

1 Article

2 Weld Magnification Factor Approach in Cruciform 3 Joints Considering Post Welding Cooling Medium 4 and Weld Size

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11 **Abstract:** The objective of this research is to develop an experimental-theoretical analysis about the
12 influence of the cooling medium and the geometry of the welding bead profile in fatigue life and
13 associated parameters with structural integrity of welded joints. A welded joint with cruciform
14 geometry is considered using SMAW, plates in structural steel ASTM A36 HR of 8 mm of
15 thickness and E6013 electrode input. A three-dimensional computational model of the cruciform
16 joint was created using the finite element method. For this model, the surface undulation of the
17 cord and differentiation in the mechanical properties of the fusion zone were considered, the
18 heat-affected zone (HAZ) and base material, respectively. In addition, an initial residual stress
19 field which was established experimentally was considered. The results were a set of analytical
20 expressions for the weld magnification factor M_k . It was found that values for the latter decrease
21 markedly in function of the intensity of the cooling medium used in the post welding cooling
22 phase, mainly due to the effect of the residual compressive stresses. The obtained models of
23 behavior of the weld magnification factor are compared with the results from other researchers
24 with some small differences, mainly due to the inclusion of the cooling effect of the post weld and
25 the variation of the leg of the weld bead. The obtained analytical equations in the present research
26 for M_k can be used in management models of life and structural integrity for this type of welded
27 joint.

28 **Keywords:** cruciform joint; fatigue; semi-elliptical crack; cooling; weld magnification factor;
29 fracture mechanics

31 1. Introduction

32 One of the common failure phenomena in structural engineering materials is fatigue failure. This is
33 associated with certain flaws in the material or any geometric detail which, after a certain number
34 of load cycles, generate the initial discontinuity. Either through manufacturing or created by
35 situations of use, pre-existing flaws create the critical conditions from which the material breakage
36 is developed. Fracture mechanics' purpose is to analyze and determine the mechanical behavior of
37 structural elements, considering the existence of flaws in the material to define the conditions or
38 criteria of breakage [1].

39 The first theory that explains the fracture of cracked solids, known as elastic linear mechanics
40 fracture (LEFM), was initially proposed by Griffith at the beginning of the last century (Griffith,
41 1920), and subsequently developed by Irwin, in the second half of the same (Irwin, 1957). Up to its
42 appearance, only the failure by plastic collapse, where the material deforms plastically without any

43 fracture, had well-structured physical and mathematical foundations. The LEFM came to fill the
 44 gap that existed in the opposite situation of the plastic collapse, when the fracture occurs in
 45 conditions of small deformation and in stress levels much lower than those that lead to the start of
 46 the material plastic deformation processes [2].

47 Using the principles of the MFEL, it is possible to assess the stable propagation of fatigue cracks in
 48 welded joints when using the empirical relationship proposed by Paris and Erdogan [3,4].

$$49 \quad \frac{da}{dN} = C(\Delta K)^m = C(\beta\Delta\sigma\sqrt{\pi a})^m \quad (1)$$

$$50 \quad \text{To:} \quad \Delta K_{th} \leq \Delta K \leq K_{Ic} \quad (2)$$

51

52 where the C and m parameters are constant of the material for a range of stress $\Delta\sigma$ and R
 53 (load rate) fixed; ΔK is the range of the stress intensity factor; β is a dimensionless function that
 54 depends on the geometry of the component and the crack size (a); ΔK_{th} is the range of the stress
 55 intensity factor threshold; and finally, K_{Ic} is the fracture toughness of the material for the
 56 condition of flat deformation.

57 When the stress intensity factor reaches a critical value, and the ASTM E399 [5] and ASTM D5045
 58 [6] requirements are met, the critical value can be regarded as a material property called fracture
 59 toughness for flat deformation, K_{Ic} . For that value, crack starts its unstable spread, fracturing the
 60 component into two parts. In this way, the local fracture approach on Mode I is determined, on the
 61 basis of the following expression [7].

$$62 \quad \beta\sigma_f\sqrt{\pi a} \rightarrow K_{Ic} \quad (3)$$

63 In welded joints, the stress fields in front of the crack are more complex to determine due to the
 64 microstructural changes that occur as a result of the thermal cycle of the cooling system [8]. The
 65 crack tip in a weld can be described as a semi-elliptical curve with depth (a) and length (2c). In
 66 general, using Mode I, the stress intensity factor is given by [9].

$$67 \quad K_I = Y\sigma\sqrt{\pi a} \quad (4)$$

68

69 Where σ is the applied stress, and Y is a correction factor dependent on the load and the geometry
 70 of the crack size. The Y parameter is influenced by a number of factors that can be represented as
 71 follows:

$$72 \quad Y = \frac{M_k + M_s + M_t}{\phi^0} \quad (5)$$

73

74 M_k is a factor which considers the presence of the weld; M_s is a correction factor of the free surface
 75 area near the crack tip; M_t is a correction factor of the free surface in the crack tip; and finally, ϕ^0
 76 complete is the integral of the ellipse. The latter can be expressed as:

77

$$78 \quad \phi^0 = \int_0^{\pi/2} \left\{ 1 - \left(1 - \frac{a^2}{c^2} \right) \sin^2 \phi \right\}^{1/2} d\phi \quad (6)$$

79

80 Where ϕ is defined as the angle of an ellipse. The values of MS and Mt depend on the joint
81 geometry, and not evaluating them can lead to an error that is normally about 0.13%. This is
82 because the stress field is low-intensity when the distance is greater from the weld of toe; therefore,
83 it can be avoided [10].

84

85 A number of researchers have determined expressions for the calculation of Mk, such as Lie and
86 Zhao [11], and Maddox and Andrews [12], who made a review of the British Standards PD6493 and
87 BS7608, for the steel structures cruciform design subjected to fatigue, establishing a value of Mk
88 between 0.83 and 1.00 for cracks located at the weld of toe. The Hobbacher researcher [13], found an
89 expression for Mk, for the case of a cruciform welded joint and 0.02 mm-sized crack, finding that
90 the effect of the weld of toe produces a variation of 5% for various relationships of assessed aspects.
91 The obtained equation by Hobbacher is described below:

92

$$93 \quad M_k = C \left(\frac{a}{T} \right)^k \quad \text{para } M_k \geq 1 \quad (7)$$

94

95 The magnitudes of C and k are dependent on the aspect and the geometry of the joint. Maddox [12]
96 presented a dimensionless factor M_k which allows estimation of the influence of stresses generated
97 by the geometric profile of the welded joints on the stress intensity factor.

98

$$98 \quad M_k = \frac{K}{\sigma \sqrt{\pi a}} \quad (8)$$

99 The researcher [9, 14] carries out a comparative analysis between the estimated models by Maddox,
100 Andrews and Hobbacher for the determination of the weld magnification factor Mk. In this work, it
101 is determined that the crack depth is a parameter that affects between 15% to 65% of the parametric
102 equation for the calculation of Mk. Concomitant researcher Brennan [15] developed a comparative
103 parametric equation for the determination of the weld magnification factor, in a cruciform welded
104 joint. In addition, the results were compared with those previously developed by the researchers
105 [10, 16, 17], establishing a good level of correspondence between the magnitudes encountered and
106 the previous research. In the case of welded joints in test tubes with cruciform geometry, Zhao and
107 Lie [11] include a set of equations for estimating the effect of misalignment on different types of
108 welded joints with a semi-elliptical surface crack. The Takeshi study [18] shows that failures start at
109 the root of the weld being the stress hub that defense the propagation of the crack and its life.

110

111 The study using numerical methods of the transient thermal behavior of the welding process goes
112 back to the 1980s, highlighting the work done by Friedman [19]. Among the numerical methods
113 used to carry out the study of transitional period thermal behavior, the finite element method is one
114 of the most popular. This technique has gained special importance mainly when it includes a mesh
115 refinement around the tip of the crack, besides the effect crack of the thermal cycle in the stress
116 intensity factors KI assessment and the weld magnification factor Mk. Although conceptually the
117 factors are obtained in a direct way, finite element analysis, with conventional elements near the
118 crack tip, underestimates the stress increase in gradient and displacement. Instead of using ever

119 smaller elements, size $1/\sqrt{r}$, some researchers [20,21] introduced a direct method, by moving the
 120 composed node of 8-noded quadrilateral elements up to a quarter of the node in the crack tip and
 121 relocating the nodes of the mid-point to a fourth at the end of the crack. In the case of linear elastic
 122 deformation, the elements Plane2 (2-D, 6-noded triangle), Plane82 (2-D, 8-noded quadrilateral), and
 123 Solid95 (3-D, 20-noded brick), are used in ANSYS to stabilize the residual stress field by moving the
 124 nodes to a fourth of the tip of the crack. Once the field of stress is established the parameters of
 125 fracture are obtained [22]. Certain configurations of elements and nodes produce unique
 126 displacements. While this type of behavior is undesirable for the majority of the analyzes, it is ideal
 127 for elasticity problems in cracks. By forcing elements in the crack tip to have a unique deformation,
 128 $1/\sqrt{x}$ can improve the accuracy and reduce the need for a high degree of refinement of mesh in the
 129 crack tip. This singular deformation is only applied in the crack tip.

130

131 Some contributions of this research is the three-dimensional computational modeling of a welded
 132 joint, using the finite element method, where the surface ripple on the surface of the weld bead and
 133 differentiation in the mechanical properties of the fusion zone, the heat-affected zone (HAZ) and
 134 base material, respectively. In addition, the use of an initial residual stress field for the welded joint
 135 and adjacent region that emulated was determined by the experimental path. The fundamentals of
 136 Fracture Mechanics were employed in the numerical modeling of the welded joint with the
 137 presence of a surface crack semi-elliptical type discontinuity at the weld toe. The latter is defined as
 138 a semi-elliptical surface crack with a small aspect. Because of this study, a set of mathematical
 139 models for the weld magnification factor were obtained for cruciform welded joints, which can be
 140 used in the prediction of the fatigue life of this type of welded joint.

141

142 2. Materials and methods

143 For the definition of the experimental and analytical procedures, previous studies were used as
 144 reference in cruciform test tubes subjected to biaxial cycles of stress to analyze fatigue. In these
 145 studies, the thicknesses, welding dimensions, and size and penetration depth of the weld were
 146 observed. For the experimental development of the present work, a carbon steel ASTM A36 HR
 147 Commercial 8 mm thickness and material of the electrode E6013 were used. The Shielded Metal
 148 ArcWelding (SMAW) process is a simple, low cost and suitable way of joining most metals and
 149 alloys commonly used in industry [23]. The electrical characteristics of the process (SMAW) used in
 150 the joint are shown in Table 1, for each weld size (leg).

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Table 1. Main characteristics of the welding procedures used.

Weld size (leg)	Diameter of the electrode E-6013	Electrical parameters	Forward Speed
3 mm	3/32"	102 volts, 72 A CD	20 cm/min
5 mm	1/8"	71.2 volts, 98 A CD	20 cm/min

155

156 For the purpose of generating a pilot input to the computational runs and comparison of the
 157 residual stress from the thermal cycle [24], the measurement of the temperature of the test piece
 158 during the post welding cooling for the two means of cooling (air and water) using two
 159 thermocouples type K, were located laterally on each edge of the bead welded. The thermocouples
 160 were connected to a data acquisition card or-9211, mounted on the NI CDAQ-9172, and then to the
 161 PC. The layout of the thermocouples in the measuring cylinder is shown in Figure 1. LabView
 162 Signal Express 2011 software was used to acquire and process data from the thermocouples and
 163 obtain the cooling curves.

164



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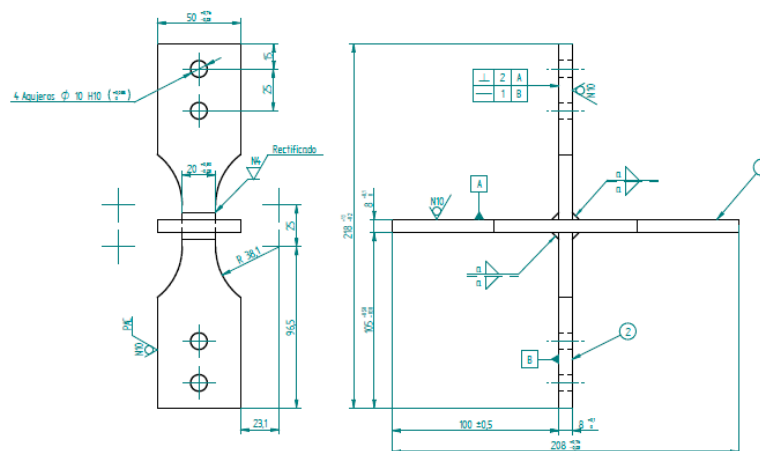
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Figure 1. Connection of the thermocouples.

167

168 For the process of plate-cutting, the technique of high-density plasma was used. Due to the cutting
 169 technique used, the heat affected zone (HAZ), with a thickness of 8 mm, reached a millimeter of
 170 depth of the surface that results from the cut. After this preliminary cut, the central area of the test
 171 piece went into a mechanical process through milling to remove the endings of the weld bead,
 172 prone to higher density of defects product at the beginning and breakdown of the electric arc. The
 173 geometry of the fixture to be used in the tests after final machining is presented in Figure 2.
 174

174



175

176

Figure 2. Geometric fixture test (mm scale).

177

178 The variables used for the manufacture of the test specimens are indicated below in Table 2.

179

180

Table 2. Variables for manufacturing

181

weld size (leg) C	Cooling means
3 mm	Air calm
5 mm	Agua

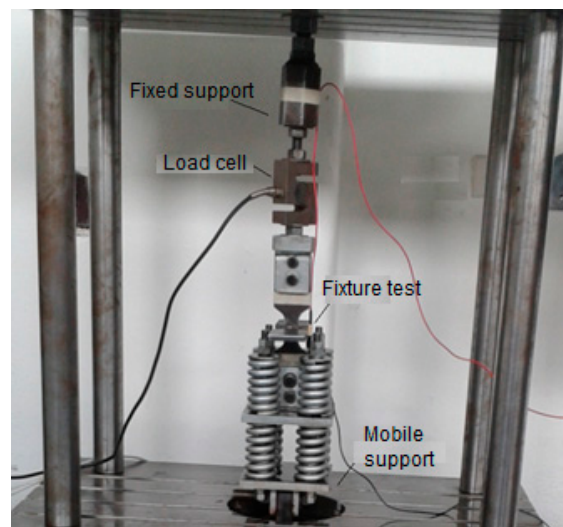
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183 Fatigue tests were performed by axial load on cruciform geometry specimens, for different load
184 ratios (R), defined as:

185 $R = P_{min}/P_{max}$, where; P_{min} : Minimum load and P_{max} : Maximum load

186 The assembly made for the test is shown in Figure 3.

187



188

189

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Figure 3. Assembly for the axial fatigue test

191

192 The operating parameters of the equipment used are indicated in Table 3.

193

194

Table 3. Parameters of the equipment.

195

Parameters	Magnitude	Unit
Maximum load	900	kgf
Frequency of operation	12	Hz
Engine power	3	hp
Nominal Motor Amperage	8,6	A
Supply voltage	206	(v)
Amperage at the Operation point	8,3	A
Load application cycles per Hour	8200	cycles
Diameter Drive Pulley [in]	6	in

Diameter Pulley Driven [in]	12	in
Transmission Ratio	0,5	
Motor Speed rpm @ 60Hz	3445	rpm

196

197 To begin the simulations by the finite element method, the software ANSYS was used. The
 198 determination of stress intensity factors for geometries and application modes of simple loads can
 199 be carried out through easily implemented analytical solutions. But when the geometries and loads
 200 are more complicated, these induce complex stress and strain fields on the structural component;
 201 therefore, it is recommended to use the Finite Element Method to determine said factors [25]. Also,
 202 the displacement correlation technique (DCT) is relatively simple to perform and offers sufficiently
 203 precise solutions for the purpose of this work. Thus, the DCT method is employed in the modeling
 204 of the cracks in the weld joint analyzed.

205

206 To describe the stress field intensity in the region near to the crack vertex, it is necessary to use
 207 singular elements, with an additional node at a distance of a quarter of the size of the fissure vertex.
 208 With these singular elements, the stress intensity factors can be calculated in the following way.

209

$$210 \quad K_I = \frac{\mu}{k+1} \cdot \sqrt{\frac{2\pi}{L}} \cdot \{4(v_b - v_d) + (v_e - v_c)\} \quad (9)$$

$$211 \quad K_{II} = \frac{\mu}{k+1} \cdot \sqrt{\frac{2\pi}{L}} \cdot \{4(u_b - u_d) + (u_e - u_c)\} \quad (10)$$

212

$$213 \quad \text{With: } \mu = \frac{E}{2(1+\nu)} \quad k = \begin{cases} 3 - 4\nu & \text{(plane strain)} \\ \frac{3-\nu}{1+\nu} & \text{(plane stress)} \end{cases} \quad (11)$$

214 Where:

215 KI, KII: Stress intensity factors for load modes I and II, respectively (MPa \sqrt{m}).

216 E: Elasticity modulus of the material (MPa).

217 ν : Poisson's ratio of the material.

218 L: Characteristic length of the singular element (mm).

219 (u_i ; v_i): Displacements of the nodes of the singular elements (mm).

220

221 The Figure 4 shows the singular elements, the disposition of the nodes and the displacements
 222 employed in calculating the stress intensity factors.

223

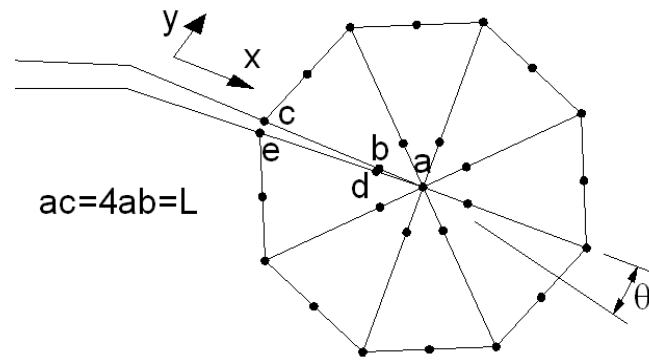


Figure 4. Disposition of control nodes on the crack vertex

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228 The tip of the crack must be meshed with small singular concentric elements and should not vary in
 229 size as the crack extends. The rest of the component is meshed with quadrangular elements that
 230 provide good precision.

231

232 Various methods are available to establish the orientation of the crack as it extends, although all
 233 basically lead to similar results. This work uses the strain energy density method on the crack
 234 vertex (ψ), which is expressed according to (12). The relative local minimum of ψ corresponds to a
 235 large volume change and is identified with the region dominated by macro dilatation leading to
 236 crack growth. Accordingly, this method establishes that the crack propagates in the direction of
 237 minimum strain energy released [26].

238

$$239 \quad \psi = A_{11}K_I^2 + 2A_{12}K_I K_{II} + A_{22}K_{II}^2 \quad (12)$$

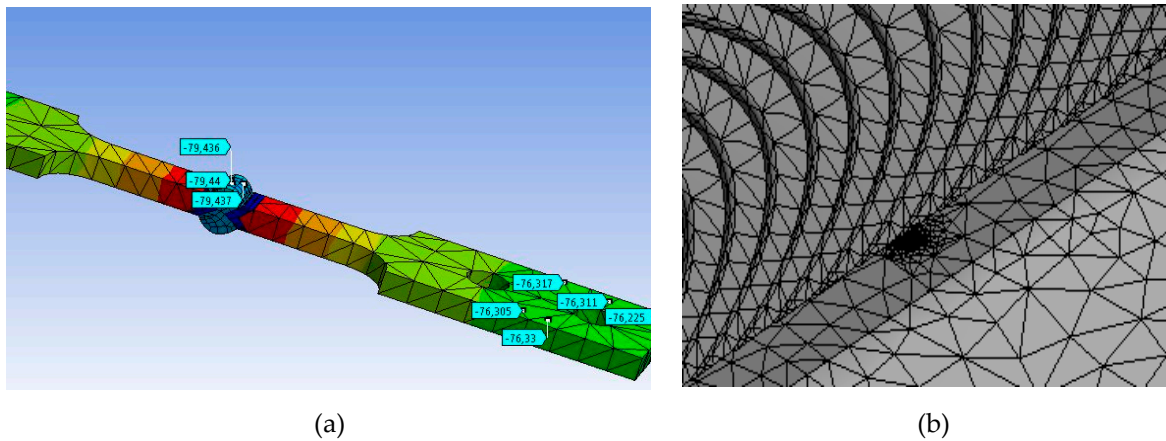
240 Where:

241 A_{ij} : Coefficients that depend on the material's elastic properties.

242

243 A 3D computer model of the cruciform test tubes for each of the two legs of welding considered
 244 included the temperature profiles obtained experimentally and the determination of the profile of
 245 stress for the residual cooling conditions in calm air and water, as shown in Figure 5 (a). At a later
 246 stage in the modeling, surface semi-elliptical, a crack was included at the weld toe, as shown in
 247 Figure 5 (b). The interest in this second model focused on studying the stress-strain field near the
 248 front of the semi-elliptical crack under various conditions of cyclic loading (changing the load ratio
 249 R). Crack sizes used in this work for the computer simulations are shown in Table 4, naming c , the
 250 size of the semi-major axis, and a , the dimension of the semi-minor axis of the semielliptical crack.

251



252 **Figure 5.** (a) The temperature profile for the cooling cycle post welding and residual stress, (b)
 253 semi-elliptical crack on welding and plain generated for the finite element model.

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 255
 256

Table 4. Crack sizes of semielliptical section.

Semi-major axis (c) (mm)	Semi-minor axis (a) (mm)
0.15	0.06
0.23	0.09
0.30	0.12
0.45	0.18
1.25	0.50
2.50	1.00
5.00	2.00
7.50	3.00

257
 258
 259
 260

With the FEM model implemented, the values of the weld magnification factor are determined for crack sizes that appear in Table 2. The weld magnification factor is calculated by:

$$261 \quad M_k = \frac{K_{I(MEF)}}{\sigma_{nom}\sqrt{\pi a}} \quad (13)$$

262 Where:

263 $K_{I(MEF)}$: Stress intensity factor obtained by FEM (MPa \sqrt{m}).

264 σ_{nom} : Nominal stress (MPa).

265

266 The magnitudes of the nominal and alternant stress of operation appear in Table 3. It is calculated
 267 using the following equation:

$$268 \quad \sigma_{nom} = \frac{F}{TL} \quad (14)$$

269 Being:

270 F: Load operation (N).

271 T: Plate Thickness (mm).

272 L: Length of the weld bead (mm).

$$273 \quad \sigma_{\text{alt}} = \frac{F}{2CL} \quad (15)$$

274 Being:

275 C: weld size leg (mm).

276

277 The values of the nominal and alternant stresses of the axial fatigue test are shown in table 5.

278

279 **Table 5.** Nominal and alternant stresses for the fatigue test.

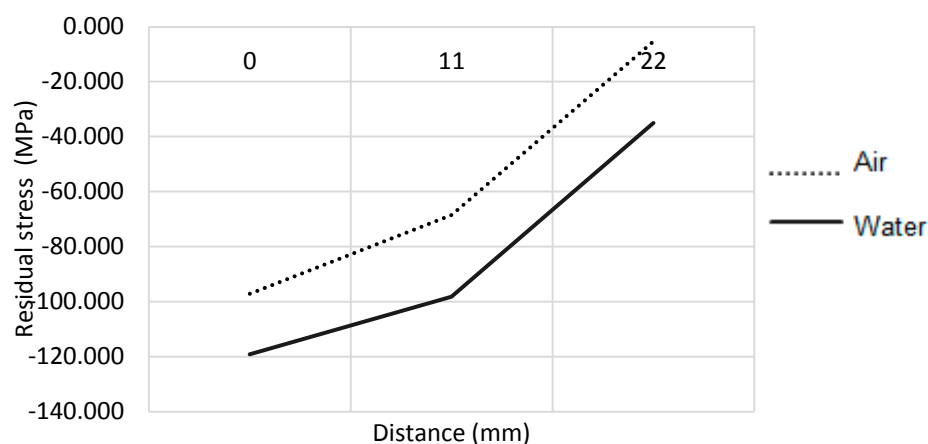
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Load rate (R=Pmin/Pmax)	Nominal stress σ_{nom} (MPa)	Alternant stress	Alternant stress
		σ_{alt} (MPa) C=3 mm	σ_{alt} (MPa) C=5 mm
0	55.2	71.3	100.9
-0.5	36.8	35.5	64.6

281

282 3. Discussion and Results

283 As a product of computational modeling, the residual stress profile was obtained for each of the
 284 legs of welding and cooling means analyzed. In Figure 6, the residual stress profile is shown for a
 285 vessel with a leg of five millimeters, where the zero position indicates the location of the weld of
 286 toe. It is found that the modeled residual compressive stresses were compressive typed and its
 287 magnitude is directly related to the intensity of the cooling medium and the size of the bead. The
 288 mean of cooling water turned out to be the most intense, introducing a rate of cooling in the initial
 289 range analyzed of $-112 \text{ }^\circ\text{C/s}$ and a residual stress at the weld of toe for a leg of 5 mm equal to -119
 290 MPa. On the other hand, it was found that large legs induce higher residual stresses, prompted by
 291 the need for a greater heat input to the board and to the greater three-dimensional restriction to
 292 thermal contraction.

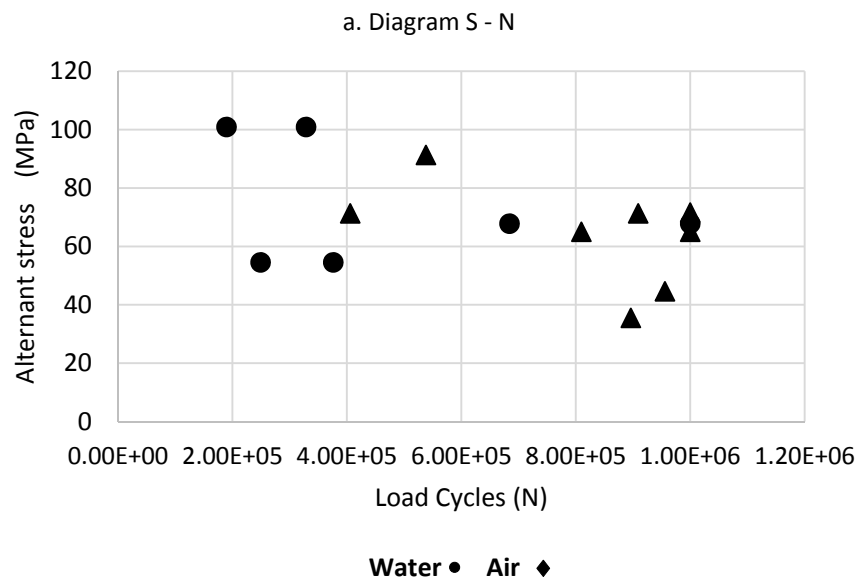


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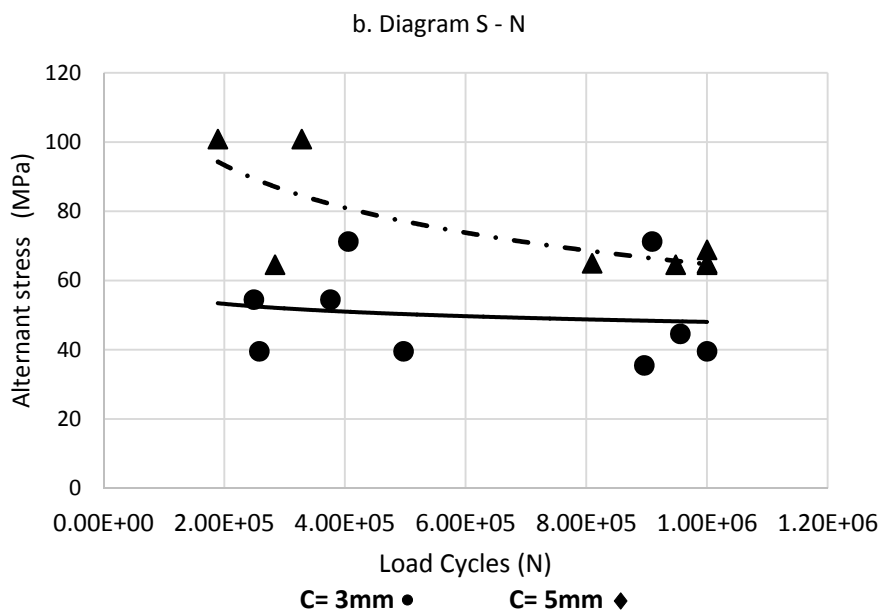
294 **Figure 6.** Residual stress obtained from the theoretical model MEF for a leg of 5 mm.

295

296 Using the axial fatigue machine, the stress - life tests were carried out for the specimens under
 297 study. The experimental results for the different means of cooling and welding legs are shown
 298 below, in Figure 7 (a). It is observed that more severe cooling means reduce life to fatigue. In
 299 Figure 7 (b) it is observed that the size of the leg did not affect the life of the specimens
 300 considerably. In Figure 7 (c), it is observed that the more tensile load ratios minimize the life of the
 301 specimens.

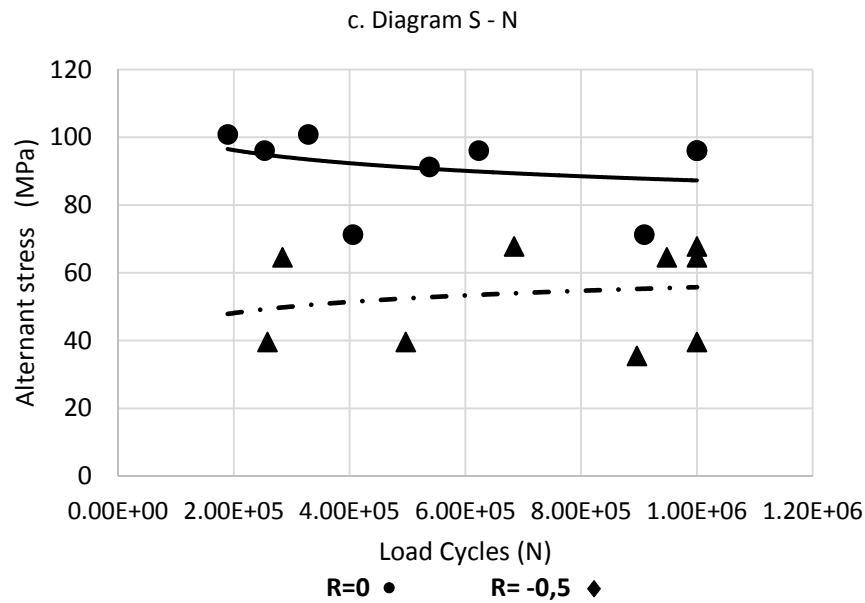


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Figure 7. Diagrams Stress – Number of Cycles

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The behavior of the weld magnification factor M_k in the presence of residual stresses was evaluated analytically. Weld magnification factors M_k obtained with the presence of a residual stress field has been appointed in the present research. This allows a distinction on this factor in the sense that it involves the effect of the residual stress field in the calculation of the stress intensity factor. The expression (9) is used in the calculation of M_k in function of the dimensionless crack depth (a/T) and the possible combinations between weld size (leg) and the cooling medium used.

In the Table 6 the values obtained for M_k are shown for the different relationships of load rate, type of cooling, and weld size of the object of study. The behavior of the modified M_k factors, in function of the dimensionless size of crack, is shown in Figure 8 for the two sizes of legs analyzed.

Table 6. Modified weld magnification factor M_k to crack at the weld toe:

(a) weld size (leg) of 3 mm and (b) weld size (leg) of 5 mm.

a) Modified weld magnification factor M_k for weld size (leg) of 3 mm.

Load rate (R)	a/T	Cooling air	Cooling water	Free of residual stress
0	0.008	0.848	1.345	1.449
	0.011	0.884	1.389	1.384
	0.015	0.878	1.399	1.404
	0.023	0.884	1.408	1.357
	0.063	0.783	1.260	1.077
	0.125	0.662	1.067	0.853
	0.250	0.547	0.811	0.746

	0.375	0.472	0.676	0.758
-0.5	0.008	1.159	1.851	1.428
	0.011	1.206	1.911	1.384
	0.015	1.199	1.925	1.404
	0.023	1.207	1.937	1.357
	0.063	1.069	1.733	1.077
	0.125	0.904	1.469	0.854
	0.250	0.746	1.135	0.746
	0.375	0.644	0.930	0.750

323

324

b) Modified weld magnification factor M_k for weld
size (leg) of 5 mm.

Load rate (R)	a/T	Cooling air	Cooling water	Free of residual stress
0	0.008	0.551	0.333	1.575
	0.011	0.534	0.359	1.531
	0.015	0.522	0.352	1.471
	0.023	0.522	0.378	1.307
	0.063	0.454	0.393	0.969
	0.125	0.440	0.422	0.803
	0.250	0.398	0.422	0.668
	0.375	0.373	0.413	0.717
	-0.5	0.008	0.719	0.455
0.011		0.697	0.491	1.538
0.015		0.681	0.494	1.472
0.023		0.682	0.529	1.307
0.063		0.593	0.536	0.969
0.125		0.574	0.576	0.804
0.250		0.520	0.576	0.674
0.375		0.509	0.564	0.717

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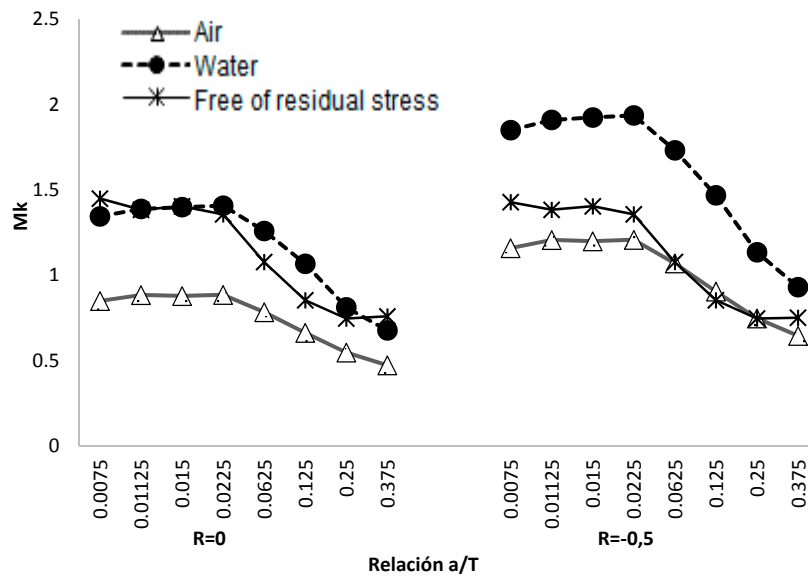
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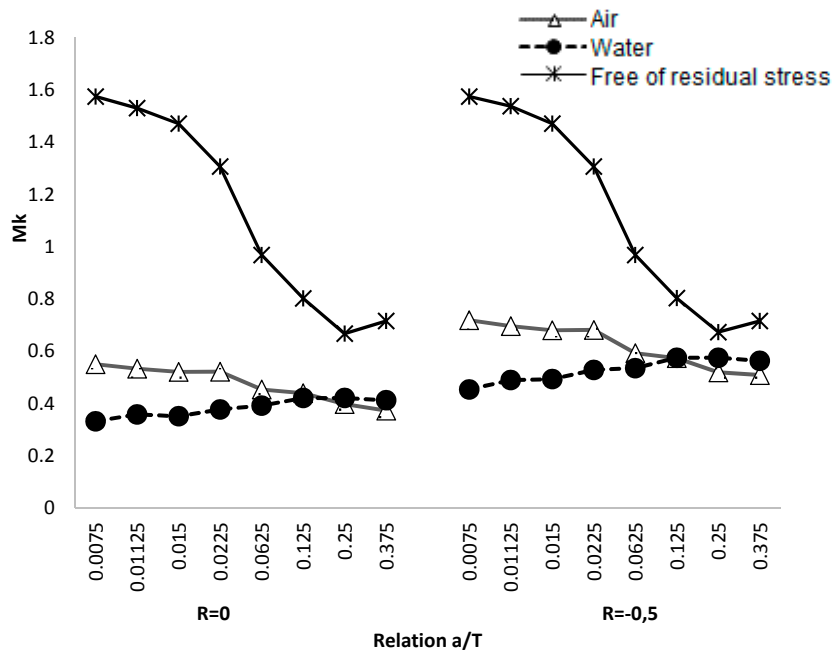


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a) Modified weld magnification factor M_k for weld size (leg) of 3 mm.



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b) Modified weld magnification factor M_k for weld size (leg) of 5 mm.

338 **Figure 8.** Modified weld magnification factor M_k to crack at the weld of toe: (a) weld size (leg) of 3

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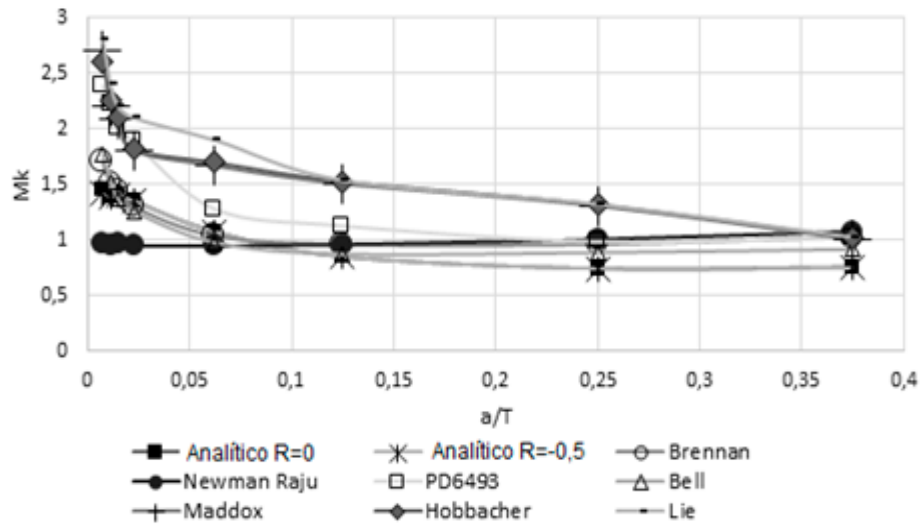
mm and (b) weld size (leg) of 5 mm.

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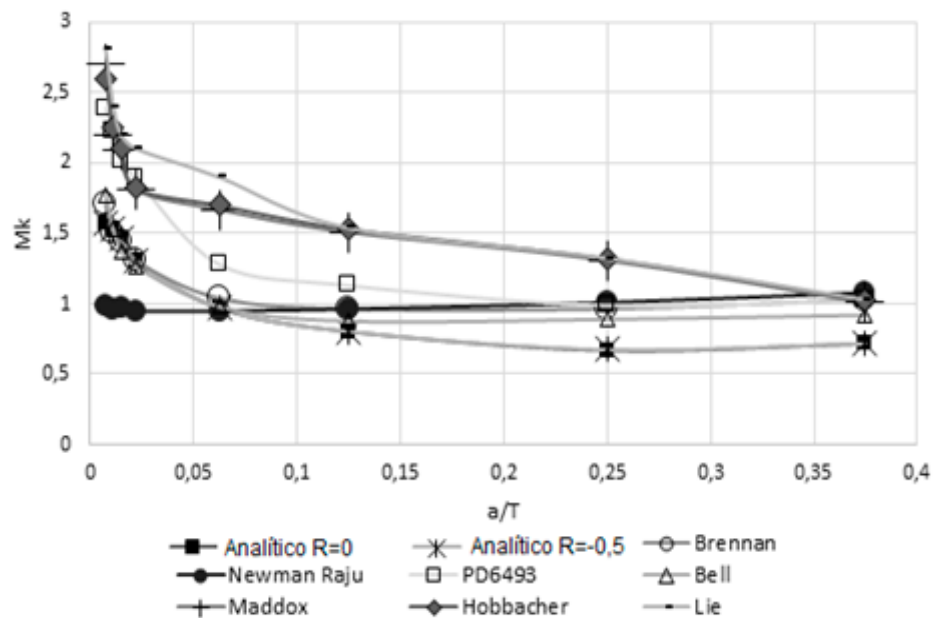
341 The theoretical obtained results in the present work for the modified weld magnification factor
 342 M_k , for condition of free stresses, were compared with the results achieved by other researchers
 343 [9-13, 15-17]. In Figure 9, the results for the weld magnification factor are shown, for the case of a
 344 crack at the weld of toe and without residual stress, and verifies the correspondence of the
 345 developed numerical model with the results obtained by other researchers. The analytical results
 346 obtained involve several weld sizes and load rates.

347

a) M_k (Free of residual stress) $C=3\text{ mm}$



b) M_k (Free of residual stress) $C=5\text{ mm}$



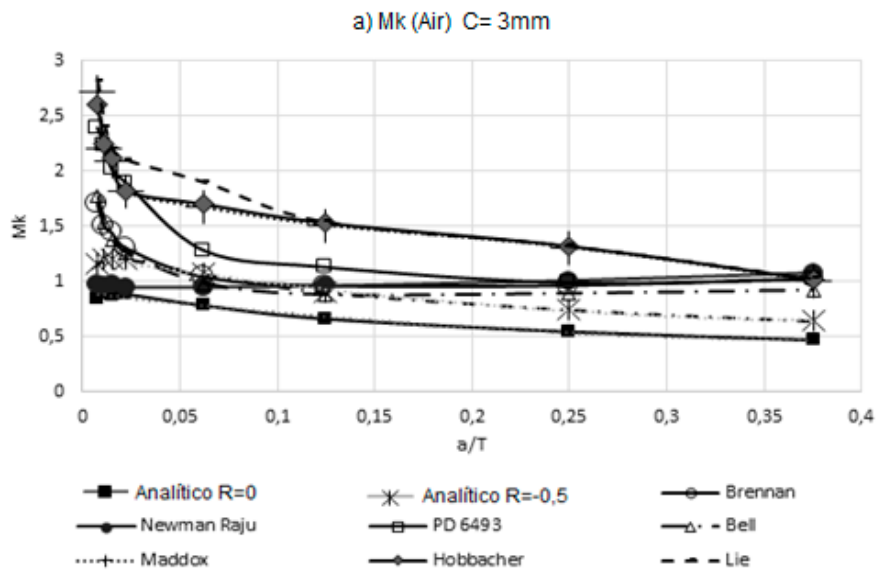
350

351 **Figure 9.** Weld magnification factor M_k without residual stress vs. results of other researchers: (a)
 352 weld size of 3 mm and (b) weld size of 5 mm.

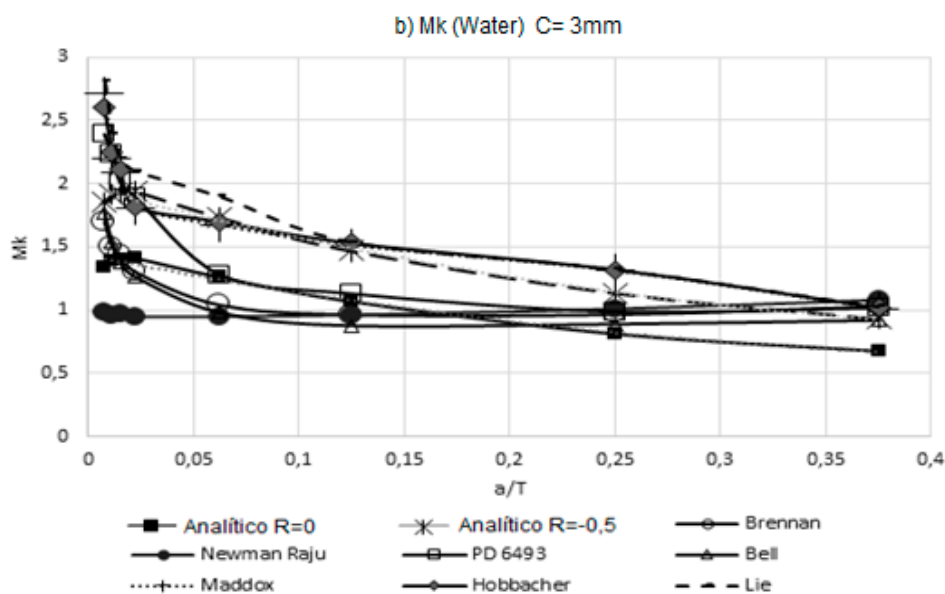
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354 In Figures 9 (a) and (b) it can be noted that the weld magnification factor M_k is independent from
 the load rate and has a similar behavior to that proposed by other researchers. Using the obtained

355 information in Table 6 for the modified weld magnification factor M_k , including the effect of the
 356 residual stress reached by the air and water cooling medium, it is possible to make a comparison
 357 with the results obtained by other researchers. This comparison of results is shown in Figures 10
 358 and 11. The observed trend with the modified weld magnification factor is to markedly diminish in
 359 function of the post weld cooling medium intensity, for the range of relative size of crack $a/T < 0.1$.
 360 This behavior is related to the coupled benefits of the residual compressive stresses that arise
 361 during the post-welding cooling for the region where the modeled crack occurs in the present work.



362



363

364 **Figure 10.** Modified weld magnification factor M_k with the presence of residual stress vs. other
 365 researchers: (a) air and weld size of 3 mm and (b) water and weld size of 3 mm.

366

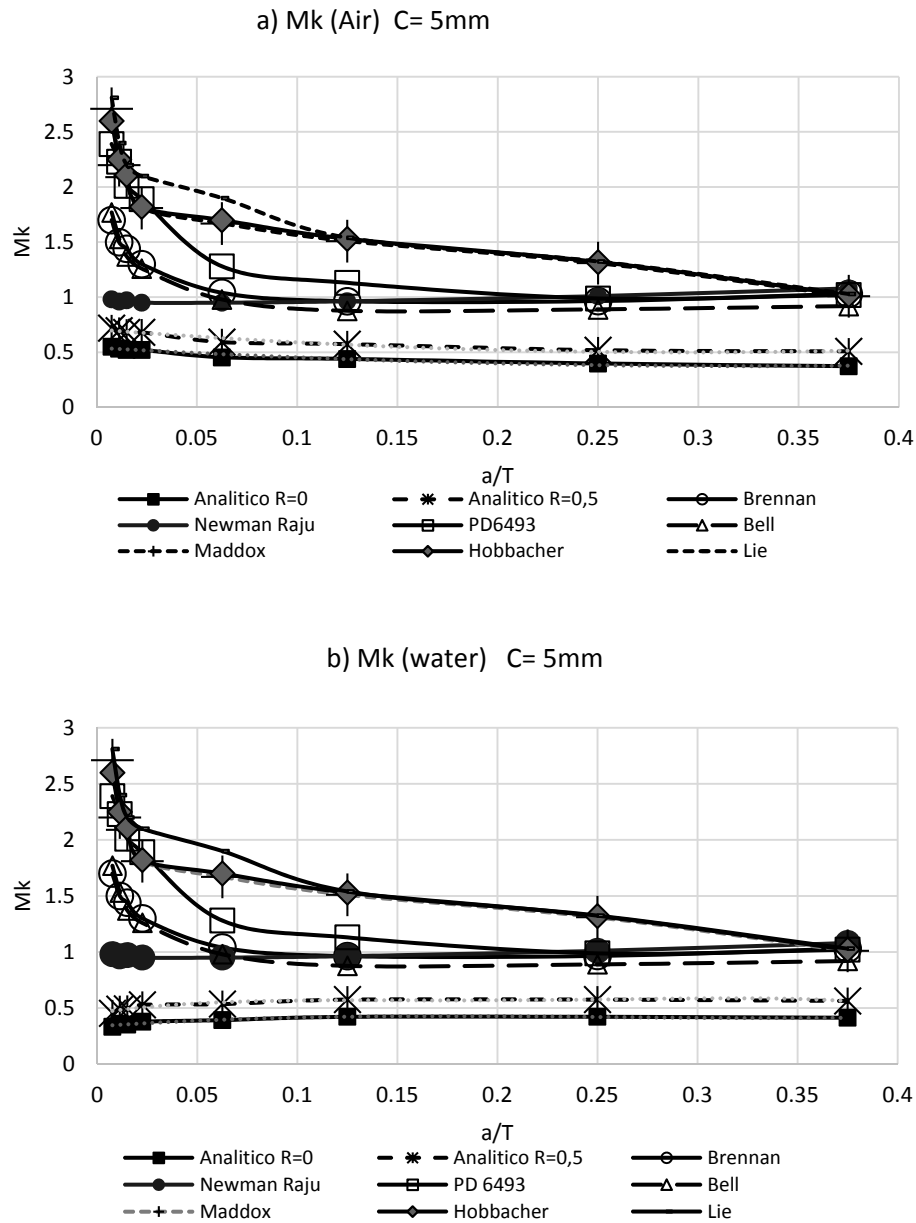


Figure 11. Modified weld magnification factor M_k with the presence of residual stress vs other researchers: (a) air and weld size of 5 mm and (b) water and weld size of 5 mm.

With the results obtained for the weld magnification factor, a regression analysis is carried out to obtain analytical equations that relate to the dimensionless size of the crack. Table 7 shows the expressions of $M_{k(a/T)}$ for the free condition of residual stresses. In Table 8, the expressions of $M_{k(a/T)}$ are shown for the condition of post-weld cooling in calm air. Finally, Table 9 shows the expressions of $M_{k(a/T)}$ for the condition of post-weld cooling in water (in the equations $\Omega=a/T$). These analytical expressions are particularly useful to establish models for the prediction of fatigue crack propagation and the design of a life management program for welded structures of the studied type.

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Table 7. Adjusted expressions for the weld magnification factor for the free condition of residual stresses.

383

Weld size (leg)	
3 mm	5 mm
$M_k = 0,0077\Omega^3 - 0,1121\Omega^2 + 0,351\Omega + 1,1592$	$M_k = 0,0101\Omega^3 - 0,1361\Omega^2 + 0,3671\Omega + 1,3123$

384

Valid for: $0.02 \leq \Omega \leq 0.33$.

385

Table 8. Adjusted expressions for the modified weld magnification factor M_k for the condition of post weld cooling in calm air.

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387

Load rate (R)	Weld size	
	3 mm	5 mm
0	$M_k = 2.5098\Omega^2 - 2.0772\Omega + 0.9002$	$M_k = 1.5822\Omega^2 - 1.0261\Omega + 0.5416$
-0.5	$M_k = 4.5708\Omega^2 - 3.7817\Omega + 1.6383$	$M_k = 3.2069\Omega^2 - 1.8877\Omega + 0.9443$

388

389

Table 9. Adjusted expressions for the modified weld magnification factor M_k for the condition of post weld cooling in water.

390

Load rate (R)	Weld size	
	3 mm	5 mm
0	$M_k = 3.2442\Omega^2 - 3.2442\Omega + 1.4311$	$M_k = 7.0363\Omega^3 - 5.4379\Omega^2 + 1.2513\Omega + 0.338$
-0.5	$M_k = 5.5871\Omega^2 - 5.7921\Omega + 2.6206$	$M_k = -117.47\Omega^4 + 97.992\Omega^3 - 28.427\Omega^2 + 3.4545\Omega + 0.6097$

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4. Conclusions

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We conducted a theoretical experimental study about the behavior of fatigue in welded joints with cruciform geometry. A 3D computer model of the welded joint was used throughout the finite element method where several features were introduced, such as the superficial natural undulation of the weld bead and established a distinction between the mechanical properties of the fusion zone, the heat affected zone and the base material, respectively. In addition, a residual stress field was introduced for the welded joint and the surrounding region, which emulates set one by experimental manner. In the computational simulation of the superficial semi-elliptical crack at the weld of toe, a convergence of the model for 405 428 nodes, with a computational cost in CPU time of 2680 s for each iteration, was reached.

403 It was determined that the residual stresses are of compression higher for the more intense cooling
404 medium (water). In addition, it can be noted that larger weld size induces greater residual stresses,
405 prompted by the need for a greater heat input to the joints and to the greater three-dimensional
406 restriction to a thermal contraction of the weld joint. Fatigue tests indicate that more severe cooling
407 means minimizing the life of the welding specimens in the same way as the more tensile load ratios.
408 It is observed that the specimens failed mainly in the weld toe.

409

410 A unique finding of the present work is the reaching of analytical expressions obtained by the weld
411 magnification factor M_k for two sizes of the weld and two post welding cooling media. The
412 analytical equations obtained consider the residual stresses induced by these two post welding
413 cooling mediums. The analytical expressions for M_k in the present research have good
414 correspondence with the obtained results by other authors, in the case of welded joints without
415 residual stresses. These expressions can improve the calculation codes, testing standards and the
416 structural integrity of welded joints verification. It can be noted that the observed trend with the
417 modified weld magnification factor is to markedly diminish, in function of the intensity of post
418 welding cooling medium for a dimensionless crack size below $a/T < 0.1$. This behavior is related to
419 the coupled benefits of the residual compressive stresses that arise during the post-welding cooling
420 for the assessment region of the type of crack studied.

421

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