

Article

CFD Analysis on the Air-Side Thermal-Hydraulic Performance of Multi-Louvered Fin Heat Exchangers at Low Reynolds Numbers

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Abstract: The air side thermal hydraulic performance of multi-louvered aluminium fin heat exchangers is investigated. A detailed study was performed to analyse the thermal performance of air over a wide range of Reynolds number i.e. from 30 to 500. Air-side heat transfer coefficient and air pressure drop were calculated and validated over the mentioned band of Reynolds numbers. Critical Reynolds number was determined numerically and the variation in flow physics along with the thermal and hydraulic performance of microchannel heat exchanger associated with Re_{cri} has been reported. Moreover, a parametric study of the multi-louvered aluminium fin heat exchangers was also performed for 36 heat exchanger configurations with the louver angles (19–31°), fin pitches (1.0, 1.2, 1.4 mm) and flow depths (16, 20, 24 mm); and the geometric configuration exhibiting the highest thermal performance was reported. The air-side heat transfer coefficient and pressure drop results for different geometrical configurations were presented in terms of Colburn j factor and Fanning friction factor f , as a function of Reynolds number based on louver pitch.

Keywords: compact heat exchanger; louvered fins; heat transfer coefficient; friction factor

1. Introduction

Fin and tube heat exchangers have been widely used throughout the world as condensers and evaporators for refrigeration and air conditioning whether it be household, food processing or automotive industry. The thermal performance of the fin and tube heat exchanger is limited by several design factors like, wakes generated in the round tube, contact resistance and the distortion of the fins due to the tube expansion. The contact resistance problem can be solved by brazing the fins to the tube, but it still has its shortcomings. On the other hand, the flat tube louvered heat exchangers have been proven to be performance wise better by its counterpart due to its compactness hence providing a large heat transfer area in a small space with high heat transfer coefficients. Over years, multi-louvered fin and flat tube heat exchangers have replaced fin and tube heat exchangers. In the forced heat transfer, air side thermal resistance is the key factor, however the air-side thermal hydraulic performance of multi-louvered fin and flat tube heat exchangers depends on the louvered fin geometry such as fin and louver pitches, louver angle, and flow depth. Rigorous efforts have been made by the researchers to further improve its thermal performance by using experimental and numerical techniques.

Over the years, a number of heat transfer analyses have been performed in order to determine the air side heat transfer coefficient and pressure drop in terms of Colburn j factor and fanning friction factor f . A large number of experiments were performed by Chang and Wang [1], Kim and Bullard [2,3] and Kim et al [4,5] to calculate the air-side heat transfer and pressure drop data. Few investigators opted for the scaled up models for better understanding of flow patterns while others went for the numerical techniques to better predict the results to understand the shortcomings in experimental methods. Webb and Jung [6] compared the heat transfer ability of louvered fin flat tube geometry with fin tube geometry and reported that for same air side thermal capacity only half of the

volume is required in case of louvered fin flat tube geometry. They performed experiments using 6 one row samples with $L_\alpha = 30^\circ$, $0.48 \leq L_p/F_p \leq 1$ for $100 \leq Re_{Lp} \leq 2000$.

Webb and Lee [7] further studied the louvered fin flat tube geometry and compared flat tube heat exchanger with round tube heat exchanger showing less than half of the material was required for the same thermal performance using flat tube heat exchanger. The flow visualization study was performed first by Davenport [8], he predicted the flow at low Reynolds number was not able to pass through two adjacent louvers of fin because of thick boundary layer generation around the louvers. Many researchers followed the trend afterward and investigated air-side heat transfer coefficient and pressure drop. It should be mentioned here that the fin corrugation pattern (Z-shaped) used by the Davenport [9] is not common. Two different louver lengths of 7.8 and 12.7 mm were used while other louver dimensions were varied as $8^\circ \leq L_\alpha \leq 36^\circ$ and $0.94 \leq L_p/F_p \leq 2.24$ for Reynolds number range of $300 \leq Re_{Lp} \leq 4000$. Later on Achaichia and Cowell [10] confirmed this phenomenon, through heat transfer tests on 15 louvered fin flat tube geometries with the following specifications; $0.24 \leq L_p/F_p \leq 0.85$ and $22^\circ \leq L_\alpha \leq 30^\circ$ for $30 \leq Re_{Lp} \leq 1000$. They proposed j and f correlations for the air side based on their own experimental data. Sunden and Svantesson [11] also proposed j and f factor correlations based on their experimental data collected from the tests carried out on 6 one row samples with $14^\circ \leq L_\alpha \leq 34^\circ$ and $0.26 \leq L_p/F_p \leq 0.91$ for Reynolds number ranging from 100 to 700.

Sahnoun and Webb's [12] analytical model for heat transfer and friction data was validated by Chang and Wang [1], they performed tests on 27 samples with the following geometric parameters; $L_\alpha = 28^\circ$ and $0.60 \leq L_p/F_p \leq 0.85$ for $100 \leq Re_{Lp} \leq 800$. Chang and Wang [13-15] also developed a generalized j and f correlation for louver fin geometry with the help of large dataset consisting of 91 samples. Louver geometry design for the locomotive company was proposed by Huihua and Xuesheng [16], they performed an experimental study on the scaled up models by varying louver angles and fin pitch values. Aoki et al. [17] conducted experiments on heat transfer characteristics of different louvered fin geometries, varying louver angles, louver pitches and fin pitches. They reported that the air side heat transfer coefficient decreases at low Reynolds number as the fin pitch increases. Also, the heat transfer coefficient increases with the increase in the louver angle reaches a maximum value and then decreases. They reported the maximum values of air-side heat transfer coefficient at louver angle of 28° - 30° . Air-side heat transfer coefficient and friction losses for high surface area density louvered fins and flat tube heat exchanger were investigated by Rugh et al. [18]. They developed j and f factor correlation and reported a 25% increase in heat transfer and 110% increase in pressure drop for louvered fin geometry in comparison to the plain fin geometry.

Springer and Thole [19] performed both numerical and experimental study to determine the flow behaviour of different louvered fin configurations. They reported the flow characteristics at different Reynolds number values. 45 samples of louvered fin flat tube heat exchangers with different louver angles (15° - 29°), fin pitches (1.0, 1.2, 1.4 mm) and flow depths (16, 20, 24 mm) were experimentally tested for the air side Reynolds number of 100-600 by Kim and Bullard [2]. A huge dataset of results was gathered, analysed and the air side heat transfer coefficient and pressure drop were reported in terms of Colburn j factor and Fanning friction f factor, as a function of Reynolds number. Dejong and Jacobi [20] investigated the phenomenon of vortex shedding in the louver geometry, the vortex shedding starts at the end louver and moves up with the increase in the Reynolds number. It was further reported that this vortex shedding phenomenon starts at critical Reynolds number, and it decreases with the increase in louver angle and decrease in fin pitch. Kim and Cho [21] performed experiments on louvered fin flat tube geometry over a wide range of Reynolds number i.e. from 40 to 1000, on 12 samples with the following set of dimensions; $15^\circ \leq L_\alpha \leq 27^\circ$, $1.21 \leq L_p/F_p \leq 1.70$ and fin pitches of (1.0, 1.2, 1.4 mm). They studied the critical Reynolds number by performing the experiments at air velocities as low as 0.3 m/s. It was reported that critical Reynolds number is where the eddies and vortices start to appear around the louvers and there is a peak noticed in the Colburn j factor curve at this point and a fall-off of the j factor curve occurs as the Reynolds number is further decreased. Kim and Cho reported that this critical Reynolds number is insensitive to the louver angle and decreases as the ratio of louver pitch to fin pitch decreases. They also asserted on the basis of their experimental results that existing correlations of critical Reynolds number do not predict the data adequately, but no new correlation of critical Reynolds number was

purposed. They compared their results with the existing j and f correlations and new correlations were proposed as none of the previous ones fully predicted the data.

Further efforts were put up for the numerical study to gather detailed flow patterns over the louvered fin flat tube heat exchangers. Achaichia and Cowell [22] modelled one louver in the fully developed flow region applying periodic boundary condition and categorized the flow into duct directed and louver directed. At low velocities, the flow was mainly duct directed due to the thick boundary layers around the louvers while, at higher velocities the flow was parallel to the louvers and was mostly louver directed. Flow efficiency was introduced by Webb and Trauger [23], they used large scale models for flow visualization experiments. They explained it as the ratio of louver directed flow to the total flow through the fins. They further reported that the flow efficiency increases with the fin pitch decrease and the Reynolds number increase. Numerical time-dependent study of the two-dimensional and three-dimensional model of the louvered fin flat tube heat exchanger was done by Atkinson et al. [24]. Reportedly, three-dimensional model presented better results than two-dimensional model. Tafti et al. [25] studied the flow transition and the instabilities within the louvered fin flat tube heat exchanger. They conducted two-dimensional, time-dependent study and reported that the instability noticed at the end louver moves upstream as the Reynolds number is increased. Perrotin and Clodic [26] performed numerical study along with a small set of experiments. They also conducted two-dimensional study to understand the turbulence in the louvered fin flat tube geometry with the increase in Reynolds number. They compared their results with previous studies in terms of j and f factors. An offset was noticed in the results since the two-dimensional model over-predicted the data due to unrealistic assumptions and three-dimensional model under-predicted the data due to the limitations in mesh and computational resources.

The literature review shows that most of the experimental and numerical studies were performed for Reynolds number higher than 100. Only a couple of studies were found that focused on the low Reynolds number range i.e. below 100. Achaicha and Cowell [22] conducted the study that includes the air side analysis of louvered fin flat plate heat exchangers up to Reynolds number value of 30, but that was for geometries with $L_p/F_p < 1.0$. Later, Kim and Cho [21] presented an experimental study with Reynolds number values as low as 30, for louvered fin flat tube geometries with $L_p/F_p > 1.0$. Two separate Colburn j factor correlations were developed for Reynolds number values of higher and lower than 150. And although the existing correlations for critical Reynolds number were reported invalid, no new critical Reynolds number correlation was proposed. Table 1 shows the summary of the previously conducted studies on the louvered fin flat tube heat exchangers along with the geometric dimensions considered in each study. Recently, Shinde and Lin [30] performed an experimental study using 26 heat exchanger samples obtained from manufacturers of United States, Europe, and Asia. The parameters of the heat exchangers were, fin pitch of 7-21.17 FPI, fin height of 5.6-10 mm, fin thickness of 0.08-0.17 mm, louver pitch of 0.9-2.44 mm, louver angle of 20-34°, louver length of 5.97-7.87 mm, tube height of 1.5-4.19 mm, tube depth of 12-30 mm, fin depth of 12-30 mm. Air-side heat transfer and pressure drop data were reported for all 26 samples in terms of j and f factors and were compared. They also proposed two correlations for low ($20 < Re \leq 80$) and high range ($80 < Re \leq 200$) of Reynolds number for both j and f factors based on their experimental data. Table 2 shows the list of j and f factor correlations published by several authors till now along with operational limitations.

Table 1. Literature review summary

Researchers	L_p (mm)	L_α (deg)	F_p (mm)	F_d (mm)	L_p/F_p	Re_{Lp}
Webb and Jung [6]	1.0-1.4	30	1.4-2.1	-	0.48-1.0	100-2000
Davenport [9]	1.5-3.0	8-36	1.0-1.6	-	0.94-2.24	300-4000
Achaichia and Cowell [10]	0.8-1.4	22-30	1.7-3.3	41.6	0.24-0.85	30-1000
Sunden and Svantesson [11]	0.8-1.5	14-34	1.5-2.0	-	0.26-0.91	100-700
Chang and Wang [1]	1.3-1.9	28	1.8-2.2	16-19	0.60-0.85	100-800
Kim and Bullard [2]	1.7	15-29	1.0-1.4	16-24	1.21-1.70	100-500
Kim and Cho [21]	1.7	15-27	1.0-1.4	20	1.21-1.70	30-1000
Present study	1.7	19-31	1.0-1.4	16-24	1.21-1.70	30-250

Table 2. Published j and f correlations

S. No.	Authors	Correlations	Operation range
1.	Davenport (1983)	$j = 0.249 Re_{Lp}^{-0.42} L_h^{0.33} \left(\frac{L_l}{H}\right)^{1.1} H^{0.26}$ $f = 5.47 Re_{Lp}^{-0.72} L_h^{0.37} \left(\frac{L_l}{H}\right)^{0.89} L_p^{0.2} H^{0.23}$ $f = 0.494 Re_{Lp}^{-0.39} L_h^{0.33} \left(\frac{L_l}{H}\right)^{1.1} H^{0.26}$	L_h is louver height j correlated for $Re_{Lp} = 300 - 4000$ f correlated for $Re_{Lp} = 70 - 4000$
2.	Achaichia and Cowell (1988)	$St = 1.54 Re_{Lp}^{-0.57} \left(\frac{F_p}{L_p}\right)^{-0.19} \left(\frac{T}{L_p}\right)^{-0.11} \left(\frac{L_h}{L_p}\right)^{-0.15}$ $f = 0.895 f_A^{1.07} F_p^{-0.22} L_p^{0.25} T^{0.26} L_h^{0.33}$ $f = 10.4 Re_{Lp}^{-1.17} F_p^{-0.05} L_p^{1.24} L_h^{0.25} T^{0.83}$	T = Transverse tube pitch Correlated for $Re_{Lp} = 150 - 3000$

3.	Chang et al. (1994)	$j = 0.291 Re_{Lp}^{-0.589} \varepsilon^{0.438}$ $f = 0.805 Re_{Lp}^{-0.514} \left(\frac{F_p}{L_p}\right)^{-0.72} \left(\frac{H}{L_p}\right)^{-1.22} \left(\frac{L_l}{L_p}\right)^{1.97}$	Re_{Lp} operational range 100 – 700 $\varepsilon = \frac{A_o}{A_{to}} = 7 - 12$
4.	Chang and Wang (1997)	$j = Re_{Lp}^{-0.49} \left(\frac{\theta}{90}\right)^{0.27} \left(\frac{F_p}{L_p}\right)^{-0.14} \left(\frac{F_l}{L_p}\right)^{-0.29} \left(\frac{T_d}{L_p}\right)^{0.23} \left(\frac{L_l}{L_p}\right)^{0.68} \left(\frac{T_p}{L_p}\right)^{-0.28} \left(\frac{\delta}{L_p}\right)^{-0.05}$	Re_{Lp} operational range 100 – 700 $Re_{Lp} = 100 - 3000$
5.	Chang et al. (2000)	$f = f1 * f2 * f3$ $f1 = 14.39 Re_{Lp}^{\left(-\frac{0.805 F_p}{F_l}\right)} \left(\log_e \left(1.0 + \left(\frac{F_p}{L_p}\right)\right)\right)^{3.04}$ $f1 = 4.97 Re_{Lp}^{0.6049 - 1.064/\theta^{0.2}} \left(\log_e \left(\left(\frac{F_p}{L_p}\right)^{0.5} + 0.9\right)\right)^{-0.527}$ $f2 = \left(\log_e \left(\left(\frac{\delta}{F_p}\right)^{0.48} + 0.9\right)\right)^{-1.435} \left(\frac{D_h}{L_p}\right)^{-3.01} (\log_e(0.5 Re_{Lp}))^{-3.01}$ $f2 = \left(\left(\frac{D_h}{L_p}\right) \log_e(0.3 Re_{Lp})\right)^{-2.966} \left(\frac{F_p}{L_l}\right)^{-0.7931 \left(\frac{T_p}{T_h}\right)}$ $f3 = \left(\frac{F_p}{L_l}\right)^{-0.308} \left(\frac{F_d}{L_l}\right)^{-0.308} \left(e^{\frac{0.1167 T_p}{D_m}}\right) \theta^{0.35}$ $f3 = \left(\frac{T_p}{D_m}\right)^{-0.0446} \log_e \left(1.2 + \left(\frac{L_p}{F_p}\right)^{1.4}\right)^{-3.553} \theta^{-0.477}$	Correlated for $Re_{Lp} < 5000$
6.	Kim and Bullard (2002)	$j = Re_{Lp}^{-0.487} \left(\frac{\theta}{90}\right)^{0.257} \left(\frac{F_p}{L_p}\right)^{-0.13} \left(\frac{H}{L_p}\right)^{-0.29} \left(\frac{F_d}{L_p}\right)^{-0.235} \left(\frac{L_l}{L_p}\right)^{0.68} \left(\frac{T_p}{L_p}\right)^{-0.279} \left(\frac{\delta}{L_p}\right)^{-0.05}$	$Re_{Lp} = 100 - 600$ Correlated for $\frac{F_p}{L_p} < 1$

		$f = Re_{Lp}^{-0.781} \left(\frac{\theta}{90}\right)^{0.444} \left(\frac{F_p}{L_p}\right)^{-1.682} \left(\frac{H}{L_p}\right)^{-1.22} \left(\frac{F_d}{L_p}\right)^{0.818} \left(\frac{L_l}{L_p}\right)^{1.97}$	
7.	Jacobi et al. (2005)	$j = \frac{aRe_{Lp}^b}{Re_{Lp}^b + d}$ $\frac{j_{modified}}{j_{Chang\&Wang}} = \frac{1.1Re_{Lp} \cosh\left(0.4\left[\left(\frac{F_p}{L_p}\right) - 1\right]\right)}{Re_{Lp} + 24 - 3\left(\frac{F_p}{L_p}\right)}$	a, b, c and d depend on the specimen. $j_{Chang\&Wang}$ is j correlation proposed in 1997.
8.	Dong et al. (2007)	$j = 0.26712Re_{Lp}^{-0.1944} \left(\frac{\theta}{90}\right)^{0.257} \left(\frac{F_p}{L_p}\right)^{-0.5177} \left(\frac{H}{L_p}\right)^{-1.9045} \left(\frac{L_h}{L_p}\right)^{1.7195} \left(\frac{F_d}{L_p}\right)^{-0.2147} \left(\frac{\delta}{L_p}\right)^{-0.05}$ $f = -0.54486Re_{Lp}^{-0.3068} \left(\frac{\theta}{90}\right)^{0.444} \left(\frac{F_p}{L_p}\right)^{-0.9925} \left(\frac{H}{L_p}\right)^{0.5448} \left(\frac{F_d}{L_p}\right)^{0.0688} \left(\frac{L_h}{L_p}\right)^{-0.2003}$	$Re_{Lp} = 200 - 2500$ Correlated for $\frac{F_p}{L_p} > 1$
9.	Kim and Cho (2008)	$j = 0.705Re_{Lp}^{-0.477} \left(\frac{\alpha}{90}\right)^{0.271} \left(\frac{L_p}{F_p}\right)^{0.155}$ $j = 0.0311Re_{Lp}^{0.183} \left(\frac{\alpha}{90}\right)^{0.0475} \left(\frac{L_p}{F_p}\right)^{-1.25}$ $f = 8.42Re_{Lp}^{-0.560} \left(\frac{\alpha}{90}\right)^{0.493} \left(\frac{L_p}{F_p}\right)^{0.535}$	First j correlation is valid for $Re_{Lp} > 150$ while second one is valid for $Re_{Lp} < 150$. f is correlated for the entire Reynolds range.
10.	Li and Wang (2010)	$j = 0.0883Re_{Lp}^{-0.289} N^{0.092} \left(\frac{\theta}{90}\right)^{2.019} \left(\frac{F_p}{L_p}\right)^{-0.293} \left(\frac{H}{L_p}\right)^{0.366} \left(\frac{L_h}{L_p}\right)^{-0.073} \left(\frac{F_d}{L_p}\right)^{-0.327} \left(\frac{\delta}{L_p}\right)^{-1.548}$ $f = 0.0171Re_{Lp}^{-0.437} N^{0.41} \left(\frac{\theta}{90}\right)^{2.4} \left(\frac{F_p}{L_p}\right)^{-0.776} \left(\frac{H}{L_p}\right)^{0.062} \left(\frac{L_h}{L_p}\right)^{0.334} \left(\frac{F_d}{L_p}\right)^{0.157} \left(\frac{\delta}{L_p}\right)^{-3.313}$	Operational for $Re = 400 - 1600$ N is number of louver regions since the correlation is proposed for multi-region louvers. Re is based on hydraulic diameter.
11.	Li et al. (2011)	$j = 0.2162Re_{Dc}^{-0.351} \left(\frac{F_d}{D_c}\right)^{-0.875} \left(\frac{H}{D_c}\right)^{0.426} \left(\frac{F_p}{D_c}\right)^{-0.543} \left(\frac{\delta}{D_c}\right)^{0.12}$ $f = 0.4183Re_{Dc}^{-0.506} \left(\frac{F_d}{D_c}\right)^{0.69} \left(\frac{H}{D_c}\right)^{1.382} \left(\frac{F_p}{L_p}\right)^{-1.837} \left(\frac{\delta}{L_p}\right)^{0.062}$	$Re_{Dc} = 200 - 1730$ D_c is the hydraulic diameter.

12.	Shinde and Lin (2016)	$j = Re_{Lp}^{-0.324} \left(\frac{F_p}{L_p}\right)^{-0.2} \left(\frac{H}{L_p}\right)^{-2.3} \left(\frac{\delta}{L_p}\right)^{-0.001} \left(\frac{\theta}{90}\right)^{1.1} \left(\frac{L_l}{L_p}\right)^{1.72} \left(\frac{D_m}{L_p}\right)^{1.88} \left(\frac{F_d}{L_p}\right)^{-0.195}$ $j = Re_{Lp}^{-0.4} \left(\frac{F_p}{L_p}\right)^{-0.07} \left(\frac{H}{L_p}\right)^{-2.48} \left(\frac{\delta}{L_p}\right)^{-0.006} \left(\frac{\theta}{90}\right)^{0.09} \left(\frac{L_l}{L_p}\right)^{1.83} \left(\frac{D_m}{L_p}\right)^{1.65} \left(\frac{F_d}{L_p}\right)^{-0.012}$ $f = Re_{Lp}^{-0.87} \left(\frac{F_p}{L_p}\right)^{-0.06} \left(\frac{H}{L_p}\right)^{-0.014} \left(\frac{\delta}{L_p}\right)^{-1.35} \left(\frac{\theta}{90}\right)^{0.67} \left(\frac{L_l}{L_p}\right)^{0.007} \left(\frac{D_m}{L_p}\right)^{0.83} \left(\frac{F_d}{L_p}\right)^{0.019}$ $f = Re_{Lp}^{-0.856} \left(\frac{F_p}{L_p}\right)^{-0.016} \left(\frac{H}{L_p}\right)^{-0.01} \left(\frac{\delta}{L_p}\right)^{-1.1121} \left(\frac{\theta}{90}\right)^{0.74} \left(\frac{L_l}{L_p}\right)^{0.31} \left(\frac{D_m}{L_p}\right)^{0.53} \left(\frac{F_d}{L_p}\right)^{0.053}$	<p>D_m is tube height</p> <p>First j and f correlation is valid for $20 < Re_{Lp} \leq 200$</p> <p>Second j and f correlation is valid for $20 < Re_{Lp} \leq 200$</p>
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The present study numerically investigates the thermal hydraulic performance of multi-louvered fin and flat tube heat exchangers using 36 heat exchanger models with different louver angles (19° - 31°), flow depths (16, 20, 24 mm) and $1.21 \leq L_p/F_p \leq 1.70$ over a Reynolds number range of 30 to 500. The heat transfer coefficient and pressure drop data for heat exchangers with different geometrical configurations are reported in terms of the Colburn j factor and Fanning friction factor f , as a function of Reynolds number based on the louver pitch. The geometric configuration showing best thermal performance for low Re range was reported. Also, the effect of louvered fin parameters on the critical Reynolds number is investigated. Critical Reynolds number was determined numerically and the variation in flow physics along with the thermal and hydraulic performance of microchannel heat exchanger associated with Re_{cri} has been reported.

2. Geometry and computational model

2.1 Geometric model

A total of 36 heat exchanger configurations having three different flow depths (16, 20, 24 mm), three different fin pitches (1.0, 1.2, 1.4 mm) and four different louver angles (19° , 23° , 27° , 31°) were considered for numerical analysis. The fin thickness and louver pitch value for all computational models was kept constant at 0.1 and 1.7 mm respectively. The analysis was performed under conditions mimicking the actual test environment. The inlet air temperature was fixed at 21°C , and since the tube-side thermal resistance needs to be minimized in order to accurately predict the air-side heat transfer coefficient, the tube temperature was kept constant at 45°C across the flow depth. Geometric dimensions for the heat exchanger models used for analysis are mentioned in detail, in Fig. 1 and Table 3.

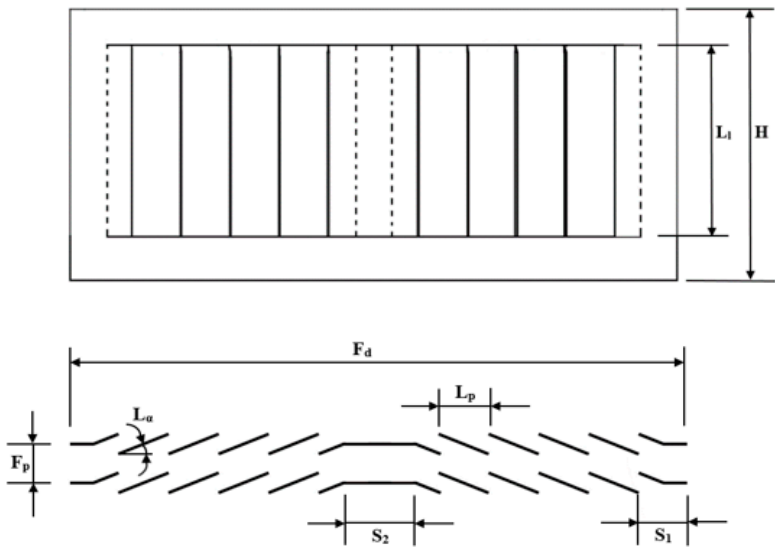


Figure 1. Geometric parameters

Table 3. Geometric specifications of modelled heat exchangers

F_d (mm)	F_p (mm)	L_p (mm)	L_{α} (deg.)	L_l (mm)	H (mm)	S_1 (mm)	S_2 (mm)	N_l
16	1.0, 1.2, 1.4	1.7	19, 23, 27, 31	6.4	8.15	1.70-1.79	0.77	8
20	1.0, 1.2, 1.4	1.7	19, 23, 27, 31	6.4	8.15	1.70-1.79	1.24	10
24	1.0, 1.2, 1.4	1.7	19, 23, 27, 31	6.4	8.15	1.70-1.79	1.79	12

The thermophysical properties of three-dimensional steady state model with air as fluid and aluminium as solid material are as following. Air was used as an ideal gas and its thermal properties were calculated at the arithmetic mean air temperature within the computational domain. The air viscosity is calculated from Sutherland Equation. Thermal conductivity of aluminium is 202.4 W/mK.

2.2 Governing Equations

A steady state laminar flow analysis was performed for all geometric models considering the fact that flow has been proven to be laminar in the compact heat exchangers up to Reynolds number value of 1200. The conservation of mass, momentum and energy equations used in an inertial reference frame for steady state conditions are shown in (1), (2) and (3).

Continuity equation:

$$\nabla \cdot \rho \mathbf{u} = 0 \quad (1)$$

Momentum equation:

$$\rho(\mathbf{u} \cdot \nabla \mathbf{u}) = -\nabla p + \mu \nabla^2 \mathbf{u} \quad (2)$$

The energy equation in steady state conditions can be described as follows:

$$\rho c_p(\mathbf{u} \cdot \nabla T) = k \nabla^2 T \quad (3)$$

2.3 Numerical schemes and Boundary conditions

Steady state, absolute velocity formulation and pressure based setting were used to setup the cases while SIMPLE pressure velocity coupling was applied. Least Square Cell-Based method was implemented for computing gradients. Second order for pressure and second order upwind discretization scheme were used for momentum and energy equations.

Velocity inlet and pressure outlet boundary conditions were applied for the air inlet and outlet. Frontal air velocity value of 0.3 – 2.15 m/s corresponding to the louver pitch based Reynolds number of 30 – 500 was applied at the air inlet boundary while zero gauge pressure was kept at the pressure outlet boundary. The air domain was divided into three sub-domains; upstream, downstream and fin domain. The width of the upstream domain and downstream domain was kept fixed at 5 mm (four times fin pitch) and 15 mm (ten times fin pitch) respectively. This was to ensure that there were zero gradients of temperature, pressure and velocity at the inlet and outlet boundaries. Only half of the fin was modelled considering the number of simulations and computational cost. Symmetry boundary condition was applied to the transverse faces of upstream and downstream air domains. Symmetry boundary conditions are used when the physical geometry of interest and the expected pattern of the flow/thermal solution have mirror symmetry, which helps to reduce the extent of computational model to a symmetric subsection of the overall physical system. ANSYS Fluent assumes a zero flux of all quantities across a symmetry boundary. No slip boundary condition was imposed on all solid walls and a constant tube wall temperature of 318 K was applied at the transverse face of the fin domain. Periodic boundary condition was used for longitudinal faces of air domain in order to mimic fully developed flow and heat transfer. Periodic boundary condition allows creating a non-conformal periodic boundary interface. This helps to predict heat transfer in periodically repeating geometries, such as compact heat exchangers, by including only a single periodic module for analysis. The detailed schematic of the boundary conditions is shown in Fig. 2.

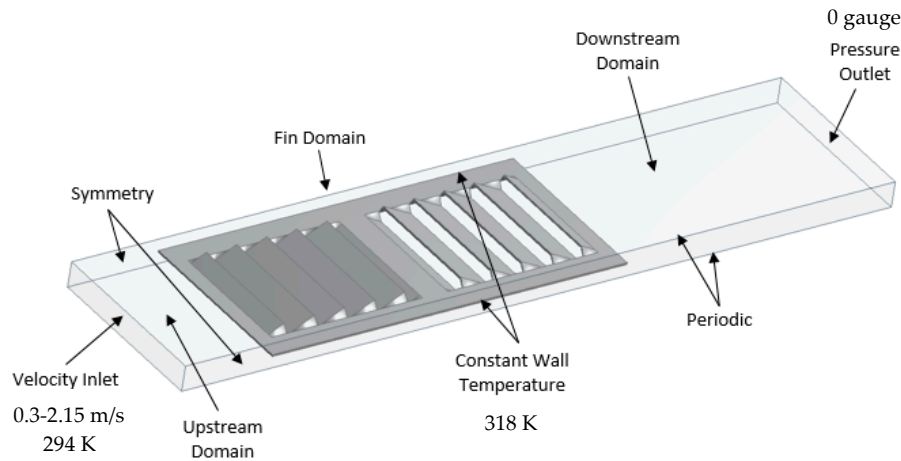


Figure 2. Three-dimensional computational domain and boundary conditions

3. Results and discussions

Conjugate heat transfer problem was solved in order to take fin conduction into account along with convection in air. Air-side heat transfer coefficient is calculated using the log mean temperature difference method for cross flow heat exchangers with both fluids unmixed. While the air-side heat transfer rate and air outlet temperature are computed numerically. The equations used for calculation of air-side heat transfer coefficient are shown in Eqs. (4-10).

$$\Delta T_m = \frac{(T_{ho} - T_{ci}) - (T_{hi} - T_{co})}{\ln\left(\frac{T_{hi} - T_{co}}{T_{ho} - T_{ci}}\right)} \quad (4)$$

Since the tube wall temperature is assumed constant ($T_{hi} = T_{ho} = T_w$), the expression for log mean temperature difference reduces to the following

$$\Delta T_m = \frac{(T_{co} - T_{ci})}{\ln\left(\frac{T_w - T_{ci}}{T_w - T_{co}}\right)} \quad (5)$$

And the air-side heat transfer coefficient is calculated using the heat transfer relation

$$Q = U_o A_o \Delta T_m \quad (6)$$

$$\frac{1}{U_o A_o} = \frac{1}{h_a A_a} + \frac{\delta_f}{k_f A_f} \quad (7)$$

Air-side heat transfer coefficient is represented in terms of Colburn j factor while air-side pressure drop is shown as Fanning friction factor f , using the equation given below

$$j = \frac{Nu}{Re_{Lp} Pr^{1/3}} \quad (8)$$

Where,

$$Re_{Lp} = \frac{\rho V_{cri} L_p}{\mu} \quad (9)$$

While,

$$f = \left(\frac{2\Delta P}{\rho V_{cri}^2} \right) \left(\frac{A_c}{A_a} \right) \quad (10)$$

3.1 Grid Independence study and data validation

Computational model consisting of solid and fluid domains was discretized using hexahedral elements. Same mesh topology was used to ensure conformal mesh interface between the two domains inorder to avoid interpolation losses. To resolve the thermal and viscous boundary layer effectively, O-grid was generated around the fins with varying near wall element sizes shown in Fig. 3. Therefore, four different mesh were generated using ICEMCFD with the sizes of 0.9, 1.7, 2.5 and 4.4 million elements. Grid independence study was performed using one of the modeled louvered fin flat tube heat exchanger geometry with following specifications; louver angle of 27°, $F_p=1.4$ mm and $F_d=20$ mm at the Reynolds number value of 350. The results gathered from all four mesh are reported in Fig. 4. Considering the minuscule difference in the results between M3 and M4, at twice the computational cost and also accounting for a very large number of simulations, mesh M3 was selected. This was done to ensure that computational analysis of the multi-louvered fin flat tube heat exchanger was independent of different mesh adaptations and mesh sizes.

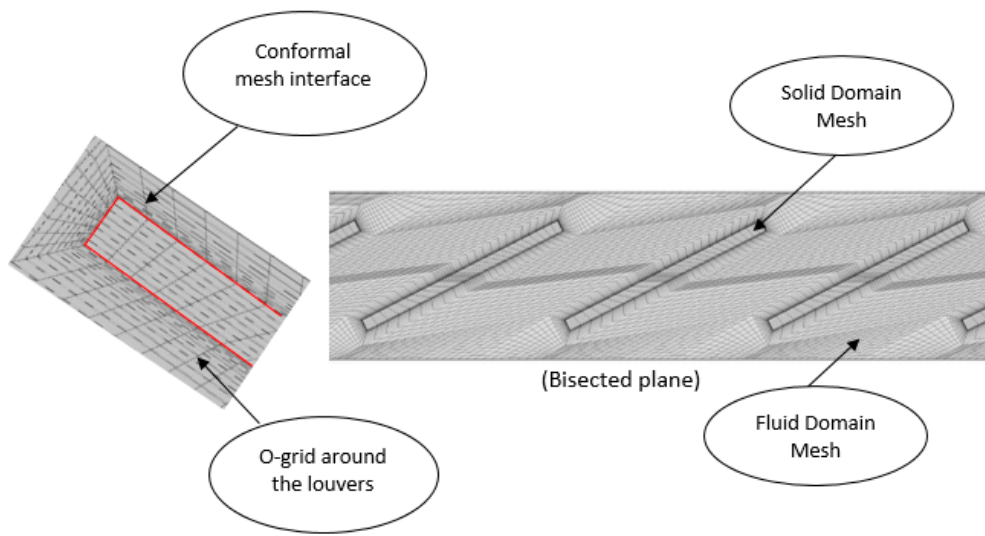


Figure 3. Mesh of fluid and solid domain on a bisected plan

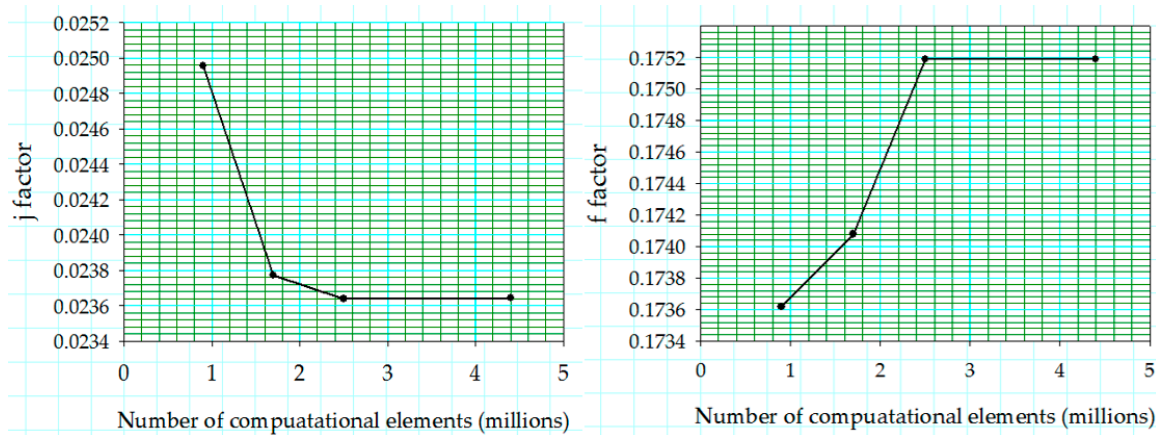


Figure 4. Mesh Independence study

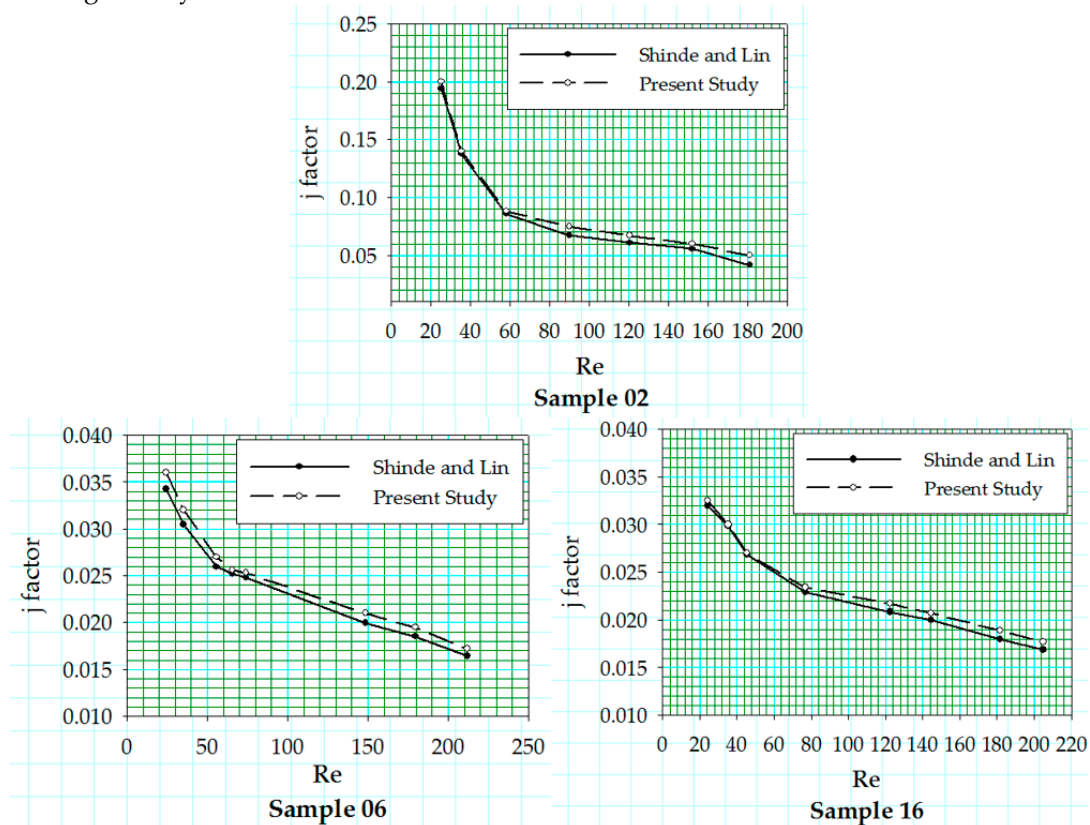
The near wall element sizes used to capture the boundary layer for four different mesh along with other mesh details are mentioned in Table 4.

Table 4. Mesh properties

Properties	M1	M2	M3	M4
Element size near wall (m)	1.80E-05	6.42E-06	4.12E-06	2.57E-06
Max. element size (m)	0.0002207	0.0001306	0.0001016	0.0000646
No. of elements	913674	1742105	2452481	4435015
No. of nodes	844560	1638900	2323584	4240800
Computation time/10 iterations (s)	170	316	466	931

3.2 Validation of numerical model

Three randomly selected louvered fin configurations from experimental study performed by Shinde and Lin [30], were modelled and analysed computationally. Sample 2 and 16 have the fin thickness value of 0.1 mm while sample 6 has the fin thickness value of 0.08 mm . The results were compared and reported in terms of nondimensionalized parameters, shown in Fig. 5, the two were found in well agreement. The j factor against low values of louver pitch based Reynolds number that is $20 \leq Re \leq 80$ agrees very well with the experimental data but a small offset is noticed for the higher range of Reynolds number.

**Figure 5.** Validation of numerical results with Shinde and Lin [30]

3.3 Effect of fin pitch

The effect of the fin pitch of the louvered fin was investigated by varying the fin pitch values at different louver angles. The results for air-side heat transfer coefficient are plotted in terms of Colburn j factor in Fig. 6, 7 and 8 at three different flow depths of 16, 20 and 24 mm respectively. The j factor increases with a decrease in fin pitch at high Reynolds number due to the reduction of boundary layer thickness, increasing the heat transfer while at low Reynolds number the boundary layer thickness is increased, reducing the heat transfer.

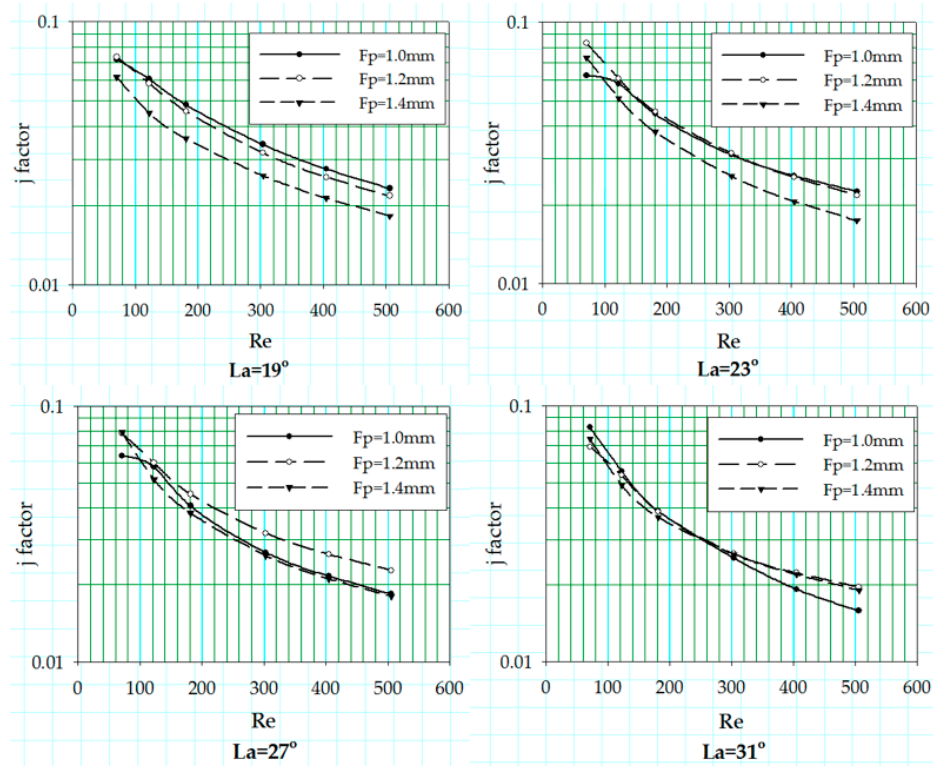


Figure 6. *j* factor corresponding to fin pitch variation at different louver angles with $F_d = 16$ mm

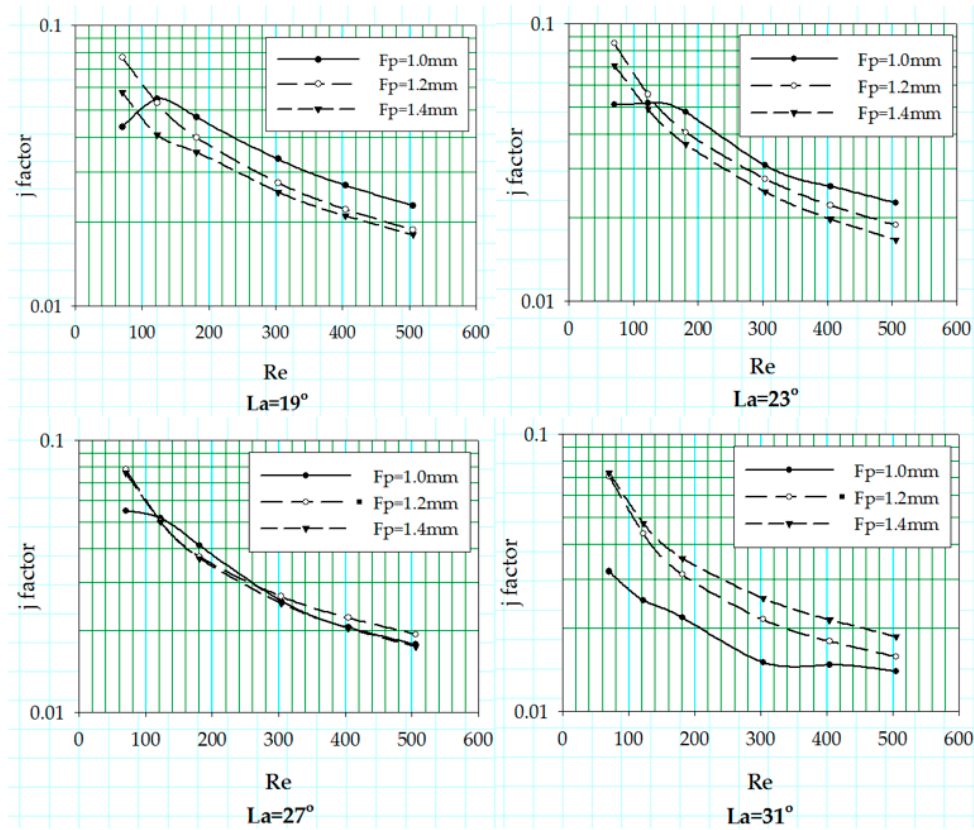


Figure 7. *j* factor corresponding to fin pitch variation at different louver angles with $F_d = 20$ mm

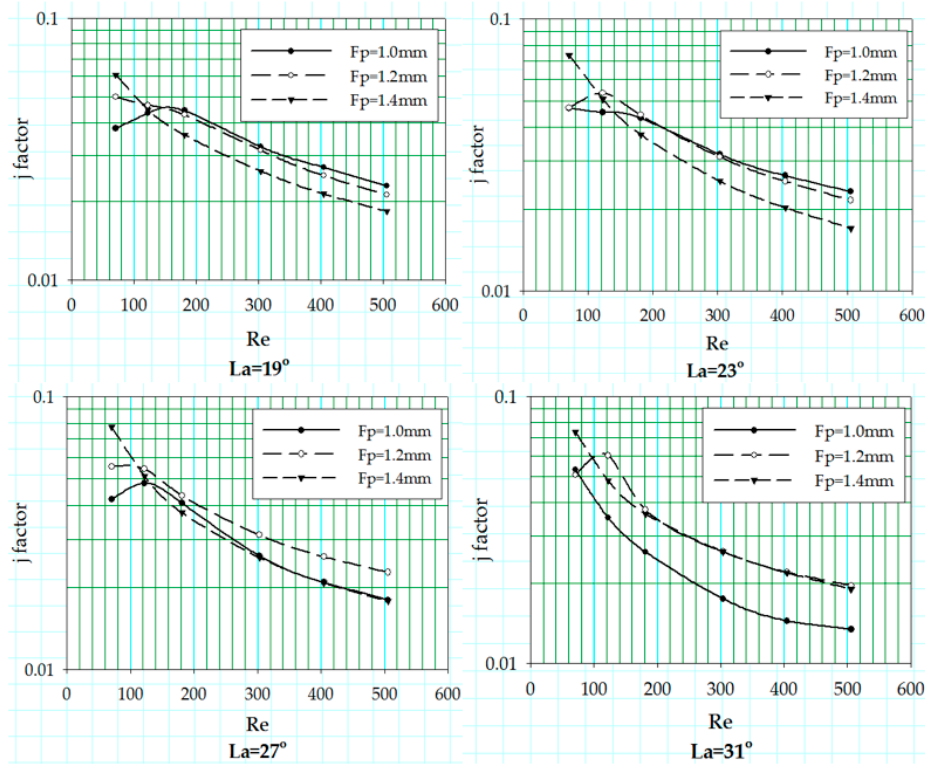


Figure 8. j factor corresponding to fin pitch variation at different louver angles with $F_d = 24$ mm

The air-side heat transfer coefficient is also strongly dependent on the relative angle between the corresponding louvers of adjacent fins. Whenever the louvers are oriented in a manner that the upstream louver reduces the effective surface area of downstream louvers available for heat transfer, the thermal performance reduces drastically. Thermal performance deteriorates significantly at low Reynolds number, when the configuration of the louvers is such that the louvers of adjacent fin rows are aligned. In such configuration, wake generated by trailing edge of the upstream louver covers the downstream louver completely. Moreover, Fig. 6 shows that as the louver angle increases the offset between the j factor curves for different fin pitch reduces due to the alignment of the neighboring louvers. Fin pitch increase at high louver angles is also most likely to deteriorate the thermal performance, since the flow is more likely to become duct directed with increasing fin pitch. The critical Reynolds number (fall-off of j factor) is only seen in the case of the fin geometry with fin pitch value of 1mm. This fall off of j factor is due to the alignment of neighboring fin louvers at those louver angles. Since fin pitch is inversely proportional to the flow efficiency, so as the fin pitch increases flow becomes more duct directed. Louver configurations along with flow profile variation for different fin pitch values are shown in Fig. 9. Webb and Trauger [23] introduced the flow efficiency as ratio of actual (N) to ideal (D) transverse distance, shown in Eq. (11).

$$\eta_f = \frac{N}{D} \quad (11)$$

The critical Reynolds number peak becomes more clear in Fig. 7 and 8, with flow depth of 20 and 24 mm, and this critical Reynolds number fall off disappears with the increase in louver angle. The critical Reynolds number is only seen for geometries with fin pitch of 1.0 and 1.2 mm. The underlying phenomenon for this j factor fall off is explained using Fig. 10, which shows the change in boundary layer generation around the louvers for fin geometry with fin pitch and flow depth value of 1mm and 24mm respectively, at four louver angles. It can be seen for louver angle 19°, 23° and 27°, that the downstream louver is not placed in the wake of upstream louver. This allows re-initialization of the boundary layer around the downstream louvers. In contrast, this re-initialization of boundary layer cannot be seen for louver angle of 31°, as the downstream louvers fall in the wake of upstream

louver. For geometry with fin pitch 1.0 mm and louver angle of 31° , the j factor curve shows a vast offset with other two curves associated to fin pitch values of 1.2 and 1.4 mm. This offset can be explained by the consequential deterioration of thermal performance caused by louver alignment, prohibiting the boundary layer re-initialization phenomenon. Fig. 8 shows an interrelation between the flow depth and the fin pitch of the louver configuration, when it comes to critical Reynolds number. The fall-off in the j factor curves also appears for the fin pitch 1.2 mm along with fin pitch value of 1.0 mm for the geometries with flow depth 24 mm. This may be because of change in flow physics due to increase in number of louvers.

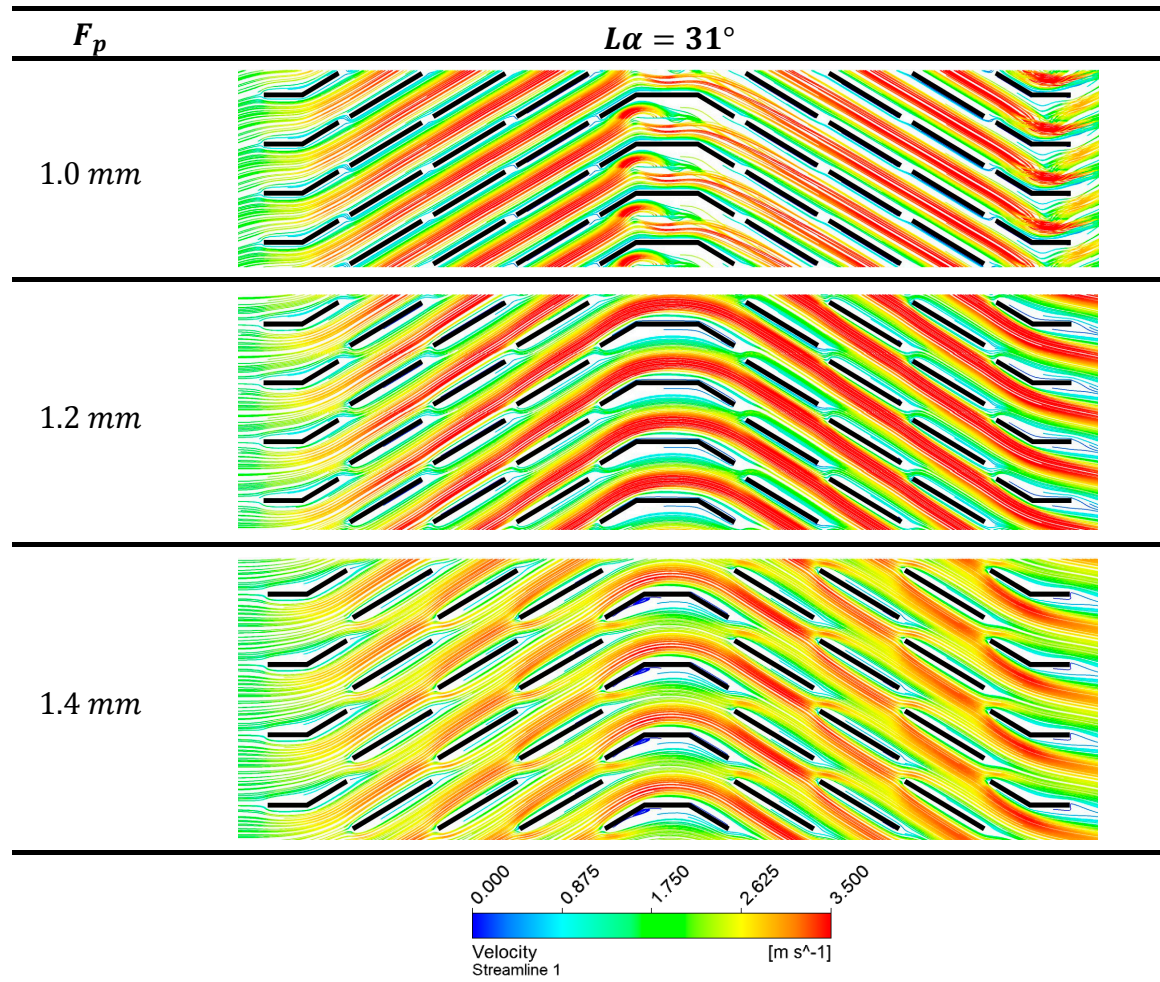


Figure 9. Louver alignment with reducing F_p

The Fanning friction factor values for different fin pitches are plotted as a function of Reynolds number at different louver angles ranging from 19° to 31° in Fig. 11, while the flow depth is set constant at 20 mm. Although the results show that there is no change in f factor curves pattern associated with the change in fin pitch values, but it depicts a drop in the f factor values as the fin pitch values increase from 1.0 to 1.4 mm.

Fig. 11 shows the f factor values at different louver angles with a variation of fin pitch, the f factor decreases with the increase in Reynolds number. The flow becomes aligned to the louvers with increasing Reynolds number resulting in low f factor values only due to the skin friction drag. While at low Reynolds number, form drag is also added to the skin friction drag consequently showing higher values of f factor. A clear offset is visible between the f factor curves associated to geometries with three different fin pitches for louver angle of 19° and it reduces as the louver angle increases. For geometries with fin pitch of 1.2 and 1.4 mm, the offset almost diminishes reaching the louver angle of 27° , but their offset with 1mm fin pitch geometry remains till the louver angle value of 31° .

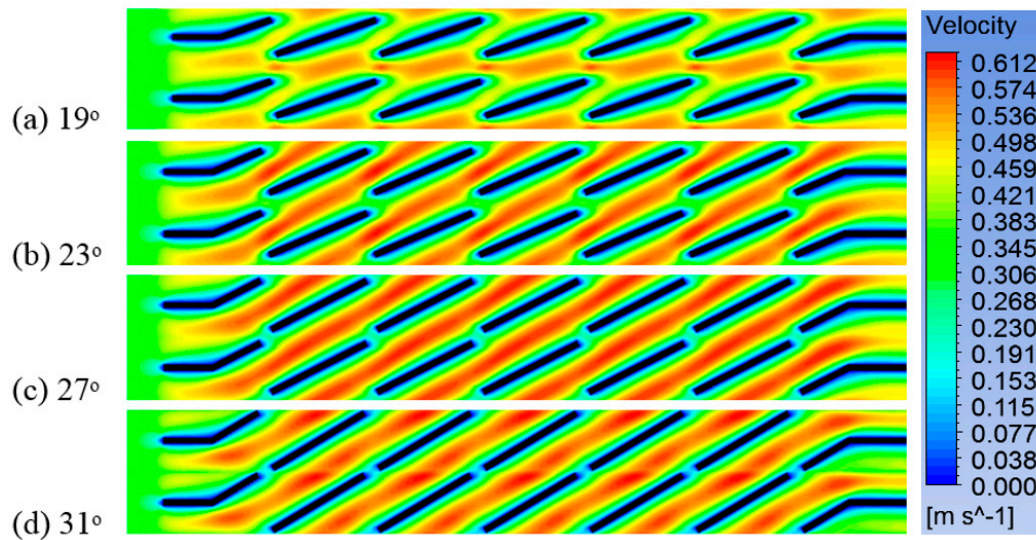


Figure 10. Velocity contours for geometry with $F_d=24$ mm and $F_p=1.0$ mm at different louver angles

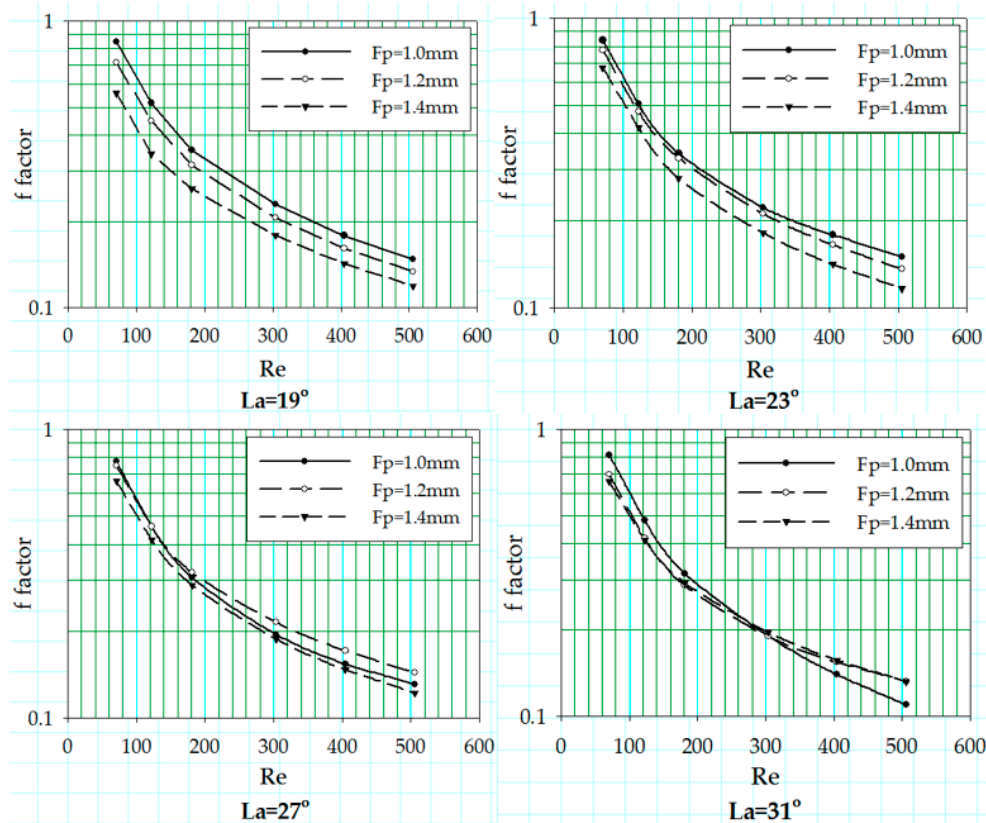


Figure 11. f factor corresponding to fin pitch variation at different louver angles with $F_d = 20$ mm

3.4 Effect of flow depth

Fig. 12 shows the air-side heat transfer coefficient in terms of j factor for the louvered fin geometries with fin pitch equal to 1.0 mm. A wide offset is noticed between the j factor curves corresponding to different flow depths at low Reynolds number, due to a significant decrease in thermal performance. This decrease is caused by the interference of upstream louver's trailing edge with the boundary layer of downstream louver resulting in increased ineffective heat transfer surface area. This offset diminishes with the increase in Reynolds number because of reduction in boundary layer thickness around louvers. In the case of louver angle 31° , the adjacent fin louvers are completely aligned and fin pitch is so small that the trailing edge of the boundary layer created around the

upstream louver does not get to dissipate and covers the rest of downstream louvers within its wake. This does not allow the downstream louvers to generate their respective boundary layer, badly affecting the thermal performance. The critical Reynolds number is only seen for the fin pitch of 1.0 and 1.2 mm when the louver angle is 19°, 23° and 27° however, critical Reynolds number peak can be seen for all three flow depths.

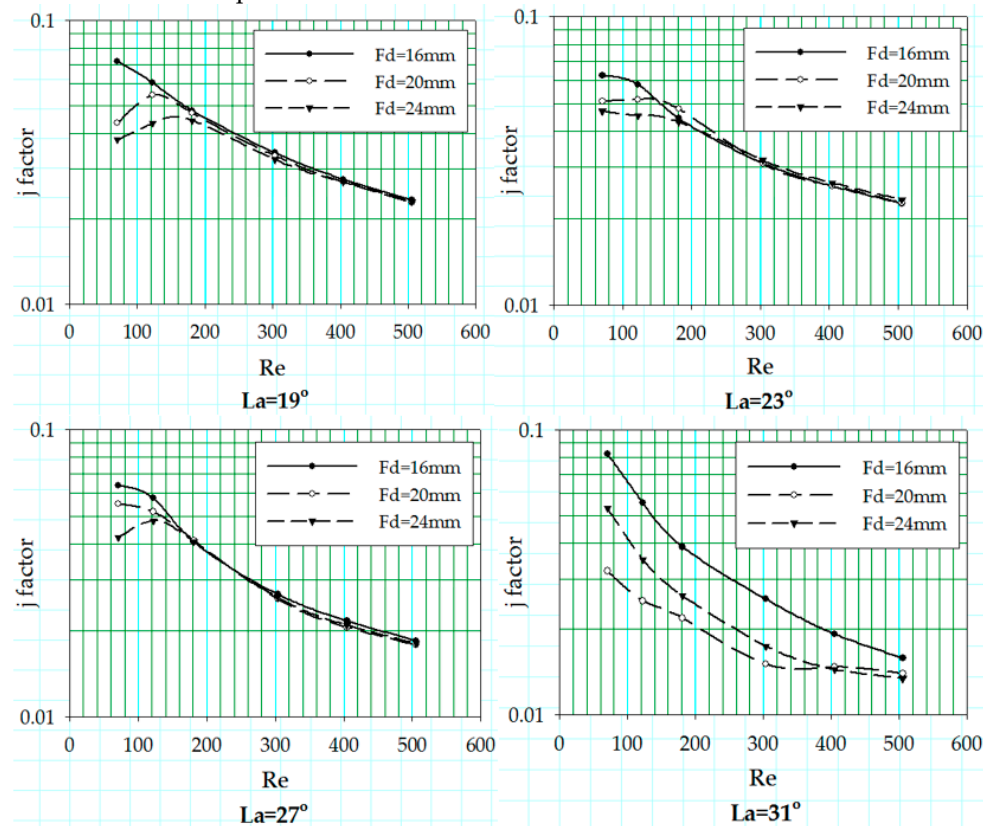


Figure 12. j factor corresponding to flow depth variation at different louver angles with $F_p = 1.0$ mm

No change is observed in the f factor with a variation of flow depth, f factor results for all three geometries with flow depths of 16, 20 and 24 mm overlap each other with miniscule offset. Also, the f factor values seem unresponsive to the change in louver angle, but a microscopic rise is noticed as the louver angle increases from 19° to 23°.

3.5 Effect of louver angle

3.5.1 Associated with change in F_p

The change in the heat transfer coefficient in terms of Colburn j factor is reported for the variation in louver angle associated with three different fin pitch values at fixed flow depth of 24 mm. The trend of the j factor curves against the Reynolds number of aforementioned geometric sets is shown in Fig. 13.

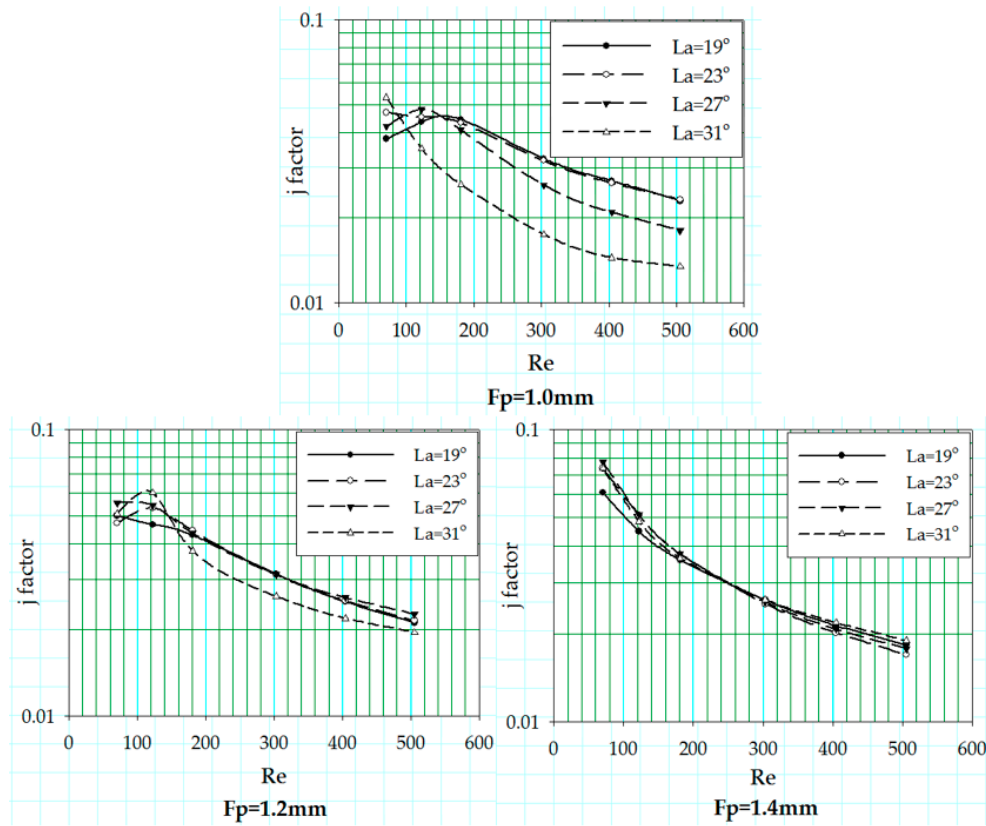


Figure 13. j factor values corresponding to louver angle variation at different fin pitches with $F_d = 24$ mm

An offset between the j factor curves associated with different louver angles is noticed that reduces with the fin pitch increase from 1.0 to 1.4 mm. A crossover of the j factor curves for different louver angles is also observed. This crossover of the j factor curves is probably due to the change in louver configuration with the changing louver angles, shown in Fig. 14. As the fin pitch values increase this crossover moves downstream towards increasing Reynolds number. Large louver angles show huge offsets between j factor curves at small fin pitch values due to the interference of upstream louver's trailing edge with downstream louver. Whereas, at large values of fin pitch, the trailing edge of upstream louver diminishes in the wake region before the flow reaches the downstream louver resulting in better thermal performance.

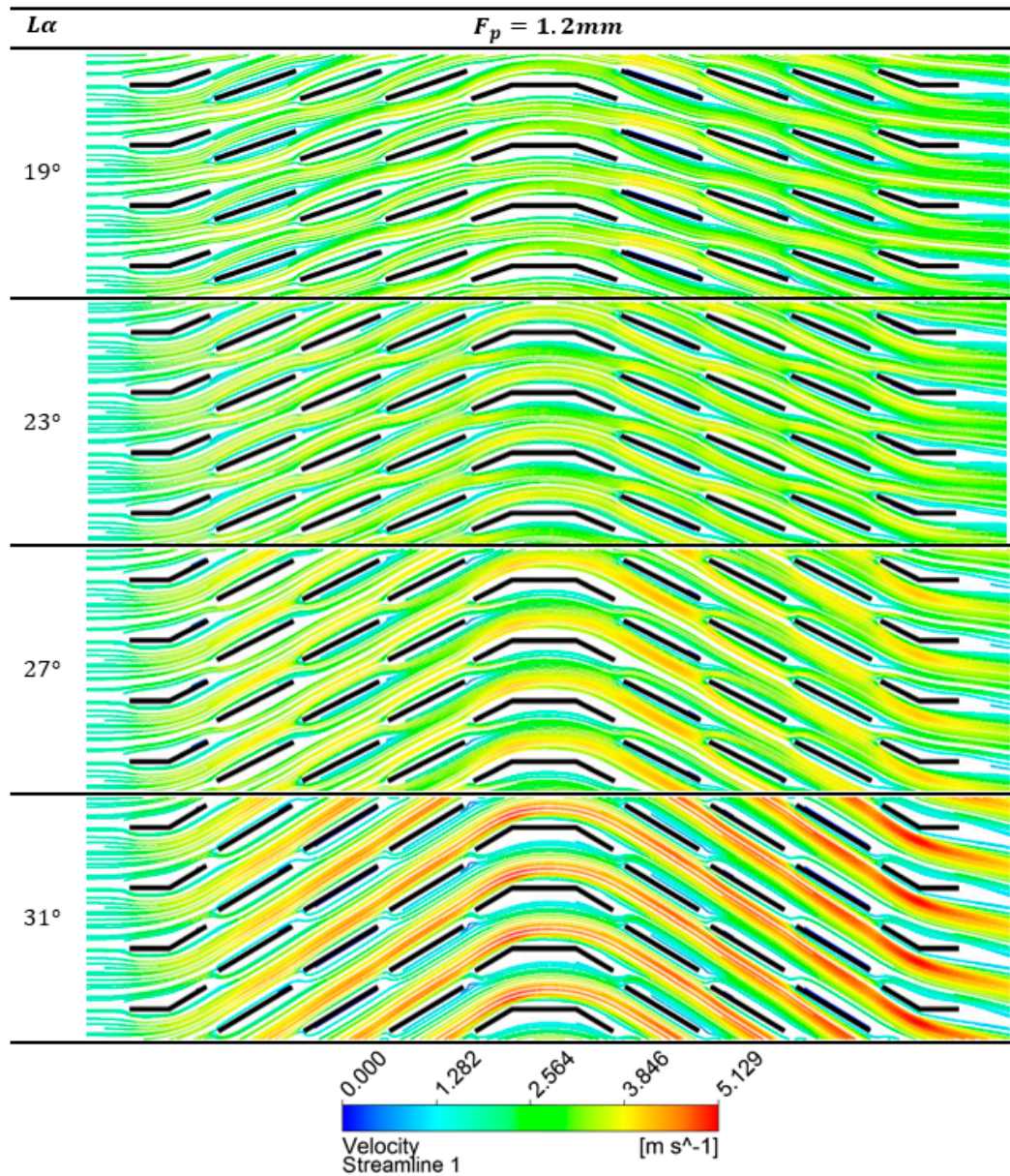


Figure 14. Louver alignment between adjacent fins with increasing $L\alpha$

3.5.2 Associated with change in F_d

The offset between the j factor curves at different louver angles was irresponsive to change in flow depth, but it decreased with the increase in fin pitch values.

In Fig. 15, two prominent offsets are noticeable, at low Reynolds number and high Reynolds number. In the case of low Re, the f factor for louver angle 19° is solely due to the skin drag, but as the louver angle increases form drag also makes a small contribution to the increase of friction factor. On the other hand, at high Reynolds number this variation in form drag with increasing louver angle amplifies. The friction factor curves at all four louver angles show no response to the flow depth variation at all.

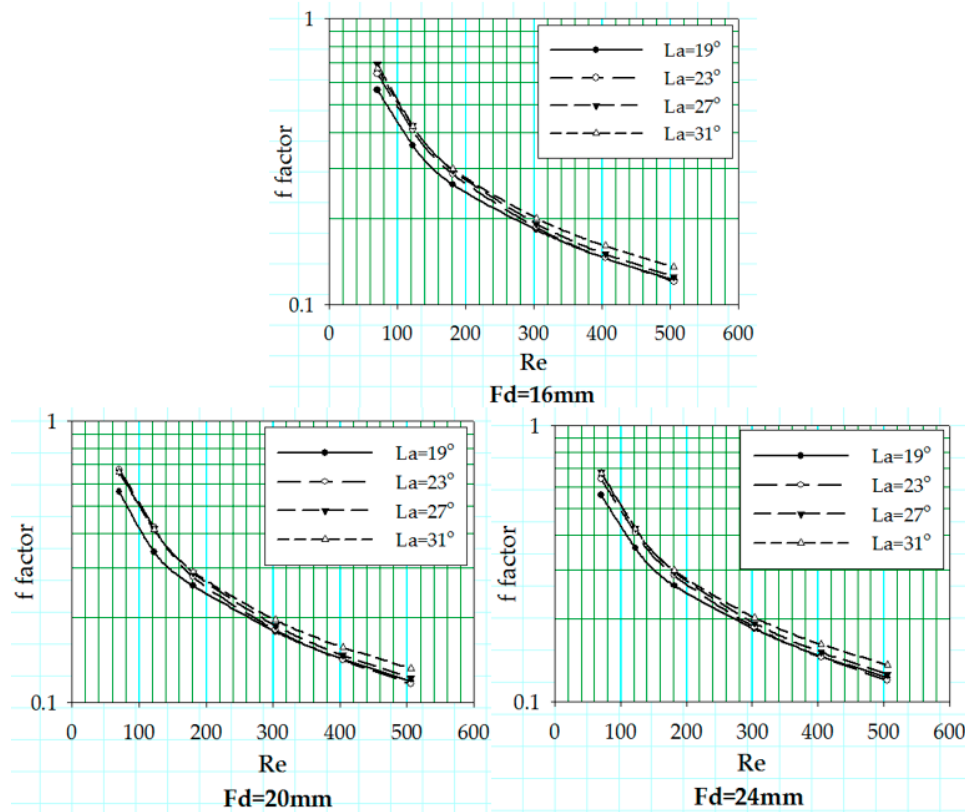


Figure 15. f factor values corresponding to louver angle variation at different flow depths with $F_p = 1.4$ mm

3.6 Critical Reynolds number

Web and Trauger [23] established that the flow efficiency decreases below a certain value of Reynolds number with a decrease in Reynolds number, they named this particular number as critical Reynolds number. Beyond this critical Reynolds number, the flow efficiency is independent of the Reynolds number.

Critical Reynolds number is the Reynolds value where fall-off of the j factor curve is observed. Numerous efforts have been made to successfully predict the critical Reynolds number through correlations. Cowell et al. [28], Webb and Trauger [23] presented their correlations for critical Reynolds number that are shown in Eq. (12) and (13).

$$Re_{cri} = \frac{4860}{\left(0.936 - \frac{1.76}{(L_p/F_p)} + 0.995L\alpha\right)} \quad (12)$$

$$Re_{cri} = 828 \left(\frac{L\alpha}{90}\right)^{-0.34} \quad (13)$$

The comparison of the critical Reynolds numbers with the ones published in literature is shown in Table 5. The correlation presented by Cowell et al. [28] (for $L_p/F_p \leq 1$) shows better results compared to the one formulated by Webb and Trauger [23] because of its dependency on the fin pitch parameter. Webb and Trauger (for $L_p/F_p \leq 1.31$) only associated the critical Reynolds number with louver angle, which predicts the critical Reynolds number values far from true values. Critical Reynolds number values predicted using Cowell et al. correlation also show some offset, but they are relatively more accurate than those of Webb and Trauger. The critical Reynolds number values calculated in this study are also compared with the ones published by Kim and Cho [21], they performed an experimental study using geometries having F_d of 20 mm only. The present study results align well with their findings, that critical Reynolds number is dependent on F_p value and relatively independent on louver angle. Moreover, the present study revealed that critical Reynolds number is

also inversely proportional to the L_p/F_d . A detailed analysis is performed to understand the behavior of critical Reynolds number using thirty-six geometric configurations with different combination of geometric parameters. Out of these thirty-six geometric samples, only twelve showed critical Reynolds number, which asserts that critical Reynolds number fall-off may not occur for all geometric configurations. The critical Reynolds number decreases with the increase in fin pitch value and is directly proportional to the flow depth parameter. Moreover, the critical Reynolds number increases with the increase in louver angle, it reaches a maximum value and then shows a drop as the louver angle is further increased. This value of louver angle at which the critical Reynolds number takes a fall is different for different fin pitch values and does not depend on the flow depth parameter at all.

Table 5. Critical Reynolds number comparison

L_α	$F_p = 1.0 \text{ mm } (L_p/F_p=1.70)$				$F_p = 1.2 \text{ mm } (L_p/F_p=1.42)$				$F_p = 1.4 \text{ mm } (L_p/F_p=1.21)$			
	19°	23°	27°	31°	19°	23°	27°	31°	19°	23°	27°	31°
	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}	Re_{cri}
$F_d=16 \text{ mm}$ ($L_p/F_d = 0.106$)	$\cong 70$	$\cong 70$	$\cong 70$	-	-	-	-	-	-	-	-	-
$F_d=20 \text{ mm}$ ($L_p/F_d = 0.085$)	$\cong 130$	$\cong 140$	-	-	-	-	-	-	-	-	-	-
$F_d=24 \text{ mm}$ ($L_p/F_d = 0.071$)	$\cong 160$	$\cong 130$	$\cong 130$	-	-	$\cong 130$	$\cong 120$	$\cong 130$	-	-	-	-
Kim and Cho [21]	140	-	140	-	110	-	130	-	70	-	-	70
Cowell et al. [28]	258	213	182	158	261	215	183	159	264	217	184	160
Web and Trauger [23]	1405	1317	1247	1190	1405	1317	1247	1190	1405	1317	1247	1190

4. Conclusion

The conclusions deduced on the basis of results extracted from the detailed low Reynolds computational study of louver parameters are presented here:

- Numerical results for low Re range reveal, the geometric configuration with $F_p=1 \text{ mm}$, $F_d=16 \text{ mm}$ and $L_\alpha= 19^\circ$, exhibited the best air-side thermal performance on the basis of heat transfer coefficient.
- Heat transfer rate is strongly dependent on the relative positioning of the louvers to the upstream louvers. Since the interference caused by the upstream louver can significantly reduce the effective heat transfer surface area of downstream louvers.
- Investigating the Re_{cri} , it was found that the fall-off of j factor at low Re is completely reliant on arrangement of the adjacent fin louvers. This is because thick boundary layer created around the upstream louver covers the downstream louvers completely at small fin pitch and large louver angles.
- Re_{cri} shows strong dependency on (L_p/F_p) and relative independency on L_α when F_d is small. At higher F_d values, Re_{cri} varies with variation in L_α .
- Critical Reynolds number rises with an increase in flow depth and decrease in fin pitch values.
- A small drop in the value of Re_{cri} is noticed with increase in louver angle up to a point where Re_{cri} starts rising again.
- At high Reynolds number, j factor is found directly proportional to fin pitch, but for low Re, an inverse relation is observed.

- Friction factor f rises with the increase in louver angle and decrease in fin pitch values.

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Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

A	: Area, m ²
A_c	: Minimum free flow area, m ²
c_p	: Specific heat, J/kgK
D	: Ideal transverse distance, m
E	: Energy, J
f	: Fanning friction factor
F_d	: Flow depth, m
F_p	: Fin pitch, m
H	: Fin height, m
h	: Air-side heat transfer coefficient, W/m ² K
j	: Colburn j-factor
k	: Thermal conductivity, W/mK
L_α	: Louver angle, deg
L_l	: Louver height, m
L_p	: Louver pitch, m
Nu	: Nusselt number (hD/k)
N	: Actual transverse distance, m
N_l	: Number of louvers
Pr	: Prandtl number (ν/α)
P	: Pressure, Pa
Q	: Heat transfer rate, W
Re_{Lp}	: Louver pitch based Reynolds number ($V_c L_p / \nu$)
Re_{cri}	: Critical Reynolds number
S_1	: Non-louvered length at inlet and exit, m
S_2	: Redirection louver length, m
T	: Temperature, K
T_m	: Log mean temperature
V_{cri}	: Critical air velocity (u_{Afr}/A_c), m/s
\mathbf{u}	: Velocity vector, m/s
$U_o A_o$: Overall thermal conductance, W/K

Greek letters

δ	: Fin thickness, m
Δ	: Difference
ρ	: Density, kg/m ³
η	: Efficiency

Subscripts

a	: Air-side
c	: Cold
cri	: Critical
f	: Fin
fr	: Frontal

h : Hot
 i : Inlet
 o : Outlet
 w : Wall

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