

Article

A New Health Assessment Index of Tunnel Lining Based on the Digital Inspection of Surface Cracks

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Abstract: The stability assessment of aged tunnel linings were mainly evaluated based on the visual inspection, and the Tunnel-lining Crack Index (TCI) is one of the most widely used tunnel lining health assessment indexes in Japan. However, the intersection and distribution of cracks, which can influence the stability of tunnel lining greatly, were not considered in the TCI. A new method was proposed for the health assessment of tunnel lining, which evaluate the lining states according to the fractal dimension of cracks. Based on the machine vision-based method, the crack image can be extracted efficiently. The fractal dimension of lining cracks in one span can be obtained in a few minutes. A series of comparative tests and field tests were conducted to evaluate the validity of this new method. The comparative tests confirmed that fractal dimension can characterize the density, width, and distribution of cracks. The intersection of cracks, which will increase the risk of lining collapse, can also increase the fractal dimension. The fractal dimensions of tunnel lining cracks were obtained according to the digital inspection test of Hidake Tunnel in Japan for all the 65 spans. Moreover, the TCI was obtained through statistical methods. The correlation between fractal dimension and TCI of tunnel lining was studied. The significance of the new evaluation index is that it can identify some unusual spans of tunnel lining and provide a basis for further internal testing. As a complement to the conventional visual inspection method, the fractal dimension of the cracks is a promising health assessment index.

Keywords: tunnel lining; health assessment; fractal dimension; tunnel-lining crack index; digital inspection test; field test

1. Introduction

A large number of tunnels have been in service for the past decades all over the world. The tunnels were mainly supported by concrete lining [1, 2]. The persistent ageing and seismic activity lead to many problems to the concrete lining, such as cracking, corrosion and leakage [3-5]. The damage of tunnel lining will decrease its integrity and subsequently increase the risk of tunnel collapse [6]. In order to deal with this situation, there is an urgent requirement for accurate tunnel lining health assessment methods [7-10].

Generally, the stability of aged tunnel linings were mainly evaluated based on the visual inspection [11]. But the evaluation standard was qualitative, and the results depended on the experience of different engineers. As a solution of this problem, the Tunnel-lining Crack Index (TCI) was proposed to quantitatively evaluate the severity of cracks [12]. It has been widely applied for inspecting the surface defects of tunnels in Japan. The stability assessment based on TCI is reasonable to some extent because the mechanical stability of a tunnel is influenced greatly by the severity of cracks in the lining [13]. However, the intersection and distribution of cracks, which can influence the stability of tunnel lining greatly, could not be considered in TCI. The uncertainty relationship

between the TCI and the instability of tunnel lining called for more alternative assessment methods and health indexes.

As the distribution of cracks in the tunnel lining is quite complex, it is difficult to make a precise description through conventional mathematical methods. Fortunately, fractal theory is used to analyze the distribution of complex graphics, and has been widely used in art, astronomy, geography, biology, fluid dynamics, probability theory, chaos theory, and pure mathematics in the past few decades [14-19]. In recent years, the fractal theory was used to describe the propagation of cracks in the rock or concrete specimens in laboratory [20-25]. These studies confirm that the cracks in concrete have fractal properties [21]. Therefore, it is possible to describe the distribution of cracks and evaluate the states of tunnel lining by fractal theory. Moreover, the development of machine vision-based method makes it possible to collect the images of tunnel lining and to calculate the dimensions of the cracks efficiently [26, 27].

In this study, the fractal dimension of cracks in tunnel lining was taken as a new health assessment index. A series of comparative tests and field tests were conducted to evaluate the validity of this new method. In addition, the quantitative correlation between fractal dimension and TCI of cracks in tunnel lining was studied.

2. Theoretical background

2.1 Concept of Tunnel-lining Crack Index

The conceptual diagram of TCI [12] was shown in Fig. 1. One span of the tunnel shown in the left side of the figure was spread out to a flat surface as shown in the right side. The basic formula of TCI is shown in equation (1):

$$F_{ij} = \frac{1}{A} \sum_{k=1}^n (t^{(k)})^\alpha (l^{(k)})^\beta \cos \theta_i^{(k)} \cos \theta_j^{(k)}. \quad (1)$$

where A is the total area of the lining; n is the number of cracks; t is the width of crack; k ; l is the length of crack; k ; θ_i and θ_j donate the angles formed by the normal vector of the crack with the x_i axis and x_j axis; α and β donate the weighting coefficients of crack width and length.

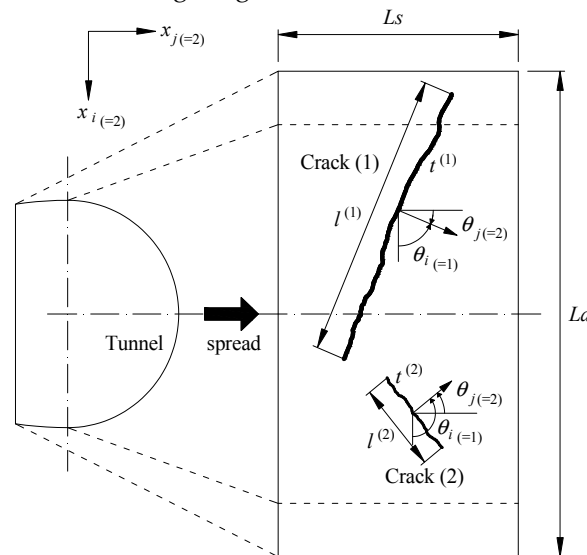


Fig. 1 The conceptual diagram of TCI

F_{11} and F_{22} obtained by the equation (1) indicated the longitudinal component and the transverse components of the TCI, respectively. The crack index F_0 was expressed as the sum of longitudinal and transverse components as shown in equation (2). Associating equation (1) with equation (2), the crack index F_0 can be derived as equation (3).

$$F_0 = F_{11} + F_{22}. \quad (2)$$

$$F_0 = \frac{1}{A} \sum_{k=1}^n (l^{(k)})^\alpha (l^{(k)})^\beta. \quad (3)$$

It is an objective evaluation method without depending on the technical force of the inspection engineer. The width, length, direction of cracks were considered. This method has been widely used in the soundness evaluation of tunnel lining in Japan.

However, the relevance of tunnel lining stability and the cracks density in the lining was questionable. On one hand, the intersection and distribution of cracks were not considered in TCI. On the other hand, some approximations have to be used in the calculation of crack index. For example, the cracks were always not straight lines, but they were divided into small segments and considered as straight lines to simplify the calculation. In addition, the calculation of TCI based on the statistical methods is extremely time consuming.

2.2 Concept of fractal dimension

The essential idea of fractional has a long history in mathematics that can be traced back to the 1600s. It was originally used to describe objects that have self-similarity features. The terms of fractal and fractal dimension were coined by mathematician Benoit Mandelbrot in 1975 [28, 29]. It was used to extend the concept of theoretical fractional dimensions to geometric patterns in nature. For example, the fractal dimension of a coastline quantifies how the number of scaled measuring sticks required to measure the coastline changes with the scale applied to the stick.

In fractal geometry, the fractal dimension is a ratio providing a statistical index of complexity comparing how detail in a fractal pattern changes with the scale at which it is measured. It has also been characterized as a measure of the space-filling capacity of a pattern that tells how a fractal scales differently from the space it is embedded in.

According to the definition, the fractal dimension can describe the density and complexity of the cracks in tunnel lining. In this case, it is a promising method to estimate the stability of tunnel lining according to the fractal dimension of cracks. The fractal dimension of cracks in a plane can be explained intuitively thinking of them as an object too detailed to be one-dimensional, but too simple to be two-dimensional. Therefore its dimension might best be described not by its usual topological dimension but by its fractal dimension, which in this case is a number between one and two.

2.3 Calculation method of fractal dimension

There are several formal mathematical definitions of fractal dimension that build on the basic concept of change in detail with change in scale [30], and the box-counting dimension is the most widely used one [31]. In fractal geometry, the box-counting dimension, also known as Minkowski dimension, is a way of determining the fractal dimension of a set S in a Euclidean space R^n , or more generally in a metric space (X, d) .

To calculate the dimension for a fractal S , imagine this fractal lying on an evenly spaced grid, and count how many boxes are required to cover the set. The box-counting dimension is calculated by seeing how this number changes as we make the grid finer by applying a box-counting algorithm. Suppose that $N(\varepsilon)$ is the number of boxes of side length ε required to cover the set. Then the box-counting dimension is defined as:

$$D = \lim_{\varepsilon \rightarrow 0} \frac{\log N(\varepsilon)}{\log(1/\varepsilon)} \quad (4)$$

Roughly speaking, the fractal dimension is the slope of the fitting line obtained by fitting a set of points $(\log N(\varepsilon), \log \varepsilon)$ [32]. In practical, the differential equation is used to estimate fractal dimension as shown in equation (5). This calculation is easy to achieve through a MATLAB program.

$$D \approx -\frac{d \log N(\varepsilon)}{d \log \varepsilon} \quad (5)$$

If the above limit does not exist, one may still take the limit superior and limit inferior, which respectively define the upper box dimension and lower box dimension.

3. Feasibility analysis of fractal dimension as a new health assessment index

To confirm the feasibility of fractal dimension as a new health assessment index, the influence factors, such as the density, the width, and the intersection of cracks, on the fractal dimension of tunnel lining cracks will be studied in this part.

3.1 Influence of crack density on the fractal dimension

The fractal dimension of cracks shown in Fig. 2 was calculated according to the method described above. In Fig. 2, two cracks were extracted from a tunnel lining in the field, and the number of cracks was increased by copying these two cracks. As there are usually several to dozens of cracks in one span of tunnel lining, the crack number was set to be 4, 8, 16, 32, 48, and 64 in the six figures, and their fractal dimension was determined to be 1.2745, 1.3062, 1.3690, 1.4504, 1.5291, and 1.5899, respectively. The relationship of fractal dimension and the number of cracks was shown in Fig. 3. According to the results, a linear relationship was found in fractal dimension and number of cracks. The results illustrated that the fractal dimension can characterize the density of the cracks in case of regular distributed cracks.

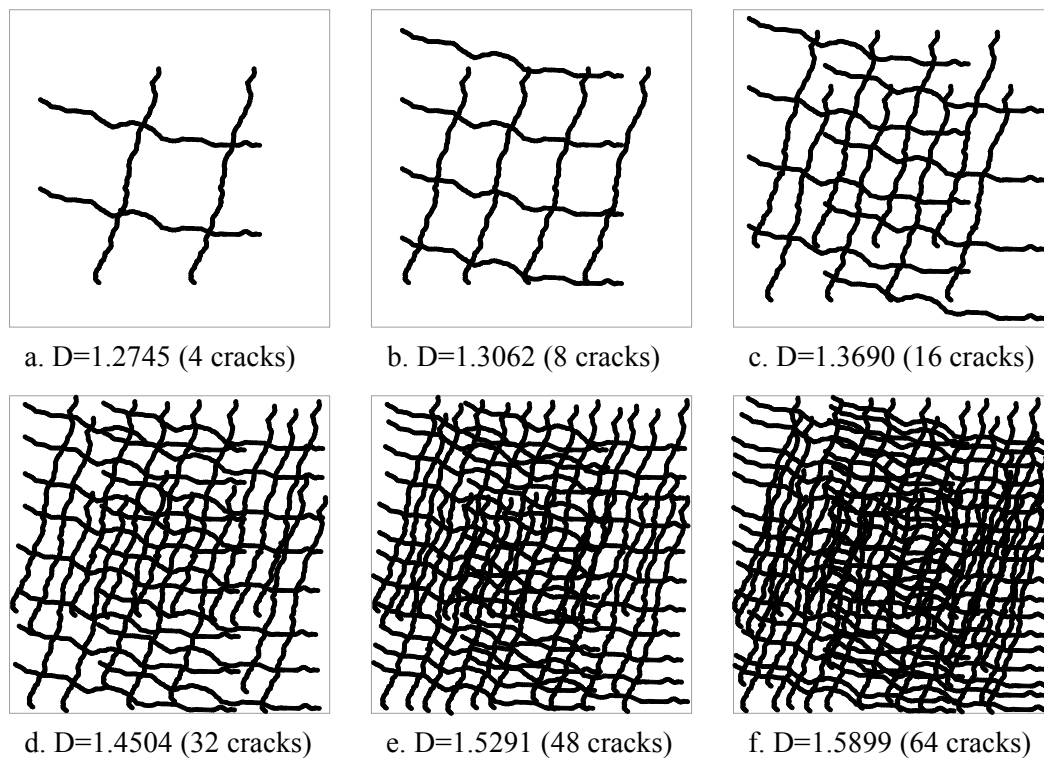


Fig. 2 The fractal dimension of different number of cracks

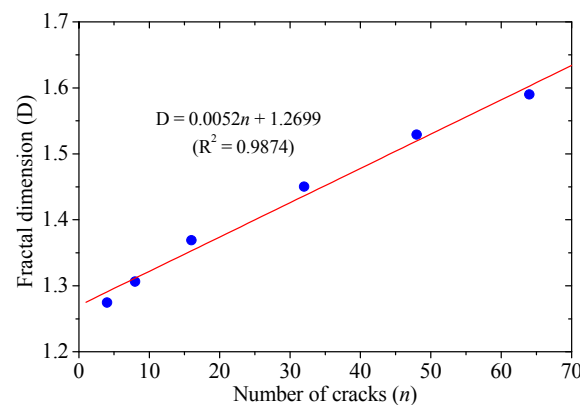


Fig. 3 The relationship of fractal dimension and the number of cracks

3.2 Influence of crack width on the fractal dimension

The fractal dimension of different width cracks shown in Fig. 4 was calculated. As the width of most cracks in tunnel lining distributed between 0.2 and 2.0mm, the crack width is set to be 0.2mm, 0.5mm, 0.7mm, 1.0mm, 1.4mm and 2.0mm, respectively. The fractal dimension was determined to be 1.0338, 1.1598, 1.2455, 1.2745, 1.3555, and 1.3857, respectively. The relationship of fractal dimension and the width of cracks was shown in Fig. 5. There was a roughly linear relationship in fractal dimension and width of cracks. The results illustrated that the fractal dimension can also characterize the width of the cracks. Moreover, it was found that the slope of the fitting curve in Fig. 4 was much larger than the one in Fig. 2. The results certificated that the influence of crack width is larger than the crack density.

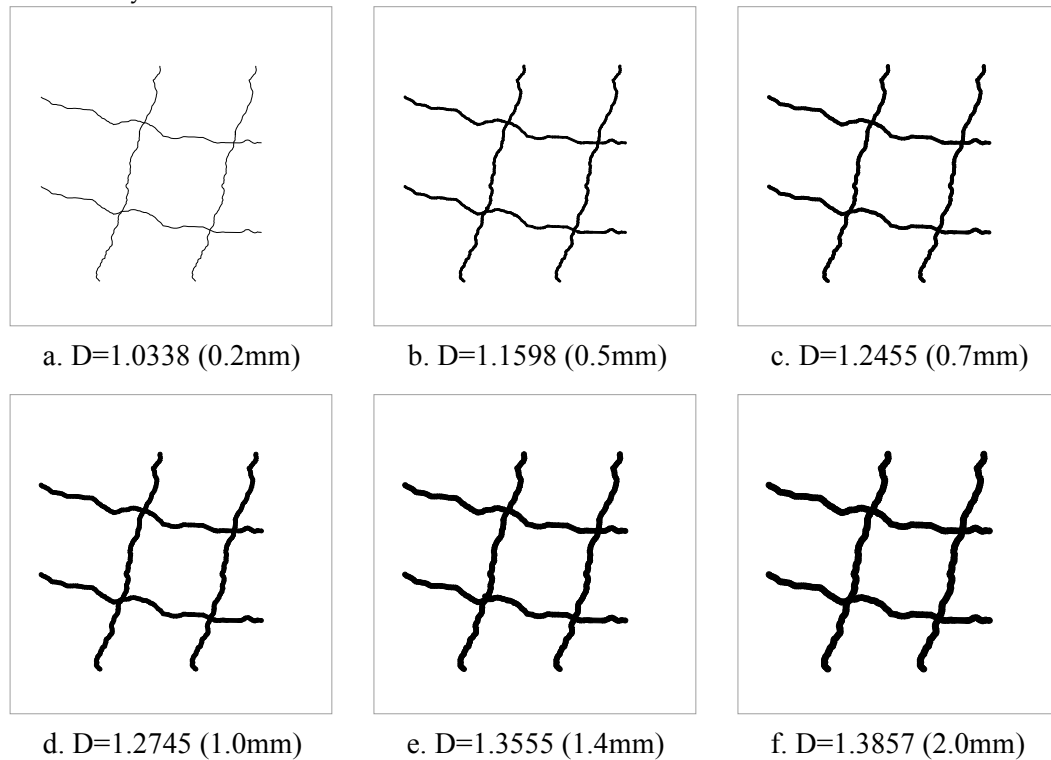


Fig. 4 The fractal dimension of different width cracks

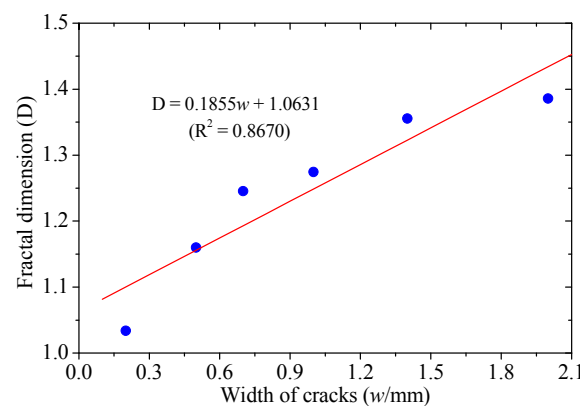


Fig. 5 The relationship of fractal dimension and the width of cracks

3.3 Influence of crack distribution on the fractal dimension

In this part, a comparative study was conducted to compare the advantages and disadvantages of the TCI and the fractal dimension. As shown in Fig. 4, four cracks were extracted from the tunnel

lining in the field, and their locations were redistributed. In these six figures, the number of intersection points increased gradually.

Since the area of the cracks is the same, the TCI is a constant value for all these figures. However, the risk of cracks in different distribution is completely different. Generally, the risk of independent cracks is relatively small. However, the risk of tunnel lining collapse will be increased greatly when these cracks interconnect with each other. This is obviously a severe shortcoming of the TCI, as the cracks distribution cannot be taken into account.

The fractal dimension of these six figures was determined to be 1.2467, 1.2685, 1.2705, 1.2874, 1.3145, and 1.3376, respectively. The relationship of fractal dimension and the number of intersection points was shown in Fig. 5. The results illustrated that the fractal dimension increased with the number of intersection points in case of the same four cracks. It is reasonable as the intersecting of different cracks makes the crack graphic more complex. The results showed that the fractal dimension can characterize the distribution of the cracks, and especially identify the intersection of different cracks, which is closely related with the health condition of tunnel lining.

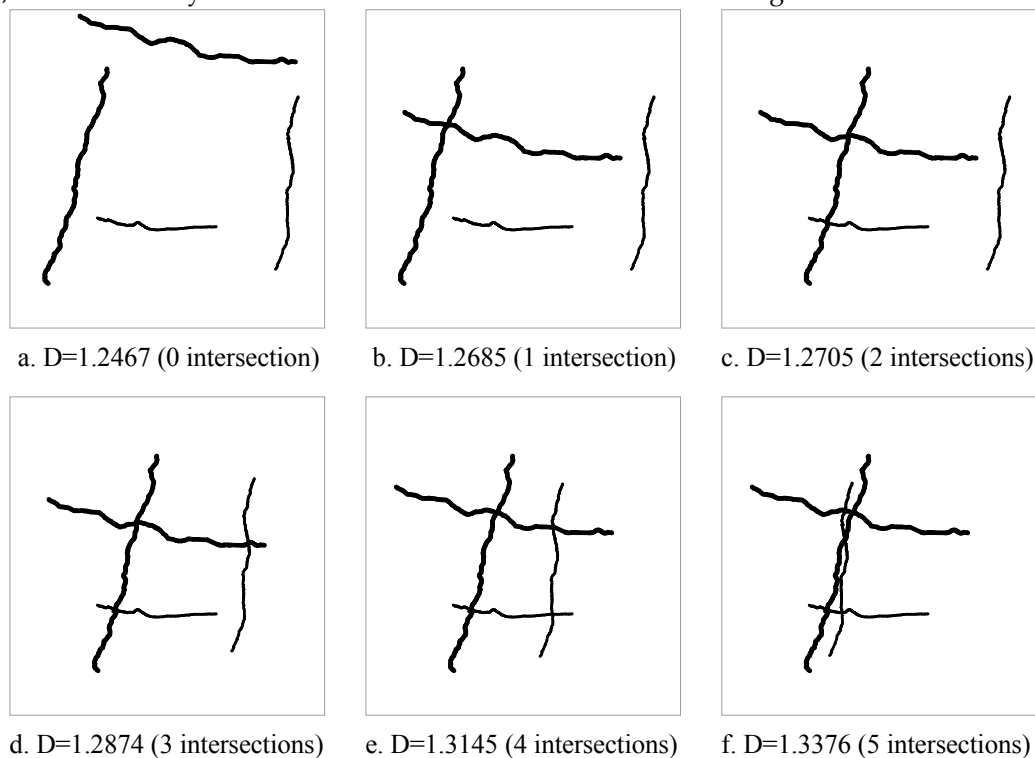


Fig. 6 The fractal dimension of different distributed cracks

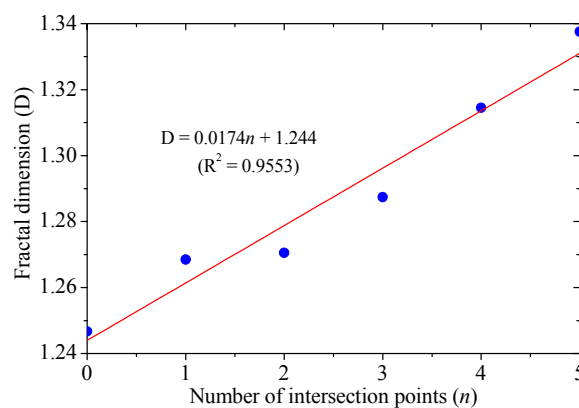


Fig. 7 Fractal dimension of different distributed cracks

4. A Case Study of Hidake Tunnel in Japan

To evaluate the validity of this new health assessment index and to study the quantitative correlation between the fractal dimension and the TCI of lining cracks, a field test was conducted at Hidake Tunnel located in Nagasaki Prefecture, Japan.

4.1. Basic condition of Hidake Tunnel

The Hidake tunnel (as shown in Fig. 6) was constructed in 1982 with the poling-board method. The tunnel length is 780m, with a total of 65 spans. The maximum depth is 25m. The thickness of the concrete lining is 0.7m at a part of the tunnel, and 0.55m at the other part. The surrounding rocks are sandstone, sand tuff, lapilli tuff, basalt, tuff breccia and lapilli tuff in different segments.

Due to the alteration of geological conditions and the deterioration of lining concrete, some defects such as cracks and seepages began appearing in the concrete lining after twenty years of service. The tunnel was also affected by the Kumamoto earthquakes, including a magnitude 7.0 main shock, on April 16, 2016.



Fig. 8 The Hidake Tunnel in Japan

4.2. Digital inspection test

To prevent the possible collapse of tunnel lining, digital inspection test was conducted to assess the extent of damage in different segments of the tunnel. The tunnel lining images were obtain by a photographing vehicle equipped with line sensor cameras. It is a non-contact detection technology that can track the information of the tunnel surface in a very short time [26, 27]. The process of extracting cracks was shown in Fig. 9. The round surface was automatically spread out to a flat surface as shown in Fig. 9a and 9b. The cracks were extracted from the images as shown in Figs. 9c and 9d by a crack identification program. The cameras was fixed on a car, and it can detect cracks with 0.2-mm resolution at a speed of 70 km/h. The cracks were extracted for all the 65 spans in Hidake Tunnel, and the results of 12 typical spans were shown in Fig. 10.

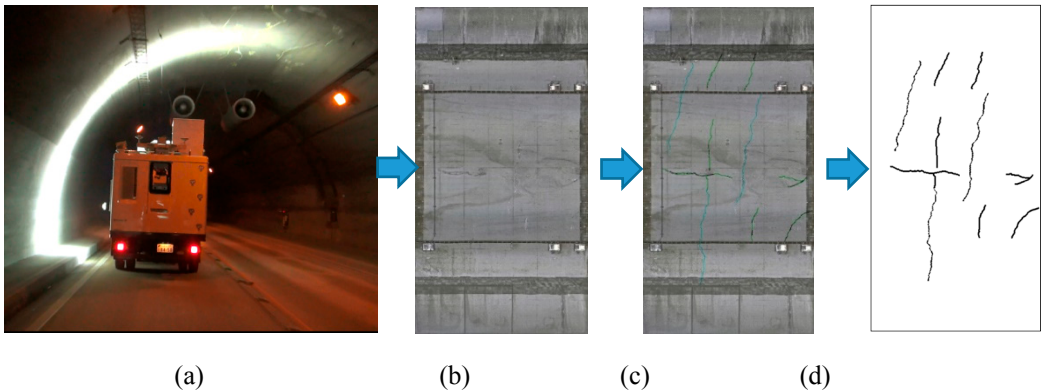


Fig. 9 Extraction of cracks on tunnel lining surface: a, unfolded crack image; b, identification of cracks; c, extraction of cracks

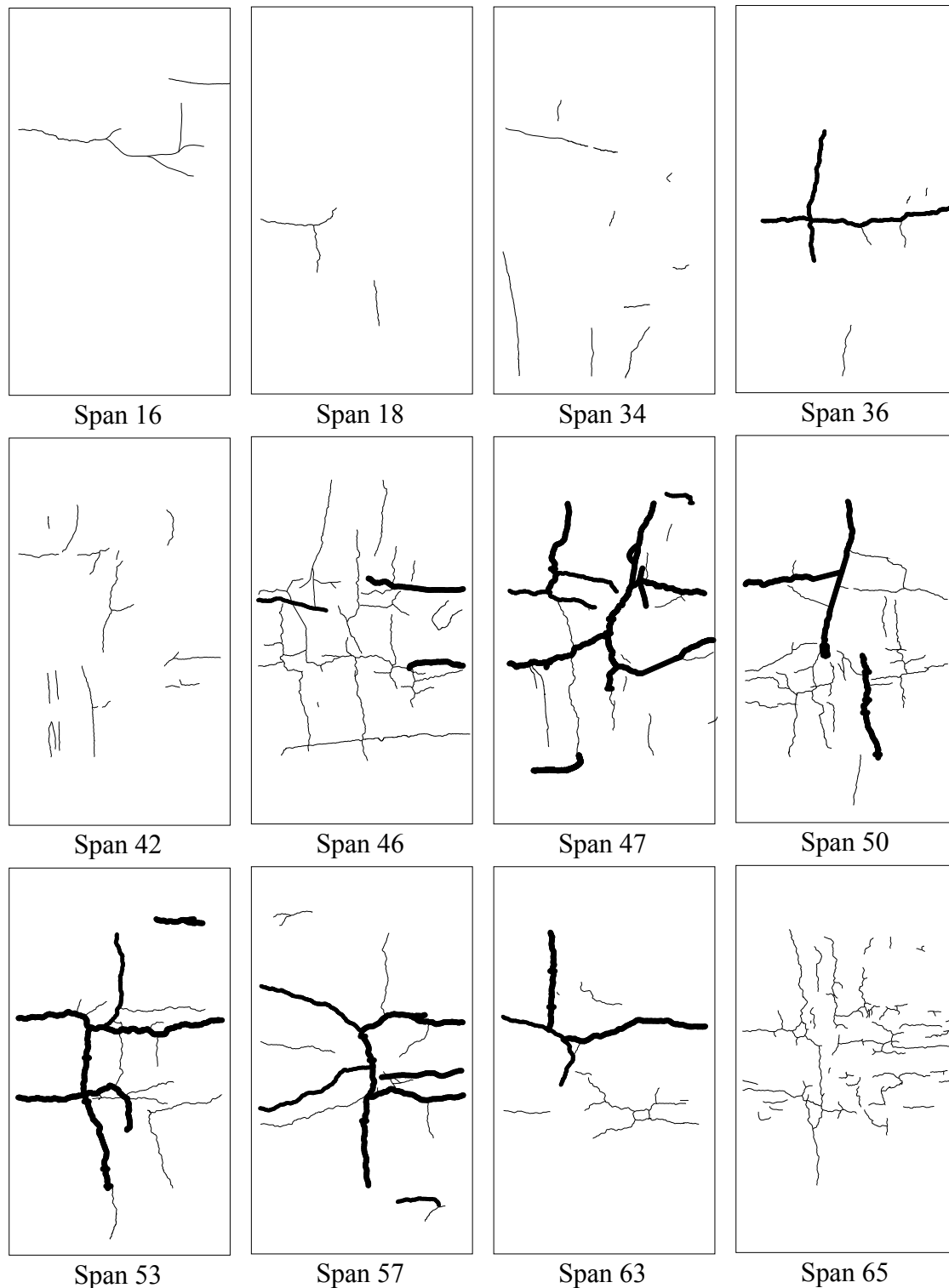


Fig. 10 The distribution of cracks in tunnel lining for twelve typical spans

A large number of cracks were found in spans 46, 47, 50, 53, and 57, including some wide cracks, which would increase the risk of tunnel lining collapse greatly. There were a large number of small cracks in span 65, but no wide cracks were found. Few cracks were found in spans 16 and 18, which may mean a smaller risk of lining collapse. Moderate degree of cracks were found in spans 34, 36, 42, and 63.

4.3. Results and discussions

According to the methods described above, the fractal dimension for all the 65 spans of Hidake Tunnel was calculated and shown in Table 1. The TCI of all the 65 spans was also calculated through the statistical method. According to the fractal dimension and TCI shown in Table 1, their correlation was presented in Fig. 11. In addition, the results of 12 typical spans were marked in this figure.

Table 1 The results of TCI and fractal dimension for all the 65 spans of Hidake Tunnel

Span No.	TCI (10 ⁻⁵)	D	Span No.	TCI (10 ⁻⁵)	D	Span No.	TCI (10 ⁻⁵)	D
1	17.3533	1.2608	23	16.6357	1.2532	45	18.9605	1.2220
2	10.5798	1.1497	24	23.4324	1.2334	46	39.33	1.2527
3	9.5022	1.1395	25	18.5511	1.2783	47	65.3763	1.4182
4	9.2307	1.1630	26	15.5637	1.2665	48	32.1322	1.3375
5	9.0364	1.1102	27	18.6519	1.2487	49	40.2816	1.2906
6	0.9478	1.0031	28	22.1968	1.2994	50	44.3911	1.3006
7	13.9902	1.1786	29	3.9063	1.0679	51	19.656	1.2832
8	13.0135	1.2480	30	4.3127	1.1104	52	30.887	1.3173
9	12.0686	1.1608	31	4.2689	1.0844	53	51.8286	1.4087
10	16.0665	1.2386	32	6.5845	1.1474	54	32.2713	1.2633
11	7.7153	1.1560	33	3.3352	1.0306	55	32.0025	1.3007
12	3.9326	1.0665	34	4.5	1.0191	56	24.6288	1.2537
13	1.7505	1.0279	35	1.8892	1.0072	57	42.2909	1.3788
14	1.5339	1.0396	36	11.5899	1.2431	58	30.6416	1.2838
15	5.7424	1.1120	37	3.8941	1.0950	59	32.5696	1.2968
16	2.0397	1.1210	38	0.7143	1.0244	60	23.9007	1.2542
17	2.0151	1.0570	39	2.5996	1.0343	61	20.0143	1.2237
18	2.6453	1.0454	40	1.9042	1.0286	62	18.2604	1.1819
19	0.3402	1.0068	41	17.5861	1.1876	63	27.706	1.3257
20	4.163	1.0663	42	10.0495	1.0961	64	11.8213	1.1860
21	5.9599	1.0823	43	16.2336	1.1936	65	26.1172	1.2229
22	8.4668	1.1521	44	27.0087	1.2482			

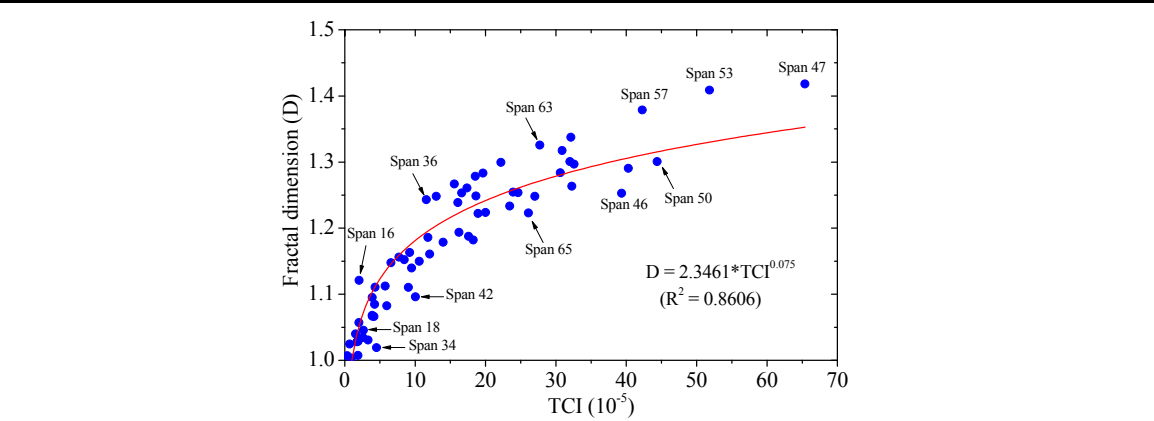


Fig. 11 The correlation between the TCI and the fractal dimension in field test

The results by two different methods can be fitted as a power function with a correlation coefficient of 0.8606. For most of the test spans, the results by the two different methods were consistent with each other. Obviously, there is a certain correlation between TCI and the new proposed index. However, for some points, the degree of risk is significantly different according to the two evaluation indices.

For span 18, there are only three small cracks, and both the TCI and the fractal dimension are in a very small state. Obviously, it is in a safe state. For span 16, there are several cracks and no wide crack is found. Therefore, the calculated TCI is quite small. Since these cracks have almost penetrate the entire lining, it is clear that the risk is underestimated. As the cracks are connected together, the calculated fractal dimension is significantly larger. This behavior indicated that the result by the new index is more consistent with the actual risk of the tunnel lining. Similar phenomenon is found in the results of spans 36 and 63, and the risk is also underestimated by the TCI. While, some wide cracks were found in the two spans, and their risk is relatively large by both method.

For spans 34 and 42, the results were located below the fitting curve, which suggested that their risk was small according to the new index and their risk was large by the index of TCI. Since there are only some small and independent cracks in the two spans, the actual damage in the tunnel lining is relatively small. Therefore, the results by the new health assessment index are closer to the actual risk of the tunnel lining. For spans 46, 47, 50, 53, and 57, the risk of lining collapses is quite large by both health assessment indexes, which suggested that proper maintenance is extremely necessary.

The above results suggested that the current method, which evaluate the health status of tunnel lining only by the index of TCI, is far from perfect. It is necessary to use a different method in which the distribution of cracks can be considered. The significance of the new evaluation index is that it can identify some unusual spans of tunnel lining and provide a basis for further internal testing. In addition, the calculation of fractal dimension is very simple and takes only a few minutes for one span. Meanwhile, a lot of time and work are need to get the TCI.

The fractal dimension of the cracks is a promising method in the health assessment of tunnel lining as shown in these tests. However, the impact factor of different elements, including the density, width, and distribution of cracks, was not fully determined. More field test data and comparative study were need to interpretation the results of the fractal dimension. Nevertheless, the new health assessment method of tunnel lining is a good complement to the conventional visual inspection method and TCI method.

5. Conclusions

A new method was proposed for the health assessment of tunnel lining, which evaluate the lining states according to the fractal dimension of cracks. Based on the machine vision-based method, the crack image can be extracted efficiently. The fractal dimension of lining cracks in one span can be obtained in a few minutes, while the calculation of TCI based on the statistical methods is very time consuming.

A series of comparative tests were conducted to evaluate the validity of this new method. The comparative tests confirmed that fractal dimension can characterize the density, width, and distribution of cracks. The results also certificated that the influence of crack width is larger than the crack density. The intersection of cracks, which will increase the risk of lining collapse, can also increase the fractal dimension, whereas the TCI keep constant.

The fractal dimensions of tunnel lining cracks were obtained according to the digital inspection test of Hidake Tunnel in Japan for all the 65 spans. In addition, the TCI was obtained through statistical methods. The correlation between the fractal dimension and the TCI of tunnel lining was studied. The significance of the new evaluation index is that it can identify some unusual spans of tunnel lining and provide a basis for further internal testing. As a complement to the conventional visual inspection method, the fractal dimension of the cracks is a promising health assessment index.

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