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Article

The Common Concept of Anticooperativity Among Molecules is Fundamentally Flawed. Conclusion Arrived at from the Novel and Unified Molecular-Wide and Electron Density (MOWeD)-Based All-Body Concept of Chemical Bonding

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Abstract: A non-linear (non-additive) increase in stability of hexamers follows an increase in the total number of (i) **aad** (a double proton acceptor) plus **add** (a double proton donor) waters commonly linked with anticooperativity and (ii) the total number of intermolecularly delocalized electrons (${}^{\text{intermol}}N^{\text{deloc}}$) in the 3D space occupied by a hexamer. Subsequently, we obtained nearly a perfect linear correlation between increase in the cluster stability and ${}^{\text{intermol}}N^{\text{deloc}}$. Individual water molecules that act as either **aad** or **add**: (i) delocalize the largest number of electrons throughout a cluster; (ii) are involved in the strongest attractive, hence energy-stabilizing intermolecular interaction with the remaining five waters; (iii) have the most significant quantum component of the intermolecular interaction energy and (iv) relative to six non-interacting water molecules, stabilize a hexamer the most, as quantified by a purposely derived *mol*-FAMSEC energy term. Clearly, the **all-body** approach used in the unified, molecular-wide and electron density (MOWeD)-based concept of chemical bonding contradicts the commonly accepted view that **aad** and **add** water molecules are involved in anticooperativity in 3D water hexamers. Consequently, we propose here a general definition of cooperativity that should be applicable to any *n*-membered molecular clusters, namely: *the quantifiable, physics- and quantum-based cooperativity phenomenon is synonymous with the intermolecular all-body delocalization of electrons leading to the increase in stability of individual molecules on an n-membered cluster formation.*

Keywords: cooperativity; anticooperativity; water clusters; molecular-wide and electron density (MOWeD)-based approach; the Fragment; Atomic; Localized; Delocalized and Interatomic (FALDI)-based electron density decomposition scheme; the Fragment Attributed Molecular System Energy Change (FAMSEC)-based method

1. Introduction

Water clusters and, in particular, non-additivity in strength and other properties of intermolecular H-bonds have been studied for many decades by exploring underlying processes coined as cooperativity [1–25] and anticooperativity [26–35] between water molecules. Actually, interest in properties of water clusters continues to date due to importance of water in, e.g., supporting life, and a few very informative reviews were published on cooperativity in water clusters [9,10,17,20,36–38]. Considering anticooperativity, this concept was introduced well after

cooperativity and it is always investigated and discussed in conjunction with cooperativity. Although it is not a subject of this contribution, it is important to stress that the concepts of cooperativity/anticooperativity are also explored in many different kinds of molecular clusters where individual molecules are involved in intermolecular H-bonding [29,39–46].

When water chains or cyclic homodromic structures are formed then all water molecules are of **ad** character, i.e., being arranged in the (proton acceptor, **a**)-(proton donor, **d**) configuration, $\cdots\text{O}-\text{H}\cdots\text{O}-\text{H}\cdots\text{O}-\text{H}\cdots$. For the **ad** configurations of water molecules in clusters, non-additivity presents itself as mutual enhancement of H-bonds leading to the binding energy being greater than that computed for a dimer. The process of the enhancement of bonding (binding energy) was named 'cooperativity' between water molecules [1].

Ojamäe and Hermansson [20] have arranged four water molecules in the form of tetrahedron using dimers as building blocks. This resulted in the central water molecule acting as a double proton acceptor (**aa**) and a double proton donor (**dd**) meaning that the central water molecule in the tetrahedron had **aadd** functionality. Using OH frequencies computed for tetrahedron, they have concluded that the **aadd** configuration works in the opposite direction when compared with a single acceptor-single donor **ad** waters in chains or homodromic pentamer. Such non-additivity that diminishes bonding typically is described as "anticooperativity" but it is clear that they were not in favor of this nomenclature. Instead, they have proposed a concept of 'strict cooperativity' that, according to them, is indisputably observed for the energies and the frequencies in chains and homodromic water pentamer (in general, in cyclic homodromic water clusters). Finally, they have concluded that '*Water molecules in a tetrahedral coordination display cooperativity, but not strict cooperativity*' [20]. Steiner stressed that, because hydrogen bonds may not only enhance, but also reduce the strengths of each other, a change of orientation of H-bonds from homodromic to antidromic arrangement leads to *local anticooperativity* [36].

Intuitively, the concept of cooperativity among water molecules can be understood as contributions made by 2-, 3-, (many-) body energy terms that enhance the strength of H-bonds in water clusters. Realizing that the same Physics and Quantum Chemical rules apply to all possible sizes and shapes of water clusters, it is difficult to explain the concept of anticooperativity. To this effect, how water molecules 'decide' on the mode of action, either enhancing or diminishing bonding using the same 2-, 3-, n -body energy terms? One must realize that neither cooperativity nor anticooperativity are well-defined quantum properties but rather are used to loosely describe 'positive' or 'negative' additivity of energy terms on a cluster formation.

Recently [47], using the **all-body** and molecular-wide and electron density (MOWeD)-based approach [48], we proposed a new and quantifiable concept of cooperativity. According to our recent interpretation, the origin of **all-body** cooperativity is rooted in physics- and quantum-based processes of electron (e) delocalization between water molecules. In other words, cooperativity is the intermolecular **all-body** e -delocalization leading to the non-additive increase in stability of a water molecule in clusters with an increase in their size.

Cooperativity is defined in Oxford dictionary as "involving doing something together or working together with others toward a shared aim. Cooperative activity is essential to effective community work." Remarkably, the Oxford definition of cooperativity agrees very well with our definition of cooperativity among molecules, namely:

- a) Intermolecular e -delocalization by water molecules in a cluster can be interpreted as equivalent to *doing something together or working together with others* from Oxford dictionary definition of cooperativity, and
- b) Reaching the lowest e -energy of a water cluster through intermolecular e -delocalization (from our definition) compares well with *Cooperative activity is essential to effective community work to achieve a shared aim* as per Oxford dictionary definition.

On the other hand, Oxford dictionary does not provide a definition of anticooperativity. In other words, neither anti-cooperativity nor anticooperativity exist in this dictionary. This might imply that people and, more relevant to this work water molecules, cannot be involved in activity (a physical

process) called anticooperativity. This supposition can be written as the following hypothesis that constitutes the focus of the present contribution.

Hypothesis-1.

From the fact that:

1. 3D 6-water clusters discussed in this work are more stable than 2D cyclic homodromic water hexamer and the latter is restricted to **ad** configurations showing only positive, non-additivity in the strength of H-bonds, i.e., classical cooperativity, and
2. Prism, being the most stable 3D 6-water hexamer, does not have water molecules of **ad** configurations (there are 3 **aad** and 3 **add** waters)

*it would follow that the double-acceptor (**aad**) and double-donor (**add**) water molecules must contribute to cluster stability more than **ad** configuration.*

If the above hypothesis holds, then the anticooperativity cannot be supported and hence must be rejected. 3D 6-water clusters (bag, book, cage, and prism) are used here as model systems as they all:

- i. Are more stable than the 6-water cyclic hexamer; notably, they are the smallest 3D clusters that are more stable than their cyclic counterparts, and
- ii. Have water molecules with **aad** and **add** configurations and these motifs are observed in each of the ice polymorphs [2].

One must stress that the **all-body** MOWeD-based protocol treats all atoms as a constellation of nuclei that spontaneously drive electron density (ED) to the global minimum of electronic energy of a molecular system. This approach is in accord with Bader's view that there are '*only two forces operative in chemistry, the Feynman force exerted on the nuclei and the Ehrenfest force exerted on the electrons*' [49]

To probe the above hypothesis, we will make use of recently developed tools incorporated in the all-body MOWeD-based approach that will provide qualitative and quantitative interpretation of cooperativity/anticooperativity, namely:

- i. The Fragment, Atomic, Localized, Delocalized and Interatomic (FALDI)-based electron density decomposition scheme [50–52]. FALDI meets the all-body requirement perfectly as it treats atoms' and atom-pairs' *e*-distributions holistically over the entire 3D space occupied by a molecular system.
- ii. The Fragment Attributed Molecular System Energy Change (FAMSEC) family of methods [53,54] is used to identify molecular fragments that either drive or obstruct a chemical change the most. FAMSEC also meets the all-body requirements as the quantified energy contributions made by fragments are harvested from entire space occupied by a system.

2. Computational Methods

All calculations were performed in Gaussian 09 Rev. D.01 [55] in the gas phase with a keyword 'opt=verytight' at the B3LYP level of theory with Grimme's [56] empirical correction for dispersion using a keyword 'empiricaldispersion=GD3'. The Dunning triple zeta basis set, aug-cc-pVTZ, which is augmented by diffuse functions, was used throughout. Coordinates of all optimized structures are given in the Supplementary Materials. Frequency calculations were performed for the optimized structures to verify that no imaginary frequency was present. Topological, QTAIM [57] molecular graphs, atomic overlap matrices and IQA [58,59] calculations were performed in AIMAll [60] using B3LYP-generated wavefunctions. The IQA energy terms, and interaction energies in particular, were found to be highly comparable to those obtained at the CCSD/BBC1 level [61]. FAMSEC and FALDI data were calculated using in-house software, and FALDI isosurfaces were visualized using VMD [62]. FALDI codes were incorporated in MOWeD-LAC (molecular-wide electron delocalization and localization atomic counts) and MOWeD-LFC (molecular-wide electron delocalization and localization fragment counts) applications; these two applications are made freely available [63].

3. Theoretical Background

3.1. The FALDI Density Decomposition Scheme

FALDI is a unique electron density decomposition scheme developed recently [50–52]. Usefulness and power of FALDI was already demonstrated in the study of numerous bonding and non-bonding interactions in a number of systems [48,50–52,64–67]. It is unique because one can compute, besides classical electron populations, the **exact** localization and **exact** delocalization electron counts that are quite different from localization and delocalization indices generated within the QTAIM formalism [57]. Another unique and very instructive feature of FALDI is its ability to generate 3D distributions of localization and delocalization patterns that can be visualized in real-space.

In this contribution, we will focus on useful aspects of FALDI that are directly applicable in the study of cooperativity and anticooperativity in 3D water clusters. Readers interested in full theoretical description of FALDI are referred to our recently published work [47] and references therein.

FALDI-based electron density (ED) decomposition scheme provides (i) *atom*-ED distribution, (ii) the contribution made by electrons localized to a selected atomic basin Ω_A , i.e. *loc*-ED distribution, and (iii) the contribution made by electrons delocalized between all unique basin-pairs (Ω_A, Ω_B), i.e., *deloc*-ED distribution. All these distributions are additive and can be conveniently combined to form fragment $\mathcal{F}$ distributions by accounting for selected atomic basins' contributions. From this follows that the total electron population of a k -atom fragment, e.g., 3-atom fragment of a molecular system, such as a water molecule $\mathcal{W}$ in a cluster, $N^{\text{total}}(\mathcal{W})$, can be decomposed as:

$$N^{\text{total}}(\mathcal{W}) = N^{\text{self}}(\mathcal{W}) + N^{\text{deloc}}(\mathcal{W}, \mathcal{R}) \quad (1)$$

where the fragment's electron population is made of two components, namely electrons that can be found only in the space occupied by a water molecule $\mathcal{W}$ - this count is called a 'self'-fragment electron population, $N^{\text{self}}(\mathcal{W})$, and electrons delocalized with the remaining five water molecules in a cluster treated as a fragment $\mathcal{R}$, $N^{\text{deloc}}(\mathcal{W}, \mathcal{R})$. It is important to realize that in the case of multi-atom fragments, such as water molecule, the 'self' fragment electron population $N^{\text{self}}(\mathcal{W})$ is made of two kinds of electrons: a) electrons localized to each atom A , $N^{\text{loc}}(A)$ of a water molecule treated as a fragment $\mathcal{W}$. Hence, for all atom-localized electrons in a water molecule we can write $N^{\text{loc}}(\mathcal{W}) = \sum N^{\text{loc}}(A)$ where $A \in \mathcal{W}$, and b) electrons delocalized amongst atoms of the fragment $\mathcal{W}$ due to intra-fragment delocalization processes taking place, $N^{\text{deloc}}(\mathcal{W}, \mathcal{W})$. Notably, the two delocalization terms, $N^{\text{deloc}}(\mathcal{W}, \mathcal{W})$ and $N^{\text{deloc}}(\mathcal{W}, \mathcal{R})$, are fundamentally different as the latter represents inter-fragment electron delocalization and it counts electrons that can be found in both fragments, $\mathcal{W}$ and $\mathcal{R}$. The term $N^{\text{deloc}}(\mathcal{W}, \mathcal{R})$, is calculated by summing up only the contributions made by atoms within the k -atom (here 3-atom) fragment $\mathcal{W}$ to diatomic DIs involving all other atoms in the molecular system (here water cluster):

$$N^{\text{deloc}}(\mathcal{W}, \mathcal{R}) = \sum_{A \in \mathcal{W}} \sum_{B \in \mathcal{R}}^k \sum^{n-k} A^{\text{DI}}(A, B) \quad (2)$$

3D placement of water molecules in each cluster is unique meaning that each water molecule $\mathcal{W}$ finds itself in a different molecular environment. This, in turn, must have an impact on the number of electrons each $\mathcal{W}$ is delocalizing to the remaining waters in a cluster. Due to additivity of FALDI-computed terms, one can compute the total number of delocalized electrons in each cluster by summing up the $N^{\text{deloc}}(\mathcal{W}, \mathcal{R})$ terms obtained for individual water molecules.

It might be very useful and informative to investigate electron delocalization patterns throughout a molecular system by computing delocalized electrons counts between molecular fragments. As an example, for the k -atom fragment $\mathcal{F}$ and l -atom fragment $\mathcal{H}$ we can write

$$\text{DI}(\mathcal{F}, \mathcal{H}) = \sum_{A \in \mathcal{F}} \sum_{B \in \mathcal{H}}^l \text{DI}(A, B) \quad (3)$$

where contributions made by individual atoms are accounted for, as $\text{DI}(A, B) = {}^A\text{DI}(A, B) + {}^B\text{DI}(A, B)$. Notably, $\text{DI}(\mathcal{F}, \mathcal{H}) = N^{\text{deloc}}(\mathcal{F}, \mathcal{H}) + N^{\text{deloc}}(\mathcal{H}, \mathcal{F})$ and, in most cases, $N^{\text{deloc}}(\mathcal{F}, \mathcal{H}) \neq N^{\text{deloc}}(\mathcal{H}, \mathcal{F})$. This means that $N^{\text{deloc}}(\mathcal{F}, \mathcal{H})$ measures the degree to which electrons from the k -atom fragment $\mathcal{F}$ are delocalized within the l -atom fragment $\mathcal{H}$. By analogy, similar applies to the $N^{\text{deloc}}(\mathcal{H}, \mathcal{F})$ term. On the other hand, $\text{DI}(\mathcal{F}, \mathcal{H})$ measures the total electron count due to delocalization of electrons between atoms of both fragments, i.e., the count of electrons **shared** by the two fragments. Naturally, Eq. 3 is useful to compute the total number of electrons shared by any water-pair in a cluster.

3.2. A Fragment Attributed Molecular System Energy Change (FAMSEC) Protocol

Many molecules, e.g., polyamines, show an incredible flexibility and are able to re-arrange their constellations of nuclei and change the associated electron density distribution in 3D space spontaneously leading to a large number of structural conformers of the same molecule. This can be seen as an intramolecular event. Moreover, many molecules can re-arrange their relative placement in 3D space leading to a countless number of molecular clusters, such as water clusters. This can be seen as intermolecular event. However, what drives a change and what is the energy contribution made by specific atoms, molecular fragments, etc. when a molecular system undergoes a change from its initial (*init*) to a final (*fin*) state? From a need of understanding and quantifying changes taking place throughout a molecular system on a chemical event, the concept of FAMSEC [53] was born.

Complex chemical events take place along the reaction energy profile (REP). A dedicated REP-FAMSEC protocol was designed [54] to explore a reaction mechanism leading to new chemical products. The FAMSEC method [53] and its 'derivatives', namely REP-FAMSEC [54,68,69] and π -FARMS (Preorganized-Interacting (π) Fragments Attributed to Relative Molecular Stability [70,71]), pinpoint n -atom molecular fragments $\mathcal{G}$ (a molecule might also be treated as $\mathcal{G}$) that drive/obstruct a chemical change the most and were also employed to investigate non-covalent interactions in a number of systems [72,73].

Many energy terms can be defined within the FAMSEC method and its derivatives that make use of the exhaustive energy partitioning schemes implemented in QTAIM [57] and IQA [58,59] where entire molecular space is occupied by atoms without voids between them. This assures that harvesting of data from all corners of a molecular system, as required by the MOWeD-based approach, can be met. Making use of the IQA-defined principle energy components of a molecular system, the *mol*-FAMSEC term was designed to quantify energy contribution made by any n -atom fragment $\mathcal{G}$ on a chemical event. To account for molecular-wide contributions made by all atoms of a molecular system, the *mol*-FAMSEC term is defined as:

$$\text{mol-FAMSEC} = \Delta E_{\text{self}}^{\mathcal{G}} + \Delta E_{\text{int}}^{\mathcal{G}} + \Delta E_{\text{int}}^{\mathcal{G}, \mathcal{R}} \quad (4)$$

The first two terms in Eq. (4) constitute the *loc*-FAMSEC = $\Delta E_{\text{self}}^{\mathcal{G}} + \Delta E_{\text{int}}^{\mathcal{G}}$ term that quantifies energy change that is localized (*loc*) to the 3D space occupied by n -atoms of a selected molecular fragment $\mathcal{G}$. This involves a) a change in self-atomic energies of atoms constituting $\mathcal{G}$ ($\Delta E_{\text{self}}^{\mathcal{G}}$) and b) the change in all unique intra-fragment diatomic interaction energies, i.e. the $\Delta E_{\text{int}}^{\mathcal{G}}$ term, on the transformation of a molecular system from the initial (*init*) to final (*fin*) state. The last term in Eq. (4), $\Delta E_{\text{int}}^{\mathcal{G}, \mathcal{R}}$, accounts for changes in the strength of all diatomic interactions between atoms of $\mathcal{G}$ and all remaining atoms treated as a molecular fragment $\mathcal{R}$. Finally, it is important to stress that all terms in Eq. (4) quantify a specific energy contribution to the electronic energy of a molecular system on the *init* $\rightarrow$ *fin* chemical event.

4. Results and Discussion

Water clusters used to study cooperativity/anticooperativity are shown in Figure 1. Each water molecule is considered as a 3-atom molecular fragment of a 6-membered water cluster named as W_n -**mode** where '**mode**' stands for either **ad**, **aad** or **add** mode of action (functionality) a water molecule is involved in. Moreover, each 3-atom fragment representing a classical intermolecular H-bond is denoted as $H\mathcal{B}$ - n . All energy terms were computed using non-interacting separate water molecules that served as a reference state throughout the entire investigation.

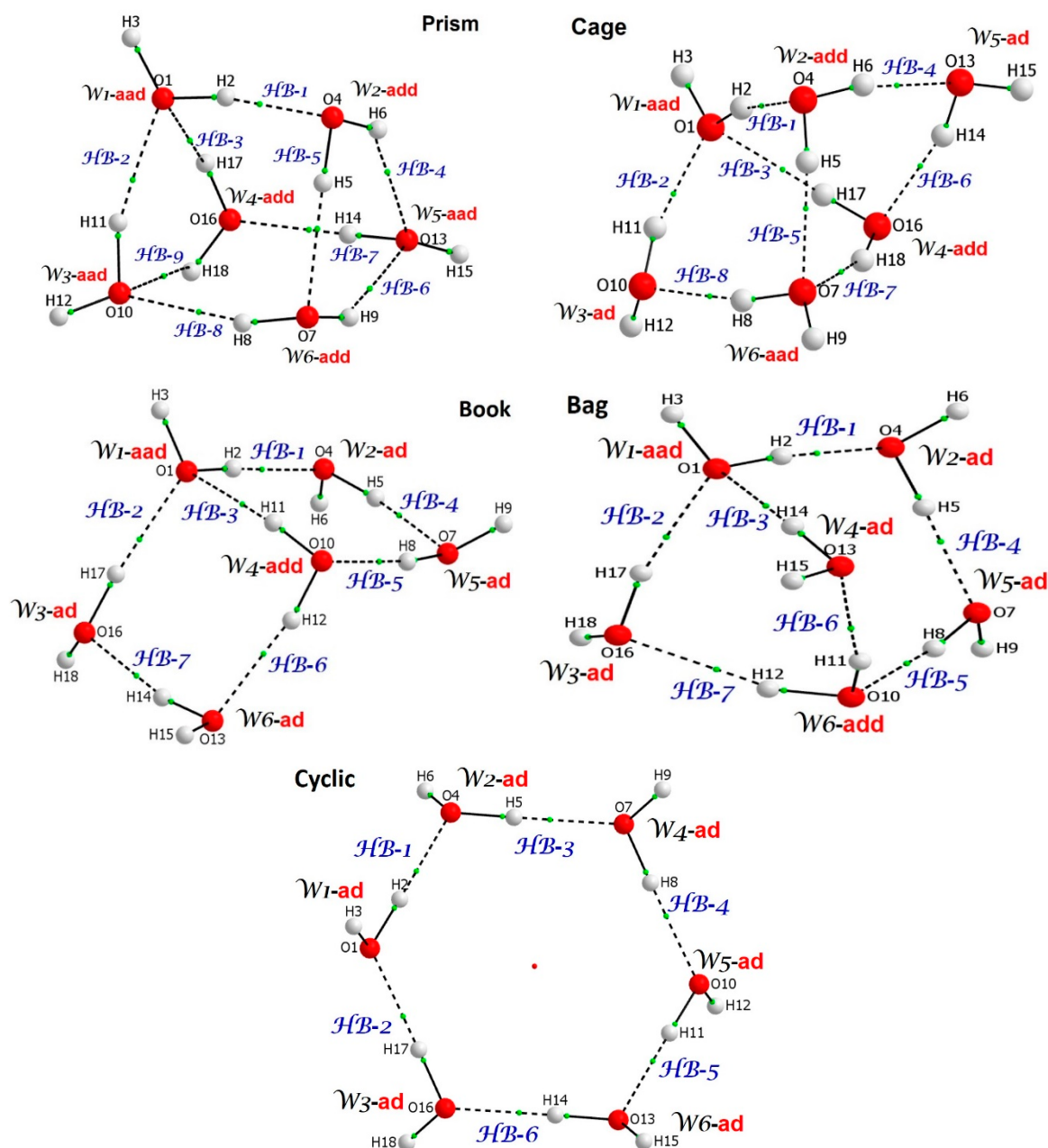


Figure 1. Molecular graphs of water hexamers investigated in this work showing atoms' numbering, numbering of water molecules (W_n) and numbering of hydrogen bonds ($H\mathcal{B}$ - n). Functionality of water molecules, in terms of accepting (a) or donating (d) a proton, is also indicated.

4.1. Validation of B3LYP-Computed Relative Stabilities of Water Hexamers

3D density distribution varies with the level of theory to some degree; hence, somewhat different electronic energies (e -energies) are expected for each cluster. Our focus, however, is on trends in values of relative electronic energies of hexamers under investigation. As exemplified by the data in

Table 1, the relative energies ($\Delta E = E(\text{hexamer}) - E(\text{prism})$) computed at a very high level of theory, namely CCSD(T)/CBS [74], compare very well with data obtained at somewhat lower levels, e.g., MP2(full)/aug-cc-pVTZ [75] and CCSD(T)/aug-cc-pVTZ [76].

Table 1. Comparison of the relative energies, as $\Delta E = E(\text{hexamer}) - E(\text{prism})$ values in kcal/mol, obtained at different levels of theory for the indicated water hexamers.

Source	Level of theory	$\Delta E = E(\text{hexamer}) - E(\text{prism})$ in kcal/mol				
		Cyclic	Bag	Book	Cage	Prism
Our data	B3LYP/aug-cc-pVTZ/GD3	2.15	1.34	0.80	0.25	0
Bates <i>et al</i> [74]	CCSD(T)/CBS	2.48	1.62	0.87	0.25	0
Kryachko [75]	MP2(full)/aug-cc-pVDZ	2.06	N/A	1.16	0.25	0
Olson <i>et al</i> [76]	CCSD(T)/aug-cc-pVTZ	2.10	N/A	1.20	0.30	0

Most importantly, however, ΔE values computed at the significantly lower level used in our studies, i.e., at the B3LYP/aug-cc-pVTZ level with the empirical GD3 Grimme's dispersion correction, follow exactly the same trend as obtained at the higher levels – Figure 2.

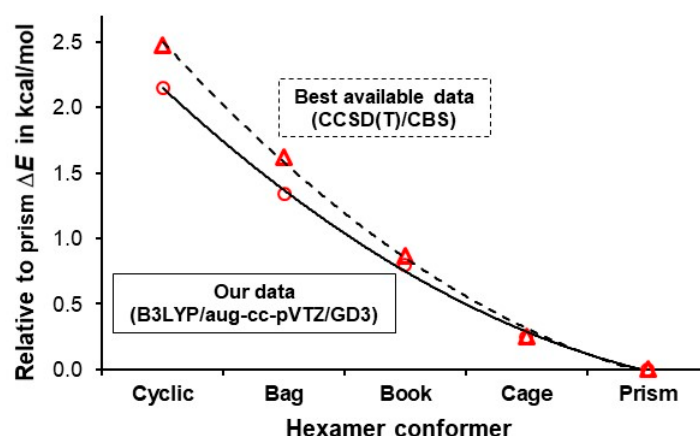


Figure 2. Trends in relative stability of hexamers obtained at the B3LYP/aug-cc-pVTZ/GD3 level of theory employed in this work (circles with the solid trend line) and best available data (triangles with the dashed trend line) obtained at the CCSD(T)/CBS level. $\Delta E = E(\text{hexamer}) - E(\text{prism})$.

One can also see that our ΔE values differ from those obtained at the higher levels by a small fraction of kcal/mol – see Table 1 and Figure 2. From that, we conclude that the FALDI- and FAMSEC-based analyses performed on optimized in this work hexamers should provide scientifically sound and highly reliable pictures and conclusions.

4.2. A Cooperativity-Driven Decrease in $E(\text{hexamer})$ Relative to $E(6\text{H}_2\text{O})$

Regardless of a chemical system considered, classical interactions and quantum effects involving all atoms govern a relative 3D placement of atoms. This means that the universal laws of Classical and Quantum Physics/Chemistry will spontaneously drive the placement of nuclei and associated distribution of ED that is characteristic for local/global electronic energy minima. Clearly, these are **all-body** processes leading to a unique constellations of atoms constituting a molecular system at each energy minimum on the potential energy hypersurface. Each constellation of nuclei generates a specific, like a fingerprint, 3D ED distribution from which all the properties of a molecular system can be derived as stressed already over a half of century ago by Hohenberg and Kohn [77], more recently by Bader [57] and in the very recent review by Koch *et al* [78].

From the above it follows that the electronic energy E of a molecular system and its fragments, like water molecules constituting a water cluster, as well as some components of E can be used to

explore physical/quantum properties leading to or linked with cooperativity or anticooperativity using the MOWeD-based approach. Recently [47], we have postulated that a non-linear increase in the stability of a water molecule, i.e., a non-linear decrease in E of a statistical water molecule with an incremental increase in the number

of water molecules in homodromic rings can be used to quantify *cooperativity phenomenon* taking place in cyclic water clusters. It is evident that our definition of cooperativity phenomenon [47], i.e., 'the intermolecular **all-body** e -delocalization leading to the non-additive increase in stability of a water molecule in clusters with an increase in their size' cannot be applied directly to clusters studied here because all of them are 6-membered 3D structures. However, it can be re-written to a more general form, namely: *the cooperativity phenomenon is synonymous with the intermolecular **all-body** e -delocalization leading to the increase in stability of water molecules on a cluster formation.*

From the above it follows that an n -membered water cluster should have lower electronic energy when compared with separate (non-interacting) n water molecules. A trend in Figure 3 shows that (i) all hexamers have much lower energy than six non-interacting water molecules and (ii) all 3D hexamers are more stable than the cyclic homodromic ring. Moreover, a non-linear decrease in electronic energy reaches a minimum value for the prism and this strongly suggests that the cooperativity phenomenon is strongest in this hexamer.

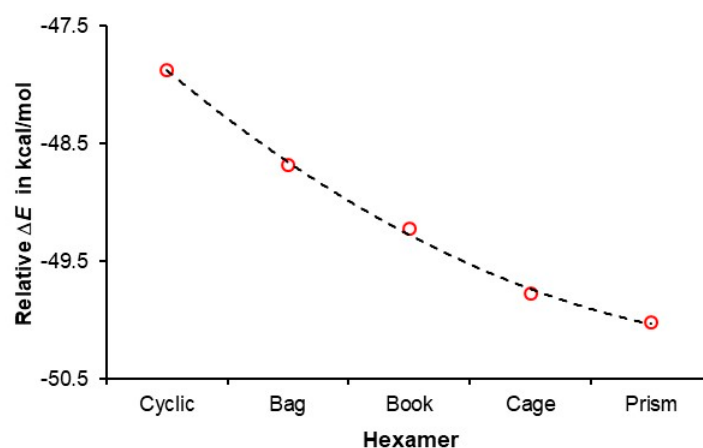


Figure 3. Relative to six free, non-interacting water molecule, an increase in the stability of indicated water hexamers. $\Delta E = E(\text{hexamer}) - E(6\text{H}_2\text{O})$.

It is accepted for decades that the double functionality of water molecules (**aad** and **add**) implies that they are involved in anticooperativity. A change in the electronic energy of a 6-membered water cluster with the total number of double acceptors and donors is shown in Figure 4. Remarkably, the trend seen in Figure 4 is a 'copy' of that seen in Figure 3 and it strongly suggests that the larger number of water molecules acting as double donor/double acceptor the more significant cooperativity among water molecules. The combined trends in Figures 3 and 4 provide the first (i) support for our hypothesis-1 stated in the Introduction and (ii) evidence against the concept of anticooperativity as all water molecules in prism act as either double acceptor or double donor.

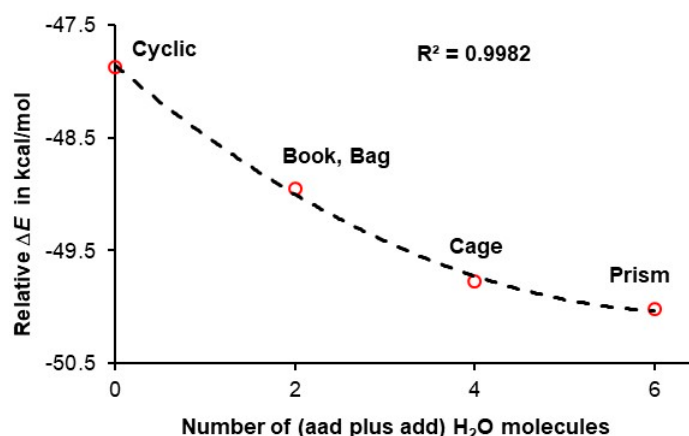


Figure 4. Relative to six non-interacting water molecules, an increase in the stability of indicated hexamers with an increase in the number of double-acceptor and double-donor water molecules in a cluster. $\Delta E = E(\text{hexamer}) - E(6\text{H}_2\text{O})$.

4.3. Quantifying Cooperativity

Considering our definition of cooperativity and looking at the data presented in Figures 3 and 4 leads us to the second hypothesis that, if confirmed, would not only support our initial hypothesis but also would provide quantified explanation on how double acceptor/donor molecules stabilize clusters more than water molecules with **ad** functionality.

Hypothesis-2

*Water molecules acting as double-donor (**add**) and double-acceptor (**aad**) must delocalize a larger number of electrons throughout a cluster than **ad** water molecules and this makes the 6-membered 3D clusters more stable than the homodromic cyclic hexamer.*

To test our **hypothesis-2**, we make use of the FALDI-defined electron delocalization indices. To gain a full description without any presumptions made, all-body contributions made to the total final property of a system by all water molecules and each atom are accounted for. Recall that FALDI expands the concept of ED sharing to entire 3D space occupied by a molecular system, such as a water cluster, and delocalization indices can be computed for all atom-pairs, atoms as well as any molecular fragment.

It is important to realize that, due to very different distribution of water molecules in 3D hexamers, each water molecule finds itself in a unique environment that must have an impact on the number of delocalized electrons. To this effect, the bag and book clusters have one **aad**, one **add** and four **ad** water molecules. Even though the number of water molecules with a specific functionality is the same, we noted that the number of intermolecularly delocalized electrons $^{\text{intermol}}N_{\text{deloc}}$ computed for **aad** (2.188e) and **add** (2.075e) waters in bag is slightly larger than in the book hexamer (2.100 and 2.048e, respectively). Also, the number of delocalized electrons by **aad** configuration appeared to be slightly larger than that by the **add** configuration in the Cage hexamer.

To account for the impact of the molecular environment and realizing that we are dealing with rather a small sample of hexamers (a total number of 80 conformers was reported by Xantheas [19]), we decided to compute the average number of $^{\text{intermol}}N_{\text{deloc}}$ for each **ad**, **aad** and **add** functionality observed in 3D hexamers studied here. We found that, on average, **ad**, **aad** and **add** water molecules in the 3D hexamers delocalize 1.54 ± 0.12 , 2.00 ± 0.18 and $1.98 \pm 0.12e$, respectively. These results show that statistically:

- (i) The number of delocalized electrons by **ad** waters in 3D hexamers examined is the same as found for cyclic hexamer for which $^{\text{intermol}}N_{\text{deloc}} = 1.557 \pm 0.001e$ [47],

- (ii) The difference in $\text{intermol}N_{\text{deloc}}$ between **aad** and **add** waters in 3D hexamers is insignificant and, the most importantly,
- (iii) There is a very significant difference in the number of delocalized electrons between **ad** and double-acceptor **aad** and double-donor **add** waters with **ad** delocalizing about $0.45e$ less.

Data seen in Figure 5 shows a non-linear, asymptotic increase in the total number of delocalized by all six water molecules electrons throughout a cluster, from the smallest value found in the cyclic 2D homodromic structure where only **ad** water molecules are present to the largest value computed for prism where there are no **ad** molecules. The impact of double functionality (**aad**/**add**) is instantly noticeable as a large increase, by over $1e$, is observed already in bag and book where only two **ad** waters are replaced by a pair of **aad** and **add** molecules.

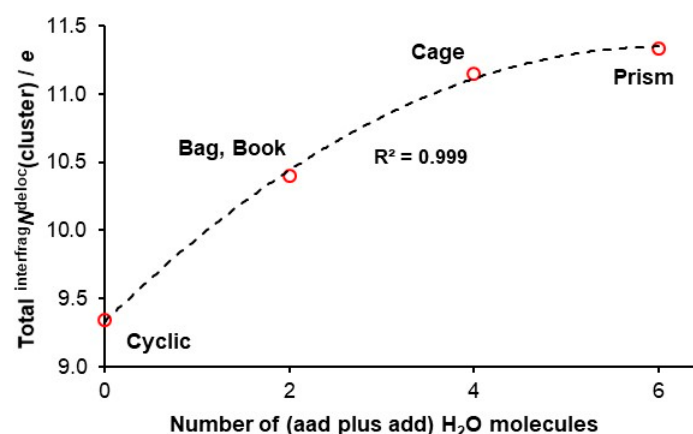


Figure 5. The trend in the total number of electrons intermolecularly delocalized by all water molecules in a cluster and the number of **aad** plus **add** water molecules in a cluster. Regression for the fitted data (dashed line) is also indicated.

There is a striking ‘similarity’ between the trends seen in Figures 4 and 5, where (i) in Figure 4 an asymptotic decrease in electronic energy of hexamers with the number of water molecules having **aad** plus **add** functionality is presented, and (ii) in Figure 5 where asymptotic increase in the number of the total $\text{intermol}N_{\text{deloc}}$ with the number of waters having double functionality is seen. These asymptotic trends, having similar shape but going in the opposite directions, suggests that there should be a direct link between clusters’ stability and the total number of delocalized electrons throughout the cluster. Indeed, an excellent linear correlation is observed in Figure 6 showing that the least stable cyclic structure has the smallest number of e -delocalized and just opposite is observed for the lowest energy hexamer, prism. Clearly, **aad** and **add** waters cooperate more (delocalize more electrons) and hence stabilize clusters more (decrease their electronic energy more) and this is in a strong support of our two hypotheses.

We would like to conclude this section by stating that, from the MOWeD-based perspective, our findings contradict decades-old concept of the **aad** and **add** functionality being involved in the anticooperativity when electronic stabilization of entire water clusters goes. It is then reasonable to consider a significant increase in the total number of electrons delocalized by all water molecule throughout the space occupied by 3D clusters as a principal driver and quantifiable measure of cooperativity as we already stipulated for the 2D cyclic clusters [47].

Finally, one might argue that the total number of delocalized electrons does not provide an insight on individual water contributions with different functionalities. One might ask, for instance, if it is possible that, in a specific cluster, **ad** water molecule is delocalizing more electrons than either **aad** or **add** waters believed to be involved in anticooperativity? To address this, relevant data is presented in Table 2 where the number of electrons intermolecularly delocalized by each individual

water molecule to the remaining five waters is presented – for brevity it is shown as N_{deloc} in Table 2 where, for convenience, functionality of each water and its number (as in Figure 1) are also included.

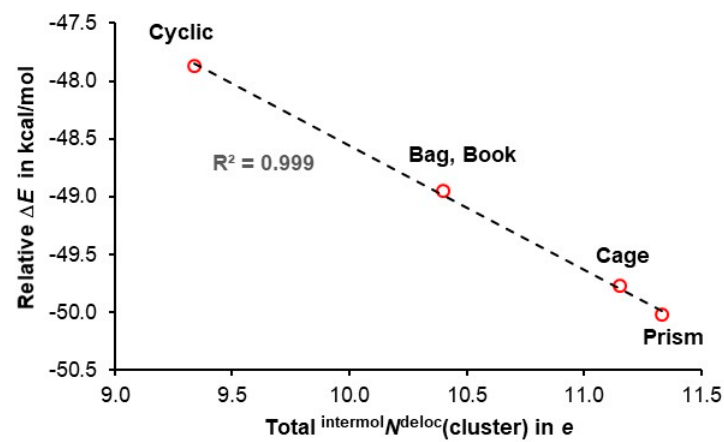


Figure 6. Relative to E of six non-interacting water molecules, the trend in the decrease in $E(\text{cluster})$ plotted vs. the total number of electrons intermolecularly delocalized by all water molecules in the indicated hexamers. Regression for the fitted data (dashed line) is also indicated.

The impact of an immediate environment on $\text{intermol}N_{\text{deloc}}$ is immediately seen in Table 2. For instance, $\text{intermol}N_{\text{deloc}}$ varies between 2.11 and 1.78e in reasonably symmetrical structure of prism where, in addition, there are no **ad** waters. A large spread of delocalized electrons by **ad** molecules is also seen for book (from 1.65 to 1.41e) and bag (from 1.72 to 1.41e) structures. Fundamentally important, however, is the finding that the **aad** and **add** water molecules in either cage, book, or bag delocalize significantly more electrons than **ad** molecules of these hexamers and this is in direct contrast to the common view of these waters being involved in anticooperativity and provide a quantified support for our hypothesis-2.

Table 2. The number of electrons delocalized by an indicated water molecule to remaining five water molecules of 3D hexamers. The functionality of water molecules and their numbering is consistent with that seen in Figure 1.

Prism		Cage		Book		Bag	
Water	N_{deloc}	Water	N_{deloc}	Water	N_{deloc}	Water	N_{deloc}
aad W1	2.112	aad W1	2.142	aad W1	2.100	aad W1	2.188
add W2	2.027	add W2	2.116	add W4	2.048	add W6	2.074
aad W3	1.771	add W4	1.935	ad W2	1.647	ad W2	1.719
add W4	1.861	aad W6	1.935	ad W3	1.484	ad W3	1.433
aad W5	1.778	ad W3	1.587	ad W5	1.603	ad W4	1.411
add W6	1.786	ad W5	1.439	ad W6	1.412	ad W5	1.677

4.4. Quantifying Individual Water’s Contribution to the Cluster’s Stability

Classically, delocalizing electrons between two atoms is known to be the measure of covalent character of chemical bonding as defined by Lewis, e.g., two electrons shared (delocalized) between two neighboring atoms represents a single covalent bond. Because in Lewis interpretation of bonding one considers shared electrons between next to each other atoms, it implies that the process of covalent bonding is an intramolecular event. Actually, according to a classic dogma, atoms are bonded only when they are connected through covalent bonds (purely ionic interactions excluding) and, in addition, atoms constituting a molecule (they are covalently bonded) might be involved in either bonding or non-bonding interactions with atoms of the same molecule (intermolecular interactions) or atoms of another molecule (intermolecular interactions).

Our all-body MOWeD-based data presented here and previously for cyclic structures [47] reveal that a large number of electrons is delocalized among water molecules in clusters – see Figure 5 showing that over 11 electrons are delocalized intermolecularly in prism and this is about 2e more than we found in the cyclic hexamer. Furthermore, all the above results clearly demonstrate that gaining stability is synonymous with delocalizing electrons throughout a cluster. The intermolecular *e*-delocalization can then be seen as intermolecular bonding of a covalent character when Lewis concept is expended to entire molecular system.

We have estimated [47] that the energetic effect of intermolecular *e*-delocalization on the stability of homodromic cyclic water clusters, where **ad** functionality is exclusively observed, is about an order of magnitude smaller when compared with intramolecular *e*-delocalization on a classical covalent single bond formation. Considering the theme of this contribution, it is of upmost interest and importance to quantify the energy contributions made to molecular system’s stability by different functionality of water molecules. To achieve that, we made a use of the dedicated for that purpose FAMSEC protocol that is incorporated in the molecular-wide and electron density-(MOWeD)-based all-body approach. We have computed a number of energy terms describing contributions made by a water molecule toward all remaining five water molecules of the cluster. As the **aad** and **add** functionalities were always linked with anticooperativity (or negative cooperativity, or not strict cooperativity) data obtained for bag and cage hexamers will be discussed in some detail as they have waters with **ad**, **aad** and **add** functionalities. Recall that bag and book hexamers have exactly the same number of **ad**, **aad** and **add** water molecules (descriptors computed for bag and book are highly comparable) whereas prism does not have **ad** water molecules.

Data pertaining to bag hexamer is included in Table 3. Trends seen in Figures that follow were computed for cage hexamer as highly comparable indices were obtained for all 3D hexamers; relevant data obtained for book, cage and prism are placed in Table S1 in the Supplementary Materials. To ease interpretation, water molecules in Table 3 follow the order of their interaction energy with the remaining five waters, $E_{int}(W,R)$, from the strongest attractive (most negative) to the least attractive. It is immediately seen in Table 3 that water molecules with **aad** and **add** functionalities are involved in the strongest interactions with remaining five waters in a cluster. Remarkably and regardless of functionality of a water molecule, intermolecular interactions are governed predominantly by the exchange-correlation (quantum) component $V_{xc}(W,R)$ that constitutes, on average, about $71.5\pm0.5\%$ for 3D structures (69% for a cyclic hexamer) of the total intermolecular interaction energy, $E_{int}(W,R)$.

Table 3. Energy terms computed for individual water molecules in bag hexamer. $E_{int}(W,R)$ and $V_{xc}(W,R)$ stand for the interaction energy and its exchange-correlation (covalent or quantum) component, respectively, computed between an indicated water molecule and remaining waters. *mol*-FAMSEC quantifies energy contribution made by a water molecule to the stability of bag hexamer.

Energy terms in kcal/mol			
Water	$E_{int}(W,R)$	$V_{xc}(W,R)$	<i>mol</i> -FAMSEC
aad W1	-100.03	-70.22	-57.81
add W6	-95.36	-69.20	-56.58
ad W2	-86.34	-59.52	-50.39
ad W5	-85.31	-59.23	-50.07
ad W3	-54.68	-40.56	-32.69
ad W4	-52.42	-39.20	-31.12
Average:	-79.0	-56.3	-46.4
St. Dev.:	20.5	13.6	11.7

By combining intermolecularly delocalized electrons $^{intermol}N_{deloc}$ (shown as N_{deloc} in Table 2) with the $V_{xc}(W,R)$ component of the interaction energy included in Table 3 one obtains a reasonable correlation – an example generated for cage is shown in Figure 7. It shows that an increase in the number of delocalized electrons throughout a cluster is followed by more significant contribution of

the XC-term (quantum component) to the interaction energy $E_{\text{int}}(\mathcal{W}, \mathcal{R})$. Furthermore and importantly, **ad** water molecules contribute the least in terms of delocalized electrons as well as contribution to stability of a cluster as measured by the always stabilizing in nature the $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$ component. This finding is in direct conflict with a commonly accepted and followed for decades concept of anticooperativity attributed to **aad** and **add** functionality of molecules.

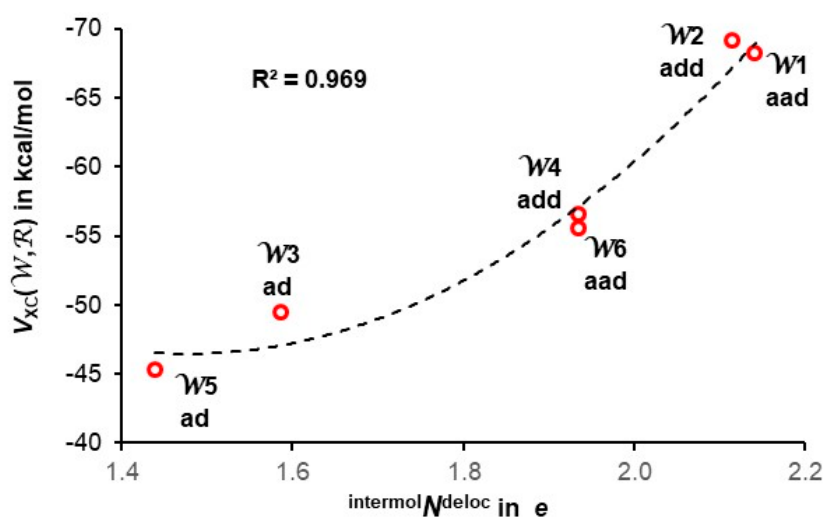


Figure 7. A trend between intermolecularly delocalized electrons ($\text{intermol}N^{\text{deloc}}$) and the XC-term of a total interaction energy between a water molecule and the remaining five waters $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$ computed for each individual molecule in the cage hexamer.

The above has demonstrated importance of the V_{xc} -term in understanding water functionality and its cooperativity. There are, however, other energy components impacting (in)stability of a system. The strongest evidence regarding individual water's contribution to cluster's (in)stability, i.e. (anti)cooperativity, should come from the purposely-derived energy term *mol*-FAMSEC. We found highly comparable trends between $\text{intermol}N^{\text{deloc}}$ and $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$ as well as between $\text{intermol}N^{\text{deloc}}$ and *mol*-FAMSEC - see Figure S1 in the Supplementary Materials prepared for cage as an example. This is an important discovery as it illustrates that there is a strong link between the total number of electrons delocalized by a water molecule throughout the space occupied by a 3D cluster ($\text{intermol}N^{\text{deloc}}$) and quantifiable measure of energy contribution to stability of a cluster made by a water molecule (*mol*-FAMSEC). Recall that the $\text{intermol}N^{\text{deloc}}$ term is interpreted here as a principal driver and quantifiable measure of cooperativity. Furthermore, data seen in Figure S1 in the Supplementary Materials suggests that there should be another important and nearly linear correlation between the quantum component of the interaction energy a water molecule is involved in with remaining waters of a cluster $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$ and *mol*-FAMSEC. Figure S2 in the Supplementary Materials shows that indeed such a linear correlation exists in the cage hexamer. Actually, we have established that high quality linear correlation between $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$ and *mol*-FAMSEC exist for all 3D hexamers discussed in this work. In each case, the most significant *mol*-FAMSEC term is observed for water molecules with **aad** and **add** functionality in a specific cluster and this strongly suggests that they are not involved in anticooperativity.

Data presented in Figure 8, where nearly perfect correlation between *mol*-FAMSEC and the interaction energy $E_{\text{int}}(\mathcal{W}, \mathcal{R})$ computed for individual water molecules is plotted for cage (red circles) and bag (violet crosses), is also observed for remaining 3D water hexamers discussed in this work (recall that $\mathcal{R}$ stands for the remaining water molecules in a cluster). This means that the combined data from all 3D hexamers follow a single linear trend that might be used as a predictive tool of either *mol*-FAMSEC or $E_{\text{int}}(\mathcal{W}, \mathcal{R})$ - see Figure S3 in the Supplementary Materials.

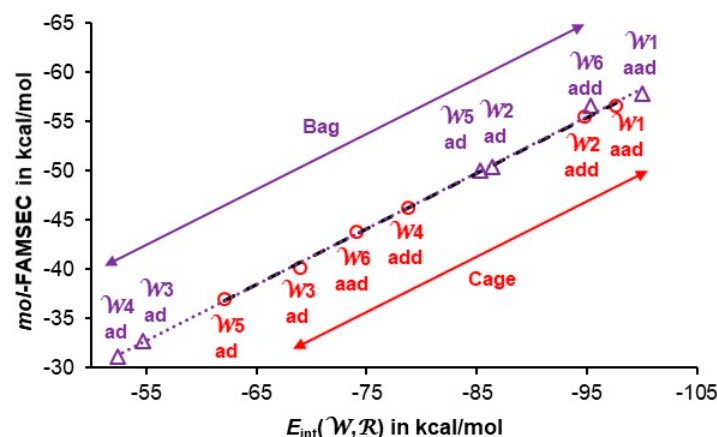


Figure 8. A correlation between the interaction energy $E_{\text{int}}(\mathcal{W}, \mathcal{R})$ and the *mol*-FAMSEC energy term computed for each individual molecule in the cage hexamer (red color) and bag hexamer (violet color). Black dashed and dotted violet lines are the trend lines for cage and bag, respectively.

To fully understand the trend seen in Figure 8, it is fundamentally important to link it with trends and expressions discussed above. According to our definition of cooperativity, this is the Physics and Quantum based quantifiable intermolecular electron delocalization that drives the formation of water clusters (clusters of molecules in general) and it leads to the non-additive decrease in their electronic energy on a n -membered cluster formation. Data in Figure 7 shows a good non-linear correlation between the driving force of cooperativity, i.e., the number of intermolecularly delocalized electrons and quantum contribution to the interaction energy $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$. In the IQA-defined energy partitioning scheme the interaction energy between any pair of atoms A and B is made of two principle components, namely the classic Coulomb term, $V_{\text{d}}(\text{A}, \text{B})$ and the XC-term (commonly interpreted as covalent or quantum contribution) $V_{\text{xc}}(\text{A}, \text{B})$. As stated above, the contribution of the V_{xc} -term to the interaction energy is nearly constant (about 71%) meaning that the %-fraction of the classic Coulomb contribution to the interaction energy made by individual water molecule is also constant and much smaller. According to classical orbital-based interpretations the intermolecular interactions, such as e.g., intermolecular H-bonds, are dominated by a classical term. One must stress here that the individual diatomic classic Coulomb intermolecular interaction energy terms $V_{\text{d}}(\text{A}, \text{B})$ in water clusters vary between large positive (repulsive) and large negative (attractive) values. However, their opposite in sign contributions largely cancel each other whereas always negative $V_{\text{xc}}(\text{A}, \text{B})$ terms sum up to a significant total value of $V_{\text{xc}}(\mathcal{W}, \mathcal{R})$.

As shown in section 3.2., the *mol*-FAMSEC term is made of two major contributions, namely *loc*-FAMSEC and the interaction energy of a selected fragment with all the remaining atoms of a molecular system, which is equivalent, in our case, to the $E_{\text{int}}(\mathcal{W}, \mathcal{R})$ term. From this and the relationship seen in Figure 8 it follows that the *loc*-FAMSEC term contributes nearly constant %-fraction to the *mol*-FAMSEC energy term computed for individual water molecules in all 3D water clusters. This fully explains the linear relationship observed in Figure 8 and Figure S2 in the Supplementary Materials.

The above undisputedly illustrates that indeed this is not the **ad** mode of action of water molecules but rather **aad** and **add** that stabilize a cluster most. Actually, we have shown that regardless of the physical/quantum property or energy component considered, regardless of the number of **ad**, **aad** and **add** waters in each cluster, the **aad** and **add** functionality always provides the most significant contribution within a specific cluster. This does not mean, however, that **ad** waters always provide smaller contributions relative to that made by **aad** and **add** molecules. This is clearly seen in Figure 8 where waters $\mathcal{W}2$ and $\mathcal{W}5$ (both **ad**) of bag hexamer provide more significant contribution to bag's stability than energy contributions made to cage by its waters $\mathcal{W}4$ -**add** and $\mathcal{W}6$ -**aad**. This nicely illustrates the overall complexity of clusters' formation and the impact made by the

immediate as well distant neighbors, the relative orientation of water molecules, distances between O-atoms and many more cooperativity-induced effects, such as $V_{xc}(W,R)$, $E_{int}(W,R)$ and *mol*-FAMSEC energy terms on the role played by a single water molecule.

4.5. Quantifying Individual Intermolecular H-bonds' Contribution to the Cluster's Stability

Considering all the above, it should be then easy to comprehend that three-way interacting **aad** and **add** molecules will show a significant spread in the computed descriptors of any kind along each H-bonded link. From the all-body MOWeD approach we conclude that the differences in values observed for the computed indices along each H-bond have nothing to do with anticooperativity as universal and quantifiable quantum and physics-based processes apply throughout all the 3D space occupied by a cluster. *Clearly, local environment determines, to some degree, the effectiveness of cooperativity between all water molecules along all possible H-bonded links that provide a unique, 'privileged' and the most effective mode of transport for electrons delocalized predominantly by O-atoms throughout a molecular system as documented previously for cyclic structures [47] and here for 3D hexamers discussed – example for bag is shown in Figure S4 in the Supplementary Materials.*

Notwithstanding the above and since it is accepted for decades that hydrogen bonds may mutually either enhance their strength when they are involved in cooperativity or reduce their strengths when involved in anticooperativity, we decided to analyze the intermolecular H-bonds in all clusters examined. We decided to make use of energy contributions made to a cluster by H-bonds using a dedicated for this purpose the *mol*-FAMSEC energy term. One must recall that the stronger a H-bond is the more significant energy-stabilizing contribution to a molecular system it provides. When making use of a classical approach that is focused on individual H-bonds, it is apparent that the values of *mol*-FAMSEC seen in Table 4 do not follow an obvious pattern that might be used to support a concept of anticooperativity.

Table 4. *mol*-FAMSEC-quantified contributions to cluster's stability made by the indicated classical intermolecular H-bonds.

H-bond	Water cluster				
	Prism	Cage	Book	Bag	Cyclic
	<i>mol</i> -FAMSEC in kcal/mol				
HB-1	-141.0	-139.3	-139.5	-142.1	
HB-2	-157.3	-145.1	-167.7	-142.7	
HB-3	-163.0	-161.0	-143.4	-143.7	
HB-4	-126.4	-133.0	-119.4	-121.8	-115.2
HB-5	-156.9	-161.5	-118.8	-119.2	
HB-6	-139.1	-150.1	-119.4	-122.4	
HB-7	-124.4	-109.8	-109.2	-125.5	–
HB-8	-138.1	-126.3	–	–	–
HB-9	-158.5	–	–	–	–
Average:	-145.0	-140.8	-131.1	-131.1	-115.2

A large spread in values of the *mol*-FAMSEC term is seen in Table 4, *e.g.* between about –110 and –168 kcal/mol in book. As one would expect, most values computed for the more stable 3D clusters are more significant than that of –115 kcal/mol obtained for a homodromic cyclic hexamer. However, the *mol*-FAMSEC terms obtained for *HB-7* in cage and book are less significant.

Focusing on three H-bonds of the most comparable *W1* water molecule in all 3D clusters (it has the same **aad** functionality throughout), they show different distribution of *mol*-FAMSEC values in each cluster. This is due to, in our view, different overall molecular environment and we see in Table

4 that *mol*-FAMSEC: (i) gradually becomes more negative in prism and cage, (ii) has much more negative value for $\mathcal{HB}$ -2 in book hexamer whereas comparable and less significant *mol*-FAMSEC terms are seen for $\mathcal{HB}$ -1 and $\mathcal{HB}$ -3, and (iii) highly comparable values for all three H-bonds we found in bag cluster. Variation in *mol*-FAMSEC values seen in Table 4 for $\mathcal{W}$ 1 water cannot be linked with anticooperativity and any selection made would be highly arbitrary and would have to be supported

A very different and consistent picture emerged when the impact of molecular environment was minimized by making use of the averaged values of the *mol*-FAMSEC terms seen in Table 4. Based on chemists' accumulated experience and knowledge, the larger number of intermolecular hydrogen bonds the more significant contribution to the water cluster's stability is expected and this is exactly what one can see in Figure 9. Relative to non-interacting six water molecules, prism is the most stable and it forms the largest number (nine) of intermolecular hydrogen bonds. Furthermore and importantly, on average, the stabilizing contribution made by a H-bond (as measured by the *mol*-FAMSEC term) increases from cyclic to prism structure.

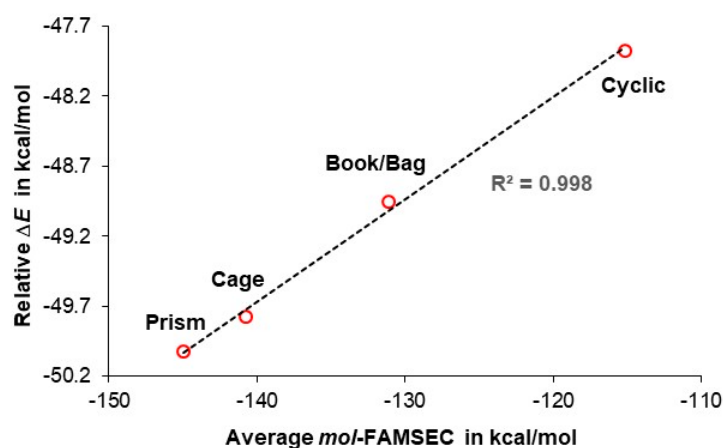


Figure 9. A trend between average *mol*-FAMSEC computed for intermolecular H-bond formed in each hexamer and, relative to non-interacting 6 water molecules, an increase in hexamer's stability.

Finally, recall that according to our understanding and definition of the cooperativity phenomenon, it is synonymous with the intermolecular **all-body** *e*-delocalization leading to the increase in stability of water molecules on a cluster formation. Analysis of data in Figure 9 leads to another supporting observation, namely the largest number of intermolecularly delocalized electrons found for prism (see Figure 6) can be attributed to the largest number of density bridges (DBs) linking water molecules due to the formation of classical intermolecular H-bonds. It becomes then clear that this is not the single DB but the network of DBs that facilitates most efficient *e*-delocalization that, in turn, determines stability of a cluster.

5. Conclusions

The proposed here general definition of the cooperativity phenomenon is a straightforward extension of our definition proposed for homodromic cyclic clusters of water [47]. The expanded definition should be applicable to any molecular cluster as it states that '*the quantifiable, physics- and quantum-based cooperativity phenomenon is synonymous with the intermolecular **all-body** delocalization of electrons leading to the increase in stability of individual molecules on an *n*-membered cluster formation.* From this follows that non-additive decrease in electronic energy of clusters, from the least stable homodromic cyclic hexamer to most stable prism is a direct result of a non-linear increase in the total number of intermolecularly delocalized electrons throughout a 3D space occupied by a hexamer, $\text{intermol}N_{\text{deloc}}$. Water molecules in 3D hexamers studied in this work can exhibit three functionalities, namely they can act as a proton acceptor and proton donor (**ad**), a double proton acceptor and a

proton donor (**aad**) and a single proton acceptor and a double proton donor (**add**). Waters with a double functionality (i.e., **aad** and **add**) are typically associated with anticooperativity (or negative cooperativity, or not strict cooperativity). Remarkably, prism that is the most stable hexamer among all possible 3D configurations of six water molecules (about 80) has all six water molecules involved in anticooperativity if one accepts the decades long interpretations. So how is that possible that prism is the most stable among them all? Our definition of cooperativity fully explains these two contradicting observations. We showed that all **aad** and **add** waters outperform **ad** molecules when the number of intermolecularly delocalized electrons is accounted for. This means that in all 3D hexamers studied, individual ‘unticooperators’, **aad** and **add** water molecules, delocalize significantly more electrons than always ‘cooperating’ **ad** waters. Hence, one is left with only one possible conclusion that the **aad** and **add** water molecules in 3D hexamers are the best ‘cooperators’ and this excludes them as being involved in anticooperativity, a term not defined in proper English (Oxford dictionary). It would be of interest and paramount importance to establish if our finding is equally applicable to all remaining 70+ 3D hexamers. This would be a mammoth job but, due to its fundamental importance, we intend to embark on that challenge and hope to report our results soon.

In our opinion, the $\text{intermol}N_{\text{deloc}}$ term is a universal quantifiable measure of cooperativity phenomenon. It can be applied to entire cluster (then it stands for the total number of electrons delocalized by all molecules of a cluster), or individual molecules within a cluster (both these options were explored in this work), or even to examine cooperativity/anticooperativity of a k -membered molecular fragment within a n -membered cluster ($k < n$).

One must stress that the physics- and quantum-based processes of e -delocalization lead to changes in properties of all imaginable properties of a molecular system, such as a water cluster. It is apparent that some of cooperativity-induced changes in local properties of a cluster were interpreted as anticooperativity. We investigated a few cooperativity-induced properties but from the molecular-wide and electron density (MOWeD) perspective we established that the changes in these properties do not corroborate with commonly accepted concept of anticooperativity. Our main focus was on contributions made to cooperativity-induced properties by individual water molecules within a 3D clusters examined. Contrary to common interpretations, the **aad** and **add** molecules have not shown any signature of anticooperativity as they always contributed the most to a cluster stability regardless of a descriptor investigated. Actually, we discovered an excellent linear relationship between *mol*-FAMSEC (a dedicated energy term to quantify the energy contribution made by a selected molecular fragment to the stability of a molecular system) and the intermolecular interaction energy a fragment (here a water molecule) is involved in with the remaining atoms of a system (here a cluster). Remarkably and considering each cluster separately, all water molecules with the **aad** and **add** functionalities outperformed the classically accepted ‘cooperators’, i.e., the **ad** water molecules, by stabilizing a cluster the most due to most significant *mol*-FAMSEC and other terms computed.

Supplementary Materials: The following supporting information can be downloaded at the website of this paper posted on Preprints.org. The Supporting Information is available free of charge as Cartesian XYZ coordinates of 3D water clusters; energies of 3D clusters; the total interaction energy and its exchange-correlation term between a water molecule and remaining waters in clusters and *mol*-FAMSEC energy term computed for each water molecule in book, cage and prism; Figures showing trends between selected descriptors computed for individual water molecules in clusters and visual presentation of FALDI 3D density distributions.

Author Contributions: Conceptualization, I.C.; Methodology, I.C. and S.Z.; Software, S.H.; Validation, S.Z. and I.C.; Formal analysis, S.Z. and I.C.; Investigation, S.Z., S.H. and I.C.; Resources, I.C.; Data curation, I.C.; Writing—original draft preparation, I.C.; Writing—review and editing, S.Z. and I.C.; Visualization, I.C. and S.Z.; Supervision, I.C.; Project administration, I.C.; Funding acquisition, I.C. All authors have read and agreed to the published version of the manuscript.

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