

1 Article

2 Discrete Sine Transform-Based Interpolation Filter 3 for Video Compression

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7 **Abstract:** High Efficiency Video Coding (HEVC) uses an 8-point filter and a 7-point filter, which
8 are based on the discrete cosine transform (DCT), for the 1/2-pixel and 1/4-pixel interpolations,
9 respectively. In this paper, discrete sine transform (DST)-based interpolation filters (IF) are
10 proposed. The first proposed DST-based IFs (DST-IFs) use 8-point and 7-point filters for the
11 1/2-pixel and 1/4-pixel interpolations, respectively. The final proposed DST-IFs use 12-point and
12 11-point filters for the 1/2-pixel and 1/4-pixel interpolations, respectively. These DST-IF methods
13 are proposed to improve the motion-compensated prediction in HEVC. The 8-point and 7-point
14 DST-IF methods showed average BD-rate reductions of 0.7% and 0.3% in the random access (RA)
15 and low delay B (LDB) configurations, respectively. The 12-point and 11-point DST-IF methods
16 showed average BD-rate reductions of 1.4% and 1.2% in the RA and LDB configurations for the
17 Luma component, respectively.

18 **Keywords:** HEVC; Interpolation filter; Sinc; DCT (discrete cosine transform); DST (discrete sine
19 transform)

20 1. Introduction

21 The ITU Telecommunication Standardization Sector-Video Coding Expert Group (ITU-T
22 VCEG) and the Moving Picture Expert Group (ISO/IEC MPEG) organized the Joint Collaborative
23 Team on Video Coding (JCT-VC) [1], and they jointly developed the next-generation video-coding
24 standard HEVC/H.265. In HEVC [2], motion-compensated prediction (MCP) is a significant
25 video-coding function that reduces the temporal redundancy in video signals. In the MCP, each
26 prediction unit (PU, block) in the encoder finds the block that has the least SAD (sum of absolute
27 difference) from the reference pictures in terms of the Lagrangian cost [3]. Since the moving objects
28 between two pictures are continuous, it is difficult to identify the actual motion vector in
29 block-based motion estimation. Therefore, the use of fractional pixels that have been derived from
30 an interpolation filter for motion-vector searches can improve the precision of the MCP.

31 The sinc function is an ideal interpolation filter in terms of signal processing [4], [5]. However,
32 the sinc-interpolation filter is difficult to implement in HEVC because the sinc-interpolation filter
33 needs to reference the neighbor pixels from $-\infty$ to ∞ . Therefore, the HEVC interpolation filters are
34 designed from the DCT type-II (DCT-II) transform [6], [7], [8] that improves the bit reduction by
35 approximately 4.0 % compared with the H.264/AVC interpolation filters [9]. The filter lengths of the
36 DCT-II-based interpolation filter (DCT-IF) are 8-point and 7-point for the 1/2-pixel and 1/4-pixel
37 interpolations, respectively. In the present paper, a DST [10]-based interpolation filters (DST-IFs)
38 that use different interpolation-filter lengths are proposed.

39 This paper is organized as follows. Section 2 presents the ideal interpolation filter, the sinc
40 function, the DCT-IF, the proposed DST-IF, and an analysis of the interpolation filters. Section 3
41 presents the experiment results, and Section 4 concludes the paper.

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43
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45 2. Interpolation Filters for Generating Fractional Pixels

46 2.1 The sinc-based interpolation filter

47 The sinc-based interpolation filter is an ideal interpolation filter in terms of signal processing
48 and its equation is as follows:

$$x(t) = \sum_{k=-\infty}^{\infty} x(kT_s) \frac{\sin \frac{\pi}{T_s}(t-kT_s)}{\frac{\pi}{T_s}(t-kT_s)} \quad (1)$$

49 where the sinc-based interpolation filter is defined as $x(t)$, t represents the locations of the
50 subsamples and k is the integer sample value, and T_s is the sampling period that is equal to 1. When
51 the sinc-based interpolation filter is lengthened from $-\infty$ to ∞ , it is the ideal interpolation filter to
52 reconstruct all the samples. Although the sinc-based interpolation filter is ideal, it is not possible to
53 implement it in HEVC. Since it is impossible to reference all of the neighbor pixels in a picture, the
54 DCT-IF is adopted in HEVC, the filter lengths of which are restricted within 8-point and 7-point for
55 the 1/2-pixel and 1/4-pixel interpolations, respectively.

56 2.2 The DCT-II interpolation filter (DCT-IF) in HEVC

57 The DCT-IF [4] in HEVC is designed in a different way but it can be designed easily in this
58 paper from the following forward/inverse DCT-II:

$$X(k) = \sqrt{\frac{2}{N}} \sum_{n=0}^{N-1} c_k x(n) \cos \frac{(n+1/2)\pi k}{N} \quad (1)$$

$$x(n) = \sqrt{\frac{2}{N}} \sum_{k=0}^{N-1} c_k X(k) \cos \frac{(n+1/2)\pi k}{N} \quad (2)$$

59 In Equation (1), $X(k)$ is the DCT-II coefficients and the input pixel $x(n)$ is the IDCT-II (Inverse
60 DCT-II) coefficients in Equation (2).

61

$$c_k = \begin{cases} \frac{1}{\sqrt{2}}, & k=0 \\ 1, & \text{otherwise} \end{cases} \quad (3)$$

62

63 where c_k is $1/\sqrt{2}$ at $k=0$, and c_k is 1 at $k \neq 0$. The substitution of Equation (1) into Equation (2) results in
64 the following DCT-IF equation:

65

$$x(n) = \frac{2}{N} \sum_{m=0}^{N-1} x(m) \sum_{k=0}^{N-1} c_k^2 \cos \frac{(m+1/2)\pi k}{N} \cos \frac{(n+1/2)\pi k}{N} \quad (4)$$

Table 1. 8-point and 7 point DCT-II based Interpolation Filter Coefficients in HEVC.

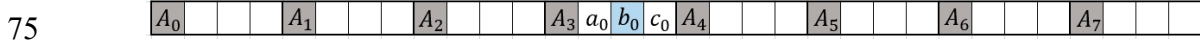
Index i	0	1	2	3	4	5	6	7
1/2-pixel filter[i]	-1	4	-11	40	40	-11	4	-1
1/4-pixel filter[i]	-1	4	-10	58	17	-5	1	

66

67 For example, the 1/2-pixel interpolation filter, when $n = 3.5$, in the 8-point DCT ($N = 8$) is derived
68 as a linear combination of the cosine coefficients and $x(m)$, $m = 0, 1, \dots, 7$. Similarly, the 1/4-pixel
69 interpolation filter, when $n = 3.25$, in the 7-point DCT ($N = 7$) is derived as a linear combination of the

70 cosine coefficients and $x(m)$, $m = 0,1,\dots,6$. Lastly, the DCT-IFs that interpolate the 1/2-pixel and
 71 1/4-pixel interpolations are shown as the integer numbers in Table 1. The filter-coefficient order of
 72 the 3/4-pixel interpolation filter is the reverse of the filter-coefficient order of the 1/4-pixel
 73 interpolation filter.

74



75

76 **Figure 1.** Fractional pixel position in Luma motion compensation.

77 Figure. 1 is an example of the integer- and fractional-pixel positions in the Luma motion
 78 compensation. In Figure 1, the capital letters (A_0 to A_7) indicate the integer-pixel position, the small
 79 letter b_0 is the 1/2-pixel position, and a_0 and c_0 are the 1/4-pixel and 3/4-pixel positions, respectively.
 80 For example, using the DCT-IF, the b_0 and a_0 are calculated from Table 1 as follows:

$$b_0 = (-1 \cdot A_0 + 4 \cdot A_1 - 11 \cdot A_2 + 40 \cdot A_3 + 40 \cdot A_4 - 11 \cdot A_5 + 4 \cdot A_6 - 1 \cdot A_7 + 32) \gg 6 \quad (5)$$

$$a_0 = (-1 \cdot A_0 + 4 \cdot A_1 - 10 \cdot A_2 + 58 \cdot A_3 + 17 \cdot A_4 - 5 \cdot A_5 + 1 \cdot A_6 + 32) \gg 6$$

81 where the computation of a_0 is the same as that of b_0 from Table 1, the computation of c_0 is in the
 82 order that is the reverse of that of a_0 , and “ \gg ” operation means the bit-wise shift right.

83 2.3 The Proposed DST-VII Interpolation Filter (DST-IF)

84 The DST-IF for HEVC can easily be designed in this paper from the forward/inverse DST-VII.
 85 The DST-VII and inverse DST-VII are defined as follows:

$$X(k) = \sqrt{\frac{2}{N + \frac{1}{2}}} \sum_{n=0}^{N-1} x(n) \sin \frac{(n+1)(k + \frac{1}{2})\pi}{N + \frac{1}{2}} \quad (6)$$

$$x(n) = \sqrt{\frac{2}{N + \frac{1}{2}}} \sum_{k=0}^{N-1} X(k) \sin \frac{(n+1)(k + \frac{1}{2})\pi}{N + \frac{1}{2}} \quad (7)$$

86 where $X(k)$ is the DST-VII coefficient and $x(n)$ represents the input pixels. The substitution of
 87 Equation (6) into Equation (7) results in the following DST-IF equation:

$$x(n) = \frac{2}{N + \frac{1}{2}} \sum_{m=0}^{N-1} x(m) \sum_{k=0}^{N-1} \sin \frac{(m+1)(k + \frac{1}{2})\pi}{N + \frac{1}{2}} \sin \frac{(n+1)(k + \frac{1}{2})\pi}{N + \frac{1}{2}} \quad (8)$$

88 In the similar way to obtain the DCT-IF coefficients, the DST-IF is derived from Equation (8).
 89 For example, the 1/2-pixel interpolation filter, when $n = 3.5$, in the 8-point DST ($N = 8$) is derived as a
 90 linear combination of the sine coefficients and $x(m)$, $m = 0,1,\dots,7$. Similarly, the 1/4-pixel
 91 interpolation filter, when $n = 3.25$, in the 7-point DST ($N = 7$) is derived as a linear combination of the
 92 sine coefficients and $x(m)$, $m = 0,1,\dots,6$. Lastly, the DST-IFs that interpolate the 1/2-pixel and
 93 1/4-pixel interpolations are shown in Table 2. The filter-coefficient order of the 3/4-pixel
 94 interpolation filter is the reverse of the filter-coefficient order of the 1/4-pixel interpolation filter [11].

95 **Table 2.** 8-point and 7 point DST-VII-based Interpolation-Filter (DST-IF) Coefficients.

Index i	0	1	2	3	4	5	6	7
1/2-pixel filter[i]	-2	6	-13	41	41	-13	6	-2
1/4-pixel filter[i]	-2	5	-11	58	18	-6	2	

96

97 In the given example, the 8-point and 7-point DST-IFs were derived, but the M-point and
 98 (M-1)-point DST-IFs, where $M > 8$, can be easily derived in a similar way for high-resolution
 99 sequences to improve the video-coding efficiency.

100 **Table 3.** 12-point and 11-point DST-VII-based Interpolation-Filter (DST-IF) Coefficients.

Index i	0	1	2	3	4	5	6	7	8	9	10	11
1/2-pixel filter[i]	-1	2	-4	7	-13	41	41	-13	7	-4	2	-1
1/4-pixel filter[i]	-1	2	-3	6	-11	58	19	-8	4	-3	1	

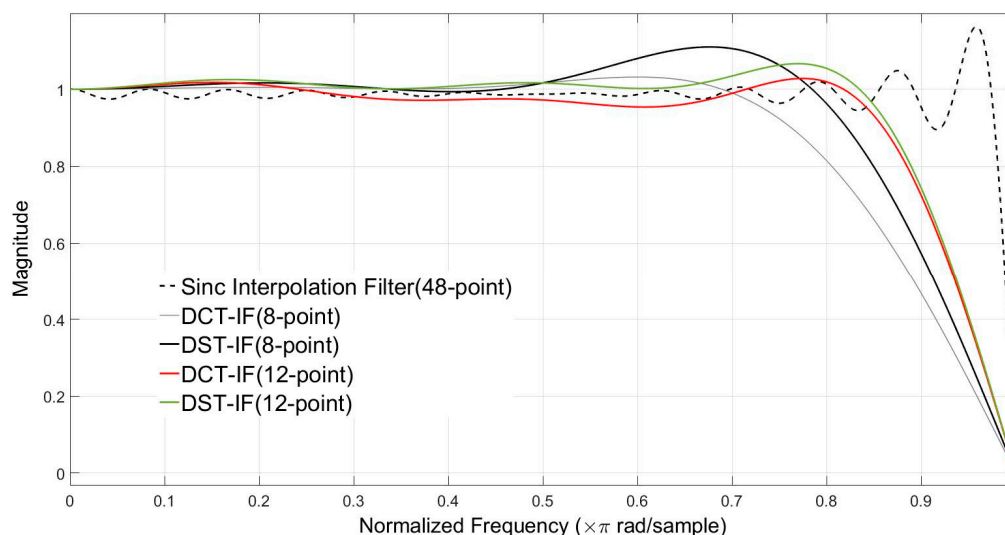
101 **Table 4.** 12-point and 11-point DCT-II-based Interpolation-Filter (DCT-IF) Coefficients.

Index i	0	1	2	3	4	5	6	7	8	9	10	11
1/2-pixel filter[i]	-1	2	-4	7	-12	40	40	-12	7	-4	2	-1
1/4-pixel filter[i]	-1	2	-3	5	-11	58	18	-7	4	-2	1	

102
103 The 12-point and 11-point DST-IFs that interpolate the 1/2-pixel and 1/4-pixel interpolations are
104 shown in Table 3. The 12-point and 11-point DST-IFs in Table 3 are derived in this paper from
105 Equation (8), where $N = 12$ and $n = 5.5$ and $N = 11$ and $n = 5.25$, respectively. In the similar way, the
106 12-point and 11-point DCT-IFs in Table 4 are derived in this paper.

107

2.4 Analysis of the interpolation filters



108
109 **Figure 2.** Magnitude Responses of Interpolation Filters for the 1/2-pixel Position in the Luma Component.

110
111 Figure 2 shows all of the different graphs of the magnitude responses of the 1/2-pixel
112 interpolation filters. In the x-axis, the discrete time frequency $\hat{\omega}$ is normalized in the range of 0 to
113 1, where 1 corresponds to the π radian. The y-axis is the magnitude response. Figure 2 illustrates the
114 magnitude-response graphs of five (5) interpolation filters reconstructing the 1/2-pixel position. The
115 sinc function, which is assumed the ideal interpolation filter, is designed with a 48-point
116 interpolation filter and represented by a dot-line. The 48-point sinc interpolation filter has relatively
117 high frequency response even around $\hat{\omega} = 0.9\pi$ compared with other interpolation filters such as
118 8-point DCT-IF, 8-point DST-IF, 12-point DCT-IF, and 12-point DST-IF and it comprises many more
119 ripples at high frequencies compared with the other interpolation filters. In particular, in the low
120 frequency responses when $\hat{\omega} < 0.5\pi$, all interpolation filters have similar responses. It can be
121 interpreted that all five (5) interpolation filters have similar low frequency responses but the high
122 frequency responses are different. Comparing the 8-point DCT-IF drawn in a gray line and the
123 8-point DST-IF drawn in a black line, the 8-point DST-IF has relatively high frequency responses
124 compared with the 8-point DCT-IF around $\hat{\omega} = 0.9\pi$ even if the low frequency responses are quite

125 similar. In case of the 12-point DST-IF and 12-point DCT-IF, which are represented by a green and
 126 red line, two interpolation filters have relatively higher frequency responses than the 8-point
 127 DST-IF and 8-point DCT-IF even if the low frequency responses are quite similar. The 12-point
 128 DST-IF and the 12-point DCT-IF have similar high frequency responses because they have almost
 129 similar interpolation filter coefficients as shown in Table 3 and Table 4 where only the filter
 130 coefficients of integer pixel position 4,5,6,7 are different in 1/2-pixel filter coefficients. It means that
 131 12-point DST-IF and 12-point DCT-IF are similar when they are derived mathematically. Therefore,
 132 comparing the 12-point DST-IF with 8-point DCT-IF and DST-IF and 12-point DCT-IF in Figure 2,
 133 the 12-point DST-IF shows relatively high frequency responses, even though the 48-point sinc
 134 interpolation filter shows better high frequency responses than other four (4) interpolation filters.
 135

136 3. Experimental Results

137 3.1. Experimental Conditions

138 The proposed DST-IF was implemented in the HEVC reference software, HM-16.6 [12],
 139 according to the HEVC common-test conditions. Table 5 shows the test sequences where the
 140 sequences of the classes B, C, D, and E comprise the resolutions of 1080p, 832 × 480, 416 × 240, and
 141 720p, respectively, and the proposed method was applied when the quantization-parameter (QP)
 142 values were 22, 27, 32, and 37, respectively. Table 6 and Table 7 show the test sequences and the
 143 BD-rate gain compared with those of HM-16.6 for the Luma component in the LDB, low delay P
 144 (LDP), and RA configurations, respectively. The random access configuration has hierarchical B
 145 pictures (IBBBBBBBP) which have a GOP (Group of pictures) size of eight (8). The low delay
 146 structure is composed of the first I (intra) picture and following P (Predictive) pictures (IPPPPP...).
 147 The P pictures in the low delay structure are GPB's (Generalized P and B pictures), in which the P
 148 pictures are replaced by B pictures having the same two reference pictures.

149 The negative sign of the BD-rate represents the bit-saving of the proposed method compared
 150 with that of HM-16.6 in the same PSNR (peak signal-to-noise ratio) reference [13].

151 **Table 5.** Test Sequences used in HEVC Common-Test Conditions.

Class	Sequence name	Frame count	Frame rate	Bit Depth
B	Kimono	240	24 fps	8
B	ParkScene	240	24 fps	8
B	Cactus	500	50 fps	8
B	BQTerrace	600	60 fps	8
B	BasketballDrive	500	50 fps	8
C	RaceHorses	300	30 fps	8
C	BQMall	600	60 fps	8
C	PartyScene	500	50 fps	8
C	BasketballDrill	500	50 fps	8
D	RaceHorses	300	30 fps	8
D	BQSquare	600	60 fps	8
D	BlowingBubbles	500	50 fps	8
D	BasketballPass	500	50 fps	8
E	FourPeople	600	60 fps	8
E	Johnny	600	60 fps	8
E	KristenAndSara	600	60 fps	8

153 3.2. Experimental Results

154 **Table 6.** DST-IF Bit-saving Results applied to Uni- and Bi-directional Prediction.

Class	Sequence name	Saving Bits(%)					
		8-point and 7-point DST-IF			12-point and 11-point DST-IF / 12-point and 11-point DCT-IF		
		LDB	LDP	RA	LDB	LDP	RA
B	Kimono	0.3	1.2	0.2	0.6/0.5	2.5/0.5	0.2/0.3
B	ParkScene	0.8	2.1	0.3	1.7/1.3	3.9/1.6	0.5/0.9
B	Cactus	0.8	2.3	0.2	1.1/1.2	3.6/1.6	0.0/0.8
B	BasketballDrive	0.1	1.2	0.1	0.3/0.4	2.3/0.6	0.3/0.3
B	BQTerrace	1.5	5.3	1.0	2.7/3.4	8.6/4.4	1.5/2.3
C	RaceHorses	-0.9	0.3	-0.2	-1.2/-0.7	0.6/-0.1	-0.5/-0.2
C	BQMall	-0.2	1.3	-0.5	-0.5/-0.6	1.8/-0.2	-1.0/-0.5
C	PartyScene	-1.7	-0.2	-2.5	-3.5/-4.4	-1.7/-3.6	-4.5/-3.8
C	BasketballDrill	0.6	1.7	0.4	1.2/0.9	2.9/1.1	0.8/0.6
D	RaceHorses	0.1	0.8	-0.1	0.0/-0.2	1.2/0.0	-0.3/-0.2
D	BQSquare	-4.1	-0.4	-5.2	-7.5/-7.2	-2.9/-4.9	-9.0/-7.4
D	BlowingBubbles	-1.5	0.0	-1.8	-2.8/-3.1	-0.9/-2.2	-3.1/-2.4
D	BasketballPass	0.5	1.2	0.2	0.9/0.9	2.0/1.1	0.4/0.4
E	FourPeople	0.6	2.4	x	1.2/1.2	4.7/1.6	x
E	Johnny	0.5	4.4	x	1.0/1.9	9.0/2.3	x
E	KristenAndSara	0.6	2.4	x	1.2/1.5	5.5/1.4	x
Overall		-0.1	1.6	-0.6	-0.2/-0.2	2.7/0.3	-1.1/-0.7

155

156 HM-16.6 uses an 8-point filter and a 7-point filter for the 1/2-pixel and 1/4-pixel interpolations,
157 respectively. From Table 6, the average bit-saving (BD-rate gain) in the RA configuration was
158 improved by 0.6 % with the use of the 8-point DST-IF for 1/2-pixel and 7-point DST-IF for 1/4-pixel.
159 Especially, the result of BQSquare in Class D achieved a bit-saving up to 5.2 % in the RA
160 configuration. The average bit-savings of 0.6 % and 0.1 % were achieved in the RA and LDB
161 configurations, respectively. However, the average bit-saving was decreased by 1.6 % in the LDP
162 configuration. In Table 6, the 12-point and 11-point DST-IFs that were applied to HM-16.6 also
163 showed bit-saving in the RA and LDB configurations and bit-increasing (BD-rate loss) in the LDP
164 configuration. In Table 6, Class E sequences in the RA configuration are not experimented because
165 they are not experimental condition in the HEVC test. Those sequences are marked as x.

166 Interestingly, the DST-IFs in the LDP configuration show bit increments (BD-rate loss), while
167 the DST-IFs in the RA and LDB configurations show bit-savings. It's because the backward
168 (uni-directional) prediction using the decoded past pictures provides the incomplete
169 motion-compensated block compared with the bi-directional prediction that utilizes the average
170 pixel values of two different blocks that were derived by the forward and backward
171 motion-compensations for subsample interpolation. Therefore, the proposed 12-point and 11-point
172 DST-IFs are applied only on the bi-directional motion-compensated blocks. The 12-point and
173 11-point DST-IFs, which are almost the same filter coefficients as the 12-point and 11-point DCT-IFs,
174 are effective on the bi-directional prediction. Table 7 shows the results of the DST-IF bit-saving
175 results applied only on the bi-directional prediction. In the RA and LDB configurations, the 8-point
176 and 7-point DST-IFs achieved bit-savings of 0.7 % and 0.3 % compared with HM-16.6, respectively,
177 and the 12-point and 11-point DST-IFs achieved bit-savings of 1.4 % and 1.2 % compared with

178 HM-16.6, respectively. Table 7 shows the results of the 12-point and 11-point DCT-IFs as well. It
 179 shows bit-savings of 0.6% and 0.7% in the LDB and RA configurations compared with HM-16.6,
 180 respectively.

181 **Table 7.** DST-IF Bit-saving Results applied to Bi-directional Prediction.

Class	Sequence name	Saving Bits(%)			
		8-point and 7-point DST-IF		12-point and 11-point DST-IF / 12-point and 11-point DCT-IF	
		LDB	RA	LDB	RA
B	Kimono	0.1	0.1	0.1/0.1	0.0/0.2
B	ParkScene	0.2	0.1	0.0/0.3	0.0/0.6
B	Cactus	0.2	0.0	-0.4/0.2	-0.3/0.6
B	BasketballDrive	0.0	0.0	-0.1/0.1	-0.1/0.2
B	BQTerrace	1.1	0.8	0.4/2.3	0.8/2.0
C	RaceHorses	-0.7	-0.2	-1.3/-0.5	-0.6/-0.2
C	BQMall	-0.3	-0.6	-1.2/-0.9	-1.3/-0.5
C	PartyScene	-1.5	-2.4	-3.8/-3.7	-4.4/-3.5
C	BasketballDrill	0.2	0.2	0.3/0.2	0.2/0.3
D	RaceHorses	-0.1	-0.2	-0.3/-0.2	-0.5/-0.2
D	BQSquare	-3.7	-5.0	-8.3/-6.3	-9.1/-6.9
D	BlowingBubbles	-1.2	-1.7	-2.9/-2.4	-3.0/-2.1
D	BasketballPass	0.0	-0.1	-0.1/0.1	-0.1/0.2
E	FourPeople	0.4	x	-0.1/0.6	x/
E	Johnny	-0.4	x	-1.5/0.2	x
E	KristenAndSara	0.2	x	-0.2/0.5	x
Overall		-0.3	-0.7	-1.2/-0.6	-1.4/-0.7

182

183 **Table 8.** Results of the Computational Complexity of the Proposed Method in the Low Delay B (LDB)
 184 Configuration.

Computational Complexity		
Proposed Methods	Encoding Time (%)	Decoding Time (%)
HM-16.6 vs. 8- and 7-point DST-IFs (uni- and bi-directional predictions)	101	101
HM-16.6 vs. 8- and 7-point DST-IFs (bi-directional prediction only)	97	99
HM-16.6 vs. 12- and 11-point DST-IFs (uni- and bi-directional predictions)	118	113
HM-16.6 vs. 12- and 11-point DST-IFs (bi-directional prediction only)	104	107

185

186 Table 8 shows the computational-complexity results. As the 12-point and 11-point DST-IFs
187 reference four additional neighbor pixels compared with the 8-point and 7-point DST-IFs in HEVC,
188 when both the uni-directional and bi-directional predictions were applied, the computational
189 complexities in the encoding process and the decoding process were increased by 118 % and 113 %,
190 respectively. However, the 12-point and 11-point DST-IFs, which were applied on only the
191 bi-directional prediction, increased the computational complexity in the encoding process by 104 %
192 and in the decoding process by 107%. The computational-complexity of the 12-point and 11-point
193 DCT-IFs is almost same as that of the 12-point and 11-point DST-IFs. Even if the complexity of the
194 proposed 12-point and 11-point DST-IFs is increased compared with that of the existing 8-point and
195 7-point DCT-IFs in HEVC, the proposed method gives better bit-saving results than the existing
196 method.

197 For an alternative method, one interpolation filter was chosen between the DCT-IF and the
198 DST-IF, and this experiment has been tested using the coding unit-level rate-distortion optimization
199 [14], but the results are worse than those of Table 6 and Table 7 because one signaling bit is needed
200 to indicate which interpolation filter is used in the decoder side.

201 5. Conclusions

202 In this paper, DST-IF pairs of 12-point and 11-point filter lengths are proposed to achieve a
203 bit-rate reduction compared with the 8-point and 7-point DCT-IFs. Interestingly, the 12-point
204 DST-IF and the 12-point DCT-IF have similar high frequency responses because the 12-point DST-IF
205 and 12-point DCT-IF derived have almost similar interpolation filter coefficients as shown in Table
206 3 and Table 4. The experiment results show that the proposed DST-IF pairs achieved coding gains in
207 the RA and LDB configurations. However, as the bit-rate was increased in the LDP configuration
208 using the uni-directional prediction, the proposed DST-IF method was applied only on the
209 bi-directional prediction. Overall, the proposed 12-point and 11-point DST-IFs achieved average
210 BD-rate reductions of 1.4 % and 1.2 % compared with the 8-point and 7-point DCT-IFs in the RA and
211 LDB configurations of the Luma component, respectively. We believe this method can be
212 considered in the next video coding standard.

213

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