

1 Article

# 2 A fuzzy path selection strategy for aircraft landing on 3 the carrier

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10

11 **Abstract:** Landing is one of the most dangerous tasks in all the operations on the aircraft carrier,  
12 and the landing safety is very important to the pilot and the flight deck operation. The problem of  
13 landing path selection is studied in this paper as there several candidates corresponding to  
14 different situations. A fuzzy path selection strategy is proposed to solve the problem considering  
15 the fuzziness of environmental information and human judgment, and the goal is to provide the  
16 pilot with more reasonable decision. The strategy is based on Fuzzy Multi-attribute Group Decision  
17 Making (FMAGDM), which has been widely used in industry. Firstly, the background of the path  
18 selection problem is given. Then the essential elements of the problem are abstracted to build the  
19 conceptual model. A group decision-making method is applied to denote the preference of each  
20 decision maker for each alternative route, and the optimal landing path under the current  
21 environment is determined taking into account the knowledge and the weight of both decision  
22 makers. Experimental studies under different setups, i.e., different environments, are carried out.  
23 The results demonstrate that the proposed path selection strategy is validated in different  
24 environments, and the optimal landing paths corresponding to different environments can be  
25 determined.

26 **Keywords:** landing, aircraft carrier, landing path, fuzziness, fuzzy multi-attribute group decision  
27 making

## 28 1. Introduction

29 Aircraft landing on the carrier is a task with high risk [1]. An aircraft can land on the carrier  
30 successfully with the probability of 70%, and the rate is lower at night. In comparison with  
31 land-based aircraft, landing on an aircraft carrier is more dangerous and complicated since a series  
32 of particular conditions needs to be taken into account. Besides, the flight condition and the  
33 maritime environment are changing all the time, and these uncertainties make the landing task  
34 difficult [2-3]. In order to guide the aircraft landing safely, an aircraft carrier must be equipped with  
35 certain special guidance devices such as the Fresnel lens optical landing system [4], the all-weather  
36 radar landing system [5] and so on. Besides, a variety of commanders and staffs are needed to  
37 guarantee the landing safety of aircraft and cope with all emergencies [6]. Among them, the landing  
38 console operator (LCO) onboard is responsible for supervising the aircraft which are about 20  
39 nautical miles away from the aircraft carrier. The landing signal officer (LSO) concentrates on the  
40 last step of landing, and he assists the pilot to land safely using the body language or by talking to  
41 the pilot directly [7]. The air officer in the control tower does the work related to the flight deck, e.g.,  
42 preparing flight deck for launching, managing the carrier aircraft on the flight deck and emptying  
43 the deck for landing. Each staff mentioned above takes their own duty at different stages of landing,  
44 and the landing safety of aircraft is accomplished by their team work.

45 In each landing stage, the above commanders and staffs make a decision to guide the aircraft in  
46 a very short time based on their knowledge and the information shown on various instruments,  
47 which makes high-level demands on the judgment and reaction of them [8]. However, there is

48 fuzziness in the environment and flight information, and accurate judgment cannot always be  
49 reached quickly, which attributes to the complicacy and variability of weather at sea, the lack of  
50 comprehensive information and other subjective factors affected. In recent years, artificial  
51 intelligence (AI) is widely applied to various fields and many great achievements have been made in  
52 this field. For instance, the complex changes and uncertainties in manufacturing can be managed by  
53 AI and machine learning techniques [9]. Another case in point is the routing problems for ground  
54 vehicles, and minimal total cost can be achieved using AI without violating the capacity and time  
55 window constraints [10]. Correspondingly, there exists a high possibility that the idea of AI can be  
56 introduce to the landing path selection system of aircraft in order to solve the fuzziness and reduce  
57 the workload of the staffs onboard. Furthermore, a new AI-based path selection strategy is expected  
58 to response quickly with more accurate judgment and improve the safety level of the landing.

59 Currently, a large amount of researchers concentrate primarily on the analysis of landing safety,  
60 the modeling of LSO's action and the establishment of variable strategy pilot model. For example,  
61 the landing safety is analyzed based on the rough set theory, and the values of kinematical  
62 parameters and their combinations are determined to define the boundary conditions for safe  
63 landing [11]. The action of LSO is described by a fuzzy language, and multiple AI techniques are  
64 applied to the landing decision-support tool. The obtained landing decision-support tool allows the  
65 LSO to make better time-critical decisions in a dangerous environment [12]. The gesture of the LSO  
66 is also studied extensively, and a multi-signal gesture database, which requires both body  
67 knowledge and hand knowledge of the LSO to distinguish gestures, was introduced. Subsequently,  
68 the true meaning of gestures obtained based on the gesture database is communicated to the pilot to  
69 enable a better understanding and assist landing [13]. Our team also conducted research intensively  
70 on the automatic landing guidance technology. A model of LSO was found for the digital simulation  
71 of a pilot-carrier system on the basis of analyzing the behaviors of LSO in the final stage of landing.  
72 Fuzzy logic laws were used to model three kinds of behaviors of the LSO. Afterwards, the carrier  
73 motion prediction of the LSO is described by a neural network model, and the model was verified by  
74 simulating landing under several kinds of conditions [14]. In the aspect of studying the pilot  
75 behaviors, a variable-strategy pilot model is established for landing. This model is comprised of two  
76 switchable components: a discrete component of the acquisition strategy for a large deviation of the  
77 glide path and a continuous component of the pursuit tracking strategy for a small deviation [15].  
78 The cited literature can explain the work of LSO, and mathematical models are established to  
79 describe the LSO's action. They presented solid research work on the automatic landing guidance  
80 technology and have potential significance in the landing safety of aircraft. The issue of landing path  
81 for aircraft carrier is also an important part of the automatic landing guidance technology. Unlike the  
82 unmanned aerial vehicles (UAV) path planning problem [16], the landing path of manned aircraft is  
83 fixed and only can be selected from several candidate modes. Therefore, instead of planning the  
84 landing path, it is determined before the aircraft is ready to reach the carrier, and determine the  
85 landing path is also a part of the LCO's work. However, no relevant literature has been reported on  
86 this issue so far. As the landing path selection is the first step to guide the aircraft landing, it is  
87 important to the automatic landing system and thus worthwhile to be studied intensively.

88 Similar to land-based aircraft, aircraft on the carrier receive the position information from the  
89 onboard equipment and use this information to confirm its location before approaching the carrier.  
90 As the carrier is moving all the time, the pilot has to keep in touch with the flight control center and  
91 correct the path constantly according to the feedbacks from the flight control center. According to  
92 the performance, the traffic conditions, a variety of weather conditions and visibility, the pilot selects  
93 one of the candidate paths. However, if the pilot senses the shortage of aircraft fuel or a mechanical  
94 failure occurred to the aircraft, he has to communicate with the LCO directly to carry on air refueling  
95 or an emergency landing on the ground in land bases. In view of the fact that fuzziness of various  
96 factors and information are involved in the landing path selection problem [17], some unreasonable  
97 decisions may be made if the knowledge and experience of human are only depended on. Therefore,  
98 a landing path selection strategy is imperative to deal with the above defects, thus reducing the  
99 workload of staffs and improving the safety level of landing.

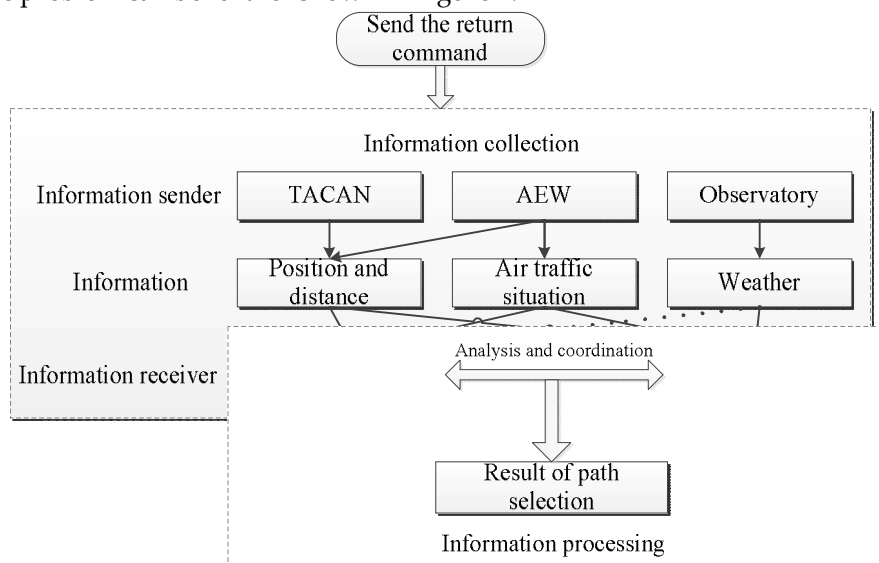
100 The main contribution of this paper is to establish a mathematical model and provide a method  
 101 to solve the landing path selection problem. This problem is a sort of decision-making problem  
 102 which belongs to the air traffic management of carrier. To make a subjective judgment optimal and  
 103 practical, a decision needs to be made based on reliable information and considering all constraints.  
 104 Obtaining the environmental information quickly is essential to the decision-making in this  
 105 problem. Moreover, how to process information according to the knowledge and experience is the  
 106 key. The problem involves various elements and fuzzy information. Therefore, it is an unstructured  
 107 decision-making problem. This kind of problem can only be solved based on the experience and  
 108 flexibility of a decision maker or using an AI method. It is also worth noting that different decision  
 109 makers may result in different judgments due to many reasons. For example, they obtain different  
 110 information, they are assigned different flight tasks and objectives, or they have different  
 111 understanding of performance criteria. Considering all the above-mentioned factors, this paper  
 112 introduces a group decision-making scheme, which is an effective method to coordinate the above  
 113 differences and result in a reasonable decision.

## 114 2. Problem statement and conceptual model establishment

115 In this section, the landing path selection problem will be described firstly, and then the  
 116 essential elements involved in the problem are discussed. A brief conceptual model is given at the  
 117 end of this section to give an overview for solving this problem.

### 118 2.1 Problem statement

119 According to the tactical imperatives, aircraft receives the returning information from the air  
 120 control system on the carrier. To ensure the safety of returning flight, the real-time position  
 121 information is provided by the Tactical Air Navigation (TACAN), which contains the relative  
 122 position to the carrier. Besides, the returning aircraft is also instructed by an airborne early warning  
 123 (AEW), which provides the returning aircraft with the overall air traffic situation. The information  
 124 from an AEW is essential when managing the landing paths for a large amount of airplanes in order  
 125 to guarantee a safe and orderly landing. The sea weather is obtained through the observatory on the  
 126 carrier and is transmitted to a pilot. To sum up, the landing path selection problem is a process that  
 127 the pilot and LCO combine/analyze various information and make quick decision accordingly. The  
 128 details of the problem can be further shown in Figure 1.



129

130 **Figure 1.** Description of the landing path selection problem.

131 The dotted line in Figure 1 denotes that when the pilot selects the optimal landing path, he/she  
 132 just treat the weather information as a reference instead of relying on it to make a judgment. This is  
 133 because the weather information is relative to the carrier, and there may be differences between the

134 places around the aircraft and around the carrier. This explains why the pilot just regards the  
 135 weather information from an observatory as a reference.

136 In Figure 1, the pilot and the LCO are the decision makers when determining the optimal  
 137 landing path. Besides, the LCO is the major decision maker because he/she masters the air traffic  
 138 situation better thus enhancing the safety level of landing. What's more, the feeling of a pilot is  
 139 considered limitedly although he/she has a comprehensive understanding of the weather  
 140 information and the performance of the aircraft. The reason is as follows. In actual work, the pilot  
 141 usually has a heavy workload, e.g., executing a flight mission and analyzing various information  
 142 simultaneously, therefore, he/she will be distracted from other work and his/her judgment will be  
 143 affected accordingly.

## 144 2.2 Essential elements

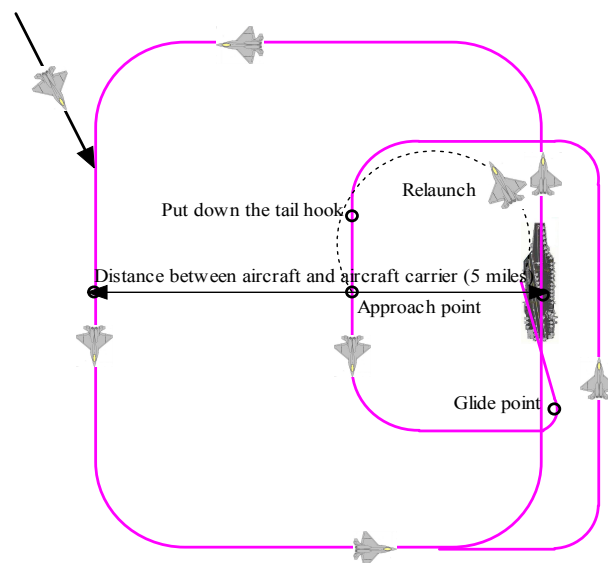
145 According to the problem description, there are several essential elements in the path section  
 146 problem: the decision makers, the alternative landing paths and the contributing factors. The  
 147 decision makers have been analyzed above, the rest two will be discussed in this section.

### 148 1. The alternative landing paths:

149 There are four modes of landing path according to the differences in atmospheric environment,  
 150 performance of an aircraft and the air traffic situation, as listed below.

151 ①  $I_1$ : The weather, visibility, performance of an aircraft and air traffic situation are all in good  
 152 conditions.

153 The pilot lands the aircraft by vision under such conditions. The aircraft flies counterclockwise  
 154 following the rectangular route above the carrier, as shown in Figure 2.



155

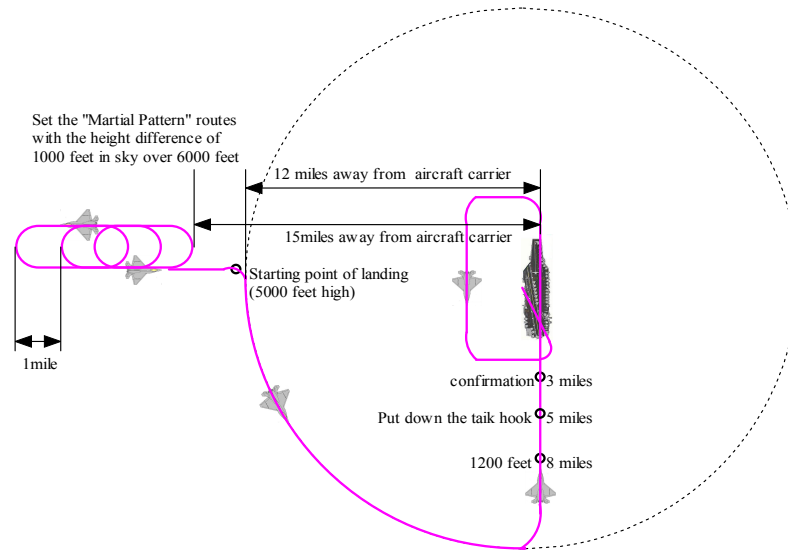
156 **Figure 2.** General view of alternative landing path  $I_1$

157 The carrier is located in the center of the right edge of the rectangle at this moment. If the aircraft  
 158 keeps waiting for the landing command, it will fly counterclockwise following the rectangular path  
 159 and get in touch with the approaching operation person every time it passes the carrier to confirm  
 160 the landing permission.

161 ②  $I_2$ : The weather and visibility are at a medium level and the performance of the aircraft and  
 162 air traffic are in good conditions.

163 A landing mode with higher safety standard will be adopted when the clouds appear between  
 164 the height of 1000 and 3000 feet and cover more than 5/8 of the sky. It becomes dangerous to land the

165 aircraft by vision due to the heaviness of clouds. Therefore, a landing path called "Martial Pattern" is  
 166 set 15 miles away from the carrier to guarantee the landing safety, as shown in Figure 3. The aircraft  
 167 will repeat the "Martial Pattern" until it is permitted to land.

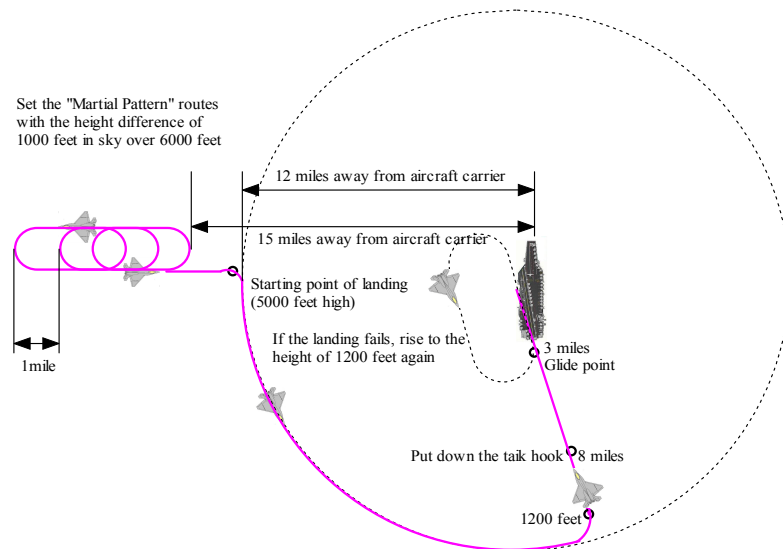


168

169 **Figure 3.** General view of alternative landing path  $l_2$

170 ③  $l_3$ : The weather and visibility are bad, but the performance of the aircraft and the air traffic  
 171 are in good conditions.

172 It is also unsafe to for the pilot to land the aircraft by vision in such conditions. Similarly,  
 173 "Martial Pattern" is set 15 miles away from the carrier and the aircraft repeats the "Martial Pattern"  
 174 before being permitted to land, as shown in Figure 4. Unlike in the case of  $l_2$ , the aircraft does not  
 175 have to fly a rectangle route around the carrier after receiving the landing permission. Instead, it  
 176 approaches the carrier directly with gliding.



177

178 **Figure 4.** General view of alternative landing path  $l_3$

179 ④  $l_4$ : The performance of aircraft is poor or the air traffic is in a bad condition.

180 There are no proper conditions for aircraft landing on the carrier. In this case, the pilot has to get  
 181 in touch with the land base for emergency landing.

182

183 2. The contributing factors:

184 According to the analysis on the alternative landing paths, the contributing factors for the  
185 landing paths selection problem can be concluded as follows:

186 ①Weather

187 It is usually difficult to predict the weather around a large area accurately because no obstacles  
188 exist above the sea and the air flow above the sea is active. Therefore, the weather information is  
189 obtained by mastering the nearby weather condition continuously. Usually,  $l_1$ ,  $l_2$  and  $l_3$  are  
190 chosen for good, medium and bad weather respectively.

191 ②The height of clouds

192 The vision of a pilot will be impaired when the clouds are low or cover a wide range of the sky.  
193 The heavy cloud may even lead to a bump of an aircraft during the flight. Therefore  $l_1$  is preferred  
194 when there are few or no clouds. Otherwise  $l_2$  or  $l_3$  which enjoy higher safety standard will be  
195 preferred.

196 ③Visibility

197 The level of visibility plays an important role in affecting the visual observation and the  
198 judgment of a pilot. Good visibility often leads to choose  $l_1$  or  $l_2$ . On the contrary,  $l_3$  or even  $l_4$   
199 will usually be chosen for poor visibility.

200 ④Performance of aircraft

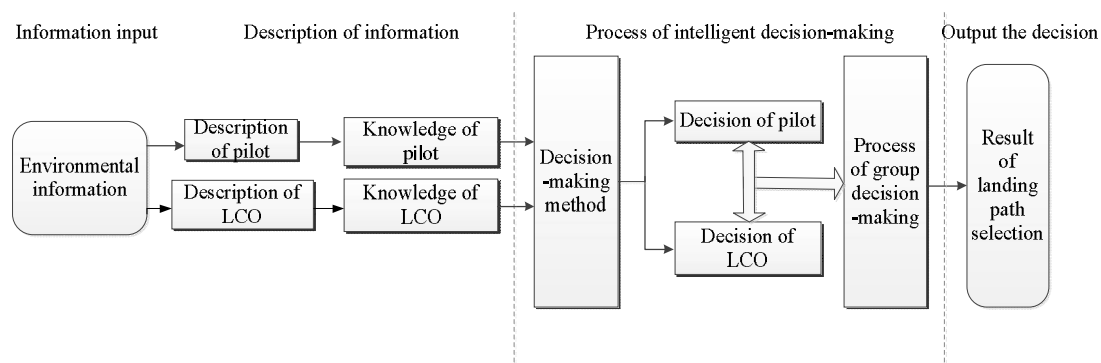
201 The aircraft is usually in good performance during the flight and will land on the carrier  
202 according to the command received. However, the aircraft may get damaged when accidents occur,  
203  $l_4$  will be the best choice in this case to guarantee the landing safety.

204 ⑤Air traffic situation

205 It refers to the status of other aircraft near the landing aircraft. If the air traffic is crowded or the  
206 returning schedule fails,  $l_4$  provides a safe landing solution.

### 207 2.3 The conceptual model

208 Based on the description of the landing path selection problem and the analysis of its essential  
209 elements, the key components involved in the problem are abstracted, and a conceptual model is  
210 established, see Figure 5, to provide the reader a general idea of decision-making when solving this  
211 problem.



212

213 **Figure 5.** Conceptual model of the landing path selection problem

### 214 3. FMAGDM (Fuzzy Multi-attribute Group Decision Making)-based path selection method

215 The conceptual model provides a general idea of decision-making. Mathematical descriptions of  
216 the essential elements are needed to establish the model. Since it is difficult to describe the real-time  
217 environmental information quantitatively, the judgment of a single pilot or a single LCO is often  
218 inaccurate. Therefore, it is necessary to develop a comprehensive decision-making method which  
219 integrates the judgments of both the pilot and the LCO to make the final decision more scientific and

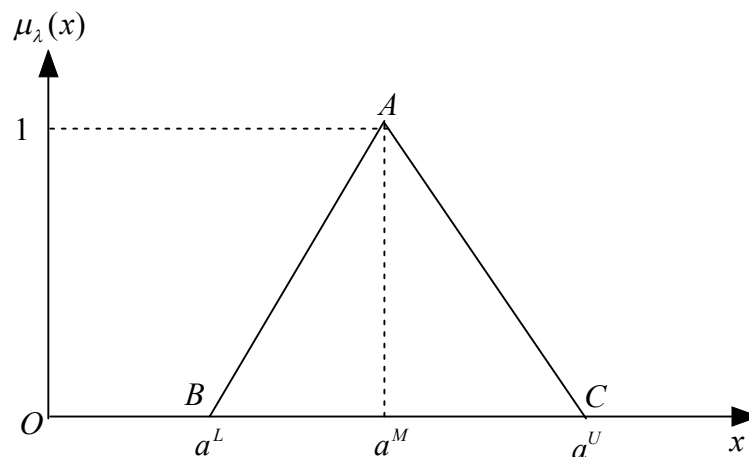


220 reasonable. In view of the abovementioned characteristic, the FMAGDM method can describe the  
 221 environmental information and the weights of decision-makers [18-20] and is suitable for solving the  
 222 path selection problem. To be specific, the fuzzy TOPSIS (Technique for Order Preference by  
 223 Similarity to an Ideal Solution) approach [21, 22] is developed, and the triangular membership  
 224 function is used to describe the performance ratings of contributing factors (short for PRCF for  
 225 convenience in the rest of this paper) and the current environmental vector. Then a mathematical  
 226 model is established to evaluate each alternative landing path. To coordinate the decisions of the  
 227 pilot and the LCO, the group decision-making method based on fuzzy judgment is introduced to  
 228 rank the alternative landing paths. Finally, the optimal landing path under the current environment  
 229 is obtained.

### 230 3.1 The PRCF and the current environmental vector

231 In the process of building a decision-making model, the PRCF or the current environmental  
 232 vector need to be described using fuzzy linguistic variables. The triangular membership function is  
 233 then introduced to define the value of each fuzzy linguistic variable. For example, "low", "medium"  
 234 or "high" is used to express the performance rating of  $l_1$  with respect to the weather, and the  
 235 triangular membership function is used to define "low", "medium" or "high". Therefore, the  
 236 triangular membership function is the foundation of establishing the decision-making model. The  
 237 concept and properties of the triangular membership function are presented below to ensure a better  
 238 understanding of its application in the path selection problem [23].

239 **Definition 1:** Let  $a = [a^L, a^M, a^U]$  be a triangular membership function with  
 240  $0 < a^L \leq a^M \leq a^U$ , as shown in Figure 6.



241

242 **Figure 6.** The triangular membership function

243 An example is presented to make a clear understanding of its function in describing the current  
 244 environmental vector. Triangular membership function  $a$  is used to describe good visibility. The  
 245 plots indicate that the possibility for this case, i.e., the current visibility belongs to the "good  
 246 visibility", increases from point B to point A and reaches the maximum in point A. On the contrary,  
 247 the possibility decreases from point A to point C and reaches the minimum in point C.

248 **Definition 2:** The mean value of a triangular membership function  $a$  is defined as

$$249 \quad s(a) = (a^L + 2a^M + a^U) / 4 \quad (1)$$

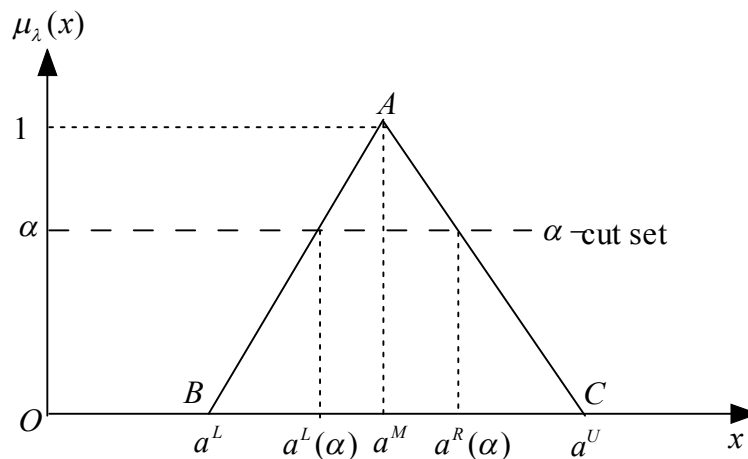
250 The mean value property is used to sort the triangular membership functions. In view of the  
 251 triangular membership functions  $a$  and  $b$ , there is a definition as follows:  $a \geq b$  if  $s(a) \geq s(b)$

252 and  $a < b$  if  $s(a) < s(b)$ . For example, if  $a$  and  $b$  describe different performances of an aircraft,  
 253  $a \geq b$  denotes the performance described by  $a$  is better than that described by  $b$  in general.

254 **Definition 3:** Assume  $U$  is a universe of discourse and the  $\alpha$ -cut set  $a_\alpha$  is defined as

$$255 \quad a_\alpha = \{x \in U \mid \mu_\lambda(x) \geq \alpha\}, \alpha \in [0, 1] \quad (2)$$

256 where  $a_\alpha$  can be denoted as  $a_\alpha = [a^L(\alpha), a^R(\alpha)]$ , as shown in Figure 7. If  $a$  presents the  
 257 medium weather,  $a_\alpha$  denotes that the degree of that is more than  $\alpha$ .



258

259 **Figure 7.** Definition of  $\alpha$ -cut set in triangular membership function

260 **Definition 4:** Given triangular membership functions  $a = [a^L, a^M, a^U]$  and  $b = [b^L, b^M, b^U]$   
 261 with  $a \geq b$ , the fuzzy distance between  $a$  and  $b$  is defined as follows.

$$262 \quad d(a, b) = [\max\{\int_0^1 d^L(\alpha) d\alpha, 0\}, d^L(1), \int_0^1 d^R(\alpha) d\alpha] \quad (3)$$

263 where  $d^L(\alpha)$  and  $d^R(\alpha)$  are defined as below:

$$264 \quad \begin{cases} d^L(\alpha) = a^L(\alpha) - b^R(\alpha) \\ d^R(\alpha) = a^R(\alpha) - b^L(\alpha) \end{cases} \quad (4)$$

265 Similar to the definition of a distance in a geometric space, the fuzzy distance also represents the  
 266 degree of approximation between these two triangular membership functions. For example, suppose  
 267 that  $a$  and  $b$  describe good and bad air traffic situation respectively, then  $d(a, b)$  represents how  
 268 large the difference is between these two air traffic conditions. It should be noted that  $d(a, b)$  is  
 269 also a triangular membership function.

270 Up to now, the knowledge of triangular membership function, which is used to describe the  
 271 fuzzy linguistic variables when establishing a decision-making model, has been given. Besides, some  
 272 main operations associated with triangular membership functions are listed below ( $a$  and  $b$  are two  
 273 random triangular membership functions,  $k$  is a random real number):

$$274 \quad \textcircled{1} a + b = [a^L, a^M, a^U] + [b^L, b^M, b^U] = [a^L + b^L, a^M + b^M, a^U + b^U]; \quad (5)$$

$$275 \quad \textcircled{2} a \times b = [a^L, a^M, a^U] \times [b^L, b^M, b^U] = [a^L \times b^L, a^M \times b^M, a^U \times b^U]; \quad (6)$$

$$276 \quad \textcircled{3} k \times a = [k \times a^L, k \times a^M, k \times a^U]; \quad (7)$$



$$277 \quad \textcircled{4} a^{-1} = [1/a^U, 1/a^M, 1/a^L]. \quad (8)$$

### 278 3.2 Decision-making process with the developed fuzzy TOPSIS approach

279 The weather condition, cloud height, visibility, performance of aircraft and air traffic situation  
 280 are the five key contributing factors determining the result of landing path selection which can be  
 281 written as  $f_1, f_2, f_3, f_4$  and  $f_5$  respectively. The PRCF are described by triangular  
 282 membership functions. Among the five contributing factors, only the performance ratings of clouds  
 283 height and visibility can be described quantitatively, as shown in Table 1.

284 **Table 1.** Description of performance ratings for five contributing factors

	$f_1$	$f_2$	$f_3$	$f_4$	$f_5$
Good		>3000 feet	>5 km	Medium	Good
Bad		1000-3000 feet	>5 km	Good	Good
Terrible		< 1000 feet	< 5km	Good	Good
Indifferent		Indifferent	Indifferent	Bad	Bad

285 The above descriptions need to be unified with the same linguistic variables, as shown in Table  
 286 2.

287 **Table 2.** Unified linguistic variables of performance ratings

Linguistic variable	No	Low	Medium	High	Very high
Expression	NO	LO	ME	HI	VH

288 It should be mentioned that all the linguistic variables in Table 2 will be described by triangular  
 289 membership functions later. Suppose that the performance rating of  $I_j$  ( $j = 1, 2, 3, 4$ ) with respect  
 290 to  $f_i$  ( $i = 1, 2, 3, 4, 5$ ) is denoted as  $e_{ij} = [e_{ij}^L, e_{ij}^M, e_{ij}^U]$  (the value of  $e_{ij}$  can be chosen from Table  
 291 2, then the fuzzy decision matrix for the path selection problem can be established as follows:

$$292 \quad D = \begin{bmatrix} e_{11} & e_{12} & e_{13} & e_{14} \\ e_{21} & e_{22} & e_{23} & e_{24} \\ \vdots & \vdots & \vdots & \vdots \\ e_{51} & e_{52} & \dots & e_{54} \end{bmatrix} \quad (9)$$

293 where matrix  $D$  is the knowledge base which has been mastered by the decision makers in advance.

294 Having introduced the basics of the developed fuzzy TOPSIS approach for solving the path  
 295 selection related decision making problem, the detailed procedure will be described below.

#### 296 Step 1: Normalize of the fuzzy decision matrix

297 Different contributing factors, e.g., the descriptions of  $f_2$  and  $f_3$ , use different measurement  
 298 units when collecting raw data. Therefore, normalization is needed to transform  $e_{ij}$  into the  
 299 interval of  $[0,1]$  in order to eliminate anomalies. In this paper, a linear transformation is adopted to  
 300 get the normalized fuzzy decision matrix  $X$ :

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} \\ x_{21} & x_{22} & x_{23} & x_{24} \\ \vdots & \vdots & \vdots & \vdots \\ x_{51} & x_{52} & \dots & x_{54} \end{bmatrix} \quad (10)$$

Since the PRCF denote the efficiency in the path selection problem,  $x_{ij}$  can be normalized using the largest value, i.e., efficiency, of this contributing factor:

$$x_{ij} = [e_{ij}^L / e_i^{U_{\max}}, e_{ij}^M / e_i^{U_{\max}}, e_{ij}^U / e_i^{U_{\max}}] \quad (11)$$

where  $e_i^{U_{\max}} = \max_{1 \leq j \leq 4} \{e_{ij}^U\} (i = 1, 2, \dots, 5, j = 1, 2, 3, 4)$ . Using Eq. (11), all linguistic variables can be transformed into the interval of [0,1].

The pilot and the LCO are regarded as the decision maker 1 and 2 respectively, and the normalized fuzzy decision matrix  $X_1$  and  $X_2$  can be established according to the knowledge and experience of decision makers.

$$X_1 = \begin{bmatrix} HI & ME & LO & NO \\ VH & HI & LO & NO \\ VH & VH & LO & LO \\ ME & HI & HI & LO \\ ME & HI & HI & LO \end{bmatrix}, X_2 = \begin{bmatrix} HI & ME & NO & NO \\ HI & ME & LO & NO \\ HI & HI & LO & NO \\ ME & HI & HI & ME \\ HI & VH & VH & LO \end{bmatrix}$$

Comparing  $X_1$  with  $X_2$ , it can be found that the performance ratings of a pilot is higher than that of the LCO with respect to the atmospheric environment in general. This is because the pilot has true feelings of the atmospheric environment, and he/she is usually conservative for safety reason when determining the landing path. Besides, performance ratings with respect to the air traffic situation are set higher by the LCO compared to the pilot. This is because the LCO grasps comprehensive traffic information, and he/she puts higher priority on safety operation around the carrier.

*Step 2: Integrate the current environment vector into the normalized fuzzy decision matrix*

The environmental vector for the case under consideration can also be described using linguistic variable, as shown in Table 3.

**Table 3.** Linguistic variable of environmental vector (for a case under consideration)

Linguistic variable	Too poor	A little poor	Normal	Good	Very good
Expression	TP	LP	NO	GO	VG

The environmental evaluation of each contributing factor is denoted as  $\omega_i = [\omega_i^L, \omega_i^M, \omega_i^U]$ ,

which compose the environmental vector ( $i = 1, 2, \dots, 5$ , the value of  $\omega_i$  can be chosen from Table 3).

Then the normalized fuzzy decision matrix integrating the environmental vector can be calculated as follows:

$$326 \quad Z = (z_{ij})_{5 \times 4} = (\omega_i x_{ij})_{5 \times 4} = \begin{bmatrix} z_{11} & z_{12} & z_{13} & z_{14} \\ z_{21} & z_{22} & z_{23} & z_{24} \\ \vdots & \vdots & \vdots & \vdots \\ z_{51} & z_{52} & \dots & z_{54} \end{bmatrix} \quad (12)$$

327 *Step 3: Determine the positive and negative ideal solutions*

328 The positive ideal solution is obtained when each PRCF chooses its highest value from the fuzzy  
329 decision matrix D, and the negative solution is obtained by choosing the lowest value for each  
330 performance rating. These solutions are called the ideal solutions because the corresponding cases  
331 are almost impossible to happen in reality.

332 The fuzzy positive ideal reference point (FPIRP) and negative point (FNIRP) are written as P  
333 and N for convenience. Besides, the FPIRP and FNIRP are defined as  $P = (p_1, p_2, \dots, p_5)$  and  
334  $N = (n_1, n_2, \dots, n_5)$  with  $p_i = \max_{1 \leq j \leq 4} \{z_{ij}\}$  and  $n_i = \min_{1 \leq j \leq 4} \{z_{ij}\}$ .

335 *Step 4: Calculate the fuzzy distance between  $l_j (j = 1, 2, \dots, 4)$  and P (or N)*

336 According to Eq. (3), the fuzzy distance between  $l_j (j = 1, 2, \dots, 4)$  and P (or N) are defined as

337 follows:

$$338 \quad d(l_j, P) = \sum_{i=1}^5 d(z_{ij}, p_i) \quad (13)$$

$$339 \quad d(l_j, N) = \sum_{i=1}^5 d(z_{ij}, n_i) \quad (14)$$

340 The optimal landing path is the one which is close to the FPIRP and far away from the FNIRP.  
341 According to different distances from the FPIRP, a ranking list of all the alternative landing paths  
342 can be determined.

343 *Step 5: Obtain the closeness coefficient*

344 The larger the closeness coefficient is, the closer the alternative landing path is to the fuzzy ideal  
345 solution. The following formula is adopted to calculate the closeness coefficient and distinguish the  
346 importance between FPIRP and FNIRP.

$$347 \quad C(l_j) = \mu \frac{d(l_j, P)}{d(l_j, P) + d(l_j, N)} + (1 - \mu) \frac{d(l_j, N)}{d(l_j, P) + d(l_j, N)} \quad (15)$$

348 where  $\mu (0 < \mu < 1)$  is a weight for different distances from FPIRP and FNIRP, and it is determined  
349 by the subjective attitude of a decision maker. If the atmospheric environment is good in general, the  
350 decision maker usually puts more attention on FPIRP and set  $\mu$  as a smaller value. A larger value  
351 will be set for  $\mu$  to put more attention on FNIRP if the air traffic situation is bad.

352 *3.3 Process of the group decision-making*

353 The decision of a pilot or a LCO can be calculated separately according to the above mentioned  
354 procedure. In reality, decision made by one of them may not be the optimal solution because

355 different decision makers obtain different information and have difference in knowledge and  
 356 preference. Therefore, to deal with the divergence and make an optimal decision, the decision of  
 357 both the pilot and the LCO should be integrated. The group decision-making problem will be  
 358 discussed and addressed in this section.

359 The main idea of solving the group decision-making problem is to regard the pilot and the LCO  
 360 as two contributing factors. Then the group decision-making problem can be translated into a single  
 361 person decision-making problem [24]. The group fuzzy decision matrix is constructed as follows:

$$362 \quad O = \begin{bmatrix} o_{11} & o_{12} & \cdots & o_{14} \\ o_{21} & o_{22} & \cdots & o_{24} \end{bmatrix} \quad (16)$$

363 where  $o_{st}$  ( $s=1,2;t=1,2,3,4$ ) is the closeness coefficient  $C(l_j)$ , which is calculated for each  
 364 decision maker using Eq. (15). The group decision-making solution is depicted in detail by the  
 365 following steps:

366 Step 1: The matrix  $O$  is a normalized fuzzy decision matrix by itself so the step of normalization  
 367 can be skipped. We assume the weights of pilot and LCO as  $\lambda_1 = [\lambda_1^L, \lambda_1^M, \lambda_1^U]$  and  
 368  $\lambda_2 = [\lambda_2^L, \lambda_2^M, \lambda_2^U]$  respectively. The weighted normalized group fuzzy decision matrix can be  
 369 calculated in the same way as in section 3.2 and is written as  $V = (v_{kj})_{2 \times 4}$  ( $k=1,2;j=1,2,3,4$ ).  
 370 Note that the opinion of the LCO should be granted greater weight due to the fact that the LCO is  
 371 less subject to many kind of distraction compared to a pilot. On the other hand, the opinion of the  
 372 pilot should be also taken into account since he/she has a better feeling in weather and knows better  
 373 the current aircraft performance.

374 Step 2: Write the fuzzy positive group ideal reference point (FPGIRP) and negative point  
 375 (FNGIRP) as  $GP$  and  $GN$  respectively. The FPGIRP and FNGIRP can be formulated as  
 376  $GP = (gp_1, gp_2)$  and  $GN = (gn_1, gn_2)$  where  $gp_k = \max_{1 \leq j \leq 4} \{v_{kj}\}$  and  $gn_k = \min_{1 \leq j \leq 4} \{v_{kj}\}$ .

377 Step 3: Calculate the fuzzy distance and the closeness coefficient.

$$378 \quad d(l_j, GP) = \sum_{k=1}^2 d(v_{kj}, gp_k) \quad (17)$$

$$379 \quad d(l_j, GN) = \sum_{k=1}^2 d(v_{kj}, gn_k) \quad (18)$$

$$380 \quad GC(l_j) = \eta \frac{d(l_j, GP)}{d(l_j, GP) + d(l_j, GN)} + (1 - \eta) \frac{d(l_j, GN)}{d(l_j, GP) + d(l_j, GN)} \quad (19)$$

381 where  $\eta$  ( $0 < \eta < 1$ ) is the subjective attitude of the group, which reflects the different importance  
 382 of FPGIRP and FNGIRP. Therefore, the principle of choosing  $\eta$  is similar to that of  $\mu$ .

383 Step 4: Calculate the mean value  $s(GC(l_j))$  according to Eq. (1). The path corresponding to  
 384  $\max_{1 \leq j \leq 4} \{s(GC(l_j))\}$  is the optimal landing path in the current environment. Besides, the rank of  
 385 alternative paths can be calculated at the meantime. Note that: the final decision has to be close to  
 386 those of both decision makers.

#### 387 4. Experimental study on landing path selection in different environments

388 In this section, experiments are conducted to investigate the effectiveness of the proposed path  
 389 selection strategy. Four different environmental conditions are set as test scenarios to verify its  
 390 reasonability. Under the known priori knowledge, experience, current environment evaluations and

391 weights of decision makers, the path selection strategy is expected to choose the optimal landing  
392 path for the current environment.

#### 393 4.1 Simulation conditions and their fuzzy descriptions

394 The performance ratings and environment evaluations are shown in Table 4.

395 **Table 4.** Expressions of performance ratings and environment evaluations

	Linguistic variables and expressions				
Performance ratings	NO	LO	ME	HI	VH
Environment evaluations	TP	LP	NO	GO	VG
Triangular membership function	[0,0,0.1]	[0.1,0.3,0.5]	[0.3,0.5,0.7]	[0.5,0.7,0.9]	[0.9,1,1]

396 Four pairs of simulations are carried out independently to validate the reasonably of the  
397 proposed method in different environments,. The environment settings and evaluations of decision  
398 makers are presented in Table 5 and Table 6.

399 **Table 5.** Environment settings

Serial number of simulation	Environments
i	The weather, clouds height and visibility are good while the performance of aircraft and air traffic situation are normal.
ii	The weather, clouds height and visibility are not good enough while the performance of aircraft and air traffic situation are good.
iii	The weather, clouds height and visibility are bad while the performance of aircraft and air traffic situation are good.
iv	The weather, clouds height and visibility are normal while the performance of aircraft and air traffic situation are bad.

400 **Table 6.** Environment evaluations of decision makers

Contributing factors		$f_1$	$f_2$	$f_3$	$f_4$	$f_5$
Simulation i	Pilot	VG	VG	VG	NO	NO
	LCO	GO	GO	GO	GO	GO
Simulation ii	Pilot	GO	GO	GO	GO	GO
	LCO	LP	LP	NO	GO	VG
Simulation iii	Pilot	TP	TP	TP	GO	GO
	LCO	TP	TP	TP	GO	VG
Simulation iv	Pilot	LP	LP	NO	NO	TP
	LCO	TP	NO	LP	NO	TP
Weight of decision maker	Pilot $\lambda_1 = [0.4, 0.5, 0.6]$ LCO $\lambda_2 = [0.8, 0.9, 1]$					

## 401 4.2 Results and analyzes of landing path selection

402 The proposed landing path selection strategy is applied to determine the optimal landing path  
 403 for four different validating environment conditions. The results are given in Table 7-10. For each  
 404 test case, the optimal landing path and the ranking the four alternative paths are given.

405 **Table 7.** Results of simulation i

Alternative route	$l_1$	$l_2$	$l_3$	$l_4$
Closeness coefficient	[0,0.82,161.06]	[0,0.80,159.28]	[0,0.51,107.62]	[0,0.20,55.49]
Mean value	40.67	40.22	27.16	13.97
Rank	$l_1 > l_2 > l_3 > l_4$			
The optimal landing path	$l_1$			

406 **Table 8.** Results of simulation ii

Alternative route	$l_1$	$l_2$	$l_3$	$l_4$
Closeness coefficient	[0,0.74,87.00]	[0,0.80,88.11]	[0,0.58,61.20]	[0,0.20,31.48]
Mean value	22.12	22.43	15.59	7.97
Rank	$l_2 > l_1 > l_3 > l_4$			
The optimal landing path	$l_2$			

407 **Table 9.** Results of simulation iii

Alternative route	$l_1$	$l_2$	$l_3$	$l_4$
Closeness coefficient	[0,0.51,5.24]	[0,0.80,5.89]	[0,0.80,6.41]	[0,0.20,2.84]
Mean value	1.57	1.87	2.00	0.81
Rank	$l_3 > l_2 > l_1 > l_4$			
The optimal landing path	$l_3$			

408 **Table 10.** Results of simulation iv

Alternative route	$l_1$	$l_2$	$l_3$	$l_4$
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Closeness coefficient	[0,0.20,6.47]	[0,0.21,6.50]	[0,0.47,7.23]	[0,0.80,6.79]
Mean value	1.72	1.73	2.04	2.09
Rank	$l_4 > l_3 > l_2 > l_1$			
The optimal landing path	$l_4$			

409 From Simulation i to Simulation iv, the environment condition set for each validation case is  
 410 degrading gradually. With the changes of the environment setups, the path selection strategy is able  
 411 to determine the optimal landing path for each validation case. Note that  $l_4$  always ranks in the last  
 412 place when the environment condition is generally good for the aircraft landing. It demonstrates that  
 413 the pilot won't land the aircraft on the ground unless the situation is too bad. In general, the above  
 414 results indicate that the proposed path selection strategy is able to describe and cope with the  
 415 fuzziness of aircraft performance, environment and traffic situation. The optimal landing path under  
 416 different environments can be obtained. The proposed path selection strategy can provide the pilot  
 417 and the LCO with a useful tool to guide the aircraft landing safely. Besides, the workload of pilot  
 418 and LCO is also reduced.

## 419 5. Conclusion

420 In this paper, the path selection problem for aircraft landing on the carrier is studied, and a new  
 421 path selection strategy is developed to solve the problem. The goal is to improve the safety level of  
 422 aircraft landing and reduce the workload of the pilot and the LCO at the same time. Firstly, the path  
 423 selection problem associated with the aircraft landing problem is described. Secondly, essential  
 424 elements involved in this problem are analyzed. Thirdly, a conceptual model that reflects the essence  
 425 of solving the problem is drawn.

426 Using the fuzzy TOPSIS approach improved in this paper, the environmental information, the  
 427 performance ratings and weights of decision makers are described using linguistic variables. By  
 428 introducing linguistic variables, fuzziness in description and judgment can be solved. Subsequently,  
 429 a mathematical model, which can evaluate the rationality of each alternative landing path for the  
 430 current environment, is built. Finally, to compromise the judgements from different decision  
 431 makers, the group decision-making approach is introduced, and the optimal landing path is  
 432 obtained by taking into account the judgments of both the LCO and the human pilot. Experimental  
 433 results under different environments indicate that the proposed landing path selection strategy has a  
 434 good performance of making a quick and reasonable decision, thus the optimal landing path is  
 435 obtained.

436 The landing selection strategy proposed in this paper can reduce the workload of the pilot and  
 437 the LCO by determining the optimal landing path for the returning aircraft. The work of this paper  
 438 belongs to one of the key technologies of automatic landing of carrier aircraft, and it is the first issue  
 439 to be addressed in the whole process of landing. In the future, the design of automatic control law  
 440 will be studied to track the landing path determined in this paper.

441

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