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Article

Physics-Based Hazard Assessment Of Anthropogenic Seismicity

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Abstract: Since the year 2001 and after decades of steady Magnitude ≥ 3 earthquake rate in the United States, the number of annual earthquakes have been increasing, deviating to up to 188 events in 2011. This is suspected to be human-induced. Although historical understanding of earthquakes have roots in classical mechanics and relatively slow motion of classical systems (e.g. plate tectonics), modern tools of physics such as statistical mechanics and complexity can shed light on processes which trigger seismicity, anthropogenic and otherwise. In this study, after introducing the methods of analysis, I have particularly examined anthropogenic processes such as wastewater and CO_2 injections which can trigger seismicity. The San Andreas Fault (SAF) and the lake-fillings nearby (Salton Sea) is chosen as a complex system of interest. Bayesian Hypothesis testing is used to better understand fault behaviors. As a case study, the SAF single-fault model with RMSE of 1.4 was improved to a two-fault model with RMSE of 1. Furthermore, anthropogenic effects on SAF itself are examined using tools of complexity.

Keywords: Bayesian; geophysical data analysis; seismicity; data assimilation; anthropogenic seismicity; complex systems

1. Introduction

Geophysicists do not yet understand the exact physical processes that cause earthquakes and this is evident in the fact that earthquakes often come as a surprise. Deformation of Earth's crusts which translate into earthquakes involve many-body problems and hence the emergence of a complex system. As an alternative approach to earthquake mechanics, Turcotte and Malamud have proposed that the tools of complexity rooted in statistical physics are capable of describing faults as a self-organizing complex system [1].

The San Andreas Fault is an example of such complex system in seismology, extending about 750 miles across central California (Figure 2.) Radiocarbon dating methods performed on this fault reveal the history of at least 10 episodes of large earthquakes on average every 132 years, ranging from the year 671 to January 9 1857 (with an estimated magnitude of 8.25) [2]. The absence of large earthquake episodes since, is explained using the theory that the fault-zone material do not heal after each de-formation and they lack strength needed to cause more destructive movements [3].

Tectonic faults behavior analysis is the central problem to geophysics and seismology [4–6] and therefore probabilistic hazard assessments require data assimilation and careful geophysical data analysis, which extend beyond the tools of complexity alone. Modern computational approaches to address fault analysis, such as Monte Carlo Markov Chain and Bayesian Inference are also rooted in statistical physics. In this study, these tools will be used to analyze fault behaviors in the presence of external factors such as hydrologic loads and anthropogenic activities (ranging from wastewater disposal to CO₂ induced seismicity, which are known to trigger earthquakes [7], in an attempt to guide better policy recommendations.

1.1. The Carbonate-Silicate Cycle

1.1.1. Earth

Walker et. al. in 1981 argued that the atmospheric CO₂ level on earth is controlled by the carbonate–silicate geochemical cycle [8] over geological timescales (Gyr). On a shorter timescale (yrs

1959-2020), the increasing CO_2 trend is shown in figure 1. Silicate weathering also impacts the Earth's climate and carbon cycle [9], which is a key process for removing anthropogenic fossil fuel emissions over the next 10-100 Kyr in the absence of any human interventions [10–13].

Sea Level vs. CO2 Concentration (Colored by Temperature Anomaly)

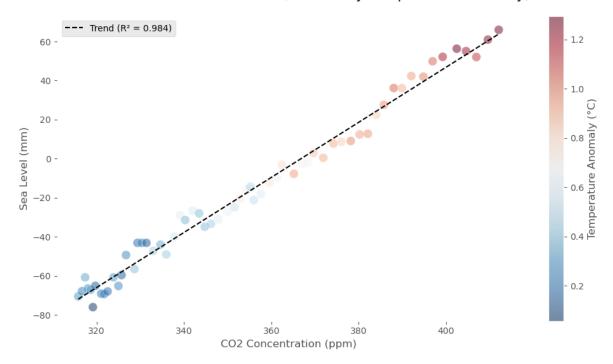


Figure 1. The correlation between variables of concern on Earth, over a few decades (1959-2020) with each data point corresponding to one year, with CO₂ as a hue, increasing every year. Higher CO₂ concentrations (Filtered annual data from Keeling et. al. [14]) are correlated with higher Sea Levels (As reported by Church 2011 and University Of Hawaii Sea Level Center) [15,16] and higher temperature anomalies (Data from: Met Office H. C. [17]).

1.1.2. Mars

On Mars, however, these cycles are not as well understood, given fewer experimental verifications which would require space missions for the purpose of Mars explorations (in the footsteps of NASA's Mariner 9 and Viking Missions). Nevertheless, the carbonate-silicate cycle (by a (H_2, CO_2) greenhouse gas is proposed to be the primary mechanism of Mars warming, with each cycle lasting up to 10 Myr, followed by extended periods of glaciation [18].

2. Bayesian Inference: The San Andreas Fault

Markov chain Monte Carlo (MCMC) has been widely used in Earth and Environmental sciences [19–22] and even in Cosmology and Materials Science [23–25]. Liu et. al. [26] have also shown that Bayesian inference can be used in inverse modeling of contaminants and air quality modeling and they used Bayesian analysis for Inverse modeling for Chernobyl and Fukushima Daiichi accidental releases of radionuclide. This author will use Bayesian Inference and MCMC to determine fault parameters from geophysical data, given a geophysical model, improving our understanding of fault mechanisms which lead to seismicity (for instance to study the relative motion of the American and Pacific plates across the San Andreas fault system, as shown in figure 2). Next, the model will be validated against the collected data and the corresponding RMSEs for each model will be calculated.



Figure 2. n aerial view of the San Andreas Fault System in Central California. It extends roughly 750 miles. Photo: [27].

2.1. The Inverse Problem: Why MCMC?

An inverse problem in science is the process (or processes) of calculating from a set of observations the causal factor(s) that produce(s) those observations [28].

$$d = [d_1, d_2, d_3, ..., d_N]^T$$
 (1)

$$M = [M_1, M_2, M_3, ..., M_N]^T$$
 (2)

That is to arrive at model parameters (The M Matrix), given data (The d Matrix). The complexity of this task increases with the model complexity and uncertainty. Meaning regular fitting methods would fail to produce satisfactory model parameters. Also, simple fittings do not use **prior knowledge** ¹ whereas MCMC as a tool in Bayesian Inference updates beliefs about model parameters based on data [28,29].

It is noteworthy that unlike the frequentist approaches that take errors as a flaw in measurements, the Bayesian approach sees error as a feature and not a flaw. This touches on the fundamental philosophy behind using such approaches in applications such as data assimilation.

2.2. Single Fault Model

The velocity function describing fault slip is given by [30]:

$$v(x) = \frac{v_0}{\pi} \tan^{-1} \left(\frac{x - x_0}{D} \right), \tag{3}$$

Where v_0 is the fault slip rate, D is the locking depth, x_0 is the fault location, and x is the spatial coordinate.

The validity of this model when applied to the San Andreas fualt, will be examined using Bayesian Inference and will be compared to the values reported in the literature. However, it is noteworthy that to date, there are several theories about whether this fault might pose risks of larger earthquakes to the surrounding areas. Smaller earthquakes experienced are explained using the theory that the fault-zone material do not heal after each deformation and they lack strength needed to cause more destructive movements [3].

Prior Knowledge, or simply the prior: Initial probability distribution assigned to a parameter or hypothesis before observing new data

2.3. Data

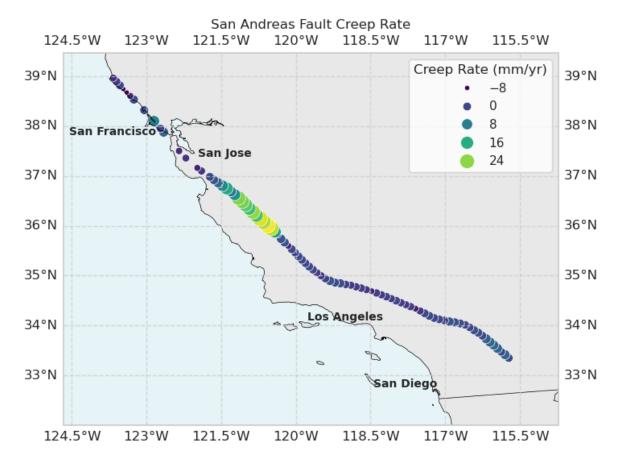


Figure 3. Location vs Creep rate data is visualized in Cartopy projection using Python. Raw data can be found in ref. [31]. The creep rate peaks between 35°N to 37°N, with a maximum of 31 \pm 3.5 (mm/year) appearing at (36.01°N, 120.57°W).

The creep rate GPS and InSAR data [31] is plotted and shown in figure 3. It is noteworthy that the creep rate peaks between 35°N to 37°N, and a maximum of 31 \pm 3.5 (mm/year) appears at (36.01°N, 120.57°W). For a better visualization of the creep rate, it is plotted against latitude and is shown in figure 4.

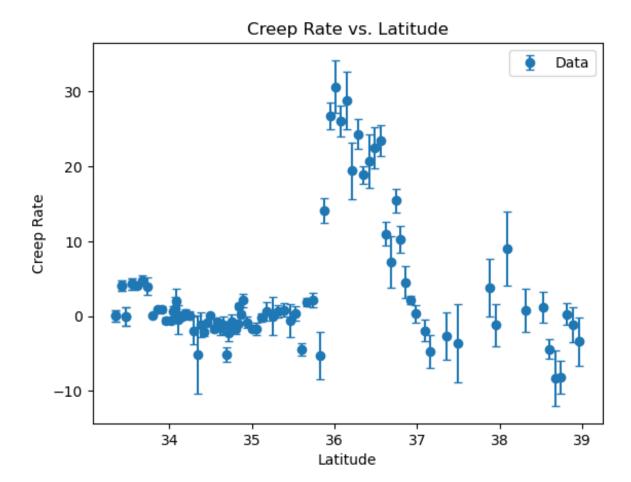


Figure 4. Creep rate vs Latitude and the corresponding uncertainties. Distributions of the uncertainties are plotted and shown in figure 5.

The Line Of Sight (LOS) velocity data [32] is assumed to have a variance of 1.

Creep rate uncertainty as suggested in [31] is 1.2 ± 1 (mm/year). The distribution of this uncertainty in measurement of the creep rate is shown in figure 5. The data is loaded from a file (available in the GitHub repository for this project), assuming a two column structure separated by commas. First column is assumed to be the x(positions) and the second is the velocities v(x). We also assume the the observational errors follow a Normal distribution, $y_j = v(x_j) + \epsilon_j$ Where $\epsilon_j \sim N(0, \sigma^2)$ and STD $\sigma = 1$ with respect to the model equation given in eq. 3.

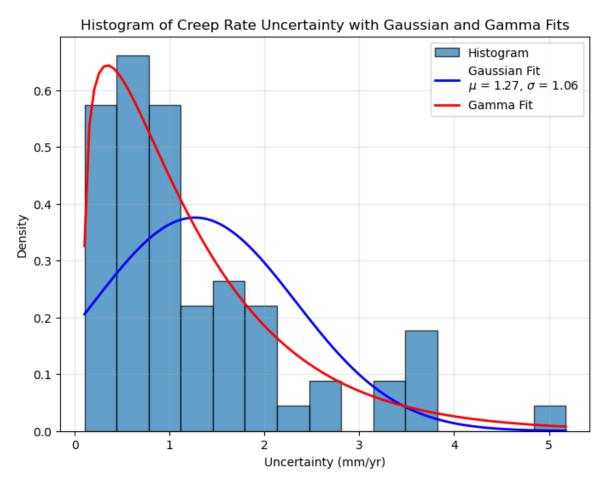


Figure 5. Creep rate uncertainty distribution plotted for San Andreas fault based on high resolution GPS and InSAR data from Ref. [31]. The Gaussian fit shows a μ of 1.27, however, given the existence of heavy tails, a Gamma fit might be a better choice to fit the uncertainty data than just using a normal distribution. Gaussian peaks around 1.27 while Gamma peaks around 0.5. In Gamma fits, the average doesn't represent the data.

2.4. Defining Log-Likelihood and Log-Prior

We want to know how well the model fits the data.

For Gaussian errors, the likelihood is [29,33]:

$$p(y_j|\theta) = \prod_{i=1}^{N_j} \frac{1}{\sqrt{2\pi\sigma^2}} \exp(-\frac{(y_j - v(x_j, \theta))^2}{2\sigma^2}).$$
 (4)

When taking the Log-Likelihhood, the product becomes a sum. Given $\sigma = 1$, it simplifies to

$$\log p(y_j|\theta) = A(-\frac{1}{2}\sum (y_j - v(x_j))^2)$$
 (5)

Where A is a constant throughout the MCMC process.

2.5. Bayesian Context

In Bayesian Context, the Posterior distribution of the parameters given the data $p(\theta|y)$, which is our goal, is given as:

$$p(\theta|y) = \frac{p(y|\theta)p(\theta)}{p(y)} \tag{6}$$

 $p(y|\theta)$ is the likelihood (How probable the observed data is under specific parameter values). $p(\theta)$ is our initial beliefs about the parameters. p(y) is the Evidence, which is a normalizing constant,

which can be ignored in MCMC since we are sampling ratios. So in order to find the posterior, we need to compute the likelihood, which determines how well a given set of parameters θ explains the data y.

2.6. Log-Prior, Single Fault

We have a uniform prior, where $p(\theta)$ is a constant if within bounds, and if not, zero. So log prior would be 0 if valid and $-\infty$ if not. The purpose of this is to constrain parameter ranges. For instance, v_0 and D both range between 0 and 80 while x_0 ranges from -50 to 50.

2.7. Random Walk Metropolis Sampler: Markov Chain Monte Carlo (MCMC)

$$p(\theta|y) \propto p(y|\theta)p(\theta)$$
 (7)

This algorithm implements the Metropolis-Hastings MCMC algorithm. Starting at an initial guess, we propose a new point $\theta' = \theta + S \cdot N(0,1)$ with S being the step scale. We then compute the log-posterior by taking the log of eq. 7, we arrive at:

$$\log p(\theta|y) \propto \log p(y|\theta) + \log p(\theta) \tag{8}$$

The outputs are chain of samples, log-posterior values and acceptance rate.

2.8. Applying MCMC: Single Fault Model Analysis

The mean and STD of v_0 , D, x_0 are our posterior stats. The posterior distribution and correlations are plotted in figure 6.

The MCMC model run over 30,000 samples burn-in of 5,000, step size 1.0:

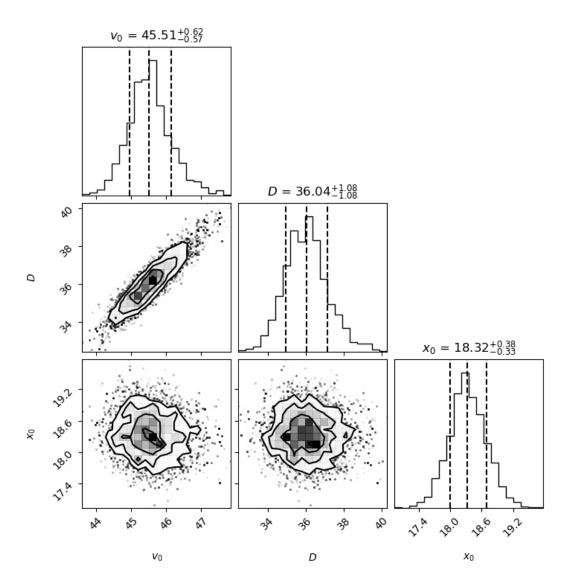


Figure 6. Posterior Plot: Visualizing the posterior distribution and correlations. Plotting data and 100 random posterior model curves. First few x values: [-97.922 41.985 95.654 -60.534 -86.19] First few v values: [-16.41 7.0886 14.671 -14.797 -16.455] Single-fault acceptance rate: 11%. Single-fault posterior means: [45.53 36.05 18.34] Single-fault posterior stds: [0.61 1.13 0.35]

2.9. Posterior Samples VS Data

Plot of the posterior samples vs Data is shown in figure 8.

2.10. RMSE and the Two-Fault Model

The RMSE is defined as

$$RMSE_i = \left(\frac{1}{N_s} \sum_{j=1}^{N_y} \left(\frac{y_j - \hat{v}(x_j, \theta_i)}{\sigma_j}\right)^2\right)^{1/2}$$
(9)

where y_i are the N_y observations of the velocity, σ_j are the standard deviations of the model errors and $\hat{v}(x_j,\theta_i)$ is the velocity at location x_j , using parameters θ_i . The RMSE for single-fault model is approximately 1.4. This is not disastrous, but not ideal either. To improve this, we consider a modified version of this model, namely "Two-Fault" model and see if we can arrive at a better RMSE.

2.11. The Two-Fault Model

In this model, instead of one fault, we consider two faults. We start by two-fault velocity, generalizing equation 3. , arriving at

$$v = \frac{v_{10}}{\pi} \arctan(\frac{x - x_{01}}{D_1}) + \frac{v_{02}}{\pi} \arctan(\frac{x - x_{02}}{D_2})$$
 (10)

The MCMC analysis is similar to that of single-fault model. The Two Fault Model Parameters are calculated and shown in table 1.

It is noteworthy that there is a negative correlation between the two velocities v_0^1 and v_0^2 and these are exclusively shown in figure 7.

Table 1. Two Fault Model Parameters.

23 ± 1
14 ± 1
0.4 ± 0.8
49 ± 1
14 ± 1
12 ± 1

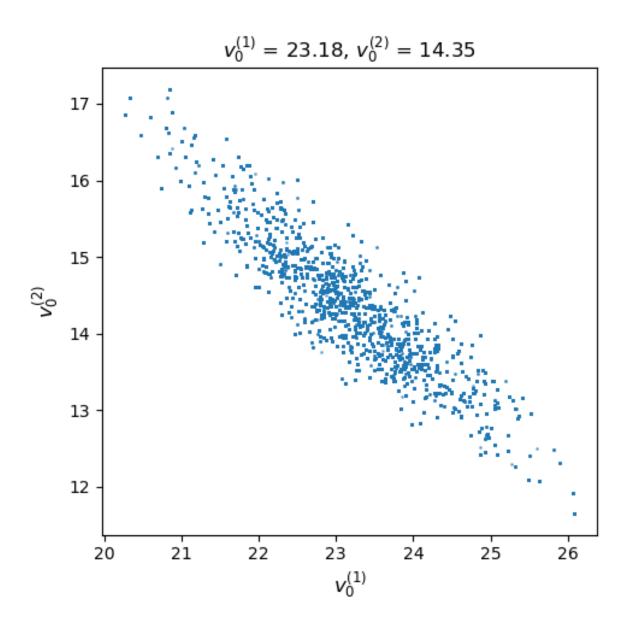


Figure 7. The negative correlation between the two velocities v_0^1 and v_0^2 are shown here.

For model validation, posterior samples are directly compared to experimental data. The error bars are not graphically displayed since they are relatively small and the points in figure 8 overlap in representing the data and the corresponding uncertainty.

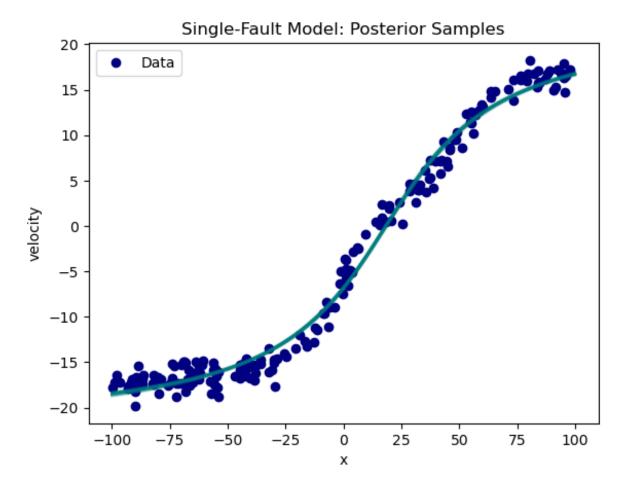


Figure 8. Posterior Samples VS Experimental Data for the geophysical single-fault model. The model fits well, but it is not ideal, given a relatively large RMSE of 1.4.

Although not very far from 1, the value of 1.4 for the RMSE is not ideal. Particularly around the origin (see fig. 8), the deviation of data from model become more obvious.

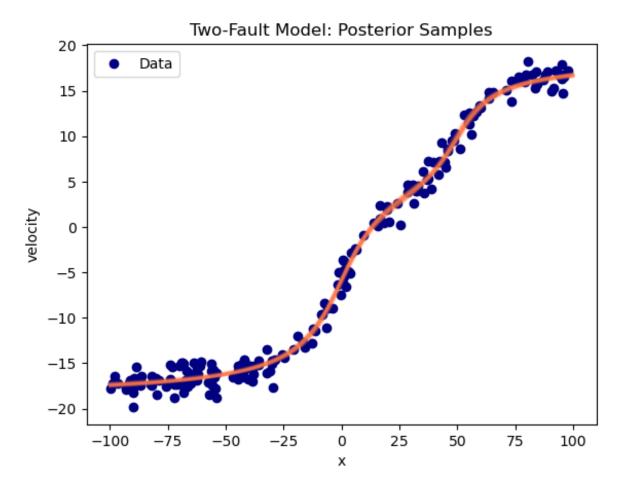


Figure 9. Two Fault Model Posterior VS Experimental Data. The RMSE is ≈ 1 .

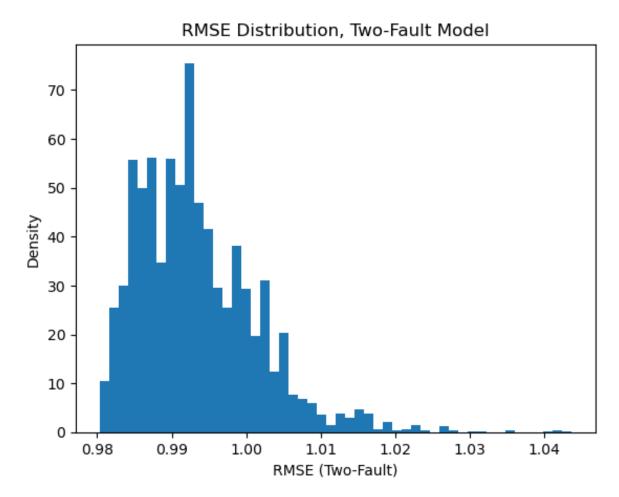


Figure 10. Two-Fault Model RMSE distribution.

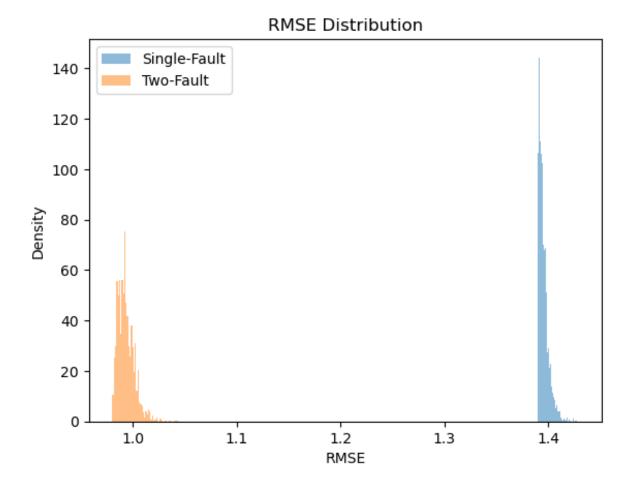


Figure 11. Two Fault Model RMSE distribution ≈ 1 (Left) VS Single Fault RMSE ≈ 1.4 (Right).

2.12. Fault Analysis: Discussion

Markov Chain Monte Carlo is a powerful method for Data Analysis. In this study, it was used as a tool in Inverse Problem, fitting model parameters to data. This geophysical model elegantly fit to data of 200 points. Using a single-fault model, the parameters were obtained, however with a RMSE of 1.4, which was not ideal. Therefore a Two-fault model was examined, arriving at a RMSE of 1.

Single Fault Model Parameters are displayed in Table 2.

Table 2. Single Fault Model Parameters

v_0	45.5 ± 0.6
x_0	18.3 ± 0.4
D	36 ± 1.1

Which all are within 95 % confidence intervals. These parameters and their error bars are plotted and presented in figure 12. It can be readily observed that the two models produce two different worldviews for the tectonic movements. The two-fault hypothesis which indicates that the two faults were formed at different times, is also backed by straightforward extrapolation of the record on the ocean floor [34].

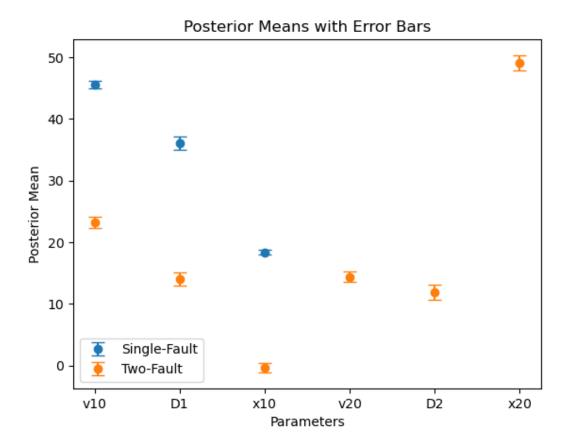


Figure 12. Model Parameter Values and their corresponding uncertainties, within 95 % Confidence Interval

2.13. Bayesian Hypothesis Testing

Based on new evidence, one can use Bayes's theorem to update the belief in a hypothesis. It is a powerful method which can be used to improve otherwise non-conclusive tests. The RMSE was already improved to the level of background noise and this can be easily seen comparing figures 5 and 11, however, Bayesian Hypothesis testing can further improve this. Widely Applicable Information Criterion (WAIC) and Bayesian Information Criterion were both applied. The result, which overwhelmingly favors the Two-fault model is plotted in figure 13.



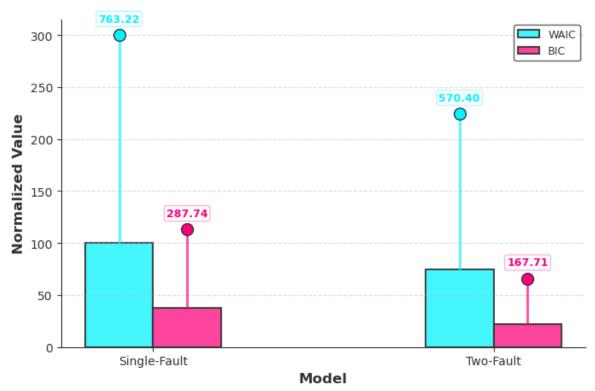


Figure 13. Comparison of the two models WAIC and BIC, which both favor the Two-Fault model. With lower values in the two methods in favor of the two-faults model.

3. Anthropogenic Seismicity

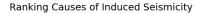
Under load, soil does not instantaneously deflect, but changes gradually and at a variable rate. This phenomenon is called **consolidation** and is mathematically formulated by Biot in 1940 [35]. Hill et. al.[36] argue that stress perturbations in the order of **0.5 MPa** are sufficient to trigger seismicity. These perturbations are dominated by pore pressure changes. They furthermore correlated the past 6 major earthquake events on the San Andreas Fault with high-stands of the ancient Lake Cahuilla, which its remnant is known today as the Salton Sea. Using Finite Element Methods (FEM) to arrive at such correlations, their model seems to be applicable to other regions where hydrologic loading is associated with seismicity, anthropogenic or not.

The anthropogenic seismicity risk factor, which I will define as \bar{R} here, (With the physical units of action per unit volume), generally follows an uncertainty relationship:

$$\Delta p \Delta t \ge \bar{R} \tag{11}$$

Where Δp represents the change in pressure and Δt is the time period, with \bar{R} resembling the system's minimized action per unit volume. This is due to the fact that higher pressures of fluid injections are usually carried out over shorter periods of time and lower pressures are carried out over a larger period of time. In other words, there is a tradeoff. For instance, a larger pressure of wastewater is injected over a short period of time while a smaller pressure of CO_2 is associated with CCS operations over longer periods of time. When examined as a complex system, this resembles a path which constraints the system's evolution in which soil consolidation undergoes dissipation.

A breakdown of these operations and their corresponding share of caused anthropogenic seismicity can be found in figure 14.



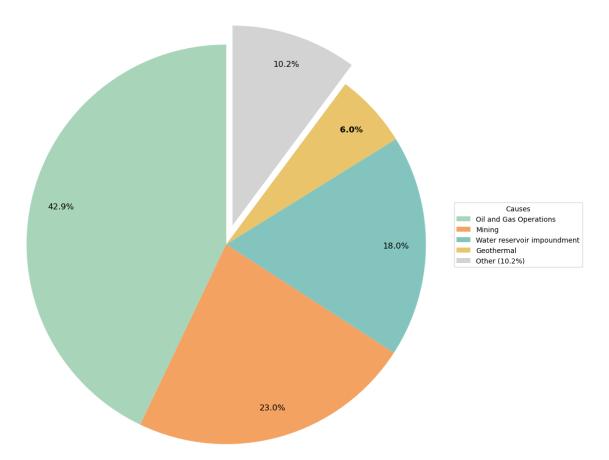


Figure 14. The share and recorded causes of anthropogenic earthquakes according to the Human Induced Earthquake Database (Hiquake) [37].

The probability of reservoir-seismicity to be widespread and deeper for a large reservoir is higher than that of a small one [38]. Elevated seismicity in Texas attributed to oil and gas extraction and fluid injections has also been observed [39], which is thought to be caused by pore pressure changes.

 CO_2 also stimulates plate tectonics due to mechanical pressure excreted by the injected fluids. In the past few years, as part of broader mitigation efforts, CO_2 has been injected into the earth. It is postulated that the injected CO_2 stays underground for decades. The pressure excreted by this gas can however threaten the integrity of the seals at injection sites. This requires further analysis on the operations as well as more simulations which could shed light on anthropogenic seismicity caused by geological injections.

It is noteworthy that the Los Angeles Oil Field produces about 3.5 barrels of oil per day and also faster than $1 \, mm/year$ LOS movement on the fault [40].

4. Discussions

Bayesian Inference certainly helps us better understand anthropogenic risks. Modern analysis tools such as the MCMC are therefore certainly useful in shedding light on contemporary problems in Earth Science and particularly inverse problems in geophysics.

Bayesian inference, however, is not a magic black box that could be used for compensating for poorly designed experiments and if information is primarily missing from data, no data analysis tools can reveal information out of thin air. That said, Bayesian inference could be used to better arrange for experimental setups to hunt for information that otherwise could not be captured [41]. This approach

can even further improve geophysics experiments which could contribute to the understanding of Earth and planetary processes and anthropogenic risk factors in seismicity.

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