

1 *Type of the Paper (Article)*

## 2 **Application of a Hybrid Method for Power System** 3 **Frequency Estimation with a 0.2-second Sampled Period**

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12 **Featured Application:** Authors are encouraged to provide a concise description of the specific  
13 application or a potential application of the work. This section is not mandatory.

14 **Abstract:** The signal processing technique is one of the principal tools for diagnosing power quality (PQ)  
15 issues in electrical power systems. The Discrete Fourier Transform (DFT) is a frequency analysis technique  
16 used to process power system signals and identify PQ problems. However, the DFT algorithm may lead to  
17 spectral leakage and picket-fence effect problems for asynchronously sampled signals that contain harmonic,  
18 inter-harmonic, and flicker components. To resolve this shortcoming, a hybrid method for frequency  
19 estimation based on a second-level DFT approach and a frequency-domain interpolation algorithm to obtain  
20 the accurate fundamental frequency of a power system is proposed in this paper. This method uses a second-  
21 level DFT to compute the cosine and sine parts for the fundamental frequency components of the acquired  
22 signals. Then, a frequency-domain interpolation approach is adopted to determine the amplitude ratio for the  
23 cosine and sine parts of the system's fundamental frequency. To demonstrate the performance of the proposed  
24 frequency estimation method, the observation window used by this paper to evaluate different estimation  
25 algorithms is 200 ms. According to the IEC standards, a 200 ms acquisition window is recommended for  
26 power system quality assessment. A set of mixed signals with harmonic, inter-harmonic, and flicker  
27 components with the fundamental frequency deviation is used. The evaluation results demonstrate the  
28 superiority of the new method over other approaches for assessing asynchronously sampled signals  
29 contaminated with noise, harmonic, inter-harmonic, and flicker components.

30 **Keywords:** frequency estimation, asynchronously sampled, harmonic, flicker.

31

### 32 **1. Introduction**

33 Power system signal analysis is a key step in PQ diagnosis. Effective extraction of power system signal  
34 features is helpful to understand the underlying physical nature of PQ's phenomena, and to evaluate its health  
35 condition, thereby providing convincing evidences for diagnosis. However, in both academic researches and  
36 engineering practices, power system signals are usually highly intricate. The vast increase usage in electronic  
37 devices may cause PQ problems such as harmonics, inter-harmonics, and voltage flickers in power systems.  
38 Such PQ problems may lead to power system, factory equipment, and public facility deviations or may even  
39 result in electrical equipment damage in severe cases.

40 The power system frequency is nonstationary. The degree of frequency change depends on the balance  
41 between power generation and load demand. Thus, the frequency is a key indicator for the safety and economy  
42 of the power system operation. A frequency below the nominal value represents an overloaded system; while a  
43 frequency above the nominal value represents a power oversupply. In general, the power system frequency is a  
44 critical indicator for power system monitoring, control, and protection [1-5]. Therefore, power system signal  
45 analysis is a key research topic and plays an important role in PQ diagnosis. International standards such as  
46 IEC-61000 have described the diagnosis of PQ.

47 In the past, several researches have successfully shown that the frequency assessment technology was able  
48 to detect the PQs of defects in power system. These technologies include Zero-crossing Algorithm [5-7],

49 Discrete Fourier Transform (DFT) [8-13], Kalman Filter (KF) [14, 15], Phase-Locked Loops (PLL) [16, 17],  
50 Newton Algorithm [18, 19], Least squares Algorithm (LMS) [20, 21], Prony Algorithm [4, 22], Taylor  
51 Algorithm [23, 24], and Artificial-intelligence Algorithm [25, 26].

52 Among them, one of the two most popular techniques adopted is the Zero-crossing Algorithm, which has  
53 the least computational complexity and the fastest execution speed. However, this method is susceptible to noise  
54 and spikes, and can only provide an accurate frequency evaluation in noise-free and disturbance-free  
55 environments [5-7].

56 In [5], using the waveform construction method to combine the Time Domain Frequency Estimation  
57 Algorithm with the Newton Interpolation method was proposed. This approach can eliminate the leakage effect  
58 caused by the FFT (Fast Fourier Transform) calculation under asynchronous sampling conditions. In this paper,  
59 a Time Domain Zero-crossing Algorithm to evaluate the basic frequency is proposed. This algorithm uses the  
60 zero-crossing frequency detection method to calculate the basic frequency. Because this algorithm can be  
61 affected by non-basic frequency signals, a pre-filter must be used to eliminate the non-basic frequency signals.  
62 After the basic frequency has been obtained, Newton Interpolation method is applied to generate a new sample  
63 waveform that conforms to the FFT application conditions. As a result, the accurate basic frequency under  
64 asynchronous sampling conditions can be obtained.

65 In [6, 7], the authors proposed the digital filter and zero-crossing technique combination frequency  
66 evaluation method. They broke down the original sample signals into two orthogonal component waveforms  
67 using cosine and sine filters. These two waveforms and the zero-crossing technique are used to assess the basic  
68 frequency of the power system. The results indicated that the orthogonal filter and the zero-crossing technique  
69 can effectively reduce the noise and disturbance interferences.

70 The other technique that is popular used in calculating the fundamental frequency of a power system is  
71 DFT/FFT. In the IEC61000-4-30 standard, PQ measurement analysis is mostly based on DFT/FFT techniques.  
72 DFT/FFT can convert the periodic signals obtained via synchronous sampling into frequency domain data to  
73 help us learn more about the spectrum composition. However, the basic frequency of an actual power system  
74 will vary from time to time and become affected by noise, flickers, harmonic waves, inter-harmonic waves, and  
75 other disturbances. Therefore, it is unrealistic and impossible to achieve strict synchronous sampling without a  
76 special technique such as PLL (Phase Lock Loop). Asynchronous sampling would cause the DFT/FFT  
77 algorithm to create the spectral leakage and picket-fence effect problems and directly cause the FFT algorithm  
78 spectrum calculation accuracy to drop dramatically [8-13].

79 In [8], it was proposed to use the window method with DFT for frequency calculation, and to obtain the  
80 basic frequency parameter values according to the multi-point spectrum near the base frequency peak point as  
81 well as the Hanning window interpolation expressed as a function of the frequency domain itself. The results  
82 indicated that this multi-point frequency domain interpolation algorithm can effectively reduce the noise and  
83 disturbances.

84 Reference [9] adopted the pseudo-synchronization technique, Hanning window, and FFT combination for  
85 frequency calculation in order to improve the frequency estimation accuracy under the noise and disturbance  
86 effects. The author combined the original sample signals with the Hanning window function, performed FFT  
87 conversion for the new wave signals, and then assessed the basic frequency of the power system. The results  
88 indicated that the pseudo-synchronization technique combined with FFT can effectively reduce the noise and  
89 disturbances.

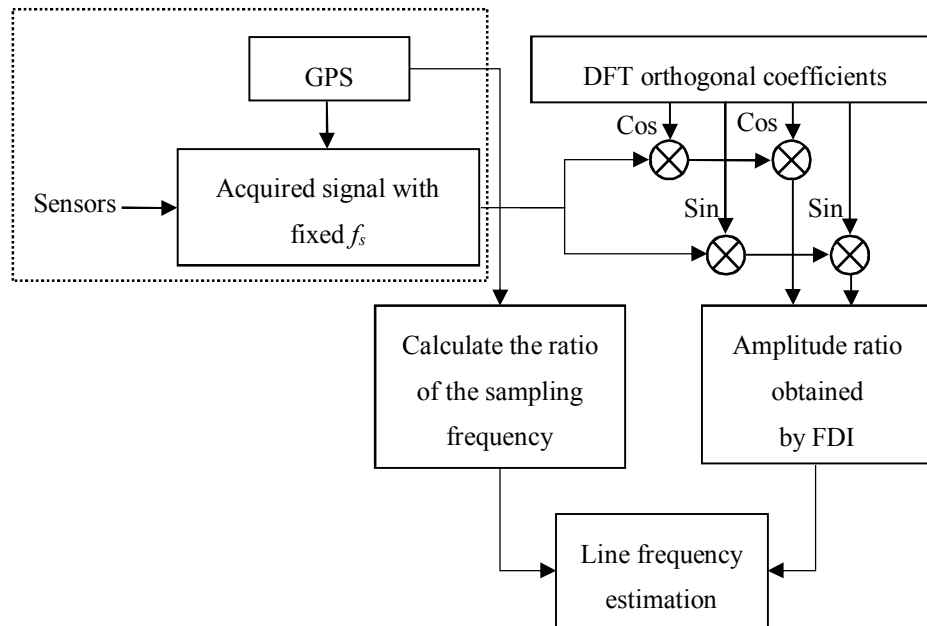
90 The PQ event detection algorithms require precise power system frequency which can be obtain using  
91 DFT-based frequency estimation algorithms under asynchronously-sampled signals that are contaminated with  
92 noise, flicker, and harmonic and inter-harmonic components. In this paper, we proposed a two-level DFT and  
93 frequency domain interpolation hybrid method to accurately calculate the basic frequency of a power system.  
94 This paper is divided into four chapters. Chapter 1 is the preface. Chapter 2 explores the two-level DFT and  
95 frequency domain interpolation hybrid method. Chapter 3 provides validation for the method. Chapter 4  
96 concludes this paper.

## 97 2. Two-Level DFT and Frequency Domain Interpolation Hybrid Method

98 Frequency evaluation technology is the foundation of PQ analysis and monitoring. Therefore, excellent  
99 frequency assessment techniques can improve power system protection and monitoring. At present, the  
100 IEC61000-4-30 standard established by the International Electrotechnical Commission (IEC) for power quality-  
101 related measurement techniques is based on the DFT/FFT technique to analyze the PQ issues. To conform to

102 the standard and facilitate development, numerous monitoring devices have adopted the fixed sampling  
 103 frequency-based DFT technique in order to simplify device design. However, the basic electricity frequency  
 104 changes may lead to asynchronous sampling problems for fixed sampling frequency devices, which may cause  
 105 leakage effects during the DFT calculations. In addition, if the sampling frequency and calculation method  
 106 window are not divisible, it would also cause the DFT method to obtain inaccurate basic frequencies.

107 The primary implementation steps of this paper are shown in Figure 1. First, we calculated the DFT  
 108 orthogonal coefficient and amplitude ratio deviation coefficient based on the power signals captured. Next, we  
 109 created two levels of orthogonal filtering based on the DFT orthogonal coefficients and power signals  
 110 calculated. We then used the two orthogonal filtering signals and frequency domain interpolation to determine  
 111 the amplitude ratio needed for the frequency calculation. Finally, we used the amplitude ratio and the amplitude  
 112 ratio deviation coefficient to calculate the frequency more precisely.



113

114

**Figure 1.** Proposed frequency assessment process.

115

### 116 2.1. DFT Orthogonal Filter Coefficients

117 The actual power system signals (such as voltage and current) can be expressed in discrete time with three  
 118 parameters: amplitude (A), frequency (f), and phase ( $\theta$ ), as shown in Equation (1).

119

$$x(n) = A \cdot \cos\left(2\pi \frac{f_a \cdot n}{f_s}\right), n = 0, 1, \dots, N-1 \quad (1)$$

$$f_s = f_0 \cdot N_0$$

120 In (1),  $f_s$  is the sampling frequency,  $f_0$  is the nominal frequency,  $f_a$  is the actual frequency,  $N_0$  is the number  
 121 of samples per cycle, and N is the total number of samples.

122 We used the DFT to convert the sample's N-point discrete signals into the N-point spectrum energy. The  
 123 DFT formula is shown in Equation (2).

$$X(i) = \frac{2}{N} \left[ \sum_{n=0}^{N-1} x(n) \cos\left(2\pi \frac{f_a}{f_0 \cdot N_0} n\right) - j \sum_{n=0}^{N-1} x(n) \sin\left(2\pi \frac{f_a}{f_0 \cdot N_0} n\right) \right] \quad (2)$$

124

Assuming there is a single window with M-point samples, Equation (2) can be expanded as follows:

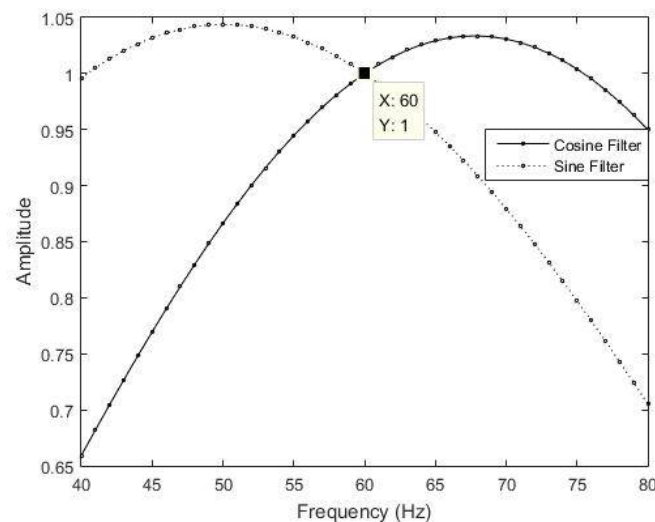
$$\begin{aligned}
X(i) = & \frac{2}{M} \left( x(1) \cos\left(2\pi \frac{f_a}{f_0 \cdot N_0}\right) + x(2) \cos\left(4\pi \frac{f_a}{f_0 \cdot N_0}\right) + \dots + x(M) \cos\left(2\pi \frac{f_a}{f_0}\right) \right) \\
& + j \frac{2}{M} \left( x(1) \sin\left(2\pi \frac{f_a}{f_0 \cdot N_0}\right) + x(2) \sin\left(4\pi \frac{f_a}{f_0 \cdot N_0}\right) + \dots + x(M) \sin\left(2\pi \frac{f_a}{f_0}\right) \right)
\end{aligned} \quad (3)$$

125 Therefore, for the  $i$ -th data window, the sine and cosine components can be expressed as  
 126 Equations (4) and (5).

$$A(i) = \frac{2}{M} \sum_{n=i}^{M+i-1} x(i) \cos\left(2\pi \frac{f_a}{f_0 \cdot N_0} n\right) \quad (4)$$

$$B(i) = \frac{2}{M} \sum_{n=i}^{M+i-1} x(i) \sin\left(2\pi \frac{f_a}{f_0 \cdot N_0} n\right) \quad (5)$$

127 If the fundamental signal frequency is equal to the assumed basic frequency ( $f_a=f_0$ ), then Equations (4)  
 128 and (5) are orthogonal to each other. At this point, A(t) and B(t) represent pure cosine and pure sine wave forms,  
 129 respectively. In Figure 2, the orthogonal filter has different amplitude responses for all frequencies other than  
 130 the nominal frequency. Its different amplitude response results clearly indicated that, when the orthogonal filter  
 131 conforms to  $f_a=f_0$  (60 Hz), the amplitude response value is 1.  
 132



133 **Figure 2.** Frequency impact of the orthogonal filter.

## 134 2.2. Frequency Estimation Algorithm

135 In summary, we can derive the frequency change rules based on the amplitude response characteristics  
 136 described above, and thus calculate the exact frequency. In practical applications, the usable vector lengths for  
 137 the cosine and sine coefficients of the two orthogonal filters have the vector matrix of  $N_0$  as expressed by  
 138 Equations (6) and (7).

$$CosWindow = \frac{2}{N_0} \left[ \left( \cos\left(\frac{2\pi}{N_0} + \frac{\pi}{N_0}\right), \cos\left(\frac{4\pi}{N_0} + \frac{\pi}{N_0}\right), \dots, \cos\left(2\pi \frac{N_0-1}{N_0} + \frac{\pi}{N_0}\right) + \cos\left(2\pi + \frac{\pi}{N_0}\right) \right) \right] \quad (6)$$

$$SinWindow = \frac{2}{N_0} \left[ \left( \sin\left(\frac{2\pi}{N_0} + \frac{\pi}{N_0}\right), \sin\left(\frac{4\pi}{N_0} + \frac{\pi}{N_0}\right), \dots, \sin\left(2\pi \frac{N_0-1}{N_0} + \frac{\pi}{N_0}\right) + \sin\left(2\pi + \frac{\pi}{N_0}\right) \right) \right] \quad (7)$$

139 Performing unilateral Z conversion for Equations (6) and (7), their amplitude response functions can be  
 140 expressed as Equations (8) and (9) [10].

$$|H_{CosWindow}(f)| = \frac{4}{N_0} \cdot \frac{\cos\left(\frac{\pi}{N_0}\right) \sin\left(\frac{\pi}{N_0} \frac{f}{f_0}\right) \sin\left(\pi \frac{f}{f_0}\right)}{\cos\left(\frac{2\pi}{N_0} \frac{f}{f_0}\right) - \cos\left(\frac{2\pi}{N_0}\right)} \quad (8)$$

$$|H_{SinWindow}(f)| = \frac{4}{N_0} \cdot \frac{\sin\left(\frac{\pi}{N_0}\right) \cos\left(\frac{\pi}{N_0} \frac{f}{f_0}\right) \sin\left(\pi \frac{f}{f_0}\right)}{\cos\left(\frac{2\pi}{N_0} \frac{f}{f_0}\right) - \cos\left(\frac{2\pi}{N_0}\right)} \quad (9)$$

141 Equations (8) and (9) can be used to derive the amplitude ratio of the two filters, and this ratio can be  
142 expressed as Equation (10).

$$R_{atio} = \frac{A}{B} = \frac{|H_{CosWindow}(f)|}{|H_{SinWindow}(f)|} = \frac{\tan\left(\frac{\pi}{N_0} \frac{f}{f_0}\right)}{\tan\left(\frac{\pi}{N_0}\right)} \quad (10)$$

143 Finally, the basic power signal frequency can be deduced using the amplitude value obtained using  
144 Equation (10), and the basic power signal frequency is shown as Equation (11).

$$f_a = f_0 \frac{N_0}{\pi} \tan^{-1} \left( \tan\left(\frac{\pi}{N_0}\right) \cdot R_{atio} \right) \quad (11)$$

145 However, the filtered signals can be affected by the amplitude responses and the frequency response  
146 effects. Therefore, the frequency evaluation using Equations (10) and (11) will be subject to these factors.  
147 Equations (12) and (13) are phase response equations that can be used to deduce the 90° angle differences. Thus,  
148 we can resolve the phase angle differences and find the ideal amplitude ratios.

$$\angle H_{CosWindow}(f) = \pi - \pi \frac{(N_0 - 1)f}{N_0 \cdot f_0} \quad (12)$$

$$\angle H_{SinWindow}(f) = \frac{1}{2}\pi - \pi \frac{(N_0 - 1)f}{N_0 \cdot f_0} \quad (13)$$

149 To resolve the phase response effects, a DFT filter is used to determine the amplitude ratio of the filtered  
150 sine and cosine signals outputted during the first level. This method uses the phase response characters to offset  
151 the filtered signal by 90° to turn the signal phase difference into 180°. Thus, the two orthogonal signals will  
152 become symmetrical signals with only the positive and negative sign differences. The vectors of the second  
153 level DFT-filtered discrete signals are represented as Equations (14) and (15).

$$A = [A_1 \ A_2 \ A_3 \ \dots \ A_n]^T \quad (14)$$

$$B = [B_1 \ B_2 \ B_3 \ \dots \ B_n]^T \quad (15)$$

154 When Equation (10) uses Equations (14) and (15) to calculate the amplitude ratio, the amplitude ratio  
155 would have a significant deviation in the vicinity of the zero-crossover for the filtered values A and B, and the  
156 frequency calculation would produce an erroneous value. To resolve the zero-crossover problem, the frequency  
157 domain difference technique is adapted to verify the amplitude ratio because, in addition to the harmonic or  
158 inter-harmonic waves, real signals also contain voltage flickers and other noises. Although this frequency  
159 assessment method is based on the DFT filtering technique and can prevent harmonic and inter-harmonic wave  
160 interferences, the method still cannot prevent voltage flickers and other signal noise interferences. Thus, the  
161 interpolation technique is applied to further suppress the interferences and calculate the precise amplitude value.

162  
163

## 164 2.3. Amplitude Interpolation Method

165 The discrete time sequence representation of a Hanning window is expressed as [8, 9]:

166 
$$W(n) = 0.5 - 0.5 \cos\left(\frac{2\pi n}{N}\right), n = 0, 1, \dots, N-1 \quad (16)$$

167 The spectrum of the dot product of  $x(\cdot)$  from Equation (1) and the  $W(\cdot)$  from Equation (16) yields Equation  
168 (17):

169 
$$X(k) = -\frac{1}{2j} \left[ A e^{j\theta} \cdot W(\lambda - k) - A e^{j\theta} \cdot W(\lambda + k) \right] \quad (17)$$

$$, k = 0, 1, \dots, N-1$$

170 where  $k$  is the frequency index of the DFT at the  $k$ -th spectral line;  $\lambda$  is the normalized frequency and can  
171 be written in two parts, as indicated in Equation (18) where  $l$  is the integer part of the frequency and  $\delta$  is the  
172 fraction part of the frequency.

173 
$$\lambda = \frac{f \cdot N}{f_0 \cdot N_0} = l + \delta, -0.5 \leq \delta < 0.5 \quad (18)$$

174 Figure 3 shows the interpolation method of the Fourier transform spectrum where  $k$  is the largest index  
175 value in the  $X_k$  amplitude. When  $N$  is large enough, the amplitude can be expressed as:

176 
$$V_k = |X_k| = \frac{N \cdot A \cdot \sin(\pi\delta)}{2\pi\delta} \quad (19)$$

177  $\delta$  is the largest frequency deviation for the true amplitude and the transformed amplitude in the spectrum,  
178 the value range of  $\delta$  is between -0.5–0.5, the left and the right maximum amplitudes have the index values of  $k$ -  
179 1 and  $k+1$ , and its amplitude is expressed as:

180 
$$V_{k\pm 1} = |X_{k\pm 1}| = \frac{N \cdot A \cdot |\sin(\pi\delta)|}{2\pi(1 - |\delta|)} \quad (20)$$

181 After the sampling signal is multiplied by the Hanning Window, the relationship between the largest  
182 amplitude frequency and the second largest amplitude frequency after the transformation— $V_k$  and  $V_{k\pm 1}$ —has  
183 the ratio of  $\alpha$  which is expressed as:

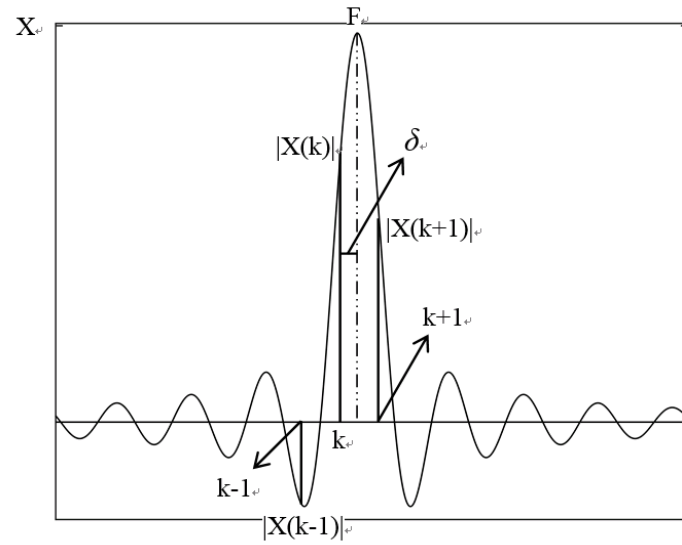
184 
$$\alpha = \frac{V_{k\pm 1}}{V_k} = \frac{1 + |\delta|}{2 - |\delta|} \quad (21)$$

185 Through the Hanning Window relationship, the deviation ratio  $\delta$  is expressed as:

186 
$$\delta = \frac{2\delta - 1}{1 + \delta} \quad (22)$$

187 The amplitude correction value is thus expressed as:

188 
$$V = \frac{2\pi|\delta|(1 - \delta^2)}{N \sin(\pi\delta)} V_k \quad (23)$$



189 **Figure 3.** Interpolation algorithm diagram.

190 Finally, after the amplitude ratio has been incorporated into the frequency domain interpolation using  
 191 Equations (14) and (15), Equation (23) is used to calculate the corrected orthogonal filter amplitude, and then  
 192 incorporate the amplitude value into Equation (11) to accurately evaluate the power system frequency.

### 193 3. Results

194 To verify the performance of the two-level DFT and frequency domain interpolation hybrid method  
 195 proposed in this paper, we performed numerical simulations based on the various voltage signals encountered  
 196 by the actual power system in a MATLAB simulation environment. They include harmonics, inter-harmonics,  
 197 flickers, noises, and frequency offsets.

198 We used four frequency evaluation methods to compare all of the test results: the zero-crossing  
 199 interpolation waveform reconstruction method (ZCIWR) [5], the frequency-domain interpolated (FDI) [8], the  
 200 frequency-domain interpolated waveform reconstruction method (FDIWR) [9], and the method proposed in this  
 201 paper. The objective of the comparisons is to understand the frequency deviations of the frequency estimation  
 202 methods. The frequency absolute value proposed in [4, 26] is used to calculate the relative error as described in  
 203 Equation (24).

$$204 \text{ Relative Error(\%)} = \frac{|\text{Actual Value} - \text{Estimated Value}|}{\text{Actual Value}} \times 100\% \quad (24)$$

205 The IEC 61000-4-7 standard has proposed the 5 Hz frequency resolution recommended value based on  
 206 the DFT technique. That is, the analysis information with the time length of 0.2 s is applied for harmonic and  
 207 inter-harmonic analyses. The sampling frequency is 3000 Hz, and the experimental data window length of  $N$  is  
 208 set to 0.2 s. For the ZCIWR method, the frequency can only be calculated near the vicinity of the zero-crossover.  
 209 To verify the performance frequency evaluation performance, the steady-state data window sliding coefficient  
 210 was obtained as one cycle, and one frequency calculation was conducted for each cycle. To obtain an accurate  
 211 and precise conclusion, each simulated measurement was performed 500 times and the average value is used.

#### 212 3.1. Asynchronous Sampling Basic Frequency Evaluation

213 The IEC 61000-4-30 standard specifies the accuracy tolerance for measurements made by PQ analysis  
 214 instruments. The basic frequency offset tolerance range for a power system with a rated frequency of 60 Hz is  
 215 between 51 Hz and 69 Hz. To test whether the frequency evaluation method can effectively calculate the basic  
 216 frequency, the simulated wave is represented using Equation (25), where  $f_a$  varies between 51 Hz and 69 Hz,  
 217 and the with 1 Hz offset.

$$218 x(t) = \cos(2\pi f_a t) \quad (25)$$

219 Table 1 shows the results according to different frequencies under the various frequency evaluation  
 220 methods. As anticipated, the proposed method is not affected by the  $a$ -th frequency offsets. Table 1 indicated  
 221 that the deviations derived from the calculation method proposed by this paper are lower than  $1e-14$ .

222 **Table 1.** Average relative frequency deviations for different basic frequency offsets.

Frequency Deviation(Hz)	Frequency Evaluation deviation (%)			
	ZCIWR	FDI	FDIWR	Proposed method
51	9.174e-07	3.187e-04	1.087e-10	0
52	4.120e-07	5.431e-05	1.952e-11	9.455e-15
53	2.192e-07	4.192e-04	3.884e-08	8.097e-15
54	1.721e-06	3.191e-04	9.737e-12	1.315e-14
55	1.860e-06	0	1.991e-10	7.027e-15
56	1.649e-06	1.747e-04	4.488e-10	1.268e-14
57	1.934e-06	3.767e-04	1.166e-08	1.246e-14
58	1.784e-06	1.270e-04	6.679e-07	3.381e-15
59	2.671e-06	1.480e-04	2.492e-08	1.204e-14
60	9.852e-13	1.184e-14	0	0
61	1.987e-06	8.175e-05	4.386e-08	1.1648-14
62	1.530e-06	1.784e-04	9.756e-09	1.1460-14
63	2.278e-06	2.697e-04	1.982e-08	0
64	2.987e-06	6.740e-05	4.351e-09	0
65	4.387e-06	0	1.126e-10	0
66	4.756e-06	1.349e-04	2.862e-10	0
67	3.702e-06	1.203e-04	1.599e-09	0
68	3.198e-06	1.211e-04	1.607e-10	0
69	4.031e-06	1.233e-04	4.218e-07	0

### 223 3.2. Basic Frequency Evaluation Under Harmonic and Inter-harmonic Environments

224 In this paper, we referenced the IEC 61000-4-30 standard to propose the harmonic and inter-harmonic  
 225 verification perimeters. The simulated waveform is represented using Equation (26) where  $f_a$  ranged from 51  
 226 Hz to 69 Hz and the offsets were made in 1 Hz increments.

$$227 \quad x(t) = \cos(2\pi f_a t) + 0.1 \cos(3 \times 2\pi f_a t) + 0.05 \cos(5 \times \pi f_a t) + 0.1 \cos(7 \times 2\pi f_a t + \pi) + 0.05 \cos(13 \times 2\pi f_a t) \\ + 0.05 \cos(25 \times 2\pi f_a t) + 0.05 \cos(29 \times 2\pi f_a t) + 0.01 \cos(3.5 \times 2\pi f_a t) + 0.01 \cos(7.5 \times 2\pi f_a t);$$

$$228 \quad (26)$$

229 Table 2 indicates that all four techniques are affected by the harmonics and inter-harmonics in the  
 230 harmonic and inter-harmonic environments. However, the average deviations derived from the frequency  
 231 evaluation algorithm adopted by this paper under a variety of frequency offsets were all better than those of  
 232 other methods.

233 **Table 2.** Average relative frequency deviation under harmonic and inter-harmonic environment.

Frequency Deviation(Hz)	Frequency Evaluation deviation (%)			
	ZCIWR	FDI	FDIWR	Proposed method
51	9.844e-07	3.781e-04	1.033e-04	3.602e-07



52	3.745e-07	4.233e-05	1.361e-05	4.119e-07
53	2.299e-07	4.126e-04	0.002	6.459e-07
54	1.601e-06	3.411e-04	4.764e-05	3.482e-07
55	1.513e-06	2.122e-06	1.565e-05	1.268e-08
56	1.414e-06	2.246e-04	2.939e-05	1.731e-07
57	1.964e-06	3.731e-04	3.879e-05	3.518e-07
58	1.894e-06	8.510e-05	4.630e-05	5.698e-08
59	2.760e-06	1.372e-04	4.218e-05	3.070e-08
60	9.971e-13	1.184e-14	0	0
61	2.025e-06	8.500e-05	4.233e-05	4.798e-09
62	1.504e-06	1.762e-04	3.616e-04	8.195e-08
63	2.169e-06	2.601e-04	7.604e-04	8.980e-08
64	2.906e-06	7.771e-05	3.063e-04	1.6156e-08
65	4.542e-06	5.025e-07	7.562e-07	1.372e-09
66	5.133e-06	1.456e-04	7.672e-06	1.004e-08
67	3.765e-06	8.755e-05	0.001	8.496e-08
68	3.364e-06	9.517e-05	0.004	3.193e-08
69	3.843e-06	1.318e-04	0.005	7.024e-08

### 234 3.3. Basic Frequency Evaluation Under Flickering Environments

235 In addition to the harmonic and inter-harmonic frequencies, power system voltages usually also contain  
 236 flicker frequencies. According to [27], human eyes are most sensitive to a flicker frequency of approximately  
 237 8.8 Hz. Thus, we added two flicker components of 5 Hz and 8.8 Hz to Equation (26), with amplitudes of 0.05%  
 238 and 0.1%, respectively.

239 Table 3 shows the frequency evaluation deviations of the four methods under the harmonic, inter-  
 240 harmonic, and flicker interference environments. The relative deviation obtained using the method proposed by  
 241 this paper was approximately 1e-4%, and was approximately 1e-1% using other methods. Thus, the method  
 242 proposed by this paper has better performance under the harmonic, inter-harmonic, and flicker interference  
 243 environments.

244 **Table 3.** Average relative frequency deviation under flicker environments.

Frequency Deviation(Hz)	Frequency Evaluation deviation (%)			
	ZCIWR	FDI	FDIWR	Proposed method
51	0.050	0.057	0.348	0.009
52	0.048	0.033	0.277	0.005
53	0.045	0.042	0.16	0.002
54	0.040	0.152	0.018	0.002
55	0.035	0.117	0.188	0.002
56	0.029	0.101	0.047	0.001
57	0.024	0.040	0.084	0.001
58	0.019	0.045	0.191	0.001
59	0.015	0.141	0.227	0.001
60	0.013	0.179	0.179	0.003

61	0.014	0.121	0.251	0.009
62	0.017	0.042	0.272	0.010
63	0.020	0.044	0.246	0.011
64	0.024	0.097	0.283	0.006
65	0.028	0.209	0.270	0.008
66	0.031	0.125	0.219	0.010
67	0.034	0.041	0.140	0.011
68	0.036	0.030	0.238	0.005
69	0.050	0.057	0.348	0.009

#### 245 3.4. Basic Frequency Evaluation Under Noise Environments

246 To test whether the frequency estimation algorithm can effectively calculate the basic frequency under a  
 247 noise interference environment, a 60 dB of noise is added to the simulated waveform discussed in 3.3.

248 Table 4 shows the maximum relevant deviation from simulating all of the frequency estimation methods  
 249 500 times in mixed environments. The table indicates that when using the ZCIWR, FDI, FDIWR, and the  
 250 method proposed by this paper in mixed interference environments with a steady-state evaluation frequency of  
 251 between 51–69 Hz; the maximum average relative deviations were 5e-02%, 2e-01%, 3e-01%, and 1e-02%,  
 252 respectively. The results indicate that all four algorithms had good responses in the 60 dB environment.

253 **Table 4.** Maximum relative frequency deviation in a mixed environment.

Frequency Deviation(Hz)	Frequency Evaluation deviation (%)			
	ZCIWR	FDI	FDIWR	Proposed method
51	0.050	0.058	0.347	0.009
52	0.048	0.033	0.278	0.004
53	0.045	0.042	0.160	0.003
54	0.040	0.152	0.019	0.002
55	0.035	0.116	0.181	0.001
56	0.029	0.102	0.047	0.001
57	0.024	0.040	0.083	0.001
58	0.019	0.045	0.191	0.001
59	0.015	0.141	0.227	0.001
60	0.013	0.178	0.175	0.003
61	0.014	0.121	0.251	0.009
62	0.017	0.042	0.272	0.010
63	0.020	0.044	0.246	0.012
64	0.024	0.096	0.282	0.006
65	0.028	0.208	0.269	0.008
66	0.031	0.125	0.219	0.010
67	0.034	0.041	0.140	0.011
68	0.036	0.030	0.238	0.005
69	0.037	0.111	0.166	0.008

254

255

#### 256 4. Conclusion

257 In this paper, we adopted the classic spectrum analysis algorithm used by the majority of scholars—DFT—  
258 as the basis for frequency evaluation for the PQ analysis. A two-level DFT and frequency domain interpolation  
259 hybrid technique is used for basic frequency evaluation. This method used the DFT filter as the basis for the  
260 frequency calculation. This approach can reduce the harmonic and inter-harmonic interferences. The orthogonal  
261 characteristics and the frequency domain interpolation method were then used to further suppress the flicker  
262 components. The experimental results indicated that when the signals sampled using the method proposed by  
263 this paper contained harmonic, inter-harmonic, and flicker components, the method can obtain high-precision  
264 basic frequency that can be used to facilitate subsequent PQ spectrum analyses.

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