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Article

# Analysis of Electric Field Distribution on Primary Windings of High-Voltage High-Frequency Transformers with Variables Characteristics

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**Abstract:** This paper present analysis of electric field distribution on windings of primary side of high frequency, and voltage transformers with variables characteristics. To study the effect of high transformer voltage, induce and high frequency for finding suitable dimension. The objective is analysis of electricity field distribution at the low voltage at the angle 0, 30, 45, 60, and 90 degrees, Comparing voltage flow out of the putting primary coil. Comparing external frequency of primary coil putting. Comparing result of distribution electricity field model between primary coil (Lp) and secondary coil. By consideration from induce that proper for Tesla transformer reproduce by using FEMLAB program. Comparing the Tesla transformer reproduce which is created the frequency 120 kHz and voltage at 120 kV. Analysis use FEMLAB program. The result isn't flash over between the low and high voltage winding.

Keywords: tesla transformer; primary winding; secondary winding; FEMLAB program

# 1. Introduction

At the present electric distribution system in bus far from ele. In the manufacture to produce Porcelain Insulator, it would use high voltage transformer to distribute the voltage for testing every insulator that produce from the manufacturer to check the primary quality that the insulators are not imperfect in the Porcelain insulator. By using flash over the surface of insulators which is follow the standard ANSI C.29.1976 that using the high frequency in testing the defect inside. It would be effect to the high electricity field stress that occur between secondary, and primary coil because this type of transformer is the air axis transformer. It would be a problem in the insulator coil that has the electric air by creating the flash over on the 2 sets of coils. The suitable distance of coil would be reducing that problem. To reduce the problem, it should not make the voltage out of high frequency, and voltage transformers which has set a determine amount. So that, this research would be study the effect of high frequency, and voltage transformers induce (Transformer of Tesla). To find suitable dimension by analyst the result that occurs in this research. It would use the model circuit of tesla transformer by using FEMLAB program. Compare with the testing results that receive from buildup transformer of Tesla [1].

Coil of Tesla was invented by Tesla. The resonance between side of secondary coils on the transformer is the operating principle of the Tesla coil [2]-[3]. Transformer of Tesla is device that provide electrical high potential.

Voltage is generated from damped oscillations at a frequency of 50 to 400 kilohertz. The Tesla transformer was created to effectively test the electrical conditions of suspensions and post-type insulators [4]-[5]. The high-voltage pulses generated will have an amplitude of several megavolts and can discharge electricity over several meters [6]-[7].

In 2008, the electric field and components were optimally designed using the FEMLAB software. The IEC standard was used to determine the PD value in the design of the cable terminator and to design the cable connector with SF6 insulation. The electrical stress was analysed [8]. In 2010, a cost-

Therefore, this paper analysed of electric field distribution on primary windings of high voltage high frequency transformers with variables characteristics.

The objective of this paper as follow:

- The analysis of electricity field distribution at the low voltage at the angle 0, 30, 45, 60, and 90 degree.
  - Comparing voltage flow out of the putting primary coil.
  - Comparing external frequency of primary coil putting.
- Comparing result of distribution electricity field model between primary coil (Lp) and secondary coil.

**Table 1.** The tube size and the high that suitable for binding high voltage coil.

	Prin	nary	Seconda	nry
$L_1$	L <sub>1</sub>	C <sub>1</sub>	L <sub>2</sub>	C <sub>2</sub>
	(μΗ)	(μF)	(mH)	(PF)
90°	28.45			
60°				
$45^{0}$	72.09	6.366	43.97	40
30°				
0°	64.70			

# 2. Equipment and Research Model

Equipment that using in the research as follow:

- 1. MATLAB Program—using the tesla transformer model to be a design before building up the real one.
  - 2. FEMLAB Program using to be a model of distribution the electricity field in tesla transformer.
  - 3. PVC tube that has diameter 4 inch using to be axis for Ls secondary coil binding.
  - 4. Enamel Copper Coil size 31 SWG using to be a LS secondary coil binding.
- 5. Copper tube 0.03 inch that diameter 0.25 inch and 0.5 inch. using to be a Lp primary coil and Transformer Protection Ring.
  - 6. Motor 1 phase speed at 1450 round per second using for drive the Rotary Spark cap.
  - 7. Low Voltage Capacitor polypropylene size 15 nF 1,600 V
- 8. Neon Sign Transformer 230 V/15,000V using for transformer power distributor of low voltage tesla transformer.

### 3. Method

- 1. High voltage circuit model, high frequency voltage at  $120\,\mathrm{kV}$ , high voltage at  $120\,\mathrm{kHz}$  by using MATLAB and FEMLAB Program.
  - 2. Create the model of components and several structure of high voltage high frequency.
  - 3. Build up the components and several structure of high voltage high frequency.
- 4. Testing to find the best feature in working of high voltage high frequency and correct the defect part.
- 5. Collect the result from the calculation and the result from the model that using FEMLAB Program and the result of high voltage high frequency that built up to compare.
  - 6. Conclusion of research and testing Tesla transformer circuits.

Transformer of Tesla circuit is shown in Figure 1.

Figure 1. Transformer of Tesla circuit.

From Figure 1.

C<sub>1</sub> is main capacitor.

L<sub>1</sub> is main inductor.

C2 is secondary capacitor.

L<sub>2</sub> is secondary inductor.

Q is spark gap.

High voltage is 120 kVrms. Frequency is 120 kHz. Voltage impulse is 0-15 kVrms. Capacity  $C_2$  value around 40 pF. Equation that uses for calculating parameter [10]-[12].

- In case that oscillation has occur between  $L_1$  and  $C_1$  the frequency that would occur can calculate in equation 1.

$$f = \frac{1}{2\pi\sqrt{L_1C_1}} \tag{1}$$

- Condition that occur from oscillation low voltage induce and high voltage tune [13] can calculate in equation 2.

$$f_1 = f_2 = \frac{1}{2\pi\sqrt{L_1 C_1}} = \frac{1}{2\pi\sqrt{L_2 C_2}}$$
 (2)

Where  $f_1$  is primary resonant frequency (Hz).

 $L_1$  is primary inductance (H).

 $C_1$  is primary capacitance (F).

Diameter (inch)	High/diameter	Length of coil binding (inch)
3	6.0:1	18.0
4	5.0:1	20.0
5	4.5:1	22.5
6	4.0:1	24.0
7	3.5:1	24.5
8	3.0:1	24.0
More 8	3.0:1	24.0

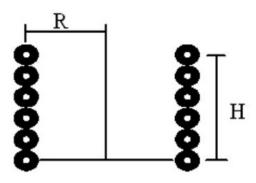


Figure 2. The dimension in binding high voltage coil [14].

Where L is induce (mH).

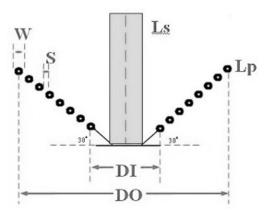
R is diameter radius to the center of coil (Inch).

N is binding amount.

H is high of binding (Inch).

Low voltage coil model

1. Angle with the floor at  $30^{\circ}$ ,  $45^{\circ}$ ,  $60^{\circ}$ , using copper tube size 5/16 inch, thick 0.03 inch for low voltage coil.



**Figure 3.** The primary coil at the angle 30°, 45°, 60° [15].

$$L = \frac{(NA)^2}{30A - DI} \tag{3}$$

$$A = \frac{DI + N(W + S)}{2} \tag{4}$$

# From Fig. 3.

Where W is diameter of copper tube = 5/16 inch.

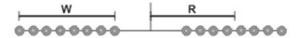
S is binding distance = 1/2 inch.

DI is inside diameter of Lp = 14 inch.

DO is outside diameter of Lp = 34 inch.

N is Lp binding = 10 round.

Angle to the floor at 0° using copper tube size 5/16 inch, thick 0.03 in to be low voltage [16].



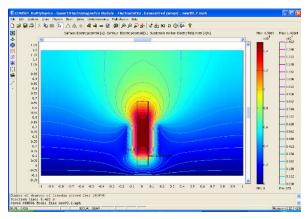
**Figure 4.** The primary coil at the angle 0°.

$$L = \frac{(NR)^2}{8R + 11W} \tag{5}$$

### 4. Results

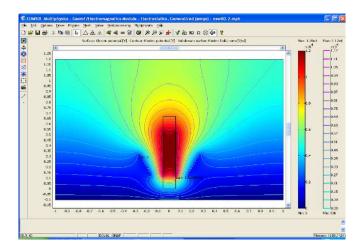
The model of electricity field distribution of high voltage high frequency transformer that follow to finite element process by using FEMLAB program. It is determined that voltage in the low coil should have electricity voltage at 15 kV. The high voltage coil has permittivity tube of PVC size 3.5, and 120 kV of voltage [14]-[15].

The comparison of electricity field model, and angle of low voltage five degrees viz ninety, sixty, forty-five, thirty, and zero degrees. The result of model of electricity field distribution at the low voltage are shown in Figure 5-10.



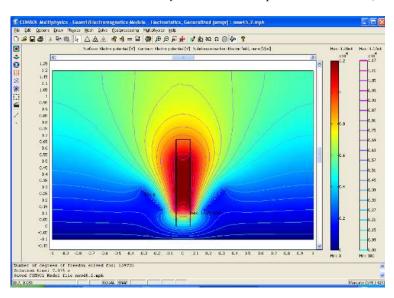
**Figure 5.** The model of electricity filed at the low voltage coil in the angle 90 degree from the floor which would have the amount of electricity field maximum equal to 20.99 kV/cm at the beginning of high voltage coil (1st dimension).

Figure 5. shows the amount of electricity field maximum equal to 20.99 kV/cm (1st dimension).



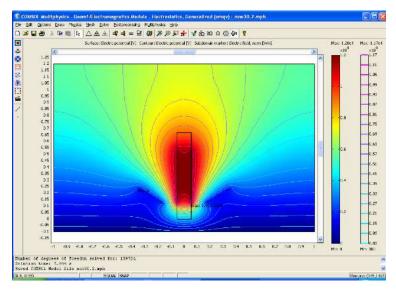
**Figure 6.** The result of model of electricity field distribution at the low voltage at the angle 60 degree from the floor. It would have electricity field maximum equal to  $15.20 \, kV/cm$  at the beginning of high voltage coil ( $2^{nd}$  dimension).

Figure 6. shows the amount of electricity field maximum equal to 15.20 kV/cm (2<sup>nd</sup> dimension).



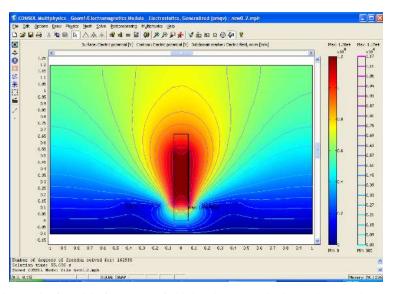
**Figure 7.** The result of model of electricity field distribution at the low voltage at the angle 45 degree from the floor. It would have electricity field maximum equal to 13.95 kV/cm at the beginning of high voltage coil (3<sup>rd</sup> dimension).

Figure 7. shows the amount of electricity field maximum equal to 13.95 kV/cm (3<sup>rd</sup> dimension).



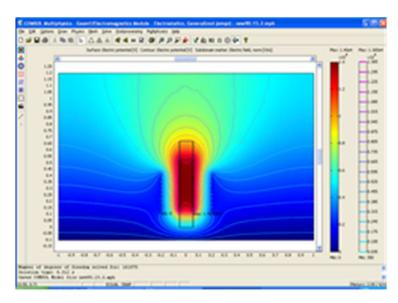
**Figure 8.** The result of model of electricity field distribution at the low voltage at the angle 30 degree from the floor. It would have electricity field maximum equal to 14.91 kV/cm at the beginning of high voltage (4th dimension).

Figure 8. shows the amount of electricity field maximum equal to 14.91 kV/cm (4th dimension).



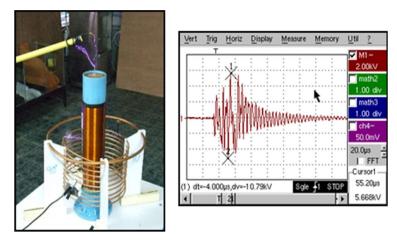
**Figure 9.** The result of model of electricity field distribution at the low voltage at the angle 0 degree from the floor. It would have electricity field maximum equal to 14.99 kV/cm high voltage of beginning (5<sup>th</sup> dimension).

Figure 9. shows amount field of electricity maximum equal to 14.99 kV/cm (5th dimension).

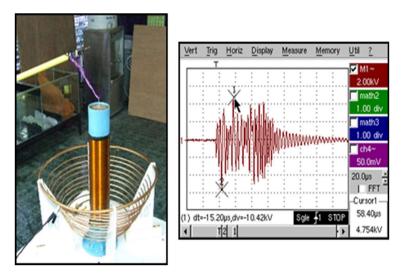


**Figure 10.** The result of model of electricity field distribution at the low voltage at the angle 90 degree from the floor. It would expand the distance between the Lp and Ls coil from the previous 4 inch to be 5.5 inch., which would have the electricity field amount maximum equal to 18.23 kV/cm. high voltage of beginning (6<sup>th</sup> dimension).

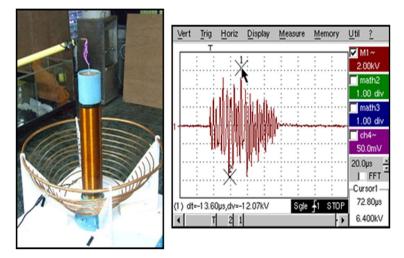
The testing result which have put the Lp coil at the angle 90, 60, 45, 30, 0 degree. Oscillation that retains it should be calculated in each type The tesla transformer testing result which have put the Lp coil at the angle 90, 60, 45, 30, 0 degree. Oscillation that retains it should be calculated in each type.



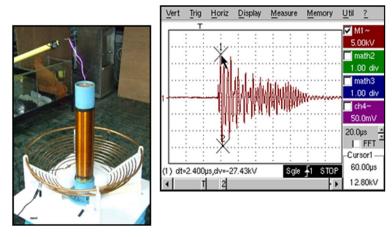
**Figure 11.** Testing in putting Lp coil at the angle 90 degree and Wave that could calculate of Lp at the angle 90 degree.



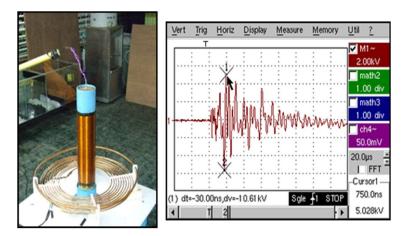
**Figure 12.** Testing in putting Lp coil at the angle 60 degree and Wave that could calculate of Lp at the angle 60 degree.



**Figure 13.** Testing in putting Lp coil at the angle 45 degree and Wave that could calculate of Lp at the angle 45 degree.



**Figure 14.** Testing in putting Lp coil at the angle 30 degree and Wave that could calculate of Lp at the angle 30 degree.

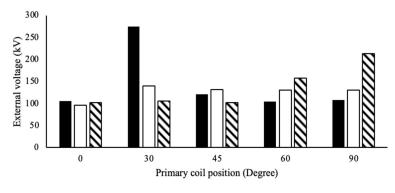


**Figure 15.** Testing in putting Lp coil at the angle 0 degree and Wave that could calculate of Lp at the angle 0 degree.

**Table 3.** The results of voltage flow out of the putting primary coil at the adjust position from the round 8 in each type.

n ' C '1	External Voltage (kV)			
Primary Coil	1 <sup>th</sup>	2 <sup>nd</sup>	$3^{\mathrm{rd}}$	D1
Position (Lp)	Without Toroid	Without Toroid	With Toroid	Remarks
00	106.1	96	102.4	
30°	274.3	139.9	105.1	
45°	120.7	131.7	102.4	
60°	104.2	129.8	157.7	
90°	107.9	120.0	212.6	$1^{st}$ and $3^{rd}$
90°		129.8		Breakdown

Comparing of voltage flow out of putting primary coil is shown in Figure 16.

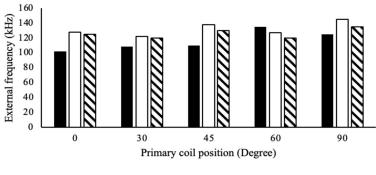


- ■External Voltage (kV) 1th Without Toroid □External Voltage (kV) 2nd Without Toroid
- ■External Voltage (kV) 3rd With Toroid

Figure 16. Comparing of voltage flow out of putting primary coil.

**Table 4.** The results of external frenquency of primary coil putting at the adjust position at 8 round binding in each type.

Duimaur Cail -	j	External Frequency (kHz)	
Primary Coil Position (Lp)	<b>1</b> th	2 <sup>nd</sup>	$3^{\mathrm{rd}}$
	Without Toroid	Without Toroid	With Toroid
00	102	128	125
30°	108	122	120
45°	110	138	130
60°	135	127	120
90°	125	145	135

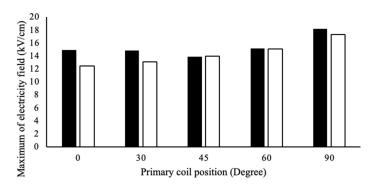


- External Frequency (kHz) 1 th Without Toroid
- □External Frequency (kHz) 2nd Without Toroid
- ■External Frequency (kHz) 3rd With Toroid

Figure 17. Comparing of external frequency of primary putting.

**Table 5.** The results of distribution electricity field model between primary and secondary coil in several angle by using FEMLAB and calculation.

Drimerry Cail Desition	Maximum of Electricity Field (kV/cm)		
Primary Coil Position -	Model Testing by using	Calculating Result by using the	
(Lp)	FEMLAB Program	formula	
00	14.99	12.48	
30°	14.91	13.16	
45°	13.95	14.00	
60°	15.20	15.15	
90°	18.23	17.32	



■ Maximum of Electricity Field (kV/cm) Model Testing by using FEMLAB Program

□ Maximum of Electricity Field (kV/cm) Calculating Result by using the formula

Figure 18. Comparing of distribution electricity field model between primary coil (Lp) and secondary coil.

According to the result of tesla transformer testing and the electricity field model that design in the putting of low and high voltage coil of tesla transformer 3 times. It would consider choosing by using the distribution impulse by indicate it in the adjustment atmosphere. Primary coil at the same point which is binding 8 rounds of primary coil at the difference angle and from the table 3 and table 4. It would see that at this point the distribution voltage, would almost the same amount with the model at 120 kV 120 kHz and it is the amount of rounding of primary coil Lp that close to the high amount from the model. According to the comparing, it can conclude that to put the primary coil (Lp) from the floor at the angle. It is the internal voltage and high electricity field stress that has the most suitable than another model.

### 5. Conclusion

This paper present analysis of electric field distribution on primary side of windings of high frequency and voltage transformers with variables characteristics. To study the effect high voltage side of transformer, induce and high frequency for finding suitable dimension. It would start in determining the transformer is external impulse and frequency. The characters of coil induce (the suitable dimension in putting the low voltage coil Lp in the several positions and the model amount that using FEMLAB. The amounts that receive from simulation, would use for comparing analyst with the result of test that get from high voltage transformer and high frequency which was created.) The analysis in the several parameters, it could be link that to put the Lp coil in the suitable angle, it should be at 60 angle according this research.

**Author Contributions:** Conceptualization, S.N. and N.R.; Methodology, S.N. and N.R.; Validation, N.R.; Investigation, S.N. and N.R.; Writing—original draft, S.N.; Writing—review & editing, N.R. and S.N. All authors have read and agreed to the published version of the manuscript.

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