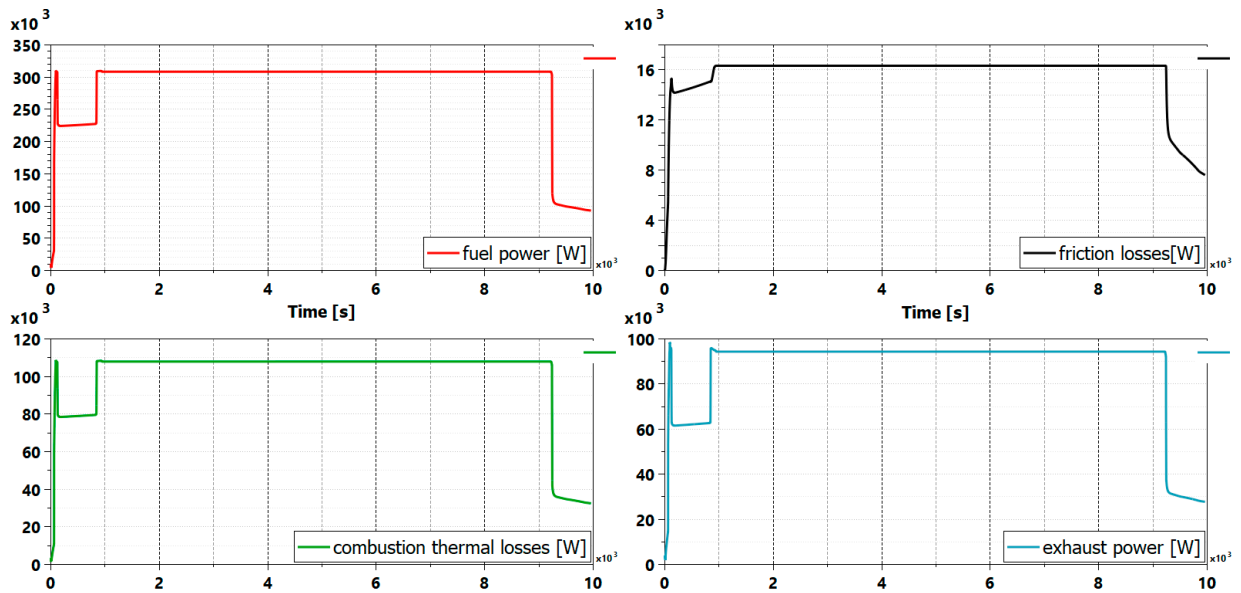
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385

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Figure 14. (a) Mechanical power of ICE and EM, (b) Motors speed vs Propeller speed – Cruise.



387

388

Figure 15. CMD22 power losses.

Table 11. Power Type @ Max-Power at Propeller (Cruise)

Power Type at the Max-Power at Propeller	[kW]
Fuel Power	307
Exhausts Power	95.8
Friction losses Power	13.9
Mechanical Power	122

Table 12. Performance @ Max-Power before Gearbox (Cruise)

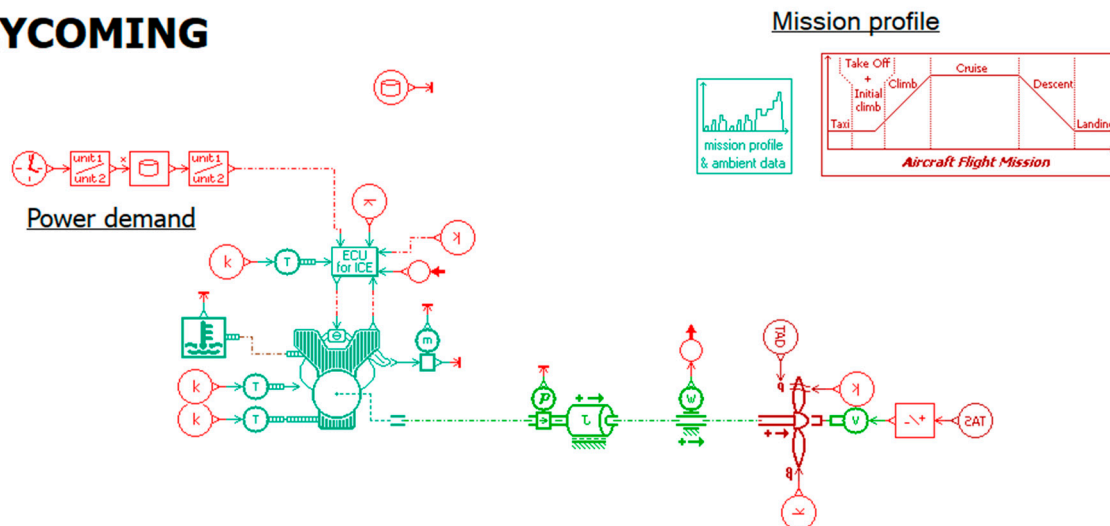
Performance at the Max-Power before Gearbox (2:1) - Hybrid: CMD22 + EMRAX208	
Mechanical Power [kW]	122
Torque [Nm]	206.2
Specific consumption [g/kWh]	292.89
Global Efficiency [-]	0.29
BMEP [bar]	9.71
IMEP [bar]	11.23

389 6. Comparison between “baseline” and “hybrid” configurations

390 The numerical results obtained by running simulations on the Hybrid-Electric propulsion
 391 solution have verified that the designed system is able to perform both mission profile, respecting
 392 the weight limits. In this section of the paper the “Hybrid” and the “baseline” configuration of the
 393 propulsion system is shown [11].

394 In order to perform the comparison, a model of the internal combustion engine Lycoming IO-
 395 360 (baseline propulsion system) has been built up. The model of the baseline configuration is shown
 396 in figure 16.

LYCOMING



397
 398

Figure 16. Model of the actual propulsion system (Lycoming IO-360).

399 The model architecture is similar to the hybrid system; however, in this case, engine and the
 400 propeller are connected on the same shaft, without speed reducer. The management and the model
 401 inputs are the same already explained. The significant differences between models concern the engine
 402 geometry and consequently the input to the model (figure 17).

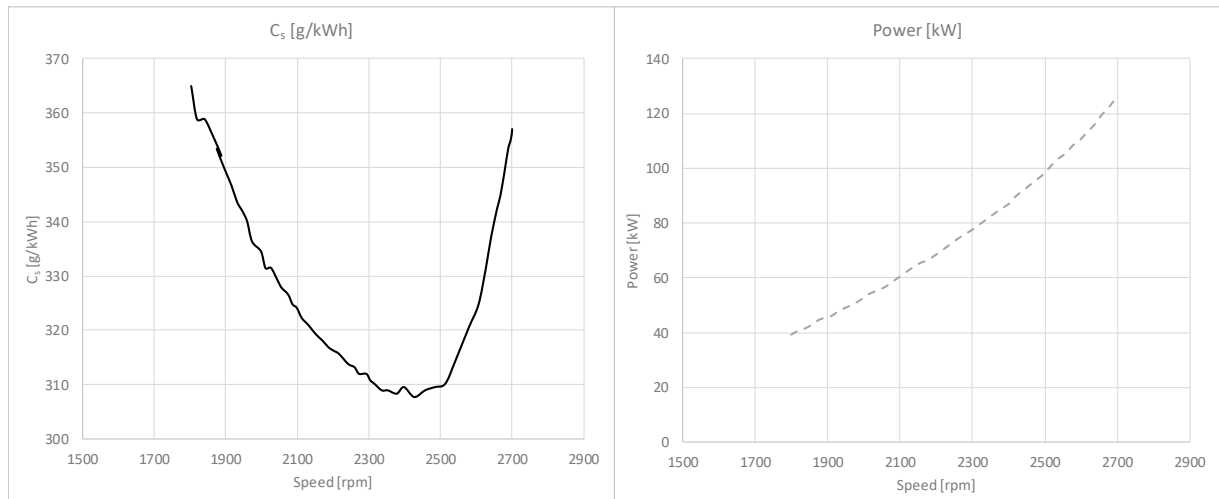


Figure 17. Lycoming Performances (Cs - Power vs engine speed).

As said, in this paragraph the comparison between the “baseline” and “hybrid” configurations has been done on the power, the speed, the torque and on the fuel saving and the CO₂ emitted into the environment. The comparison between the propulsion configurations has been performed for both mission profile.

6.1 Training profile: Performance and consumption

Both model configurations have been run in the training mission profile. Figure 18 represents the trends of the power, the torque and rotary speed; that, for the hybrid configuration, have been read before the speed reducer. In figure 18, the “baseline” configuration is in red and the “hybrid” one is in black.

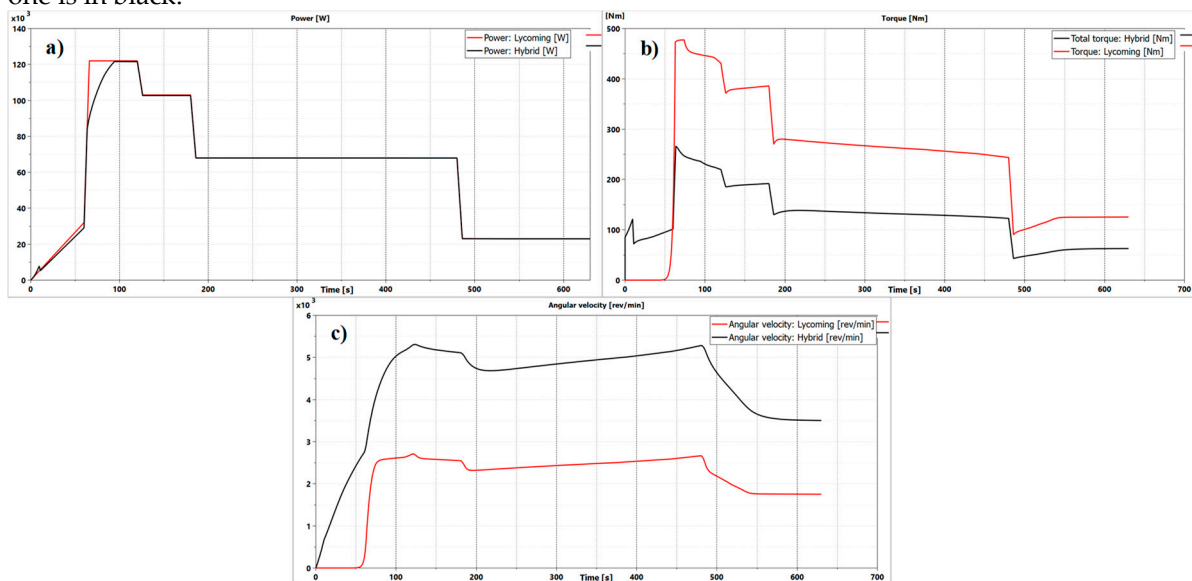


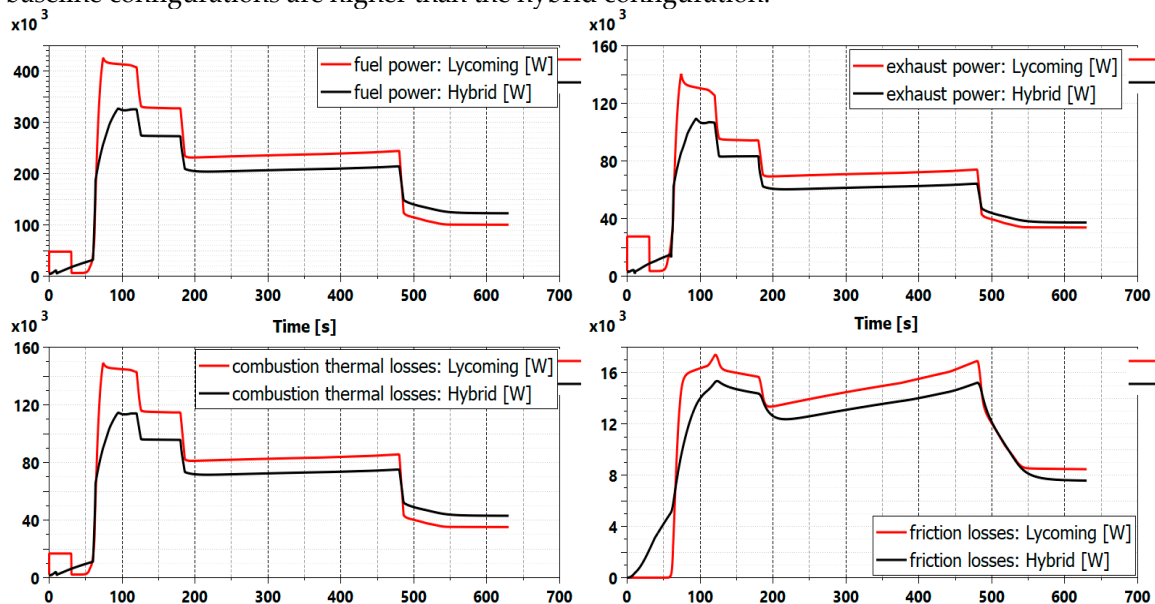
Figure 18. Comparison between configurations: (a) Power, (b) Torque and (c) Speeds (Training profile).

Power profiles in figure 18 a) are the same, while the torque of the hybrid configuration is one half of the other, vice versa for the rotary speed, figure 18 b) and 18c) respectively. After the speed reducer applied on the hybrid configuration, torques and speeds become equal to the baseline configuration.

Figure 19 represents the comparison between the powers used to define efficiencies. In fact, the engine efficiency depends by the combustion efficiency, the mechanical efficiency and the thermodynamic efficiency. These parameters are function of the power loss due to the combustion, the exhaust and the mechanical components.

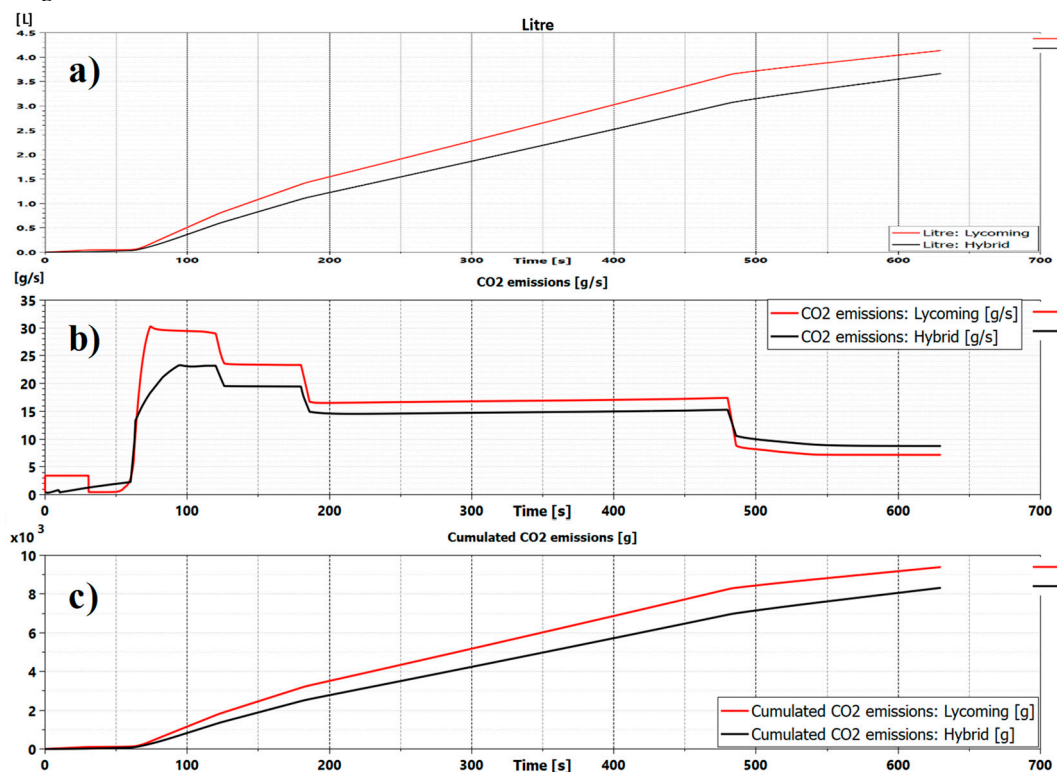
The baseline configuration, as said, has a bigger engine with higher nominal power able to cover the power demand by itself. Otherwise, the ICE of the hybrid system is smaller and with less nominal

426 power, so it is used to cover only a part of the power demand, depending by the missions and
 427 consequently by the segments analyzed. For these reasons, trends of the powers relative to the
 428 baseline configurations are higher than the hybrid configuration.



429
 430 **Figure 19.** Comparison between the powers (Training profile).

431 Figure 20 a) represents comparison on the fuel consumption during the first cycle of the mission
 432 profile. However, differences between configurations has been found also for the other cycles (3-5).
 433 Other important data are shown in figure 18 b) where the comparison of the emission of CO_2 have
 434 been diagrammed.



435
 436 **Figure 20.** (a) Fuel consumption, (b) CO_2 emissions [g/s], (c) CO_2 cumulated [g] (Training profile).

437
 438 Table 13 summarizes the numerical results showed in the previous figures. Therefore, the table
 439 reposts the consumption and emissions of the two configurations for the training profile.

440
 441

Table 13. Consumption and emissions (Training)

Type	Lycoming IO-360			Hybrid: CMD22 + EMRAX 208		
	1 Cycle	3 Cycles	5 Cycles	1 Cycle	3 Cycles	5 Cycles
Consumption [l]	4.33	12.55	20.95	3.66	11	18.33
Grams	3158.7	9085.1	15140.5	2641.9	7930.9	13219.8
Emitted CO₂ [g]	9950	28618.2	47692.7	8322.1	24982.5	41642.5

442 Tables (14 and 15), otherwise, represent the saving in terms of consumption and CO₂ emission
 443 passing from the baseline configuration to the hybrid configuration for the training mission profile.

Table 14. Delta consumption (Training)

	1 Cycle	3 Cycles	5 Cycles
Liters	-0.67	-1.55	-2.62
Grams	-516.8	-1154.2	-1920.7
CO₂ [g]	-1627.9	-3635.7	-6050.2

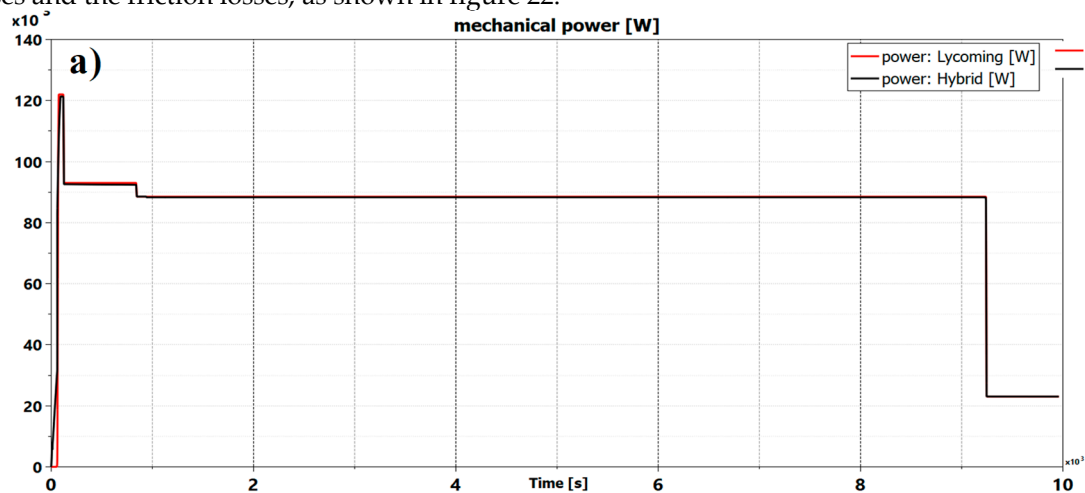
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Table 15. Percentage saving (Training)

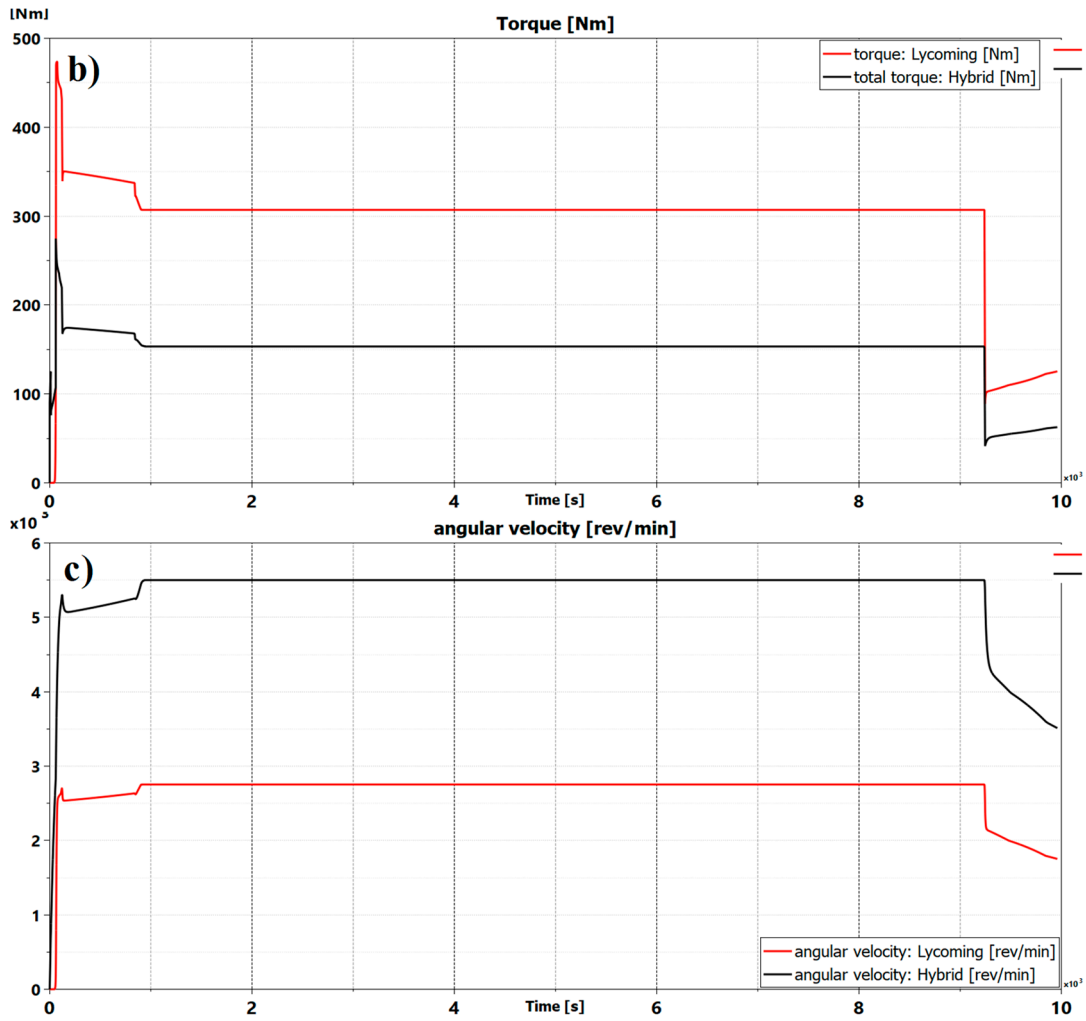
	1 Cycle	3 Cycles	5 Cycles
Liters	15.7 %	12.4 %	12.5 %
Grams	16.4 %	12.7 %	12.7 %
CO₂ [g]	16.4 %	12.7 %	12.7 %

445 6.2 Cruise profile: performance and consumption

446 As already done for the training mission profile, models of both configurations have been run
 447 following the cruise mission profile. The values and the trends, as expected, change but the concepts
 448 expressed above about power, torque and speed are the same also for this mission profile (figure 21).
 449 The comparison has been performed also on the fuel power, exhausts power, combustion thermal
 450 losses and the friction losses, as shown in figure 22.

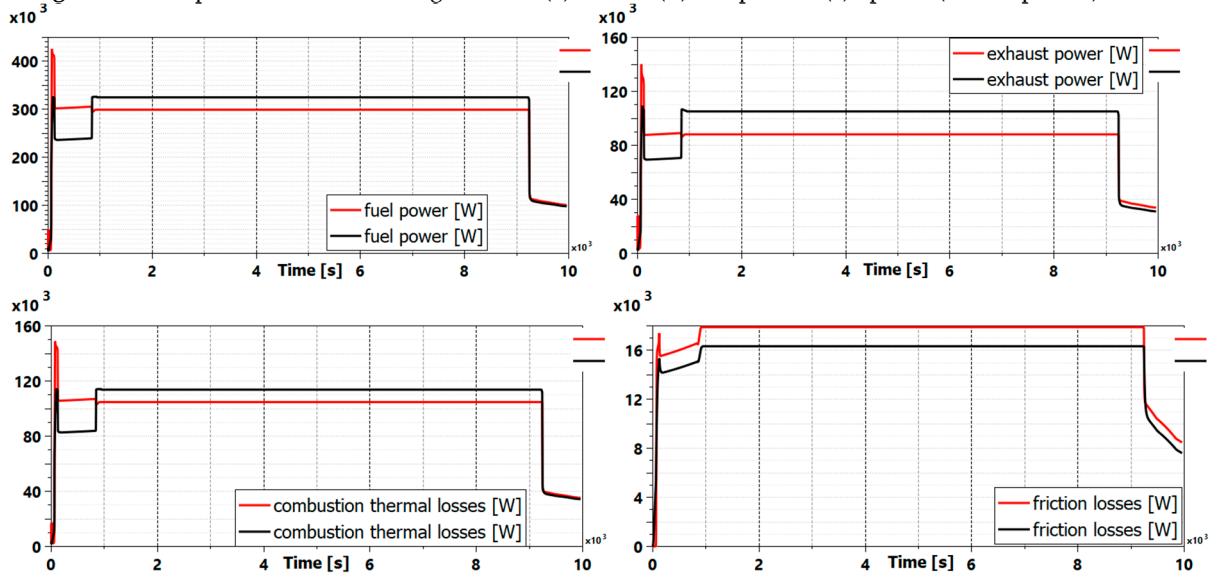


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Figure 21. Comparison between configurations: (a) Power, (b) Torque and (c) Speeds (Cruise profile).



454

455
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Figure 22. Comparison between the powers (Cruise profile).

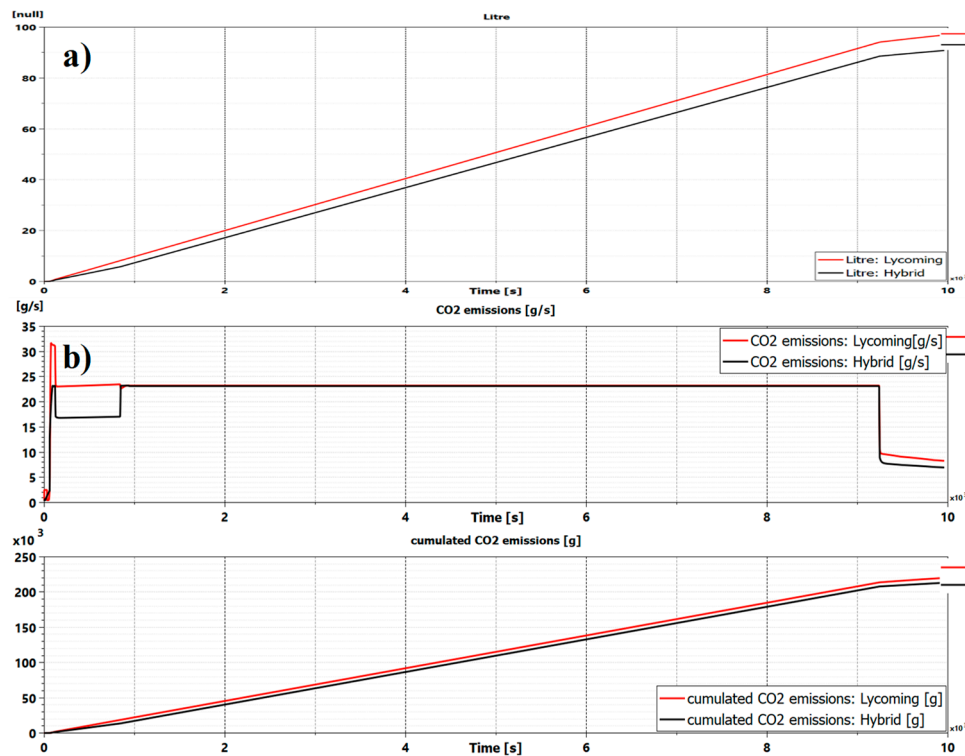


Figure 23. (a) Fuel consumption, (b) CO₂ consumption (Cruise profile).

Figure 23 shows the fuel saving also for the cruise profile confirming that also for the cruise mission profile there is a reduction of consumption and emissions. Therefore, the goal of this research has been achieved.

The tables (16 and 17) represent the amount of saving and consequently the percentage of reduction for the cruise profile.

Table 16. Consumption and emissions (Cruise profile)

	Lycoming IO-360	Hybrid: CMD22 + EMRAX 208
Consumption [L]	96.92	90.83
Grams	69882.6	67671.5
Emitted CO ₂ [g]	220130	213165

Table 17. Delta consumption and percentage saving (Cruise profile)

Delta Consumption		Percentage Saving	
Consumption [L]	-6.09	Liters	6.3%
Grams	-2211.1	Grams	3.16%
Emitted CO ₂ [g]	-6965	CO ₂ [g]	3.16%

465 Conclusions

466 The feasibility and the potential environmental benefits of a hybrid electric propulsion system
467 for light aircraft has been investigated.

468 The paper presents an analysis of a parallel hybrid-electric propulsion system for the general
469 aviation aircraft.

470 This system has been modeled with a multi-physical and multi-domain commercial code
471 AMESim®. Each component of the system has been characterized: internal combustion engine,

472 electric machine, mission profiles (training and cruise), battery pack, system inertia, propeller, the
473 power demands and the flight speed.

474 The numerical model has demonstrated to be a useful tool for the choice and the sizing of system
475 components. In particular, different battery configurations were examined, both with training and
476 cruise mission profiles, giving clear indications on the best configuration of the system.

477 The comparison between the benchmark propulsion system -with only the ICE- and the
478 hybrid-electric system has been the conclusive part of simulations to validate the tool. Results has
479 shown that the hybrid-electric propulsion system for a light aircraft is advantageous for the fuel
480 saving and the pollutants emissions decreasing. In particular, the simulations highlight a fuel saving
481 over the 12% for the training profile and amount the 6% for the cruise profile.

482 All achieved results are relative to a system modeled using off the shelf component and
483 technologies which suggests that already nowadays can be convenient operate with an aircraft
484 powered by an hybrid-electric propulsive system.

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487 Original Draft Preparation, C. Pascarella and A. Senatore; Writing-Review & Editing.

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492 **Conflicts of Interest:** The authors declare no conflict of interest.

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