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Article

Kriging Variance Informed Multi-Robot Path Planning and Task Allocation for Efficient Mapping of Soil Properties

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Abstract: Soil property mapping is an essential step in precision agriculture for informed fertiliser application, tillage, and irrigation management to improve crop yields. The current practices involve manual soil property sampling and lab tests of the samples. Due to the slow manual sampling of large land areas and the high costs of the lab tests, these mappings are carried out at very low spatial resolution. A realistic approach to resolve this challenge is to use multiple robots with proximal soil sensors to parallelise the sampling process and to create soil property maps in high spatial resolutions. Multi-robot soil sampling is underexplored in the literature. Therefore, auction-based multi-robot task allocation approaches are proposed in this work to efficiently coordinate the sampling process. To reduce the necessary number of samples for accurate mapping, while maximising information gained per sample, a dynamic sampling strategy, informed by kriging variance from kriging interpolation of sampled soil compaction values, has been implemented. This is enhanced by insertion heuristics for task queuing, and thresholding of tasks which aren't expected to offer significant information gain. The evaluation trials show the suitability of the proposed Distance Over Variance bid calculation, combined with the cheapest insertion heuristic and median kriging variance based task dropping, resulting in substantial improvements in key performance metrics. Although this work looks at soil compaction data, information-driven dynamic sampling of other soil properties from large areas can also utilise the kriging interpolation and kriging variance approach.

Keywords: multi-robot systems; task and motion planning; agricultural automation

1. Introduction

Managing soil health is an essential practice in agriculture and sports ground management (e.g., golf and football). These industries have seen increasing digitisation and automation to enable more precise land management, utilising its potential to reduce inputs, waste, and environmental harms, while simultaneously increasing soil health and crop yields [1]. The mapping of soil properties is critical to precision land management, allowing for localised soil management to address spatially variable deficiencies [2]. There are governmental financial incentives for farmers to map their soils and demonstrate the maintenance of soil health, such as the United States Department of Agriculture's "Environmental Quality Incentives Program", the EU (European Union)'s "Common Agricultural Policy", and the "Sustainable Farming Initiative" of the United Kingdom's Department for Environment Food and Rural Affairs [3–5], which provide additional commercial motivation for high-resolution soil mapping.

In this work, the soil compaction dataset of [6] is resampled in a multi-robot simulation, to demonstrate these developments, as multiple bespoke automated penetrometers have not yet been developed to facilitate this experiment with real robots. Soil compaction, i.e., increased soil density and reduced porosity due to pressure or vibration [7], is one property of interest in measuring soil health, which we

map in this work to demonstrate a proposed multi-robot soil mapping system. High soil compaction is most commonly caused by the pressure on the soil surface from the operation of heavy machinery. It impedes the ability of crops to penetrate the soil with their roots, having negative effects on yields [8]. Excess compaction also causes a lower concentration of SOM (Soil Organic Matter), making the soil less effective at sequestering CO2 [9]. Treatment of soil compaction often involves deep tillage, with the machinery used for this tillage requiring large quantities of fossil fuels [10]. As such, a higher resolution mapping of soil compaction could reduce CO2 emissions by allowing more localised tillage.

Efficient and accurate high-resolution mapping of such soil properties requires optimised coverage due to significant spatial variations in these properties. [11] used OK (Ordinary Kriging) interpolation [12], which is widely used to interpolate geospatial data, to predict soil property measurements at locations where samples have not yet been taken, using a limited number of recorded samples as input. OK produces a variance value for each of its predictions, a metric of the prediction's uncertainty. Relatively high kriging variance can indicate areas that are likely to provide the highest information gain, and most decrease the uncertainty of the OK's predictions. The authors of [11] use this kriging variance for IPP (Informative Path Planning) in single-robot mapping of soil compaction, using the output of OK to direct a Thorvald outdoor robot [13] with a bespoke penetrometer to navigate to and sample at a location where the kriging variance is highest. Although this work looks at soil compaction data, information-driven dynamic sampling of other soil properties from large areas can also utilise the kriging interpolation and kriging variance approach.

This IPP was later extended to multiple robots in [14], generating sampling tasks at multiple positions for each new measured sample, and the new interpolation that follows. This work contributes further extensions to this multi-robot greedy NBV (Next Best View) IPP approach and presents methods of additionally informing auction-based MRTA (Multi-Robot Task Allocation) using kriging variance, allowing sampling tasks to be delegated more efficiently. We expect that the system demonstrated effectively mapping soil compaction here can be applied to efficient mapping of other soil properties, and possibly spatial data from other areas of environmental monitoring or inspection.

The core contributions of this work are:

- 1. DOV (Distance Over Variance) A kriging variance informed bid calculation for auction-based MRTA.
- 2. Integration of the DOV bid calculation into the cheapest insertion heuristic [15].
- 3. Thresholding of tasks at low kriging variance locations at the point of task creation.
- 4. Experimental evaluation of these IPP and task allocation contributions in simulation.
- 5. A free and open-source ROS implementation of the multi-robot soil mapping system available at https://github.com/laurencejbelliott/ROS_multi-robot_soil_mapping_sim.

The remainder of this paper is organised as follows. Section 2 presents existing work related to this. Section 3 introduces the proposed multi-robot coordination system, with details of the different bid calculation approaches and heuristics used. The experimental setup is explained in Section 4. This is followed by the outcomes of the empirical evaluations in Section 5 and concluding discussions in Section 6.

2. Related Work

2.1. Automated Soil Properties Mapping

2.1.1. Aerial Sensing

Although multi-robot soil mapping is underexplored in academic literature, there are numerous existing methods of automated mapping of soil properties, each capable of measuring or predicting a different set of properties, and having unique strengths and limitations. One of the earliest of these methods is aerial sensing, using imagery captured by sensors or cameras on satellites in orbit of Earth, or UAVs flying within the earth's atmosphere. The data captured by these satellites is typically low in spatial resolution, but is captured continuously, allowing for high temporal resolution. Some of these data are open access, such as that of the EU's Sentinel satellites [16]. RGB image data from satellites

has been used to accurately estimate crop biomass [17], and NDVI (Normalised Difference Vegetation Index) [18], a metric of crop health. Data from hyperspectral sensors, mounted on satellites or on UAVs (Unmanned Ariel Vehicles) and UGVs (Unmanned Ground Vehicles), has facilitated accurate prediction of pH, SOM, clay content [19], and soil moisture [20]. And microwave sensing has been used to directly measure soil moisture [21].

While UAVs can map a large area in a short time, this speed comes at the expense of resolution, as higher resolution mapping requires reduced distance to the ground, which also reduces the coverage speed. Measurements cannot be obtained below the soil surface, which can also be obscured by a crop's canopy. It is not presently possible to remotely capture such a gamut of soil properties as on-the-ground probe sensors can, with remote sensing largely limited to prediction or proxy measurements from vision sensors, e.g., visual indices such as NDVI and hyperspectral Physiological Reflectance Index (PRI) [22]. Prediction of soil properties from aerial imagery often involves machine learning models such as Random Forest [20], and neural networks trained on aerial multispectral or hyperspectral imagery [23].

2.1.2. Wireless Sensor Networks

It is important to note that some soil properties cannot be accurately measured or predicted by remote sensing, and those that cannot be estimated at depths below the soil surface using these sensing methods [19,24]. WSNs (Wireless Sensor Networks) offer more direct continuous sensing of soil properties at or below the soil surface, typically using TDR (Time Domain Reflectometry). However, the costs of WSNs scale linearly with their spatial resolution, making high-resolution mapping of large areas prohibitively expensive. Despite this, WSNs are gaining industrial adoption, with commercial solutions available from companies such as Soil Scout [25] and Agrovista [26].

2.1.3. Ground-Based Robotic Solutions

Outdoor ground-based mobile robots have the ability to capture soil property data at a very high spatial resolution, through hyperspectral imagery or probe sensor measurements, compared to UAV and satellite visual remote sensing which suffer from poor image resolution [27]. Compared with WSN measurements, ground robots have the ability to sample an arbitrary number of points [28] and change the spatial resolution of the sampling as necessary. An example of this can be seen in [29], which creates a multi-layered map from composites of stereo RGB, Visable / Near Infrared (VIS-NIR), and thermal images. The thermal and VIS-NIR images are projected onto the point cloud from the stereo camera, to enrich them with the same depth information that a stereo camera brings to its RGB imagery. This high-resolution 3D map includes surface readings of the soil temperature and NDVI.

Being able to capture and predict soil properties from high-resolution hyperspectral imagery is useful, but the unique advantage of ground-based outdoor robots compared to other methods of automated soil sensing is their ability to measure soil properties more directly and at variable depths below the soil surface using probe sensors. This extra dimension enables the mapping of soil properties in 3D, as demonstrated by 3D mapping of soil compaction by [11], using the Thorvald agricultural robot platform equipped with an automated penetrometer at sampling locations informed by kriging variance.

2.2. Informative Path Planning

Informative path planning algorithms aim to produce paths that avoid collisions and optimize one or more particular objectives [30]. [28] presents an informative path planning method based on the the kriging variance, a measure of the uncertainty of predictions made by OK interpolation. A single ground-based Thorvald robot mapping soil moisture, after each new measurement and subsequent OK interpolation, navigates to the location where this uncertainty metric is highest to perform its next soil moisture measurement. We extend this greedy Next Best View (NBV) adaptive sampling method described in their work, creating sampling tasks at the *x* highest kriging variance locations, where *x* is

the number of robots. This multi-robot kriging variance based informative path planning is described in more detail in Section 3.1.

2.3. Multi-Robot Coordination

SSI (Sequential Single-Item) auction was identified as the most effective of a set of auction-based MRTA algorithms tested for dynamic task environments in [31]. Dynamic task environments are produced by informative path-planning, as tasks are not known a priori and new tasks are continually created throughout the sampling mission. Auction-based MRTA also has the benefit of allowing for domain specific information to be encoded in its bid calculation to better inform task allocation [32,33], agnostic of the particular auction-based task allocation algorithm used. We utilise this by designing a kriging variance-informed bid calculation to further incentivise sampling in areas of high information gain and use it to extend the cheapest insertion heuristic [15]. The cheapest insertion heuristic calculates the cost of a robot traversing a queue of tasks in sequence, given the insertion of a prospective task at the index which will contribute the lowest increase in this cost. Our bespoke bid function and its use in combination with the cheapest insertion heuristic is described in more detail in Section 3.2.

3. Methodology

3.1. Multi-Robot Informative Path Planning from Kriging Variance

In this work, we consider that the environment is partitioned into a course-grain "sampling grid" pattern with square-shaped cells, similar to the standard geological mapping approaches. We use this grid structure to reduce the chances of multiple sampling tasks in close proximity by limiting to a maximum of one sampling task in each grid cell. In this grid pattern, the cell's side $cell_{dim}$ of each of this grid's cells is calculated as

$$cell_{dim} = \lfloor \sqrt{\frac{(w \cdot h)}{N_c}} \rfloor, \tag{1}$$

where w and h are the width and height of the environment being sampled, and N_c is the approximate total number of cells in the grid pattern, resulting in cells of area $A = cell_{dim}^2$. These cells are created in rows, starting in the North-Western (Top-Left) corner of the environment, and are cropped where they intersect with the limits of the environment. In the data considered in this work, the environment was divided into 64 grid cells ($N_c = 64$).

Our multi-robot soil mapping system uses a centralised coordinator as a proof-of-concept for easier kriging interpolation to identify the task locations and as the fixed auctioneer for the task allocation auctions. With the task allocation already based on auctions, the kriging interpolation could be easily decentralised with each robot interpolating independently and a consensus process propagating and converging the information across the robotic fleet. The coordinator is responsible for performing the kriging interpolation and broadcasting new sampling tasks at the locations with high kriging interpolation values. We extend the greedy NBV adaptive sampling method described in [28], creating sampling tasks at the N_r highest kriging variance locations, where N_r is the number of robots, after each round of interpolation. These tasks are allocated using SSI auctions, with each robot storing its allocated tasks in a FIFO (First-In-First-Out) task queue.

Initial sampling tasks are created at the robots' initial positions, as a minimum of three samples are required for kriging interpolation. This assumes a team of at least three robots is engaged in the sampling. If fewer robots are used, the initial three sampling tasks are created in their initial positions, and random positions within the environment.

Before these created tasks are allocated using auction-based MRTA, we "drop" new sampling tasks where the kriging variance at the task's position is less than the median of the kriging variance matrix. This is intended to reduce the incidence of robots being allocated sampling tasks that are unlikely to significantly reduce the uncertainty of the kriging interpolation of the soil property being mapped.

3.2. Bid Calculation for Allocation of Soil Sampling Tasks

3.2.1. Distance Over Variance (DOV) Bid Function for Auction-Based Multi-Robot Task Allocation

In this work, the SSI auction approach is used as the MRTA algorithm to reduce the computational complexities associated with combinatorial auctions. A general approach in such auction-based methods is to use the Euclidean distance between the robot and the task location as the bid value. However, to select a task that will improve the information gain with minimal navigation, we propose a bespoke bid calculation we term "DOV (Distance Over Variance)", calculated as

DOV =
$$\frac{\sqrt{(x_r - x_t)^2 + (y_r - y_t)^2}}{Vx_{t_t}y_t}$$
, (2)

where (x_r, y_r) is the robot's position, (x_t, y_t) is the task's position, and V is the 2D kriging variance matrix produced by the most recent kriging interpolation.

This bid calculation divides the Euclidean distance between the robot and the task by the kriging variance at the task's position, incentivising sampling in nearby areas where the interpolation has high uncertainty, and is therefore expected to result in the highest information gain with minimal navigation of the robot.

3.2.2. Cheapest-Insertion Heuristic

The cheapest insertion heuristic proposed in [15] is implemented as an optional feature within the coordinator, and when enabled, is used in calculating the bid function. In a robot's bid calculation, for each possible insertion of the currently auctioned task into its task queue, the cost is calculated for the robot traversing from its current position, to the sampling position in the first task in the robot's queue, and then iteratively from that task's sampling position to the sampling position of the next task in the queue, until this cost is calculated for the whole queue. When using the DOV bid function, the cost of traversing from one position to another is calculated as the Euclidean distance between the two positions, divided by the kriging variance at the second position.

3.3. Abstract ROS Simulation of Multi-Robot Soil Compaction Mapping

Historical soil compaction data [6], sampled from an arable field by a single Saga Robotics Thorvald robot [13] in a grid pattern using a bespoke automated penetrometer, was interpolated using OK to create a ground truth soil compaction distribution, pictured in Figure 1, for re-sampling by multiple simulated robots. We consider a fleet of three ground-based outdoor wheeled robots. However, larger robotic fleets can be considered. The robots are simulated using the multi-robot simulator included in 'move_base_abstract' [34]. This simulator represents robots with a high level of abstraction, not modelling collisions, sensors, complex physics simulation, or 3D graphics, to enable faster-than-realtime simulation of systems that don't require these features. It models only time and the poses and navigation of an arbitrary number of robots. It uses a drop-in replacement of the standard 'move_base' robot navigation in ROS, to move the robots to positions along a straight line to their goal according to their maximum speed and acceleration, enabling faster-than-realtime simulations.

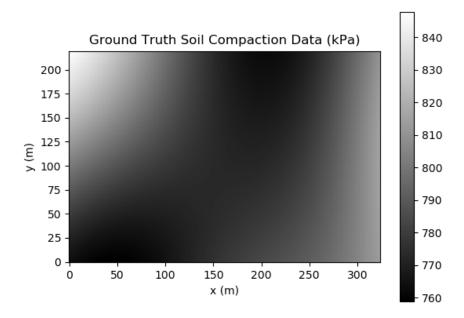


Figure 1. The grid-sampled soil compaction data from [6], interpolated using OK, and used as a ground truth soil compaction distribution in the simulated multi-robot soil compaction mapping.

4. Experimental Design

Eight auction configurations of the multi-robot soil properties mapping system were tested in the simulation:

- ED Euclidean Distance as the bid value.
- EDCI Euclidean Distance as the bid value with Cheapest Insertion heuristic.
- EDTD Euclidean Distance as the bid value with Task Dropping.
- EDCITD Euclidean Distance as the bid value with Cheapest Insertion heuristic and Task Dropping.
- DOV Distance Over Variance as the bid value.
- DOVCI Distance Over Variance as the bid value with Cheapest Insertion heuristic.
- DOVTD Distance Over Variance as the bid value with Task Dropping.
- DOVCITD Distance Over Variance as the bid value with Cheapest Insertion heuristic and Task Dropping.

Thirty trials of simulated 3-robot soil compaction mapping were conducted for each of these configurations. Each trial ran with a time budget of 480 seconds of simulation time so that the performance of the system could be measured at the end of this time, and compared between configurations using a number of performance metrics and testing of statistically significant differences between the values of these metrics across different configurations. The robots' starting locations within the simulated field environment were randomly generated. The trial number, incrementing from one to 30 in each batch of 30 trials run for each configuration of the system, was used as a seed for this random number generation, so that trial one of 30 in the ED trials, for example, had the three robots start at the same locations as they did in trial one of 30 in the trials run for DOV, and the other configurations tested.

Values of different performance metrics, listed below, were calculated at the end of each trial. The arrow, next to the metric name, indicates if a high value (\uparrow) or a low value (\downarrow) is preferred for that metric.

- Kriging RMSE (Root Mean Squared Error) (↓) The RMSE between the kriging interpolation of soil compaction produced from the samples taken by the multi-robot sampling, and the ground truth soil compaction data.
- Max task queue length (↓) The maximum length measured across all of the robots' task queues.

• Mean TA (Task Allocation) equality (\uparrow) - A metric that measures how equally distributed tasks are between the robot team. This equality E is calculated using the equal allocation proportion

$$e = \frac{1}{N_r},\tag{3}$$

where N_r is the number of robots. With this we can calculate

$$E = 1 - |e - \frac{T_i}{\sum_{r=1}^{\#(T)} T_r}|,\tag{4}$$

where T is the set of task counts for all robots¹, indexed by robot ID r, and i is the ID of the robot we are calculating the TA equality for.

This TA equality is calculated for each robot, and the mean is taken to represent the equality of TA for the whole team.

- Mean kriging variance (↓) The mean of the kriging variance matrix generated from the most recent kriging interpolation.
- Mean task completion time (seconds) (↓) The mean time taken to execute a sampling task, across
 all robots and tasks, measured from the beginning of robot navigation towards the task, to task
 completion following the measurement of the task's sample.
- Number of samples (↑) The total number of samples of soil compaction measured by the robot team. A high value is considered to be the best value, as the trials are run for a specific time.
 If the trials are run for an arbitrary time until the Kriging Variance comes below a threshold value, a low value would be ideal for this metric.
- Total distance travelled (metres) (↓) The total distance travelled by the robot team, measured in metres.
- Total idle time (seconds) (↓) The total time that robots within the team have spent idle (stationary, without any current or queued tasks). A low value is considered to be the best here, assuming maximum utilisation. However, if the number of samples is smaller for the same number of robots, the idle time can be high.
- Total robot tasks count (↓) The total number of sampling tasks allocated to the robot team.

5. Simulated Experiment Results

Thirty trials of simulated 3-robot soil compaction mapping were conducted for each of the eight different task allocation configurations. Each trial ran with a time budget of 480 seconds of simulation time. Figure 2 shows the screenshot of rViz window with the robot positions during the mission (yellow, green and red arrows) and the background showing heatmap of soil compaction interpolated using OK from the sampling completed so far. Figure 3 (a) shows the kriging-interpolated soil compaction at 439.0 s and Figure 3 (b) shows the corresponding kriging variance at the next iteration at 440.0 s for future allocations when DOVTD strategy was used. The routes taken by each robot are highlighted with sampling locations. It can be clearly observed that the Kriging variance is extremely low near the sampled locations. The task locations and allocations are different for the eight configurations based on the initial locations of the robots, bid calculation and task queue maintenance strategies. This can be seen by comparing Figure 3 with Figure 4 which shows the kriging interpolated soil compaction values (a), kriging variance (b) and the colour-coded routes takes by each robot when DOVCITD strategy was used.

Please note that #(T) is used to denote the cardinality of T, to distinguish it from the notation for absolute distance.

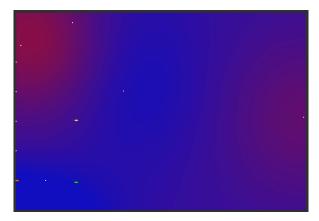


Figure 2. A cropped screenshot of the visualisation of a simulated soil compaction mapping mission in progress. The soil compaction predicted by the limited simulated sampling by OK is displayed as a heatmap. Overlaid on this heatmap are robots' locations represented by colour-coded arrows, and sample positions are denoted as white markers.

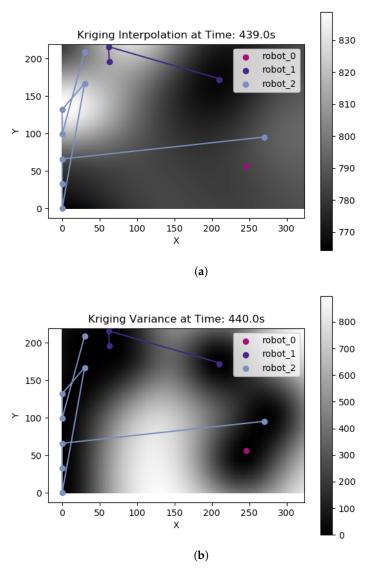
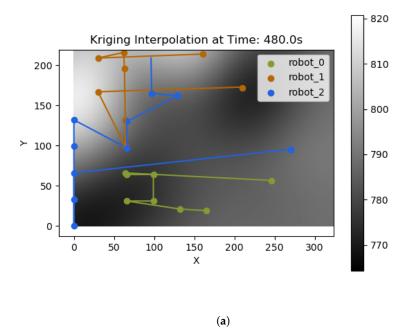


Figure 3. Heatmaps of kriging variance and predicted soil compaction values (kPas) from OK performed at the final second of trial 1 in the simulated testing of the DOVTD configuration of the multi-robot soil mapping system. Color-coded robot trajectories, and sample positions, are overlaid as points and lines respectively. (a) Predicted soil compaction values (kPas) from OK at 439.0 seconds into trial 1 of the DOVTD trials. (b) Kriging variance from OK at 440.0 seconds into trial 1 of the DOVTD trials.



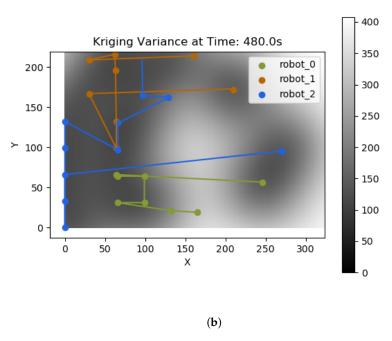


Figure 4. Heatmaps of kriging variance and predicted soil compaction values (kPas) from OK performed at the final second of trial 1 in the simulated testing of the DOVCITD configuration of the multi-robot soil mapping system. Color-coded robot trajectories, and sample positions, are overlaid as points and lines respectively. (a) Predicted soil compaction values (kPas) from OK at 480.0 seconds into trial 1 of the DOVCITD trials. (b) Kriging variance from OK at 480.0 seconds into trial 1 of the DOVCITD trials.

Mean and standard deviation were calculated from each metric described in Section 4 at the end of the 8-minute time budget given to the sampling, across 30 trials within each configuration of the multi-robot soil mapping system. These summary statistics can be found in Table 1. D'Agostino and Pearson's normality test [35] was run for each performance metric and configuration of the system, on the values observed for the given metric in the last second of each simulated trial in the given configuration.

Table 1. Mean and standard deviation (σ) of performance metrics calculated from 30 trials in each of the 8 configurations of the multi-robot soil mapping system tested in simulation. The best and second best value for each metric is highlighted in green and yellow respectively.

	ED	EDCI	EDTD	EDCITD	DOV	DOVCI	DOVTD	DOVCITD
Kriging RMSE (Root Mean Squared Error)	17.46 ± 13.9	17.11 ± 9.44	16.85 ± 20.17	15.41 ± 8.98	19.13 ± 16.33	17.09 ± 9.92	12.88 ± 4.74	20.41 ± 18.41
Max task queue length	11.8 ± 4.28	6.87 ± 2.4	8.76 ± 4.77	5.83 ± 1.78	8.93 ±65 3.76	5.2 ± 1.54	5.47 ± 3.25	3.3 ± 1.37
Mean TA equality	0.78 ± 0.05	0.78 ± 0.03	0.81 ± 0.09	0.81 ± 0.04	0.8 ± 0.05	0.8 ± 0.03	0.83 ± 0.06	0.84 ± 0.05
Mean kriging variance	339.68 ± 127.94	352.65 ± 158.21	347.76 ± 156.15	340.45 ± 135.26	398.21 ± 160.69	336.17 ± 122.24	335.26 ± 145.38	280.36 ± 121.05
Mean task completion time (seconds)	28.16 ± 10.67	36.33 ± 13.28	24.71 ± 8.57	40.25 ± 11.02	36.95 ± 9.45	43.03 ± 5.73	31.93 ± 10.91	38.76 ± 10.01
Number of samples	20.43 ± 14.54	16.8 ± 2.82	16.03 ± 3.01	16.4 ± 2.13	15.87 ± 2.3	15.53 ± 2.01	14.23 ± 3.04	15.43 ± 2.1
Total idle time (seconds)	318.6 ± 529.65	139.57 ± 112.15	324.75 ± 230.95	217.29 ± 190.79	185.51 ± 142.27	205.7 ± 149.11	416.08 ± 308.98	455.05 ± 250.52
Total robot tasks count	45.87 ± 10.08	42.93 ± 8.14	33.41 ± 10.12	35.07 ± 6.86	40.47 ± 6.32	38.17 ± 5.58	26.43 ± 8.68	27.87 ± 7.76

This normality testing was used to determine whether parametric or non-parametric significance tests would be more appropriate for comparing performance between different configurations of the system across the recorded metrics. It was found that per-configuration observations for all metrics were normally distributed, except for kriging RMSE. It was thus decided that significance testing would first investigate, for each performance metric, using the Kruskal-Wallis [36] test for kriging RMSE, and ANOVA [37] for the other metrics, whether there was a statistically significant difference between the means of these metrics between different configurations of the multi-robot soil mapping system.

ANOVA and Kruskal-Wallis tests showed a significant difference in the means of all performance metrics across the tested configurations of the system, except for kriging variance. This could be explained by the very high standard deviation seen in Table 1, which suggests that the initial positions of the robots may have a significant impact on the kriging variance. This may be due to the ground truth soil compaction distribution, pictured in Figure 1, having relatively small "hot-spots" of high soil compaction, which could be measured and accounted for in kriging interpolation immediately in cases where one or more robots start sampling within these areas of interest.

Following the ANOVA and Kruskal-Wallis tests, Tukey's HSD (Honestly Significant Difference) test [38] was conducted within each metric comparing every pair of configurations, except for kriging RMSE, where non-parametric Wilcoxon signed-rank tests [39] were used instead, given that the data for this metric was not normally distributed. The configuration of the system that resulted in the lowest mean kriging RMSE, a key metric of the accuracy of the mapping, after 480 seconds, was DOVTD. Wilcoxon signed-rank tests showed that DOVTD performed significantly better for kriging RMSE than DOV, DOVCI, and EDCI. This indicates that the "task dropping", introduced in Section 3.1, results in improved interpolation accuracy within a time-limited mapping when used in conjunction with the DOV bid calculation, and more effectively improves interpolation accuracy than using DOV with the cheapest insertion integration (DOVCI). It should be noted however that a significant difference in RMSE was not found between ED and EDTD, so the improvement in interpolation accuracy when dropping tasks at low kriging variance positions is not seen when using Euclidean distance instead of DOV for the bid calculation.

One limitation of the SSI auction-based task allocation used in this system is that some robots can be under-utilised, sitting idle without any tasks in their task queues. This can result from a robot giving low bids due to its initial position not being as near areas of high kriging variance where tasks are created by the IPP. DOVCITD was found to best address this out of the 8 configurations tested, achieving the highest mean TA equality, and lowest max task queue size. This demonstrates a more even distribution of tasks, which is supported by Tukey's HSD tests showing that DOVCITD had a significantly lower mean for the max task queue length metric than DOV, ED, EDTD, EDCI, and EDCITD.

Another important metric is the total distance travelled, a proxy of the energy expended by the system and the compaction that the operation of the robots on the soil surface contributes. EDTD resulted in the lowest mean for this metric but was not significantly lower than that of the DOVTD, which scored second lowest. Given DOVTD's superior interpolation accuracy and not significantly lower total distance, it may be argued that DOVTD represents a more acceptable trade-off between interpolation accuracy and energy consumption and soil compaction resulting from the system than other configurations tested.

6. Conclusions

This work has presented novel contributions in IPP and MRTA, including thresholding of sampling tasks at the point of task creation using median kriging variance, the DOV bid calculation, and integration of DOV within the cheapest insertion heuristic for a multi-robot soil sampling system. This approach has wider applications in other ground sampling, where kriging interpolations are used traditionally. A free and open-source ROS coordinator and simulation has been developed to

implement and test these contributions, individually, and in combination, and against the baseline Euclidean distance bid calculation.

The kriging variance informed MRTA contributions presented in this work, i.e., DOV bid calculation in conjunction with the dropping of tasks at low kriging variance locations, was found to produce the most accurate maps of soil compaction of all configurations of the multi-robot soil mapping system tested in simulated experiments. Significance testing described in Section 5 demonstrated that the task-dropping feature significantly improved this interpolation accuracy when combined with DOV. DOVTD was also found to not be significantly worse than the best-performing configurations for TA equality, task completion time, and total distance travelled.

The integration of DOV into the cheapest insertion heuristic did not result in more accurate mapping but did produce the most equal allocation of tasks, addressing an issue observed in some trials where one robot would be assigned very few sampling tasks and be underutilised. Future work may investigate alternative solutions to this task allocation inequality, such as limiting the size of each robot's task queue, and test whether this improves the system's performance. The coordinator's ROS compatibility, and use of the move_base action client to direct robot navigation, should allow it to be deployed and tested as a real-world multi-robot system with relative ease. The multi-robot mapping of spatial data demonstrated here can easily be applied to other soil properties and even spatial data from other applications within environmental monitoring and inspection. Future work may investigate its effectiveness in mapping other distributions of spatial data.

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