Broadening of the Neutral Helium 492 nm Line in a Corona Discharge: Code Comparisons and Data Fitting

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Abstract: Passive plasma spectroscopy is a well-established non-intrusive diagnostic technique. Depending on the emitter and its environment which determine the dominant interactions and effects governing emission line shapes, passive spectroscopy allows the determination of electron densities, emitter and perturber temperatures as well as other quantities like abundances. However, using spectroscopy needs appropriate line shape codes retaining all the physical effects governing the emission line profiles. This requires for line shape code developers to continuously correct or improve them to increase their accuracy when applied for diagnostics. This is exactly the aim expected from code-code and code-data comparisons. In this context, the He I 492 nm emitted in a helium corona discharge at room temperature represents an ideal case since its profile results from several broadening mechanisms: Stark, Doppler, resonance and van der Waals. The importance of each broadening mechanism depends on the plasma parameters. Here the profiles of the He I 492 nm in a helium plasma computed by various codes are compared for a selected set of plasma parameters. In addition, preliminary results related to plasma parameter determination using experimental spectra from a helium corona discharge at low pressure 1-2 bars, are presented.

Keywords: Stark broadening; van der Waals broadening; line shapes; helium plasma; corona discharge; plasma diagnostics; code comparison; neutral broadening; pressure broadening

1. Introduction

Passive plasma spectroscopy is a well-established non-intrusive diagnostic technique [1-2]. Depending on the emitter and its environment which determine the dominant interactions and effects governing emission line shapes, passive spectroscopy allows the determination of electron densities, emitter and perturber temperatures as well as other quantities like abundances. However, using passive (and also active) plasma spectroscopy needs appropriate line shape codes retaining all the physical effects governing the emission line profiles. Therefore, line shape code developers to continuously correct, update and improve their codes in the aim of increasing their accuracy when applied for diagnostics. In that context, Spectral Line Shape in Plasmas code comparison workshops [3-4], in which line profile codes are compared against each other through well identified cases but also against experimental data, contribute to the achievement of such an aim. The He I 492 nm line emitted in a helium corona discharge at room temperature represents a rather unique case since its profile results from several broadening mechanisms whose relative importance depends on the plasma parameters. Generally, in such plasmas created by corona discharges in helium, a small amount of hydrogen is introduced for spectroscopic diagnostics like those based on the hydrogen Balmer-β line spectra, which is a subject of a separate paper in this issue [5]. Therefore in this kind of...
plasmas, in addition to the plasma electrons and ions, there are also hydrogen and helium neutrals. The ion population is dominated by singly ionized helium ions, i.e., He$^+$ ions. Also often such plasmas are not at thermodynamics equilibrium and ions, neutrals and electrons may have different temperatures. These circumstances are favorable to many broadening mechanisms which compete in the formation of shapes of lines like the He I 492 nm one. Therefore in addition to Stark broadening due to the interaction of the neutral helium emitters with the plasma electrons and ions and to Doppler broadening due to the emitter own thermal motion, this line may be subject to both resonance and van der Waals broadenings due to interactions of the emitters with neutrals of the same species or not. More details on these mechanisms will be given later. Experimental spectra containing this line (492 nm) and its neighbor hydrogen H$\beta$ line (486 nm) were proposed as a challenge requiring codes to infer the plasma parameters if possible from both lines for consistency. The spectra were obtained for pressures in the range 1-5 bars but as only these lines were treated unequally by the contributors with all H$\beta$ line spectra were analyzed while only those corresponding to low pressure cases for the He I 492 nm and with only few codes in a preliminary way, it was estimated that these lines need to be treated separately. Therefore, this paper is focused on comparisons of the profiles of the He I 492 nm in a helium plasma computed by various codes for a selected set of plasma parameters corresponding to a non-equilibrium plasma. In addition, preliminary results related to plasma parameter determination using experimental spectra from a helium corona discharge at a low pressure 1.5 bars, will be presented.

The paper is divided in two parts. The first part focuses on the profiles of the He I 492 nm line emitted by neutral helium atoms perturbed by the electrons and He$^+$ ions of a helium plasma as well as other neutrals (hydrogen and helium atoms). Here profiles of the He I 492 nm line broadened by only Stark effect are compared for a selected set of plasma parameters corresponding to or close to conditions met in corona discharges in a helium gas with some traces of hydrogen. More precisely, a prescribed grid of six electron density and temperature pairs called subcases were proposed: $n_e=10^{15}$ and $10^{16}$ cm$^{-3}$ for the electron density while the values 0.1, 0.2 and 0.4 eV have been proposed for the electron and ion temperatures assumed to be equal ($T_i=Ti$). In this way, calculations of theoretical profiles allow to point out any differences between codes that may result from the various treatment of the ionic and electronic contributions to Stark broadening, the treatment of other broadening mechanisms being common to all codes. The second part of this paper deals with preliminary comparisons with some experimental spectra of the same line measured in a corona discharge in helium.

2. Description of the atomic system and the line shape codes

In this section we present some basic atomic physics allowing the definition of radiator system and introduce the codes involved in the study of the six subcases of case 15. For an isolated neutral helium atom, the 492 nm line is the result of an allowed transition of the optical electron between two singlet levels, with the upper and lower levels being respectively 1s4d $^1D$ and 1s2p $^1P^o$. It was proposed to retain for the line profile calculations the 1s4p $^1P^o$ and 1s4f $^1F$ levels which are coupled to the 1s4d $^1D$ term by allowed dipolar transitions. In a plasma, the couplings of these levels to the 1s4d $^1D$ one due to the electric microfield, i.e 1s4d $^1D$-1s4f $^1F$ and 1s4d $^1D$-1sp $^1P^o$ lead to the appearance of the originally forbidden transitions 1s2p $^1P^o$-1s4f $^1F$ and 1s2p $^1P^o$-1s4p $^1P^o$. These forbidden transitions appear as lateral components accompanying the 492 nm line whose intensities increase with increasing electron density. Four codes including one numerical simulation method were involved in this case. The simulation code is SimU for which good descriptions may be found for instance in [6-7]. The remaining three codes are PPP [8], QC_FFM [9] and the references therein and a new code called ZEST [10] which relies on a quasi-static description of the ions and an impact approximation for the
electrons. At the time of calculations, ZEST neglected the collisional shift due to the electrons, the interference terms between upper and lower states, the non-diagonal terms of the collision operator and the frequency dependence of the impact width. At the time of the calculations presented here, the ZEST code did not include the ion dynamics effects but now, in its most recent version it does [10], the ion dynamics effects being modeled within the framework of the fast FFM [11]. In the next section, we compare the calculated profiles and the widths at half-maximum for the two densities (lower density $n_e=10^{15}$ cm$^{-3}$) and higher density ($n_e=10^{16}$ cm$^{-3}$).

3. Code comparison through profiles and line widths

3.1. He I 492 nm line profiles for the lowest density

The results of the code calculations for the lower density case ($n_e=10^{15}$ cm$^{-3}$) are respectively illustrated for equal ion and electron temperatures of 0.1, 0.2 and 0.4 eV in Figures 1-3. For each figure corresponding to a subcase, the profiles were plotted using a logarithmic scale together with the linear scale to point out more clearly the differences. As it can be seen from figure 1, the calculations carried out by PPP, ZEST and SimU codes are comparable and agree to some extent. Of course they give different widths with SimU calculations providing the lowest FWHM followed closely by ZEST and PPP. This relative agreement is also seen on the forbidden components. Indeed, the three codes give profiles showing the lateral forbidden components already mentioned previously. The highest lateral peak (closest peak to the line center) represents the $1s2p\,{}^1P^o-1s4f\,{}^1F$ transition while the weakest peak (located far from the line center) refers to the $1s2p\,{}^1P^o-1s4p\,{}^1P^o$ transition. An average FWHM of about 2.8 cm$^{-1}$ has been estimated for this subcase. The profile calculated by QC_FFM is different from all the others. As expected, QC_FFM gave much broader profiles with no forbidden components. Indeed, recall that the QC model is derived assuming (i) an H-like (fully degenerate) atomic system and (ii) a transition with $\Delta n \gg 1$. For these reasons, neither forbidden components nor detailed line core structure (such as a dip in H-β) can be reproduced. As a result, since the He I $n=4$ singlet states at lower densities are far from being degenerate, QC_FFM is very inaccurate, and should not be used in real-life scenarios. However, as the plasma density is increased (see below), the atomic system approaches the degenerate-case assumption and the results of QC_FFM become more reliable. When it comes to the second case corresponding to 0.2 eV shown on figure 2, the situation is identical for SimU, PPP and ZEST whose calculations are in a relative overall agreement with ZEST calculations being more closer to those of PPP than to those of SimU. Both three codes agree in showing forbidden components in terms of positions even though there are differences in their widths and shapes. The weak forbidden component $1s2p\,{}^1P^o-1s4p\,{}^3P^o$ is visible on both linear and logarithmic scales while the most central forbidden component $1s2p\,{}^1P^o-1s4f\,{}^1F$ is visible only on the logarithmic scale. The situation is worse for QC_FFM with a large overestimation of the width which is at least two or three times the average one of about 3.5 cm$^{-1}$ shown on figure 2. For the last subcase corresponding to a temperature of 0.4 eV shown on figure 3, again QC_FFM calculations are completely different from all others with a clear overestimation of the broadening. In terms of FWHM, there is no change with respect to the previous subcase with the same average FWHM of 3.5 cm$^{-1}$. Again one can see the agreement between PPP, ZEST and SimU which is even better in terms of widths. There are still some small differences in the shapes of the forbidden components.
Figure 1. Theoretical Stark profiles of the He I 492 nm line calculated for helium plasma with an electron density of $10^{15}$ cm$^{-3}$ and a temperature of 0.1 eV for both plasma He$^+$ ions and electrons corresponding to case 15.1.1.1. The profiles are centered at 492 nm and expressed as wavenumbers using cm$^{-1}$ units. (a) Linear scale. (b) The profiles are the same but a logarithmic scale is used to highlight the differences between the different calculations. In both (a) and (b), the average FWHM is shown. Red dot-dashed line: SimU, solid blue: ZEST, solid green: PPP, solid grey: QC_FFM.

Figure 2. Same as Figure 1 but for $T_e=T_i=0.2$ eV.
3.2. He I 492 nm line profiles for the highest density

As for the previous case, the results of code calculations for the higher density case \((n_e=10^{16} \text{ cm}^{-3})\) with the same temperatures 0.1, 0.2 and 0.4 eV are respectively shown in Figures 4-6. Unlike the previous case, by showing a broadening about twice than the other code calculations, the profiles given by PPP seem to be inadequate for the conditions of this subcase. This is attributed to the frequency independence of the GBK (Griem-Blaha-Kepple) formulation of the [12] collision operator used in this PPP version to treat the line electron broadening electron broadening and to the use of a Holtsmark field distribution for the ions. This demonstrate that the use of a frequency-dependent collision operator may show up narrower profiles as compared to those calculated by a frequency independent operator. For this density, the expected discrepancy between the calculations carried out by the PPP code using the GBK collision operator and those of the other codes are more pronounced confirming the non-validity of this form of collision operators at high densities and low temperatures. One can see that for the remaining calculations, SimU is close to ZEST in terms of widths but differs significantly when it comes to the intensity of the forbidden components. QC_FFM shows higher widths than ZEST and SimU. Similar remarks can be said for the calculations of the second subcase of figure 4 (0.2 eV). However, the subcase of figure 6 seems more favorable for all codes. These conditions correspond in terms of results to those of Figures 1-3. Except the intensity of the forbidden components, SimU and ZEST give very close results especially at the line wings. The widths of the PPP profiles are close to those of QC_FFM.
Figure 4. Theoretical Stark profiles of the He I 492 nm line calculated for a helium plasma with an electron density of $10^{16}$ cm$^{-3}$ and a temperature of 0.1 eV for both plasma He$^+$ ions and electrons. The profiles are centered at 492 nm and expressed as wavenumbers in cm$^{-1}$ units. Blue: ZEST, green: PPP, grey: QC_FFM, red dot-dashed: SimU. (a) Linear scale. (b) Same profiles in a logarithmic scale.

Figure 5. Same as Figure 4 but for $T_e=T_i=0.2$ eV. Same line styles and code colors as Figure 4.
3.3. Comparison of the FWHM of the He I line

The FWHM (Full Widths at Half Maximum) of the He I line vs the electron temperature (0.1, 0.2 and 0.4 eV) deduced from all the synthetic profiles are shown on Figure 7 for two values of the electron density $n_e=10^{15}$ and $10^{16}$ cm$^{-3}$. In this figure (a), we can see that the widths deduced from QC_FFM calculations are about twice the average one. The values deduced from the remaining codes agree at higher electron temperatures but show a dispersion with a factor of two at the lowest temperature. In figure 7 (b), the value of the FWHM at the lowest electron temperature is much higher than in comparison to other codes. The other widths show some dispersion with a factor 2 to 3 between the codes.

Figure 6. Same as Figures 4 and 5 with the same line styles and code colors but for $T_e=0.4$ eV.

Figure 7. The He I line Full Widths at Half Maximum (FWHM) versus the electron temperature as deduced from the profiles calculated by the four codes PPP, QC_FFM, SimU and ZEST. (a) Lowest density ($n_e=10^{15}$ cm$^{-3}$). (b) Highest density ($n_e=10^{16}$ cm$^{-3}$).
4. Preliminary comparisons with experimental spectra

4.1. Experimental spectra

The experimental spectra proposed for analysis were measured in a corona discharge in helium performed in an electrical engineering laboratory for the study of the dielectric properties of insulators [13-14]. Spectra of the neutral helium 492 nm and its neighboring hydrogen H-β (486.1 nm) lines were measured at room temperature for various values of the pressure. Spectra corresponding to six values of the pressure in the range 1-5 bars are shown in Figure 8. The He I 492 nm line spectra (left peaks) corresponding to pressures of 1, 1.5, 2, 3, 4 and 5 bars are respectively termed 15a, 15b, 15c, 15d, 15e and 15f. One can see that both helium and hydrogen lines become broader as the pressure is increased indicating an increase in the Stark broadening of both lines. More specifically, it can be also seen that the helium line (left peak of each spectrum) presents an increasing asymmetry which is partially due to the forbidden components. Therefore, high pressure spectra with complex features are difficult to reproduce by calculations. That is why only few cases were considered mainly spectra 15a and 15b. Therefore, the comparisons code-experimental data which are presented here are preliminary and are only used for illustration.

![Figure 7. Superposition of six experimental spectra of the He I 492 nm (left) H-β 486.2 nm (right) lines measured at room temperature for the following pressures in the range 1-5 bars. Black: 1 bar, red: 1.5 bars, dark brown: 2 bars, light brown: 3 bars, green: 4 bars and blue: 5 bars. Helium spectra are labelled 15a (P=1 bar) to 15f (P=5 bars).](image)

4.2. Broadening of the neutral helium line

The 492 nm line emitted by neutral helium atoms in a corona discharge is broadened by several mechanisms. For the experimental data considered here, the instrumental function was estimated from a helium calibration lamp to be a Gaussian with a FWHM less than 0.01 nm [14]. Beside the instrumental function and the natural broadening which are very small, the line may be subject to Stark, Doppler, resonance and van der Waal broadenings. Resonance and van der Waals broadenings [15] which are due to collisions between neutrals can be represented by Lorentzian shapes whose FWHM depend on the ratio (P/T) as follows: \( \Delta \lambda_{\text{res}} \propto (P/T) \) and \( \Delta \lambda_{\text{vdW}} \propto \left( \frac{P}{P_0 T_0} \right) \), where P and T are respectively the pressure and the neutral temperature. For the considered spectra, the resonance broadening was estimated to be negligible in comparison to other broadening mechanisms and was
therefore ignored. Estimated FWHM of the van der Waals broadening for each experimental
spectrum are shown in Table 1. The van der Waals broadening represents about 30% of the total
broadening of the line.

218 Table 1. Summary of the FWHM of the van der Waals broadening compared with the experimental
FWHM of the six experimental spectra of the He I 492 nm line.

<table>
<thead>
<tr>
<th>Pressure (bars)</th>
<th>( \Delta \lambda_{vdW} ) (nm)</th>
<th>( \Delta \lambda_{exp} ) (nm)</th>
<th>( \Delta \lambda_{vdW}/\Delta \lambda_{exp} ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.045</td>
<td>0.150</td>
<td>30</td>
</tr>
<tr>
<td>1.5</td>
<td>0.068</td>
<td>0.228</td>
<td>30</td>
</tr>
<tr>
<td>2</td>
<td>0.091</td>
<td>0.283</td>
<td>30</td>
</tr>
<tr>
<td>3</td>
<td>0.136</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>4</td>
<td>0.182</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>5</td>
<td>0.227</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

4.3. Preliminary comparison with an experimental spectrum

We present here only a preliminary comparison of some theoretical profiles calculated by three
codes PPP, QC_FFM and ZEST for the case of spectrum 15b corresponding to a pressure of 1.5 bars.
This is illustrated on Figure 8. This figure illustrates the difficulty to fit this spectrum and the
difficulty is even higher for the cases of higher pressures. These spectra have been very recently fitted
with a genetic algorithm coupled to the PPP code and the fitting results can be found in [16].

5. Conclusion

Theoretical pure Stark profiles of the neutral helium 492 nm line calculated by four codes have
been compared for plasma conditions supposed to cover those of a corona discharge in helium with
traces of hydrogen. These conditions correspond to plasmas of singly ionized helium ions with
electron densities of \( 10^{15} \) and \( 10^{16} \) cm\(^{-3} \) and equal ions and neutral temperatures of 0.1, 0.2 and 0.4 eV.
For the lowest density, three codes are in a relative agreement: PPP, SimU and ZEST showing
comparable widths sometimes within a factor up to two with a relatively good agreement concerning
the appearance of the forbidden components (lateral components) unlike QC_FFM which
overestimates the broadening. For the highest density, the surprise comes from PPP which
overestimates in this case the broadening especially at 0.1 eV even if this discrepancy tends to
disappear for temperatures higher than 0.4 eV. This discrepancy was expected for two reasons: the
use of non-frequency collision operator instead of frequency-dependent one and the use of a
Holtmark field distribution which may not be valid. There is an overall agreement between ZEST,
SimU and QC_FFM (although the later, evidently, is not able to model any forbidden component).
For the comparisons with experimental spectra, the task was hard and only few attempts were tried.
This is due to the complexity of the spectra showing an asymmetry increasing with increasing
pressure in addition to the appearance of the forbidden components whose intensity depends on the
pressure too. Only a preliminary comparison has been presented for an illustrative purpose. Since
the time these calculations and comparisons have been done, other more recent works have been
done and will be published.

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