The development of a 1-D integrated hydro-mechanical model based on flume tests, to unravel different hydrological triggering processes of debris flows

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Abstract: Many studies, which try to analyze conditions for debris flow development, ignore the type of initiation. Therefore this paper deals with the following questions: What type of hydro-mechanical triggering mechanisms for debris flows can we distinguish in upstream channels of debris flow prone gullies? Which are the main parameters controlling the type and temporal sequence of these triggering processes and what is their influence on the meteorological thresholds for debris flow initiation? A series of laboratory experiments were carried out in a flume, 8 m long and with a width of 0.3 m, to detect the conditions for different types of triggering mechanisms. The flume experiments show a sequence of hydrological processes triggering debris flows, namely erosion and transport by intensive overland flow and by infiltrating water causing failure of channel bed material. On the basis of these experiments an integrated hydro-mechanical model was developed, which describes Hortonian and Saturation overland flow, maximum sediment transport, through flow and failure of bed material. The model was calibrated and validated using process indicator values measured during the experiments in the flume. Virtual model simulations, carried out in a schematic hypothetical source area of a catchment show that slope angle and hydraulic conductivity of the bed material determine the type and sequence of these triggering processes. It was also clearly demonstrated that the type of hydrological triggering process and the influencing geometrical and hydro-mechanical parameters may have a great influence on rainfall intensity-duration threshold curves for the start of debris flows.

Keywords: triggering of debris flows; overland flow; infiltration; laboratory experiments; modelling; rain intensity-duration threshold curves.

1 Introduction

A debris flow is one of the most dangerous types of mass movement because depending on the rheology and topography it can reach a very high speed and large run-out distance. Important study aspects are the mechanism and boundary condition of the initiation process of a debris flow, because it determines the meteorological threshold conditions and further evolution and it will provide clues for future mitigation strategies [1].

One can make different classifications of initiation mechanisms based on different viewpoints [1]. It was among others [2-3], who stressed the importance of the infiltration capacity of the soil as a key factor for either the development of shallow landslides or surficial erosion and transport of material by overland flow, that might create different types of flow like mass movements. Effective overland flow driven triggering processes are mainly concentrated in channels where high water discharges, severe erosion and transport lead to high solid concentrations generating debris flows.
[4-9]. Material is supplied to these debris flows by detachment and transport of the bed material but also through lateral erosion of the channel bed. The channel can be partly or totally blocked by landslide dams. High run off discharges eroding these landslide dams can also lead to initiation and rapid grow of debris flows ([10-12]. Landslide damming can also be initiated by rapid incision of the channel bed destabilizing the side walls [13]. With infiltrating driven triggering mechanisms, shallow landslides are generated, which may or may not transform into debris flows. This failure mechanism by infiltrating water can occur in channel beds filled with loose material [14] and on planar slopes where shallow landslides can also transform into debris flows [15-18]. The transformation of a failed mass into a debris flow is rather complex and depends on various hydro-mechanical processes related to pore pressure development and supply of abundant overland flow water further mobilizing the failed mass ([19-23].

Several authors analyzed partly the role of hydro-mechanical and morphometric factors controlling the type of initiation of debris flows. Berti [24] analyzed the hydrological factors for the generation of debris flows in typical source areas in the Italian Alps by modelling channel overland flow in the channel bed from a source area as a response to rainfall impulses. Kean [25] proposed an integrated hydro-geotechnical dynamic model to describe sediment transport by overland flow and consequently mass failure transforming into debris flow surges. Hu [26] highlighted the initial soil moisture and thus infiltration capacity as a controlling factor for the type of initiation: wet soils created mainly surficial run-off and erosion and incision, bank failure, damming and debris flow development while dry soils showed mainly infiltration and landslide failure and debris flow initiation.[1] Zhuang focused more on the slope gradient as a controlling factor for different types of initiation. Their flume studies revealed that at gentler slope gradients around 10° ± 2°, incision and bank failure is dominant, creating channel damming and dam failure, inducing debris flows. At intermediate slopes around 15° ± 3° erosion of bed material occur at high discharges. The high sediment transport capacity with high sediment concentrations is sufficient to create debris flows. At steeper slopes around 21°± 4° bed failure by infiltrating overland flow water with debris flow formation is the most dominant process.

Meteorological thresholds for the initiation of debris flows are closely related to the process of initiation. In many studies about these meteorological thresholds, no clear distinction was made between the types of triggering ([27]. The assessment of these thresholds in relation to various morphometric and geological factors was made in most cases using statistical techniques [28-30].

Until now only isolated aspects of the hydrological triggering system of debris flows has been studied. There is a need for a comprehensive frame work which gives insight in the controlling factors for the evolution of different triggering systems in upstream channels of debris flow gullies. Therefore this paper will try to give answers on the following questions:

1. What type of hydro-mechanical triggering mechanisms for debris flows can we distinguish in upstream channels of debris flow prone gullies?
2. Which are the main parameters and in what way are they controlling the type and temporal sequence of these triggering processes?
3. What is the influence of hydro-mechanical parameters and related triggering processes on the meteorological thresholds for debris flow initiation?

In order to answer these questions we have carried out a number of flume tests to detect the conditions for different types of hydro-mechanical triggering mechanisms of debris flows (Section 2). Based on the process information revealed by these experiments we will develop an integrated hydro-mechanical model describing these triggering processes (Section 3). The model will be calibrated and validated using indicator values obtained from the processes measured in the flume (Section 4). Virtual model simulations will be carried out in a schematic hypothetical source area of a catchment to make a frame work of the type and sequence of these triggering processes as a function of slope angle and the hydraulic conductivity of the bed material (Section 5). The model will also be used for sensitivity analyses to study the influence of important geometrical and hydro-mechanical parameters and the related type of initiation process on rainfall intensity-duration threshold curves, for the start of debris flows (Section 6).
2 Flume tests to reveal types of debris flow triggering

2.1 Set up of the flume experiments

A flume was designed to see whether we could simulate in an 1D framework the initiation of debris flows by different hydro-mechanical triggering mechanisms. (Figure 1). The flume has a length of 8 m and a width of 0.3 m. The material simulating the channel bed with a thickness of 0.1 m and a width of 0.3 m is positioned at a distance of 4 m from the top of the flume and has a length of 2 m. The material was brought into the flume in layers of about 2 cm and was slightly compacted (dry density see Table1). There is an outflow at a distance of 2 m from the lower end of the channel bed (Figure 1). The water is entered at the upper end of the flume with a controlled discharge, simulating run on water from an upstream area.

![Figure 1: Design of the flume test. For explanation of the parameters see text](image)

<table>
<thead>
<tr>
<th>Particle size class</th>
<th>Friction (°)</th>
<th>Density kNm⁻³</th>
<th>Hydraulic conductivity (m s⁻¹)</th>
<th>D₃₀ (mm)</th>
<th>D₅₀ (mm)</th>
<th>D₇₀ (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coarse</td>
<td>34.6</td>
<td>15.4</td>
<td>4.91E-03</td>
<td>9</td>
<td>11</td>
<td>18</td>
</tr>
<tr>
<td>Medium</td>
<td>33.7</td>
<td>16.3</td>
<td>3.28E-03</td>
<td>4</td>
<td>6</td>
<td>16</td>
</tr>
<tr>
<td>Fine</td>
<td>29.2</td>
<td>19.5</td>
<td>0.54E-03</td>
<td>0.7</td>
<td>1.6</td>
<td>8</td>
</tr>
</tbody>
</table>

Table I. Hydro-mechanical characteristics of three types of bed material, used in the flume tests. Friction means friction angle of the material in degrees. D₃₀/₅₀ means that 30/50% of the sample has a lower diameter than what is indicated in the column.

Three types of material were used in the experiments with different grain size distributions (Figure 2). We could vary the slope angle of the flume between 14° and 20°. The initial moisture content of the flume material was more or less dry. The initial moisture content is important for the infiltration capacity but since we used in the laboratory a large influx of water from above into coarse bed material, we ignored the effect of the Sorpetivity (related to the initial moisture content) on the infiltration capacity of the bed material.
Figure 2: Cumulative grain size distribution of the three bed materials, used in the flume tests

The friction of the three materials was measured with the conventional direct shear apparatus [31]. The hydraulic conductivity of saturated cylindrical soil samples of the three grain sizes was measured with a constant head gradient between the upper and lower end of the sample ([32]). Table I gives further information about the friction, hydraulic conductivity and gradient of the materials used for the experiments.

Pore pressure was measured at three places (Figure 1) at the bottom of the flume. The pore pressure sensors, type :YP4049, were produced by Yom Technology Company. The measuring range of pore pressure is from -100kPa to +100kPa.

Laser sensors (ZLDS100 ZSY Group; resolution 0.03 % FS) at three points with a spacing of 0.5 m (Figure 1) were used to monitor topographical heights, especially with the aim to monitor abrupt changes in relief due to bed failure.

In addition video-recordings were performed (Figure 1) to follow the sequence of processes in the course of the experiments. During the process of overland flow erosion, samples were taken six times for more or less steady state conditions at the outlet of the Flume (Figure 1). The discharge of water with sediments was collected in baskets during 5 seconds. The sediments were sieved, dried and weighted to measure the concentration of the fluid.

An integrated model (Section 3) for surface and sub surface flow, sediment transport and bed slope stability was developed to describe the processes in the flume, which was used later to analyze the sequence of different initiation processes at the field scale.

2.2 Observations on different types of hydrological triggering mechanisms in flume tests.

The flume tests were carried out in order to reveal different types of hydrological triggering mechanisms, which may create debris flows and to establish indicators related to these triggering processes which will be used to calibrate and validate our theoretical model (Section 4) During the flume tests with the three bed materials under different slope angles, observation were carried out by means of video images and the laser sensors. Some of the observed process indicators are given in Table II.
Grain size | Slope | Inflow l/s m$^{-1}$ | Time to run-off initiation (sec) | Time to bed failure (sec) \\
--- | --- | --- | --- | --- \\
Coarse | 20$^\circ$ | 0.18 | 402 | 411 \\
 | 18$^\circ$ | 0.22 | 103 | 110 \\
 | 16$^\circ$ | 0.29 | 63 | 72 \\
 | 15$^\circ$ | 0.40 | 73 | 82 \\
 | 14$^\circ$ | 0.41 | 59 | 69 \\
Medium | 20$^\circ$ | 0.11 | 168 | 168 \\
 | 18$^\circ$ | 0.13 | 140 | 140 \\
 | 16$^\circ$ | 0.16 | 54 | 64 \\
 | 15$^\circ$ | 0.18 | 27 | 37 \\
 | 14$^\circ$ | 0.19 | 46 | 56 \\
Fine | 20$^\circ$ | 0.03 | 30 | 40 \\
 | 18$^\circ$ | 0.06 | 220 | 230 \\
 | 16$^\circ$ | 0.09 | 90 | 100 \\
 | 15$^\circ$ | 0.10 | 110 | 120 \\
 | 14$^\circ$ | 0.11 | 102 | 112 \\

### Table II.

Observed time to overland flow and bed failure, overland flow type and failure mode in flume experiments for three types of bed material and for different bed slope angles: a) Saturation overland flow; b) Hortonian overland flow; c) slow continuous bed failure; d) rapid failure; nf: no failure.

In slope hydrology two types of overland flow can be distinguished: Saturation overland flow and Hortonian overland flow [32]. These two types could be distinguished during the different flume experiments (Table II). Saturation overland flow was characterized, after complete saturation of the soil, by a more or less spatially randomly ponding of water at the soil surface, while Hortonian overland flow, which occurs when the rainfall intensity or supply of overland flow water is larger than the infiltration capacity of the soil, showed a more concentrated continuous flow over the length of the flume bed. According to these visual indicators we could establish a boundary between Saturation overland flow and Hortonian overland flow, which in our flume tests was found in the medium grain size materials at a slope gradient of 16$^\circ$ (Table II). This could be verified with our model simulation (see below Section 4.2). For courser materials (Ks values of 4.19E-03 and 3.28E-03 m s$^{-1}$) and higher slope angles (> 16$^\circ$) the time to Saturation overland flow is immediately followed by failure or with a small delay until 9 seconds. Also one can clearly observe that the time to Saturation overland flow (and thus failure) is decreasing with decreasing slope angle (Table II).

Hortonian overland flow [32] was initiated in most cases on the finer sediments, which is ascribed to the lower infiltration capacity (Ks = 0.54E-03 m s$^{-1}$). Bed failure in this case occurred a certain time after the start of Hortonian overland flow with a time lag ranging between 35 and 160 seconds (Table II), because in this case, due to the lower percolation rate it takes time to bring the groundwater in the bed material to a critical failure level.

Bed failure initiation is controlled by the bed gradient and the internal friction of the material and occurred in our experiments on slopes of approximately 16 degrees and higher. At lower slope angles no bed failure occurred (nf in Table II) and sediment delivery occurred only by overland flow erosion.

The medium and course materials show bed failure characterized by slow movements over the total depth combined with fast surficial entrainment of grains by saturated overland flow.

Movement of bed material is slow and continuous or sometimes intermittent showing a surging
pattern (Table II). Instead of the slow and more flow like movements observed for the medium and coarse sediments, failure of the fine sediments occurred suddenly with a very rapid surge of more or less coherent blocks followed by fluidization, (Table II).

Sediment transport by overland flow on these steep slopes reached volumetric concentrations between 0.46 and 0.64, which is characteristic for debris flows.

We can conclude on the basis of these observations that the flume tests carried out with the three materials revealed three types of processes, which created debris flows in these range of slopes gradients namely debris flow Initiation by Hortonian Overland flow Erosion (RhE-I), Saturation Overland flow Erosion (RsE-I) and by Bed Failure (BF-I). The occurrence and sequence of these processes seems to be controlled by slope gradient and hydraulic conductivity of the bed sediment. Figure 3 gives a schematic overview of these process types.

3 Integrated model (1D) for debris flow initiation in upstream channels

The flume tests observations brought us to the concept of the triggering of debris flows caused by Hortonian and Saturation overland flow initiating surficial erosion of bed material. Bed failure and entrainment of material was initiated by infiltration and subsurface flow leading to instability.

First we have to simulate the hydrological component of the triggering mechanisms of debris flows. For that we need the mass balance equation for overland (Eq.(1a)) and through flow (Eq.(1b)), which is given by:

\[
\frac{\partial q_f}{\partial x} + \frac{\partial h_f}{\partial t} = B_1 \tag{1a}
\]

\[
\frac{\partial q_s}{\partial x} + \frac{\partial h_s}{\partial t} = B_2 \tag{1b}
\]

where \( q_f \) is overland flow discharge per unit width (m\(^3\)m\(^{-1}\)s\(^{-1}\)); \( q_s \) is subsurface discharge per unit width (m\(^3\)m\(^{-1}\)s\(^{-1}\)); \( h_f \) is thickness of overland flow (m); \( h_s \) (m) is thickness of subsurface flow, \( \partial x \) (m) is distance along the slope \( \partial t \) is the time (s) and \( B_1 \) 2 are terms (m s\(^{-1}\)) describing the inflow or outflow of water from the flow system, which is defined as follows:

\[
B_1 = \begin{bmatrix} r - l_f(a) \\ 0 - l_f(b) \end{bmatrix} \tag{2a}
\]

\[
B_2 = i_f \tag{2b}
\]

where \( r \) (m s\(^{-1}\)) describes the external input of rain into and \( i_f \) (m s\(^{-1}\)) the outflow of water by infiltration out of the overland flow system (Eq. (2a)) (see also Figure 1). When there is no supply of rain, like in our flume experiments: \( r=0 \). In the case of subsurface flow \( i_f \) in Eq.(2b) is considered now as an inflow term of the subsurface flow system. If \( h_s/\partial t \) is larger than the infiltration capacity \( K_s \) (m s\(^{-1}\)) of the bed material the latter one is the limiting factor. Therefore the infiltration term \( i_f \) of
Eq. (2) is the minimum (min) value of the infiltration capacity $K_s$ (m s$^{-1}$) and the current water depth ($h$), which can infiltrate in one time step $\Delta t$ into the bed material:

$$i_f = \min(K_s, h/\Delta t)$$ (3)

We introduce here a general momentum equation for the water flow processes [33]:

$$h_f = \alpha_f q_f^{\beta_f}$$ (4a)

$$h_s = \alpha_s q_s^{\beta_s}$$ (4b)

For turbulent overland flow the parameters $\alpha$ and $\beta$ in Eq.(4a) can be defined as follows:

$$\alpha_f = \left( \frac{n}{S_0} \right)^{0.6}$$ and $\beta_f = 0.6$ (5)

where $n$ is Manning’s $n$ and $S_0$ the slope gradient of the bed material.

For subsurface flow we can write according to Darcy’s law:

$$q_s = K_s \sin \theta h_s \rightarrow h_s = \frac{1}{K_s \sin \theta} q_s$$ (6)

where $q_s$ is the amount of subsurface flow water per unit width (m$^3$ m$^{-1}$ s$^{-1}$); $\theta$ is slope angle (degrees) and $h_s$ is the height of the flowing water component in the soil matrix (m). By comparing Eq.(6) with the general momentum Eq. (4b) we can define the parameters $\alpha$ and $\beta$ for subsurface flow:

$$\alpha_s = \frac{1}{K_s \sin \theta}$$ and $\beta_s = 1$ (7)

A combination of the mass balance Eq.(1) with Eq.(4) delivers an expression for overland flow or subsurface flow discharge ($q_f, q_s$) [33]:

$$\frac{\partial q_f}{\partial x} + \alpha_f \beta_f q_f^{(\beta_f - 1)} \frac{\partial q_f}{\partial t} = B_1$$ (8a)

$$\frac{\partial q_s}{\partial x} + \alpha_s \beta_s q_s^{(\beta_s - 1)} \frac{\partial q_s}{\partial t} = B_2$$ (8b)

The 1D model is implemented in a fixed Eulerian frame where the variation in water flow variables is described at fixed coordinate points at a distance $\Delta x$ along the slope as a function of time step $\Delta t$. A numerical solution for Eq.(8) is given by [33]:

$$q_{x+1}^{t+1} = \frac{\Delta t}{\Delta x} \left[ q_{x+1}^{t+1} + \alpha q_{x+1}^{t+1} \left( q_{x+2}^{t+1} + q_{x}^{t+1} \right)^{\beta - 1} + \Delta t \left( \frac{q_{x+1}^{t+1} + q_{x}^{t+1}}{2} \right)^{\beta - 1} \right]$$ (9)

where $q, \alpha$ and $\beta$ should be read as $q_{f,s}, \alpha_{f,s}$ and $\beta_{f,s}$ respectively.

To simulate the initiation of debris flows by mass failure we used the equation for the infinite slope equilibrium model [31], which is the trigger for failure:

$$F = \frac{(\gamma_s \cos \theta - p) \tan \phi}{\gamma_w}$$ (10a)

$$p = \gamma_w h_s \cos \theta$$ (10b)

where $F$ is the safety factor; failure occurs when $F=1$; $\gamma_s$ and $\gamma_w$ are the saturated bulk density of the material and water respectively; $\phi$ is friction angle of the material; $z$ and $h_s$ are the thickness of the soil and the height of the groundwater layer respectively. $h_s$ can be solved with Eq. (9) and Eq.(6) respectively.

The overall stability of the bed material expressed with the safety factor ($F$) for the infinite slope model is calculated as an average of the safety factor of the different nodes. The inflow of water into the flume is coming from upstream and therefore the pore pressure gradient is decreasing downstream. This means that the safety factor is always increasing downstream and therefore the average approach of the safety factor over the length of the sample in the flume seems a reasonable approximation of the overall safety factor.
For estimating the transport capacity on steep slopes Rickenmann [34-35] proposed a bedload transport equation based on a shear stress approach, where discharge, bed slope gradient and material grading are used as parameters to characterize flow hydraulics.

For steeper slopes, in the range of 0.03<S<0.2 (1.7°-11.3°) Rickenmann [34] performed a regression analysis with the steep flume data on bed load transport obtained at ETH Zurich that resulted in the equation:

\[ q_{\text{solid}} = \frac{12.6}{(d_s-1)^{1.2}} \left( \frac{D_{90}}{D_{30}} \right)^{0.2} (q_f - q_c) S^2 \]  

(11)

where \( D_{90} \) and \( D_{30} \) are grain sizes at which 90% and 30% respectively by weight of the material are finer; \( d_s \) is the mass density of the solids and \( S \) is the slope gradient and \( q_c \) is the critical flow discharge for bed load entrainment. The experimental slopes were in the range of 0.03>S>0.20. (1.7°-11.3°) and the \( D_{90} \) of the material ranged between 0.9> and 2 cm and \( D_{30} \) between 0.06 and 1 cm with inflow rates of 10-30 l/s In the section below we will calibrate Eq.(11) for the steeper slopes in our flumes.

The integrated model developed in this section is able to describe the different types of hydro-mechanical triggering mechanisms for debris flows. It delivers us the physical parameters, which controls these processes, which will be applied in our virtual simulations in Section 5 and 6.

In the next section (4) we will calibrate our model on some process indicator values obtained from our flume tests.

4. Calibration and validation of the theoretical model on the basis of flume test results

We will use here a number of process indicator values measured during the flume experiments to calibrate and validate the outcomes of our theoretical model. These are: Saturation or Hortonian overland flow, time to overland flow, maximum pore pressure, time to bed failure and solid concentration by overland flow erosion. Hortonian overland flow and the time to Hortonian overland flow in the model is declared when surface water \( h_f \) reaches the lower end of the bed material while the bed material is still not saturated (\( h_s < Z_s \)). Saturation overland flow and the time towards it, is declared when \( h_s = Z_s \) over the entire bed. Pore pressure is calculated each time step according to Eq (10b). The discharge of \( h_f + h_s \) is reported each time step at the end of the flume. Bed failure is declared as said before when the average Safety factor \( F \) over the bed length reaches the value of 1.

For the flume simulations the distance between the nodes (\( \Delta x \)) was 0.1 m and the time interval (\( \Delta t \)) was 0.2 seconds.
Figure 4. Observed and calculated time to Saturation overland flow (black symbols) and Hortonian
overland flow (open symbols)

Figure 4 shows the relation between observed and calculated time to overland flow for the
different flume tests. There is a moderate 1:1 correlation between observed and predicted time to
overland flow for the medium and coarse sediments and for the fine sediments, showing Hortonian
overland flow, there is no correlation at all. However the model was able to predict the type of
overland flow according to what was observed during the flume tests (see Table II).

Despite the malfunctioning of some pore pressure sensors we were able to make a 1:1
comparison between the average maximum measured pore pressure for the three sensors (Figure 1)
and the average calculated maximum pore pressure (Figure 5).

Fig 5. Maximum pore pressure measured during flume tests in relation to calculated pore pressures.

The Figure shows that in many cases there is a slight overestimation of the calculated pore
pressure. Time series of measured pore pressure of the three sensors compared to modelled
temporal pore pressure development showed that in most cases the onset towards maximum pore
pressure for the three sensors is more irregular compared to the calculated development of the pore
pressures (Figure 6). This can be ascribed to the heterogeneity of the sediment or (and) the
imperfect response of the sensors.
Fig 6 Example of the rise in pore pressure (measured/calculated) due to infiltration of run-on water in the bed material (Test: Medium grain size 20°).

In relation to pore pressure development we compared the time to failure for the different test runs on the different materials. Since the time towards average maximum calculated and measured pore pressure coincided more or less, one would expect also corresponding calculated and measured failure times. Table II and Figure 7 show that the match between observed and calculated failure time is reasonable except for two outliers (coarse-20°; fine-18°). Further we can observe that the calculated time to failure is underestimated for the coarse material and overestimated for practically all the tests on the medium and fine materials. The deviations between calculated and observed values must be ascribed to heterogeneity of the material, deviating friction values, and incorrect assessment of the overall safety factor.

We calibrated also the parameters of the Rickenmann [35] equation, (Eq.11) on our flume tests, which were carried out on slopes ranging between 0.25>S>0.36 (14°-20°), with grain sizes for 0.9>d90>2 and 0.05>d30>1 cm and with flow rates 0.5>q>15 L s^{-1} m^{-1}. Figure 8 shows the best linear fit between q_{solid}/q_{f} and (d_{90}/d_{30})^{0.2}S^{2}, which delivered the following modified equation for slopes between 14° and 20°:

\[
q_{\text{solid}} = 7.28 \left( \frac{d_{90}}{d_{30}} \right)^{0.2} q_{f} S^{2}
\]  

(12a)
which gives for $d=2.6$:

$$q_{solid} = \frac{15.44}{(d-1)^{1.6}} \left( \frac{D_{90}}{D_{30}} \right)^{0.2} q_f S^2$$

(12b)

Figure 8. Calibration of Rickenmann’s bedload equation for steeper slopes in our flume tests between 14 and 20 degrees.

The calibration revealed that $q_c$ in Eq.(11) becomes zero or practical zero in Eq.(12). At slopes larger than 15° the down slope component of the grain weight may reduce the critical shear stress $\tau_c$ which in our case obviously reduced to nearly zero.

We may conclude that the model is able to predict in a reasonable way essential process indicators for different hydrological triggering processes of debris flows in upstream channels. In the next section we will apply the model on the field scale to predict hydro-mechanical triggering patterns for debris flows as a function of the hydrological conductivity of the bed material and the channel slope gradient.

5. Hydro-mechanical triggering patterns for debris flows in relation to hydrologic conductivity of bed materials and channel gradient

5.1. The design of a schematic source area at the field scale.

First we will design a virtual landscape of a potential debris flow source area where our model can be applied to analyze the influence of terrain parameters on the type of triggering mechanisms (Section 5.2) and the meteorological thresholds of debris flows (Section 6).

Figure 9 shows this virtual source area, which is linked to an upstream channel filled with bed material receiving surface water from the surrounding slopes to initiate a potential debris flow. This geomorphological setting resembles more or less the source areas described among others by Coe [7] and Berti [24]. The upstream area of our hypothetical catchment has a radius $R$. The channel is further surrounded by lateral slopes with a length $L$. The length of the channel bed is $L_x$, the width $W$ and the slope angle is $\theta$. The hydraulic conductivity of the bed material is $K_s$, the porosity $\text{Por}$ and the friction angle $\phi$. (Figure 9).
Figure 9: Morphometric and hydro-mechanical parameters, which were used for model simulations of debris flow initiation. For an explanation see Table 3 and text. D90/D30: 90% and 30% lower than grainsize D90 and D30 respectively: $\phi$: friction angle; $K_s$: hydraulic conductivity; Por: porosity; $Z_s$: depth of material; $\theta$: slope angle, $q_{up}$: water that flows into the upper end of the channel bed; $R$: radius of source area above the channel; $L_x$ and $W$: length and width of the channel bed; $L$: length of lateral contributing slope; latin: lateral inflow of water to the channel; CN: curve number value for the soil hydrological and land use characteristics of the contributing slopes.

The sink term $B$ in (1) and (8) is now adapted to the field scene and given by:

$$B = 2l_{\text{atin}} + r - i_f$$

(13)

where $l_{\text{atin}}$ (m s$^{-1}$) is the lateral inflow of overland flow water from the slopes along the channel (Figure 9), $r$ direct rain intensity input to the channel bed and $i_f$ infiltration rate into the bed (see Eq.(3)). The lateral inflow is calculated for these sensitivity analyses in a simple way, assuming steady state conditions in the mass balance equation for overland flow:

$$l_{\text{atin}} = \frac{r_{cn} L}{W}$$

(14)

$r_{cn}$ (m/s) is calculated using the Curve Number method [36], $L$ is the length of the lateral slope and $W$ the width of the channel (see Figure 9). In our simulations we selected overland flow supplying slopes with soils with moderate to slow infiltration rates and a poor condition grass cover, which corresponds to a Curve Number(CN) of about 80. The CN number, reflecting the hydrological soil characteristics, land use and antecedent soil moisture conditions that we can expect in high mountainous areas, was chosen arbitrarily and was kept constant in our simulations.

The overland flow water that flows into the upper end of the channel bed, which is given by $q_{up}$ (m$^2$ s$^{-1}$) (Figure 9)

$$q_{up} = \frac{r_{cn} 0.5 \pi R^2 \cos \theta}{W}$$

(15)

5.2 The influence of the hydraulic conductivity ($K_s$) and slope ($\theta$) of the channel bed on the type and sequence of hydrologic triggering processes for debris flows

In the flume we could observe the effect of slope angle and hydraulic conductivity on the type and sequence of triggering processes, which may lead to the initiation of debris flows. In this section we will investigate with our theoretical model the effect of these two factors at the catchment scale. The values of the other factors used in our model simulations are shown in bold as default parametric values ($Z_s, \phi, W, L_x, Por, R, L, n$ bed) in Table III (see also Figure 9).
Table III. Default values (bold italic) and maximum and minimum values of input parameters for Overland flow Erosion (RE-I) and Bed Failure (BF-I) triggering debris flows. $K_s$: saturated hydraulic conductivity; $Z_s$: thickness of bed material; $\phi$: friction angle of material; $\theta$: slope angle of channel bed; $W$ and $L_x$: width and length of channel bed respectively; $P_{or}$: available volumetric pore space; $R$: radius of source area; $L$: length of lateral slopes; $n$: Manning’s $n$ of bed material.

Table IV gives the range in $K_s$ values (first row) and bed slope angles (first column), which were used in our simulations to study the effect of these parameters on the hydro-mechanical process development at the catchment scale. For these simulations two rain scenarios were used with an intensity of 80 mm (Table IVa) and 40 mm per hour (Table IVb) respectively. The Tables show domains with different shades of gray with various combinations of hydro-mechanical triggering processes. In the white sections no debris flow initiation is expected to develop in the source area because of a too low sediment concentration of the overland flow. Table IVa shows that in the domain $\theta=28^\circ-20^\circ$ and $K_s=0.001-0.005$ m s$^{-1}$, the debris flow is initiated in the first stage by Hortonian overland flow erosion ($R_h$E-I). The overland flow discharge reaches a steady state after a certain relatively short time. During the steady state groundwater will rise by infiltration of run-on water until failure of the bed material, which happens between 1.7 and 11.2 minutes depending on the slope $\theta$ and $K_s$. In Table IVa we see a dramatic drop in discharge between slopes with $K_s=0.001$ and 0.005. The last $K_s$-value reaches a significant boundary which determines whether or not a debris flow can be initiated by Hortonian overland flow transport.
<table>
<thead>
<tr>
<th>80 mm Ks</th>
<th>0.001 m s⁻¹</th>
<th>0.005 m s⁻¹</th>
<th>0.01 m s⁻¹</th>
<th>0.1 m s⁻¹</th>
<th>Concent l l⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>Slope</td>
<td>Initiat proc.</td>
<td>Time min.</td>
<td>Dischar l s m⁻¹</td>
<td>Time min.</td>
<td>Dischar l s m⁻¹</td>
</tr>
<tr>
<td>degrees</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>28</td>
<td>Rₘ,E-I</td>
<td>1.0</td>
<td>912</td>
<td>1.3</td>
<td>139</td>
</tr>
<tr>
<td></td>
<td>BF-I</td>
<td>5.4</td>
<td>1.7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>24</td>
<td>Rₘ,E-I</td>
<td>1.0</td>
<td>783</td>
<td>1.3</td>
<td>119</td>
</tr>
<tr>
<td></td>
<td>BF-I</td>
<td>8.4</td>
<td>2.3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>Rₘ,E-I</td>
<td>1.1</td>
<td>683</td>
<td>1.4</td>
<td>104</td>
</tr>
<tr>
<td></td>
<td>BF-I</td>
<td>11.2</td>
<td>2.9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>16</td>
<td>Rₘ,E-I</td>
<td>1.1</td>
<td>606</td>
<td>1.5</td>
<td>92</td>
</tr>
<tr>
<td></td>
<td>Rₘ,E-I</td>
<td>14.2</td>
<td>1.5</td>
<td>732</td>
<td>3.7</td>
</tr>
<tr>
<td>12</td>
<td>Rₘ,E-I</td>
<td>1.2</td>
<td>550</td>
<td>1.5</td>
<td>83</td>
</tr>
<tr>
<td></td>
<td>Rₘ,E-I</td>
<td>14.8</td>
<td>3.9</td>
<td>665</td>
<td>3.8</td>
</tr>
</tbody>
</table>

414
415

a
It is confirmed by Table IVb with a lower rain input (40 mm) where at $K_s \geq 0.005$, no initiation by Hortonian overland flow is possible anymore.

Going back to Table IV-a: in the domain $\theta = 16^\circ-12^\circ$ and $K_s = 0.001-0.005 \text{ m/s}$ slope failure does not occur. The debris flow is initiated by overland flow. First by Hortonian overland flow and later when the groundwater has reached the surface by Saturation overland flow. Discharge is relatively low when there is Hortonian overland flow, while obviously discharge dramatically increases at Saturation overland flow. However due to the lower slope angles, the volumetric sediment concentration is low ($0.21$ at $16^\circ$ and $0.13$ at $12^\circ$, Table IV-a last column), which means the flow changes from a hyper concentrated flow into a water flood with conventional suspended load and bed load.

At higher conductivities in the domain $K_s = 0.01-0.1 \text{ m/s}$ and $\theta = 28^\circ-20^\circ$, bed failure seems the most dominant process (Table IVa). Due to the larger $K_s$ values, infiltration into the bed is more important than overland flow discharge. The bed material turns out to be partly saturated in the upper part due to the larger upstream inflow, creating partly Saturation overland flow and Hortonian overland flow. However within one minute after the run off discharge reached the lower end of the bed, failure of the bed material occurred already. Therefore the contribution of overland flow to the transport of debris by overland flow can be ignored.
In the domain $K_s=0.01-0.1 \, \text{m/s}$ and lower slope gradients ($\theta=16^\circ-12^\circ$) there is no slope failure but only Saturation overland flow, (Table IVa) with low sediment concentrations in most cases not enough to call it a debris flow.

Table IV-b shows the simulation results with an intensity of 40 mm per hour. The domains with a specific combination of hydro-mechanical triggers still exist. There is only a shift of the boundary for the $K_s$-values with no Hortonian overland flow ($>0.005 \, \text{m/s}$) to the left. The Tables IVa and b show a decrease in overland flow discharge and increase in time to bed failure with a decreasing slope angle. Around 16 degrees the channel bed is stable but still steep enough to have transport capacities with concentrations in the domain of a hyper concentrated flow. These are induced by Hortonian and Saturation overland flow at lower $K_s$ values and only Saturation overland flow at higher $K_s$ values. At lower slope angles (see slopes around 12 degrees) sediment concentrations are too low to call it a debris flow. Table V gives a summary of the type and sequence of initiation processes related to different $K_s$ and slope angle values.

<table>
<thead>
<tr>
<th>$40 \text{mm}$</th>
<th>$K_s$ values</th>
<th>$0.001 , \text{m/s}^{-1}$</th>
<th>$0.005 , \text{m/s}^{-1}$</th>
<th>$0.01 , \text{m/s}^{-1}$</th>
<th>$0.05 , \text{m/s}^{-1}$</th>
<th>$0.1 , \text{m/s}^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gradient</td>
<td>Flow type</td>
<td>$Initiation \ process$</td>
<td>$Initiation \ process$</td>
<td>$Initiation \ process$</td>
<td>$Initiation \ process$</td>
<td>$Initiation \ process$</td>
</tr>
<tr>
<td>$28^\circ$</td>
<td>Debris flow</td>
<td>$t1$: Hortonian overland flow</td>
<td>$t1$: Bed failure</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$24^\circ$</td>
<td>Debris flow</td>
<td>$t1$: Hortonian overland flow</td>
<td>$t2$: Saturation overland flow</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$20^\circ$</td>
<td>Hyper concentrated flow</td>
<td>$t1$: Hortonian overland flow</td>
<td>$t2$: Saturation overland flow</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$16^\circ$</td>
<td>No debris flow</td>
<td>$t1$: Hortonian overland flow</td>
<td>$t2$: Saturation overland flow</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$12^\circ$</td>
<td>No debris flow</td>
<td>$t2$: Saturation overland flow</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table V: Sequence of different initiation processes for debris (hyper concentrated) flows in relation to the hydraulic conductivity and slope of the channel bed material. Simulated rain intensity is 40 mm.

We designed a framework, which gives insight in what kind of debris flow initiation can be expected for a given slope gradient and hydraulic conductivity of the material. In the next section we will give an impression how different hydro-mechanical parameters of triggering processes can influence meteorological thresholds for debris flows.
6. Sensitivity analyses for parameters influencing the rain Intensity-Duration (I-D) threshold curves for different initiation processes of debris flows

In the foregoing we revealed the influence of $K_s$ and bed slope gradient on the sequence of processes mechanisms involved in the initiation of debris flows. We want to investigate here the effect of the other parameters (including $K_s$ and slope gradient) on rainfall thresholds in terms of Intensity Duration (I-D) curves for the triggering of debris flows by two main process mechanism: initiation by Hortonian overland flow ($R_{E-I}$) and bed failure ($BF-I$). As we have seen in Table IV and V, debris flow initiation by Saturation overland flow ($R_{S-E-I}$) can only take place around 16 degrees At lower slope angles sediment concentrations are too low to call it a debris flow (Table IV). At higher slope angles we have bed failure before Saturation overland flow can take place.

Figure 10 shows the effect of different parameters on the I-D curves for debris flows initiated by Hortonian overland flow. The intensity and duration value of a rain event which creates overland flow that just reaches the end of the channel bed with a sediment concentration of $>0.2$, is defined by us as a threshold rain event for debris flow initiation. The intensity and duration values for a variety of different critical rain events were plotted in a graph with on the y-axis the intensity and on x-axis the duration. In this way an Intensity Duration (ID) curve can be constructed. Table III gives an overview of the range of the different parameters and the default values (in bold italic), which were used in the simulation and which give a realistic representation of geometric and geotechnical parameters for source area conditions. The threshold curves for debris flow initiation by Hortonian overland flow are shown in Figure 10. In this figure the threshold curves, which are constructed, using the default values given in table III, are depicted with open rectangular markers. They are equal in all the sub-figures. This enables one to compare for the different parameters the difference between the ultimate curves and the default curve. For each selected parametric value there is an ultimate minimum rain intensity below which not enough overland flow and thus a debris flow can be initiated, irrespective
Figure 10. I-D curves for debris flow initiation by Hortonian overland flow in relation to different geometrical and hydrological parameters. For the definition of parameters see Table III.

The most obvious selected parameter for overland flow initiation is the hydraulic conductivity $K_s$. Other parameters are related to geometry of the source area (see Figure 6) like length of the bed $L_x$, roughness $n$, and width $W$. The simulations show that at intensities below this critical dotted line the overland flow water never reach the lower end of the bed due to a too high infiltration rate on its pathway compared to the supplied amount of water (direct rain input and surrounding overland flow) and finally bed failure may be the primary triggering process.
lateral slopes along the channel \((L)\), radius of the upstream area of the channel \((R)\) Length \((Lx)\) and width \((W)\) of the channel bed, channel bed gradient \((\theta)\) and further Manning’s \(n\) of the bed material.

We saw in the forgoing that Hortonian overland flow plays a dominant role for \(Ks\) values < 0.005 m s\(^{-1}\). Figure 10 a shows the influence of the \(Ks\) value on the I-D threshold curves for run off erosion initiation \((R\&E-I)\). The range of \(Ks\) values is chosen between 0.0005 and 0.005 m s\(^{-1}\). The Figure shows that for \(Ks\) values lower than 0.001 m s\(^{-1}\) there is nearly no effect of \(Ks\) on the position of the I-D curve but there is a difference in the minimum intensity values (dotted lines) below which no debris flow can occur. A slight difference can be observed for lower intensities (<60 mm hr\(^{-1}\)). Higher \(Ks\) values (> 0.001 m s\(^{-1}\)) have a larger influence on the I-D curves. (Figure 10a)

The simulations show that the scale of the source area and lateral slopes \((R\&L)\), the length of the river bed \((Lx)\) and the width of the bed \((W)\) have the largest effect on the position of the threshold curve for the initiation of debris flow by Hortonian overland flow (Figure 10 b,d,f respectively). The threshold curves are less sensible for the effect of the slope gradient \(\theta\) and Manning’s \(n\) of the bed material (Figure 10 c,e respectively).
Figure 11 shows the influence of the different geotechnical and geometrical factors on the threshold values for the triggering of debris flows by bed failure. The range in $K_s$ values for which bed failure (BF-I) is the dominant process is chosen between 0.001 and 0.1 m s$^{-1}$ with a default value of 0.01 m s$^{-1}$. The effect of the selected range in geometric values $R, L, M, W, \phi$, and $Z_s$ (Figure 11 b,d,f,g,h respectively) seems to be more or less the same. Less effect has the porosity $Por$ of the bed material and the $\phi$ values (Figure 8 c,e respectively). No effect has the hydraulic conductivity $K_s$ (Figure 8a), which is related to the simplicity of the model describing instantaneous downward percolation for these high permeable bed materials. Interesting is to see that at lower $K_s$ values (around 0.001 m s$^{-1}$) and higher rain intensities the rate of groundwater storage and therefore the critical duration for failure is nearly the same (Figure 8a).

The I-D curves obtained by our simulations suggest that the duration range is strongly influenced by the type of initiation. Debris flows initiated by Hortonian overland flow seems to be initiated within several minutes while debris flow initiated by bed failure within one to two hours. I-D curves find in the literature give threshold curves with a larger duration range of one to several hours. The relative quick response to debris flow initiation can be explained by the large effect we give in our simulations to the contributing slopes with sparse vegetation and low infiltration rates, which in other areas may be minor due to higher infiltration rates of denser vegetation and lower overland flow rates. The use of the curve number method also explains the quick response to initiation; because it does not take into account the effect of the initial moisture content which for dry soils gives larger infiltration rates and time to ponding in the first period of a rain event. It also does not simulate the travel time towards the channel. The relative quick response for channel bed failure initiation was also found by Berti [24] dealing with nearly impermeable rock slopes in the source area.
Fig 12. Ultimate variation in I-D curves as a result of our sensitivity analyzes compared to the maximum difference in I-D curves found world wide.

Fig 12 compares two extreme I-D curves [38-39] and one in between the two [37] obtained world-wide with the two extreme curves produced in our simulation. The minimum curve in our simulation is related to the maximum channel slope (28°) and the maximum threshold curve is related to the largest length (Lx) of the channel bed. Fig.12 shows that a simple variation of parameters for the initiation of debris flows in channel beds of source areas, gives already a significant range in variation compared to the range in threshold values for debris flows worldwide. The Figure shows that, for reasons given above, our simulated curves are positioned in the lower part of the domain covered by all the curves obtained from different parts of the world.

We have shown in this section that the I-D curves for debris flows triggered by over land flow and bed failure are especially sensitive to the morphometric parameters of the source area and less sensitive to the hydro-mechanical parameters. The I-D curves for debris flows, triggered by the overland flow process are more sensitive to these parameters than the I-D curves related to the bed failure triggering process (compare Figure 10 and 11). The sensitivity of these curves for these process parameters cover a range, which is quite significant compared with the ultimate range of I-D curves found world wide.
7. Discussion

This paper unraveled the effect of different hydro-mechanical processes on the initiation of debris flows. It is focused on the initiation in channels and it gives a detailed insight in the influence of different hydro-mechanical process mechanisms in the source area on the type of debris flow initiation. It shows how the hydrologic conductivity \( (K_s) \) and slope gradient \( (\theta) \) determine the sequence of various process mechanisms.

Our simulations suggest that the type of initiation and related factors have also a clear influence on the values of the I-D curve as shown in Fig 10 and 11. These I-D curves, determined by our two simulated process mechanisms, Hortonian overland flow and bed failure show a relative quick response of debris flow initiation compared to what is generally provided by the literature. Our calculations were focused on the initiation of debris flows in the source area in channel beds surrounded by slopes with scarce vegetation and rather impermeable soils. A quick response (within one hour) was also observed by Berti [24] where, as in our simulations, debris flows were initiated in the source area by the dominant effect of run-on water to the channel delivered by a bare impermeable catchment upstream.

The assessment of rainfall threshold values for debris flow initiation are based in most cases on statistical empirical approaches using large data sets without detailed knowledge of the different triggering processes and its influencing factors [2, 29]. Our quantitative approach to analyze the threshold conditions for debris flow initiation gives a more detailed insight in the effect of different parameters than the indicative parameters used in statistical techniques. Apart from the fact that no distinction is made in the mechanism of initiation, important morphometric characteristics, like channel width, slope length thickness of bed material etc, are ignored in most cases. As a consequence the prediction of the probability debris flow initiation on the basis of rainfall for individual catchments can be very inaccurate. Further investigations must reveal the accuracy of both approaches to predict the initiation of debris flows.

The CN value, which we used in the simulation of overland flow on the contributing slopes, reflects in a lumped way the dynamic soil and land use characteristics. Especially the amount of storage of water before the time to ponding and thus the estimate of the total overland flow production of a rain event can be rather inaccurate especially for rain events with shorter durations. The use of a more detailed infiltration model incorporating the effect of the initial moisture content will give better predictions. However in this paper we did not unravel in detail the effect of these soil and land use characteristics on threshold conditions for debris flow initiation but uses a constant CN value as input for the run-on simulation to the channel bed. Initial moisture conditions in the channel bed, which will affect the permeability and hence the boundary conditions for the initiation of overland flow were not considered either in this paper. The effect of the initial moisture content of the bed material is minor due to the large amounts of influx of water and the relative coarse material in the channel bed.

In this paper we mentioned the transport capacity of overland flow as a limiting factor for the initiation of debris flows. On slopes (\(<16^\circ\) ) sediment concentrations are too low (\(<0.2\)) to call it a debris or hyper concentrated flow. For these lower channel gradients we did not consider the effect of the delivery of extra material by side wall collapses and failure of landslide dams [1, 13], which may lead downstream to a rapid loading of the fluid and an instantaneous transformation into a debris flow.

The initiation of debris flows by bed failure is also more complex since it depends on certain boundary conditions related to pore pressure development at failure and a large amount of run off water, which must be supplied during failure to keep the material moving [20, 22, 23]. It is interesting to analyze the potential in development further downstream of debris flows triggered by bed failure (BF-I) with high solid concentrations. On steeper slopes failure of the bed material occurs under lower groundwater heights \( (h_s) \) and therefore after failure much additional overland flow water is needed to maintain the movement further down slope. Important is also the
mechanism of erosion and erosive power of both types of debris flows further downstream in order to grow to a mature debris flow [6, 40-43].

8. Conclusions

We could distinguish in our flume tests three types of hydro-mechanical processes which may trigger debris flows in channel beds of first order source areas. These are erosion and transport by intensive Horton overland flow (RO-I), Saturation overland flow (RO-I) and by infiltrating water causing failure of channel bed material (BF-I). On the basis of these flume tests an integrated hydro-mechanical model was developed, which was calibrated and validated with a number of process indicators measured during the flume tests. We were able to assess by means of this model the influence of important parameters on the mode of debris flow initiation. The hydraulic conductivity of the bed sediments is an important factor controlling the type and sequence of processes triggering debris flows. At lower Ks values Hortonian overland will be the first process to start debris flows followed by bed failure or Saturation overland flow. At higher Ks values triggering by Hortonian overland flow is not possible anymore in this relatively coarse bed material and triggering by bed failure will be the dominant process if the slope gradient is steep enough (>16°).

Therefore the slope gradient of the channel bed is a second important factor controlling the type of hydo-mechanical triggering. On gentler slopes which remain stable under saturated conditions, Saturation overland flow might create debris flows if slope gradient is not too gentle and therefore sediment concentration too low to call it a debris flow.

We further analyzed also the effect of different important morphometric and hydro-mechanical parameters on meteorological thresholds for triggering debris flows by overland flow or bed failure respectively. With respect to overland flow triggering, the morphometric factors related to the size of the source area and width and length of the channel bed have the largest influence on the position of the I-D curves. Meteorological thresholds for bed failure triggering are also sensitive to morphometric parameters while the hydro mechanical parameters have relative less influence on these threshold values.

Individual contribution of authors: Van Asch, Yu and Hu conceived and designed the experiments; Yu performed the hydro-mechanical measurements on the materials and performed the experiments; Van Asch and Yu analyzed the data; Van Asch did the modelling and wrote the paper.”

References


