

Review

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Review

### Physics-Informed Machine Learning for Intelligent Gas Turbine Digital Twins: A Review

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#### **Abstract**

Gas turbine digital twins are increasingly critical for real-time diagnostics, predictive maintenance, and performance optimization under both baseload and flexible operations. Advances in hybrid modeling that integrate physics-based simulations with machine learning, offer tremendous opportunities to develop intelligent digital twins that are both physically consistent and computationally efficient. This review surveys current research and industrial practices in hybrid artificial intelligence (AI) models for gas turbines and introduces a classification of four distinct methodologies: (1) ANN-augmented thermodynamic models for enhanced component-level diagnostics; (2) physics-integrated operational architectures combining live sensor data, AI, and modular physics models for system-level optimization; (3) physics-constrained neural networks (PcNNs) and computational fluid dynamic (CFD) surrogates that embed governing equations into learning frameworks for consistent flow and thermal predictions; (4) generative and model-discovery approaches for synthetic data generation and interpretable equation extraction. A comparative maturity framework is presented to evaluate these approaches across five criteria: data dependency, interpretability, deployment complexity, integration with simulation and design workflows, and real-time capability. Industrial implementations by leading OEMs and independent research institutes are analyzed within this context. The review concludes by outlining key challenges and a roadmap toward scalable, interpretable, and operationally robust intelligent digital twin architectures for next-generation gas turbines.

**Keywords:** physics-informed machine learning; hybrid modeling; gas turbine diagnostics; artificial neural networks; intelligent digital twin; virtual sensing; remaining useful life; transfer learning; generative models

#### 1. Introduction

Gas turbines remain a cornerstone of modern energy infrastructure, delivering both primary and dispatchable power generation while also supporting propulsion systems and industrial mechanical drives. As energy systems transition toward decarbonization and incorporate a larger share of renewable sources, the role of gas turbines is evolving. First, they are increasingly being adapted to operate on carbon-free fuels such as hydrogen and ammonia, as well as carbon-neutral synthetic fuels and low-carbon biofuels. Second, they are playing a growing role as reliable backup power sources for intermittent renewables [1,2]. The shift from steady baseload operation to flexible service—characterized by rapid load changes, frequent cycling, and extended part-load operation—has introduced new operational challenges, particularly for aging fleets. Under these conditions, multiple degradation mechanisms act simultaneously, at varying rates, including (but not limited to) fatigue crack growth, hot corrosion, erosion, tip clearance increases, and blade twist. Together, these effects reduce aerodynamic performance and overall efficiency. Frequent load fluctuations also increase the occurrence of thermal—mechanical stress cycles, making traditional degradation patterns less predictable and accelerating the overall deterioration process. These evolving operational

demands underscore the need for advanced monitoring and predictive capabilities, such as hybrid AI–based digital twins, that combine physics-based degradation models with operational data to enable proactive maintenance, optimize performance, and extend the service life of critical turbomachinery assets [2–5].

The concept of the digital twin, detailed in [6], describes a virtual representation of a physical asset, system, or process that mirrors its state and behavior in real time, enabling monitoring, simulation, and analysis throughout its lifecycle. This definition has since evolved into structured frameworks for product and system design that integrate multi-source data and lifecycle considerations [7,8]. Building on this foundation, the intelligent digital twin integrates artificial intelligence, machine learning, and advanced analytics to enable learning from multi-source data, adaptive behavior under changing operating conditions, and support predictive decision-making [9]. This progression from descriptive and predictive modeling toward adaptive, autonomous operation represents a critical step in applying digital twin technology for complex, high-performance systems such as gas turbines [10,11].

This represents a substantial progression beyond purely physics-based methods such as conventional gas turbine diagnostic approaches, which predominantly depend on physics-based methods such as thermodynamic cycle simulations, component performance maps, and gas path analysis (GPA) [12–14]. Physics-based methods are interpretable and reproducible but often computationally intensive, require proprietary geometric details, but they are limited in their ability to adapt to degraded, off-design, or transient operating conditions [12,13]. In contrast, purely data-driven approaches—particularly those employing artificial neural networks (ANNs)—can capture complex, highly nonlinear relationships between sensor measurements and performance metrics, enabling rapid inferences. However, data-driven models frequently struggle to generalize beyond their training domain and typically lack physical interpretability [14–17].

The limitations of both purely physics-based and purely data-driven methods have motivated the emergence of hybrid artificial intelligence (AI) approaches, commonly referred to as physicsinformed machine learning (PIML). For instance, hybrid diagnostic frameworks that integrate artificial neural networks (ANNs) with gas path analysis (GPA) have demonstrated notable improvements in diagnostic sensitivity and degradation tracking [14,15]. Nevertheless, they remain challenged by issues such as limited data quality, sparse fault representation, and the need to maintain alignment with underlying physical principles [16-23]. These methods embed physical constraints, simulation outputs, or governing equations directly into learning architectures, enhancing predictive accuracy while preserving consistency with physical laws. Hybrid AI research for gas turbine modeling is progressing along several parallel and interrelated trajectories, many of which share common mathematical and computational foundations. For example, equation discovery methods, such as Sparse Identification of Nonlinear Dynamics (SINDy) and its open-source implementation (PySINDy) extract governing equations directly from measurement data, enabling the development of interpretable dynamic models [24]. Physics-constrained neural networks, including Physics-Informed Neural Networks (PINNs) and Navier-Stokes Flow Net (NSFnet) variants, embed conservation laws directly into loss functions to model laminar and turbulent flows, with residualbased attention mechanisms improving convergence [5,25-27]. Operator learning frameworks, such as the Fourier Neural Operator (FNO) and Fourier DeepONet, learn resolution-invariant mappings for parametric partial differential equations (PDE)s, enabling scalable, mesh-independent aerodynamic and thermal predictions [28–32]. Architectures that preserve physical invariants, such as Lagrangian Neural Networks (LNNs) and graph neural networks (GNNs), offer scalable inference for coupled thermo fluid-structural systems [33-38]. Physics-informed ML methods have also been applied to high-fidelity thermal processes that are directly relevant to gas turbine operation and related manufacturing and coating processes. In manufacturing applications [39], these methods enable accurate prediction of complex, transient temperature fields during processes such as thermal barrier coating deposition, additive manufacturing, and component heat treatment, where precise thermal control is critical for microstructural integrity and lifespan of hot section gas turbine components. In

forced convection systems [40], physics-informed architectures have achieved real time prediction of transient thermal behavior by embedding governing heat transfer equations into neural networks, allowing for fast, physically consistent simulation under changing flow and boundary conditions.

These capabilities are directly applicable to gas turbine intelligent digital twins and their embedded sub-simulations, enhancing preventive maintenance strategies and remaining life assessments when and where required.

## 2. Hybrid AI Methodologies for Gas Turbine Applications: Description and Advantages and limitations

Hybrid artificial intelligence (AI) for gas turbines real-time diagnostics, predictive maintenance, and performance optimization, make use of the strengths of data-driven learning and physics-based modeling. This is to overcome the limitations each approach has when applied independently. Based on a comprehensive literature review, four distinct categories of hybrid methods are identified:

- ANN-augmented thermodynamic models;
- Physics-integrated operational architectures;
- Physics-constrained neural networks and Computational Fluid Dynamics surrogates;
- Generative and model discovery approaches.

Each category presents distinct trade-offs in terms of generalizability, accuracy, computational cost, and suitability for real-time implementation.

#### 2.1. ANN-Augmented Thermodynamic Models

ANN-augmented thermodynamic models couple classical thermodynamic simulations and gas path analysis with artificial neural networks (ANNs) to improve diagnostic sensitivity, robustness, and real-time applicability. These methods are widely used for component-level diagnostics, degradation tracking, and health assessment [41].

ANN modules learn nonlinear relationships from synthetic or historical datasets, enabling rapid inference while retaining interpretability through their physics-based foundation [42–49]. For example, [46] developed a hybrid diagnostic framework that couples artificial neural network modules with thermodynamic performance maps to infer compressor flow capacity reduction and turbine efficiency loss, enhancing fault detection accuracy and enabling earlier warnings.

As illustrated in Figure 1, these models use process-map-based thermodynamic simulations to generate training data under both nominal and degraded scenarios, enabling the prediction of critical gas path parameters. Physics-based thermodynamic cycle or component simulations are used to create synthetic datasets representing degradation modes such as compressor fouling or turbine efficiency loss. ANNs are then trained to map measurable engine parameters such as pressures, temperatures, or fuel flow. These mappings are then used to estimate unmeasured health and performance indicators such as flow capacity, efficiency loss, or fault severity [42–49]. By learning nonlinear relationships between observed sensor data and hidden degradation states, these hybrid models extend the capability of classical GPA while enabling robust, real-time health monitoring.

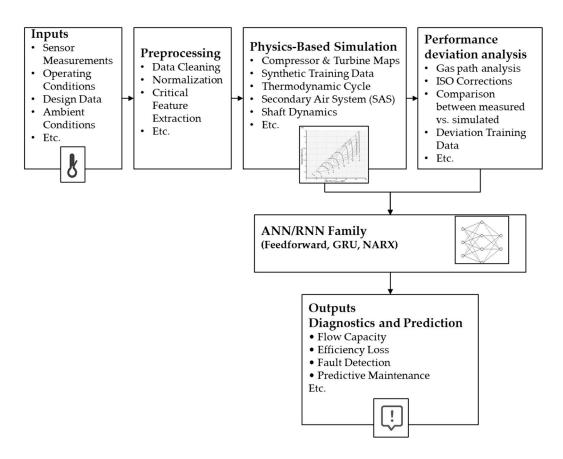


Figure 1. Process map diagram for the ANN-augmented thermodynamic model.

ANN-augmented thermodynamic models have demonstrated robustness to noisy sensor data and adaptability under off-design operating conditions [17,50–52]. They rely largely on synthetic datasets generated from thermodynamic simulations, preserve interpretability through their grounding in cycle physics, and focus on component-level health indicators. However, such models often require domain adaptation or retraining when transitioning from simulation-generated datasets to real engine environments, owing to mismatches in operating conditions, sensor noise characteristics, and unmodeled degradation effects [4,13].

[42–45] developed hybrid diagnostic models for gas turbines that integrate ANNs with thermodynamic cycle simulations to estimate component degradation levels such as compressor flow capacity loss and turbine efficiency reduction, thereby improving early fault detection using simulated deterioration data. Similarly, [46–48] proposed a distributed ANN-based gas path analysis (GPA) framework employing classification, auto-associative, and approximation networks to isolate and quantify multiple simultaneous faults. Their system demonstrated robust fault identification, localization, and severity estimation under nonlinear and noisy operating conditions, outperforming conventional GPA approaches [53].

#### 2.1.1. Advantages:

- Improved diagnostic accuracy compared with purely physics-based models, particularly in nonlinear or multivariate degradation scenarios [43,48];
- Fast inference speeds suitable for real-time and field-deployed applications. While inference is computationally efficient, the training phase can involve substantial overhead depending on the fidelity and validity of the underlying thermodynamic simulations [8,11];
- Ability to leverage synthetic training datasets even when historical fault data are limited [9,11];
- Demonstrated robustness to noisy sensor data and adaptability to off-design operating conditions [17,50–52].

#### 2.1.2. Limitations:

- Strong dependence on the quality and completeness of simulation data; any inaccuracies or biases in the input data directly propagate into the trained model, reducing its reliability in realworld applications [9,25];
- Limited coverage of degradation modes in the simulation dataset may bias predictions and reduce the model's ability to generalize to unobserved faults [9,25];
- Limited extrapolation beyond the design space represented in the simulation or training dataset [3,10];
- The "black-box" characteristics of ANNs can reduce physical interpretability unless explainable AI techniques are applied [17,50–53].

To address the former limitation, hybrid approaches increasingly incorporate physics-informed neural networks [41], grey-box models that combine thermodynamic principles with data-driven ANN modules [9], or explainable AI methods [54]. These strategies aim to ensure predictions remain physically meaningful while retaining the flexibility and adaptability of data-driven learning.

#### 2.2. Physics-Integrated Operational Architectures

Physics-integrated operational architectures combine real-time data with modular physical models and embedded AI elements such as physics-informed neural networks (PINNs), ANN surrogates, and advanced optimization algorithms to deliver full system-level decision support and operational intelligence. These architectures extend beyond algorithm development, focusing instead on control, load allocation, predictive maintenance, and fleet-level operational planning [9,11,22,54,55].

Thermodynamic cycle models and component conservation equations provide the physically consistent backbone for these frameworks, ensuring accurate estimation of critical parameters such as turbine inlet temperature (TIT) and specific fuel consumption (SFC). Embedded AI modules enhance computational speed, improve robustness to sensor uncertainty, and capture nonlinear degradation effects that classical physics models alone cannot fully represent.

Figure 2 illustrates a representative architecture in which live measurements are fused with simulation models and AI surrogates to infer hidden states, optimize performance, and deliver actionable control recommendations. PINNs integrate physical constraints directly into their loss functions [19,54], while ANN surrogates trained on high-fidelity simulations replace computationally expensive physics modules to enable fast, real-time operation [11,55]. Optimization layers, such as particle swarm optimization (PSO), quadratic programming (QP) and other advanced techniques, are employed. In the case of PSO, this evolutionary algorithm which is inspired by swarm behavior, efficiently explores the solution space, while QP provides a deterministic, mathematically rigorous approach for constrained optimization. Combined, these methods improve control performance and overall energy efficiency [22,54,55]

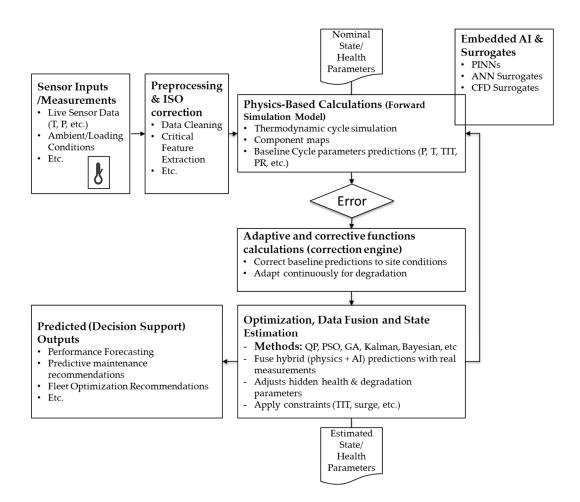


Figure 2. Process map diagram for the Physics-Integrated Operational Architecture.

A representative example is the Electric Power Research Institute (EPRI) Turbine Digital Twin, which integrates live sensor data with Numerical Propulsion System Simulation (NPSS)–based thermodynamic modules and AI-enabled virtual sensors to provide operator-focused performance forecasting, anomaly detection, and predictive maintenance capabilities [56]. General Electric (GE) Vernova applies digital twin technologies such as SmartSignal predictive analytics and three-dimensional visualization twins to optimize power plant performance, increase reliability, and reduce operating costs across more than 7,000 monitored assets worldwide [57]. Siemens employs its Autonomous Turbine Operations and Maintenance (ATOM) framework, an agent-based intelligent digital twin that combines system-level physical modeling with AI optimization layers to support fleet operations, load sharing, and long-term operational planning [58].[54] demonstrated a PINN-enabled intelligent digital twin that accurately predicted hidden variables such as turbine inlet temperature (TIT) and specific fuel consumption (SFC) under sensor uncertainty, while [55] implemented an ANN-surrogate-based architecture for combined heat and power (CHP) gas turbines, enabling real-time modeling of degradation, load sharing, and control.

#### 2.2.1. Advantages:

- Real-time, system-wide representation of engine behavior using live sensor data integrated with physics-based thermodynamic cycle models such as NPSS [56];
- Embedded AI modules (ANN surrogates, PINNs, PcNNs) support adaptive performance modeling, virtual sensing, anomaly detection, and predictive maintenance [16,22,34,54,55];
- Demonstrated improvements in diagnostic accuracy and degradation tracking under nonlinear, noisy, or off-design operating conditions compared to classical gas path analysis [9,10,33];

- Computational efficiency through surrogate models (ANNs, operator-learning networks, CFD surrogates), enabling rapid virtual prototyping, design iteration, and real-time optimization [27,32,42];
- Scalable architectures suitable for plant-wide integration and fleet-level deployment, as demonstrated in EPRI's operator-focused twin, GE Vernova's SmartSignal platform, and Siemens' ATOM framework [56–58];
- Generative and model discovery methods (GANs, RNNs, SINDy) augment sparse datasets and extract interpretable governing equations, enhancing model robustness for rare-event prognostics and transient validation [39,45,63].

#### 2.2.2. Limitations:

- Integration complexity, including sensor synchronization, model calibration, and the need for robust data pipelines when interfacing with existing Condition Monitoring Systems (CMS)s [56];
- Dependence on the quality and coverage of training data; poor representation of degraded or transient conditions may bias predictions [9,42,49];
- ANN-heavy approaches exhibit "black box" behavior with reduced interpretability unless constrained by physics-informed or explainable AI methods [42,47,51];
- High computational costs during training for PcNNs, PINNs, and generative surrogates due to embedded PDE residuals and automatic differentiation, with additional challenges in stability and convergence [20,21,29];
- Cross-platform generalization is limited; calibrated twins often require domain adaptation, and standardized benchmarks for validation are lacking [42,49,55];
- Cybersecurity and latency concerns in interconnected SCADA and historian environments, exposing vulnerabilities in critical infrastructure [56,57];
- High development and lifecycle costs, requiring multidisciplinary expertise in thermodynamics, control systems, data science, and IT infrastructure [16,22,54].

#### 2.3. Physics-Constrained Neural Networks and CFD Surrogates

Physics-constrained neural networks embed governing physical laws such as Navier–Stokes, continuity, and energy balance equations directly into the training process, ensuring physically consistent predictions even when labeled data are sparse or noisy [8,10,21,23,31,59]. These constraints may be imposed as soft penalties in the loss function or as hard constraints within the network architecture, thereby enforcing adherence to conservation laws such as the non-isothermal Navier–Stokes equations [26] and energy balance principles. By integrating these physical priors, PcNNs reduce dependence on dense experimental datasets and bridge the gap between purely data-driven models and high-fidelity physics-based simulations. A typical PcNN workflow and CFD surrogate pipeline for gas turbine applications is illustrated in Figure 3, where geometry, boundary conditions, and operating parameters are provided as inputs, and embedded constraints ensure flow, thermal, and structural predictions that remain consistent with fundamental physics.

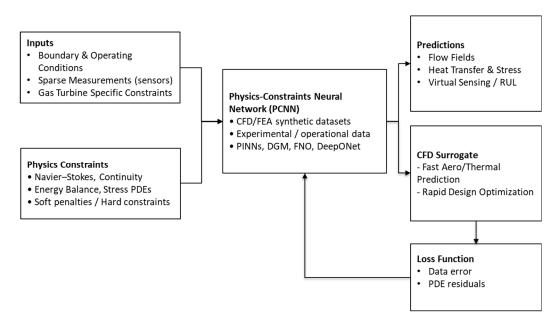


Figure 3. Process map diagram for the Physics-Constrained Neural Networks (PcNNs).

Applications in gas turbines include flow-field inference, heat-transfer analysis, structural stress estimation, and virtual sensing. For example [19] applied Physics-Informed Neural Networks (PINNs) to reconstruct temperature and velocity fields within turbine passages using sparse sensor measurements, embedding Navier-Stokes and energy equation residuals into the loss function to improve generalization and physical fidelity. [21] reviewed broader PINN applications in industrial gas turbines, including aerodynamic and aero-acoustic field estimation, blade flutter and fatigue prediction, combustion instability diagnostics, and turbine vane heat-transfer modeling. Likewise, [39] demonstrated how physics-informed learning can solve conductive and convective heat-transfer PDEs in high-temperature engineering applications, showing that embedded physics constraints can yield reliable predictions even when experimental thermal data are limited. Foundational approaches include Physics-Informed Neural Networks (PINNs) [31] and the Deep Galerkin Method (DGM) [32], which enable solving forward and inverse problems for nonlinear PDEs without requiring structured meshes. These examples highlight the suitability of PcNNs for predicting coupled aero-thermal behavior in turbine components, where flow and heat transfer are closely linked to degradation mechanisms such as thermal fatigue and creep. PcNNs also enable the development of CFD surrogate models, significantly reducing computational cost compared to conventional solvers. [60] introduced a transformer-based surrogate for three-dimensional compressible flow prediction in axial compressors without mesh generation, enabling near-instantaneous aerodynamic predictions for early-stage design optimization. [61] applied deep learning to model the impact of manufacturing and build variations on multistage axial compressor aerodynamics, showing how high-fidelity synthetic datasets can improve surrogate accuracy for complex multistage flows. Other surrogate models leveraging convolutional neural networks, graph neural networks, and generative models trained on high-fidelity CFD datasets [1,13,17,29,62,63] have achieved substantial speed-ups while maintaining accuracy. [45] developed a transformer-based, data-driven AI model for turbomachinery compressor aerodynamics that enables rapid approximation of 3D flow solutions from CFD data. Although accuracy decreases for designs far outside the training distribution, the method provides a computationally efficient surrogate for aerodynamic design and optimization. Trained on highresolution compressor flow simulations, the model reproduces key aerodynamic features and allows derivation of performance metrics such as efficiency. Operator learning architectures extend these capabilities further: the Fourier Neural Operator (FNO) and Fourier DeepONet can learn full solution operators for entire families of PDEs, enabling mesh-independent, resolution-invariant predictions across different geometries and operating regimes [25,28,64,65]. These approaches support virtual

sensing of otherwise unmeasurable states, accelerated aerodynamic and thermal design iterations, and physically consistent diagnostics and prognostics.

#### 2.3.1. Advantages:

- Physically consistent outputs even when labeled data are sparse or noisy [13,22,60];
- Reduced reliance on labeled datasets through embedded physical laws [3,8,10,21,23,59];
- Fast surrogate predictions for flow, thermal, and stress analyses, enabling rapid design optimization and diagnostics [1,13,17,29,60,62,63];
- Resolution-invariant learning using operator learning frameworks Fourier Neural Operator (FNO), Fourier DeepONet for generalization across geometries and operating conditions [25,28,64–68].

#### 2.3.2. Limitations:

- High computational cost during training due to embedded PDE residuals and automatic differentiation [10,23];
- Numerical stability and convergence challenges, especially in multi-physics environments [13,62,63];
- Limited transferability across turbine platforms unless domain adaptation or transfer learning is applied [1,17,29];
- Lack of standardized benchmarks and evaluation protocols for cross-platform validation [8,21].

#### 2.4. Generative and Model Discovery Approaches

Generative and model discovery approaches address challenges related to data scarcity, interpretability, and modeling of complex multi-component interactions in gas turbine systems. These methods are particularly valuable when operational fault data are rare, extreme events are underrepresented, or physics-based models are incomplete or too computationally expensive for real-time deployment [8,69]. Generative and model discovery can be further classified into three methods: generative models, which create synthetic operating scenarios to expand scarce datasets [8]; model discovery methods, which extract governing equations from data to improve interpretability [24,30,69]; and emerging architectures, which extend these capabilities to complex geometries and multi-physics systems [27,28,36,37,65].

#### 2.4.1. Generative Models

Techniques such as Generative Adversarial Networks (GANs), Variational Autoencoders (VAEs), and Recurrent Neural Networks (RNNs) generate synthetic sensor data representing rare or extreme scenarios, enabling robust model training under limited data conditions [8]. Beyond diagnostics, generative AI has been applied to engineering design, where neural network–aided approaches systematically explore design spaces, integrate multidisciplinary objectives, and accelerate concept evaluation. For example, [48] demonstrated how a neural network–aided technological evolution system optimized product development by learning from prior designs. Similar methodologies have been used for circular design [66], process control and fault diagnosis [67], and multidisciplinary product specification [68]. For gas turbines, such generative frameworks improve rare-event coverage, enhance design robustness, and reduce validation costs. [40] further showed that RNN architectures can provide super real-time transient thermal predictions in convection systems, demonstrating potential for virtual sensing and rare-event prognostics.

#### 2.4.2. Model Discovery

Model discovery methods complement data generation by extracting parsimonious governing equations directly from data. Approaches such as Sparse Identification of Nonlinear Dynamics (SINDy) [69] and its PySINDy implementation [24] produce interpretable reduced-order models suitable for control, fault detection, and diagnostics in regimes not captured by classical simulations. However, applying model discovery in practice requires careful feature engineering, noise filtering,



and domain knowledge to prevent spurious dynamics from being identified as governing equations. Figure 4 illustrates the combined workflow: synthetic data generation expands scenario coverage, while model discovery identifies simplified yet physically meaningful system dynamics. This integration improves rare-event representation and strengthens hybrid intelligent digital twins.

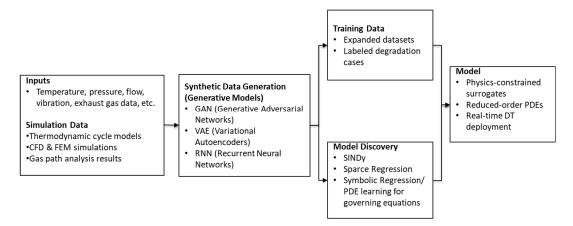


Figure 4. Process map diagram for the Generative and Model Discovery Approaches.

#### 2.4.3. Emerging Architectures

Recent advances extend these methods to scalable multi-physics inference. Physics-informed graph neural Galerkin networks [36], graph convolutional neural networks [37], and Discretization Net [27] embed mesh connectivity and discretization principles into learning architectures, achieving high accuracy on irregular domains, accelerating Navier–Stokes solutions, and improving virtual sensing from sparse measurements [30]. Energy-preserving designs such as Lagrangian Neural Networks (LNNs) [33] further enable robust inference across interdependent subsystems. Together, these advances move beyond data augmentation and equation discovery toward physics-consistent digital twins, with applications in hot-gas-path monitoring, secondary air system modeling, and adaptive flow/thermal field reconstruction.

#### 2.4.4. Advantages:

- Synthetic data augmentation, improving model robustness under rare or previously unobserved conditions [8,40];
- Equation discovery and interpretability, supporting reduced-order modeling, control and diagnostics [24,69];
- Scalable graph-based and energy-preserving architectures for complex multi-component systems [30–37].

#### 2.4.5. Limitations:

- Generative models may produce physically unrealistic signals if not properly constrained [8,40];
- Equation discovery methods such as SINDy are sensitive to noise and feature selection [69];
- Graph-based and energy-preserving neural architectures can be computationally demanding when scaled to full-system or fleet-level applications [27,30,36,37].

Integrating generative, discovery, and graph-based methods into industrial digital twins requires rigorous validation to ensure regulatory compliance, user confidence, and robustness under unseen operating conditions. Without explicit physical constraints, generative models may produce infeasible outputs such as negative mass flow rates, unrealistic efficiency values, or fail to capture the coupled thermo-fluid–structural dynamics of gas turbines. Likewise, model discovery techniques risk misidentifying governing equations when trained on noisy or incomplete datasets. To ensure reliability, validation mechanisms are essential. Emerging strategies include embedding physics-consistency checks, such as conservation of mass and energy laws, into training pipelines, applying

adversarial filtering to reject non-physical synthetic signals, and cross-validating synthetic scenarios against high-fidelity CFD or thermodynamic simulations before deployment [8,69]. Analogous safeguards are already being adopted in other domains. In aerospace, physics-informed GANs have been used to generate turbulence-consistent flow fields. In manufacturing, VAEs constrained by metallurgical rules ensure plausible microstructural evolution [8,39,40]. These parallels underscore that combining generative AI with physics-based validation is critical to ensuring that synthetic data strengthens—rather than undermines—the robustness of intelligent gas turbine digital twins.

#### 3. Results

The comparative analysis shows that no single hybrid AI method is best for all gas turbine digital twins. Each approach works better in certain contexts. The choice depends on the goal such as online diagnostics, component-level optimization, or fleet-wide asset management. Results also depend strongly on available computational resources and the quality of data. To evaluate these approaches systematically, a novel maturity classification framework is developed based on five key criteria:

- Data dependency (simulation-driven, sensor-driven, or physics-driven);
- Physical interpretability (low, medium, or high transparency of learned relationships);
- Deployment complexity (computational effort and integration burden);
- Compatibility with simulation/design workflows (ability to integrate with thermodynamic models, CFD, or structural solvers);
- Real-time capability (suitability for online diagnostics, control, or prognostics).

  The radar plot in Figure 5 illustrates the comparative maturity of hybrid AI approaches across five key criteria. Maturity is evaluated on a 1-5 scale:
- 1–2 indicate low maturity, representing methods that are limited or not widely deployable;
- 3 reflects medium maturity, covering approaches with potential but notable gaps;
- 4–5 denote high maturity, corresponding to robust, proven, or scalable methods suitable for practical deployment.

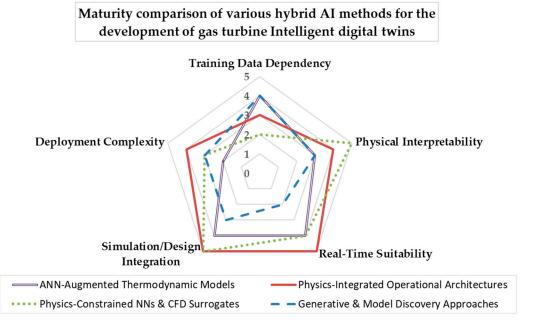


Figure 5. Radar Plot of Hybrid AI Methods Maturity for Gas Turbines Intelligent Digital Twins.

First, ANN-augmented thermodynamic models are entry-level solutions. They require substantial amounts of synthetic or historical datasets [10,42]. Their interpretability is moderate, as they retain some transparency from the thermodynamic baseline but depend on black-box ANN

layers. Deployment complexity is relatively low, which makes them practical for component-level diagnostics and degradation tracking. They integrate reasonably well with simulation workflows such as gas path analysis and provide medium–high real-time suitability, making them effective for rapid health monitoring [10,41,43,70,71].

Second, physics-integrated operational architectures represent the most mature category. They combine live sensor data with modular physics-based models, AI surrogates, and optimization algorithms [56–58]. Their interpretability is high because the physics modules anchor the AI components, and they integrate strongly with simulation and design tools. These systems achieve the highest maturity for real-time suitability, enabling adaptive control, predictive maintenance, and fleet-level decision support. However, they require substantial volumes of operational data and present high deployment complexity, including the need for robust data pipelines and advanced computing infrastructure [56].

Third, physics-constrained neural networks (PcNNs) and CFD surrogates provide a balanced trade-off. By embedding governing equations directly into training, they reduce data dependency and achieve very high interpretability [17,21,29,31]. They are particularly suitable for virtual sensing, thermal and flow field reconstruction, and rapid design iteration. Their strong alignment with CFD and structural analysis workflows ensures excellent simulation compatibility, while their real-time suitability is medium to high once training is complete. Deployment complexity is moderate, reflecting the significant training demands and computational cost [25,36,62].

Finally, generative and model discovery approaches remain at an early stage of maturity. Generative models such as GANs, VAEs, and RNNs can create synthetic datasets to address data scarcity, while discovery methods such as SINDy extract simplified governing equations [8,24,69]. These approaches show promise for rare-event prognostics, transient validation, and synthetic data augmentation, but their interpretability is only moderate and their reliance on diverse datasets remains high [8,39,40]. Real-time suitability is limited, as most applications remain experimental or offline. Their simulation and design integration is also low-to-moderate, since they typically complement rather than directly embed within engineering workflows. Deployment complexity is moderate but validation requirements are significant, as unconstrained generative models may produce non-physical signals. Overall, these methods should be regarded as exploratory rather than production-ready, representing a frontier for future research rather than a proven industrial standard.

Together, these categories show a clear path of development. It begins with ANN models for component-level monitoring, moves through physics-constrained surrogates and mature hybrid operational architectures, and extends to generative and discovery methods. These newer approaches are still in the research stage, but they offer ways to handle rare events and data gaps. This progression reflects an evolution toward fully adaptive, fleet-integrated intelligent digital twins.

#### 4. Discussion and Future trends

This section examines the maturity of hybrid AI methods, the barriers that limit their deployment, and the opportunities for advancing intelligent gas turbine digital twins. It also highlights practical integration challenges and proposes a layered hybrid AI framework for future development.

#### 4.1. Comparative Maturity of Hybrid AI Methods

The maturity comparison presented in the results section 3 shows a clear progression from component-level entry points to fully integrated, adaptive system-level platforms. ANN-augmented thermodynamic models remain practical early-stage solutions due to their low deployment complexity and ease of implementation. However, their heavy reliance on synthetic datasets and limited interpretability restricts their adaptability to evolving operational scenarios [47,49]. At the opposite end, hybrid intelligent digital twins with embedded AI represent the highest maturity level, enabling real-time adaptive control, predictive maintenance, and fleet-wide optimization through

continuous sensor data integration [5,11,21,50,56]. These advanced capabilities, however, come at the cost of high deployment complexity, requiring significant infrastructure and robust data pipelines.

Physics-constrained neural networks (PcNNs) and CFD surrogates provide a middle ground. By embedding governing equations, they reduce data needs and improve interpretability. This makes them well suited for virtual sensing, thermal and flow field reconstruction, and rapid design iteration [17,25,27,28,31,33–36,39,45,59].

Generative and model discovery approaches remain less mature. They address rare-event data scarcity and improve interpretability by generating synthetic scenarios and discovering governing equations [8,24,30,37,40,69]. However, most applications are still offline, with limited real-time use. Similar patterns are visible in aerospace, where physics-informed operators, neural fields, and graph-based surrogates provide scalable alternatives to high-fidelity CFD for aerodynamic flow prediction and aeroelastic analysis [72–75]. These advances show lessons that can transfer to gas turbine digital twins, which face similar challenges of nonlinear dynamics, multiphysics coupling, and real-time requirements.

Overall, the trajectory is clear: starting with ANN-based models, moving through physics-constrained surrogates and hybrid operational frameworks, and extending to generative approaches for rare-event readiness. This aligns with evidence that hybrid AI outperforms purely data-driven or purely physics-based methods under degraded or uncertain conditions [19,22,42,43]. It also reflects industry trends toward multi-fidelity data fusion [71] and Bayesian PINNs for uncertainty-aware decision-making [70].

#### 4.2. Challenges and Opportunities

Despite the clear progress across hybrid AI categories, several common challenges continue to limit their full-scale deployment in intelligent gas turbine digital twins. Data scarcity remains a primary barrier: high-quality degraded-condition datasets are rare, and there is no standardized, open benchmarking framework for training and validation [3,4,8,11,62], making it difficult to evaluate competing approaches or accelerate technology adoption. High computational cost is another constraint, as real-time CFD surrogates and physics-constrained networks require substantial processing resources to operate within industrial timeframes [25,27,28]. Integration complexity adds further difficulty. Embedding hybrid AI into existing SCADA and plant control networks demands secure, low-latency data pipelines and strict compatibility with established operational protocols [56]. Integration must not compromise these core functions.

At the same time, the opportunities are significant. Generative models can expand limited datasets with realistic rare-event scenarios, improving model robustness under critical fault conditions [8]. Transfer learning offers a pathway to cross-platform generalization, enabling models trained on one turbine type to adapt efficiently to others [9]. Multimodal sensor fusion can strengthen situational awareness by integrating vibration, temperature, acoustic, and operational logs into a unified operational picture [71]. Embedding hybrid AI into secure, cloud-enabled digital twin platforms would support fleet-level lifecycle optimization, centralized monitoring, and coordinated decision-making across assets [56–58]. Finally, uncertainty quantification methods such as Bayesian PINNs can improve the trustworthiness of predictions, providing operators with confidence in AI-driven recommendations under uncertain or degraded conditions [70].

#### Operational Integration of Hybrid AI Intelligent Digital Twins

A critical but often underexplored challenge for hybrid AI digital twins is their integration into the operational ecosystem of gas turbine plants. While SCADA and cybersecurity concerns are frequently mentioned, successful deployment also depends on alignment with control room practices, reliability standards, and regulatory compliance.

First, control room practices and operator trust are decisive for adoption. Hybrid AI predictions must be communicated through operator-facing dashboards in terms of conventional key performance indicators (e.g., efficiency, heat rate, turbine inlet temperature) rather than opaque

anomaly scores. Experience from the Electric Power Research Institute (EPRI) Turbine Digital Twin shows that embedding AI-driven virtual sensors and predictive health indicators directly into SCADA displays improves operator acceptance and supports daily decision-making [56]. Similarly, GE Vernova's digital twin integrates AI outputs into performance dashboards that enable load adjustments and cost-optimization strategies [57]. Siemens' ATOM platform extends this approach to fleet operations, combining AI with physical models for load sharing and maintenance planning [58]. These examples demonstrate that human–machine interface considerations are as critical as modeling accuracy.

Second, reliability standards and safety protocols define the operational envelope within which hybrid AI must function. Gas turbine fleets operate under strict reliability and safety requirements, with condition-based maintenance strategies ensuring that inspection intervals and load allocations do not compromise safety margins. Hybrid AI systems must therefore embed physical constraints into optimization loops to guarantee that recommendations remain within certified operational limits. Previous reviews of diagnostic and monitoring practices [6,41,62] emphasize that long-term adoption of hybrid AI depends on demonstrable improvements in reliability and compliance with established maintenance frameworks.

Third, cybersecurity and data pipeline integrity impose additional restrictions on integration architectures. Since SCADA systems are designated as critical infrastructure, hybrid AI models must be deployed within secure, low-latency data pipelines that preserve both availability and resilience. [11] highlighted that predictive maintenance platforms must address issues of sensor synchronization, robust pipelines, and secure integration with existing supervisory control systems. Likewise, [51] emphasized that embedding advanced ML frameworks into physical systems introduces additional complexity in ensuring stable and secure operation. These studies underscore that operational integration is not only a technical challenge but also a regulatory and organizational one.

Together, these considerations highlight that hybrid AI deployment requires not only algorithmic advances but also the design of secure, operator-trusted, standards-compliant integration pathways that enable intelligent digital twins to be adopted at scale in critical energy infrastructure.

#### 4.3. Future Research Directions and Proposed Hybrid AI Framework

Future research in hybrid AI for intelligent gas turbine digital twins should focus on four complementary priorities. First, developing standardized benchmarks and open datasets is essential to accelerate model innovation and ensure fair, transparent performance comparisons across hybrid AI methodologies [3,4,8,11,62]. Second, advancing uncertainty quantification and physics-informed transfer learning offers a pathway to more robust and generalizable intelligent digital twin solutions, capable of adapting across diverse turbine platforms and operating conditions [9,19,70]. Third, the industry must establish secure, scalable integration strategies that support plant-wide intelligent digital twins with real-time monitoring and predictive control, while ensuring cyber resilience and operational reliability [11,51,56-58]. Finally, there is significant potential in ensemble and layered hybrid AI architectures that merge ANN-based diagnostics, physics-constrained surrogates, and generative models to deliver rare-event readiness, improved interpretability, and faster deployment timelines [17,22,24,30,47]. To address these priorities, this review presents a layered hybrid AI framework for gas turbine intelligent digital twins. The framework shown in Figure 6 is organized into four synergistic layers: a Physics Backbone anchoring thermodynamic and component models, an AI Modeling Layer integrating advanced learning architectures, a Robustness and Uncertainty Layer incorporating generative models and uncertainty quantification, and an Optimization and Intelligence Layer enabling predictive control and fleet-level decision-making.

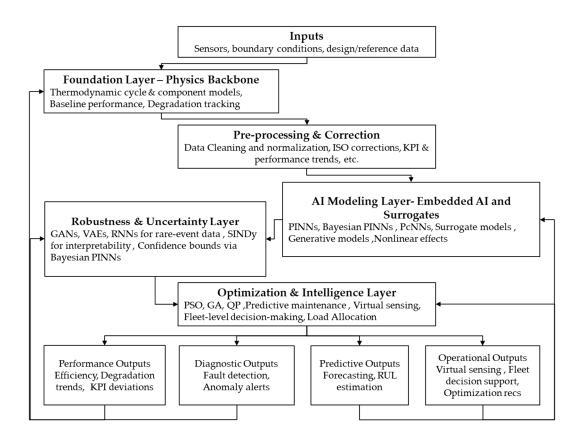


Figure 6. Proposed hybrid AI framework for gas turbine intelligent digital twins.

#### 4.3.1. Physics Backbone (Foundation Layer)

Physics Backbone (Foundation Layer). At the base, physics-based thermodynamic and component models provide consistent performance predictions and interpretable degradation characterization. This ensures that the digital twin remains grounded in established conservation laws and engineering principles, offering trustworthy baseline estimates for critical parameters such as efficiencies, flow capacity, and heat balance residuals.

#### 4.3.2. AI Modeling Layer

Building upon this foundation, advanced machine learning modules extend model fidelity and speed. This includes Physics-Informed Neural Networks (PINNs) [31] and Bayesian/variational PINNs [29,70] for uncertainty-aware diagnostics, as well as operator-learning surrogates—such as LSTMs, graph neural networks [34,35], and neural operators like Fourier Neural Operators (FNO) and DeepONet [28,65]. These models capture nonlinear degradation effects and accelerate computationally intensive CFD and structural simulations. In practice, PINNs can infer unmeasured combustion parameters (e.g., air–fuel ratio, combustion efficiency), while ANNs optimized with metaheuristics such as Particle Swarm Optimization (PSO) enable rapid, multi-output predictions of turbine inlet temperature, specific fuel consumption, and power output for real-time decision support [5].

#### 4.3.3. Robustness and Uncertainty Layer

To strengthen reliability under sparse or rare-event conditions, a dedicated layer addresses data augmentation and uncertainty quantification. Generative models such as GANs, VAEs, and RNNs [8] expand training datasets, while physics-informed data generation and model discovery techniques (e.g., PySINDy [24], sparse PDE learning [30], and SINDy [69]) extract interpretable governing equations for unseen scenarios. Uncertainty-aware approaches—including Bayesian

PINNs [70] and conformal prediction—attach confidence bounds to predictions, improving operator trust and providing actionable confidence levels for decision-making.

#### 4.3.4. Optimization and Intelligence Layer

At the highest level, embedded optimization and adaptive control modules enable predictive maintenance, virtual sensing, and fleet-wide decision-making. Low-latency optimization methods such as PSO, GA, and quadratic programming integrate with the digital twin workflow to recommend constraint-aware set-point adjustments and maintenance actions. As demonstrated in [5], these optimization loops can recover lost performance during alarm conditions while meeting industrial requirements for safety and responsiveness.

These integrated layers bridge design-phase simulations with real-time operational intelligence, creating a framework that is interpretable, scalable, and physics-consistent. By accurately capturing nonlinear behaviors and degradation mechanisms, the proposed architecture is particularly well suited to gas turbines, where high-fidelity physics and robust adaptability are essential for dependable operation. Overcoming persistent barriers—especially data scarcity, integration complexity, and computational cost—will require coordinated efforts across research communities, industrial partners, and standardization bodies.

The proposed framework aligns with emerging industrial implementations of intelligent digital twins, demonstrating both scalability and practical relevance. The EPRI turbine digital twin [56], designed for operator-focused integrated diagnostics, exemplifies how hybrid AI can be embedded into utility-scale platforms to enhance decision support. Similarly, the GE Vernova case [57] and the Siemens ATOM platform [58] illustrate fleet-wide deployment of intelligent digital twins, where cloud-enabled architectures and embedded AI modules deliver predictive maintenance, lifecycle optimization, and coordinated decision-making. These case studies validate the layered hybrid AI approach and highlight the pathway toward widespread adoption of intelligent digital twins in the gas turbine industry.

#### 5. Conclusions

This review introduced a classification and maturity framework for hybrid AI approaches in gas turbine intelligent digital twins. The analysis showed that no single method is universally superior. Each category including ANN-augmented thermodynamic models, physics-integrated operational architectures, physics-constrained neural networks with CFD surrogates, and generative/model discovery approaches, offers distinct trade-offs in data needs, interpretability, real-time suitability, and deployment complexity. Hybrid AI methods consistently outperform purely data-driven or purely physics-based approaches by improving diagnostic accuracy, computational efficiency, and resilience under degraded or uncertain conditions. Future progress will depend on standardized benchmarks, open datasets, secure integration with SCADA systems, and uncertainty-aware techniques such as Bayesian PINNs and physics-constrained generative augmentation to strengthen rare-event readiness. Overall, physics-informed hybrid AI provides a robust foundation for next-generation intelligent digital twins, enabling interpretable real-time monitoring and supporting the energy sector's transition to cleaner, more flexible, and resilient systems.

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#### **Abbreviations**

The following abbreviations are used in this manuscript:

AI Artificial Intelligence
ANN Artificial Neural Network
CFD Computational Fluid Dynamics
CHP Combined Heat and Power

CMS Condition Monitoring System

FNO Fourier Neural Operator GA Genetic Algorithm

GAN Generative Adversarial Network

GNN Graph Neural Network

GPA Gas Path Analysis

LNN Lagrangian Neural Network

ML Machine Learning

NPSS Numerical Propulsion System Simulation

NSFnet Navier-Stokes Flow Network

PcNN Physics-Constrained Neural Network

PDE Partial Differential Equation

PINN Physics-Informed Neural Network PIML Physics-Informed Machine Learning

PySINDy Python implementation of Sparse Identification of Nonlinear Dynamics

QP Quadratic Programming RNN Recurrent Neural Network

RUL Remaining Useful Life

SCADA Supervisory Control and Data Acquisition

SFC Specific Fuel Consumption

SINDy Sparse Identification of Nonlinear Dynamics

TIT Turbine Inlet Temperature VAE Variational Autoencoder

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