On the Applicability of Quantum Machine Learning

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Abstract: In this article, we investigate the applicability of quantum machine learning for classification tasks using two quantum classifiers from the Qiskit Python environment: the Variational Quantum Classifier (VQC) and the Quantum Kernel Estimator (QKE). We test the performance of these classifiers on six widely known and publicly available benchmark datasets and examine how their performance varies depending on the number of samples for artificially generated test classification data sets.

Our results demonstrate that the VQC and QKE can outperform basic machine learning algorithms such as advanced linear regression models (Ridge and Lasso). However, they cannot match the accuracy and runtime performance of sophisticated modern boost classifiers like XGBoost, LightGBM, or CatBoost. We conclude that while quantum machine learning algorithms may eventually outperform classical machine learning algorithms in the future, particularly when physical quantum infrastructure becomes widely available, they currently remain inferior to classical approaches.

To promote further research in this area and ensure the transparency of our study, we provide the complete code in a linked GitHub repository.

Keywords: quantum machine learning; Variational Quantum Circuit; Quantum Kernel Estimator; Qiskit; Ridge; Lasso; XGBoost; LightGBM; CatBoost; classification; quantum computing; boost classifiers; neural networks

Quantum computing has recently gained significant attention due to its potential to solve complex computational problems exponentially faster than classical computers [1]. Quantum machine learning (QML) is an emerging field that combines the power of quantum computing with traditional machine learning techniques to solve real-world problems more efficiently [2,3]. Various QML algorithms have been proposed, such as Quantum Kernel Estimator (QKE) [4] and Variational Quantum Classifier (VQC) [5], which have shown promising results in diverse applications, including pattern recognition and classification tasks, [6–8].

In this study, we aim to compare QKE (Quantum Kernel Estimator) and VQC (Variational Quantum Circuit) with powerful classical machine learning methods such as XGBoost [9], Ridge [10], Lasso [11], LightGBM [12], CatBoost [13], and MLP (Multi-Layer Perceptron) [14] on six benchmark data sets partially available in the scikit-learn library [15] as well as artificially generated data sets. To ensure a fair comparison on the benchmark data sets, we perform a randomized search to optimize hyperparameters for each algorithm, thereby providing a comprehensive statistical comparison of their performance. Further, we provide the full program code in a GitHub repository [16] to make our results reproducible and boost research that can potentially build on our approach.

Since quantum machines are not readily accessible, we can only compare these algorithms' performance on simulated quantum circuits. Although this approach does not reveal the full potential of quantum machine learning, it does highlight how the discussed quantum machine learning methods handle different levels of complexity inherent in the data sets. This will estimate the possible improvements that basic quantum machine learning algorithms can offer over classical methods in terms of accuracy and efficiency, considering the computational resources needed to simulate quantum circuits.

In this study, we address and partially answer the following research questions:

1. How do QKE and VQC algorithms compare to classical machine learning methods such as XGBoost, Ridge, Lasso, LightGBM, CatBoost, and MLP regarding accuracy and efficiency on simulated quantum circuits?
2. To what extent can randomized search make the performance of quantum algorithms comparable to classical approaches?
3. What are the limitations and challenges associated with the current state of quantum machine learning, and how can future research address these challenges to unlock the full potential of quantum computing in machine learning applications?

The research presented in this article is partially inspired by the work of Zeguendry et al. [17], which offers an excellent review and introduction to quantum machine learning. However, their article does not delve into the tuning of hyperparameters for the quantum machine learning models employed, nor does it provide the complete program code of their experiments. Our intention is not to falsify their results and experiments but to broaden the discussion and examine the performance of quantum machine learning compared to classical counterparts and more sophisticated algorithms. This analysis will help determine the current state of quantum machine learning performance and whether researchers should employ these algorithms in their studies.

Furthermore, we provide the entire program code of our experiments and all the results in a GitHub repository, ensuring the integrity of our findings, fostering research in this field, and offering a comprehensive code for researchers to test quantum machine learning on their classification problems. Thereby, a key contribution of our research is not only the provision of a single implementation of a quantum machine learning algorithm but also the execution of a randomized search for potential hyperparameters of both classical and quantum machine learning models.

We a structured this article as follows:

Section 1 discusses relevant and related work.

In Section 2, we describe and reference all employed techniques. note that we will not discuss the mathematical details here but rather refer the interested reader to the referenced sources and the article by Zeguendry et al. [17].

The following Section 4 describes our performed experiments in detail, followed by the obtained results in Section 5, which also features a *discussion* of our findings.

Finally we conclude our findings in Section 6.

1. Related Work

Considerable research was conducted in the last years to advance quantum machine learning environments and their application field. This starts in the data encoding process, in which Schuld and Killoran [18] investigated quantum machine learning in feature Hilbert spaces theoretically. They proposed a framework for constructing quantum embeddings of classical data to enable quantum algorithms that learn and classify data in quantum feature spaces.

Further research was conducted on introducing novel architectural frameworks. For such, Mitarai et al. [19] presented a method called quantum circuit learning (QCL), which uses parameterized quantum circuits to approximate classical functions. QCL can be applied to supervised and unsupervised learning tasks, as well as reinforcement learning.

Havlíček et al. [4] introduced a quantum-enhanced feature space approach using variational quantum circuits. This work demonstrated that quantum computers can effectively process classical data with quantum kernel methods, offering the potential for exponential speedup in certain applications.

Furthermore, Farhi and Neven [5] explored the use of quantum neural networks for classification tasks on near-term quantum processors. They showed that quantum neural networks can achieve good classification performance with shallow circuits, making them suitable for noisy intermediate-scale quantum (NISQ) devices.

Other research focussed on advancing on applying quantum fundamentals on classical machine learning applications. Hereby, Rebentrost et al. [20] introduced the concept of a quantum support vector machine for big data classification. They showed that the quantum version of the algorithm can offer exponential speedup compared to its classical counterpart, specifically in the kernel evaluation stage.

To advance the application field of Quantum Machine Learning, Liu and Rebentrost [21] proposed a quantum machine learning approach for quantum anomaly detection. They demonstrated that their method can efficiently solve classification problems, even when the data has a high degree of entanglement.

In this regard, it is worth mentioning the work of Broughton et al. [22] introduced TensorFlow Quantum, an open-source library for the rapid prototyping of hybrid quantum-classical models for classical or quantum data. They demonstrated various applications of TensorFlow Quantum, including supervised learning for quantum classification, quantum control, simulating noisy quantum circuits, and quantum approximate optimization. Moreover, they showcased how TensorFlow Quantum can be applied to advanced quantum learning tasks such as meta-learning, layerwise learning, Hamiltonian learning, sampling thermal states, variational quantum eigensolvers, classification of quantum phase transitions, generative adversarial networks, and reinforcement learning.

In the review paper by Zeguendry et al. [17], the authors present a comprehensive overview of quantum machine learning (QML) from the perspective of conventional machine learning techniques. The paper starts by exploring the background of quantum computing, its architecture, and an introduction to quantum algorithms. It then delves into several fundamental algorithms for QML, which form the basis of more complex QML algorithms and can potentially offer performance improvements over classical machine learning algorithms. In the study, the authors implement three machine learning algorithms: Quanvolutional Neural Networks, Quantum Support Vector Machines, and Variational Quantum Classifier (VQC). They compare the performance of these quantum algorithms with their classical counterparts on various datasets. Specifically, they implement Quanvolutional Neural Networks on a quantum computer to recognize handwritten digits and compare its performance to Convolutional Neural Networks, stating the performance improvements by quantum machine learning.

Despite these advancements, it is important to note that some of the discussed papers may not have used randomized search CV from scikit-learn to optimize the classical machine learning algorithms, thereby, overstating the significance of quantum supremacy. Nevertheless, the above-mentioned works present a comprehensive overview of the state of the art in quantum machine learning for classification, highlighting the potential benefits of using quantum algorithms in various forms and applications.

2. Methodology

This section presents our methodology for comparing the performance of classical and quantum machine learning techniques for classification tasks. Our approach is designed to provide a blueprint for future experiments in this area of research. We employ the Scikit-learn library, focusing on the inbuilt functions to select a good set of hyperparameters, i.e., `RandomizedSearchCV` to compare classical and quantum machine learning models. We also utilize the Qiskit library to incorporate quantum machine learning techniques into our experiments, [23]. The selected data sets for our study include both real-world and synthetic data, enabling a comprehensive evaluation of the classifiers' performance.

3. Supervised Machine Learning

Supervised Machine Learning is a subfield of artificial intelligence that focuses on developing algorithms and models to learn patterns and make decisions or predictions based on data [24],[25]. The main goal of supervised learning is to predict labels or outputs of new, unseen data given a

set of known input-output pairs (training data). This section briefly introduces several classical machine learning techniques used for classification tasks, specifically in the context of supervised learning. These techniques serve as a baseline to evaluate the applicability of quantum machine learning approaches, which are the focus of this paper. Further, we will then introduce the employed quantum machine learning algorithms.

One of the essential aspects of supervised machine learning is the ability to predict/classify data. The models are trained using a labeled dataset, and then the performance of the models is evaluated based on their accuracy in predicting the labels of previously unseen test samples [26]. This evaluation is crucial to estimate the model's ability to generalize the learned information when making predictions on new, real-world data.

Various techniques, such as cross-validation and train-test splits, are often used to obtain reliable performance estimates of the models [27]. By comparing the performance of different models, researchers and practitioners can determine which model or algorithm is better suited for a specific problem domain.

3.1. Classical Supervised Machine Learning Techniques

The following list describes the employed algorithms that serve as a baseline for the afterwards described and later tested quantum machine learning algorithms.

- **Lasso and Ridge Regression/Classification:** Lasso (Least Absolute Shrinkage and Selection Operator) and Ridge Regression are linear regression techniques that incorporate regularization to prevent overfitting and improve model generalization [10,28]. Lasso uses L1 regularization, which tends to produce sparse solutions, while Ridge Regression uses L2 regularization, which prevents coefficients from becoming too large.

  Both of these regression algorithms can also be used for classification tasks.
- **Multilayer Perceptron (MLP):** MLP is a type of feedforward artificial neural network with multiple layers of neurons, including input, hidden, and output layers [14]. MLPs are capable of modeling complex non-linear relationships and can be trained using backpropagation.
- **Support Vector Machines (SVM):** SVMs are supervised learning models used for classification and regression tasks [29]. They work by finding the optimal hyperplane that separates the data into different classes, maximizing the margin between the classes.
- **Gradient Boosting Machines:** Gradient boosting machines are an ensemble learning method that builds a series of weak learners, typically decision trees, to form a strong learner [30]. The weak learners are combined by iteratively adding them to the model while minimizing a loss function. Notable gradient boosting machines for classification tasks include XGBoost [9], CatBoost [13], and LightGBM [12]. These three algorithms have introduced various improvements and optimizations to the original gradient boosting framework, such as efficient tree learning algorithms, handling categorical features, and reducing memory usage.

3.2. Quantum Machine Learning

Quantum machine learning is an emerging interdisciplinary field that leverages the principles of quantum mechanics and quantum computing to improve or develop novel algorithms for machine learning tasks [31]. This section introduces two key quantum machine learning techniques, Variational Quantum Classifier (VQC) and Quantum Kernel Estimator (QKE), and discusses their connections to classical machine learning techniques. Additionally, we briefly introduce Qiskit Machine Learning, a Python package developed by IBM for implementing quantum machine learning algorithms. Also, we want to mention the work done by [17] for a review of quantum machine learning algorithms and a more detailed discussion of the employed algorithms.

- **Variational Quantum Classifier (VQC):** VQC is a hybrid quantum-classical algorithm that can be viewed as a quantum analog of classical neural networks, specifically the Multilayer

Perceptron (MLP) [4]. VQC employs a parametrized quantum circuit, which is trained using classical optimization techniques to find the optimal parameters for classification tasks. The learned quantum circuit can then be used to classify new data points.

- **Quantum Kernel Estimator (QKE):** QKE is a technique that leverages the quantum computation of kernel functions to enhance the performance of classical kernel methods, such as Support Vector Machines (SVM) [32]. By computing the kernel matrix using quantum circuits, QKE can capture complex data relationships that may be challenging for classical kernel methods to exploit.

3.3. Qiskit Machine Learning

Qiskit Machine Learning is an open-source Python package developed by IBM for implementing quantum machine learning algorithms [23]. This package enables researchers and practitioners to develop and test quantum machine learning algorithms, including VQC and QKE, using IBM's quantum computing platform. It provides tools for building and simulating quantum circuits, as well as interfaces to classical optimization and machine learning libraries.

Thus we used this environment and the corresponding Quantum Simulators described in Appendix A for our experiments.

3.4. Accuracy Score for Classification

The accuracy score is a standard metric used to evaluate the performance of classification algorithms. We employed the accuracy score to evaluate all presented experiments. It is defined as the ratio of correct predictions to the total number of predictions. The formula for the accuracy score is defined as follows:

$$\text{Accuracy} = \frac{\text{Number of correct predictions}}{\text{Total number of predictions}} \tag{1}$$

In Scikit-learn, the accuracy score can be computed using the `accuracy_score` function from the 'sklearn.metrics' module [15].

For more information on the accuracy score and its interpretation, refer to the Scikit-learn documentation [15].

3.5. Data Sets

In this study, we used six classification data sets from various sources. Two data sets are part of the Scikit-learn library, while the remaining four are obtained/fetched from OpenML. The data sets are described below:

1. **Iris Data Set:** A widely known data set consisting of 150 samples of iris flowers, each with four features (sepal length, sepal width, petal length, and petal width) and one of three species labels (Iris Setosa, Iris Versicolor, or Iris Virginica). This data set is included in the Scikit-learn library [15].
2. **Wine Data Set:** A popular data set for wine classification, which consists of 178 samples of wine, each with 13 features (such as alcohol content, color intensity, and hue) and one of three class labels (class 1, class 2, or class 3). This data set is also available in the Scikit-learn library [15].
3. **Indian Liver Patient Dataset (LPD):** This data set contains 583 records, with 416 liver patient records and 167 non-liver patient records [33]. The data set includes ten variables: age, gender, total bilirubin, direct bilirubin, total proteins, albumin, A/G ratio, SGPT, SGOT, and Alkphos. The primary task is to classify patients into liver or non-liver patient groups.
4. **Breast Cancer Coimbra Dataset:** This data set consists of 10 quantitative predictors and a binary dependent variable, indicating the presence or absence of breast cancer [34**?**]. The predictors are anthropometric data and parameters obtainable from routine blood analysis. Accurate prediction models based on these predictors can potentially serve as a biomarker for breast cancer.

5. **Teaching Assistant Evaluation Dataset:** This data set includes 151 instances of teaching assistant (TA) assignments from the Statistics Department at the University of Wisconsin-Madison, with evaluations of their teaching performance over three regular semesters and two summer semesters [35,36]. The class variable is divided into three roughly equal-sized categories ("low", "medium", and "high"). There are six attributes, including whether the TA is a native English speaker, the course instructor, the course, the semester type (summer or regular), and the class size.

6. **Impedance Spectrum of Breast Tissue Dataset:** This data set contains impedance measurements of freshly excised breast tissue at the following frequencies: 15.625, 31.25, 62.5, 125, 250, 500, and 1000 KHz [37,38]. The primary task is to predict the classification of either the original six classes or four classes by merging the fibro-adenoma, mastopathy, and glandular classes whose discrimination is not crucial.

These data sets were selected for their diverse domains and varied classification tasks, providing a robust testing ground for the quantum classifiers we employed in our experiments.

Further, we used artificially generated data sets to control the number of samples, etc.. Here scikit-learn provides a valuable function called `make_classification` to generate synthetic classification datasets. This function creates a random n-class classification problem, initially creating clusters of points normally distributed about vertices of an n-informative-dimensional hypercube, and assigns an equal number of clusters to each class [15]. It introduces interdependence between features and adds further noise to the data. The generated data is highly customizable, with options for specifying the number of samples, features, informative features, redundant features, repeated features, classes, clusters per class, and more. For more details on the `make_classification` function and its parameters, refer to the Scikit-learn documentation available on scikit-learn.org.

4. Experimental Design

In this section, we describe our experimental design, which aims to provide a fair and comprehensive comparison of the performance of classical machine learning (ML) and quantum machine learning (QML) techniques, as discussed in Sections 3.1 and 3.2. Our experiments involve two main components: Firstly, assessing the algorithms' performance on artificially generated data sets with varying parametrizations, and secondly, evaluating the algorithms' performance on benchmark data sets using randomized search to optimize hyperparameters, ensuring a fair comparison. By carefully selecting our experimental setup, we avoid the issue of "cherry-picking" only a favorable subset of results, a common problem in machine learning leading to heavily-biased conclusions.

4.1. Artificially Generated Data Sets

To generate the synthetic classification dataset, we utilized scikit-learn's `make_classification` function. We employed two features and two classes while varying the number of samples to obtain a performance curve illustrating how the chosen algorithms' performance changes depending on the sample size.

We partitioned each dataset such that 20% of the original data was reserved as a test set to evaluate the trained algorithm, producing the accuracy score used for our assessment. Further, each data set was normalized such that all features are within the unit interval $[0, 1]$.

As a baseline, we employed the seven classical machine learning algorithms described in Section 3.1, namely Lasso, Ridge, MLP, SVM, XGBoost, LightGBM, and CatBoost. We used two different parameterizations for the classical machine learning algorithms for our comparisons. Firstly, we applied the out-of-the-box implementation without any hyperparameter optimization. Secondly, we used an optimized version of each algorithm found through scikit-learn's `RandomizedSearchCV` by testing 20 different models.

We then examined 20 distinct parameter configurations, each for the VQC and QKE classifiers, randomly selected from a predefined parameter distribution. Appendix A discusses the parameter grids for all utilized algorithms and all experiments.

4.2. Benchmark Data Sets and Hyperparameter Optimization

Our next experiment was to test the two employed quantum machine learning algorithms against the classical machine learning algorithms on six benchmark data sets (Section 3.5). For this reason, we employed scikit-learn's `RandomizedSearchCV` to test 20 randomly parameterized models for each algorithm to report the best of these tests. Again we used a train-test-split to keep 20% of the original data to test the trained algorithm. Further, each data set was normalized such that all features are within the unit interval $[0, 1]$.

5. Results

In this section, we present the results of our experiments, comparing the performance of classical machine learning (ML) and quantum machine learning (QML) techniques on both artificially generated data sets and benchmark data sets (Section 3.5). By analyzing the results, we aim to draw meaningful insights into the strengths and weaknesses of each approach and provide a blueprint for future studies in the area.

5.1. Performance on Artificially Generated Data Sets

In this section, we compare the performance of quantum machine learning (QML) algorithms and classical machine learning (ML) algorithms on artificially generated classification datasets. The comprehensive experimental setup can be found in Section 4.1.

Regarding accuracy and runtime, our findings are presented in Tables 1 and 2 and Figures 1, 2, and 3. While QML algorithms perform reasonably well, we observe that they are not a match for properly trained and/or sophisticated state-of-the-art classifiers. Even out-of-the-box implementations of state-of-the-art ML algorithms outperform QML algorithms on these artificially generated classification datasets.

The accuracy of the algorithms varies depending on the dataset size, with larger datasets posing more challenges. CatBoost performed best in our experiments, both out-of-the-box and when optimized in terms of high accuracy over all experiments. The Quantum Kernel Estimator (QKE) is the third-best algorithm overall in terms of accuracy, though it outperforms CatBoost regarding the runtime for CatBoost's optimized version. XGBoost and Support Vector Classification (SVC) follow closely, with competitive performances in terms of accuracy. However, Variational Quantum Circuit (VQC) struggles to achieve high accuracy compared to sophisticated boosting classifiers or support vector machines.

Other algorithms, such as Multi-Layer Perceptron (MLP), Ridge regression, Lasso regression, and LightGBM, exhibit varying performances depending on data set size and optimization. Despite some reasonable results from QKE, we conclude that classical ML algorithms, particularly sophisticated boosting classifiers, should be chosen to tackle similar problems due to their ease of implementation, better runtime, and overall superior performance.

In summary, while QML algorithms have shown some promise, they cannot yet compete with state-of-the-art classical ML algorithms on artificially generated classification datasets in terms of accuracy and runtime.

Table 1. This table presents the scores/accuracies of our experiments conducted on artificially generated classification data sets. This table is sorted in decreasing order of the average accuracy over all sample sizes of each algorithm. The parametrization for the QKE is as follows: QKE, Feature Map, Quantum Simulator, C-Value for the SVM-Algorithm The parametrization for the VQC is as follows: VQC, Feature Map, Ansatz, Optimizer, Quantum Simulator.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
CatBoost, OutOfTheBox	1.0	1.0	0.98	0.97	0.925	0.93	0.9425
CatBoost, RandomizedSearchCV	1.0	1.0	0.96	0.95	0.93	0.94	0.9425
QKE, PauliFeatureMap, statevector-simulator, 1000.0	1.0	1.0	0.96	0.93	0.93	0.93	0.925
XGBoost, RandomizedSearchCV	1.0	0.95	0.94	0.95	0.935	0.936667	0.95
SVM, RandomizedSearchCV	1.0	1.0	0.92	0.96	0.94	0.9	0.94
XGBoost, OutOfTheBox	1.0	0.95	0.94	0.96	0.91	0.936667	0.95
SVM, OutOfTheBox	1.0	1.0	0.92	0.92	0.94	0.933333	0.93
QKE, ZZFeatureMap, statevector-simulator, 177.82794100389228	1.0	1.0	0.94	0.93	0.915	0.926667	0.9225
QKE, ZFeatureMap, statevector-simulator, 5.623413251903491	1.0	1.0	0.92	0.91	0.925	0.93	0.9375
MLP, OutOfTheBox	1.0	1.0	0.94	0.89	0.905	0.916667	0.9275
MLP, RandomizedSearchCV	1.0	0.95	0.96	0.88	0.9	0.933333	0.94
Ridge, OutOfTheBox	1.0	1.0	0.94	0.88	0.9	0.896667	0.9025
Ridge, RandomizedSearchCV	1.0	1.0	0.94	0.88	0.88	0.893333	0.9025
QKE, ZFeatureMap, qasm-simulator, 5.623413251903491	1.0	1.0	0.94	0.82	0.91	0.92	0.9025
Lasso, RandomizedSearchCV	1.0	1.0	0.94	0.86	0.895	0.9	0.8875
QKE, ZZFeatureMap, statevector-simulator, 31.622776601683793	1.0	0.95	0.92	0.88	0.88	0.926667	0.9175
QKE, PauliFeatureMap, statevector-simulator, 5.623413251903491	1.0	0.95	0.92	0.85	0.895	0.93	0.92

Table 1. Cont.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
QKE, ZFeatureMap, statevector-simulator, 0.1778279410038923	1.0	0.95	0.9	0.88	0.9	0.92	0.9125
QKE, ZFeatureMap, aer-simulator, 0.1778279410038923	1.0	0.95	0.9	0.87	0.905	0.92	0.9125
QKE, ZZFeatureMap, qasm-simulator, 5.623413251903491	1.0	0.95	0.92	0.86	0.89	0.91	0.9175
QKE, PauliFeatureMap, qasm-simulator, 5.623413251903491	1.0	0.95	0.92	0.86	0.89	0.91	0.9175
VQC, ZFeatureMap, EfficientSU2, COBYLA, statevector-simulator	1.0	0.95	0.9	0.9	0.92	0.893333	0.88
VQC, ZFeatureMap, EfficientSU2, COBYLA, qasm-simulator	1.0	0.95	0.9	0.88	0.92	0.91	0.845
QKE, PauliFeatureMap, aer-simulator, 1.0	0.9	0.95	0.92	0.89	0.89	0.93	0.91
VQC, ZFeatureMap, EfficientSU2, SPSA, qasm-simulator	1.0	0.95	0.9	0.86	0.925	0.91	0.845
VQC, ZFeatureMap, EfficientSU2, COBYLA, aer-simulator	1.0	0.95	0.92	0.88	0.9	0.906667	0.8275
VQC, ZFeatureMap, EfficientSU2, SPSA, statevector-simulator	1.0	0.95	0.92	0.87	0.89	0.89	0.835
VQC, ZFeatureMap, RealAmplitudes, COBYLA, aer-simulator	1.0	0.95	0.9	0.86	0.905	0.85	0.865
LightGBM, RandomizedSearchCV	0.4	1.0	0.96	0.95	0.935	0.933333	0.95
LightGBM, OutOfTheBox	0.4	1.0	0.96	0.94	0.925	0.936667	0.9375
VQC, PauliFeatureMap, EfficientSU2, SPSA, qasm-simulator	0.9	0.75	0.9	0.84	0.89	0.86	0.8675
VQC, ZFeatureMap, EfficientSU2, NFT, statevector-simulator	1.0	0.95	0.86	0.72	0.9	0.776667	0.77
QKE, PauliFeatureMap, aer-simulator, 31.622776601683793	1.0	0.85	0.96	0.7	0.875	0.826667	0.735
QKE, ZFeatureMap, aer-simulator, 31.622776601683793	1.0	1.0	0.88	0.62	0.835	0.736667	0.7475

Table 1. Cont.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
QKE, PauliFeatureMap, aer-simulator, 1000.0	1.0	0.85	0.96	0.58	0.87	0.826667	0.665
VQC, PauliFeatureMap, EfficientSU2, SPSA, aer-simulator	0.8	0.75	0.9	0.73	0.845	0.86	0.8525
VQC, PauliFeatureMap, EfficientSU2, NFT, statevector-simulator	0.8	0.65	0.9	0.8	0.84	0.783333	0.8475
QKE, ZFeatureMap, qasm-simulator, 177.82794100389228	0.9	1.0	0.88	0.57	0.875	0.73	0.6375
VQC, ZZFeatureMap, EfficientSU2, COBYLA, aer-simulator	0.7	0.7	0.9	0.71	0.82	0.826667	0.835
VQC, ZZFeatureMap, RealAmplitudes, COBYLA, qasm-simulator	0.8	0.7	0.9	0.62	0.775	0.816667	0.785
VQC, ZZFeatureMap, RealAmplitudes, NFT, qasm-simulator	0.7	0.7	0.9	0.86	0.775	0.786667	0.535
VQC, PauliFeatureMap, RealAmplitudes, NFT, qasm-simulator	0.6	0.7	0.9	0.49	0.8	0.763333	0.78
VQC, ZZFeatureMap, RealAmplitudes, COBYLA, aer-simulator	0.5	0.65	0.84	0.73	0.83	0.83	0.575
QKE, PauliFeatureMap, aer-simulator, 0.03162277660168379	0.4	0.35	0.9	0.65	0.86	0.923333	0.8275
QKE, PauliFeatureMap, aer-simulator, 0.005623413251903491	0.4	0.35	0.9	0.49	0.75	0.766667	0.8275
QKE, PauliFeatureMap, qasm-simulator, 0.005623413251903491	0.4	0.35	0.9	0.49	0.75	0.766667	0.8275
QKE, ZFeatureMap, statevector-simulator, 0.005623413251903491	0.4	0.35	0.84	0.49	0.63	0.85	0.83
VQC, ZFeatureMap, TwoLocal, SPSA, statevector-simulator	0.7	0.65	0.52	0.51	0.52	0.493333	0.58
QKE, PauliFeatureMap, qasm-simulator, 0.001	0.4	0.35	0.9	0.49	0.48	0.753333	0.4975
Lasso, OutOfTheBox	0.4	0.35	0.5	0.49	0.48	0.506667	0.4975
VQC, ZZFeatureMap, TwoLocal, COBYLA, qasm-simulator	0.2	0.35	0.28	0.35	0.225	0.216667	0.3975
VQC, PauliFeatureMap, TwoLocal, SPSA, qasm-simulator	0.2	0.35	0.26	0.38	0.185	0.223333	0.4
VQC, PauliFeatureMap, TwoLocal, COBYLA, statevector-simulator	0.2	0.35	0.28	0.36	0.19	0.223333	0.39
VQC, PauliFeatureMap, TwoLocal, SPSA, statevector-simulator	0.2	0.35	0.28	0.36	0.19	0.223333	0.39

Table 2. This table presents the run times in seconds of our experiments conducted on artificially generated classification data sets. This table is sorted in increasing order of the average runtimes over all sample sizes of each algorithm. The parametrization for the QKE is as follows: QKE, Feature Map, Quantum Simulator, C-Value for the SVM-Algorithm The parametrization for the VQC is as follows: VQC, Feature Map, Ansatz, Optimizer, Quantum Simulator.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
Lasso, OutOfTheBox	0.002163	0.000836	0.000638	0.000596	0.000571	0.000552	0.000575
Ridge, OutOfTheBox	0.007653	0.001171	0.00121	0.001453	0.001333	0.00142	0.001452
SVM, OutOfTheBox	0.001014	0.000671	0.001049	0.002419	0.003195	0.005537	0.012677
XGBoost, OutOfTheBox	0.018497	0.008215	0.009782	0.021166	0.029465	0.032339	0.07877
LightGBM, OutOfTheBox	0.013812	0.012791	0.01488	0.027696	0.054648	0.04419	0.054521
MLP, OutOfTheBox	0.086815	0.090133	0.150594	0.231203	0.437073	0.647381	0.853657
SVM, RandomizedSearchCV	1.993112	0.410673	0.468471	0.4341	0.658507	0.945457	0.896971
XGBoost, RandomizedSearchCV	1.34873	0.358433	0.426441	0.519127	0.790996	1.049813	1.439898
Ridge, RandomizedSearchCV	2.357919	0.298155	0.469647	0.706193	0.662371	0.774265	0.835577
Lasso, RandomizedSearchCV	3.401839	0.482512	0.422395	0.473103	0.486651	0.438773	0.480838
CatBoost, OutOfTheBox	1.045732	1.243495	0.812176	0.762516	0.865055	1.9962	1.268149
LightGBM, RandomizedSearchCV	2.67037	0.536059	0.668838	0.900941	1.628797	1.389068	1.168039
VQC, ZFeatureMap, TwoLocal, SPSA, statevector-simulator	0.502447	0.82391	1.319602	2.9078	6.75953	11.81601	18.064725
VQC, PauliFeatureMap, TwoLocal, COBYLA, statevector-simulator	0.536454	0.886945	1.757877	3.486975	8.137821	14.688881	22.79476
VQC, PauliFeatureMap, TwoLocal, SPSA, statevector-simulator	1.981785	0.715829	1.621059	3.488372	8.517624	15.170185	22.300972
VQC, PauliFeatureMap, TwoLocal, SPSA, qasm-simulator	0.750719	1.154406	2.53449	5.000262	11.265137	19.493945	29.031463
VQC, ZZFeatureMap, TwoLocal, COBYLA, qasm-simulator	0.734865	1.097202	2.514703	4.990832	11.895971	19.283406	29.318269
MLP, RandomizedSearchCV	3.568304	2.701256	3.490188	8.736222	13.817605	20.424873	38.117078
QKE, ZFeatureMap, statevector-simulator, 0.1778279410038923	1.343983	0.802286	2.170829	5.965899	18.504546	36.659922	59.889941
QKE, ZFeatureMap, statevector-simulator, 0.0056234132519034941	0.411296	0.697461	2.154164	6.122564	19.670819	37.297334	62.1901
QKE, PauliFeatureMap, statevector-simulator, 1000.0	0.470933	0.956269	2.721257	7.2817	21.356298	40.130716	67.422908
QKE, PauliFeatureMap, statevector-simulator, 5.623413251903491	0.501446	0.922237	2.775664	7.454642	21.780637	40.426036	66.758927
QKE, ZFeatureMap, statevector-simulator, 5.623413251903491	0.378018	0.757363	2.141677	4.962464	19.901565	41.913003	71.453831
QKE, ZZFeatureMap, statevector-simulator, 31.622776601683793	0.214386	0.567282	1.650304	5.302437	20.77629	42.614517	72.871078

Table 2. Cont.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
QKE, ZZFeatureMap, statevector-simulator, 177.82794100389228	0.461093	0.943574	2.780804	7.580857	22.906811	41.955521	68.045553
CatBoost, RandomizedSearchCV	8.292872	7.778893	19.636858	43.697806	33.126305	51.559816	42.05208
VQC, ZFeatureMap, RealAmplitudes, COBYLA, aer-simulator	47.438183	63.446748	192.148143	404.233954	1060.291657	1619.397205	2290.222381
VQC, ZZFeatureMap, RealAmplitudes, COBYLA, qasm-simulator	43.113636	83.175558	166.040938	421.278374	1064.238564	1702.893006	2719.340939
VQC, ZZFeatureMap, RealAmplitudes, COBYLA, aer-simulator	45.909504	83.201411	152.20265	509.1956	1158.902532	1654.065907	2603.942577
VQC, ZFeatureMap, EfficientSU2, COBYLA, statevector-simulator	48.546243	81.030425	190.958188	402.121722	1044.855825	1807.676357	2751.241623
VQC, ZFeatureMap, EfficientSU2, COBYLA, aer-simulator	57.728111	100.590997	240.174666	507.58709	1253.080578	2139.855218	3196.07247
VQC, ZFeatureMap, EfficientSU2, COBYLA, qasm-simulator	59.058898	100.862056	242.285405	507.171731	1262.650143	2151.503499	3191.745568
VQC, ZZFeatureMap, EfficientSU2, COBYLA, aer-simulator	59.651649	105.629842	254.918442	601.245125	1335.017904	2260.354294	3366.65501
QKE, ZFeatureMap, qasm-simulator, 177.82794100389228	4.589478	13.184805	82.633779	332.71327	1337.102907	3020.689579	5368.201509
QKE, ZZFeatureMap, qasm-simulator, 5.623413251903491	4.352785	15.921249	97.165028	390.472092	1573.103197	3549.629798	6282.670251
QKE, PauliFeatureMap, aer-simulator, 0.03162277660168379	3.549125	15.094144	98.970568	393.496921	1581.662241	3554.962927	6317.355669
QKE, PauliFeatureMap, aer-simulator, 0.005623413251903491	3.373257	15.311538	99.2351	390.52131	1574.108371	3555.3048	6339.026443
QKE, PauliFeatureMap, qasm-simulator, 0.005623413251903491	3.812115	19.479307	101.289711	404.432384	1636.24686	3642.937393	6307.605039
QKE, PauliFeatureMap, aer-simulator, 31.622776601683793	3.848578	17.062982	101.387533	408.69903	1635.863136	3674.976257	6555.811507
VQC, ZFeatureMap, EfficientSU2, NFT, statevector-simulator	98.831974	167.48274	394.378037	836.913451	2197.652135	3719.047116	5621.134708
VQC, PauliFeatureMap, EfficientSU2, NFT, statevector-simulator	103.914165	177.047181	423.423603	1014.963511	2338.078356	3953.861723	5905.433094
VQC, ZZFeatureMap, RealAmplitudes, NFT, qasm-simulator	105.987181	183.918751	427.016702	1036.605473	2366.463152	4052.521035	6042.538015
VQC, PauliFeatureMap, RealAmplitudes, NFT, qasm-simulator	103.625823	180.306618	425.488049	1041.160999	2371.366715	4044.856475	6048.573929
VQC, ZFeatureMap, EfficientSU2, SPSA, statevector-simulator	119.513477	200.101417	474.113288	1008.932874	2601.731917	4505.306268	6781.089745
VQC, ZFeatureMap, EfficientSU2, SPSA, qasm-simulator	145.295744	256.711762	609.791229	1272.675059	3150.527537	5366.116602	8009.649075
VQC, PauliFeatureMap, EfficientSU2, SPSA, aer-simulator	144.280811	259.102175	625.193096	1502.476923	3356.340799	5689.827615	8454.144295
VQC, PauliFeatureMap, EfficientSU2, SPSA, qasm-simulator	152.666649	269.680847	642.400747	1505.762521	3388.662998	5709.505826	8438.957709
QKE, ZFeatureMap, aer-simulator, 31.622776601683793	5.993241	25.852654	166.703792	669.201309	2934.169598	6729.31411	12037.430687
QKE, PauliFeatureMap, qasm-simulator, 5.623413251903491	8.384715	32.795287	206.595473	890.414904	3753.488868	8537.768589	15232.745542
QKE, PauliFeatureMap, qasm-simulator, 0.001	7.792093	32.566225	207.832614	896.042249	3778.324351	8610.335147	15348.810142

Table 2. Cont.

Algorithm/Parametrization	Size 50	Size 100	Size 250	Size 500	Size 1000	Size 1500	Size 2000
QKE, ZFeatureMap, aer-simulator, 0.1778279410038923	10.511296	43.335078	276.810734	1111.545614	4799.032996	10979.135601	19768.073574
QKE, ZFeatureMap, qasm-simulator, 5.623413251903491	11.573929	43.186982	277.291314	1113.664313	4842.587094	10978.908476	19798.821156
QKE, PauliFeatureMap, aer-simulator, 1000.0	12.596938	51.788837	332.281104	1434.208601	5986.631006	13592.866065	24280.544075
QKE, PauliFeatureMap, aer-simulator, 1.0	12.261604	51.508959	332.561822	1423.111135	5984.902587	13603.956887	24362.83202
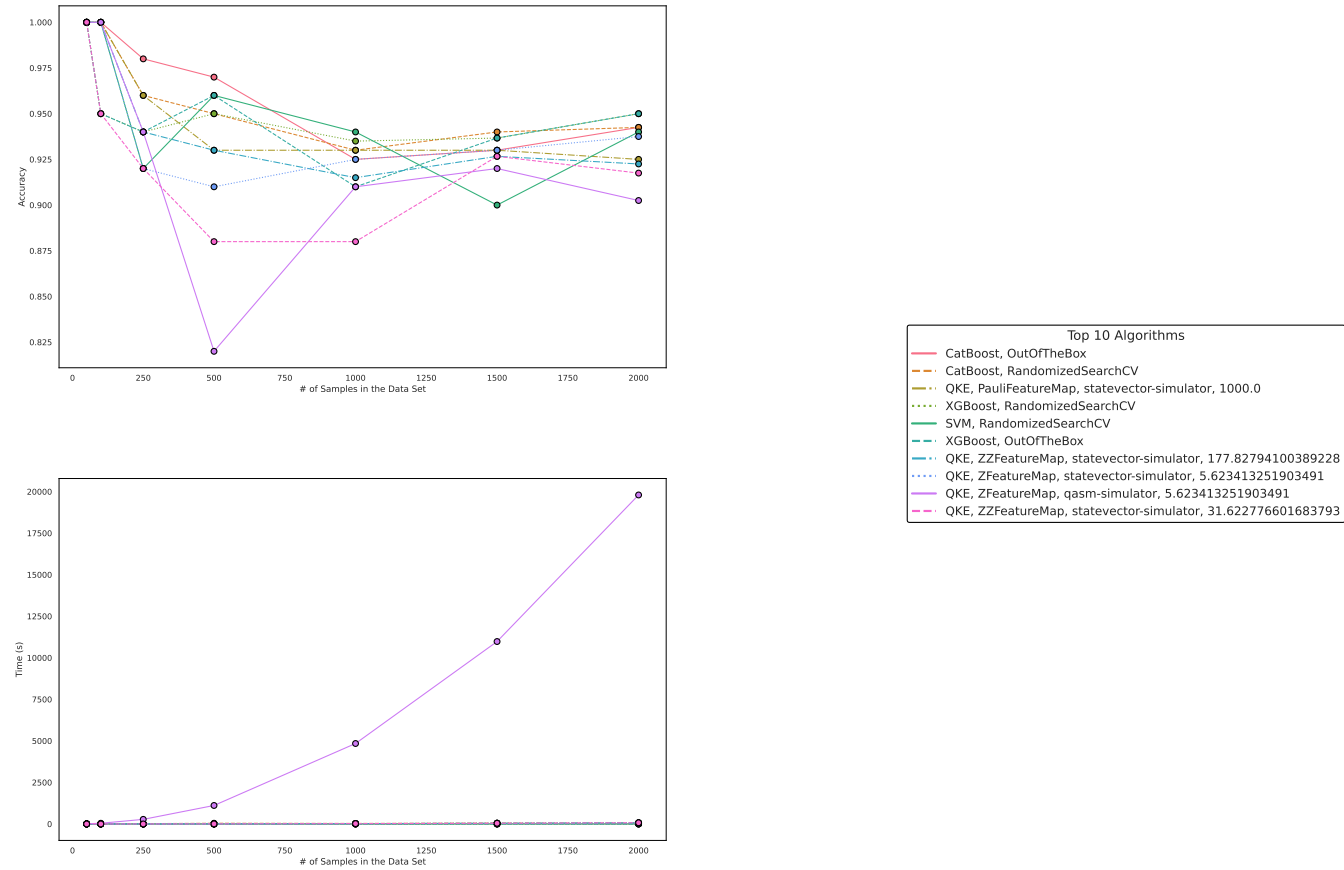
Figure 1. These figures depict the results from our experiments, comparing the five best QML and classical ML algorithms on artificially generated datasets in terms of accuracy. The upper part illustrates the accuracy of the algorithms on different sample sizes, while the lower part demonstrates how the runtimes change with increasing size of the test dataset. The right part contains the legend, indicating which algorithms were used, and more specifically, the different parametrizations of the employed Quantum Machine Learning algorithms. Furthermore, the legend is sorted in decreasi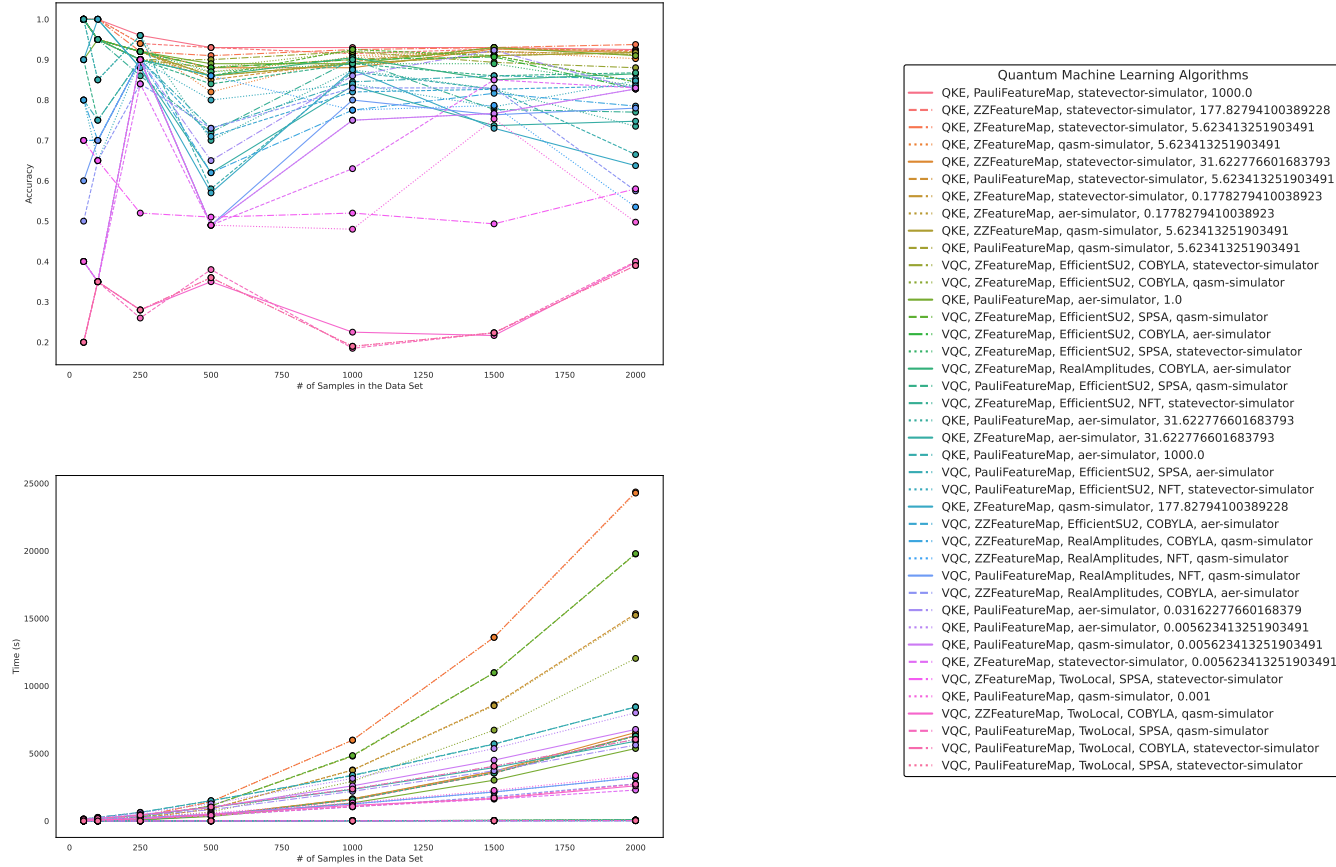ng order of the average accuracy of the employed algorithms. The parametrization for the QKE is as follows: QKE, Feature Map, Quantum Simulator, C-Value for the SVM-algorithm
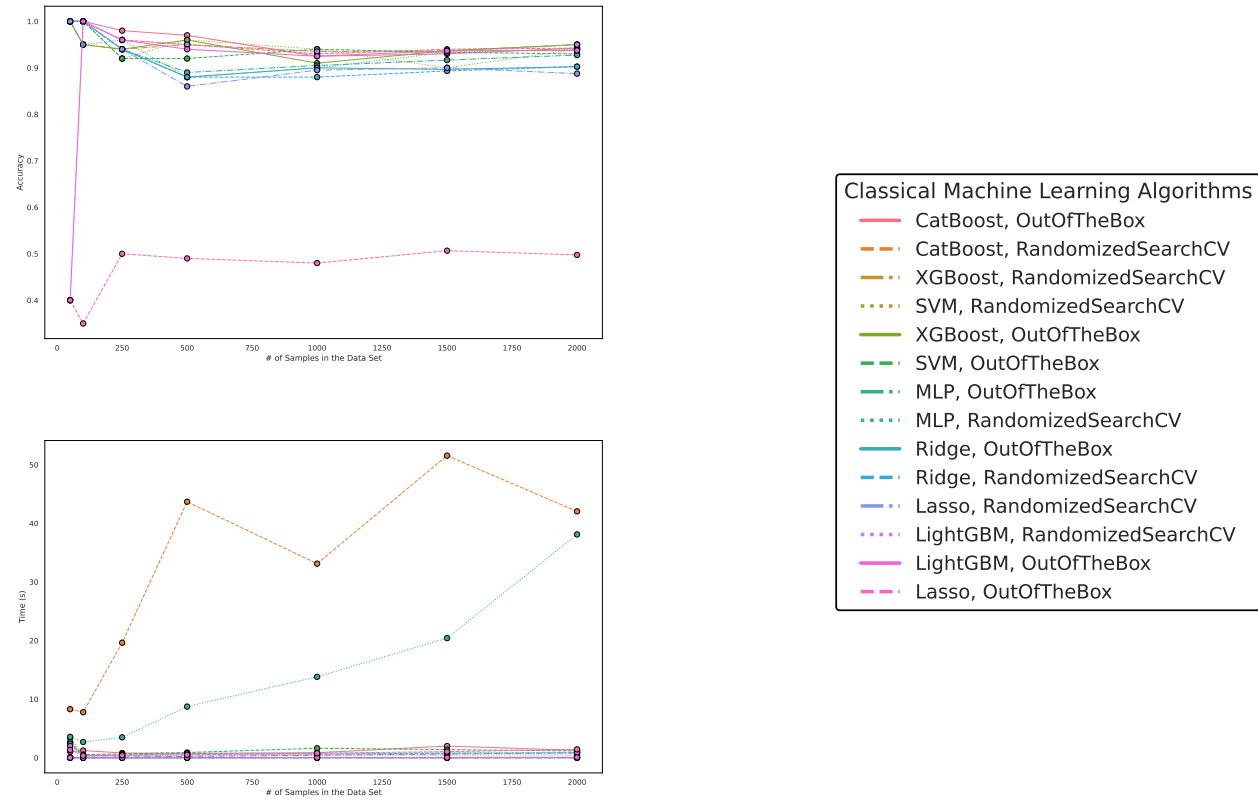
Figure 2. These figures depict the results from our experiments, comparing differently parameterized classical machine learning algorithms on artificially generated datasets. The upper part illustrates the behavior of the accuracies, while the lower part demonstrates how the run times change with the increasing size of the test dataset. The right part contains the legend, indicating which algorithms were used, and more specifically, the different parametrizations of the employed Machine Learning algorithms. Furthermore, the legend is sorted in decreasing order of the average accuracy of the employed algorithms.

Figure 3. These figures depict the results from our experiments for the artificially generated data sets, comparing differently parameterized QML algorithms on artificially generated datasets. The upper part illustrates the behavior of the accuracies, while the lower part demonstrates how the runtimes change with the increasing size of the test datasets. The right part contains the legend, indicating which algorithms were used, and more specifically, the different parametrizations of the employed Quantum Machine Learning algorithms. Furthermore, the legend is sorted in decreasing order of the average accuracy of the employed algorithms. The parametrization for the QKE is as follows: QKE, Feature Map, Quantum Simulator, C-Value for the SVM-Algorithm. The parametrization for the VQC is as follows: VQC, Feature Map, Ansatz, Optimizer, Quantum Simulator

5.2. Results on Benchmark Data Sets

In this section, we discuss the performance of quantum machine learning (QML) and classical machine learning (ML) algorithms on six benchmark datasets described in Section 3.5. We include results for the quantum classifiers detailed in Section 3.2 and the classical machine learning classifiers discussed in Section 3.1. The scores/accuracies were obtained using Randomized Search cross-validation from Scikit-learn with 20 models and 5-fold cross-validation.

Our results, shown in Table 3, display the best 5-fold cross-validation scores (upper table) and the scores of the best model evaluated on an unseen test subset of the original data (lower table), which makes up 20% of the original data. We observe varying performances of the algorithms on these benchmark datasets.

Notably, Variational Quantum Circuit (VQC) and Quantum Kernel Estimator (QKE) classifiers show competitive performance on several datasets but do not consistently outperform classical ML algorithms. In particular, QKE achieves a perfect score on the Iris dataset, but its performance varies across the other datasets.

Classical ML algorithms, such as Multi-Layer Perceptron (MLP), Support Vector Machines (SVM), XGBoost, LightGBM, and CatBoost, exhibit strong performance across all data sets, with some algorithms achieving perfect scores on multiple data sets. CatBoost consistently performs well, ranking as the top-performing algorithm on three of the six datasets. Ridge and Lasso regression show high accuracy on Iris and Wine datasets but perform poorly on the others.

When comparing the runtimes of the experiments, as presented in Table 4, it becomes evident that QML algorithms take substantially longer to execute than their classical counterparts. For instance, the VQC and QKE classifiers take hours to days to complete on various datasets, whereas classical ML algorithms such as Ridge, Lasso, MLP, SVM, XGBoost, LightGBM, and CatBoost typically take seconds to minutes.

This significant difference in runtimes could be attributed to the inherent complexity and resource requirements of QML algorithms, which generally demand specialized quantum hardware and simulators. On the other hand, classical ML algorithms are optimized for execution on conventional hardware, making them more efficient and faster to run.

In conclusion, while QML algorithms like VQC and QKE demonstrate potential in achieving competitive performance on certain datasets, their relatively longer runtimes and less consistent performance across the benchmark datasets may limit their practical applicability compared to classical ML algorithms. Classical ML algorithms such as CatBoost, XGBoost, and LightGBM continue to offer superior and more consistent performance with faster execution times, solidifying their place as reliable and powerful tools for classification tasks.

Table 3. These tables present the scores/accuracies of our experiments conducted on publicly available classification datasets. The upper table displays the best 5-fold cross-validation scores, obtained using Randomized Search cross-validation from Scikit-learn, which were employed to identify the optimal model. The lower table shows the scores of the best model evaluated on an unseen test subset of the original data. We include results for the six datasets described in Section 3.5, the quantum classifiers detailed in Section 3.2, and the classical machine learning classifiers discussed in Section 3.1.

Classifier\Dataset	Iris	Wine	ILPD	BC-Coimbra	TAE	Breast-Tissue
VQC	0.817	0.817	0.706	0.599	0.417	0.339
QKE	0.908	0.853	0.706	0.620	0.483	0.382
Ridge	0.914	0.875	0.080	0.053	0.053	<0.001
Lasso	0.914	0.870	0.085	0.004	0.004	<0.001
MLP	**0.975**	0.937	**0.712**	0.687	0.425	0.406
SVM	0.958	0.759	0.706	0.630	0.450	0.382
XGBoost	0.958	**0.986**	0.695	0.656	**0.533**	**0.441**
LightGBM	0.967	**0.986**	0.699	0.666	0.475	0.393
CatBoost	0.950	0.979	0.702	**0.688**	0.525	0.440

Classifier\Dataset	Iris	Wine	ILPD	BC-Coimbra	TAE	Breast-Tissue
VQC	0.767	0.639	0.744	0.541	0.388	0.334
QKE	**1.0**	0.833	0.744	0.792	0.613	0.409
Ridge	0.947	0.878	0.115	0.234	<0.001	<0.001
Lasso	0.945	0.882	0.115	0.296	<0.001	<0.001
MLP	**1.0**	**1.0**	**0.769**	0.875	0.387	0.455
SVM	**1.0**	0.972	0.743	0.875	0.355	0.455
XGBoost	**1.0**	**1.0**	0.735	**0.917**	0.533	0.441
LightGBM	**1.0**	**1.0**	0.752	**0.917**	0.419	0.455
CatBoost	**1.0**	**1.0**	0.744	**0.917**	**0.645**	**0.545**

Table 4. This table presents the combined runtimes of our experiments conducted on well-known and publicly available classification datasets. The runtimes include both the 5-fold Randomized Search cross-validation process from Scikit-learn, which was employed to identify the optimal model, and the evaluation of the best model on an unseen test subset of the original data. We include results for the six datasets described in Section 3.5, the quantum classifiers detailed in Section 3.2, and the classical machine learning classifiers discussed in Section 3.1.

Classifier\ Dataset	Iris	Wine	ILPD	BC-Coimbra	TAE	Breast-Tissue
VQC	3:32:16.547605	1 day, 13:56:59.455185	2 days, 23:03:26.398856	9:55:17.907443	2:46:25.921553	9:01:58.623806
QKE	2:03:57.921154	21:41:38.738255	7 days, 6:30:41.179676	5:02:26.430001	1:28:54.069725	3:37:05.655104
Ridge	0:00:00.175009	0:00:00.496771	0:00:00.399229	0:00:00.240857	0:00:00.209600	0:00:00.296966
Lasso	0:00:00.173051	0:00:00.181444	0:00:00.237455	0:00:00.192257	0:00:00.229508	0:00:00.225531
MLP	0:00:16.876288	0:00:10.477420	0:00:26.748907	0:00:10.951229	0:00:08.475263	0:00:13.729790
SVM	0:00:00.143353	0:00:00.165431	0:00:00.484485	0:00:00.180694	0:00:00.228508	0:00:00.226784
XGBoost	0:00:03.809085	0:00:04.030425	0:00:04.752627	0:00:02.744122	0:00:05.820371	0:00:06.864497
LightGBM	0:00:02.971164	0:00:03.180770	0:00:03.062553	0:00:01.462174	0:00:03.056615	0:00:04.540870
CatBoost	0:00:06.465975	0:00:18.511612	0:00:11.352944	0:00:07.460460	0:00:06.964821	0:00:26.639070

5.3. Comparison and Discussion

In this study, we have compared the performance of quantum machine learning (QML) and classical machine learning (ML) algorithms on six benchmark datasets and artificially generated classification datasets. We included results for quantum classifiers, such as Variational Quantum Circuit (VQC) and Quantum Kernel Estimator (QKE), and classical machine learning classifiers like CatBoost, XGBoost, and LightGBM, among others. Our experiments showed that while QML algorithms demonstrate potential in achieving competitive performance on certain datasets, they do not consistently outperform classical ML algorithms. Additionally, their longer runtimes and less consistent performance across the benchmark data sets may limit their practical applicability compared to classical ML algorithms, which continue to offer superior and more consistent performance with faster execution times.

It is essential to highlight that the QML algorithms' performance in our experiments was based on simulated quantum infrastructures. This is a significant limitation to consider, as the specific constraints and characteristics of the simulated hardware may influence the performance of these algorithms. Further, given the rapid advancement of quantum technologies and hardware, this constraint might be obsolete in the near future.

One possible direction for future research is exploring quantum ensemble classifiers and, consequently, quantum boosting classifiers, as suggested by Schuld et al. [39]. This approach might help in improving the capabilities of QML algorithms and make them more competitive with state-of-the-art classical ML algorithms in terms of high accuracies.

Finally, the relatively lower performance of the employed quantum machine learning algorithms compared to, for example, the employed boosting classifiers might be attributed to Quantum Machine Learning being constrained by specific rules of quantum mechanics.

In the authors' opinion, Quantum Machine Learning (QML) might be constrained by the unitary transformations inherent in, for example, the variational quantum circuits. These transformations are part of the unitary group $U(n)$. Thus all transformations are constrained by symmetry properties. Classical machine learning models are not constrained by these limitations, meaning that, for instance, different activation functions in neural networks do not preserve certain distance metrics or probabilities when processing data. However, expanding the set of transformations of quantum machine learning and getting rid of possible constraints might improve the capabilities of quantum

machine learning models such that these algorithms might be better capable of capturing the information of more complex data. However, this needs to be discussed in the context of quantum computers such that one determines what all possible transformations on a quantum computer are. This means that future research needs to consider the applicability of advanced mathematical frameworks for quantum machine learning regarding the formal requirements of quantum computers.

Further, another constraint of quantum machine learning is that it, and quantum mechanics in general, relies on Hermitian matrices, e.g., to provide real-valued eigenvalues of observables. However, breaking this constraint might be another way to broaden the capabilities of quantum machine learning to better capture complexity, e.g., by using non-Hermitian kernels in a quantum kernel estimator. Here, we want to mention the book by Moiseyev [40], which introduces non-Hermitian quantum mechanics. Further, quantum computers, in general, might provide a testing ground for non-Hermitian quantum mechanics in comparison to Hermitian quantum mechanics. However, at this point, all of this is rather speculative, but given that natural data is nearly always corrupted by noise and symmetries are never truly perfect in nature, breaking constraints and symmetries might be ideas to expand the capabilities of QML.

6. Conclusion

In this research, we have explored the applicability of quantum machine learning (QML) for classification tasks by examining the performance of Variational Quantum Circuit (VQC) and Quantum Kernel Estimator (QKE) algorithms. Our comparison of these quantum classifiers with classical machine learning (ML) algorithms, such as XGBoost, Ridge, Lasso, LightGBM, CatBoost, and MLP, on six benchmark datasets and artificially generated classification datasets demonstrated that QML algorithms can achieve competitive performance on certain datasets. However, they do not consistently outperform their classical ML counterparts, particularly with regard to runtime performance and accuracy. Quite the contrary, classical machine learning algorithms still demonstrate superior performance, especially in terms of increased accuracy, in most of our experiments.

As our study's performance comparison relied on simulated quantum circuits, it is important to consider the limitations and characteristics of simulated hardware, which may affect the true potential of quantum machine learning. Given the rapid advancement of quantum technologies and hardware, these constraints may become less relevant in the future. Future research should also consider exploring quantum ensemble classifiers and quantum boosting classifiers, as well as addressing the limitations imposed by the specific rules of quantum mechanics. By breaking constraints and symmetries and expanding the set of transformations in quantum machine learning, researchers may be able to unlock its full potential.

Despite the current limitations, this study has shed light on the potential and challenges of quantum machine learning compared to classical approaches. Thus, by providing our complete code in a GitHub repository, we hope to foster transparency, encourage further research in this field, and offer a foundation for other researchers to build upon as they explore the world of quantum machine learning.

Acknowledgments

Appendices

A. Parametrization

This Appendix lists the parameter grids for all employed algorithms per the implementations from scikit-learn and qiskit, [15,23]. Thus for further explanations on the parameters and how they influence the discussed algorithm, the reader is referred to the respective sources, which we linked in Sections 3.1 and 3.2.

A.1. Ridge

```
param_grid = {
    'alpha': [0.001, 0.01, 0.1, 1, 10, 100],
    'fit_intercept': [True, False],
    'normalize': [True, False],
    'copy_X': [True, False],
    'max_iter': [100, 500, 1000],
    'tol': [1e-4, 1e-3, 1e-2],
    'solver': ['auto', 'svd', 'cholesky', 'lsqr', 'sparse_cg', 'sag', 'saga'],
    'random_state': [42]
}
```

A.2. Lasso

```
param_grid = {
    'alpha': [0.001, 0.01, 0.1, 1, 10, 100],
    'fit_intercept': [True, False],
    'normalize': [True, False],
    'precompute': [True, False],
    'copy_X': [True, False],
    'max_iter': [100, 500, 1000],
    'tol': [1e-4, 1e-3, 1e-2],
    'warm_start': [True, False],
    'positive': [True, False],
    'random_state': [42],
    'selection': ['cyclic', 'random']
}
```

A.3. SVM

```
param_grid = {
    'C': [0.1, 1, 10, 100],
    'kernel': ['linear', 'poly', 'rbf', 'sigmoid'],
    'degree': [2, 3, 4],
    'gamma': ['scale', 'auto'],
    'coef0': [0.0, 1.0, 2.0],
    'shrinking': [True, False],
    'probability': [False],
    'tol': [1e-4, 1e-3, 1e-2],
    'cache_size': [200],
    'class_weight': [None, 'balanced'],
    'verbose': [False],
```

```
    'max_iter': [200, 300, 400],
    'decision_function_shape': ['ovr', 'ovo'],
    'break_ties': [False],
    'random_state': [42]
}
```

A.4. MLP

```
param_grid = {
    'hidden_layer_sizes': [(50,), (100,), (150,)],
    'activation': ['relu', 'tanh'],
    'solver': ['adam', 'sgd'],
    'alpha': [0.0001, 0.001, 0.01],
    'learning_rate': ['constant', 'invscaling', 'adaptive'],
    'max_iter': [200, 300, 400]
}
```

A.5. XGBoost

```
param_grid = {
    'max_depth': [3, 5, 7, 10],
    'learning_rate': [0.01, 0.05, 0.1, 0.2],
    'n_estimators': [50, 100, 150, 200],
    'subsample': [0.5, 0.8, 1],
    'colsample_bytree': [0.5, 0.8, 1]
}
```

A.6. LightGBM

```
param_grid = {
    'max_depth': [3, 5, 7, 10],
    'learning_rate': [0.01, 0.05, 0.1, 0.2],
    'n_estimators': [50, 100, 150, 200],
    'subsample': [0.5, 0.8, 1],
    'colsample_bytree': [0.5, 0.8, 1]
}
```

A.7. CatBoost

```
param_grid = {
    'iterations': [50, 100, 150, 200],
    'learning_rate': [0.01, 0.05, 0.1, 0.2],
    'depth': [3, 5, 7, 10],
    'l2_leaf_reg': [1, 3, 5, 7, 9],
}
```

A.8. QKE

For this Algorithm we precomputed the Kernel-Metrix using qiskit and then performed the support vector classification via the vanilla SVM-algorithm from scikit-learn.

```
param_grid = {
    'feature_map': [PauliFeatureMap, ZFeatureMap, ZZFeatureMap],
    'quantum_instance': [
        QuantumInstance(Aer.get_backend('aer_simulator'), shots=1024),
```

```
        QuantumInstance(Aer.get_backend('qasm_simulator'), shots=1024),
        QuantumInstance(Aer.get_backend('statevector_simulator'), shots=1024)
    ],
    'C' : np.logspace(-3, 3, 9),
}
```

A.9. VQC

```
param_grid = {
    'feature_map': [PauliFeatureMap, ZFeatureMap, ZZFeatureMap],
    'ansatz': [EfficientSU2, TwoLocal, RealAmplitudes],
    'optimizer': [
        COBYLA(maxiter=max_iter),
        SPSA(maxiter=max_iter),
        NFT(maxiter=max_iter),
    ],
    'quantum_instance': [
        QuantumInstance(Aer.get_backend('aer_simulator'), shots=1024),
        QuantumInstance(Aer.get_backend('qasm_simulator'), shots=1024),
        QuantumInstance(Aer.get_backend('statevector_simulator'), shots=1024)
    ],
}
```

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