Article

An agent-based approach to interbank market lending decisions and risk implications

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Abstract: In this study, we examine the relationship of bank level lending and borrowing decisions and the risk preferences on the dynamics of the interbank lending market. We develop an agent-based model that incorporates individual bank decisions using the temporal difference reinforcement learning algorithm with empirical data of 6600 U.S. banks. The model can successfully replicate the key characteristics of interbank lending and borrowing relationships documented in the recent literature. A key finding of this study is that risk preferences at individual bank level can lead to unique interbank market structures which are suggestive of the capacity that the market responds to surprising shocks.

Keywords: Interbank market; Contagion risk; Multi-agent system; Reinforcement learning agents

0. Introduction

Prior to the financial crisis in 2008, central banks and market regulators were primarily concerned with banks’ performance through a microprudential lens, examining individual banks’ asset and liability portfolios to control risk. While this perspective has been commonly used to identify problematic banks, it does not consider the system-wide implications of troubled banks. During the crisis, it was evident that the interbank market suggested a heightened concern for counterparty risk, which reduced liquidity and increased the cost of financing for weaker banks [1]. Banks overall were less likely to lend liquid assets to each other. Large banks, which play a central role in this market, increased their liquidity buffers [2]. This action forced medium and small banks to seek new sources of liquidity.

As banks are highly interconnected, a macroprudential approach that incorporates interbank relationships would not only help identifying potential latent fragility within this market, but also indicate macro risk preferences and tolerances which either would support or hinder the market. Banks are autonomous decision makers to achieve individual objectives. They also respond to market changes to adapt to different risk situations that are dynamic in nature. We develop a multi-agent model in which bank agents are capable of learning using a temporal difference reinforcement learning approach based on performance goals and the changing macro environment. This model presents connections among banks from the systemic perspective, which also solves the lack of dynamics in network formation models [3–5].

We collect data from the U.S. Federal Deposit Insurance Corporation (FDIC) and build a model to represent the U.S. interbank lending system, aiming to investigate how different institutions interact, how risk preferences influence lending/borrowing decisions, and finally how these endogenous
interactions lead to converging policies of different agents. This framework reconstructs interbank exposures of autonomous banks by having each bank learn how to achieve their risk preferences through policy selection. This model captures the dynamic nature of interbank lending networks, including overnight (federal funds), short-term and long-term debts markets.

The primary contribution of this study is to develop a dynamic interbank market model with learning agents to reconstruct the banking system based on banks’ behavioral patterns. From system-wide modeling perspective, we design two experiments to answer the following questions.

1. Can a multi-agent system with learning agents reconstruct the dynamics of an interbank network?
2. Does the change of agent’s risk preference cause the system less prone-to contagion?

To answer these questions, we first examine the characteristics of networks generated from the learning agents. Then we design experiments to investigate the network property changes of U.S. interbank market with different bank risk profiles. We record the equilibrium interbank network of lending and borrowing that is formed under varying lending policies. We then compute and compare the network properties of the modeled interbank market under these different risk preference settings. Results show that the network degree begins to decline as bank agents continue to tighten their lending policies. Overall, our model bridges the gap in banking system contagion literature where most stress testing methods implicitly assume that banks are highly stylized with no individual optimal behavior.

The rest of the paper is organized as follows. In Section 1, we provide background literature. We present the interbank lending model framework and introduce reinforcement learning agents into the interbank framework to build a multi-agent system in Section 2. And then we discuss the data used in the study in Section 3. In Section 4, we describe the validation methods of the model and discuss the convergence of the learning process. Finally, we conduct two experiments and discuss findings accordingly in Section 5. We then conclude the paper in Section 6.

1. Background and related literature

1.1. Interbank network topology

Empirical studies about interbank network structure, especially for overnight market, have been applied to explain system-wide risk exposures. [6], [7], and [8] discovered similar network characteristics of banking system in Austria, Italy and German respectively. They suggested that interbank market presents various distinctive characteristics such as sparsity, power law degree distribution, small clustering, and small world properties. In a similar but more comprehensive study, [9] used balance sheet data to investigate Brazilian interbank network and documented that it fails to satisfy the small world conditions in terms of the arbitrary small clustering coefficient.

Other studies have explored bilateral exposures from the perspective of bank behavioral preferences. By categorizing banks into two groups, small and large banks, [10] concluded that small banks rely on large banks to borrow funds, while large banks tend to hold consistent relationships with familiar counterparties because of lower interest payments. [11] utilizes a collective dataset of an idiosyncratic and sudden shock caused by a large Indian bank. The analysis finds that interbank connections further increase the financial contagion effect and small banks tend to be more exposed to large deposit withdrawal.

1.2. Multi-agent systems in interbank networks

As an alternative method to the traditional general equilibrium models, multi-agent systems are better at modeling real social phenomena, such as adaptive agents’ reaction to macroeconomic environment changes, and information diffusion in the interbank market [12,13]. A multi-agent system consists of autonomous agents with independent behavioral rules, connections to other agents, and an exotic environment [14]. Providing a platform for endogenously learning the network formation, multi-agent systems have been applied on network topologies and contagion risk among banks [3–5].
[15] extended this framework to a multi-layered network structure to replicate multiple types of interbank loans market. Another interesting study of an interbank trading model is to incorporate memory mechanism in agents’ counterparty selection policy [16].

1.3. Multi-agent learning systems

In a multi-agent system, there are often two prominent types of agents: Zero-intelligence agents and learning agents. Zero-intelligence agents are described as those who “do not seek or maximize profits, and does not observe, remember, or learn” [17]. Zero-intelligence agents have been widely adapted to simulate market trading environment in which traders are represented by these agents [18]. On the other hand, learning agents can improve their performance through learning from past experiences. Reinforcement learning methods are often used in developing learning agents. The method allows agents to select an action for each state that tends to maximize the expected future value of the reinforcement signal [19]. Various learning algorithms are used in reinforcement learning and the most common approaches are temporal difference learning and Q learning. Temporal difference learning is a value prediction method that updates its estimate based on its previous estimation (bootstrap) after receiving each reinforcement signal for every action taken. Q learning is one of the most important algorithms used to optimize the expected future reward for each state-action pair. The optimal policy can be learned implicitly using Q learning.

More closely connected to our model is the work done by [5]. In this paper, [5] built a dynamic multi-agent learning system that banks within the system will experience regular deposit shocks and they have to act accordingly in order to remain solvent. They rely on the fundamental reinforcement learning concept to select their counterparties by updating the trust factor between banks.

2. Methodology

This section presents a multi-agent model to simulate the U.S. interbank lending market. We design an iterative dynamic framework in which banks settle debts, process payments, and update financial reports in each iteration. One iteration is equivalent to a quarter, or 3 months. During this process, reinforcement learning agent framework is utilized to determine how bank’s lending and borrowing needs are satisfied based on individual banks’ behaviors and preferences, and the interbank market network dynamics emerge endogenously as a result.

2.1. Multi-agent interbank lending framework

First the model initializes a lending network with 6600 banks linked by interbank debts. There are two types of banks and three types of debts (see Table 1). This initial network is calculated by balance sheet data in 2006 using maximum entropy approach. However, knowing that this algorithm solves the bilateral exposure problem by generating too many links comparing with empirical findings of the real U.S. overnight interbank market, we then allow the model to reorganize itself through the multi-agent learning process.

Table 1. Interbank lending network setting

<table>
<thead>
<tr>
<th>Node Types</th>
<th>Bank of America, Citibank, J.P. Morgan Chase Banks, and Wells Fargo Bank</th>
</tr>
</thead>
<tbody>
<tr>
<td>Large Banks</td>
<td>Small Banks</td>
</tr>
<tr>
<td>Other Banks</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Link Types</th>
<th>Federal funds, usually expire overnight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overnight Debts</td>
<td>Federal securities, usually expire within 3 months</td>
</tr>
<tr>
<td>Short-term debts</td>
<td>Loans expire less than 1 year</td>
</tr>
</tbody>
</table>
In every iteration, banks first process payments to existing debts. According to expiration of the three types of interbank lending, overnight debts are paid fully, short-term debt payments and long-term debt payments are drawn from $U(99\%, 100\%)$ and $U(25\%, 100\%)$ respectively. We adopt Eisenburg-Noe iterative clearing vector algorithm to clear payments [20]. In this process, banks may face liquidity or solvency issue that prevents them to fulfill their obligations (see equations 1 and 2). In this case, the lenders realize write-down for debts with defaulting banks according to the Eisenburg-Noe algorithms pro rata loss distribution method.

Secondly banks settle debts by actively searching for counterparties. Generally, each bank sends borrowing requests to potential lenders, and lenders response with approval or rejection. Detailed decision making policies are associated with agent reinforcement learning process which will be introduced in Section 2.2. At the end of each iteration, banks process balance sheet updates to realize collected payments and latest borrowing/lending activities. Moreover, we incorporate retained earnings based on an empirically fitted distribution $Beta(17.36, -0.1, 0.3)$.

$$E_i(t) \leq A_i(t) - L_i(t)$$  \hspace{1cm} (1)
$$C_i(t) < ON_i^p(t) + ST_i^p(t) + LT_i^p(t)$$  \hspace{1cm} (2)

where $ON_i^p(t)$, $ST_i^p(t)$, and $LT_i^p(t)$ are bank $i$’s payments of overnight borrowing, short-term borrowing, and long-term borrowing on period $t$.

2.2. Bank lending-borrowing with reinforcement learning

In this section, we present a learning method to simulate bank’s behavior in the U.S. interbank lending and borrowing market. This method utilizes reinforcement learning to guide bank decisions to lend and borrow based on the public and private information available. The rest of this section covers the reinforcement learning framework, and how bank’s lending and borrowing needs are matched to form the interbank network.

Reinforcement learning is a computational technique that allows agents to learn and determine the ideal behavior based on past experience. More specifically, agents learn by receiving reinforcement signals generated through interacting with the environment. The objective of a reinforcement learning agent is to maximize its accumulative reward in the future.

There are three elements that drive the interaction between an agent and the environment: state, action, and reward. Upon evaluating the current state, the agent selects an action that maximizes their expected cumulative reward in the long run. The process of selecting an action based on a given state is typically specified in agent’s policy. The environment will return a reward signal that agent can use to learn and improve their future evaluation of states. In our model, agents adopt the temporal difference approach to improve their policy in the current state based on the environment.

This approach does not involve policy optimization, but instead agents have a target policy toward selecting their counterparties for new debts.

2.3. Banking system states

A state refers to all current information, both public and private, received by an agent to determine what to do next. The decision to select an action is based on the agent’s policy and their evaluation of the current state. View on a certain state may be altered upon receiving a reinforcement signal from an action performed in the past. In other words, agent updates their prospect of how good an action is for a given state when they receive updated signal from the environment.

In the model, banks keep track of two scores for all other banks in order to pick the counterparties for new debts: a size score, $S_{\text{size}}$, and a relationship score, $S_{\text{relation}}$. The size score is calibrated through the comparison of bank size to the average size of existing counterparties (This is consistent with the preference of banks to build relationships with large banks).
\[
q_{ij}(t) = \log A_j(t) - \sum_{k,j=1}^{t-1} \log A_k(t-1) I_{i,k}(t-1) \\
I_{i,k}(t) = \begin{cases} 
1, & \text{if } i \text{ and } k \text{ are connected on period } t \\
0, & \text{Otherwise}
\end{cases}
\]

where \(S_{size}^{size}(t)\) is the size score of bank \(j\) evaluated by bank \(i\) on the period \(t\), \(A_j\) is the total assets of bank \(j\), \(I_{i,k}(t)\) is a binary variable for keeping track previous debt obligations.

The relationship score captures the preference of continuing business with existing counterparties. Therefore, the score will be updated upon receiving the reinforcement signal from the lending and borrowing actions a bank makes in each iteration. In the model, temporal difference (TD) method is adopted to update the relationship score, and the updating process is explained and illustrated by a simplified stylized network in Section 2.5. In addition, banks also hold private information about their own target ratios and evaluate the status of their balance sheet to help guide the lending and borrowing policy. We assume that each bank has a settled business model that determines the fraction of assets (or debts) to lend (or borrow) in overnight, short-term, and long-term markets. These target ratios are set as the average on 2001-2005 balance sheet ratios.

2.4. Actions - bank’s lending and borrowing policy

In reinforcement learning, the objective of a policy is to map the current state to an action that optimizes the expected sum of discounted utilities. Agents can either adopt a fixed policy to select an action (passive learning) or learn to select an optimal action based on previous reward signals received (active learning). In this model, banks are modeled as passive learning agents that rely on a fixed policy to select their lending and borrowing counterparties. However, banks may learn to select better counterparties by learning and updating the utilities of states.

In the model, banks first check their current balance sheet ratios and the target ratios to establish their demand of lending and borrowing in overnight, short-term, or long-term markets. For example, if a bank’s current overnight lending ratio is lower than its target, it will look for borrowers in the overnight market. Similarly, if a bank’s current overnight borrowing ratio is lower than its target, it will look for a lender in the overnight market. A bank will keep seeking counterparties until it reaches all of its targets. A score-driven process is then applied to select their counterparties for initializing new debts each period.

Targeting borrowing expectation, first each bank would send borrowing request to large banks based on \(S_{relation}\) because of higher opportunity to obtain funds. As long as the targets are not met entirely, it sends requests to highest scoring bank. If the targets are still not completed, it goes to the highest \(S_{size}\) bank and ask for new debts. This process would continue until the requests are satisfied perfectly or no more fund is available in the market.

Upon receiving a borrowing request, banks go through two key questions: 1) should they provide new debts to borrowers? 2) how much to lend to each requester? Possessing lending preferences, each bank with space in its overnight, short-term, or long-term lending follows a similar scoring system as described in equation (4). Accordingly, banks go through each requests and make decisions until lending targets are completed or no more request left to fill. However, banks may refuse to accept requests from other banks in the market even though they have capacity. The banks utilize an \(S\)-shaped function, \(p(S_{ij}^{total})\), to assess the chance to lend to each specific borrower, which is a revised form but the same assumption in [21]

\[
S_{i,j}^{total} = \omega S_{i,j}^{relation} + (1 - \omega) S_{i,j}^{size}
\]

where \(s(i,j)\) is the score that borrower \(i\) assigns to lender \(j\). It is the weighted average of relationship score and size score of bank \(j\). We set equal weights to these scores so that \(\omega = 0.5\).
In this function, \( p(s_{ij}^{\text{total}}) \) presents the probability that borrower \( i \) lends to lender \( j \), and \( \alpha \) and \( \beta \) respectively control intercept and slope. \( \alpha \) is a real number and \( \beta \) is a negative real number.

Following a uniform distribution, lending banks decide the fraction they want to lend out from their lending pool. The new debt amount is set as the lower value between the one determined by the lending bank and requested by the borrowing bank. This new debt established is observed by both banks as a reward that their bank balance ratios move closer to their respective target ratio. In summary, the flow of the bank’s policy can be represented and illustrated by Figure 1.

**Figure 1.** Bank lending and borrowing policy flowchart

2.5. Temporal difference learning update

The TD algorithm combines the characteristics of both the Monte Carlo method and dynamic programming. Similar to Monte Carlo method, TD algorithm is a model-free approach that is able to evaluate the value of a given state by learning directly from past experiences. In addition, it also incorporates the idea of bootstrapping from dynamic programming that the estimation of their update is based on a previous estimate. In this model, we use TD(0) method to allow banks to learn from past lending and borrowing actions. \( TD(0) \) is formulated as follows:

\[
V(s_t) = V(s_t) + \alpha[r_{t+1} + \gamma V(s_{t+1}) - V(s_t)]
\]

where \( V(s_t) \) is the estimate of expected sum of discounted rewards at time \( t \), \( r_{t+1} \) denotes the observed reward, \( \alpha \) is the learning rate, and \( \gamma \) is a discount factor for \( V(s_{t+1}) \).
In the model, at the beginning of each iteration (a quarter), each bank determines its lending and borrowing actions according to the bank policy described in previous section. Lending and borrowing actions are decided by the size score of each bank and relationship score between two banks. Since size score is determined by the total assets presented in the balance sheet, banks do not update the size score using the temporal difference method. However, since the nature of relationship score is to capture a bank’s tendency to keep existing relationships, banks update their relationship score with other banks by using the TD(0) algorithm. The updating process is described below.

When bank $i$ and bank $j$ established a new relationship, relationship score between the two banks, $s_{relation}$ will be updated using equation (6). At the beginning of each quarter, TD learning is applied to every bank to update their relationship score. In equation (6), $V_t$ denotes the bank’s evaluation of its relationship score with all other banks. $V_{t+1}$ is the estimation of the sum of debts established in the future and it can be formulated as equation (7). In this model, banks assume that all debts received from that counterparty equal to the last reward observed in the future. Therefore, equation (7) can be expended and simplified to equation (8).

$$V(s_{t+1}) = \sum_{k=0}^{\infty} \gamma^k \times r_{t+k+2}$$  \hspace{1cm} (7)
$$V(s_{t+1}) = \sum_{k=0}^{\infty} \gamma^k \times D_{t+k+2}$$
$$= (\gamma \times D_{t+2}) + (\gamma \times D_{t+3}) + (\gamma \times D_{t+4}) + ...$$
$$= D_{t+1}(1 + \gamma^1 + \gamma^2 + ...)$$  \hspace{1cm} (8)

where $D_t$ is the new debts between two banks in period $t$.

As a result, the TD(0) updating process of relationship score can be expressed as:

$$s_{relation}^{relation}(i,j)(t) = S_{i,j}(t) + \varphi[D_{t+1} + \gamma \frac{D_{t+1}}{1 - \gamma} - S_{i,j}(t)]$$  \hspace{1cm} (9)

We make further assumption that the learning rate $\varphi$ is equal to $1 - \gamma$, resulting in:

$$s_{relation}^{relation}(i,j)(t) = S_{i,j}(t) + (1 - \gamma)D_{t+1} - \alpha S_{i,j}(t)$$
$$= S_{relation}^{relation}(i,j)(t) + D_{t+1}$$  \hspace{1cm} (10)

3. Data

Financial reports are one of the key information sources that disclose banks’ financial fundamentals and business conditions. The Federal Reserve, FDIC, and OCC require all U.S. regulated banks to submit quarterly reports known as Federal Financial Institutions Examination Council Reports of Condition and Income. Those banks include national banks, state member banks and insured state nonmember banks. Similar to regulators that rely on balance sheets to monitor banks’ liquidity status and banking system structures, we use balance sheets data from March, 2001 to December, 2014, covering around 10,000 banks (see Table 2).
Table 2. Description of the bank balance sheet

<table>
<thead>
<tr>
<th>Asset: A</th>
<th>Liability: L</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overnight lending: $ON^a$</td>
<td>Overnight borrowing: $ON^b$</td>
</tr>
<tr>
<td>Short-term lending: $ON^a$</td>
<td>Short-term lending: $ON^b$</td>
</tr>
<tr>
<td>Long-term lending: $ON^a$</td>
<td>Long-term borrowing: $ON^b$</td>
</tr>
<tr>
<td>Cash and balance due: C</td>
<td>Other liabilities: $OL$.</td>
</tr>
<tr>
<td>Other assets: $OA$</td>
<td><strong>Equity</strong>: $E$</td>
</tr>
</tbody>
</table>

In the model, we assume that banks target at a series of balance sheet ratios (see Table 3), associated with banks’ decisions of lending and borrowing. These targets guarantee that banks maintain their lending-borrowing preferences for overnight, short-term, and long-term debts. Additionally, we use the equity multiplier, the ratio of its total assets to its equity, to control a bank’s expected leverage.

Table 3. Banks’ target ratios

<table>
<thead>
<tr>
<th>Equity multiplier</th>
<th>$E/A$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overnight lending, borrowing ratio</td>
<td>$(ON^a/A) , (ON^b/L)$</td>
</tr>
<tr>
<td>Short-term lending, borrowing ratio</td>
<td>$(ST^a/A) , (ST^b/L)$</td>
</tr>
<tr>
<td>Long-term lending, borrowing ratio</td>
<td>$(LT^a/A) , (LT^b/L)$</td>
</tr>
</tbody>
</table>

4. Model validation

We run a number of validation exercises to ensure that model can produce inter-bank markets resembling of the real interbank markets. The model is first initialized based on 2001 financial data. The distribution of the four selected ratios is validated according to simulation data of 20 quarters and empirical data from 2001 to 2006. A comparison of the distributions of the four observed versus simulated ratios shows that from a balance sheet perspective, the simulation closely resembles real bank lending and borrowing behaviors. And then we compare the network topology features to those described in the current literature.

4.1. Network properties validation

We validate overnight lending market with the U.S. federal fund market. [22] collected interbank transactions in 2006 from Fedwire and analyzed the empirical network topology. To compare the network structures, we conducted 100 experiments with the same number of agents (see Table 4). An interesting finding is that the intelligent agents generate a network structure that is very close to our previous study [21].

Table 4. U.S. Federal Funds Market Interbank Network Property Comparison (100 simulations)

<table>
<thead>
<tr>
<th></th>
<th>Average In-Degree</th>
<th>Average Out-Degree</th>
<th>In-Clustering Coefficient</th>
<th>Out-Clustering Coefficient</th>
<th>Power Law</th>
</tr>
</thead>
<tbody>
<tr>
<td>U.S. Fed. Funds Market Model</td>
<td>9.30</td>
<td>19.10</td>
<td>0.10</td>
<td>0.28</td>
<td>2.00</td>
</tr>
<tr>
<td></td>
<td>10.39</td>
<td>17.14</td>
<td>0.03</td>
<td>0.21</td>
<td>1.94</td>
</tr>
</tbody>
</table>

4.2. Convergence of relationship score learning

Banks use temporal difference learning to update their relationship scores as they receive reinforcement signals from borrowing and lending actions. In this experiment, we study the effectiveness of applying $TD(0)$ method in a complex interbank network environment. [19] provides a
thorough proof that $TD(0)$ method coverages to a optimal evaluation for linear problems. However, effectiveness of applying $TD(0)$ method in complex real-world problems remain unclear. [23] investigates the effectiveness of TD method on complex practical issues such as the game of backgammon and self-play. In this model, we validate the use of temporal difference learning by investigating the convergence of relationship score (the TD updating target) over time.

![Figure 2. Learning convergence of TD target](image)

The experiment runs for 100 iterations of bank lending and borrowing interactions. At each iteration, the mean squared error of relationship score is recorded and computed for the entire bank population. From Figure 2, we can see that the mean squared error of relationship score converges as the system runs for 100 iterations.

5. Experiments and discussions

The multi-agent learning model simulates the banking system dynamics and provides a realistic tool to investigate problematic issues in the interbank lending system. In this section, we conduct two experiments to examine the model effects on interbank market structures due to banks’ risk behaviors.

5.1. Interbank network topologies

Interbank network degree is asymmetric. Both in-degree and out-degree are heavily right skewed, indicating that most bank agents have few established relationships (see Figure 3 and Figure 4). Moreover, we observe power-law decaying pattern in the in-degree distribution (see Figure 3). Obviously, banks prefer to maintain a lower number of lenders. Over 10% of banks only borrow from one lender. However, it is not common to minimize the number of borrowers due to consideration of risk diversification.
In this experiment, we examine the interbank network structure after 50 iterations of the model simulation and discuss the preliminary results that show the differences between a risk-seeking lending policy and a risk-averse lending policy. We present two network structures that identify the lending and borrowing relationships between banks. Figure 5 shows the interbank network when banks adopt a risk-seeking lending policy and Figure 6 shows the network when banks become more risk averse in accepting lending requests. In both network plots, we labeled the four large bank agents as “1,2,3,4” because empirical studies have suggested that they tend to establish more lending and borrowing relationships than other banks [10]. From these results we discover that large banks tend to form their own clusters when they employ a risk seeking policy. On the other hand, this phenomenon becomes less obvious when they adopt a more risk-averse policy.
5.2. Network adaptation and risk preferences

The bank lending policy (equation 5) shows that $\alpha$ is the risk tolerance parameter. A small $\alpha$ represents higher risk tolerance. Put it differently, when $\alpha$ decreases, banks risk-seeking lending policy and have higher chance to lend out. In this experiment, we study the network property adaptation by altering $\alpha$ from $-5$ to $5$. We explore changes in average degree, clustering coefficient, and average shortest path (see Table 5). These network characteristics of the interbank systems are generally inline with the empirical observations [6–8].
Table 5. Interbank network topology

<table>
<thead>
<tr>
<th></th>
<th>Average degree</th>
<th>Clustering coefficient</th>
<th>Power law</th>
<th>Average path</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Overnight</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Risk-Seeking Policy</td>
<td>15.12</td>
<td>0.35</td>
<td>2.39</td>
<td>2.34</td>
</tr>
<tr>
<td>Risk-Averse Policy</td>
<td>11.51</td>
<td>0.19</td>
<td>2.42</td>
<td>2.66</td>
</tr>
<tr>
<td><strong>Short-term</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Risk-Seeking Policy</td>
<td>1.04</td>
<td>0.43</td>
<td>2.44</td>
<td>2.30</td>
</tr>
<tr>
<td>Risk-Averse Policy</td>
<td>1.04</td>
<td>0.53</td>
<td>2.29</td>
<td>2.21</td>
</tr>
<tr>
<td><strong>Long-term</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Risk-Seeking Policy</td>
<td>2.42</td>
<td>0.40</td>
<td>2.14</td>
<td>2.44</td>
</tr>
<tr>
<td>Risk-Averse Policy</td>
<td>2.42</td>
<td>0.57</td>
<td>2.15</td>
<td>2.28</td>
</tr>
</tbody>
</table>

As the model forms a directed network in which edges are pointing from lender to borrower. We can measure how the calibration of \( \alpha \) impacts the average number of in-degree (lending) and out-degree (borrowing) relationships. We observe similar patterns for the two measures. The network degree is stable when \( \alpha \leq -1 \), however degree decreases with increasing \( \alpha \) (see Figure 7 and Figure 8). This result confirms that a tightened lending policy reduces the amount of debt, or counterparities, in interbank network. Moreover, the 95% confidence interval of in-degree is much larger than that of out-degree. These results are consistent with our finding of asymmetric distributions for lending and borrowing. With an increasing \( \alpha \), it becomes harder for banks to find lenders such that the in-degree is decreasing with a tighter confidence interval (see Figure 7).

Figure 7. Risk preference \( \alpha \) vs. In-degree
The average shortest path, as shown in Figure 9, agrees with the hypothesis that interconnectedness of banks declining as $\alpha$ increases. We observe longer distance among banks when $\alpha$ is positive, indicating that the whole system is less connected.

Upon inspecting Figure 10, we find the clustering coefficient of the network becomes less clustered as the risk aversion increases. This phenomenon shows that when banks become more averse to lending to other banks, the network becomes less clustered thus more sparse than complete. This is validated by also a decreased degree and increasing average shortest path, which also indicate a loosely connected network.
6. Conclusion

This study proposes a multi-agent learning model to reconstruct interbank lending networks and examine their dynamics. We incorporate a reinforcement learning framework to guide bank decisions. Banks learn and update their choice parameters based on past interaction within the system. Our model is able to capture the individual preferences of banks while allowing them to vary their policies to the environmental conditions presented.

Two experiments are conducted in this study to investigate the network properties of the interbank lending market as adaptive bank risk preferences are varied. First, we look at two different interbank networks of banks adopting a risk-seeking lending policy and a tightened lending policy respectively. We compare the network properties of the two interbank lending networks, and show that given a certain level of risk preference, the network degree begins to decline as bank continue to tighten their lending policies. Secondly, we examine the interconnectedness of bank agents by computing the clustering coefficients and average shortest path amount banks. This suggests that as banks tighten their lending policies, the network becomes sparser and thus more concentrated. As a result, the interbank network is less at risk to concerns of contagion. Though banks are less likely to find new counterparties, they are generally more capable of sustaining stresses, thus demonstrating how individual choices presents beneficial overall market structure condition due to the adaptive learning capabilities of the banks. This finding supports the general observation during the financial crisis.

The methodology proposed in this study offers a new perspective on how one can utilize reinforcement learning to model bank agents. Combined with the use of financial data, we provide guidance on how central banks and regulators may consider building more functional models for examining the interbank systemic risks. Future research might include exploring how banks dynamically select the optimal policy based on the observed states, and consider how monetary policy influences competition in interbank lending.

References


