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[Sabitova Alfira](#) , [Mukhamediyarov Nurlan](#) , [Mussabayeva Binur](#) <sup>\*</sup> , [Rakhadilov Bauyrzhan](#) , [Aitkazin Nurbol](#) , [Bayakhmetova Bulbul](#) , [Sharipkhan Zhanna](#) , [Gaisina Balzhan](#)

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## Article

# The Effect of the Granulometric Composition of Slags on the Efficiency of Non-Ferrous Metals' Extraction

Sabitova Alfira <sup>1</sup>, Mukhamediyarov Nurlan <sup>1</sup>, Mussabayeva Binur <sup>2,\*</sup>, Rakhadilov Bauyrzhan <sup>3</sup>, Aitkazin Nurbol <sup>1</sup>, Bayakhmetova Bulbul <sup>1</sup>, Sharipkhan Zhanna <sup>1</sup> and Gaisina Balzhan <sup>1</sup>

<sup>1</sup> Shakarim University, Semey, 071400, Kazakhstan

<sup>2</sup> Astana International University, Astana, 010017, Kazakhstan

<sup>3</sup> PlasmaScience LLP, Ust-Kamenogorsk, 070018, Kazakhstan

\* Correspondence: mussabayevabinur@gmail.com

**Abstract:** The processing of metallurgical slags is an urgent task, as they contain residual amounts of precious and non-ferrous metals such as gold, silver and copper. The efficiency of extraction of these metals directly depends on the granulometric composition of the processed material, which determines the need for its detailed analysis. The purpose of this study is to study the effect of the granulometric composition of slags on the efficiency of extraction of precious metals using various enrichment methods. For this purpose, studies were carried out, including granulometric analysis, chemical composition analysis, flotation tests using Na<sub>2</sub>S and 3418A reagents, as well as magnetic separation. The analysis showed that the main part of the slag consists of particles less than 3.36 mm, while the content of copper is 0.60%, zinc – 2.37%, gold – 0.1 g/t, and silver – 7.2 g/t. Flotation experiments have confirmed that the use of Na<sub>2</sub>S and 3418A increases the recoverability of copper and silver, and reducing the particle size to d<sub>80</sub> <10 microns increases the efficiency of copper extraction by 7%. Magnetic separation did not have a significant effect on the concentration of non-ferrous metals, but it allowed us to isolate an iron-containing fraction suitable for further processing. Thus, optimization of flotation processes and control of granulometric composition make it possible to increase the efficiency of metallurgical waste processing, reduce losses of valuable metals and reduce the environmental burden.

**Keywords:** granulometric composition; flotation; metallurgical slag; precious metals; non-ferrous metals

## 1. Introduction

In modern conditions of mining and processing of ore materials, special attention is paid to the integrated use of raw materials and the maximum extraction of valuable components. One of the promising areas is the processing of metallurgical slags, which are man-made mineral resources containing residual amounts of non-ferrous and precious metals. Their effective extraction contributes not only to increasing the profitability of production, but also to reducing the anthropogenic impact on the environment [1–6].

The granulometric composition of the processed material plays a key role in the efficiency of precious metal extraction processes. The particle size determines the surface area available for interaction with reagents, and also affects the processes of flotation, leaching, and gravity enrichment. Studies show that different fractions of the material can exhibit different degrees of metal recoverability, which makes granulometric analysis an important stage in the development and optimization of slag processing technologies [7–13].

The relevance of the study is due to the need to increase the efficiency of metallurgical waste processing and to search for new methods of their enrichment. Various approaches to slag processing

are used in world practice, including X-ray fluorescence sorting, magnetic separation and hydrometallurgical methods. For example, studies have shown that X-ray fluorescence sorting makes it possible to effectively isolate non-ferrous metals from industrial waste, depending on the properties of the particle surface [14–17]. In addition, it was found that the characteristics of the granulometric composition have a significant effect on the processes of metal reduction in the peripheral zone of the blast furnace [18,19].

The present work is devoted to the study of the granulometric composition of slag samples and its effect on the efficiency of extraction of precious metals. In the course of the study, laboratory experiments were conducted to determine the granulometric composition of slags, analyze the effect of particle sizes on metal extraction processes, as well as a comparative analysis of various technological approaches to waste processing. The results obtained will make it possible to develop recommendations for optimizing the processing of metallurgical waste, increase the recoverability of valuable metals and minimize losses during their processing.

2. Materials and Methods

The study included sampling of slag from the slag dump of the former Shymkent lead plant (Figure 1), grinding using a mill and then conducting a granulometric analysis using a sieve method, chemical analysis to determine the content, as well as flotation experiments [20,21].



Figure 1. Slag dump of lead production.

A 178×356 mm “Unal” rod mill operating at 45 rpm was used for the study. The sample, pre-ground to a size of 1 mm, weighing about 1000 g, was processed at a ratio of solid: liquid = 1:1 for different times given below. The particle size distribution was recorded after each stage of using wet sieving. The results are shown in Table 1.

Table 1. Values of grinding time and size distribution.

Grinding time, min	Cumulative (%), sifted							
	150	106	75 microns	63 microns	53 microns	45 microns	38 microns	20
	microns	microns						microns
17	88,49	63,67	43,69	35,57	30,68	26,76	22,85	18,15
25	98,04	89,68	65,67	56,68	45,67	39,91	33,66	26,68
35	99,76	97,86	88,87	78,15	66,48	58,50	49,15	37,49
45	100,00	99,74	97,18	92,28	84,69	77,59	67,80	54,56
60	100,00	100,00	99,27	97,28	94,97	90,53	81,52	60,33

3. Experimental Part

Flotation experiments with Na<sub>2</sub>S-3418A

In this series of experiments, sulfurization with various amounts of Na<sub>2</sub>S was performed before using coarse and control flotation, and then 3418A was used as a collector. Flotation tests were carried out between pH values from 9.50 and above, which constitute the natural level of the alkaline slag environment. Other variables were maintained on an ongoing basis to see the effect of pH changes, the experiment was conducted in a control flotation by lowering the pH level to 7.60.

The process of purification of coarse concentrate in the experiments was carried out in a maximum of 6 stages. With different size distributions, as shown in Figure 2. Since the number of cleaning steps has different numbers, after cleaning they are expressed as "Residue after cleaning".

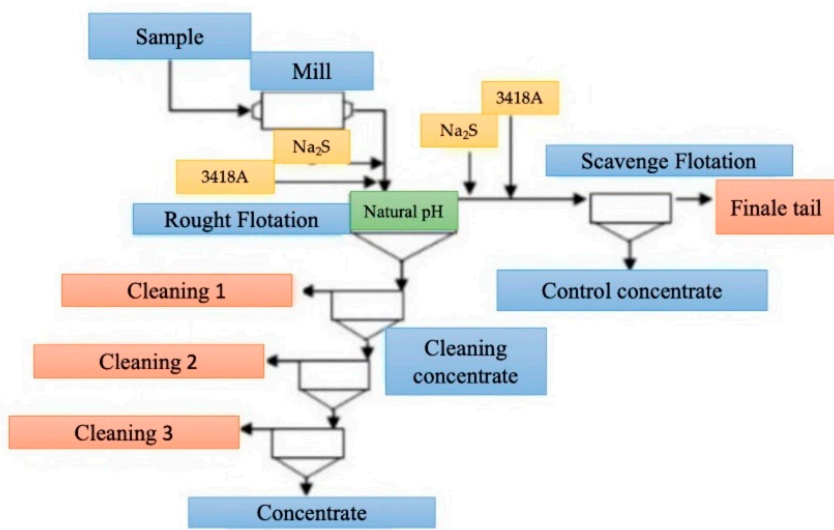


Figure 2. General flowchart of experiments with Na<sub>2</sub>S-3418A.

Flotation experiments with KAX-Na<sub>2</sub>S-3418A

Unlike the previous experiment, KAX was used as a collector instead of 3418 A, and AX was added directly to the mill. Na<sub>2</sub>S was added before the control flotation, the condition was created within 5 minutes, and 3418A was used as a collector. The experiments were carried out in various size distributions, according to the general flow chart of the experiments, as shown in Figure 3.

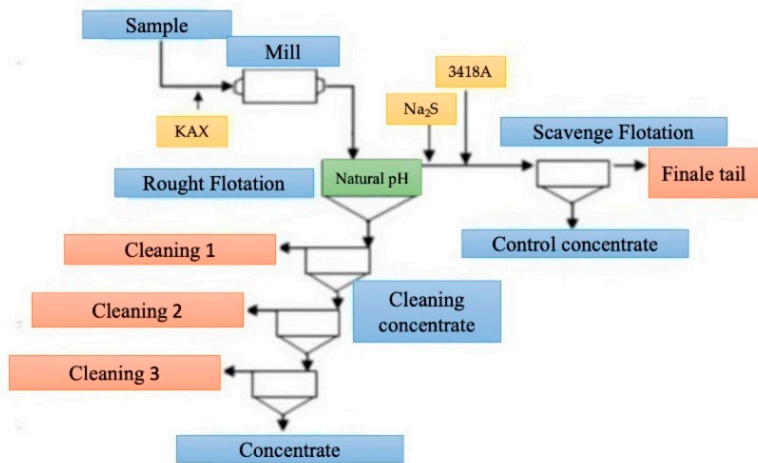
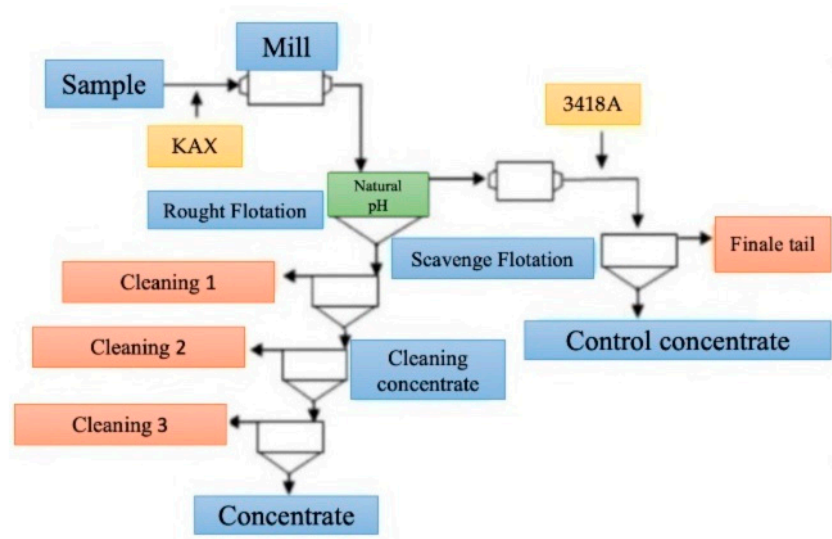


Figure 3. General flow chart of experiments with KAX-Na<sub>2</sub>S-3418A.



Flotation experiments with the sample after grinding of coarse residues

Unlike previous experiments, Na<sub>2</sub>S was not used in this series. The general flow chart of the experiments is shown in Figure 4.



**Figure 4.** General flowchart of experiments with control flotation after crushing coarse residues.

## 4. Results and Discussion

### 4.1. Time of Grinding and Size Distribution of Coarse Sludge Residues

Table 1 shows the results that show the dependence of the cumulative particle size distribution on the grinding time, where the proportion of sifted particles corresponds to different time intervals.

Table 1 shows an accelerated decrease in the proportion of large particles and a gradual increase in the content of small fractions over the grinding time. The most intensive grinding takes place between 17 and 25 minutes, after which the process slows down significantly. For large particles (for example, 150 microns), the cumulative yield reaches 100% by 35 minutes of grinding. At the same time, for smaller particles (for example, 20 microns), the cumulative increase is noticeable even after 45 minutes, which indicates the continued crushing of the material.

The results show the efficiency of rod mills for grinding slag: after 35 minutes, most of the material reaches a size of less than 75 microns. When grinding for up to 60 minutes, almost all the material passes through a sieve with a mesh size of 20 microns, which significantly affects the processing steps such as flotation or hydrometallurgy. The data obtained on the particle distribution and the grinding time of coarse sludge residues are in good agreement with the literature data. For example, Liu et al. (2019) showed that increasing the grinding time of dry-granulated blast furnace slag from 10 to 20 minutes makes it possible to achieve an optimal average particle size (D<sub>50</sub> ~16.6 microns), which has a positive effect on cement strength. With a further increase in time to 30-50 minutes, particle agglomeration and deterioration of properties were observed [19]. Li et al. (2024) also noted that when grinding steel slag, the optimal time is about 20 minutes — during this period, the maximum specific surface area is reached, and excess time leads to clumping of particles [21].

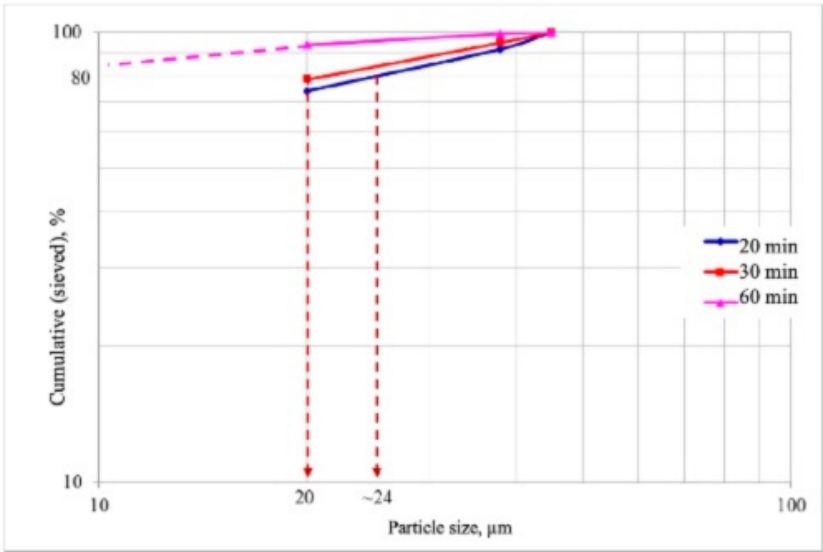
As part of the control flotation, to study the effect of the particle size (38 microns), the coarse flotation residues were subjected to repeated grinding. Experiments on control flotation were carried out with particle sizes in the following fractions: 24 microns, 20 microns and <10 microns (Table 2).

**Table 2.** Results of particle size distribution analysis during the grinding of coarse residues.

Particle size range (microns)	Weight, in %			Cumulative (%), sifted		
	20 min	30 min	60 min	20 min (24 microns )	30 min (20 microns)	60 min (<10 microns)
-45+38	8,37	5,28	0,81		100,00	100,00
-38+20	17,60	16,15	5,46	91,63	94,72	99,19
-20	74,03	78,57	93,72	74,03	78,57	93,72
The input sample	100,00	100,00	100,00	-	-	-

The table shows the results of particle size distribution after grinding coarse residues in various time intervals. When analyzing the particle distribution after grinding coarse particles, the following changes are observed. For synchronization of 38 microns, the weight fraction drops from 8.37% (30 minutes) to 5.28% (60 minutes), while the cumulative value remains at 100% for the lower time intervals, which indicates the complete removal of large particles. At the same time, the mass fraction of particles with particle sizes of 20 microns varies slightly: it decreases from 17.6 at 30 minutes to 16.15% at 60 minutes, however, a cumulative increase in the proportion from 91.6 to 94.72% indicates a gradual decrease in large particles. The most noticeable increase occurs within 20 microns, where the weight fraction of fine particles increases from 74.0 (30 minutes) to 78.57% (60 minutes), and the cumulative value for this group reaches 93.72%. These results indicate the effectiveness of long-term grinding to prepare the material for further processing.

Figure 5 shows that with particle sizes of about 20 microns, the cumulative distribution increases over the grinding time, reaching about 80% after 20 minutes, slightly more than 85% after 30 minutes, and about 93% after 60 minutes. For smaller particles (<20 microns), the largest increase in cumulative mass is observed during the transition from 30 to 60 minutes of grinding. At the same time, for large particles (>24 microns), the cumulative value remains close to 100% regardless of the grinding time, which indicates the almost complete removal of large fractions. Thus, an increase in the grinding time leads to a more significant reduction in particle size and a significant increase in the proportion of small fractions.



**Figure 5.** The effect of grinding time on the particle size distribution of coarse residues.

In the work of Marwa (2023), it was found that small waste fractions (<10 mm) exhibit high values of acidity and intensive metal leaching, emphasizing the importance of fineness control to

reduce environmental risks [16]. The article by Lyalyuk et al. (2013) emphasizes the importance of coke crushing to improve the gas permeability of the blast furnace charge, where reducing large fractions (>80 mm) to 1-2% increases furnace productivity and reduces coke consumption [18]. In addition, data from Jani et al. (2018) indicate that even for landfill waste, fine fractions (<10 mm) are of key importance for the mobility of heavy metals (Zn, Cu, Cr), which is important to consider during processing and reclamation [13]. Pfandl et al. (2019) noted that the efficiency of X-ray fluorescence sorting of non-ferrous metals from slags strongly depends on the particle size range (optimally 10-32 mm), and smaller fractions require separate processing [19]. Thus, our own results confirm the importance of choosing the optimal grinding time in order to maximize the release of valuable components, minimize large fractions, and improve technological performance during subsequent processing stages. This is consistent with the literature data on the need to control particle distribution at different stages of raw material preparation.

4.2. The Effect of Particle Size Distribution on the Extraction of the Studied Components from Slags

Particle size plays a key role in the efficiency of the flotation process, as it directly affects the interaction of reagents with metallurgical waste containing valuable elements. Table 3 shows the values of the results of flotation experiments using various reagents (Na<sub>2</sub>S-3418A, KAX-Na<sub>2</sub>S-3418A) with different particle fractions.

Table 3. Estimated values of flotation experiments.

Conditions	Products	Weight, %	Estimated values, %		Output, %	
			Cu	Zn	Cu	Zn
	Estimated values of flotation experiments Na <sub>2</sub> S-3418 A					
63 microns	Total flotation	17,74	2,16	3,85	53,86	19,04
	Residue	82,26	0,40	3,53	46,14	80,96
	*Input	100,00	0,71	3,59	100,00	100,00
45 microns	Total flotation	21,32	1,89	3,92	56,28	22,68
	Residue	78,68	0,40	3,62	43,72	77,32
	*Input	100,00	0,72	3,68	100,00	100,00
38 microns	Total flotation	22,59	1,91	4,02	58,39	25,15
	Residue	77,41	0,40	3,49	41,61	74,85
	*Input	100,00	0,74	3,61	100,00	100,00
	Estimated values. Coarse flotation: KAX, Control flotation: 3418 A					
63 microns	Total flotation	17,08	1,78	3,15	46,75	18,47
	Residue	82,92	0,42	2,87	53,25	81,53
	*Input	100,00	0,65	2,92	100,00	100,00
45 microns	Total flotation	23,68	1,54	3,25	56,23	26,28
	Residue	76,32	0,37	2,83	43,77	73,72
	*Input	100,00	0,65	2,93	100,00	100,00
38 microns	Total flotation	25,54	1,53	3,28	59,05	28,45
	Residue	74,46	0,36	2,83	40,95	71,55
	*Input	100,00	0,66	2,94	100,00	100,00
	Experimental results of crushed coarse residues during control flotation					
24 microns	Total flotation	25,74	1,28	2,27	49,38	19,94
	Residue	74,26	0,45	3,16	50,62	80,06

20 microns	*Input	100,00	0,67	2,93	100,00	100,00
	Total flotation	25,74	1,28	2,27	49,38	19,94
	Residue	74,26	0,45	3,16	50,62	80,06
<10 microns	*Input	100,00	0,67	2,93	100,00	100,00
	Total flotation	32,84	1,10	2,53	55,88	28,21
	Residue	67,16	0,43	3,14	44,12	71,79
	*Input	100,00	0,65	2,94	100,00	100,00

The results show that nearly half of the Cu can be recovered during rougher flotation, and the Cu grade in the concentrate can reach up to 20.15% after six stages of cleaning. The use of Na<sub>2</sub>S during coarse flotation had a positive effect, but no effect was observed during control flotation, which is consistent with the conclusions (Sajjad & Otsuki, 2022), which emphasize that the effectiveness of reagents and their interaction with minerals depend on the stages of the process and the characteristics of the suspension [22]. Also, reducing the pH level in the control flotation proved to be insufficiently effective. An increase in flotation efficiency was achieved by regulating the particle size distribution, which fully corresponds to the conclusions Kazemi et al. [23], where the optimal particle fraction of +40-60 microns gave the greatest Cu extraction in laboratory conditions (Table 3) [23–25].

The conducted studies on lead-produced slags revealed important patterns: the particle size of 38 microns turned out to be the most suitable for the initial stages of flotation, providing a sufficient contact area of the waste with flotation reagents and minimizing copper losses. This is also confirmed by studies Chi Wang et al., [26], which show that fine particles can improve interaction with air bubbles and reagents, but their excess can negatively affect the process due to aggregation and changes in the rheological properties of the pulp [26,27].

Reducing the particle size to <10 microns demonstrated a positive effect on copper extraction: Cu extraction increases by about 7%, and the overall flotation efficiency reaches about 60%. This effect is associated with an increase in the available surface of minerals for interaction with reagents and air bubbles, which improves the formation of partially bubble aggregates and promotes better separation of valuable components from waste rock. Similar approaches aimed at improving the efficiency of flotation of fine particles using nanobubbles and nanoparticles are discussed in detail in [28] (Sigauke et al., 2025), which emphasizes their role in increasing hydrophobicity, stabilizing foam, and improving separation [28–30].

However, it is important to take into account that excessive grinding, resulting in a particle size of <10 microns, is not always the optimal solution. If the grinding is too fine, a number of negative consequences are observed, including a deterioration in pulp filtration, an increase in the viscosity of the slurry, the formation of aggregates of fine particles, as well as a significant increase in energy consumption for grinding. These problems reduce the efficiency of the subsequent stages of the process, require longer time for dehydration of concentrates and can lead to the loss of some valuable components due to non-selective capture of particles in tailings. This is confirmed in the work [31] (Zeng et al., 2023), where the authors emphasize the importance of finding a balance between the degree of grinding and the efficiency of flotation, noting that excessive grinding contributes to the formation of aggregates ("card houses"), increased viscosity and deterioration of filtration, which is especially critical in the design and modernization of processing plants [31–33].

It should also be noted the significant content of precious metals (Au, Ag), which showed that their magnitudes in concentrates at 38 microns reach 1.3 g/t of gold and 416 g/t of silver, although the content of these metals in the initial sample was quite low. This is due to the fact that gold and silver are often associated with finely dispersed minerals, which makes them more vulnerable to flotation extraction in fine fractions. Thus, the obtained results and literature data emphasize that achieving maximum efficiency of flotation of copper and precious metals requires an integrated approach:



particle size control, optimization of grinding time, proper selection of flotation reagents, consideration of pulp rheology and, if necessary, the introduction of innovative methods — from flotation with carriers to the use of nanotechnology. All this raises the relevance of further research on optimizing the processing of metallurgical waste and improving the economic and environmental efficiency of processes [34].

## 5. Conclusions

The conducted research has shown that the granulometric composition of slags significantly affects the efficiency of extraction of non-ferrous and precious metals. The optimal particle size of about 38 microns ensures the highest efficiency of copper flotation, and reducing the size to <10 microns additionally increases extraction, but is accompanied by a deterioration in filtration and an increase in energy consumption. Noble metals (Au, Ag) are concentrated mainly in fine fractions, which makes their extraction effective at the stage of copper flotation. The data obtained make it possible to recommend the optimization of grinding modes and the selection of flotation reagents to increase the profitability of metallurgical waste processing and reduce the environmental burden.

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