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Posted Date: 26 May 2025

doi: 10.20944/preprints202505.1953.v1

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Article

# Transfer Learning-Enhanced Prediction of Glass Transition Temperature in Bismaleimide-Based Polyimides

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Abstract: The glass transition temperature (Tg) is a pivotal parameter governing the thermal and mechanical properties of bismaleimide-based polyimide (BMI) resins. However, limited experimental data for BMI systems posed significant challenges for predictive modeling. To address this gap, this study introduces a hybrid modeling framework leveraging transfer learning. Specifically, a multilayer perceptron (MLP) deep neural network is pre-trained on a large-scale polymer database and subsequently fine-tuned on a small-sample BMI dataset. Complementing this approach, six interpretable machine learning algorithms-Random Forest, Ridge Regression, K-Nearest Neighbors, Bayesian Regression, Support Vector Regression, and Extreme Gradient Boosting —are employed to construct transparent predictive models. SHapley Additive exPlanations (SHAP) analysis is further utilized to quantify the relative contributions of molecular descriptors to Tg. Results demonstrate that the transfer learning strategy achieves superior predictive accuracy in data-scarce scenarios compared to direct training on BMI dataset. SHAP analysis identified charge distribution inhomogeneity, molecular topology, and molecular surface area properties as the major influences on T<sub>g</sub>. This integrated framework not only improves the prediction performance, but also provides feasible insights into molecular structure design, laying a solid foundation for rational engineering of high-performance BMI resins.

**Keywords:** bismaleimide-based polyimides; transfer learning; T<sub>g</sub> prediction; molecular design; machine learning; glass transition temperature

#### 1. Introduction

The thermal stability of polymer substrates in high-temperature environments represents a critical technical bottleneck limiting the advancement of advanced composite materials. The glass transition temperature (Tg), a key parameter governing the transition from the glassy to the rubbery state, directly influences the morphological stability and mechanical property retention of thermoplastic and thermosetting polymers under extreme conditions[1]. For high-performance thermosetting polymers such as bismaleimide-based polyimides (BMI) resins, Tg determines their practical application potential in critical fields such as aerospace thermal protection structures and microelectronic packaging materials[2]. However, optimizing Tg in BMI resins remains a complex challenge, as it is highly dependent on composite and architecture of polymers[3–6]. Traditional trial-and-error approaches are constrained by lengthy experimental cycles, prohibitive testing costs, and difficulties in elucidating microscopic mechanisms. While computational methods like density functional theory (DFT)[7] and molecular dynamics (MD) simulations offer theoretical frameworks for Tg prediction[8–10], the intricate cross-linking networks, multidimensional aromatization

reactions, and synergistic functional group interactions in BMI resins introduce dual challenges: exponentially increasing computational resource demands and empirical force field parameter selection in atomic-scale simulations.

Recent advances in polymer informatics have introduced a data-driven paradigm for materials development, enabling inverse analysis of structure-property relationships through machine learning[11–15]. Notable progress includes, Lei et al.'s[16] systematic benchmarking of 79 models for Tg prediction, which revealed synergistic interactions between molecular fingerprints and neural architectures. He et al.[17] demonstrated the scalability of this approach by developing a quantitative structure-property relationship (QSPR) model for 695 polyesters, achieving experimental validation errors within 17.4°C through virtual screening. Ning et al.[18] further advanced this paradigm by implementing deep learning frameworks for fluorinated polybenzoxazole systems, enabling simultaneous prediction of multiple physical properties. While these studies highlight the transformative potential of machine learning in polymer design, their success critically depends on large-scale, high-quality datasets[19–22]. In contrast, the BMI resin field is constrained by data scarcity and label noise arising from inconsistent experimental conditions, severely limiting model predictive capabilities.

To address the data scarcity challenge in BMI resin research, we employ transfer learning, a paradigm where knowledge gained from large datasets is repurposed for related tasks with limited data[23]. This approach has demonstrated efficacy in materials informatics. Yamada et al.[24] achieved high predictive performance in material property estimation using only tens of samples through their XenonPy.MDL pre-trained model library. Zhang et al.[25] developed a transfer learning framework to predict stress-strain curves of polymer composites, achieving 46.14% accuracy improvement in plastic deformation stages through optimal transport integration. Kazemi-Khasragh et al.[26] extended this concept to diverse polymer property prediction, accurately forecasting thermal and mechanical properties using datasets as small as 13 samples. Building on these foundations, we propose a hybrid framework that combines transfer learning and interpretable machine learning to overcome data limitations in BMI resin studies.

By working on a baseline database (Data\_1) consisting of 3916  $T_g$  measurements of different polymer types, we build a base model with a large amount of physical information. To perform feature extraction, we employ a multilayer perceptron (MLP) architecture inspired by the pioneering work of Chen et al.[27], who demonstrated the efficacy of neural networks in capturing the relationship between polymer structure and  $T_g$ . We extend this approach to address the problem of data scarcity for BMI resin by integrating transfer learning. Experimental results show that our constructed model accommodates the experimental inconsistency in the target BMI dataset (Data\_2, n = 78) and achieves a prediction performance of Root Mean Squared Error (RMSE) = 27.27°C and Coefficient of Determination ( $R^2$ ) = 0.44 on the Data\_2 test dataset.

In order to elucidate the structure-performance relationship of the BMI resin, we systematically expanded the chemical space beyond the limited experimental data (Data\_2, n = 78) by structurally perturbing a virtual database (Data\_3, n = 1092). Using this expanded dataset (Data\_3), the Extreme Gradient Boosting (XGBoost)[28] model was trained using 67 molecular descriptors to achieve  $R^2$  = 0.63 on the Data\_3 test dataset. In addition, SHapley Additive exPlanations (SHAP) values were calculated to quantify the contribution of the descriptors, revealing three main  $T_g$  determinants: charge distribution inhomogeneity, the molecular topology, and surface area properties. By transitioning from "black-box prediction" to "white-box analysis", our approach achieves a quantitative mapping between chemical structure and thermal properties. This work demonstrates the feasibility of data-efficient material discovery in a traditionally data-scarce field and provides a transferable paradigm for high-temperature polymer engineering.

# 2. Materials and Methods

#### 2.1. Data Collection

A two-tier dataset architecture was employed: The base dataset (Data\_1) comprised 3916 diverse polymers[29], among which 697 polyimides (PI)[30] were added due to their topological similarity with the imine pentacyclic structure of bismaleimide-based polyimides (BMI) to improve the pretraining effect of BMI-specific feature extraction. The target dataset (Data\_2), constructed through experimental synthesis and literature curation[4,31–52], contained 78 BMI molecules, which is a scarcity that posed the primary challenge for model development.

In order to systematically characterize the two-tier dataset architecture, we visualized the  $T_g$  distribution of the dataset (Figure 1a) using kernel density estimation (KDE) and distributional analysis. Here, the horizontal coordinates represent the  $T_g$  values corresponding to each data point, while the vertical coordinates indicate the frequency density. The green curve denotes Data\_1, and the red curve denotes Data\_2. Figure 1a reveals the multimodal distribution of Data\_1 (the average value  $\mu$  = 251.25°C), reflecting its composition of diverse polymer families, and the right-skewed distribution of Data\_2 ( $\mu$  = 312.87°C), sugge[4,31–52]sting rigid structural patterns specific to BMI resins. The distinct distributional differences between the two datasets underscore the uniqueness of BMI resins compared to other polymers, explaining why generalized polymer models cannot directly predict the  $T_g$  of BMI.

Molecular structures from both datasets were encoded as Morgan fingerprints (see Section 2.2 for details) and subjected to principal component analysis (PCA). This method projects high-dimensional feature relationships onto interpretable 2D scatter plots, where the horizontal and vertical axes represent the first two principal components after dimensionality reduction. As shown in Figure 1b, partial domain overlap exists between green Data\_1 clusters and red Data\_2 clusters, indicating transferable latent representations while preserving domain-specific characteristics. The black arrows symbolize the knowledge transfer pathway from the general polymer space to BMI-specific regions.

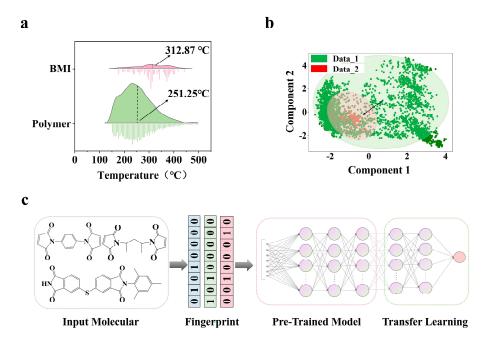


Figure 1. Data Characterization and Methodological Framework: (a) Comparative KDE profiles: Data\_1 (green) shows multimodal distribution patterns, whereas Data\_2 (red) exhibits elevated mean values attributed to rigid structural motifs; (b) PCA dimensionality reduction: Green/red regions denote Data\_1/Data\_2 distributions; arrows indicate transfer learning pathways; (c) Technical Roadmap: Molecular structure  $\rightarrow$  RDKit fingerprint

generation  $\rightarrow$  Deep neural modeling  $\rightarrow$  Transfer learning adaptation, forming a framework for cross-domain knowledge migration.

#### 2.2. Feature Engineering

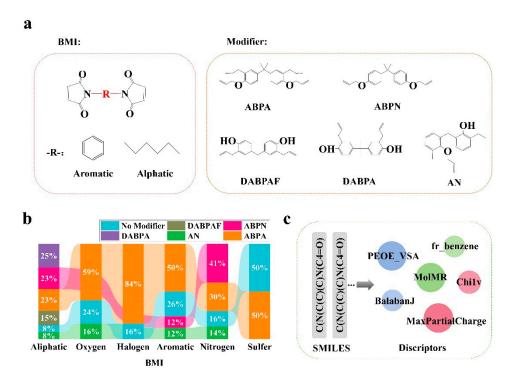
Morgan fingerprint[53] is a circular fingerprint encoding molecular substructures through hashed bit patterns. This encoding strategy preserves topological information at multiple scales while maintaining computational efficiency for neural processing. Unlike scalar molecular descriptors that aggregate global properties (e.g., molecular weight, the number of aromatic rings), Morgan fingerprints retain spatial relationships between functional groups, enabling neural networks to learn representations of structural features for Tg determination. The data preprocessing workflow (Figure 1c) utilized RDKit (RDKit: Open-source cheminformatics; http://www.rdkit.org) to generate 2048dimensional Morgan fingerprints canonical SMILES[54] using from GetMorganFingerprintAsBitVect function with radius = 3 and nBits = 2048, capturing local chemical environments up to three bonds away while maintaining computational efficiency for neural processing.

#### 2.3. Training Strategy of Transfer Learning Model

To address the sample scarcity in Data\_2, a two-stage transfer learning framework was devised (Figure 1c): Stage 1 involved pre-training a MLP model on Data\_1, featuring a 2048-dimensional input layer followed by three fully connected layers (1024/512/256 neurons with ReLU activation) and 30% Dropout regularization. The model underwent 200 training epochs using the Adam optimizer with dynamic learning rate adjustment via ReduceLROnPlateau. Stage 2 implemented selective fine-tuning during transfer to Data\_2: all parameters except the final five layers were frozen, enabling gradient updates only in the last two fully connected layers. This hierarchical adaptation mechanism preserved cross-domain generalizable features while significantly enhancing prediction performance on the low-resource target domain through localized parameter tuning. Evaluation metrics included Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), Mean Squared Error (MSE), and Coefficient of Determination (R²). The presentation and calculation of the evaluation metrics are described in the support informationI.

#### 2.4. Virtual Structure Proposed

In order to elucidate the structure-property relationship between BMI molecules and their  $T_g$ , we categorized BMI molecules into aromatic (conjugated systems such as benzene rings) and aliphatic (linear or branched alkanes) based on the characterization of the R-groups as shown in Figure 2a. We employed a multiscale functional group modification strategy by introducing thioether (-SH), amino group (-NH<sub>2</sub>/NO<sub>2</sub>), oxygen-containing (hydroxyl, carbonyl, ester), and halogen substituents (F, Cl, Br, I). Additionally, five representative copolymer-modified architectures were incorporated, including ABPN, ABPA, DABPA, DABPAF, AN, and unmodified self-polymerization samples, to simulate real-world modification processes[55–57]. The functional group type distribution is visualized in Figure 2b, comprehensively reflecting the structural diversity of BMI resin molecules. The  $T_g$  prediction of these designed virtual structures using Model\_1 yielded a virtual database of BMI (Data\_3, n = 1092).



**Figure 2.** BMI molecular design (**a**) classification framework based on R-group features (aromatic/aliphatic) and systematic functional group modification strategies; (**b**) modifier types showing functional group compositions in five copolymer structures and self-polymerized samples; (**c**) process of calculating descriptors.

#### 2.5. Descripter Calculated

Unlike Morgan fingerprints, molecular descriptors are more suitable for analyzing and quantifying global physicochemical properties, so we use molecular descriptors[60] as feature inputs in the interpretable modeling process instead of Morgan fingerprints. We used RDkit to calculate molecular descriptors (Figure 2c), including 67 descriptors such as maximum partial charge value carried by the atoms in the molecule (MaxpartialCharge), Balaban's topological index (BalabanJ), the sum of atomic molar refractivities (MolMR), and so on. The specific descriptors and their meanings are shown in Supporting Information II. A hybrid feature selection method combining Pearson correlation coefficient identified 23 core descriptors for quantitative structure-property relationship modeling. The results of screening the characterization correlations using the Pearson correlation coefficient method are shown in Supporting Information III.

#### 2.6. Interpretable Model

We tried six machine learning algorithms. Random Forest (RF)[58] operates as an ensemble method combining multiple decision trees via bagging and feature randomness, thereby reducing variance and improving generalization. Ridge Regression[59] extends ordinary least squares by introducing L2 regularization to penalize large coefficients, effectively mitigating multicollinearity and overfitting. K-Nearest Neighbors (KNN)[60] follows a non-parametric, instance-based learning paradigm where predictions are derived from the weighted average of the target variable in the nearest training examples within the feature space. Bayesian Regression (NB)[61] incorporates probabilistic framework by assuming a prior distribution over model parameters, with predictions formulated as posterior distributions via Bayes' theorem. Support Vector Regression (SVR)[62] extends the principles of Support Vector Machines to regression tasks by mapping input features into a high-dimensional kernel space through nonlinear transformations. Extreme Gradient Boosting (XGBoost)[28] implements a gradient boosting framework that sequentially trains decision trees to correct residual errors, employing regularization terms and shrinkage to enhance robustness against overfitting while maintaining computational efficiency through parallel tree construction. We used

5-fold cross-validation in our model training. Specific parameter settings for the model training process are given in support informationIV.

#### 2.7. SHAP Analysis

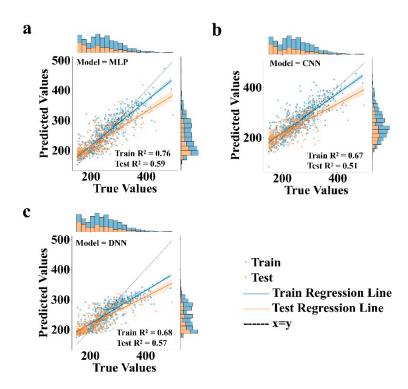
SHapley Additive exPlanations (SHAP)[63], a game-theoretic framework rooted in cooperative game theory, was employed to decompose model predictions into feature contributions by quantifying Shapley values—the marginal impact of each molecular descriptor on  $T_g$  predictions. By aggregating local explanations across the dataset, SHAP generated globally interpretable insights through summary plots and force diagrams, enabling visualization of both linear and non-linear descriptor relationships. The final model leverages SHAP-derived descriptor importance rankings to construct a transparent structure-property map, where each molecular descriptors contribution to thermal transition behavior is represented.

# 3. Results and discussion

3.1. Performance Comparison of Different Neural Network Frameworks as Pre-trained Models in Transfer Learning

Given that the success of transfer learning hinges critically on the pre-trained model possessing robust generalization capabilities, we systematically compared the performance of different neural network frameworks within the transfer learning framework. We selected three distinct neural network frameworks for pre-trained model comparison: Multilayer Perceptron (MLP), Convolutional Neural Network (CNN), and Deep Neural Network (DNN). MLP, as a fundamental feedforward neural network, excels in capturing nonlinear relationships within data through its fully connected layers, making it particularly suitable for processing high-dimensional sparse molecular fingerprint data, such as Morgan fingerprints. In this study, the MLP model, employing a three-layer hidden structure, demonstrated exceptional predictive capability on the test dataset of Data\_2, achieving an R<sup>2</sup> value of 0.59. In contrast, CNN, renowned for its convolutional and pooling layers, excels in tasks like image recognition. However, within the transfer learning framework of this study, the CNN architecture did not surpass MLP in terms of predictive accuracy and generalization performance. This discrepancy might stem from CNN's proficiency in handling local features and spatial hierarchies, which may not be fully leveraged when dealing with high-dimensional sparse molecular data. DNN, or Deep Neural Network, enhances model representational power by increasing network depth. The DNN model adopted in this study comprised five hidden layers, enabling it to learn more complex feature representations. Despite its theoretical strong fitting capability, DNN's performance on the specific tasks and datasets of this study still slightly lagged behind MLP. This could be attributed to potential overfitting issues during DNN training, as well as challenges posed by data scarcity and quality heterogeneity in this study.

To visually illustrate the performance disparities among these models, Figure 3 presents the parity plots for pre-training on the Data\_1 dataset across all three models. In these plots, the horizontal axis represents the true values, while the vertical axis denotes the model predictions. The black dashed line signifies the x = y diagonal, where points closer to this line indicate predictions closer to the true values. The blue line represents the training regression line, and the yellow line denotes the test regression line. Blue dots correspond to training dataset points, and yellow dots to test dataset points. Figure 3a specifically depicts the parity plot for the MLP model trained on Data\_1, with training and test  $R^2$  values of 0.76 and 0.59, respectively. Figure 3b and 3c showcase the parity plots for CNN and DNN models, with training  $R^2$  values of 0.67 and 0.68, and test  $R^2$  values of 0.51 and 0.57, respectively.



**Figure 3.** Pre-training performance comparison of neural network frameworks on Data\_1: (a) MLP parity plot (training  $R^2 = 0.76$ , test  $R^2 = 0.59$ ); (b) CNN parity plot (training  $R^2 = 0.67$ , test  $R^2 = 0.51$ ); (c) DNN parity plot (training  $R^2 = 0.68$ , test  $R^2 = 0.57$ ). Diagonal line indicates ideal prediction (x = y), with training/test data points and regression lines shown in blue/yellow.

The effectiveness of transfer learning hinges on the pre-trained model's performance, particularly its generalization ability, as this directly impacts the subsequent fine-tuning process on Data\_2. The superior performance of the MLP model in pre-training, as evidenced by its higher test R² value and closer alignment of test data points to the diagonal line in Figure 3a, underscores its advantage in handling high-dimensional sparse molecular data. Based on this finding, we selected the MLP model as the pre-trained model, and subsequent transfer learning tasks and methodological explorations were all conducted based on the MLP model.

#### 3.2. Necessity and Technical Advantages of Transfer Learning

Confronting the dual challenges of data scarcity (Data\_2, n = 78) and quality heterogeneity in predicting the  $T_g$  of BMI, our proposed transfer learning framework (Figure 1c) demonstrates significant technical advantages. As our objective focuses on predicting the  $T_g$  of BMI resins, we allocated 10% of Data\_2 as the test set (designated as Test\_2) for comparative analysis across different modeling strategies. Table 1 systematically compares the performance of three MLP-based modeling strategies evaluated on Test\_2, building upon the 3.1 section's conclusion that MLP constitutes the optimal neural architecture for this task. As established, all three strategies utilize the MLP framework but differ in training paradigms: (1) standalone training on Data\_1 (general molecular database), (2) standalone training on Data\_2 (n = 78 BMI-specific dataset), and (3) the two-stage transfer learning paradigm combining Data\_1 pretraining with Data\_2 finetuning. Specifically, the transfer strategy freezes all layers except the final five during finetuning, which is an optimal knowledge transfer mechanism validated in Section 3.3.

However, despite the initial expectation that Data\_1—a large-scale general polymer dataset—would provide robust predictive capability (as evidenced by its  $R^2$  = 0.59 on internal testing in Section 3.1), the model's performance on BMI-specific Test\_2 plummeted to  $R^2$  = -6.19. This dramatic degradation stems from fundamental domain differences: BMI resins exhibit unique thermal behavior mechanisms distinct from conventional polymers, rendering generic structural patterns in

Data\_1 poorly transferable. While standalone training on Data\_2 (n = 78) might seem a logical alternative, the resulting  $R^2$  = -4.10 and RMSE = 82.15°C reflect inherent limitations: (1) extreme data scarcity prevents learning of meaningful representations, and (2) manual aggregation from heterogeneous literature sources introduces uncontrolled experimental noise, forcing the model to memorize spurious correlations rather than genuine structure-property relationships.

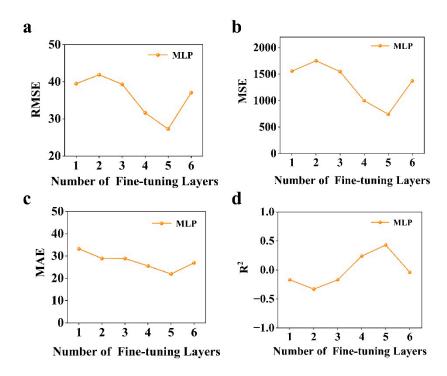
**Table 1.** Performance Comparison of MLP-Based Strategies on Test\_2.

Metrics	Data_1 Standalone	Data_2 Standalone	Transfer Learning (from Data_1 to Data_2)	
RMSE (°C)	97.53	82.15	27.27	
MSE	9512.74	6747.92	743.61	
MAE (°C)	89.49	79.47	21.92	
$\mathbb{R}^2$	-6.19	-4.10	0.44	

Faced with these challenges—Data\_1's domain mismatch and Data\_2's poor quality, the transfer learning framework strategically leverages Data\_1's generalizable physical information as foundational knowledge, while adapting to BMI-specific features through fine-tuning. As shown in Table 1, the transfer learning approach achieved significant improvements in all evaluation metrics. There, MSE measures squared differences between predictions and true values; RMSE represents absolute error magnitude aligned with target variable scale; MAE directly reflects average prediction deviation magnitude. All three metrics follow the "lower the better" principle. R2 evaluates model's explanatory power for data variance, with values closer to 1 indicating better performance, while negative values signify worse performance than baseline mean prediction. When evaluating the three distinct modeling strategies on Test\_2, the transfer learning approach demonstrates superiority across all performance metrics. Notably, transfer learning improves R2 from -6.19 to 0.44 when compared to training on Data\_1 alone, directly demonstrating the framework's ability to correct for domain shift. The RMSE decreases by 72.40% (from 97.53°C to 27.27°C), which indicates a significant improvement in real-world applicability. The results for the Data\_2 standalone training show a negative R<sup>2</sup> (-4.10) and considerable RMSE (82.15°C), indicating that the model is not predicting accurately. The behavior that stems from the model learning spurious correlations rather than true structure-attribute relationships in the small Data\_2 dataset. The transfer learning framework utilizes the structural knowledge in Data\_1 to effectively mitigate this issue, as evidenced by the positive R<sup>2</sup> (0.44) and RMSE (27.27°C) on Test\_2. The consistent performance gains across RMSE, MSE, MAE, and R<sup>2</sup> metrics collectively validate the framework's capacity to mitigate data scarcity limitations in predicting the T<sub>g</sub> of BMI resin.

#### 3.3. Optimizing Transfer Learning Performance Through Layer-Wise Fine-Tuning in MLP Architectures

We explored the impact of varying fine-tuning layer counts on MLP-based transfer learning performance, with a particular focus on identifying the optimal balance between preserving pre-trained knowledge and adapting to target-domain specifics. As shown in Figure 4, each subplot systematically evaluates a critical performance metric—RMSE (4a), MSE (4b), MAE (4c), and R² (4d)—along the vertical axis, while the horizontal axis spans the number of fine-tuned layers (ranging from 1 to 6). Given the MLP architecture comprises 6 layers in total (excluding the input layer and output layer), our experiments systematically unfreeze 1 to 6 consecutive layers from the output end backward, enabling a investigation of adaptation effects.



**Figure 4.** Layer-wise fine-tuning analysis for MLP-based transfer learning: (a) RMSE, (b) MSE, (c) MAE, and (d) R<sup>2</sup> performance trends across 1–6 fine-tuned layers. The MLP architecture comprises 6 layers (excluding input/output layers), with experiments systematically unfreezing 1–6 consecutive layers from the output end. Horizontal axis indicates the number of fine-tuned layers; vertical axes show error metrics (°C units for RMSE/MAE) and coefficient of determination.

The experimental curves reveal a consistent performance evolution pattern across all metrics. Initially, as layers are progressively unfrozen (moving from 1 to 5 layers), model performance improves markedly: RMSE drops to 27.27°C, MSE decreases to 743.61, MAE reduces to 21.92°C, and R² climbs to 0.44. This improvement phase peaks at 5 fine-tuned layers, indicating optimal adaptation where the model sufficiently adjusts higher-level representations for the target domain while retaining pre-trained feature extraction capabilities from the frozen initial layers. Beyond this optimal point, continued layer unfreezing (6 layers) triggers performance deterioration across all metrics. This degradation suggests excessive parameter adjustment may introduce domain-specific noise or disrupt previously learned robust features, negating the benefits of transfer learning.

These observations validate our strategy of adapting the last five layers. Such configuration creates a critical balance: maintaining frozen layers ensures stability in handling high-dimensional molecular data, while funing layers provides necessary flexibility for domain-specific calibration. The resulting pretrained model, trained with this 5-layer fine-tuning approach, represents the optimal intersection of transfer efficiency and adaptive capacity, achieving the highest predictive accuracy without compromising generalization capability.

### 3.4. Feature Interpretability Analysis

According to the 3.3, the layer-wise fine-tuning strategy culminated in the development of Model\_1, an optimized MLP architecture incorporating transfer learning principles that directly enabled the Tg predictions for BMI resins. To comprehensively elucidate the intrinsic physicochemical relationships governing the Tg of BMI resins, we conducted an interpretable machine learning analysis comparing experimental data (Data\_2) and computationally augmented datasets (Data\_3). While Morgan fingerprints excel in capturing structural patterns for predictive modeling, their inherent black-box nature limits physicochemical interpretability. Molecular descriptors, by contrast, encode quantifiable physicochemical properties, enabling direct correlation

analysis between specific structural attributes and  $T_g$ . This rationale motivated our selection of descriptors for interpretable model development.

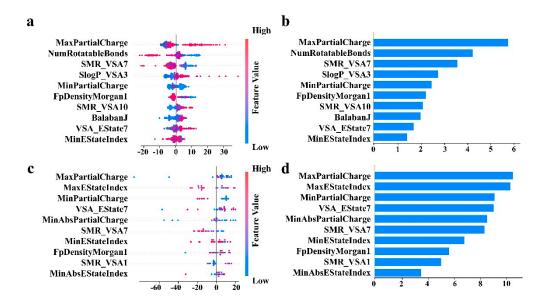
Initially, we attempted to derive interpretable insights directly from Data\_2, but the insufficient data quantity and methodological variability across experimental sources precluded reliable descriptor analysis. To overcome this limitation, we designed 1092 novel BMI structures, then employed Model\_1 to predict their  $T_g$  values, thereby established the Data\_3 dataset. Table 2 presents the quantitative performance metrics of six regression algorithms evaluated on both datasets. Notably, all models exhibited significantly improved predictive capabilities when trained on Data\_3: for instance, the XGBoost model achieved a test set  $R^2$  of 0.63 with RMSE = 17.06°C on Data\_3 compared to  $R^2$  = -1.97 (RMSE = 48.35°C) on Data\_2. This dramatic performance disparity stems from Data\_2's limited sample size (n = 78) and inherent experimental heterogeneity across literature sources, which introduced confounding noise that compromised model generalization.

Table 2. Performace of six interpretable machine learning models on test dataset from Data\_2 and Data\_3.

Model	Dataset	RMSE (°C)	MSE	MAE (°C)	R <sup>2</sup>
RF	Data_2	43.18	1864.35	36.42	-0.81
KF	Data_3	17.32	299.97	12.27	0.62
D: J	Data_2	37.39	1398.15	30.72	-0.36
Ridge	Data_3	21.75	472.98	15.33	0.40
KNN	Data_2	64.09	4107.56	48.96	-2.98
KININ	Data_3	20.45	418.29	13.65	0.47
Parrocian	Data_2	37.39	1397.86	30.33	-0.36
Bayesian	Data_3	21.60	466.51	15.18	0.41
CVD	Data_2	37.02	1370.61	30.39	-0.33
SVR	Data_3	19.07	363.58	13.38	0.54
XGBoost	Data_2	48.35	2337.33	39.91	-1.97
AGD00St	Data_3	17.06	290.98	12.09	0.63

According to the results in Table 2, given the superior performance of XGBoost on Data $_3$  (R<sup>2</sup> = 0.63, RMSE = 17.06°C), this model was selected for SHAP-based descriptor analysis. Figure 5 systematically shows the ordering of the effects and importance of different descriptors on the positive and negative correlations of T<sub>g</sub>. SHAP summary plots (Figure 5a, c) visualize feature contributions via color gradient encoding: red/blue tones indicate high/low feature values, with saturation intensity reflecting predictive impact magnitude. The feature importance ranking (Figure 5b, d) further quantifies the relative contribution of each descriptor, the horizontal coordinate represents the relative value of feature importance, and the vertical coordinate is each descriptor. For Data\_3 (5a, 5b), the most important descriptors including MaxPartialCharge, which represents the maximum partial charge value carried by the atoms in the molecule. The fact that this descriptors rank in the most important indicates that the inhomogeneity of the charge distribution affects Tg. MinPartialCharge, which represents the value of the smallest partial charge carried by an atom in a molecule. The importance ranking of MinPartialCharge is also high, and it works with MaxPartialCharge. A larger difference between the two represents a stronger localized concentration of charge within the molecule, which may lead to stronger electrostatic interactions between the molecules. It can be seen that MaxPartialCharge and MinPartialCharge have an important effect on the T<sub>g</sub> of BMI, however, there is no obvious positive or negative correlation pattern. Besides, one of the most important descriptor is the number of rotatable bonds (NumRotatableBonds), which indicates the number of single bonds in the molecule that can be freely rotated. The molecules with fewer NumRotatableBonds have restricted chain segment mobility, more rigid molecular conformation and higher T<sub>S</sub>. Meanwhile, the specific molecular surface area contribution (SMR\_VSA7) and the specific surface area contribution to the lipid-water partition coefficient (SlogP\_VSA3) also ranked high, indicating that the molecular surface area properties also affect T<sub>8</sub>, probably because

they affect the stacking mode of the molecules and intermolecular interactions, which in turn have an effect on  $T_g$ .



**Figure 5.** Feature role analysis (**a**) SHAP summary plot for training interpretable models on Data\_3, color shades indicate the degree of feature contribution, and red/blue represents the size of feature values; (**b**) feature importance ranking for training interpretable models on Data\_3, horizontal axis is the relative value of feature importance, vertical axis is the feature; (**c**) SHAP summary plot for training interpretable models on Data\_2, color shades indicate the degree of feature contribution, and red/blue represents the size of feature values; (**d**) feature importance ranking for training interpretable models on Data\_2, horizontal axis is the relative value of feature importance, vertical axis is the feature.

In order to verify the authenticity of the analysis results of the virtual data Data\_3, we use Data\_2 to train the XGBoost model for feature significance analysis, and get the results (Figure 5c, 5d) similar to those of Data\_3. Notably, MaxPartialCharge, MinPartialCharge, representing charge inhomogeneity, and SMR\_VSA7, representing molecular surface properties, are still in the top rank, but the model fails to capture the influences such as NumRotatableBonds, representing molecular topological complexity. This is directly related to the small number of data sets.

Two experimentally characterized BMI derivatives (BMI-I and BMI-II) sourced from literature[64–66] were subjected to computational analysis (detailed in Support InformationV). The Model\_1 predictions yielded  $T_g$  values of 263.75°C and 323.03°C for BMI-I and BMI-II respectively, demonstrating exceptional agreement with the literature-reported experimental values of 260°C and 300°C (errors  $\leq$ 3.75°C and  $\leq$ 7.67% relative deviation). Concomitant calculation of molecular descriptors revealed that while most topological parameters remained consistent between the two systems, the NumRotatableBonds metric exhibited a marked difference (22 and 16 bonds), inversely correlating with measured  $T_g$ . This experimental and model compared analysis not only validates the Model\_1's predictive accuracy but also reinforces the structural complexity- $T_g$  relationship posited by the interpretable framework, as reduced molecular flexibility (lower NumRotatableBonds) directly corresponds to evaluate  $T_g$ , thereby substantiating molecular topology as a critical determinant influencing  $T_g$ .

#### 4. Conclusion

The hybrid framework proposed in this study integrates transfer learning and interpretable machine learning to successfully achieve efficient prediction of BMI resin  $T_g$ . Through SHAP analysis, this study elucidates the core mechanism of molecular descriptors' influence on  $T_g$ . Specifically,

topological complexity (represented by NumRotatableBonds), charge distribution properties (represented by MaxPartialCharge and MinAbsPartialCharge), and molecular surface properties (SMR\_VSA7 and SlogP\_VSA3) are identified as the dominant influencing  $T_g$  factors. This success can be attributed to the effective transfer of chemical spatial knowledge through transfer learning and the explicit resolution of higher-order interactions through SHAP analysis. Additionally, Ten possible higher  $T_g$  structures are given based on the predictions of the discriminator model (Support InformationVI).

However, the study acknowledges certain limitations, particularly the exclusion of external variables such as processing parameters, which may affect the model's generalizability under varying processing condition[64–66]. Future research could extend this work by incorporating processing parameters and molecular characteristics to comprehensively reveal the multi-scale regulation mechanisms of T<sub>g</sub>, further advancing the field of high-temperature-resistant polymer design with both predictive accuracy and mechanistic transparency.

**Supplementary Materials:** The following supporting information can be downloaded at the website of this paper posted on Preprints.org. The detailed datasets of these models can be found at https://doi.org/10.5281/zenodo.15481912.

**Author Contributions:** Conceptualization, Z.W. and J.Z.; methodology, Y.L.; software, P.K.; validation, Z.W., Z.L. and P.K.; formal analysis, Z.W.; investigation, J.Z.; resources, Y.L.; data curation, X.X.; writing—original draft preparation, Z.W.; writing—review and editing, P.K.; visualization, Z.W.; supervision, P.K.; project administration, L.Z.; funding acquisition, Y.L.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Data Availability Statement: The data are available from the authors upon request.

Conflicts of Interest: The authors declare no conflicts of interest.

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