

Article

Marine Turbine Hydrodynamics by a Boundary Element Method with Viscous Flow Correction

Francesco Salvatore*, Zohreh Sarichloo, and Danilo Calcagni

CNR-INSEAN, National Research Council, Marine Technology Research Institute
Via di Vallerano 139, 00128 Rome, Italy

* Correspondence: francesco.salvatore@cnr.it; Tel.: +39-06-5029-9313

Abstract: A computational methodology for the hydrodynamic analysis of horizontal axis marine current turbines is presented. The approach is based on a boundary integral equation method for inviscid flows originally developed for marine propellers and adapted here to describe the flow features that characterize hydrokinetic turbines. To this purpose, semi-analytical trailing wake and viscous-flow correction models are introduced. A validation study is performed by comparing hydrodynamic performance predictions with two experimental test cases and with results from other numerical models in the literature. The capability of the proposed methodology to correctly describe turbine thrust and power over a wide range of operating conditions is discussed. Viscosity effects associated to blade flow separation and stall are taken into account and predicted thrust and power are comparable with results of blade element methods that are largely used in the design of marine current turbines. The accuracy of numerical predictions tend to reduce in cases where turbine blades operate in off-design conditions.

Keywords: Marine Current Turbine, Hydrodynamics, Boundary Element Methods, Trailing wake Models, Viscous Flow Correction

1. Introduction

Marine or hydrokinetic turbines for the production of renewable energy from tidal and ocean currents is a rapidly growing technology. Large scale installations mainly address horizontal-axis turbines installed on structures fixed to the seabed or supported by floating platforms.

The relatively fast maturation of hydrokinetic turbine technology as compared to other ocean energy harvesting systems is partly due to experience gained over the last decades in the wind energy sector. In most cases the aspect of marine turbine blades resembles wind rotor blades except for the aspect ratio that is quite smaller to resist hydrodynamic loads in water. It is then not surprising that Blade Element Momentum Methods (simply, BEM) originally developed for wind turbines are extensively used for analysis and design of tidal and ocean current turbines, see *e.g.* [1]. BEM provides fast and reliable estimates of turbine performance if suitable tuning is applied to overcome important methodology weaknesses [2], [3]. Specifically, blade loading is derived by prescribed lift and drag properties of two-dimensional profiles and semi-empirical three-dimensional flow corrections are necessary to account for blade tip effects, blade/hub interaction, number of blades.

In contrast to this, the hydrodynamic design of marine propellers is typically based on boundary element or panel methods that, under limiting inviscid-flow assumptions, provide a consistent representation of the three-dimensional flow around rotors in steady or unsteady flow. To avoid confusion with blade element (momentum) methods, the terminology Boundary Integral Equation Method (BIEM) is used here. In spite of that, only few example exist of applications of BIEMs to hydrokinetic turbines, see *e.g.* Young et al. [4], Kinnas et al. [5]. Results in the literature highlight the difficulty of boundary element methods to correctly describe the hydrodynamic performance of turbines designed to extract energy from an onset flow. A major difficulty is that turbine blades frequently operate at high angle of attack and viscosity induced separation and stall significantly affect

38 generated thrust and power. Baltazar & Falcão de Campos [6], [7] address the problem by comparing
39 different models to correct inviscid-flow predictions by BIEM.

40 The problem is tackled in the present work by the development of original viscous flow and
41 trailing wake models that are integrated into a BIEM originally developed for marine propellers, see
42 *e.g.* Salvatore et al. [8],[9], [10]. In the proposed methodology, the trailing wake geometry is determined
43 by a semi-analytical model with wake pitch alignment consistent with turbine-induced velocity
44 perturbation and an experimental-based definition of the expansion rate of the streamtube downstream
45 the rotor plane. Inspired to blade element methods, a viscous-flow correction is determined by
46 comparing distributions of blade loads by the inviscid-flow BIEM and lift and drag properties of
47 representative blade sections under flow separation and stall. Lift and drag data are obtained from
48 available experimental data or from numerical predictions by two-dimensional viscous-flow solvers.

49 The resulting methodology with Viscous-Flow Correction (VFC) is referred to here as BIEM-VFC.
50 A validation study for the proposed computational model is addressed by considering two case studies
51 taken from the literature with experimental results for three-bladed model turbines. Specifically,
52 Gaurier et al. [11] present results from the first round-robin test on tidal turbines carried out in the
53 framework of the EU-FP7 MaRINET Project [12], with turbine performance measurements from
54 two towing tanks (Strathclyde University and CNR-INSEAN) and two flume tanks (IFREMER and
55 CNR-INSEAN). Next, Bahaj et al. [13] present a detailed characterization of marine current turbine
56 performance by considering the effects of blade pitch variations. For this case study, BIEM-VFC is also
57 compared with other numerical models based on BEM and BIEM. Results of the comparative analysis
58 provide a clear overview of the accuracy of the proposed BIEM-VFC methodology and its range of
59 applicability as a marine current turbine analysis and design tool.

60 The paper is organised as follows. The theoretical and computational BIEM-VFC methodology
61 is outlined in Section 2, with details of viscous flow and trailing wake models. The validation study
62 is addressed in Sections 3 to 5, while strenghts and weaknesses of the methodology are discussed in
63 Section 6.

64 2. Theoretical model

65 The computational model proposed here for the hydrodynamic analysis of marine current turbines
66 is based on a Boundary Integral Equation Method (BIEM) that is valid under inviscid flow assumptions.
67 The methodology has been originally developed at CNR-INSEAN to study marine propulsors, see *e.g.*,
68 Salvatore et al. [8], [9], and Pereira et al. [10].

69 The extension of the methodology to analyse marine turbine flows requires the introduction of
70 suitable models to describe trailing vorticity dynamics and to correct blade loads when turbine blades
71 undergo flow separation and stall. In this section, the original BIEM is briefly reviewed and models
72 specifically developed for turbine trailing vorticity and viscosity effects are described in details.

73 Assuming the onset flow is incompressible and inviscid, the perturbation velocity \mathbf{v} induced by the
74 turbine may be described by a scalar potential as $\mathbf{v} = \nabla\phi$, and general mass and momentum equations
75 are dramatically simplified. Mass conservation yields the Laplace equation for the perturbation velocity
76 potential, $\nabla^2\phi = 0$, while the momentum equation reduces to the Bernoulli Equation for pressure p

$$\frac{\partial\phi}{\partial t} + \frac{1}{2}\|\nabla\phi + \mathbf{v}_I\|^2 + \frac{p}{\rho} + gz_0 = \frac{1}{2}\|\mathbf{v}_I\|^2 + \frac{p_0}{\rho}, \quad (1)$$

77 where p_0 is the free-stream reference pressure, and $\mathbf{v}_I = \mathbf{w} + \boldsymbol{\Omega} \times \mathbf{x}$ is the inflow velocity as seen from
78 an observer fixed with blades rotating at angular velocity $\boldsymbol{\Omega}$ while \mathbf{w} is the onset flow velocity. In case
79 of uniform inflow aligned to turbine axis x , one has $\boldsymbol{\Omega} = \Omega\mathbf{e}_x$, $\mathbf{w} = V\mathbf{e}_x$ with \mathbf{e}_x unit vector along x ,
80 see Fig. 1. Finally, gz_0 is the hydrostatic head term referred to a reference vertical position $z = 0$.

81 The Laplace equation for ϕ is solved via a boundary integral formulation where problem
82 unknowns are distributed on the body surface and on its *trailing wake*. By potential flow theory
83 for lifting bodies, the trailing wake denotes a zero-thickness layer where vorticity generated by lifting

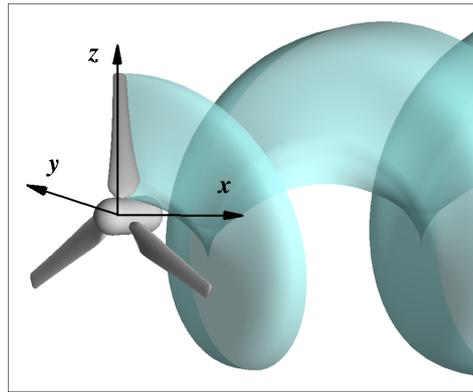


Figure 1. Sketch of the frame of reference associated to the solid boundary describing an isolated turbine and the surface of trailing wake shed by one blade.

84 surfaces is shed into the downstream flow. Through a classical derivation (see, *e.g.*, Morino [14]) the
 85 following boundary integral representation for φ at an arbitrary field point \mathbf{x} is obtained

$$E(\mathbf{x}) \varphi(\mathbf{x}) = \oint_{S_{BUN}} \left(\frac{\partial \varphi}{\partial n} G - \varphi \frac{\partial G}{\partial n} \right) dS(\mathbf{y}) - \int_{S_W} \Delta \varphi \frac{\partial G}{\partial n} dS(\mathbf{y}). \quad (2)$$

86 Dealing with isolated turbines modelling by BIEM, a typical schematization is to represent the device
 87 as an assembly of blades attached to a nacelle of finite length immersed in an unbounded flow, as
 88 sketched in Fig.1. In the above equation, S_{BUN} denotes the solid surface combining blades S_B and
 89 nacelle S_N , while S_W is the trailing wake. Quantity \mathbf{n} is the unit normal to these surfaces, pointing
 90 outward on solid boundaries and from pressure to suction sides at blade trailing edges to define the
 91 orientation on the wake. The symbol Δ in Eq. (2) is used to denote discontinuity of velocity potential
 92 across the trailing wake surface defined according to the convention used for the unit normal to S_W ,
 93 whereas $E(\mathbf{x})$ is a function that makes the same equation to be valid for points \mathbf{x} on the body surface
 94 ($E = 1/2$) or inside the fluid domain, $E = 1$. Moreover, quantities $G, \partial G / \partial n$ are unit source and
 95 dipoles in the unbounded three-dimensional space and depend only from the mutual position between
 96 the collocation point \mathbf{x} and the influencing point \mathbf{y} on the boundary surfaces. A distinguishing feature
 97 of the present formulation is that analytical expressions are used to evaluate the exact contributions of
 98 source and dipole terms on hyperboloidal quadrilateral surface elements, see [14] for details.

99 Boundary conditions for the velocity potential are imposed at infinity (vanishing perturbation
 100 φ), on solid surfaces (impermeability, $\partial \varphi / \partial n = -\mathbf{v}_i \cdot \mathbf{n}$) and on the trailing wake, where convection
 101 of vorticity generated on blades is imposed and a Kutta-Morino condition is used to impose identity
 102 between velocity potential difference at blade trailing edge pressure and suction sides and $\Delta \varphi$ on the
 103 wake.

104 Equation (2) with $E = 1/2$ and related boundary conditions represents a boundary integral
 105 equation whose solution determines φ on the body surface. By discretizing boundaries S_{BUN} and S_W
 106 into surface panels, and enforcing Eq. (2) at centroids of body panels, a linear set of algebraic equations
 107 is obtained. The wake surface S_W can be determined as a part of the solution by a wake-alignment
 108 iterative procedure, as described in [15]. A faster and more robust approach is used in the present
 109 study as described in Sect. 2 below.

110 Once Eq. (2) is numerically solved, the velocity potential and its gradient are known on the body
 111 surface and pressure can be evaluated using the Bernoulli Eq. (1). Hydrodynamic loads generated by
 112 the turbine are then obtained by integrating pressure and tangential stress τ over the blades surface. In

particular, the force contribution by a blade element of radial extension dr and chord c can be written as

$$d\mathbf{f}(r) = d\mathbf{f}_p(r) + d\mathbf{f}_\tau(r) = (-p\mathbf{n} + \tau\mathbf{t}) dS, \quad (3)$$

where $dS = c dr$, \mathbf{t} is the unit vector tangent to the surface and aligned to the local flow and quantities $\mathbf{f}_p, \mathbf{f}_\tau$ denote, respectively, contributions by normal (pressure) and tangential (friction) stress. Integrating elementary forces on all blades, turbine thrust T and torque Q follow

$$T = \int_{S_B} \mathbf{f} \cdot \mathbf{e}_x dS, \quad Q = \int_{S_B} (\mathbf{x} \times \mathbf{f}) \cdot \mathbf{e}_x dS. \quad (4)$$

Surface stress τ is not part of the inviscid-flow solution and could be evaluated by a coupled viscous/inviscid model in which BIEM is combined with a boundary-layer model, as described in Salvatore et al. [8]. A simplified approach popular in marine propeller models consists in estimating quantity τ from formulas valid for attached laminar and turbulent flow over a flat plate, see e.g. [16]

$$\begin{aligned} C_F &= 1.328/\sqrt{Re_r} & (Re_r < 10^5) \\ C_F &= 0.075/(\log_{10}(Re_r) - 2)^2 & (Re_r \geq 10^5) \end{aligned} \quad (5)$$

where $C_F = \tau/\frac{1}{2}\rho V_I^2(r)$ is the friction coefficient, and

$$Re_r = c(r)V_I(r)/\nu = c(r)\sqrt{V^2 + (\Omega r)^2}/\nu, \quad (6)$$

defines the Reynolds number characterizing the flow around the blade section at radius r , where ν is the water kinematic viscosity.

The accuracy of this approximated viscosity correction to hydrodynamic loads by BIEM is typically limited to attached flows on blade sections at low angle of attack. The VFC approach proposed here aims to cope with a wider range of conditions including flow separation and stall, as outlined in Section 2.2.

2.1. Trailing wake model

In the present study, a semi-analytical model is used to determine the wake surface S_w in Eq. (2). The wake is defined as a generalised helicoidal surface with distributions of axial pitch and radial expansion of the streamtube downstream the rotor that are consistent with the operating mode of hydrokinetic turbines.

For the axial pitch, two regions are considered: the *tip-vortex* region and the *blade wake* extending spanwise between vortices released at blade root and tip. In the blade wake, trailing vortices are convected downstream with velocity given as the average of the onset flow speed and of the velocity perturbation induced by the wake itself, \mathbf{v}_w . A boundary integral representation of \mathbf{v}_w is obtained by taking the gradient of the velocity potential equation (2). Here, an approximated representation of this velocity field across the fluid region of interest is obtained by using BIEM to evaluate \mathbf{v}_w at the rotor plane and imposing a linear variation downstream to match a given farfield distribution.

Then, the axial component of the wake-induced velocity, $v_{x,w} = \mathbf{v}_w \cdot \mathbf{e}_x$, may be written as

$$v_{x,w} = (1 - \zeta_x) \frac{\partial \tilde{\varphi}}{\partial x} \Big|_{RP} + \zeta_x v_{x,w} \Big|_{FF}, \quad (7)$$

where ζ_x is a normalised abscissa with $\zeta_x = 0$ at rotor trailing edge and $\zeta_x = 1$ at the downstream end of the discretised wake surface. Consistent with Betz theory [17], the axial induced velocity at farfield $v_{x,w} \Big|_{FF}$ is twice the intensity at the rotor plane. Symbol $(\tilde{\cdot})$ denotes wake-induced velocity potential obtained from the gradient of Eq. (2), while subscript RP refers to the rotor plane axial position.

146 In the tip-vortex region, Okulov & Sørensen [18] describe a trailing vortex shedding model with
 147 axial velocity given as the average between velocity in the blade wake, Eq. (7), and the unperturbed
 148 axial velocity V outside the streamtube. Thus, denoting by $\phi_{w,0}$ the hydrodynamic pitch associated to
 149 the unperturbed flow, one obtains the following expressions for the wake pitch ϕ_w

$$\phi_{w,bla}(x,r) = \left(1 + \frac{v_{x,w}(x,r)}{V}\right) \phi_{w,0}; \quad \phi_{w,tip}(x) = \frac{1}{2} (\phi_{w,bla}(x, \hat{r}) + \phi_{w,0}), \quad (8)$$

$$\phi_w(x,r) = \xi_r \phi_{w,tip}(x) + (1 - \xi_r) \phi_{w,bla}(x,r),$$

150 where pedices *bla* and *tip* denote, respectively, blade wake and tip vortex, and ξ_r is a radial weight
 151 function (in the present analysis, $\xi_r = (r/R)^3$ has been used, where R is the turbine radius). In the
 152 evaluation of $\phi_{w,tip}$, the blade wake pitch $\phi_{w,bla}$ is evaluated at a representative radial station \hat{r} .

153 Next, the radial expansion of the wake streamtube downstream the rotor plane is determined as

$$r = R + r_0 \left(1 - e^{-\xi_x/C_2}\right), \quad (9)$$

154 where constants r_0, C_2 are derived from experimental data describing the wake evolution of
 155 hydrokinetic turbines over a range of operating conditions. In the present study, wake flow
 156 measurements by Micek et al. [19] (here referred to as IFREMER rotor) and by Del Frate et al. [20]
 157 (SABELLA rotor) have been considered, see Fig. 2. The assumption is that at short distance from the
 158 rotor, trailing wake expansion is weakly dependent by the rotor shape and a general trend can be
 159 derived from flow measurements.

160 Combining Eqs. (7) to (9), the generalised helicoidal surface defining the trailing wake S_w is
 161 obtained. In fact, the evaluation of the velocity potential $\tilde{\varphi}$ in Eq. (7) depends on the definition of
 162 surface S_w in Eq. (2) and hence an iterative procedure is required. In the numerical analysis addressed
 163 in the present work, it has been found that the iteration converges after few steps.

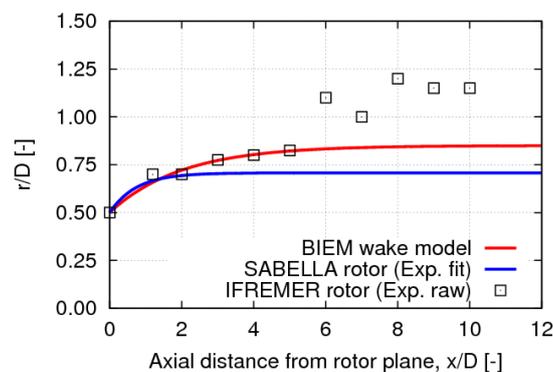


Figure 2. Streamtube radius downstream rotor plane from Eq. (9) and comparative data from experiments.

164 2.2. Viscous-flow correction model

165 Assumptions of inviscid, irrotational flow underlying BIEM yield that turbine hydrodynamics
 166 is studied by fast numerical solutions of a linear problem with unknowns distributed only on the
 167 solid surface of the turbine. Unfortunately, turbine performance is dramatically affected by blade
 168 flow separation and stall and hence neglecting viscosity effects may result into completely unreliable
 169 predictions of turbine hydrodynamic loads and power output.

170 A methodology is proposed here to correct blade loads predicted under inviscid-flow assumptions
 171 by a procedure that preserves the reduced computing effort typical of BIEM. The idea is to (i) identify
 172 conditions where blade flow is subject to boundary layer separation and stall and (ii) estimate the

173 effect of viscosity on blade loads under such conditions. The BIEM model including this viscous-flow
174 correction is hereafter referred to as BIEM-VFC.

175 To this purpose, sectional loads along blade span evaluated by BIEM are compared to lift and drag
176 properties of two-dimensional (2D) profiles describing blade sections. Equivalence between operating
177 conditions of three-dimensional rotating blade sections and corresponding 2D profiles is enforced in
178 terms of local Reynolds number Re_r (see Section above) and of the *effective* angle of attack α_e .

179 Quantity α_e defines the angle of attack where wake-induced velocity contributions are accounted
180 for to evaluate the total velocity incoming to blade sections. A graphical definition of α_e is given
181 in Fig. 3, where inflow velocity components and hydrodynamic force components for a turbine blade
182 section at radius r are sketched. Axial and tangential induced velocity components, respectively Δu_i
183 and Δv_i , represent three-dimensional flow effects induced by trailing vortices shed by blades. These
184 quantities are zero in case of 2D flow around a lifting surface of infinite span and the effective and
nominal angle of attack α coincide.

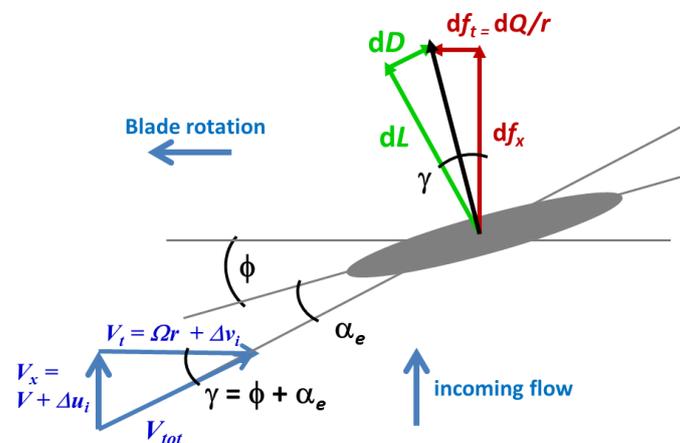


Figure 3. Inflow velocity components and hydrodynamic force components on turbine blade section at radius r .

185 Lift and drag properties representative of blade section shape and operating conditions (α_e, Re_r)
186 are deduced from 2D foil polar curves, as sketched in Fig. 4. Flow separation occurs when the lift
187 curve departs from linear dependence with incidence α (points labelled as SE+, SE-), while stall occurs
188 when lift drops as α increases in absolute value and drag has an abrupt rise (point ST).

189 Inviscid-flow solutions by BIEM determine blade sectional loads that are consistent with linear
190 relationship between lift and angle of attack and, using the flat-plate analogy in Eq. (5) with minimum
191 drag reflecting attached flow conditions (curves in red in Fig. 4). The comparison between sectional lift
192 and drag properties motivates the following definition of factors to correct sectional loads by BIEM to
193 represent both attached and separated flow conditions:
194

$$\mathcal{K}_D(\alpha_e, Re_r) = dD_{2D} / dD_{2D}^{inv} \quad (10)$$

$$\mathcal{K}_L(\alpha_e, Re_r) = dL_{2D} / dL_{2D}^{inv}$$

195 where D_{2D}^{inv} and L_{2D}^{inv} are, respectively, drag and lift per unit length determined under inviscid 2D flow
196 conditions (*i.e.* by a 2D BIEM) at angle of attack α_e , while D_{2D} and L_{2D} are profile drag and lift under
197 2D viscous flow conditions.

198 Once quantities $\mathcal{K}_D, \mathcal{K}_L$ are known, blade loads correction is obtained through the following
199 procedure. From the BIEM solution, sectional contributions to axial force df_x and tangential force df_t

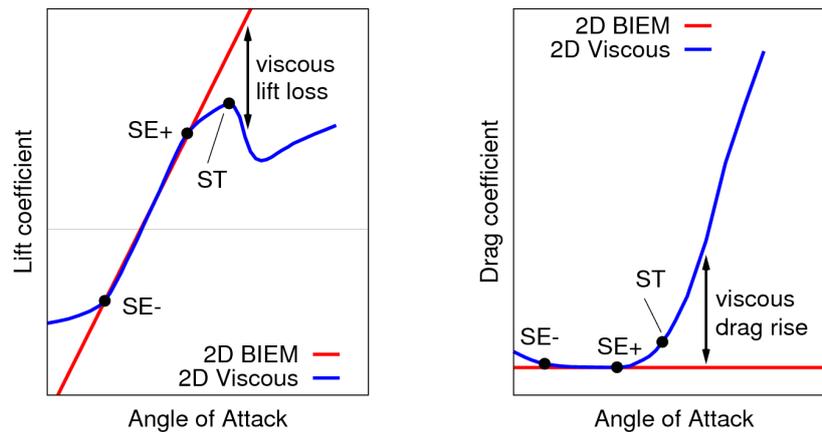


Figure 4. Lift and drag curves of two-dimensional profile: viscous-flow compared with corresponding quasi-inviscid flow.

200 are determined from Eq. (3). Next, wake-induced velocity along blade span is determined by taking
 201 the gradient of Eq. (2) (with $E = 1$), and the radial distribution of the effective angle of attack $\alpha_e(r)$ is
 202 evaluated. Radial distributions of sectional drag and lift dD, dL follow by projecting force in direction
 203 normal and tangent to the effective inflow, as sketched in Fig. 3, where ϕ is the angular pitch of blade
 204 section at radius r .

205 Separating pressure-induced and friction-induced contributions to force df as defined in Eq. (3),
 206 lift and drag contributions are also splitted into pressure-induced and friction-induced terms.
 207 Correction factors from Eq. (10), yield

$$\begin{aligned} d\hat{L}_p &= \mathcal{K}_L dL_p, & d\hat{D}_p &= \mathcal{K}_L^2 dD_p \\ d\hat{L}_\tau &= \mathcal{K}_D dL_\tau, & d\hat{D}_\tau &= \mathcal{K}_D dD_\tau \end{aligned} \quad (11)$$

208 where symbol ($\hat{\cdot}$) labels viscous-flow corrected quantities. While corrections for pressure-induced
 209 lift L_p and friction-induced drag D_τ are obvious, the assumption made here is that correction factor
 210 for drag \mathcal{K}_D can be used to account for flow separation and stall effects on friction-induced lift L_τ .
 211 Pressure-induced drag D_p correction by \mathcal{K}_L^2 stems from the approximated relationship between induced
 212 drag and lift that is broadly valid for lifting surfaces. Numerical studies prove that contributions from
 213 *diagonal* terms L_τ and D_p are very small as compared to, respectively, contributions D_τ, L_p .

214 Converting lift and drag back to respectively axial and tangential load components yields
 215 quantity $d\hat{f}_x$ that integrated along blade span returns corrected blade axial force, while quantity
 216 $d\hat{Q} = d\hat{f}_t r$ returns corrected blade torque. Summing on all blades, turbine corrected thrust \hat{T} and
 217 torque \hat{Q} are obtained (formally, Eq. (4) with \mathbf{f} replaced by $\hat{\mathbf{f}}$).

218 A full exploitation of the viscosity correction model described above implies that an iterative
 219 procedure is enforced to make the potential flow solution consistent with the modified loading on
 220 blades. No iteration has been considered in the present analysis and the subject is briefly address later
 221 in Section 6.

222 3. Case studies for validation of computational model

223 Numerical applications of the proposed computational model are discussed by considering two
 224 case studies taken from the literature. Both cases address three-bladed model turbines designed for
 225 research activity.

226 For a turbine having radius R , swept area $A = \pi R^2$, rotating at angular speed $\Omega = 2\pi n$ in a
 227 current with nominal freestream velocity V , the Tip Speed Ratio (TSR or λ) is defined as

$$\lambda = \Omega R / V.$$

228 Turbine performance is described through thrust, torque and power coefficients, respectively C_T, C_Q, C_P ,
 229 defined as

$$C_T = \frac{T}{\frac{1}{2}\rho AV^2}, \quad C_Q = \frac{Q}{\frac{1}{2}\rho AV^2 R}, \quad C_P = \frac{\Omega Q}{\frac{1}{2}\rho AV^3} = C_Q \cdot \text{TSR}$$

230 and $P = \Omega Q$ is the power generated by the turbine.

231 3.1. Fixed pitch turbine

232 Gaurier et al. [11] describe a 700 mm diameter, fixed-pitch model turbine developed at IFREMER,
 233 France. The model has been the subject of the first round-robin test on tidal turbines carried out in
 234 the framework of the EU-FP7 MaRINET Project [12], with turbine performance measurements from
 235 two towing tanks (Strathclyde University and CNR-INSEAN) and two flume tanks (IFREMER and
 236 CNR-INSEAN). Turbine performance curves measured at inflow speed between 0.6 and 1.2 m/s. are
 237 presented as mean values and standard deviations.

238 Main turbine geometry parameters are summarized in Table 1. A full description is given in [11].
 This testcase is referred to here as the IFREMER-FP turbine.

Table 1. IFREMER-FP turbine main geometry parameters.

Rotor diameter, D	700 [mm]
Blades number, Z	3
Pitch angle at 70% span, Φ	7.3 [deg]
Thickness ratio, 75% span, t/c	0.21
Hub/rotor diameter ratio	0.131
Blade section profile	NACA 63-4xx

239

240 3.2. Variable pitch turbine

241 Bahaj et al. [13] consider a 800 mm diameter, variable-pitch model turbine developed at the
 242 University of Southampton (U.K.). This model was analysed by extensive towing tank and cavitation
 243 tunnel tests. Experimental data provide turbine performance at different blade pitch settings, with
 244 blades rotated about the spanwise axis over a range of 15 degrees, from $\Phi = 15^\circ$ to 30° , while $\Phi = 20^\circ$
 245 is taken as the design condition. This pitch definition refers to the nose-tail angle of the blade at
 246 radius $r/R = 0.2$. Turbine performance curves are available for inflow speed between 0.8 and 2.0 m/s
 247 (cavitation tunnel tests) and between 0.8 and 1.5 m/s (towing tank tests).

248 Main turbine geometry parameters are summarized in Table 2, while a complete description can
 be found in [13]. This testcase is referred to here as the UoS-VP turbine.

Table 2. UoS-VP turbine geometry parameters.

Rotor diameter, D	800 [mm]
Blades number, Z	3
Pitch angle at 20% span, Φ	15, 20, 25, 27, 30 [deg]
Thickn. ratio, 75% span, t/c	0.151
Hub/rotor diameter ratio	0.125
Blade section profile	NACA 63-8xx

249

250 4. Fixed pitch turbine study

251 The analysis of the IFREMER-FP turbine performance is performed by considering experimental
 252 conditions corresponding to the highest inflow speed, $V = 1.2$ m/s. This choice is motivated to avoid
 253 a too small Reynolds number characterizing the blade flow. The Tip Speed Ratio λ is varied between
 254 zero and 8. Comparing with the physical model in [11], it may be noted that the stanchion supporting
 255 the turbine is not described in numerical simulations. Similarly, the nacelle portion downstream the
 turbine hub is not present in the computational model.

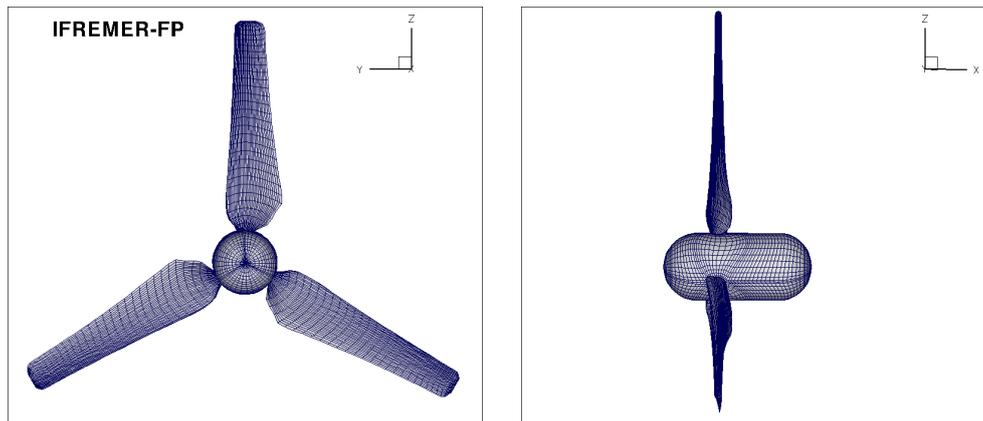


Figure 5. IFREMER-FP turbine. Computational grid used for calculations by BIEM.

256 Blade and hub surface discretization parameters are determined as the result of a grid sensitivity
 257 study. Each blade is discretized into M_B elements chordwise from leading edge to trailing edge
 258 and N_B elements spanwise. Four blade grid levels with $M_B = 24, 36, 48, 60$ and $N_B = 20, 30, 40, 50$
 259 are considered. Hub and wake surface discretizations are built according to blade grid refinement
 260 level. Figure 6 presents inviscid-flow thrust and torque predicted by BIEM using the four grids. Three
 261 representative TSR values are considered. The torque coefficient evaluated by including the viscous-flow
 262 correction is also presented to highlight that the VFC model has no effect on the sensitivity of results
 263 to grid refinement. From these results it is concluded that a discretization with $M_B = 36, N_B = 30$ is
 264 adequate to minimise the effect of further grid refinement on results. In this case, the hub surface is
 265 divided into 42 and 54 elements, respectively, in circumferential and longitudinal directions, and the
 266 wake is discretized into 36 elements along radius and 60 elements streamwise per revolution. The
 267 wake portion considered in the numerical solution of Eq. (2) extends for 10 revolutions.

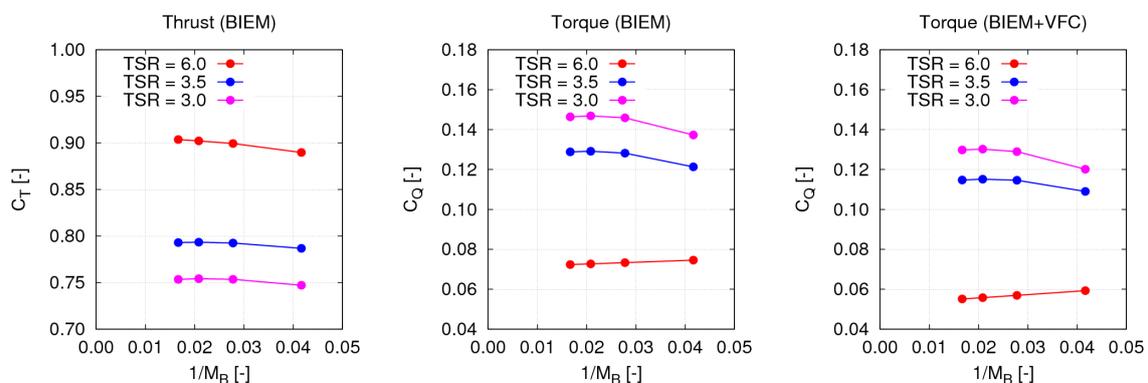


Figure 6. IFREMER-FP turbine. Grid sensitivity study.

269 The trailing wake model described in Section 2 is used to determine the turbine wake
 270 surface. Figure 7 maps the intensity of wake-induced velocity evaluated by BIEM at axial locations
 271 corresponding to rotor blade trailing edge and at different radial positions over a range of operating
 conditions identified by the parameter TSR . The resulting surfaces for three representative values of

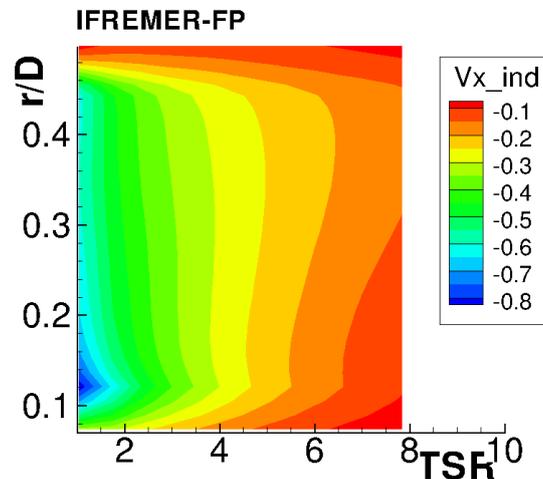


Figure 7. IFREMER-FP turbine. Calculated axial induced velocity distribution at rotor plane.

272 TSR are shown in Fig. 8. The effect of TSR on wake axial pitch is clear: trailing vortices are rapidly
 273 shed away from the rotor at low TSR , while wake spirals pack-up close to the rotor as TSR increases.
 274 In all cases, wake pitch increases from inner radii to the tip vortex.

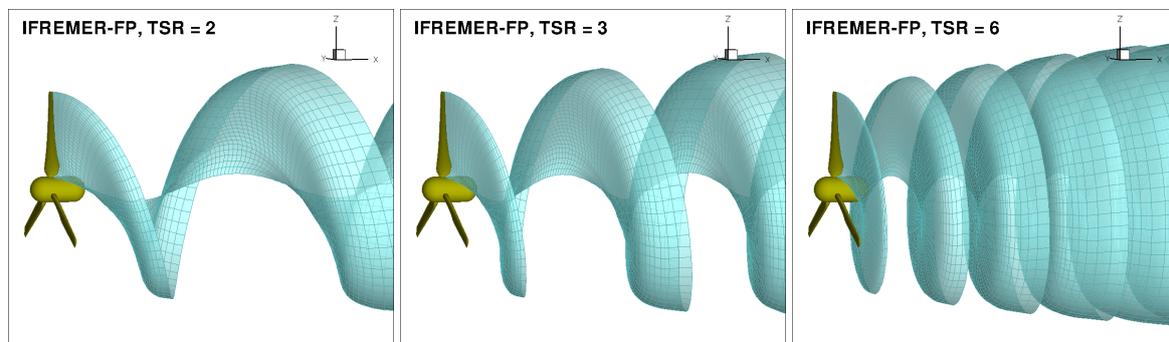


Figure 8. IFREMER-FP turbine. Trailing wake geometry of BIEM model at different operating conditions. From left to right, $TSR = 2, 3, 6$.

275 Viscous flow effects on blade loads are determined by applying the VFC model described in
 276 Section 2.2. The evaluation of correction factors in Eqs. (11) requires that blade section lift and drag
 277 properties are known. To this purpose, the inviscid-flow BIEM solution is used to estimate the local
 278 Reynolds number Re_r from Eq. (6), and the effective angle of attack α_e in Fig. 3, at all blade sections
 279 for the TSR range from zero to 8 considered in model tests. Results in left Fig. 9 show that the local
 280 Reynolds number varies between $1 \cdot 10^5$ and $3.5 \cdot 10^5$ over most of the TSR range of interest. Right
 281 Fig. 9 depicts a positive effective angle of attack α_e that increases from values close to zero at the
 282 highest TSR to 20-25 degrees for TSR between 1 and 2. At given TSR , both Reynolds and angle of
 283 attack present limited variations over a wide blade portion between 30% and 90% of span.
 284

285 Experimental data of lift and drag curves of NACA 63-4xx profiles are available in the literature
 286 only at Reynolds number of 10^6 and higher, which is outside the range of interest in the present analysis
 287 as shown above. Lack of experimental data is overcome here by using numerical predictions of polar

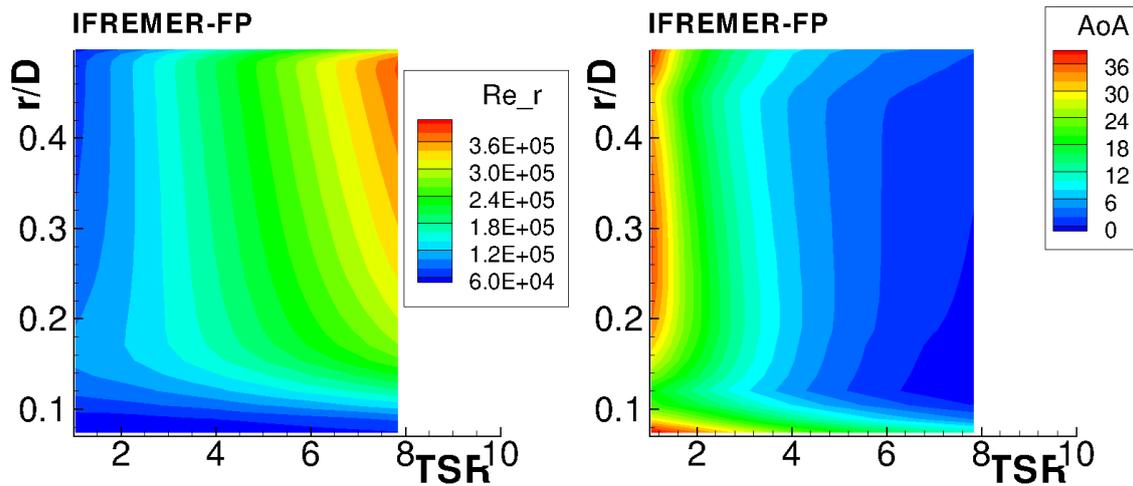


Figure 9. IFREMER-FP turbine. Reynolds number Re_r (left) and effective angle of attack α_e (right) as a function of radius r and of TSR.

288 curves by the X-Foil code [21]. This solver integrates a BIEM for two-dimensional, steady flow with the
 289 solution of boundary layer equations in integral form and is largely used in combination with blade
 290 element (momentum) methods. The NACA 63-421 profile corresponding to 21% thick blade sections
 291 at 70% of span is taken as representative of all blade sections. At angle of attack beyond stall, X-Foil
 292 predictions are not reliable and polar curves are completed by the following extrapolation procedure.
 293 At very high incidence angles (here, $\alpha \geq 30^\circ$), lift and drag values are taken from experimental data
 294 for the NACA 0015 profile by Sheldahl & Klimas [22]. The assumption is that for very high angles,
 295 hydrodynamic loads are not sensitive to profile shape details. A polynomial fit is used to merge NACA
 296 63-421 data from X-Foil and high angle of attack NACA 0015 data at angle of attack between stall and
 297 30 degrees. This procedure to complete lift and drag information over the full angle of attack range of
 298 interest is alternative to the approach in [23] largely used in the literature.

299 Lift and drag curves calculated by X-Foil are presented in Fig. 10. In particular, results for 5 values
 300 of Reynolds number are considered in order to adequately describe lift and drag properties over the
 301 Re_r range of interest (left Fig. 9). Lift and drag curves from experimental data at $Re = 3E6$ in [24] are
 also given for comparison.

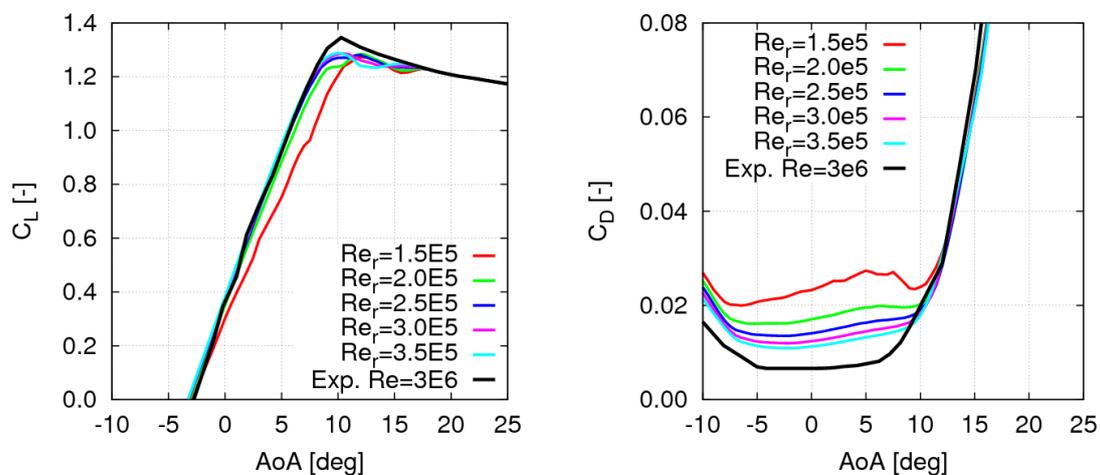


Figure 10. NACA 63-421 2D foil: lift (left) and drag (right) coefficients calculated by X-Foil and from experiments [24].

302 Figure 11 maps correction factors $\mathcal{K}_D, \mathcal{K}_L$ along blade span and over the TSR range of interest.
 303 Values close to one denote conditions where blade flow is attached or weakly separated and no
 304 correction of sectional loads by BIEM is needed. This occurs at $TSR \simeq 2.5$ and higher, which corresponds
 305 to effective angle of attack below 10-12 degrees, as shown in Fig. 9. At lower TSR , the effective angle
 306 of attack increases up to stall, as apparent from polar curves in Fig. 10. As expected, the lift factor \mathcal{K}_L
 307 drops below 1, while the drag factor \mathcal{K}_D rapidly grows, to simulate, respectively, stall-induced lift loss
 and drag rise.

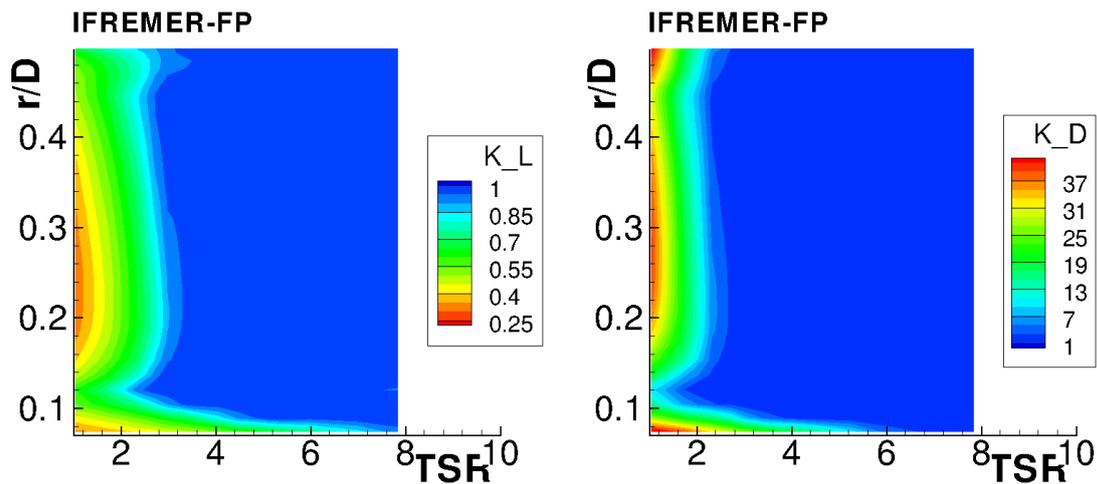


Figure 11. IFREMER-FP turbine. Correction factors for radial contributions to lift (left) and drag (right) as a function of radius r and of TSR .

308 Predicted turbine thrust, torque and power curves are presented in Fig. 12 and compared with
 309 experimental data at $V = 1.2$ m/s from three facilities involved in the round-robin test: CNR-INSEAN
 310 towing tank (INSEAN), IFREMER flume tank (IFREMER) and Kelvin Hydrodynamics Laboratory at
 311 University of Strathclyde (KHL). Results from the fourth facility participating to the round robin test,
 312 CNR-INSEAN flume tank, are omitted here since they fall within the range given by those considered
 313 in plots. For the sake of precision, measured thrust and power coefficients only are presented in [11].
 314 Here, also the torque coefficient is considered because this quantity provides a direct indication of the
 315 accuracy of blade tangential forces evaluated by the numerical model.
 316

317 It is important to observe that present experimental and numerical results use different definitions
 318 of thrust and torque. Numerical thrust and torque are determined by integrating hydrodynamic
 319 loads on blade surfaces, while in the experimental set-up, turbine torque denotes the axial moment
 320 measured by a torque sensor placed between the rotating hub and the fixed nacelle. Assuming the
 321 contribution to torque of the rotating hub is negligible, numerical and experimental data are consistent.
 322 Both numerical and experimental power are evaluated from the hydrodynamic torque Q as $P = 2\pi nQ$.

323 Less direct is the comparison between numerical and measured thrust. Turbine thrust reported
 324 in [11] denotes the axial force at the top of the mast supporting the turbine. This quantity combines
 325 blades thrust with a non negligible resistance contribution D_{HDM} from hub, nacelle and the mast
 326 piercing the free surface. Tests performed at IFREMER of a dummy IFREMER-FP rotor with no blades
 327 determined $D_{HDM} = 16.89N$ at $V = 0.8$ m/s (not reported in [11]). For the sake of completeness, top
 328 left Fig. 12 also presents measured axial force with the D_{HDM} contribution subtracted. This result is
 329 referred to as 'Exp IFREMER Corr.'

330 Numerical results in Fig. 12 include both BIEM without viscosity correction and corrected values
 331 by Eqs. (11) (label BIEM-VFC). As expected from the discussion above, viscosity effects are negligible
 332 at $TSR = 5$ and higher, while small differences between standard BIEM (that is, with non viscous-flow

333 corrections) and BIEM-VFC predictions are noted for $3 < TSR < 5$. In this range, numerical and
 334 experimental results for torque and power are in good agreement, while thrust is underestimated in
 335 numerical results. The reason for this difference in thrust is not clear and could be related to hub,
 336 nacelle and mast resistance contributions that are only approximately subtracted from axial force
 337 measurements.

338 At TSR lower than 3, massive flow separation and stall determine a dramatic reduction of thrust,
 339 torque and power that is missed in standard BIEM results, while BIEM-VFC results capture the correct
 340 trend. In particular, measured peak values of C_Q and C_p are matched at the correct TSR values. At very
 341 low TSR , where deep stall conditions occur on blades, the BIEM-VFC model overpredicts both torque
 342 and power, but the viscous-flow correction allows to recover most of the error affecting inviscid-flow
 predictions by non-corrected BIEM.

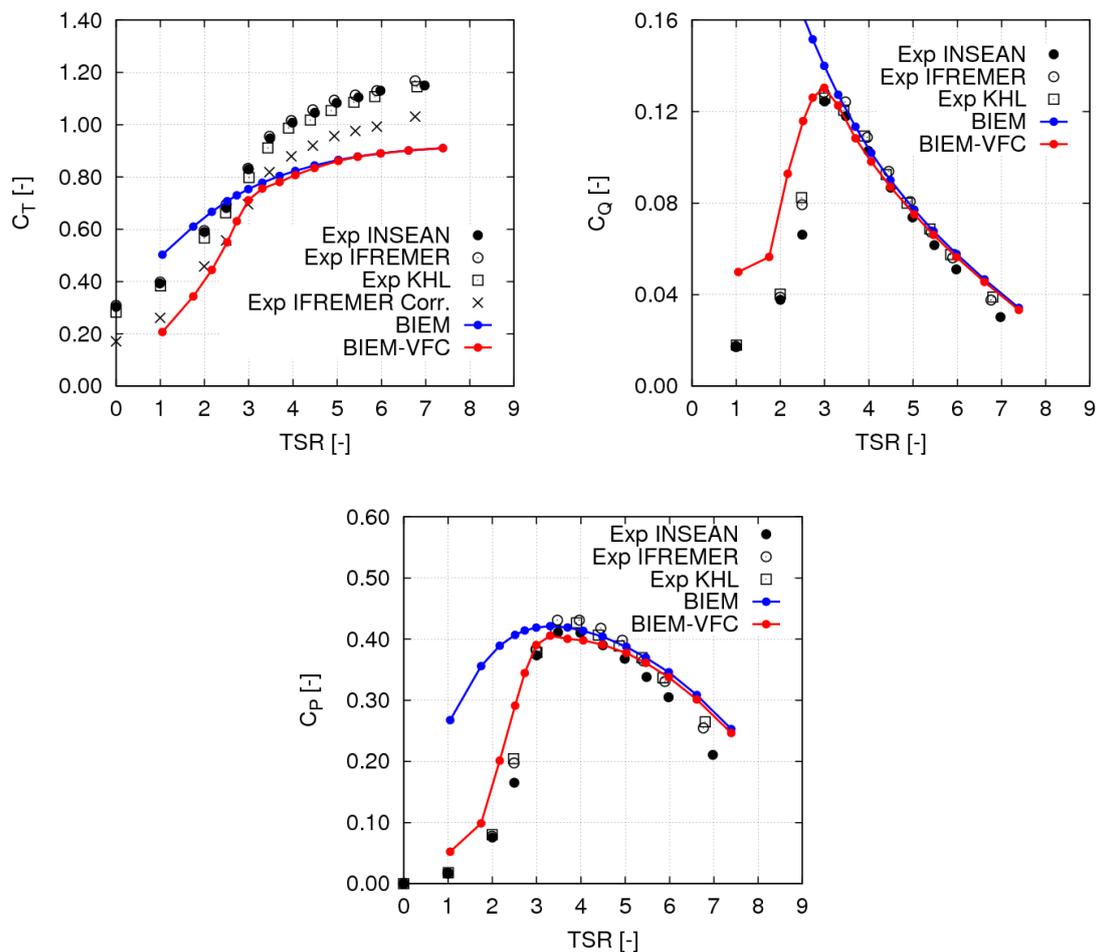


Figure 12. IFREMER-FP turbine performance predictions by BIEM and BIEM-VFC compared to experimental data in [11]: thrust (top left), torque (top right) and power (bottom) coefficients.

343

344 Figures 13 and 14 address blade pressure distributions evaluated by BIEM. Specifically, the
 345 pressure coefficient is defined as

$$C_p = \frac{p - p_0}{\frac{1}{2}\rho V_i^2}, \quad (12)$$

346 where the pressure p is evaluated by BIEM and $V_i(r) = [V^2 + (\Omega r)^2]^{1/2}$ is the velocity of the flow
 347 incoming to the blade section at radius r . Recalling that the VFC model applies only to global loads and
 348 not to the pressure distribution, calculated C_p is representative only in the TSR range where viscosity

349 correction is not significant. For the present case, this approximately holds for $TSR > 3$. Figure 13
 350 depicts pressure distributions on blades pressure and suction sides at $TSR = 3.3$ (peak power condition,
 351 see Fig. 12). The effect of TSR on blade pressure distribution is illustrated in Fig. 14, where C_p along the
 352 blade section at $r/R = 0.7$ for three values of TSR is plotted. As expected, the pressure jump between
 pressure and suction sides tends to reduce as TSR is increased from the peak power condition.

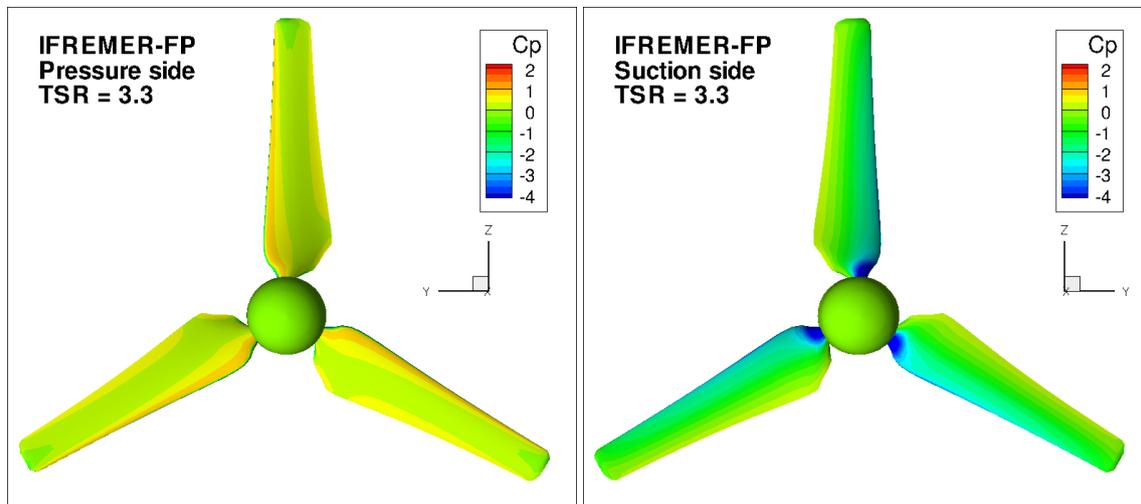


Figure 13. IFREMER-FP turbine. Pressure distribution evaluated by inviscid-flow BIEM, $TSR = 3.3$ (peak power condition).

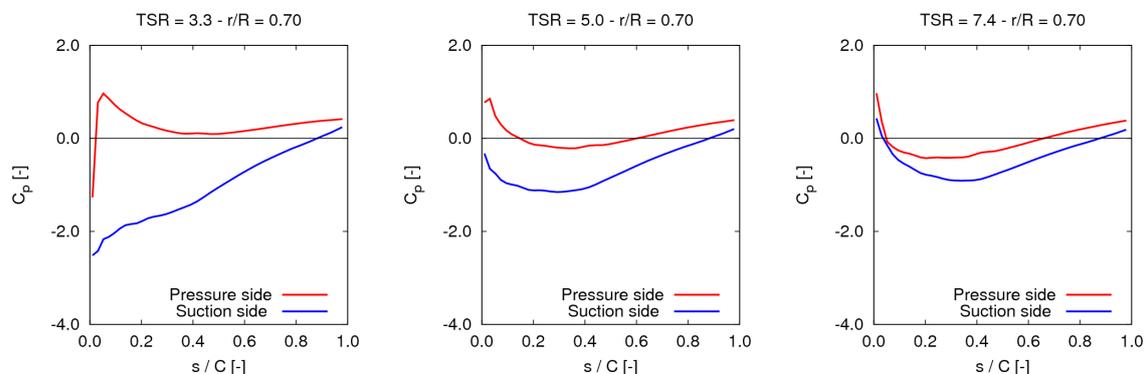


Figure 14. IFREMER-FP turbine. Pressure distribution evaluated by inviscid-flow BIEM at radial section at 70% of blade span. From left to right: $TSR = 3.3, 5, 7.4$.

353

354 5. Variable pitch turbine study

355 The variable-pitch UoS-VP turbine described in Bahaj et al. [13] represents a valuable benchmark
 356 to investigate the capability of a computational model to capture the effect of blade pitch variations
 357 on turbine loads and in particular to correctly describe performance in off-design conditions. As
 358 for the fixed-pitch IFREMER-FP turbine discussed above, a simplified three-dimensional model is
 359 used in which the aft portion of the nacelle and the supporting stanchion are omitted. Another
 360 difference exists at blade root where NACA 63-8xx sections are used in the computational model,
 361 while the physical model presents cylindrical sections to make possible pitch variations. Figure 15
 362 shows the computational grid built for BIEM calculations. Discretization parameters are similar to the
 363 IFREMER-FP case.

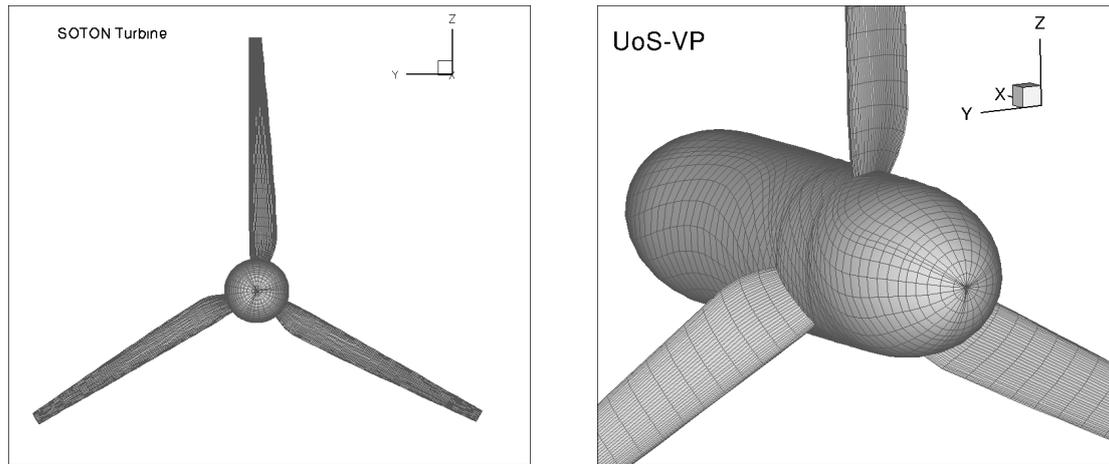


Figure 15. UoS-VP turbine. Three-dimensional model and details of the computational grid for BIEM analysis.

364 Figure 16 depicts the intensity of wake-induced velocity $v_{x,w}$ from Eq. (7) evaluated by BIEM at
 365 axial locations corresponding to rotor blade trailing edge and 70% of blade span. Different blade pitch
 366 settings and a range of operating conditions corresponding to model tests are plotted. The resulting
 367 trailing wake surfaces for the design condition $\Phi = 20^\circ$ and for three representative values of TSR are
 shown in Fig. 17.

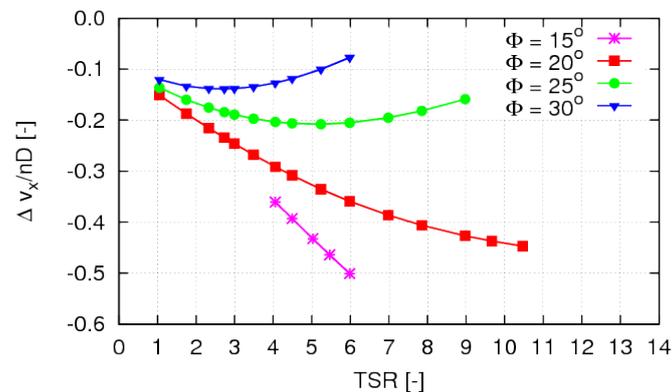


Figure 16. UoS-VP turbine. Axial induced velocity distribution at rotor plane and 70% of blade span. Different pitch settings Φ compared.

368

369 Turbine operating conditions considered in the present analysis refer to selected cavitation tunnel
 370 test conditions from [13] as summarized in Table 3.

371 Recalling Eq. (6), Reynolds number Re_r characterizing blade section flow at radius r depends on
 372 the inflow velocity V . Figure 18 maps its distribution as a function of radius and TSR for pitch setting
 373 $\Phi = 20^\circ$, while Fig. 19 compares Re_r at 70% of blade chord for the highest and lowest inflow speed
 374 cases from Table 3. Results indicate that Re_r approximately varies between $1 \cdot 10^5$ and $3.5 \cdot 10^5$ over
 most of the operating range of interest here.

Table 3. UoS-VP turbine. Inflow speed conditions.

Blade pitch setting, Φ [deg]	15	20	25	27	30
Inflow speed, V [m/s]	1.40	1.73	1.54	1.30	1.54

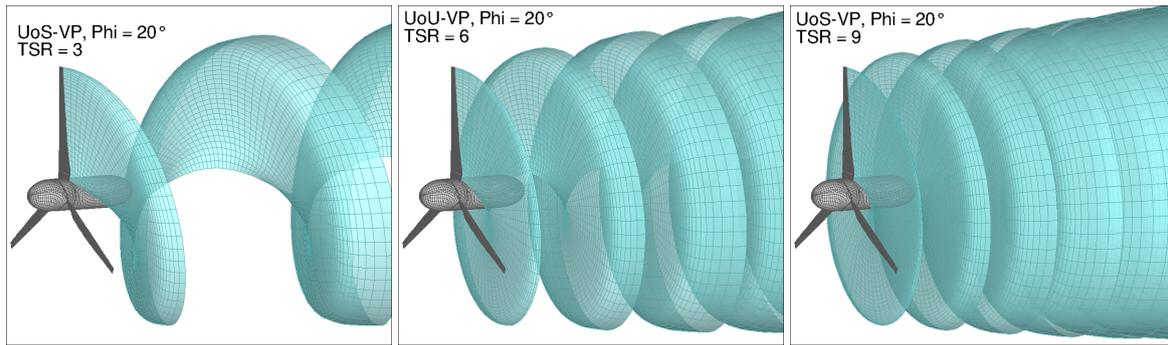


Figure 17. UoS-VP turbine. Wake geometry of BIEM model at different operating conditions. From left to right, $TSR = 3, 6, 9$. Design pitch setting, $\Phi = 20^\circ$.

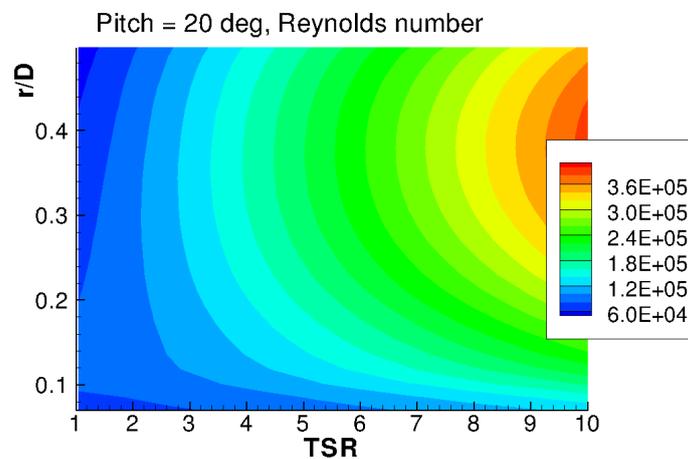


Figure 18. UoS-VP turbine. Reynolds number Re_r as a function of radius r and of turbine operating condition (TSR).

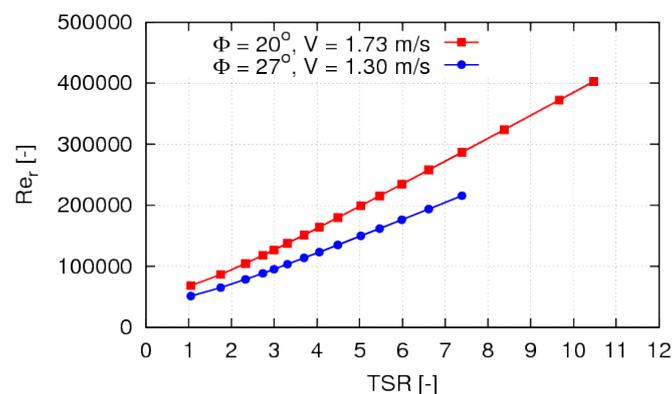


Figure 19. UoS-VP turbine. Reynolds number Re_r at radius $r/R = 0.7$ for pitch settings corresponding to the highest inflow speed ($V = 1.73$ m/s, $\Phi = 20^\circ$), and for the lowest inflow speed ($V = 1.3$ m/s, $\Phi = 27^\circ$).

375 The effective angle of attack α_e evaluated by standard BIEM is presented in Fig. 20. Specifically, α_e
 376 distributions along blade span at variable TSR are presented for design pitch setting, $\Phi = 20^\circ$, and

377 Fig. 21 presents the variability of this quantity at different pitch settings at 70% of blade span. Case
 378 $\Phi = 20^\circ$ shows blade sections mostly operating in the range $-5^\circ < \alpha_e < 25^\circ$ with higher values only
 at $TSR < 2$. As expected, larger pitch angles determine lower α_e values.

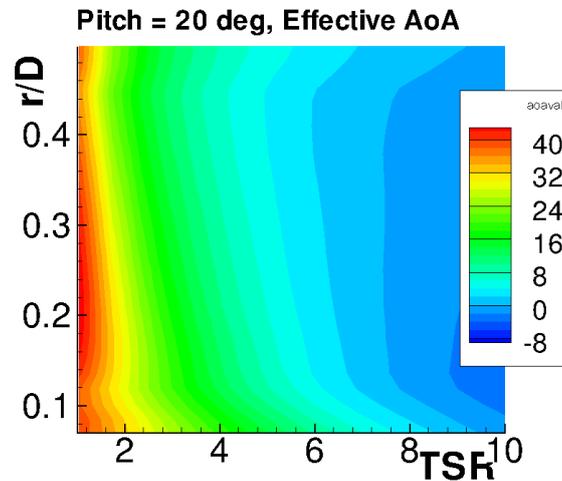


Figure 20. UoS-VP turbine. Effective angle of attack α_e as a function of radius r and of turbine operating condition (TSR). Design pitch setting $\Phi = 20^\circ$.

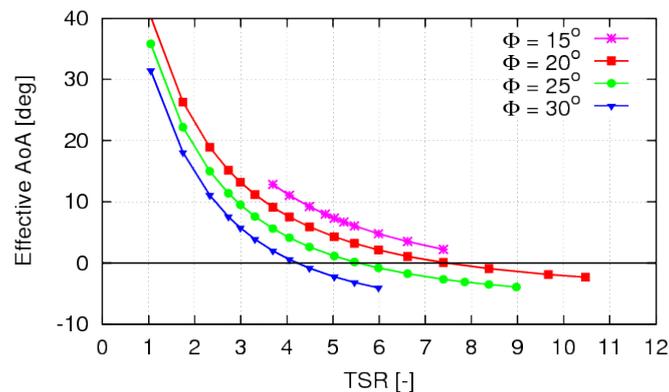


Figure 21. UoS-VP turbine. Effective angle of attack α_e at radius $r/R = 0.7$ for different pitch settings and TSR .

379 Reference [25] provides lift and drag curves of the NACA 63-815 foil at $Re = 8 \cdot 10^5$. This 15%
 380 thick foil is taken as representative of UoS-VP turbine sections whose thickness ratio varies from 0.176
 381 at 50% of span to 0.126 at tip. Recalling Fig. 19, $Re = 8 \cdot 10^5$ is quite higher than the range of interest in
 382 the present analysis. In order to obtain lift and drag data in the actual Re_r and α_e ranges, the X-Foil
 383 code is used and 6 polar curves for $1.5 < Re_r < 4.0 \cdot 10^5$ are evaluated. Polar data are completed at
 384 very high angle of attack using NACA 0015 profile data and polynomial interpolation as described
 385 in Section 3.2 for the IFREMER-FP turbine. Resulting lift and drag curves are plotted in Fig. 22 and
 386 experimental data from [25] are also shown for comparison. Lift curves show that stall conditions are
 387 predicted by X-Foil at about 10-12 degrees, while experimental data show a more gradual transition
 388 to stall between 8 and 12 degrees. Results for drag are in agreement only at negative angle of attack,
 389 while experimental data present quite larger C_D values than X-Foil between 2 and 12 degrees. These
 390 differences cannot be explained because of the different Re numbers in the two datasets. Furthermore,
 391 drag measurements also denote a large scattering.
 392

393 Lift and drag properties predicted by X-Foil are used to feed the viscous-flow correction model
 394 described in Section 2. Contour maps in Fig. 23 show \mathcal{K}_L and \mathcal{K}_D factors for design pitch setting
 395 $\Phi = 20^\circ$, while Fig. 24 depicts the variation of these quantities at $r/R = 0.7$ over the pitch settings
 396 range. In case $\Phi = 20^\circ$, viscosity effects on blade section lift and drag are negligible at TSR of about
 397 3.5-4 and higher, which corresponds to non-separated flow conditions at angle of attack below 8-10
 398 degrees, see Fig. 20 and Fig. 22. At lower TSR , the lift correction factor \mathcal{K}_L gradually decreases to
 399 about 0.3 (lift loss under stall) while the drag correction factor \mathcal{K}_D suddenly increases to values of 30
 400 and more (drag crisis).

401 Consistent with sectional angle of attack values commented above, pitch settings $\Phi > 20^\circ$ limit
 402 flow separation and stall effects to very low values of TSR , while in case $\Phi = 15^\circ$, most of the
 addressed operating range is under the effect of flow separation and stall.

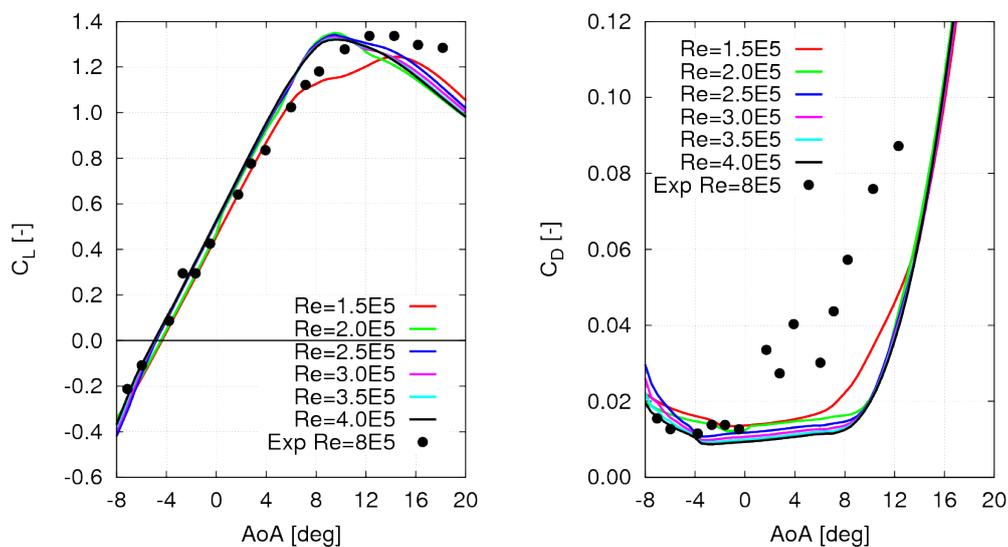


Figure 22. NACA 63-815 2D foil: lift (left) and drag (right) coefficients used for the viscous-flow correction of BIEM.

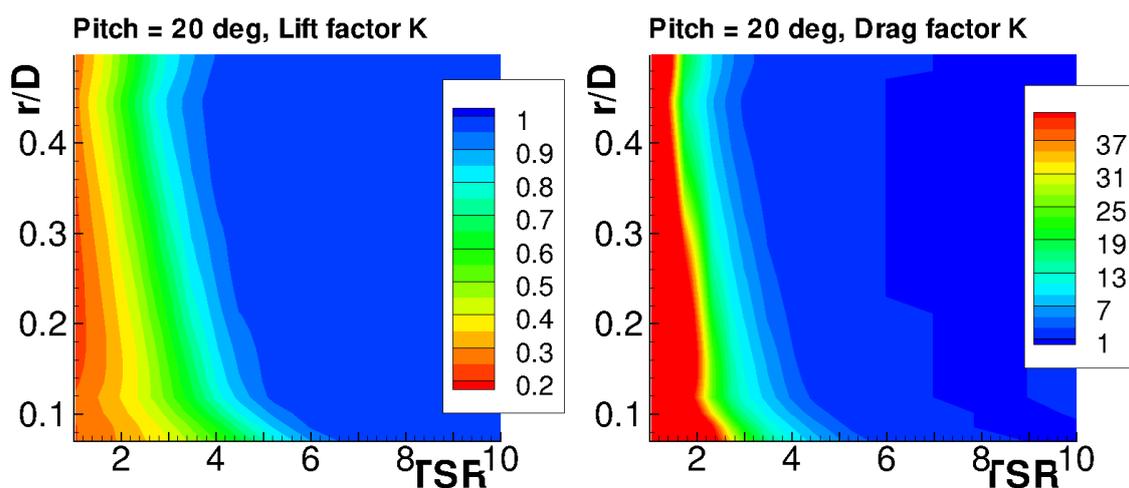


Figure 23. UoS-VP turbine. Correction factors for radial contributions to lift (left) and drag (right) as a function of radius r and of operating condition (TSR). Pitch setting $\Phi = 20^\circ$.

403

404 Turbine thrust and power predictions by BIEM and by BIEM-VFC using blade section polar data
 405 from X-Foil are compared with model test measurements from [13] in Figs. 25 and 26. In general, it

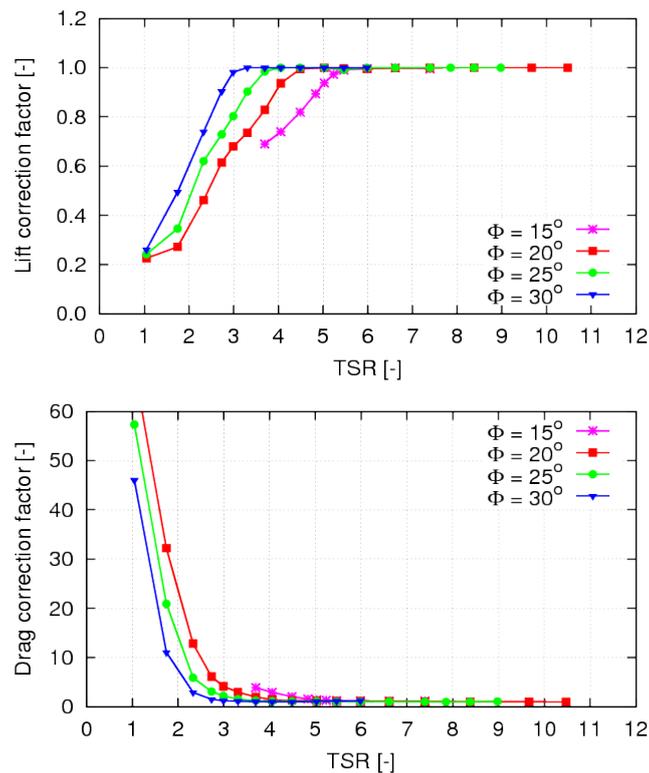


Figure 24. UoS-VP turbine. Lift correction factor \mathcal{K}_L (top) and drag correction factor \mathcal{K}_D (bottom) at radius $r/R = 0.7$ for different Pitch settings.

406 may be noted that standard BIEM predictions of both thrust and power fairly reproduce experimental
 407 data only in the high TSR range for pitch setting cases $20^\circ < \Phi < 27^\circ$. For operating conditions
 408 corresponding to peak power TSR and lower values of TSR , standard BIEM results overpredict both
 409 thrust and power, since the effects of blade flow separation and stall are not captured. When the VFC
 410 model is applied to correct BIEM, predicted thrust and power are in fair agreement with measured
 411 data over a full TSR range. For extreme off-design cases $\Phi = 15^\circ$ and $\Phi = 30^\circ$, large differences
 412 between numerical and experimental results are observed even if the viscous-flow correction is applied.
 413 In particular, at $\Phi = 15^\circ$ predicted C_T presents an unphysical trend with increasing TSR . A possible
 414 explanation of this result is that under extreme off-design conditions, blade flow is affected by a
 415 complex separated flow phenomenology that is beyond the limits of the proposed VFC model, and a
 416 detailed CFD analysis would be necessary. Unfortunately, experimental data do not give information
 417 at very low TSR where deep-stall conditions are expected. Large scattering of measured thrust and
 418 power is also noted in extreme off-design conditions.

419 The capability of the BIEM-VFC model to correctly describe turbine performance trends at
 420 different pitch settings can be discussed considering results in Fig. 27, where four performance
 421 indicators are considered: maximum value of thrust coefficient $C_{T_{max}}$, maximum value of power
 422 coefficient $C_{P_{max}}$, and corresponding values of TSR where maxima are established. Numerical
 423 predictions by BIEM-VFC and polar data from X-Foil (label: VFC, XFOIL Polar) are compared with
 424 polynomial fits of experimental data from cavitation tunnel tests as presented in Fig. 7 of [13] (label:
 425 Model tests). Numerical results by BIEM-VFC using experimental data for blade section lift and drag
 426 taken from measurements in [25] are also presented (label: VFC, Exp. Polar).

427 Quantity $C_{T_{max}}$ by BIEM-VFC and X-Foil and the corresponding TSR values fairly reproduce the
 428 trend observed in experiments over the range $20^\circ < \Phi < 30^\circ$. Same comments can be made for the
 429 maximum power except for case $\Phi = 30^\circ$, where predicted $C_{P_{max}}$ is some 20% lower than measured.

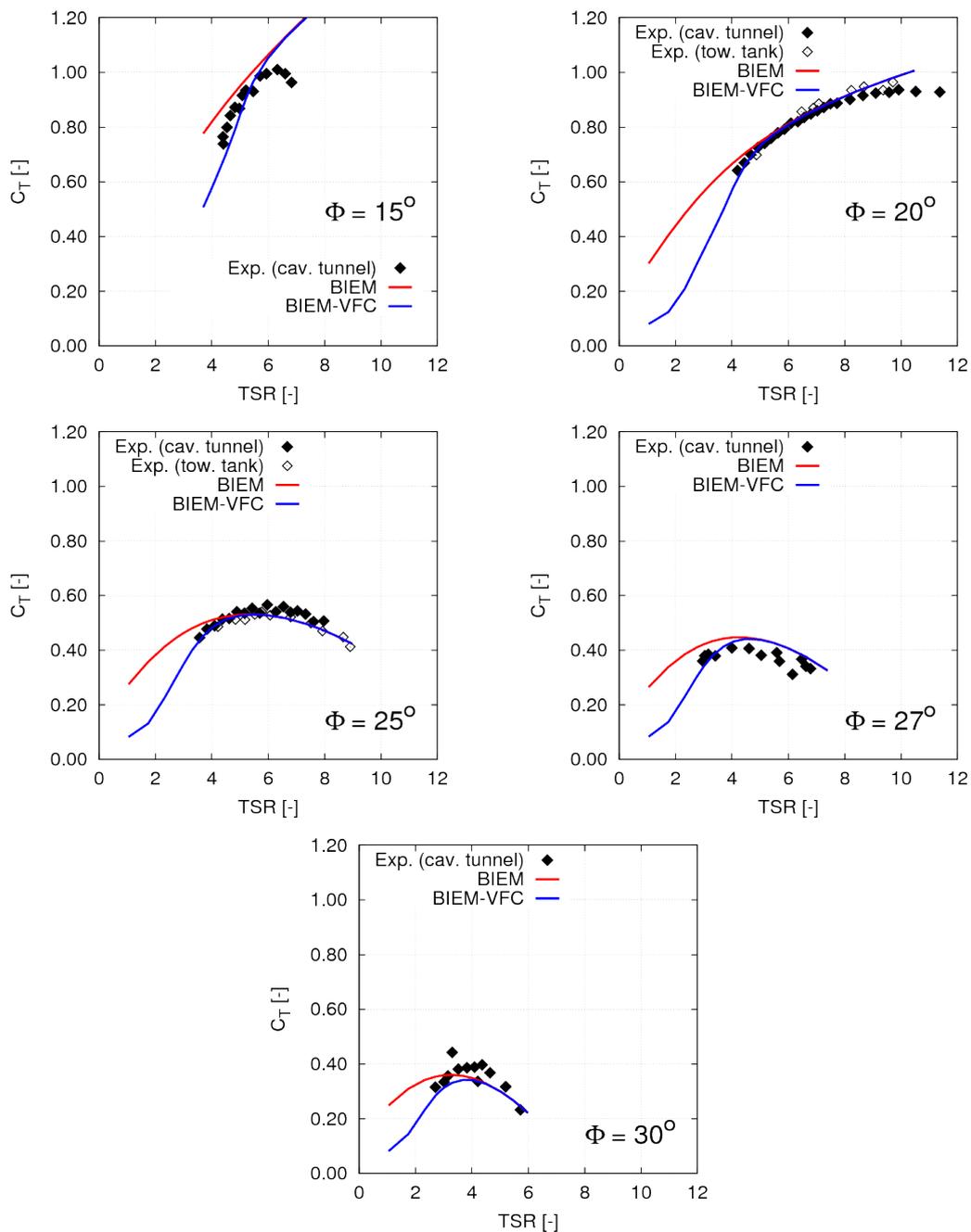


Figure 25. UoS-VP turbine performance predictions by BIEM and BIEM-VFC compared to experimental data in [13]. Thrust coefficient at pitch settings $\Phi = 15^\circ, 20^\circ, 25^\circ, 27^\circ, 30^\circ$.

430 However, fitted experimental data at $\Phi = 30^\circ$ show a rather inconsistent trend with Φ . At off-design
 431 pitch $\Phi = 15^\circ$, BIEM-VFC and X-Foil results match experimental data for $C_{P_{max}}$ and the corresponding
 432 TSR , while the $C_{T_{max}}$ prediction is not plotted since numerical results show an unphysical trend with
 433 increasing TSR as already discussed.

434 Figure 27 allows to compare BIEM-VFC results based on X-Foil predictions of sectional lift
 435 and drag properties with those obtained by considering measured lift and drag in [25]. As already
 436 commented in Fig. 22, measured drag is much higher than X-Foil predictions over a significant range
 437 of angle of attack. As expected, this turns into underestimated turbine power coefficient, bottom left

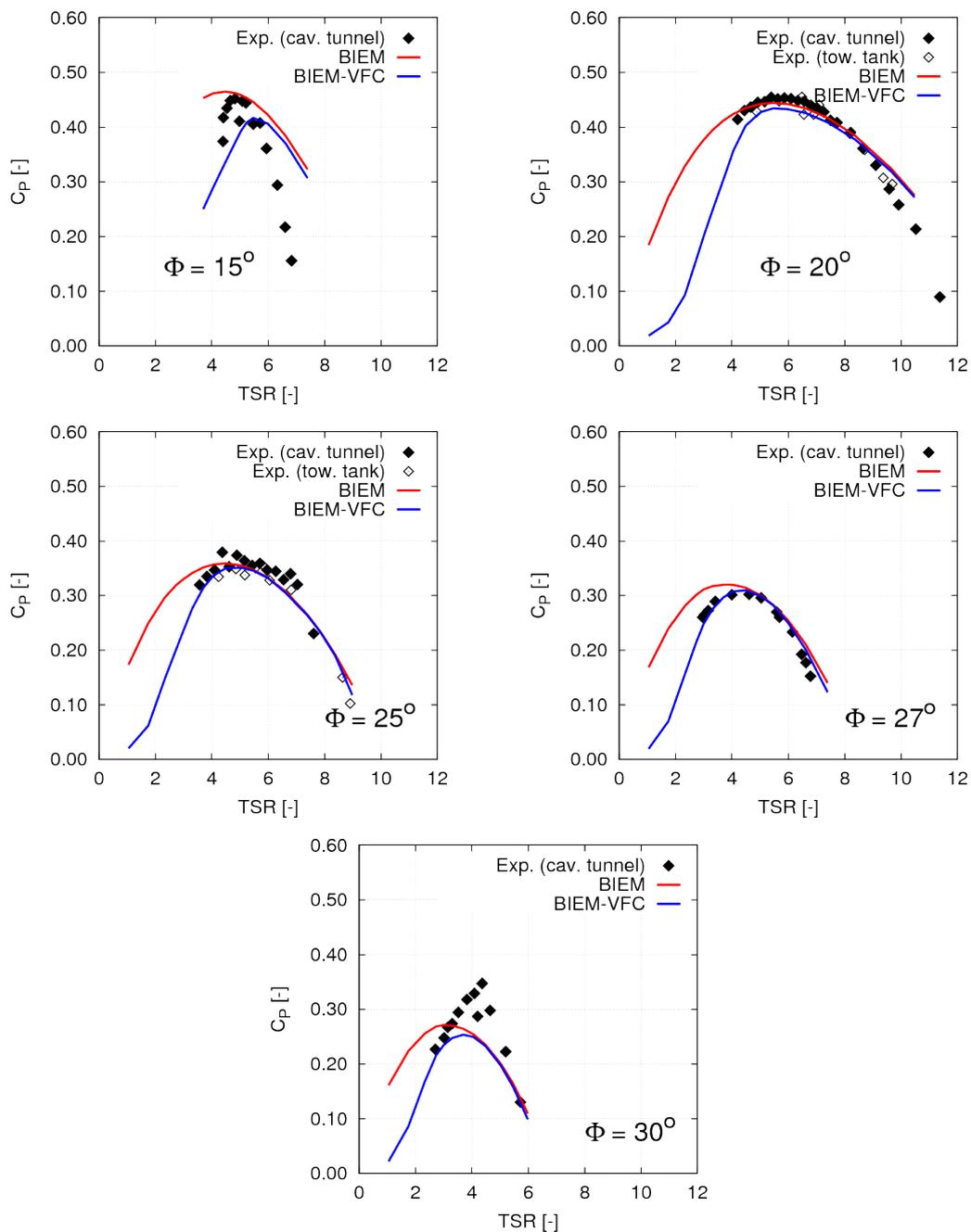


Figure 26. UoS-VP turbine performance predictions by BIEM and BIEM-VFC compared to experimental data in [13]. Power coefficient at pitch settings $\Phi = 15^\circ, 20^\circ, 25^\circ, 27^\circ, 30^\circ$.

438 Fig. 27. Smaller differences between measured and X-Foil lift observed in left Fig. 22, have a negligible
 439 effect on predicted turbine thrust coefficient, as shown in top Fig. 27.

440 In order to complete the present validation study, it is also interesting to compare results by the
 441 proposed BIEM-VFC approach with data from the literature obtained using different computational
 442 models. Two cases are considered here: Bahaj et al. [26] present results by two solvers based on Blade
 443 Element Method (BEM) for pitch settings from $\Phi = 15^\circ$ to 27° . Next, Baltazar & Falcão de Campos [6]
 444 present results by BIEM with viscous flow corrections for cases $\Phi = 20^\circ$ and 25° .

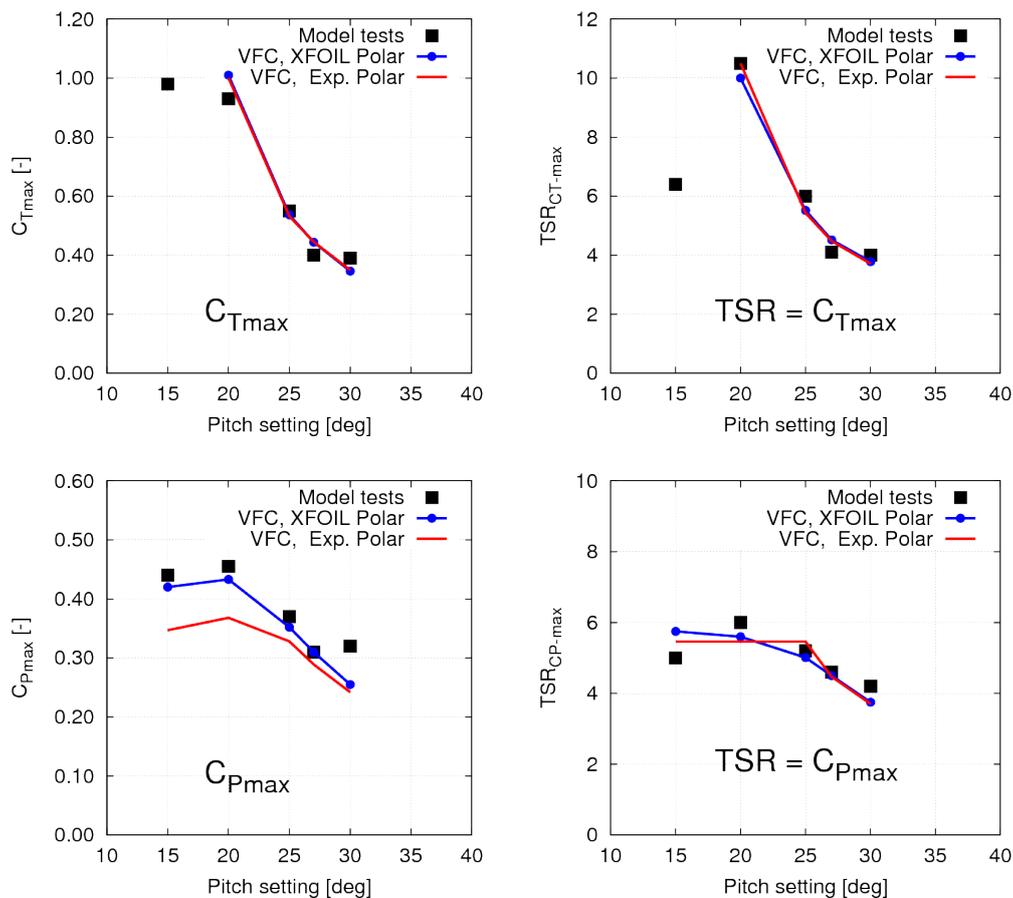


Figure 27. UoS-VP turbine. Effect of pitch setting Φ : from top to bottom, left to right, C_{Tmax} , C_{Pmax} and corresponding TSR values.

445 Thrust coefficient predictions are compared in Fig. 28. Results by BEM solvers GH-Tidal and
 446 SERG-Tidal show an accuracy with respect to model test results in [13] that is broadly comparable to
 447 what is obtained using the present BIEM-VFC. Predictions by BIEM-VFC and GH-Tidal are closer to
 448 experiments than SERG-Tidal for pitch settings $\Phi = 20^\circ, 25^\circ, 27^\circ$, while the opposite holds for $\Phi = 27^\circ$.
 449 This trend is only in part confirmed in Fig. 29 where power coefficient results are shown.

450 While BIEM-VFC and SERG-Tidal show a comparable accuracy for C_p at $\Phi = 20^\circ, 25^\circ, 27^\circ$, results
 451 by GH-Tidal overestimate experimental data. It is also noted that off-design case $\Phi = 15^\circ$ shows similar
 452 results between BEM and the present BIEM-VFC for the thrust coefficient, while power coefficient
 453 results are very different, with BEM models fairly capturing power peak and failing to predict results at
 454 higher TSR . Finally, thrust and power by the BIEM model with viscous correction presented in Baltazar
 455 & Falcão de Campos [6] are underestimated for both pitch setting cases addressed. It is interesting to
 456 observe that results comparable to present BIEM-VFC model are obtained in [6] by considering only
 457 drag correction of standard BIEM predictions. Details of this further comparison are not given here for
 458 the sake of conciseness.

459 6. Discussion

460 The analysis of present results compared to reference data from the literature highlights the
 461 importance of adding a viscous-flow correction to standard BIEM results obtained under inviscid-flow
 462 assumptions. Although simple and partially based on semi-empirical corrections, the proposed
 463 BIEM-VFC approach allows to significantly improve the reliability of turbine performance predictions
 464 by BIEM over a full range of operating conditions, including design and off-design blade pitch settings.

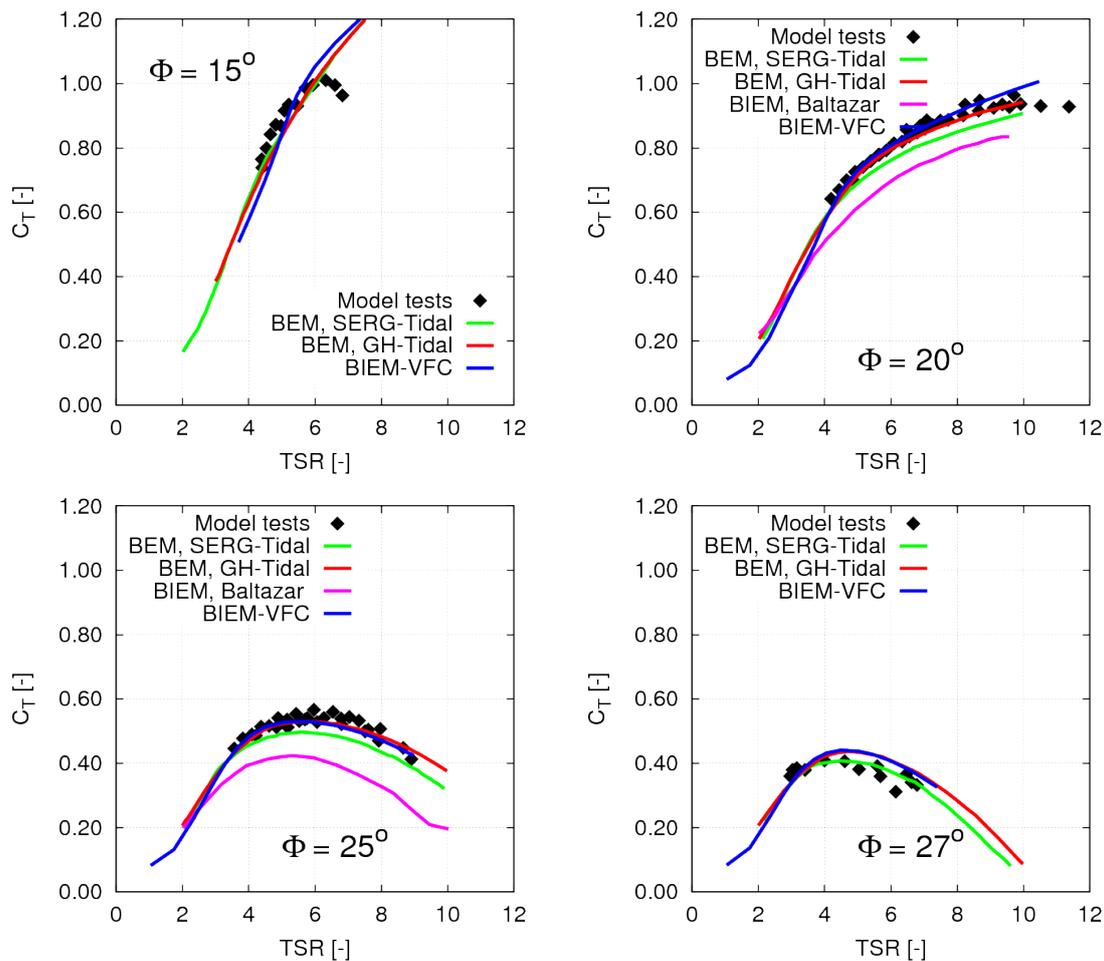


Figure 28. UoS-VP turbine performance predictions by BIEM-VFC compared to results from the literature: thrust coefficient C_T . Pitch settings $\Phi = 15^\circ$ to 27° .

465 Main advantage of BIEM modelling with respect to blade element momentum methods
 466 routinely used for marine turbines is the possibility to determine a consistent representation of the
 467 three-dimensional flow around rotor blades and hub in steady or unsteady flow. Pressure distributions
 468 on the blade surface can be used as input to predict the occurrence of cavitation and to estimate its
 469 detrimental effects in terms of vibrations, noise, erosion.

470 Nonetheless, a major weakness of the present BIEM-VFC approach is that viscosity correction
 471 applies only to blade loads and not to the potential flow solution as a whole. In particular, the correction
 472 does not apply to the intensity of the vortex sheet shed at blade trailing edge, nor to the induced
 473 velocity field necessary to evaluate the effective angle of attack. Neglecting these effects is expected to
 474 be the source of errors in performance predictions when the turbine operates at TSR lower than the
 475 peak power condition.

476 To overcome this limitation, a generalization of the present VFC model is the subject of work
 477 underway. Specifically, trailing vorticity distributions that are compatible with the correction of blade
 478 loads determined by the VFC scheme described in Section 2.2 can be obtained through an iterative
 479 procedure in which the direct relationship between axial and tangential force contributions by a blade
 480 element at radius r and turbine-induced velocity perturbation is derived by momentum and moment
 481 of momentum balance. Furthermore, the boundary integral representation (2) is generalised to include
 482 additional source terms according to the viscous/inviscid coupling methodology proposed in [27].

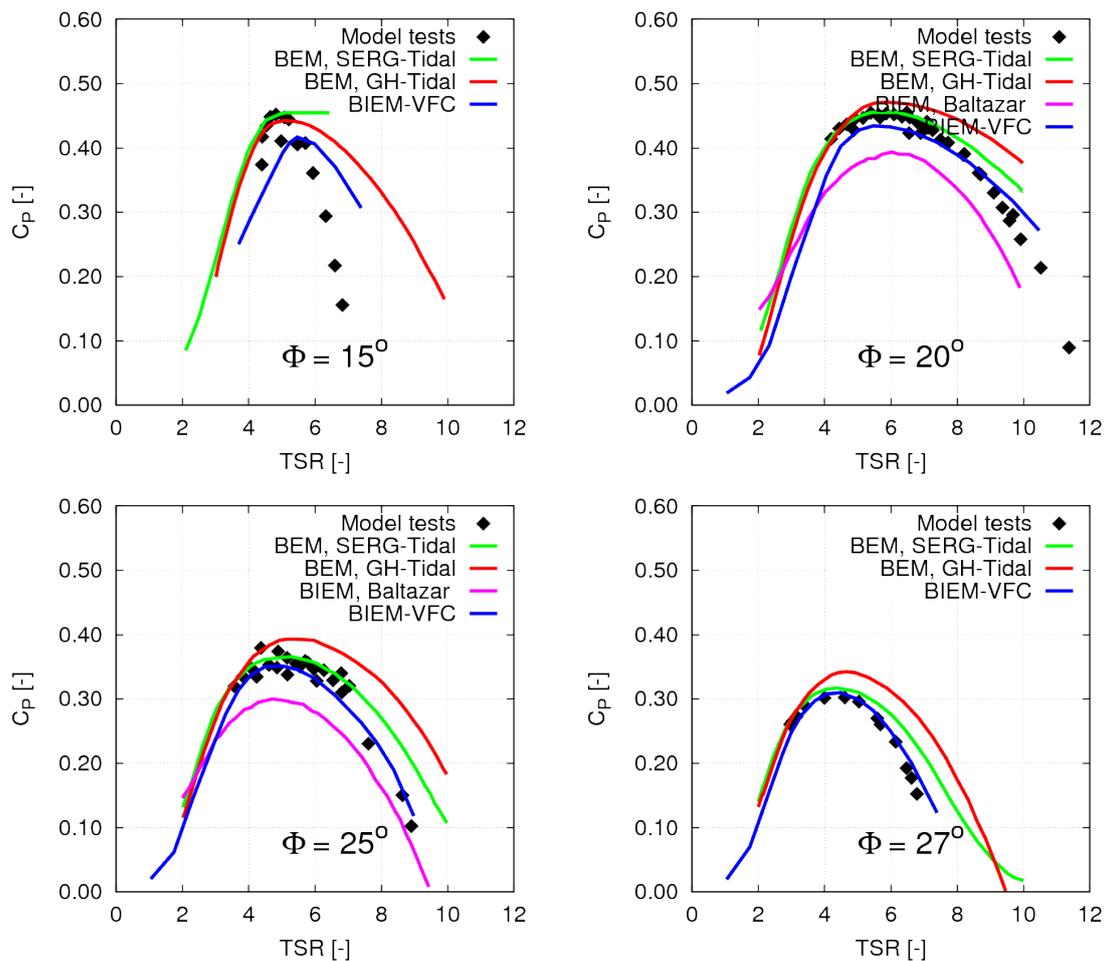


Figure 29. UoS-VP turbine performance predictions by BIEM-VFC compared to results from the literature: power coefficient C_p . Pitch settings $\Phi = 15^\circ$ to 27° .

483 In addition to single turbine performance studies, the BIEM-VFC methodology is also applied
 484 to study the hydrodynamic behaviour of turbines operating in arrays. In this case, the inviscid-flow
 485 BIEM with VFC model is combined with a viscous flow solver (Reynolds-Averaged Navier-Stokes,
 486 RANS) to correctly describe the turbulent, vortical stream that characterizes the inflow to a turbine in
 487 the wake of similar devices placed upstream. An application of this combined BIEM-VFC and RANS
 488 computational methodology has been discussed by the authors in [28] where a preliminary study by
 489 BIEM-VFC of the IFREMER-FP test case addressed above is also addressed.

490 7. Conclusions

491 A computational methodology for the hydrodynamic analysis of horizontal-axis marine current
 492 turbines has been presented, and results of a validation study have been discussed. The approach
 493 is based on a Boundary Integral Equation Model (BIEM) for inviscid flows that is combined with
 494 a trailing wake model specific for hydrokinetic turbines and with a viscous flow correction model
 495 (VFC) to include blade flow separation and stall effects on predicted hydrodynamic loads. The latter is
 496 derived by a semi-empirical approach in which inviscid-flow blade loads by BIEM are corrected on the
 497 basis of lift and drag properties of two-dimensional foils describing blade sections under equivalent
 498 three-dimensional flow conditions.

499 Numerical predictions by BIEM-VFC have been validated through comparisons with experimental
 500 data and with numerical results from the literature. The analysis highlights the capability of the

501 proposed methodology to correctly describe turbine performance over a full range of operating
502 conditions. Specifically, reliable predictions of turbine thrust, torque and power are obtained at
503 medium/high Tip Speed Ratio (*TSR*) regimes, when blade flow is mostly attached, but also at
504 relatively low *TSR*, where blade flow separation and stall determine thrust loss and drag crisis. More
505 in details, good predictions of turbine performance are obtained for blade pitch settings close to design,
506 while discrepancies for both thrust and torque (power) are observed in off-design conditions.

507 Comparing BIEM-VFC with other computational models in the literature, a key finding is that
508 the accuracy the proposed approach is aligned with blade element methods that are routinely used
509 for the analysis and design of marine as well as wind turbines. Such a result is particularly important
510 in that the present methodology based on BIEM provides a physically consistent description of the
511 three-dimensional flow around a turbine in arbitrary onset flow, while blade element methods rely on
512 tailored, case-dependent corrections for blade tip effects, for blade/hub interaction, number of blades.
513 Well known limitations of blade element methods to analyse non-uniform flow conditions as well as
514 to study turbine cavitation are also overcome through the more general description of turbine flow
515 obtained by a BIEM approach.

516 Future work will address the generalization of the present VFC scheme to achieve trailing
517 vorticity distributions and induced velocity distributions that are fully consistent with the viscosity
518 correction applied on blade loads. Further validation studies will focus the capability of the generalised
519 BIEM-VFC model to predict turbine performance at low *TSR* and when turbine blades operate in
520 off-design conditions.

521 **Acknowledgments:** The work described has been funded under the CNR-INSEAN Project ULYSSES
522 (Underpinning LaboratorY for Studies on Sea Energy Systems). The authors wish to thank Dr. Benoit Gaurier for
523 his kind support in the analysis of validation data from experiments at IFREMER. Part of validation data have
524 been developed under the EU-FP7 MaRINET Project (Grant 262552).

525 **Author Contributions:** Francesco Salvatore and Zohreh Sarichloo developed the original viscous-flow correction
526 and trailing wake models while Danilo Calcagni and Francesco Salvatore adapted the existing BIEM model.
527 Zohreh Sarichloo and Francesco Salvatore were responsible for computational model validation studies. All the
528 authors contributed to results analysis and discussion.

529 **Conflicts of Interest:** The authors declare no conflict of interest.

530 **Appendix Nomenclature**

	Symbol	Description	Units
	c	Turbine blade chord	[m]
	C_p	Pressure coefficient	[-]
	C_p	Power coefficient	[-]
	C_F	Friction coefficient	[-]
	C_Q	Torque coefficient	[-]
	C_T	Thrust coefficient	[-]
	D	Turbine diameter, $2R$	[m]
	D	Drag	[N]
	J	Advance coefficient, V/nD	[-]
	\mathcal{K}_D	Drag correction factor	[-]
	\mathcal{K}_L	Lift correction factor	[-]
	L	Lift	[N]
	n	Turbine rotational speed	[s ⁻¹]
531	P	Turbine power	[W]
	p_0	Reference pressure	[Pa]
	Q	Turbine torque	[Nm]
	R	Turbine radius	[m]
	Re_r	Reynolds number, Eq. (6)	[-]
	T	Turbine thrust	[N]
	$TSR; \lambda$	Tip Speed Ratio	[-]
	V	Freestream velocity	[ms ⁻¹]
	α	angle of attack	[deg]
	ν	Kynematic viscosity	[m ² s ⁻¹]
	ϕ	Velocity scalar potential	[m ² s ⁻¹]
	Ω	Turbine rotational speed	[rads ⁻¹]
	ϕ	Wake (linear) pitch	[m]
	Φ	Blade pitch	[deg]
	ρ	Water density	[kgm ⁻³]

532 **References**

- 533 1. Hansen, M. O. L. *Aerodynamics of Wind Turbines.*, 2nd Ed.; Earthscan: London, U.K., 2008.
- 534 2. Buhl, M.L.Jr. A New Empirical Relationship between Thrust Coefficient and Induction Factor for the Turbulent
535 Windmill State. *Technical Report NREL/TP-500-36834*, 2005.
- 536 3. Shen, W. Z., Mikkelsen, R., Sørensen, J. N., Bak, C. Tip Loss Corrections for Wind Turbine Computations.
537 *Wind Energy*, 2005, 8, 457-475.
- 538 4. Young, Y.L., Motley, M.R., Yeung, R.W. Three-Dimensional Numerical Modeling of the Transient
539 Fluid-Structural Interaction Response of Tidal Turbines. *Journal of Offshore Mechanics and Arctic Engineering*,
540 2010, 132, 1-12.
- 541 5. He, L., Xu, W., and Kinnas, S.A. Numerical Methods for the Prediction of Unsteady Performance of Marine
542 Propellers and Turbines., In Proceedings of the *ISOPE 2011* Twenty-first International Offshore and Polar
543 Engineering Conference, Maui, Hawaii, 19-24 June 2011.
- 544 6. Baltazar, J., Falcão de Campos, J.A.C. Unsteady Analysis of a Horizontal Axis Marine Current Turbine in
545 Yawed Inflow Conditions With a Panel Method. In Proceedings of the *SMP'09* First International Symposium
546 on Marine Propulsors, Norway, 22-24 June 2009; Koushan, K., Steen, S., Eds; MARINTEK (Norwegian Marine
547 Technology Research Institute); Trondheim, Norway, 2009.
- 548 7. Baltazar, M.J., Falcão de Campos, J.A.C. Hydrodynamic design and analysis of horizontal axis marine current
549 turbines with lifting line and panel methods. In Proceedings of the *OMAE2011* ASME 30th Int. Conference
550 on Ocean, Offshore and Arctic Engineering, Rotterdam, The Netherlands, 19–24 June 2011; The American
551 Society of Mechanical Engineers; Rotterdam, The Netherlands, 2011; 5, 453-465.

- 552 8. Salvatore, F., Testa, C., Greco, L. A Viscous/Inviscid Coupled Formulation for Unsteady Sheet Cavitation
553 Modelling of Marine Propellers. In Proceedings of the CAV 2003 Fifth International Symposium on Cavitation,
554 Osaka, Japan, 1-4 November 2003.
- 555 9. Salvatore, F., Greco, L., Calcagni, D. Computational analysis of marine propeller performance and cavitation
556 by using an inviscid-flow BEM model. In Proceedings of the SMP'11 Second Int. Symposium on Marine
557 Propulsion, Hamburg, Germany, 15-17 June 2011.
- 558 10. Pereira, F., Salvatore, F., Di Felice, F. Measurement and Modelling of Propeller Cavitation in Uniform Inflow.
559 *Journal of Fluids Engineering*, **2004**, *126*, 671-679.
- 560 11. Gaurier, B., Germain, G., Facq, J.-V., Johnstone, C. M., Grant, A. D., Day, A. H., Nixon, E., Di Felice, F.,
561 Costanzo, M. Tidal energy Round Robin tests: comparisons between towing tank and circulating tank results.
562 *Int. Journal of Marine Energy*, **2015**, *12*, 87-109.
- 563 12. EU-FP MaRINET Project. Available online: https://cordis.europa.eu/project/rcn/98372_en.html (accessed
564 on 29 March 2018).
- 565 13. Bahaj, A.S.; Molland, A.F.; Chaplin, J.R.; Batten, W.M.J. Power and thrust measurements of marine current
566 turbines under various hydrodynamic flow conditions in a cavitation tunnel and a towing tank. *Renewable*
567 *Energy*, (2007), *32*, 407-426.
- 568 14. Morino, L. 'Boundary Integral Equations in Aerodynamics.' *Applied Mechanics Reviews*, **1993**, *46*(8), 445-466.
- 569 15. Greco, L., Salvatore, F., Di Felice, F. Validation of a Quasi-potential Flow Model for the Analysis of Marine
570 Propellers Wake. In Proceedings of the ONR-2004 Twenty-fifth ONR Symposium on Naval Hydrodynamics,
571 St. John's, Newfoundland, Canada, 2004; National Academies Press: Washington, DC, USA, 2004.
- 572 16. Carlton, J.S. *Marine Propellers and Propulsion*, 1st Ed.; Butterworth-Heinemann: Oxford, UK., 1994.
- 573 17. Betz, A. The Maximum of the Theoretically Possible Exploitation of Wind by Means of a Wind Motor. *Wind*
574 *Engineering*, **2013**, *37*(4), 441-446. (Translation by Hamann et al. of original paper published in 1920 by the
575 author in German).
- 576 18. Okulov, V.L., Sørensen, J.N. Maximum efficiency of wind turbine rotors using Joukowsky and Betz approaches.
577 *Journal of Fluid Mechanics*, **2010**, *649*, 497-508.
- 578 19. Micek, P., Gaurier, B., Germain, G., Pinon, G., Rivoalen, E. Experimental study of the turbulence intensity
579 effects on marine current turbines behaviour. Part I: One single turbine. *Renewable Energy*, **2014**, *66*, 729-746.
- 580 20. Del Frate, C., Di Felice, F., Alves Pereira, F., Romano, G.P., Dhomé, D., Allo, J.-C. Experimental Investigation of
581 the turbulent flow behind a horizontal axis tidal turbine. In *Progress in renewable Energies Offshore*, Proceedings
582 of the RENEW 2016 2nd Int. Conference on Renewable Energies Offshore, Lisbon, Portugal, 24-26 October
583 2016.
- 584 21. Drela, M. XFOIL: An Analysis and Design System for Low Reynolds Number Airfoils. In *Low Reynolds*
585 *Number Aerodynamics*. Proceedings of the Conference Notre Dame, Indiana, USA, 5-7 June 1989; Lecture
586 Notes in Engineering, Bd. 54; Springer Berlin: Heidelberg, 1989; 1-12; 978-3-540-51884-6.
- 587 22. Sheldahl, R.E., Klimas, P.C. Aerodynamic Characteristics of Seven Symmetrical Airfoil Sections Through
588 180-Deg. Angle of Attack for Use in Aerodynamic Analysis of Vertical Axis Wind Turbines. *Report*
589 *SAND80-2114*, SANDIA, **1981**, Albuquerque, NM, USA.
- 590 23. Viterna, L. A., Corrigan, R. D. Fixed pitch rotor performance of large horizontal axis wind turbines.
591 DOE/NASA workshop on large HAWTs. Cleveland, Ohio, 1981.
- 592 24. Abbott, I. R.; von Doenhoff, A. E. Summary of airfoil data. *NACA Report 824*, **1945**.
- 593 25. Molland, A.F., Bahaj, A.S., Chaplin, J.R., Batten, W.M.J. Measurements and predictions of forces, pressures
594 and cavitation on 2D sections suitable for marine current turbines. *Journal of Engineering for the Maritime*
595 *Environment*, **2004**, *218*(2), 127-138.
- 596 26. Bahaj, A., Batten W., McCann, G. Experimental verifications of numerical predictions for the hydrodynamic
597 performance of horizontal axis marine current turbines. *Renewable Energy*, **2007**, *32*, 2479-2490.
- 598 27. Morino, L., Salvatore, F., Gennaretti, M. A New Velocity Decomposition for Viscous Flows: Lighthill's
599 Equivalent-Source Method Revisited. *Computer Methods in Applied Mechanics and Engineering* **1999**, *173*(3-4),
600 317-336.
- 601 28. Salvatore, F., Calcagni, D., Sarichloo, Z. Development of a Viscous/Inviscid Hydrodynamics Model for
602 Single Turbines and Arrays. In Proceedings of the EWTEC 2017 Twelfth European Wave and Tidal Energy
603 Conference, Cork, Ireland, 27 August - 1 September 2017.