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Article

A Game-Based Scheme for Prime Minister Approval in Korea-like Presidential Systems

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Abstract: This paper addresses the issue of gridlocks in the approval of prime ministers in semi-presidential countries and presidential countries with prime ministers, focusing on the case of South Korea. A game-based scheme for prime minister approval specifically designed for presidential systems like Korea's is then proposed, along with two supporting provisions. The scheme has an adjustable parameter tentatively set at $3/5$ to ensure a balanced system, and it also introduces a new form of cohabitation — hard cohabitation — where the prime minister is not nominated by the president. The supporting provisions aim to cope with two challenges likely to arise from hard cohabitation: potential cabinet instability and difficulties in cooperation between the president and the prime minister. The reform package proposed here is thus believed to be smooth, fair, and effective, and is strongly hoped to be adopted by South Korea or other similar countries in the future.

Keywords: gridlocks; game theory; constitutional reform; presidential system; cohabitation

1. Prime Ministerial Appointment Gridlocks

In semi-presidential countries or presidential countries with prime ministers, it is commonly stipulated in the constitutions that the president needs approval from the parliament to appoint the prime minister. However, if the president and the parliament majority belong to opposing parties, the parliament may refuse to approve the nomination, even repeatedly, resulting in a gridlock. This is called an **appointment gridlock** in this paper.

In presidential countries, appointment gridlocks occur also for other executive officials. For example, in the United States, appointments of cabinet members need to be confirmed by the Senate. However, it is perceived by the present author that it is much more difficult to resolve appointment gridlocks for executive officials other than prime minister within the presidential setting. While that topic may be explored in a future paper, the current study is limited to the analysis of prime ministerial appointment gridlocks.

Prime ministerial appointment gridlocks are worth studying also because of their high visibility. In countries with prime ministers, the president makes decisions on ministerial appointments based on the prime minister's proposals, without requiring further parliamentary approval. Essentially, controlling the prime minister means having near-total control over the government. As a result, neither the president nor the parliament will easily give up this position.

We conducted a survey¹ on the prime ministerial appointment procedures of the 55 UN members that have a semi-presidential system or a presidential system with a prime minister, and our findings are tabulated below. For ease of comparison, the countries are divided into 5 geopolitical groups: mainstream European countries, Russia and former Soviet countries strongly influenced by Russia, Asian-Pacific countries, African countries, and American countries.

¹ Date of survey: 25-Dec-2024

Country	Prime Minister Must Be a Member of Parliament	Parliamentary Approval Required before Appointment	Parliament Can Remove Prime Minister by Vote of No-Confidence with Simple Majority	President Can Dissolve Parliament after [How Many Approval Failures or How Long after First Nomination, Pass of No-Confidence]
Austria	Normally YES	NO	YES	[Not Applicable, SP1]
Bulgaria	Normally YES	YES	YES	[2, NO]
Croatia	Normally YES	YES	YES	[2, YES]
Czech Republic	Normally YES	NO	YES	[2 Months, NO]
Finland	Normally YES	YES	YES	[Reasonable Time, NO]
France	Normally YES	NO	YES	[Not Applicable, SP2]
Georgia	Normally YES	YES	YES	[2, NO]
Lithuania	Normally YES	YES	YES	[2, NO]
Moldova	Normally YES	YES	YES	[45 Days, NO]
North Macedonia	YES	YES	YES	[20 Days, YES]
Portugal	YES	YES	YES	[2, SP2]
Romania	Normally YES	YES	YES	[60 Days, YES]
Serbia	YES	YES	NO	[3, YES]
Ukraine	NO	YES	NO	[60 Days, YES]
Russia	NO	YES	SP3	[3 Months, SP3]
Azerbaijan	NO	YES	NO	[3 or 3 Months, YES]
Belarus	NO	YES	NO	[3, NO]
Kazakhstan	NO	YES	NO	[3, YES]
Kyrgyzstan	YES	YES	SP4	[3, YES]
Tajikistan	NO	YES	NO	[1 Month, YES]
Turkmenistan	NO	NO	NO	[Not Applicable, NO]
Uzbekistan	NO	YES	YES	[2, NO]
Korea (South)	NO	YES	NO	[NO, NO]
Mongolia	YES	YES	YES	[30 Days, NO]
Sri Lanka	YES	NO	YES	[1 Month, NO]
Timor-Leste (East Timor)	YES	YES	YES	[30 Days, YES]
Algeria	NO	YES	YES	[1, YES]
Burundi	NO	YES	NO	[Not Specified, SP2]
Cabo Verde	NO	NO	YES	[Not Applicable, NO]
Cameroon	NO	NO	NO	[Not Applicable, SP2]
Central African Republic	NO	NO	YES	[Not Applicable, SP2]
Comoros	NO	NO	NO	[Not Applicable, NO]
Congo (Brazzaville)	NO	NO	NO	[Not Applicable, SP2]
Congo (Kinshasa)	NO	NO	YES	[Not Applicable, SP2]
Côte d'Ivoire	NO	NO	NO	[Not Applicable, NO]
Djibouti	NO	NO	NO	[Not Applicable, NO]
Egypt	NO	YES	YES	[30 Days, NO]
Gabon	NO	NO	YES	[Not Applicable, SP2]
Guinea	NO	NO	NO	[Not Applicable, SP2]
Guinea-Bissau	NO	NO	YES	[Not Applicable, SP2]
Madagascar	NO	NO	NO	[Not Applicable, SP2]
Mauritania	NO	NO	YES	[Not Applicable, SP5]
Mozambique	NO	NO	NO	[Not Applicable, SP2]
Namibia	YES	NO	NO	[Not Applicable, SP2]
Niger	NO	NO	YES	[Not Applicable, SP2]

Rwanda	NO	NO	NO	[Not Applicable, SP6]
Sao Tome and Principe	NO	NO	YES	[Not Applicable, SP2]
Senegal	NO	NO	YES	[Not Applicable, SP2]
Tanzania	YES	YES	YES	[60 Days, NO]
Togo	NO	NO	NO	[Not Applicable, SP2]
Tunisia	Normally YES	YES	YES	[4 Months, NO]
Uganda	YES	YES	YES	[NO, NO]
Guyana	YES	NO	YES	[Not Applicable, SP2]
Haiti	YES	NO	YES	[Not Applicable, NO]
Peru	NO	NO	YES	[Not Applicable, YES]

SP1: The president can dissolve the parliament if several chancellors in a row failed to secure parliamentary confidence.
SP2: No explicit mention of dissolution for this reason. But the president can dissolve the parliament for a wide range of reasons.
SP3: A single pass of no-confidence can be disregarded, but if no-confidence is passed for the second time within three months, either the prime minister is removed or the president dissolves the state дума and the prime minister stays until a new prime minister is in place.
SP4: In the case of no-confidence, the president has the option to retain the prime minister, but this can only happen once within a term of parliament. If a second no-confidence vote is passed, the president must remove the prime minister and appoint a new one.
SP5: If, in an interval of less than 3 years, two changes of government have intervened following a vote of no-confidence or of a motion of censure, the president can, after consulting the national assembly, pronounce the dissolution of it.
SP6: No explicit mention of dissolution for this reason. But the president can dissolve the parliament for a wide range of reasons, albeit only once.

We see that there are already three measures for avoiding or controlling prime ministerial appointment gridlocks: parliament membership requirement, relinquishment of prior approval, and dissolution of parliament. These measures are discussed below one by one.

Parliament membership requirement: All parliamentary countries have this requirement, so semi-presidential countries with strong parliamentary influence naturally have this requirement too. Thus the original purpose of this requirement is by no means avoiding gridlocks. But it indeed serves that purpose, as it dramatically reduces the number of choices that the president and the parliament have.

Relinquishment of prior approval: Many countries, such as France and Togo, have relinquished the requirement for the president to obtain formal parliamentary approval to appoint the prime minister, thereby eliminating appointment gridlocks. To be considered semi-presidential, these countries must allow the parliament to remove the prime minister with a simple majority, as France does. Those countries without this provision but with relinquishment of prior approval should be classified as presidential or even authoritarian countries.

Dissolution of parliament: Dissolving the parliament is the last resort to resolve a gridlock. In relation to prime minister, there are three scenarios that may call for the dissolution of the parliament: 1) In parliamentary countries, the parliament is so fragmented that they cannot even elect a prime minister for a prolonged period. This is quite rare. 2) In semi-presidential countries, the president and the parliament cannot reach an agreement on the selection of the prime minister for a long time. 3) The parliament has expressed no-confidence in the prime minister, but the president wants to retain them. Despite its high cost and potential for abuse, parliament dissolution is effective against gridlocks for two reasons: 1) It has deterrent effect to parliament members. 2) The new parliament may have a very different political composition than the old parliament. However, if the new parliament insists on the position of the old parliament, then either the gridlock persists or the president has to surrender, because a freshly elected parliament cannot be dissolved.

France is the prototype of a semi-presidential system. It has adopted all the above three measures, and it is indeed excellent both in eliminating gridlocks and in overall governance. In later sections, the measures used by France will be referenced for consideration.

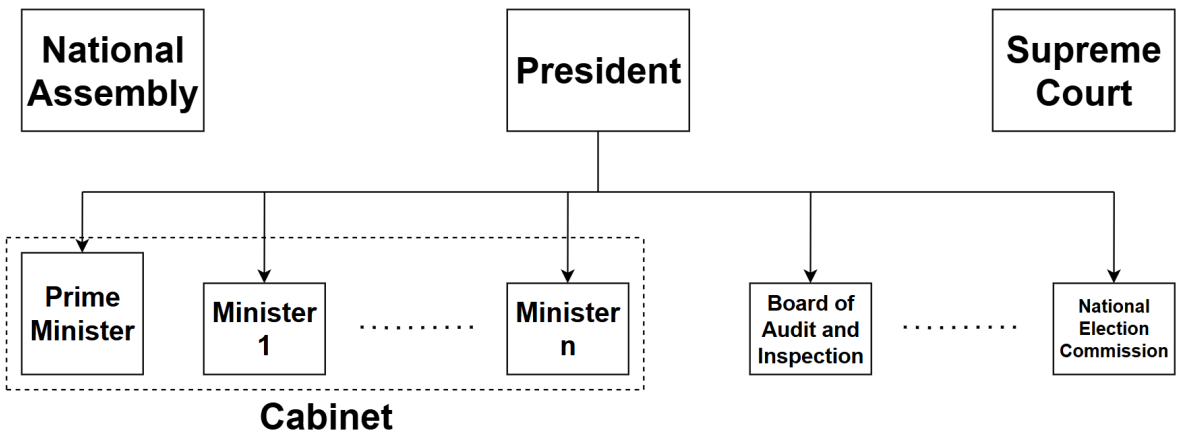
2. Prime Ministerial Appointment Gridlocks in Korea

References [1,2] have focused on the comparative study of prime ministerial appointment gridlocks, offering a broad overview of the topic. In contrast, our paper is specifically focused on Korea², making it closely tied to the country’s political system. It is more solution-oriented and offers more technical detail than the existing studies.

Korea is very special in that it is the only country in the world having the following properties:

- 1. The president is directly elected.
- 2. The parliament is directly elected and cannot be dissolved before its term expires.
- 3. There is a prime minister who is appointed by the president with approval from the parliament.
- 4. Unless convicted, the prime minister and other ministers can only be removed by the president.
- 5. The prime minister is the head of the cabinet, and the president appoints and dismisses other members of the cabinet (the ministers) based on the recommendations of the prime minister, without needing approval from the parliament.

Properties 1–4 are typical features of a presidential system, but Property 5 has a semi-presidential flavor. Overall, Korea is a presidential republic. In the sequel, we refer to a political system with Properties 1-5 as a **Korea-like** presidential system. Currently, there is only one Korea-like presidential system, which is Korea’s. But theoretically we cannot rule out other countries in the future may adopt a Korea-like presidential system.



Admittedly, Korea’s political system has essential properties not included in the above list. In other words, Korea is more than Korea-like. For example, Korea’s president has the power to dismiss the prime minister at will, but this was not mentioned above. This omission is intensional, as we will later propose modifications to the current Korean political system, and we want the modified system to remain Korea-like as defined above.

Now let us return to the discussion of prime ministerial appointment gridlocks. The framers of Korea’s current sixth republic constitution envisioned the prime minister’s appointment to resemble that of the U.S. Secretary of State, which is why they did not include provisions to address potential gridlocks in the appointment process. However, in terms of constitutional power, Korea’s prime minister is akin to the prime ministers of semi-presidential countries, and nearly all such countries have incorporated anti-gridlock provisions in their constitutions.

Historically, the political parties in Korea seemed to have respected the tradition formed during the authoritarian era, that is, the prime minister should be a subordinate to the president. Hence, each time a prime ministerial nomination was up for approval, even when the opposition controlled the National Assembly (Kore’s parliament), they ultimately gave up on obstructing the president’s nominee from being approved, who was always chosen from the president’s own camp. In other words, Korea’s political parties have been restrained in using their constitutional power. Therefore,

² In the body of this paper, we use “Korea” to refer to South Korea, that is, the Republic of Korea.

although there were in history a few gridlocks (see table below), they did not erupt violently and were finally resolved through negotiations.

Time	President	Nominee for Prime Minister	Party Controlling the National Assembly
1998	Kim Dae-jung (1998–2003)	Kim Jong-pil	Grand National Party (right wing)
2007	Roh Moo-hyun (2003-2008)	Kim Hwang-sik	Grand National Party (right wing)
2022	Yoon Suk-yeol (2022-)	Han Duck-soo	Democratic Party of Korea (left wing)

However, things are going to have a change, and we may not be as fortunate as we were. Political polarization in Korea has intensified, and recent events (President Yoon Suk-yeol ordered a curfew and was later impeached) have proven this point. Therefore, ad hoc, non-constitutional methods for resolving gridlocks may need to give way to systematic, constitutional ones.

3. The Game-Based Scheme for Prime Minister Approval

The French Approach for avoiding gridlocks is quite satisfactory per se, but if Korea were to adopt it, the whole constitution needs to be rewritten. A key fact is that the presidential system has been deeply rooted in the Korean culture, and a reform plan that would preserve the presidential system would be most likely to succeed. In this vein, the dissolution of parliament measure is not usable, and to be balanced, the parliament should not be granted the power to remove the prime minister with a simple majority; hence also to compensate it, the prior parliamentary approval should not be relinquished. Now in our arsenal we have two remaining weapons: parliament membership requirement and redesigning of the approval scheme. We discuss them one by one.

Parliament membership requirement: The advantages of this measure were discussed in the previous section. However, Korea has the tradition of choosing prime ministers from bureaucrats, such as past ministers, mayors, diplomats, etc., therefore restricting the choice to parliament members may be very controversial. So this measure will only be partially adopted in the scheme we describe later.

Redesigning of the approval scheme: Our current approval scheme is based on a false hypothesis: The parliament is unselfish; by going through the approval process they will help the president filter out candidates with poor character or insufficient ability, while also being happy to accept candidates who belong to the president’s camp. But the reality is: The parliament itself can be very partisan; what they care most is usually not the candidate’s character or abilities, but is the candidate’s political alignment. This is human nature, which we cannot resist. Therefore, we should redesign our approval scheme to respect and even leverage this nature, which means we must accept the candidate to be somewhat of a compromise between the president and the parliament. And when the opposition party holds a strong majority (two thirds, for instance) in the parliament, we must accept **cohabitation**.

Now it is time to provide a detailed description of our redesigned scheme. It is presented in the form of simulated Korean constitution articles.

Article N1

The office of Prime Minister shall be deemed vacant under any of the following circumstances:

1.

The term of the President who appointed the Prime Minister expires.

2.

The Prime Minister resigns and the resignation is confirmed by the President.

3.

The Prime Minister is dismissed by the President.

4.

The Prime Minister dies or is declared permanently incapacitated through a legal procedure.

5.

The Prime Minister is convicted in an effective judicial ruling.

Article N2

In the event of a vacancy in the office of Prime Minister, if the remaining term of the President is longer than forty days, the following procedures shall apply:

1. The President shall, within fourteen days after the vacancy, nominate a President's Candidate for Prime Minister to the National Assembly.
2. The National Assembly shall, within ten days after the President's nomination, either accept the nomination, or elect from the Members of the National Assembly a Legislative Quasi-Candidate for Prime Minister, and hold a vote of confidence on said quasi-candidate. If and only if the quasi-candidate receives the confidence of more than half of the Members of the National Assembly in the vote, the National Assembly shall nominate him or her as the Legislative Candidate for Prime Minister on the day of the vote.
3. If the National Assembly accepts the President's nomination or fails to nominate a Legislative Candidate for Prime Minister, the President shall appoint the President's Candidate for Prime Minister as Prime Minister.
4. If the Legislative Candidate for Prime Minister receives the confidence of at least three-fifths of the present Members of the National Assembly in the vote of confidence, the President shall, within one day after the vote, appoint the Legislative Candidate for Prime Minister as Prime Minister. Otherwise, the President shall appoint either the President's Candidate for Prime Minister or the Legislative Candidate for Prime Minister as Prime Minister.

This scheme needs detailed explanations.

1. This scheme is competitive, or put differently, a game. The outcome is guaranteed within the specified time frame, with no possibility of delay. The current scheme, which is traditional approval, usually requires at least one side to make a concession. If neither side concedes, the process could be delayed indefinitely. The application of game theory in policy-making is explored in [3]. However, to the best of the author's knowledge, the use of game as a mechanism for selecting a prime minister has not yet been reported in the literature.
2. The 3/5 (present) threshold for cohabitation is higher than that of France, which is simple majority. This is reasonable given Korea's presidential history and culture. Moreover, by definition, the cabinet is the president's inner circle, and its responsibility is to assist the president in exercising executive power. This is another reason for the president to have more say on the formation of the cabinet.
3. The 3/5 (present) threshold for cohabitation, which will be called **cohabitation threshold** in the sequel, is a crucial parameter of our scheme. Its value set here is only tentative, and can be adjusted if it is inappropriate. This parameter must be set within the $(1/2, 1)$ interval, with two choices of the denominator when calculating the confidence ratio: all members or present members, and two choices from "more than" and "at least". If the parameter is set near 1, then our scheme results in a ultra-presidential system; if the parameter is set very near $1/2$, then our scheme results in a system resembling the French system.
4. We partially adopted the parliament membership requirement. For the president's candidate, it is not required, but the legislative candidate is required to be a parliament member. The legislative candidate particularly relies on support from the parliament, and by requiring this, the election is entirely within the parliament, making it much simpler and more efficient. Countries that adopt this requirement usually also stipulate that losing parliamentary membership means losing the position of prime minister. This we believe is unnecessary. Therefore in our scheme, parliament membership is required only when the legislative candidate is nominated.
5. It may seem odd that no vote on the president's candidate is arranged in our game-based scheme. But actually there is. The confidence vote on the legislative quasi-candidate is actually a vote of comparison between the two candidates, because all the members of parliament know that one of the two must win the position. It is thus no wonder that we set the threshold for legislative

candidate to simple parliamentary majority. If one becomes the legislative candidate, it means that the members of parliament believe they are a better choice than the president's candidate. To implement Article N2, the parliament will pass a resolution (or law, but a resolution should suffice), and the resolution is expected to include arrangement of hearings for the president's candidate and the candidates for legislative quasi-candidate, so that the members of parliament have a basis to rely on at the election.

6. The last sentence in Article N2 says that the president has two choices, but in fact we all know the president will definitely choose their own nominee. But we must write it this way, because otherwise, the president will be prohibited to appoint the legislative candidate, and that is absurd.
7. Why should the president provide their nomination first? If not, then the legislative candidate's failure to pass the cohabitation threshold will enable the president to appoint any person they want, who may be good for the president but bad for the people. By requiring the president to provide their nomination first, to win the game, the president is pressured to nominate a person with moderate positions, good image and strong qualifications. If the president insists on a candidate who is only loyal to them but lacking good qualifications, they risk losing the position of prime minister to their opposing camp.
8. Which scheme makes it easier for the president to pass their nomination, the current scheme or the game-based scheme? Hard to tell. The current scheme is multi-round, and no one can force the president to nominate a person not in their camp, albeit with the price of gridlocks. Our game-based scheme is single-round. However, comparing the two schemes in terms of a single round, the parliament is harder to reject the president's nomination with our scheme, because they now need to elect a very strong alternative candidate. This is very similar to the idea of "constructive vote of no confidence" adopted in the German Basic Law. In fact, our scheme was inspired from that idea. By the way, some may ask: "Why not arrange a traditional vote of approval first, if not approved, then proceed to the election of the legislative candidate?" Our answer is yes. It is perfectly compliant with the game-based scheme, because the scheme described above does not stipulate how for the parliament to decide to accept the president's nomination and how to elect their quasi-candidate, and a traditional approval vote is just an implementation of acceptance. However, that is not for their benefit. If the parliament does so, they will give the president extra chance of passing their nomination. Imagine the scenario: The president is left wing, and the parliament is composed of 35% left wing, 20% central wing, and 45% right wing. The central wing can cooperate with the left wing as well as the right wing. Now the president nominates a left wing candidate, then in the traditional approval vote, the left wing and the central wing vote for the candidate, and the nomination gets passed. But actually, if the traditional approval vote is not held, the right wing can ask for the help of the central wing, and they can pass the cohabitation threshold to win the position. By holding a traditional approval vote first, the parliament (which is right-leaning) loses a battle that they could have won.
9. Indeed, the very attributes of the current scheme that make it prone to gridlocks are also the ones that contribute to its two key advantages: avoiding hasty decisions through multiple rounds and ensuring acceptability by both sides. Thus, until better schemes are invented, the current scheme remains the most suitable for approving officials in neutral, independent agencies, while our game-based scheme is ideally suited for approving prime ministers. Compared with the current scheme, our scheme is more likely to yield a result that pleases only one side, and as a result, the prime minister is more likely to be politically polarized. But this is perfectly fine because cabinet members are allowed and even encouraged to be somewhat politically polarized. Moreover, in our defense, our game-based scheme is in fact also multi-round, only that the rounds are unofficial consultations between the involved parties. Furthermore, in the current scheme, there is no mechanism to quantify whether the demands or concessions of each party are reasonable or not, or to determine who should bear responsibility for gridlock if it occurs. A crafty president might even play this trick: They first nominate a candidate completely at their will, whom the

parliament will almost certainly reject, then the president concedes gradually, ultimately making the parliament feel that they've rejected too many times and, fearing the responsibility of a gridlock, reluctantly approves the president's nomination. An honest president would, for the first time, nominate a candidate who has been carefully compromised, but would instead face strict scrutiny from the parliament and fail to be approved. In short, the current scheme has the tendency to award crafty, tough parties, while punish honest, concessive ones. With our game-based scheme, all these problems disappear, and a crafty or tough president has no chance of gaining any advantage; on the contrary, they will be punished by losing the game.

10. Depending on the composition of the parliament, the president's candidate could either be their ideal choice or a compromise candidate reached after consultations with other parties in the parliament. The 14-day period mentioned in Article N2 is reserved for such consultations. If the president nominates a compromise candidate, that nominee has a very high chance of being accepted. And a president who has made concessions is likely hoping to secure some assurances from their nominee. Therefore, this 14-day period can also be used for negotiations between the president and the nominee on power-sharing after taking office. Similarly, the 24(14+10)-day period allocated to the parliament is for intra-parliament bargaining, preliminary voting activities, and so on. If these time frames are not suitable, they can be adjusted.
11. This scheme does not stipulate that the two candidates must be different, because there is no need for that. The effect of having this rule is exactly the same as not having it.

Now, if a parliament member becomes prime minister, shall they retain, suspend, or resign their parliament seat? The "resign" option is too risky for them, because they will permanently lose their parliament seat while they may only be prime minister for a short time. The "retain" option is a direct violation of the separation of powers principle set out in the constitution. So the only reasonable option is "suspend". And then we have the following provision³:

Provision N3

A Member of the National Assembly shall not hold any office in the executive branch, except for the office of Prime Minister. During his or her tenure as Prime Minister, a Member of the National Assembly shall cease to function as a Member of National Assembly, and shall not be included in the total count of Members of National Assembly.

As for other ministers, there is no need to change the current practice, which is typical of a presidential system. In presidential systems, it is not encouraged to choose ministers from parliament members; to be a minister, a parliament member needs first to resign.

Article N2 is insufficient for a prime minister's vacancy due to the expiration of the president's term. If this article were applied, the new president would have to wait for about twenty days before appointing a prime minister. Without a prime minister, there can be no ministers, meaning that in the initial days of the new government, the state affairs will not be handled timely and effectively. Therefore, it is preferable for the new president to have a prime minister on the same day of their inauguration. For this reason, I have written the following article:

³ This rule is designated as a provision and intended to be included within an article, because it is considered not sufficiently broad or self-contained to constitute an independent article.

Article N4

During the period that there is a President-elect and on the day the President-elect assumes office, the following procedures shall apply:

1. The President-elect shall, within the thirty to fifteen days before he or she assumes office, nominate a President's Candidate for Prime Minister to the National Assembly.
2. The National Assembly shall, before the President-elect assumes office, either accept the President's nomination, or elect from the Members of the National Assembly a Legislative Quasi-Candidate for Prime Minister, and hold a vote of confidence on said quasi-candidate. If and only if the quasi-candidate receives the confidence of more than half of the Members of the National Assembly in the vote, the National Assembly shall nominate him or her as the Legislative Candidate for Prime Minister on the day of the vote.
3. If the National Assembly accepts the President's nomination or fails to nominate a Legislative Candidate for Prime Minister, the President-elect shall, on the day he or she assumes office, appoint the President's Candidate for Prime Minister as Prime Minister.
4. If the Legislative Candidate for Prime Minister receives the confidence of at least three-fifths of the present Members of the National Assembly in the vote of confidence, the President-elect shall, on the day he or she assumes office, appoint the Legislative Candidate for Prime Minister as Prime Minister. Otherwise, the President-elect shall, on the day he or she assumes office, appoint either the President's Candidate for Prime Minister or the Legislative Candidate for Prime Minister as Prime Minister.

When applying the above article, it is best that the parliament is the same before and after the new president takes office. If the presidential or parliamentary election dates are random (for example, in Korea, the parliamentary election dates are fixed, while the presidential election dates are random), there is a very small probability that the president's inauguration coincides with a parliamentary turnover. If both the presidential and parliamentary elections are scheduled on the same fixed date, it is possible to arrange for the new parliament to convene a month (in the United States this period is 17 days) before the new president's inauguration, which would further reduce this small probability to zero, and when the president-elect nominates a prime minister, the new parliament is already in session. A reform plan was recently proposed in [4] suggesting the introduction of fixed election dates and midterm elections in Korea.

4. Supporting Provisions of the Game-Based Scheme

4.1. Provisions for Cabinet Stability

Cabinet stability has never been an issue in the sixth republic of Korea, and we need to take care to ensure that this advantage is not lost after our reform proposal is adopted. The stability of the cabinet is essentially equivalent to the stability of the prime minister. Below, we will go through the various possibilities in which the prime minister might step down.

Possibilities that the prime minister wants to resign: If the prime minister wants to resign because they feel their performance is poor or because of public opposition, it is normal and there are no institutional reasons for it. Otherwise, the prime minister's desire to resign is generally due to a poor relationship with the president. There may be institutional reasons for it and the next subsection contains a relevant discussion about it.

Possibilities that the president wants to dismiss the prime minister:

1. The president feels that the prime minister's performance is poor, or there is public opposition against the prime minister or even the president, and in the latter case, the president wants to save themselves by throwing the prime minister under the bus. However, none of these are related to our new approval scheme, therefore we will not discuss them further.

2. The president finds it difficult to get along with the prime minister. There may also be institutional reasons for it and the next subsection contains a relevant discussion about it.
3. The president's party gained more seats in a recent parliamentary election and the president wants to replace the prime minister with someone who is closer to them. This is a normal political decision and should not be discouraged at the legal level.
4. The president thinks they made a bad decision in the nomination-approval process and got a prime minister they are dissatisfied with (who must be a legislative candidate). They want to dismiss the prime minister and go through the process again. This is usually a reckless action that would waste state resources and could even provoke an unnecessary crisis, and as such, it should be discouraged. So we have the following provision.

Provision N5

The President may dismiss the Prime Minister, but a Prime Minister who was not nominated by the President may be dismissed only if the National Assembly consents to the dismissal, or the National Assembly that nominated the Prime Minister has expired.

We believe the above provision provides sufficient deterrence, because obtaining parliamentary consent of dismissal is quite difficult, as now the parliament majority is held by the opposition.

With Provision N5, it is inaccurate to say that the president can dismiss the prime minister at will, and that is why we stated Property 4 in Section 2 that way.

Previously we mentioned the case that the president's party gains more seats in the election. How about the contrary? Imagine this scenario: the president's party shifts from being the majority party in parliament to a minority party. The parliament does not have the power to remove the prime minister. Therefore, if the prime minister doesn't have any problems of their own, then the parliament has no way of doing anything about the prime minister and the cabinet. However, if the prime minister is in poor health or involved in a scandal and needs to resign, then, through the process of selecting a new prime minister, the opposition may be able to grab the position of prime minister, and form a cabinet in their control. Therefore, in this case, the stability of the cabinet which the president can directly control depends on the prime minister's health and reputation.

There is also a practice worth mentioning, which is "fake resignation, actual dismissal". The president can, before nomination or appointment, request a candidate for prime minister to submit a resignation letter without a date. Then, at any time during the prime minister's term, the president can announce the prime minister's resignation, even though the prime minister does not actually wish to resign. In reality, this is effectively a dismissal. This practice is recognized in the constitutional practices of various countries. In our game-based scheme with Provision N5, there are two cases that this practice can be used:

1. A President's Candidate for Prime Minister may be requested for a resignation letter before their nomination, or later but before appointment, if there is a Legislative Candidate for Prime Minister who only fails to pass the cohabitation threshold, in which case the president has two choices. However, the president does not need to do so, because in this case the prime minister is nominated by the president, and the president can dismiss the prime minister at will.
2. A Legislative Candidate for Prime Minister who only fails to pass the cohabitation threshold may be requested for a resignation letter, because it is possible for the president to appoint them. In this case, the president genuinely needs this letter, as it allows the president to circumvent constitutional restrictions (see Provision N5).

A Legislative Candidate for Prime Minister who passes the cohabitation threshold is mandatorily to be appointed as prime minister. Therefore, the candidate will almost certainly refuse any such request, if it exists, therefore typically, the president will not make such a request to them.

Finally, it is believed that cabinet stability after adopting our game-based scheme with Provision N5 will be quite good. A fundamental fact is that who will be prime minister is largely determined

by the political composition of the parliament, therefore, the president can only expect to gain an advantage from changing the prime minister immediately following a parliamentary election, and as a result, the cabinet is expected to remain stable between parliamentary elections.

4.2. Provisions for Cohabitation

When the nomination-approval process is finished, the result can be one of the following:

1. **Non-cohabitation:** The prime minister and the president belong to the same party, so of course, the prime minister is nominated by the president.
2. **Soft cohabitation:** The prime minister and the president do not belong to the same party, but the prime minister is nominated by the president.
3. **Hard cohabitation:** The prime minister is not nominated by the president.

The term “hard cohabitation” has already appeared in the literature, for example, in [5]. In existing studies, it typically refers to a situation characterized by significant conflict or tension between the president and the prime minister. Clearly, the term is used with a different meaning in this paper. We initially sought to avoid terminological conflicts but were unable to find a better term to convey our intended meaning. As a result, we have no choice but to retain “hard cohabitation”. Another reason for this choice is that the situation we define as “hard cohabitation” often coincides with the scenario described by the term in the existing literature.

Earlier, we used the term “cohabitation”, but it actually means “hard cohabitation” here. The distinction between hard cohabitation and the other two terms is legal in nature, whereas the difference between soft cohabitation and non-cohabitation is mere political.

In Korea, there have been cases exclusively of non-cohabitation. In France, there have been cases of non-cohabitation and soft cohabitation. Hard cohabitation (as defined in this paper) is the artifact of our game-based scheme, and has never appeared in human history so far.

In [6], analysis is provided about the dynamics of semi-presidential systems and presidential systems, with a focus on the relationship between presidents and prime ministers. In this paper, we will look at the issue with a different perspective. The constitution leaves a significant grey area regarding the distribution of powers between the president and the prime minister. The appointment and dismissal of every cabinet member and government official require the president and the prime minister to consult and reach a common decision. However, if both use their constitutional powers to the fullest, a deadlock occurs when their opinions differ. In the case of non-cohabitation, since the president is superior to the prime minister within their party, the president’s opinion often prevails, thus avoiding a deadlock. In the case of soft cohabitation, the relationship between the president and the prime minister is like that of a “mentor” and “disciple”. Additionally, since they usually have a power-sharing agreement reached before the nomination, a deadlock generally does not occur. The issue is severest in the case of hard cohabitation. The two may refuse to cooperate, leading to a more frequent deadlock. This issue needs to be addressed, and we suggest to amend the constitution to include a provision as follows.

Provision N6

The President may exercise final discretion in the appointment and dismissal of the Minister of Defense, other officials in the Ministry of Defense whom the President is legally authorized to appoint, the Minister of Foreign Affairs, and other officials in the Ministry of Foreign Affairs whom the President is legally authorized to appoint.

The purpose of this provision is that, in the absence of a power-sharing agreement, the president and the prime minister can each govern their respective domains with minimal interference from one another. This arrangement for cohabitation, where the president is in charge of defense and foreign affairs, while the prime minister is responsible for domestic affairs, has been in place in France for decades, but in France, it remains a constitutional convention and has not yet been codified. France

can use it as a constitutional convention because, in France, the prime minister is always nominated by the president, and there exists a power-sharing agreement — whether explicit or tacit — between them. But this is not the case with hard cohabitation, because there the prime minister is not nominated by the president. However, this provision does not forbid the president and the prime minister from reaching a power-sharing agreement later during their cohabitation. A power granted by the law does not have to be fully exercised; it is permissible to exercise a power with restraint in exchange for the other party's commitment. Therefore, if there is a power-sharing agreement between the two, the president may intervene in domestic affairs, while the prime minister may take on responsibilities in defense and foreign affairs, even in a situation of hard cohabitation.

Symmetrically, could we stipulate that the prime minister hold some decision-making power in domestic affairs? This is probably not a good idea. First, the president holds a higher ceremonial status than the prime minister, and such a provision could be seen as disrespectful to the president. Second, the constitution already grants the prime minister significant authority: in domestic matters, the prime minister's recommendations regarding the appointment and dismissal of ministers are legally binding. Third, introducing such a provision would create an overly rigid division of powers between the president and the prime minister, hindering their communication and potentially worsening their relationship. Then, is it appropriate to have such a provision specifically for hard cohabitation? Still no. In hard cohabitation, with Provision N5, the president has virtually no power to dismiss the prime minister, leaving them with no choice but to accept the prime minister's control over domestic affairs, unless they have a power-sharing agreement. Therefore, such a provision would be unnecessary.

5. Conclusion

We addressed the issue of gridlocks in the approval of prime ministers in semi-presidential countries and presidential countries with prime ministers. After analyzing prime ministerial appointment gridlocks in South Korea, we explored potential measures to resolve them. In light of South Korea's presidential culture, we proposed a game-based scheme for prime minister approval, specifically designed for presidential systems like Korea's. Our proposed constitutional reform incorporates this game-based approval scheme (comprising three articles and one provision) alongside two supporting provisions, requiring only minimal revisions to the existing constitution.

This scheme has two salient features. First, it is actually not a single scheme, but rather a family of schemes. It has a parameter that can be adjusted, enabling the political system to gradually transition from a French-style semi-presidential system to an ultra-presidential system. We have tentatively set the value of this parameter at $3/5$, which is considered balanced, though whether it is truly balanced awaits testing in future practice. Second, the scheme introduces a new form of cohabitation: hard cohabitation, in which the prime minister is not nominated by the president. Hard cohabitation will likely bring about two new challenges: potential cabinet instability and difficulties in cooperation between the president and the prime minister. And the two supporting provisions are specifically designed to address these challenges.

Overall, we believe that, if implemented, this reform will effectively eliminate gridlocks, ensure fairness for all parties, maintain cabinet stability, and preserve a balanced distribution of power between the president and the prime minister. We strongly hope that this reform will eventually be adopted by South Korea or other countries with similar presidential systems.

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