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[Bernard Stanisław TWARÓG](#) *

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Article

Change in Optimal Shares of PV and Wind in Hybrid Power Plants in Europe Due to Climate Variability Using the Monte Carlo Method

Bernard Twaróg

Cracow University of Technology; btwarog@pk.edu.pl

Abstract: The article provides a comprehensive analysis of optimizing the component shares in hybrid solar and wind power plants across European countries. The study is based on long-term meteorological data from 1980–2022 with a spatial resolution of 0.25x0.25 degrees. Calculations of gross and net available energy were conducted using daily values of solar radiation, wind speed, and temperature, incorporating technical constraints. Optimal proportions for utilizing various energy sources were determined using Markowitz Portfolio Theory (MPT). Historical daily data on solar radiation, wind speed, and temperature, coupled with Mann-Kendall tests at a 5% significance level, were utilized to assess trends and identify climate variability over time. Statistical models employing Monte Carlo Methods were applied to forecast daily values of solar radiation, wind speed, and temperature over a 10-year horizon. Based on these forecasts, the shares of components in hybrid power plants were re-optimized, enabling an evaluation of the impact of predicted climate changes on the energy mix. To illustrate potential financial implications of these climatic changes, the study calculated variations in revenue from energy sales for a 2 MW hybrid system (1 MW solar, 1 MW wind) across individual countries. The analysis revealed disparities in revenue changes, with losses of up to -150 EUR/day in southern Europe but gains of up to +135 EUR/day in northern and central regions, such as the British Isles and eastern Germany. These findings emphasize the need for tailored energy strategies to mitigate economic risks in vulnerable areas while maximizing opportunities in regions forecasted to benefit from climatic shifts. The results are presented graphically and conclude with a discussion on the implications of climate change for the economic viability of hybrid energy systems. This study highlights the importance of integrating climatic forecasts, advanced modeling techniques, and financial analysis in the strategic planning of renewable energy infrastructure.

Keywords: hybrid power plants; WT power; PV power plants; MPT; optimization; RES variability; Monte Carlo methods

1. Introduction

Climate change represents one of the most significant challenges of our time, serving as a key driver of the global transition towards sustainable energy systems [1–4]. Achieving carbon neutrality and reducing greenhouse gas emissions requires a shift away from fossil fuels towards renewable energy sources (RES) [2–7]. Among the most promising solutions are hybrid power plants that combine photovoltaic (PV) and wind turbine (WT) technologies. These systems leverage the complementary characteristics of solar and wind energy, enhancing stability, efficiency, and reliability in energy production [2,5,6,8–11].

Europe, as a global leader in energy decarbonization, aims to achieve an 80–95% share of RES in its energy mix by 2050 [12]. However, integrating RES into existing grids faces challenges due to the natural variability of resources like solar radiation and wind speed [13–15]. Solar energy production peaks during the day, while wind energy is often more available at night or under low sunlight conditions [16]. This complementarity makes them ideal components of hybrid systems, but their availability is highly dependent on climatic conditions. Climate variability, shaped by long-term

changes in temperature, solar radiation, and wind patterns, directly impacts the future potential of PV and WT energy production [4,17,18]. Forecasts suggest a 10–12% decline in solar energy potential in Northern Europe [19], with moderate increases expected in Southern regions, while wind energy exhibits even more complex regional variability [1,20–22].

To address these uncertainties, advanced analytical approaches like Monte Carlo simulations are crucial. These probabilistic methods enable modeling of diverse climate scenarios, allowing for a more accurate assessment of long-term RES performance and the optimization of hybrid energy system design [13,23,24]. This study aims to evaluate the impact of climate variability on the optimal shares of PV and WT in hybrid power plants across Europe, providing actionable insights for strategic energy policy and planning [25–27]. By incorporating Monte Carlo modeling, this analysis captures the complex interplay between climatic trends and RES resources, offering robust frameworks for maximizing resource utilization and system reliability [28–30].

Achieving the ambitious goal of climate neutrality by 2050 requires energy systems resilient to climatic fluctuations. Understanding the variability and complementarity of PV and WT resources is key to developing stable systems capable of maintaining energy supply even under extreme weather conditions [31–34]. This study supports not only the decarbonization agenda but also strengthens Europe's energy security by reducing dependence on imported fossil fuels [34]. The application of Monte Carlo methods represents a significant step forward in optimizing hybrid PV-WT systems, ensuring their sustainability and adaptability to future climatic conditions [25,33,35–37].

The increasing share of RES in energy systems comes with additional technical challenges, such as ensuring supply stability and minimizing the risk of energy shortages. Production variability necessitates more precise forecasting tools and flexible technologies. Regional integration and optimization of renewable installations play a pivotal role, especially in Europe, where climatic conditions vary significantly. By analyzing an extensive 43-year dataset on temperature, wind speed, and solar radiation across Europe, this study examines the impact of climate variability on the potential for PV and WT energy production. Modern Portfolio Theory (MPT), widely used in finance to optimize risk and return, has been adapted to the energy sector to determine the optimal mix of PV and WT technologies. This approach minimizes production variability while maximizing efficiency, providing valuable guidance for renewable energy planning.

Monte Carlo simulations explore multiple climate scenarios, accounting for uncertainties in long-term forecasts. This approach forms the basis for defining how PV and WT shares may evolve under different climatic conditions. The findings highlight the importance of flexible energy planning to reduce production variability and optimize resource allocation [9,38]. Regional strategies tailored to local climatic conditions are essential for ensuring stable and efficient energy supply. These insights are vital for investors and policymakers, providing a foundation for long-term energy strategies that minimize risks and costs associated with energy shortages.

The application of Markowitz's model refines these strategies, enabling identification of approaches that maximize efficiency while minimizing risk in hybrid energy systems [20,39–42]. Flexible and adaptive energy systems are essential for managing local and global climatic changes, promoting efficient resource utilization and strategic energy planning [3,12,26,32,33,37,43,44]. In summary, this study provides practical tools and insights supporting the development of hybrid energy systems resilient to climate variability. The results contribute to achieving climate neutrality goals, ensuring stable and sustainable energy supplies, and solidifying Europe's leadership in renewable energy integration. Subsequent sections discuss the methodology, results, and implications for the future of Europe's energy sector.

2. Modern Portfolio Theory

Modern Portfolio Theory (MPT) extends the classical portfolio theory initially introduced in the 1950s by Harry Markowitz, a Nobel laureate in economics [41,40]. Markowitz proposed a methodology for selecting efficient investment portfolios, based on maximizing the expected rate of return while considering the level of risk investors are willing to accept [25]. This theory assumes that

investors evaluate investments using two fundamental variables: expected return and variance. According to MPT, risk-averse investors prefer portfolios that offer the maximum expected return for a given level of risk or minimize risk for a set expected return.

The mean-variance model, which forms the foundation of MPT, highlights the benefits of investment diversification, enabling the minimization of risk while maintaining the desired expected return. This approach allows for the identification of the efficient frontier, which represents different investment portfolios in the risk-return space [20,45,46]. Portfolios located on this frontier are considered efficient because they provide the best balance between risk and return. Investors are advised to select portfolios along the efficient frontier, as these offer optimal outcomes based on their individual preferences for risk and return.

The mathematical representation of a portfolio's expected value and variance is defined by the following equations:

$$E(r_p) = \sum_{i=1}^N \omega_i E(r_i), \quad (1)$$

$$\sigma_p^2 = \sum_{i=1}^N \sum_{j=1}^N \omega_i \omega_j \rho_{ij} \sigma_i \sigma_j, \quad (2)$$

where: $E(r_p)$ – expected return of the portfolio, $E(r_i)$ – expected return of the i-th component of the portfolio, ω_i – weight of the i-th component in the portfolio, σ_p^2 – Variance of the portfolio, ρ_{ij} – correlation coefficient between the i-th and j-th components of the portfolio, σ_i – standard deviation of the i-th component of the portfolio.

Alternatives for Investment Decision-Making:

- Maximizing the Expected Return for a Given Level of Risk (Equations (1)–(6)):

The investor determines the maximum level of risk they are willing to accept and selects a portfolio that maximizes the expected return within that risk threshold. This corresponds to identifying a portfolio on the efficient frontier that meets the risk tolerance criterion:

$$\max E(r_p), \quad (3)$$

$$\sigma_p^2 \leq \hat{\sigma}^2, \quad (4)$$

$$\sum_{i=1}^N \omega_i = 1, \quad (5)$$

$$\omega_i \geq 0 \quad (6)$$

- Minimizing Risk for a Given Expected Return (Equations (1), (2) and (7)–(10)):

The investor specifies a desired expected return and chooses a portfolio that minimizes variance (risk) at that return level. In this case, the portfolio on the efficient frontier provides the lowest possible risk for the established expected return:

$$\min \sigma_p^2, \quad (7)$$

$$E(r_p) = \sum_{i=1}^N \omega_i E(r_i) = E(\hat{r}), \quad (8)$$

$$\sum_{i=1}^N \omega_i = 1, \quad (9)$$

$$\omega_i \geq 0, \quad (10)$$

Amid increasing climate variability and unpredictable weather events, the classical MPT approach requires adaptation to the specifics of the renewable energy sector [47,48]. Fluctuations in temperature, wind speed, and solar radiation intensity make models based solely on historical data

insufficient for predicting future energy production conditions. Therefore, more flexible models are necessary to incorporate new risk dynamics and the impact of climate change.

For wind and solar farms, weather variability leads to fluctuations in energy production, increasing the risk of unanticipated losses. Expanding MPT to include climate variables enables more precise investment planning and the development of hybrid systems resilient to climate change. This approach supports the optimization of the energy mix through dynamic adjustments of PV and WT installations based on climate forecasts. The flexibility of this solution reduces risk and ensures energy supply stability over the long term [25,45,40].

Modern Portfolio Theory is increasingly applied in the energy sector, particularly in the strategic planning of electricity generation. MPT facilitates the evaluation of trade-offs between energy production levels and the risks associated with resource unpredictability, such as wind and solar energy [47,48]. In practice, it helps investors and policymakers better manage risk and plan stable energy systems that are resilient to changing climate conditions [25].

3. PV Component

The Sun, acting as a perfect black body, continuously emits radiation, a portion of which reaches the Earth, where it is absorbed or reflected by the atmosphere and clouds. The intensity of this radiation, measured in units of $[W/m^2]$, along with the Global Horizontal Irradiance (GHI)—which represents the total radiation reaching the Earth's surface throughout the day—are key indicators for assessing the photovoltaic potential of a given area. Photovoltaic energy production, which involves converting sunlight into electricity through the photovoltaic effect, takes place in solar power plants. These plants are often integrated with other renewable energy sources, enhancing their flexibility and reliability.

For the purpose of analysis, a photovoltaic farm with an installed capacity of 1 [MWp] was considered. The output power (Equations (11) and (12)) of the panels was calculated using the formula provided below :

$$P_{out} = \eta P_{STC} \left(\frac{R_{hor}}{R_{STC}} \right) [1 - \alpha_p (T_m - T_{STC})], \quad (11)$$

where: P_{out} - output power of the panel [W], $\eta = 0,85$ efficiency factor, P_{STC} - nominal power of the PV panel [W], $R_{STC} = 1000$ $[W/m^2]$ irradiance under Standard Test Conditions (STC), T_m - operating temperature $[^\circ C]$, $T_{STC} = 25$ $[^\circ C]$ - reference temperature under Standard Test Conditions (STC), R_{hor} - average irradiance on a horizontal surface, $[W/m^2]$.

Finally, the following formula was adopted:

$$P_{out} = 0,225 R_m [1 - 0,0042 (T_m - T_{STC})], \quad (12)$$

R_m - total solar radiation (direct, reflected, and diffuse) $[W m^{-2}]$.

4. Wind Power Plant Component

Wind power plants harness wind energy (the kinetic energy of moving air masses) and convert it into a useful form of energy, typically mechanical or electrical [49]. The devices where this transformation takes place are called wind turbines. Energy conversion occurs when an air stream passes through the area swept by the rotor of a wind turbine. The rotor blades are aerodynamically shaped to move perpendicularly to the air stream, utilizing a portion of the kinetic energy available in the moving wind [49]. The amount of wind energy depends on wind speed and air density. Not all the kinetic energy available in the wind can be converted into another form of energy as it passes through a wind turbine. The ratio of the kinetic energy that can be converted by wind turbines to the kinetic energy available in the wind is known as the power coefficient (C_p). The maximum value of the power coefficient that can be achieved by a wind turbine is $16/27$ (59.3%, Betz's law) of the kinetic energy available in the wind [50].

The output power of a wind turbine (Equations (13) and (14)) varies with wind speed according to the following equation [49,50]:

$$P_{\text{out}} = \frac{1}{2} C_p \rho A v^3, \quad (13)$$

where: P_{out} - output power [W], C_p - power coefficient, ρ - air density [kg/m^3], A - area swept by the rotor blades, [m^2], v - wind speed, [m/s], Wind speed adjusted to a height of 100 [m], with a scaling factor of 1.044.

$$v_2 = v_1 \frac{\log(\frac{h_2}{z_0})}{\log(\frac{h_1}{z_0})}, \quad (14)$$

where: v_2 [m/s] – wind speed at height h_2 [m], v_1 [m/s] – wind speed at height h_1 [m], $z_0=0.03$ [m] (open agricultural land without fences and hedges; maybe some far apart buildings and very gentle hills).

Both the power coefficient (C_p) and the output power depend on wind speed. The efficiency of a wind turbine is generally represented by its power curve, which illustrates the exact output power achievable from a wind turbine for each wind speed value. The cut-in speed is the wind speed at which the wind has enough energy to start moving the rotor blades from their static position. The rated speed is the wind speed at which the turbine achieves its rated output power or maximum power capacity. Beyond this speed, the output power remains constant at the rated power level. At wind speeds above the cut-out speed, the wind turbine must be shut down to prevent damage. The power curve of a wind turbine is typically provided by turbine manufacturers as a representation of its performance [50].

In this model, the air density was additionally determined using the relationship between temperature, pressure, and density (Equations (15) and (16)), employing the following approach [50]:

$$p = p_0 \exp\left(-\frac{\mu g h}{RT}\right), \quad (15)$$

$$\rho = \frac{pM}{RT}, \quad (16)$$

where:

$p_0 = 1013.25$ [hPa] – atmospheric pressure at reference level,

$\rho_{\text{STP}} = 1.293$ [kg m^{-3}] – reference air density,

$\mu = 0.0289644$ [kg mol^{-1}] – molar mass of air,

$g = 9.81$ [m s^{-2}] – gravitational acceleration,

$R = 8.314462618$ [$\text{J mol}^{-1} \text{K}^{-1}$] – gas constant,

$T_k = T_c + 273.15$ [$^{\circ}\text{K}$] – air temperature (Kelvin),

$M = 0.0289$ [kg mol^{-1}] – effective molar mass of air,

ρ [kg m^{-3}] – air density,

h [m] - elevation above mean sea level, including an additional 100 m for the turbine hub height above ground level.

5. Data Used in the Analysis

The analysis in this article is based on daily data presented in a grid format, sourced from published products by the National Oceanic and Atmospheric Administration (NOAA) and the European Union's Earth Observation Programme [51,52]. The study covers an area of $5750 \text{ km} \times 4100 \text{ km}$ (latitude: -15° to 40° and longitude: 35° to 75°) [53]. A spatial resolution of $0.25^{\circ} \times 0.25^{\circ}$ was adopted for the analysis. The grid products are accessible online. The study utilized data characterizing wind energy potential, solar energy potential, and temperature. Terrain elevation information (DEM) was also included in the calculations [53].

6. The Concept of Energy Cooperation—An Example

This example illustrates the application of MPT in energy cooperation analysis. The analysis was conducted for the location of Scarborough, England. For data on solar radiation, temperature, and wind speed at a height of 100 m above ground level, a detailed analysis of the gross energy potential available at the location was performed. The analysis characterized a minimum risk value of 70.09 [W/m²] and an expected available energy value of 120.77 [W/m²] (Figure 1). For the optimal point at minimum risk, the weight coefficients for the energy components are as follows: wind energy component $\omega_{wind} = 0.076$ and solar energy component $\omega_{PV} = 0.924$. The maximum expected gross energy value available at this location, at a risk level of 381.89 [W/m²], is 257.68 [W/m²]. The weight coefficients for this scenario are: wind energy component ($\omega_{wind} = 1.0$) and solar energy component ($\omega_{PV} = 0$).

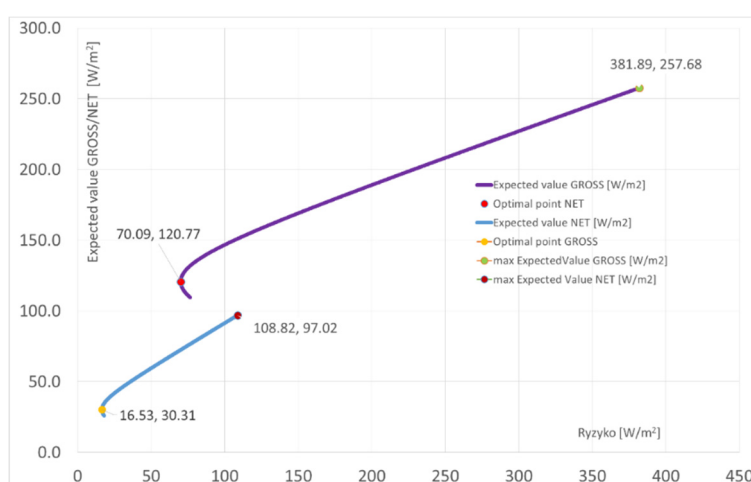


Figure 1. Shift in the location of the optimal point after implementing technological solutions compared to solar and wind energy potential, geographical coordinates (54°17', 0°24'), historical data, Scarborough, England.

The introduction of modern technological solutions in the form of a hybrid power plant composed of a photovoltaic (PV) plant and a wind power plant, each with a capacity of 1 [MW], allows the conversion of this gross potential into net electrical energy (Figure 1). However, as a result of implementing these technical solutions, the maximum achievable energy parameters are:

- At minimum risk: 16.53 [W/m²], with an expected value of 30.31 [W/m²]. The weight coefficients are ($\omega_{wind} = 0.059$) and ($\omega_{PV} = 0.941$).
- The maximum expected net energy value at this location, at a risk level of 108.82 [W/m²], is 97.02 [W/m²]. The weight coefficients for this scenario are ($\omega_{wind} = 1.0$) and ($\omega_{PV} = 0$).

The results of the MPT analysis indicate a reduction in the optimal gross energy value to net energy by 75% $((120.77 - 30.31)/120.77 = 75.0\%)$ with a 76% reduction in minimum risk $((70.9 - 16.53)/70.09 = 76\%)$. Consequently, the efficiency of the net electrical energy obtained from PV and wind power plants reached approximately 43.2% $(30.31 \text{ [W/m}^2\text{]}/120.77 \text{ [W/m}^2\text{]})$ relative to the available potential.

For the concept of a 2 MW energy mix, the following parameters were assumed:

- PV power plant: 1 MWp capacity with a PV cell rated at 225 [W/m²] (STC),
- Wind power plant: a 1 [MW] turbine by LM Glasfiber with an active blade area of 2290 [m²].

7. Climate Change

Ongoing climate change, driven by both natural processes and anthropogenic factors, underscores the growing need for carefully designed hybrid systems that are resilient to increasingly pronounced and varied extreme weather conditions. Climate change amplifies the polarization of extreme events, resulting in a higher frequency and intensity of phenomena such as droughts, storms,

heatwaves, and strong winds [54]. These extreme conditions directly affect key parameters for renewable energy production: temperature, solar radiation, and wind speed.

Higher temperatures can reduce the efficiency of photovoltaic (PV) panels, while changes in solar radiation intensity—caused by cloud cover or irregular sunshine—affect the stability of solar systems. Similarly, wind speed, a critical factor for wind energy production, is becoming increasingly unpredictable, complicating energy supply planning and stability [13,16]. Variability in these parameters increases the risk of mismatches between energy production and demand, necessitating more flexible approaches to energy system design [55].

This study analyzes the impact of climate change on the optimal energy mix over the next decade. Climate variability leads to significant fluctuations in production potential, particularly for wind and solar systems, requiring dynamic adjustments to their proportions based on local conditions [56]. In regions with high seasonal variability, the shares of PV and wind energy can differ significantly depending on the time of year.

Findings based on Modern Portfolio Theory (MPT) provide valuable insights for strategic planning of investments in hybrid energy systems. The choice of location and technology should account for changing climate conditions and the resulting uncertainties. Flexible strategies that dynamically adjust the shares of wind and solar energy in the energy mix can minimize financial risks and enhance the stability of energy infrastructure [7].

The introduction of advanced methods, such as Monte Carlo simulations, enables better prediction of extreme weather impacts and improved management of risks related to energy supply disruptions. Such analyses support the design of more resilient hybrid systems that can adapt to climate variability and ensure long-term energy stability.

Regions with high seasonal variability, such as southern Europe, require more adaptive approaches to energy mix planning, including compensating for seasonal deficits of one source with another. More stable regions can implement less complex strategies, but they still need to account for potential future climate changes.

Creating regional energy strategies allows for better resource utilization and minimizes the risk of supply disruptions. Aligning energy production with local weather conditions increases system stability and reduces operational risks. Advanced climate models are essential for effective planning and management of these systems.

The synergy between PV and wind turbine (WT) systems, supported by energy storage solutions, is a key component of modern hybrid energy systems. Wind energy can compensate for solar energy shortages during prolonged cloudy periods, while PV systems provide energy during windless periods. The integration of energy storage further enhances this synergy by enabling surplus energy produced during periods of high resource availability, such as sunny or windy days, to be stored and used during times of lower production. This increases the stability and reliability of the entire system.

Energy storage plays a crucial role in minimizing supply disruptions and optimizing the use of renewable resources. This is particularly important in regions with high seasonal variability, where the ability to store energy helps compensate for seasonal deficits of one energy source with another, enabling more stable and predictable operation of energy systems. Additionally, the integration of energy storage allows for the creation of localized strategies tailored to specific climatic and operational requirements, enhancing the efficiency and flexibility of hybrid systems [7].

Regular adjustments to the proportions of PV and WT installations, combined with energy storage capabilities, allow for effective responses to changing climate conditions. This flexibility is essential not only for ensuring continuity of energy supply but also for better resource utilization, increasing energy efficiency, and reducing operational risks. As a result, hybrid energy systems supported by energy storage become more resilient to climate variability and better prepared for future challenges.

Advanced forecasting tools and dynamic management strategies are indispensable for energy systems to flexibly respond to changing weather patterns. MPT-based analyses support the

development of more resilient hybrid systems, maximizing energy efficiency and reducing risks associated with climate variability. This approach not only enables better use of available resources but also prepares energy systems for future challenges.

8. Application of Monte Carlo Methods for Climate Forecasting

Modeling climate processes is essential for designing hybrid energy systems, particularly given the increasing variability and unpredictability of weather conditions [13,22,57]. Without accounting for dynamic climate changes, these systems may struggle to cope with extreme events, risking energy supply disruptions. Variability in parameters such as solar radiation, temperature, and wind speed necessitates the use of advanced modeling methods to ensure the resilience and adaptability of energy infrastructure [49,58].

Monte Carlo simulations enable the generation of numerous climate scenarios, providing better forecasts of how changing conditions might impact energy systems [49]. Integrating these simulations with modern techniques, such as artificial intelligence (AI) and deep learning, significantly enhances predictive accuracy. Algorithms like recurrent neural networks (RNN) and long short-term memory networks (LSTM) analyze historical and real-time weather data, identifying complex patterns and trends. This allows systems to dynamically adjust the balance between wind and solar energy based on actual and forecasted conditions [20,59].

This study applied Monte Carlo simulations to analyze climate change over a ten-year horizon. Using historical data and seasonal trends, a population of daily values for temperature, solar radiation, and wind speed was generated. The results indicate how changing conditions can influence the optimal proportions of energy sources in hybrid systems, improving their resilience.

In this study, the Monte Carlo method was employed to model climatic variability, enabling the simulation of numerous potential scenarios [49]. This approach provides insights into how changing conditions may influence the optimal proportions of energy sources, enhancing the robustness of energy system design. Monte Carlo modeling is particularly valuable for integrating uncertainty and risk, ensuring energy systems remain reliable and adaptable over long operational periods [49,58].

The forecasting model was based on the normal distribution. Anderson-Darling tests were conducted for all datasets to assess the suitability of using a normal distribution. Across the analyzed European region, for daily data on solar radiation, temperature, and wind speed, the normal distribution assumption was confirmed at a 5% significance level [60,61].

The next modeling step involved determining seasonal trend values. Monthly trends, based on daily historical data, were selected. Calculations for trends in temperature, wind speed, and solar radiation changes were performed using the non-parametric Mann-Kendall statistical test at a 5% significance level [54,62]. In areas where the use of Sen's slope was confirmed, the calculated trend value was adopted [63]. For areas where Sen's slope was not applicable, a zero trend value was assumed. For daily values, Monte Carlo simulations generated 1,000 iterations of solar radiation, temperature, or wind speed (Equations (16)–(18)). The mean value of these random iterations was adopted as the final result. Statistical modeling of climate variability factors was performed using the following mathematical model.

The climate variability modeling relied on the following equations:

$$Z_t^{PV}(x, y) = \max [0, \mu_m^{PV}(x, y) + \sigma_m^{PV}(x, y) \cdot N(0,1) + \text{trend}_m^{PV}(x, y) \cdot t], \quad (16)$$

$$Z_t^{TP}(x, y) = \mu_m^{TP}(x, y) + \sigma_m^{TP}(x, y) \cdot N(0,1) + \text{trend}_m^{TP}(x, y) \cdot t, \quad (17)$$

$$Z_t^{WD}(x, y) = \max[0, \mu_m^{WD}(x, y) + \sigma_m^{WD}(x, y) \cdot N(0,1) + \text{trend}_m^{WD}(x, y) \cdot t], \quad (18)$$

where:

t – number of years since the beginning of the forecast,,

x, y – geographic coordinates (latitude, longitude) for a 0.25° x 0.25° grid area,

PV, TP, WD – indicators for solar radiation, temperature, and wind speed data, respectively,

$Z_t^{PV}, Z_t^{TP}, Z_t^{WD}$ – daily forecasted values of solar radiation, temperature, or wind speed at time t ,
 $\mu_m^{PV}, \mu_m^{TP}, \mu_m^{WD}$ – mean values for solar radiation, temperature, or wind speed for a given month based on historical data,

$\sigma_m^{PV}, \sigma_m^{TP}, \sigma_m^{WD}$ – standard deviation values for solar radiation, temperature, or wind speed for a given month based on historical data,

$N(0,1)$ – random value drawn from a normal distribution with a mean of 0 and a standard deviation of 1,

$\text{trend}_{i,\text{month}}$ – climatic trends (linear regression slopes) representing changes in solar radiation, temperature, or wind speed over time.

This approach enabled the generation of daily values for temperature, wind speed, and solar radiation over the projected decade. The results serve as a basis for analyzing the anticipated impact of climate change on the performance of hybrid energy mixes

9. Discussion of Research Results

The analysis conducted for Europe includes spatial distributions of optimal gross and net power at minimal risk, based on both historical and forecasted data. The results also account for maximum gross and net power values, providing insights into the energy mix potential of solar and wind power plants. Comparing historical data with forecasts enables the proposal of strategies to minimize losses, improve efficiency, and adapt systems to changing climatic conditions. Spatial power maps for the entire continent support the regionalization of energy strategies for the coming decade. The scenarios are detailed in a table, considering climate changes, implications for the energy mix, the development of adaptive technologies, infrastructure planning, and recommendations for improving system efficiency and stability.

Figure 2 illustrates the spatial distribution of the optimal expected values of available gross power density (at minimal risk) from the solar and wind power plant energy mix based on historical data. The maximum values of optimal available power reach 127 W/m^2 , while the minimum values are 16 W/m^2 . The highest values are located in the northern parts of Central and Eastern Europe, including England, France, Germany, Poland, southeastern Romania, northern Bulgaria, the Czech Republic, eastern Austria, northwestern Hungary, and western Slovakia (in the range of 70 to 100 W/m^2). In contrast, the northern coast of Norway, eastern Spain, and southern Italy exhibit significantly lower values of available power. The distribution patterns of optimal expected power density from hybrid solar and wind energy systems, as illustrated in Figure 2, align with broader climate-driven forecasts. The observed gradient, where northern and central European regions exhibit higher densities compared to southern or coastal regions, reflects anticipated shifts in climatic conditions affecting solar irradiance and wind patterns. These findings support the notion from attached data that future renewable energy systems will likely exhibit greater stability and adaptability due to advances in modeling and infrastructure. However, the regional disparities emphasize the importance of tailored energy strategies, leveraging both climate models and emerging technologies like AI and deep learning for optimized resource utilization and risk management.

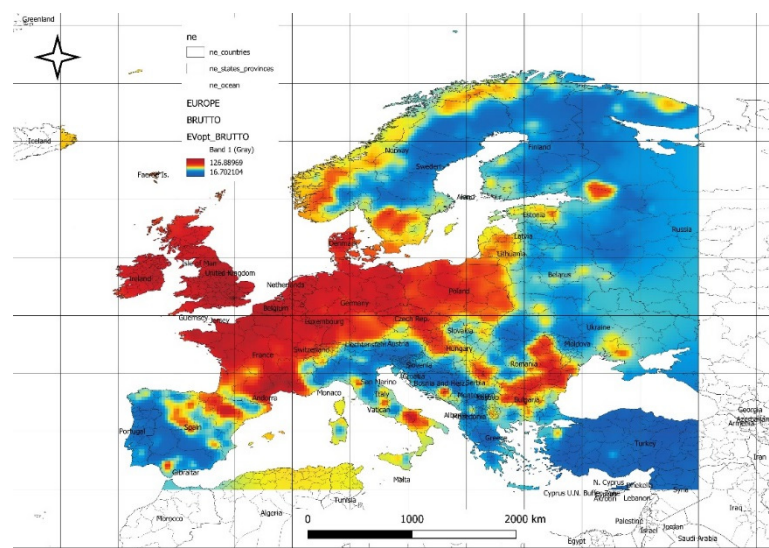


Figure 2. Optimal expected values of gross power density (at minimal risk) from the energy mix [W/m²].

The spatial distribution of optimal expected net power values at minimal risk, achievable from the solar and wind power plant energy mix based on historical data, is shown in Figure 3. The maximum power values reach 34 [W/m²], while the minimum values are 4 [W/m²]. The maximum values are located in similar regions as the gross power values. The spatial distribution of net power values, as shown in Figure 3, reflects the reduction from gross values due to efficiency losses, aligning closely with regional trends observed for gross power densities. The higher net power densities in northern and central European regions emphasize their favorable climatic conditions for hybrid solar and wind systems, while lower values in southern and coastal areas highlight efficiency challenges tied to variability in resources. This aligns with observations from the uploaded dataset, which suggests that efficiency factors and regional climatic variations must be carefully integrated into energy planning to maximize reliability. These findings further underline the importance of combining advanced predictive tools and tailored regional strategies to enhance hybrid energy system performance and minimize operational risks.

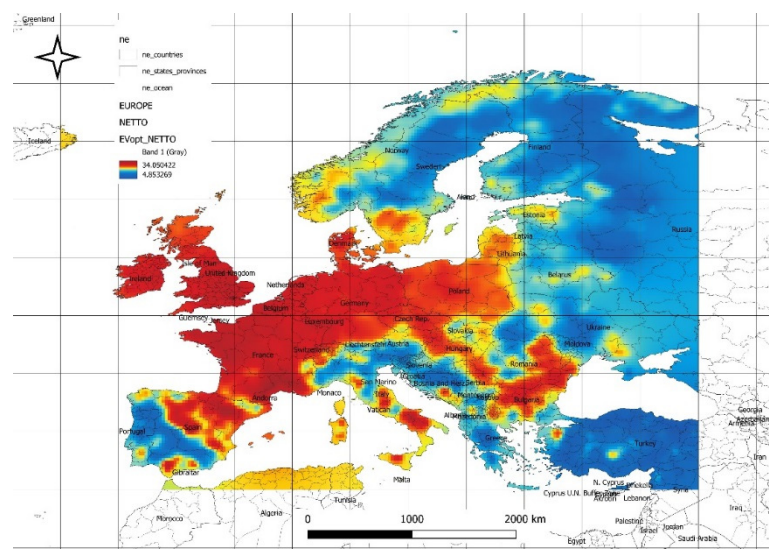


Figure 3. Optimal expected values of net power density (at minimal risk) from the energy mix [W/m²].

Figure 4 illustrates the spatial distribution of maximum expected values of available gross power density from the solar and wind power plant energy mix based on historical data. The maximum values of available optimal power reach 343 [W/m²], while the minimum values are 75 [W/m²]. The highest

values are located in England and eastern Ireland, as well as in the latitude band up to the 45° parallel. This is primarily associated with high levels of solar radiation intensity. The maximum expected values of gross power density, as depicted in Figure 4, emphasize the significant influence of solar radiation intensity on hybrid energy potential, particularly in regions like England, eastern Ireland, and areas up to the 45° parallel. These observations align with insights from the uploaded data, which stress the role of latitude and regional climatic conditions in optimizing energy mix outputs. This spatial variability underscores the importance of tailoring hybrid energy system designs to specific regional strengths, leveraging both solar and wind resources for maximum efficiency and resilience.

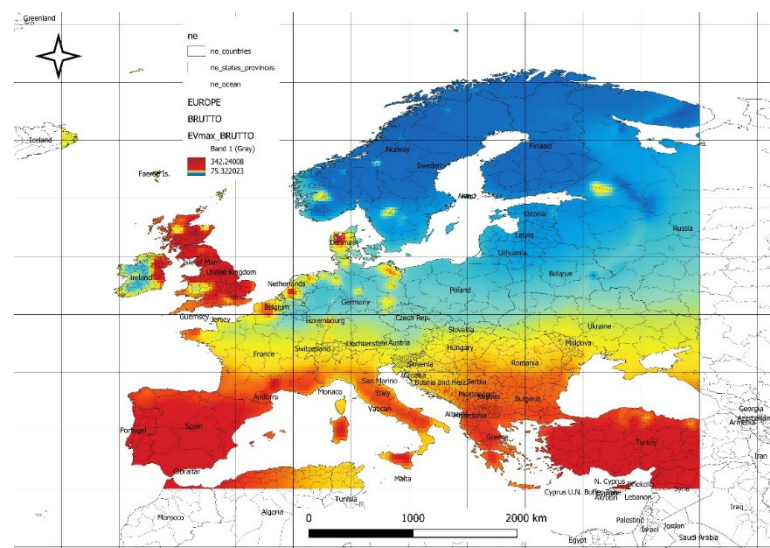


Figure 4. Maximum expected values of gross power density from the energy mix [W/m^2].

The spatial distribution of maximum expected net power values achievable from the solar and wind power plant energy mix based on historical data is shown in Figure 5. The maximum power values reach $102 \text{ [W/m}^2]$, while the minimum values are $17 \text{ [W/m}^2]$. The highest values are located in southern and central Spain, Turkey, northern regions of France, Germany, Belgium, and the Netherlands, as well as Denmark and the British Isles. The spatial distribution of maximum net power values in Figure 5 highlights the influence of regional climatic conditions and resource efficiency, with notable peaks in southern Spain, Turkey, and northern parts of central Europe. This pattern, supported by the data, underscores the importance of integrating both solar and wind resources in regions with complementary resource availability. It also demonstrates that strategic planning in these high-potential areas can optimize energy outputs while addressing variability and maximizing system reliability.

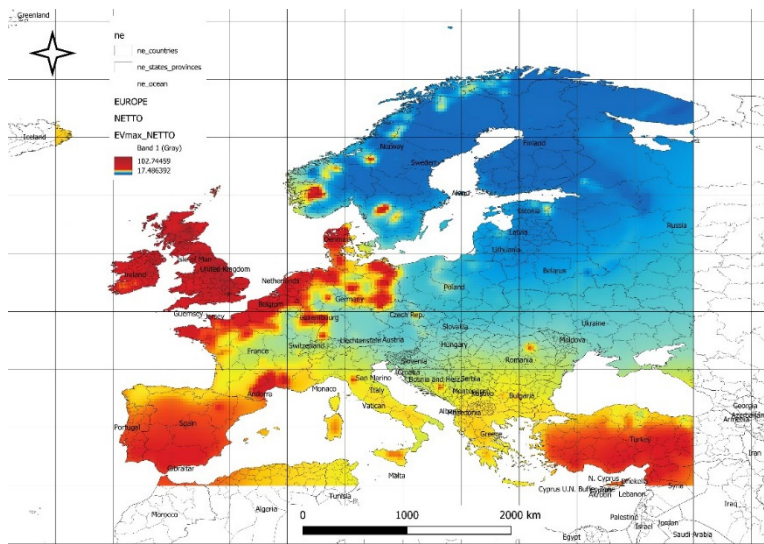


Figure 5. Maximum expected values of net power density from the energy mix [W/m²].

Figure 6 illustrates the spatial distribution of optimal share coefficients for solar and wind power plants in the energy mix for gross power values. The maximum optimal shares of the solar component are located in England, eastern Ireland, northern France, Belgium, the Netherlands, Germany, Denmark, northern Poland, and northern Norway. The spatial distribution in Figure 6 highlights regions where solar energy achieves a dominant share in the optimal energy mix, particularly across northern and central Europe. This trend aligns with observations, which emphasize the importance of solar contributions in areas where consistent sunlight complements reduced wind variability. The data further suggest that balancing solar and wind shares in these regions can enhance system resilience and maximize gross power output under diverse climatic conditions.

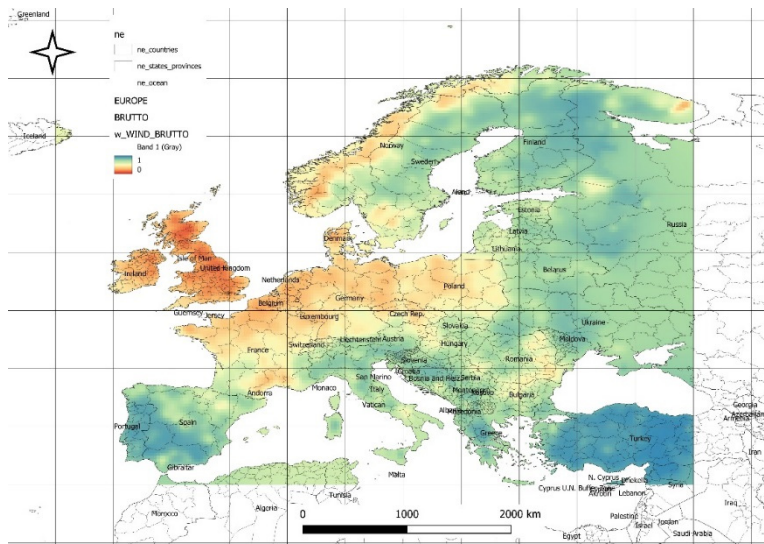


Figure 6. The value of optimal share coefficients for the gross wind energy component in the energy mix.

Figure 7 illustrates the spatial distribution of optimal share coefficients for solar and wind power plants in the energy mix for net power values. The distribution corresponds to the gross shares for the solar component. The spatial distribution in Figure 7 indicates that the optimal net shares for solar power closely mirror the gross shares, highlighting the consistency of solar’s contribution to the energy mix across regions. As noted in the efficiency factors affecting net power values minimally alter the regional dominance of solar energy in areas with favorable solar irradiance. This alignment

underscores the robustness of solar’s role in the energy mix, emphasizing the need for targeted optimization to leverage its full potential alongside wind resources.

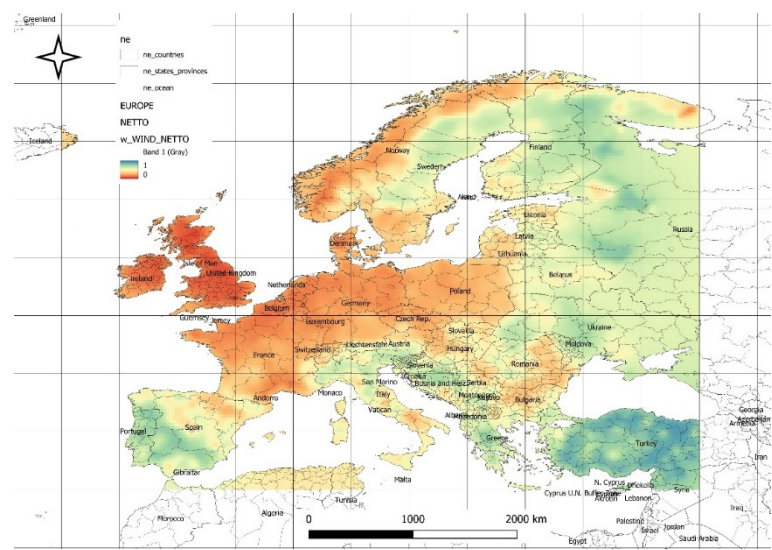


Figure 7. The value of optimal share coefficients for the net wind energy component in the energy mix.

Figure 8 illustrates the spatial distribution of optimal expected values of available gross power density (at minimal risk) from the solar and wind power plant energy mix based on forecasted data. The maximum values of available optimal power reach 122 [W/m²], while the minimum values are 16 [W/m²]. The highest values are located in the northern part of Central and Eastern Europe, including England, France, Germany, Belgium, the Netherlands, and Poland. The spatial distribution in Figure 8 demonstrates that forecasted data maintain a similar trend to historical observations, with the highest gross power densities concentrated in northern and central European regions. This highlights the consistent potential of these areas for hybrid solar and wind systems, further supported by their favorable climatic conditions and resource availability.

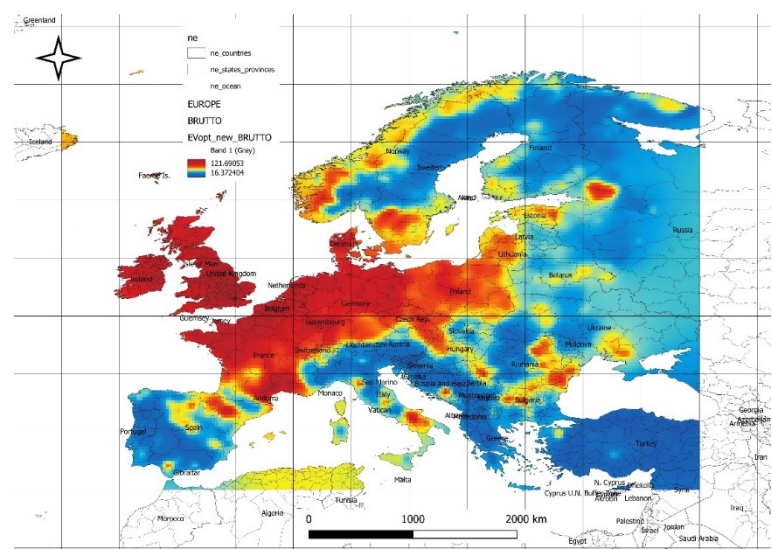


Figure 8. The value of optimal expected forecasted gross power values (at minimal risk) from the energy mix [W/m²].

Figure 9 illustrates the spatial distribution of the difference between forecasted and historical calculated optimal expected gross power values from the solar power plant energy mix. The maximum values of available optimal power reach 6 [W/m²], while the minimum values are -32

[W/m²]. Positive values, indicating an improvement in optimal gross power values over the next decade, are observed in northern France, Germany, Belgium, the Netherlands, Denmark, Turkey, Portugal, Finland, Latvia, Lithuania, Estonia, and Sweden. In other areas, a decline in optimal power values is expected. The spatial distribution in Figure 9 highlights regional disparities in the forecasted changes to gross power values for solar power, with notable improvements in northern and central Europe, including countries like France, Germany, and the Netherlands. The observed declines in other regions emphasize the importance of adaptive energy strategies to mitigate potential reductions in solar efficiency and to capitalize on areas with forecasted growth.

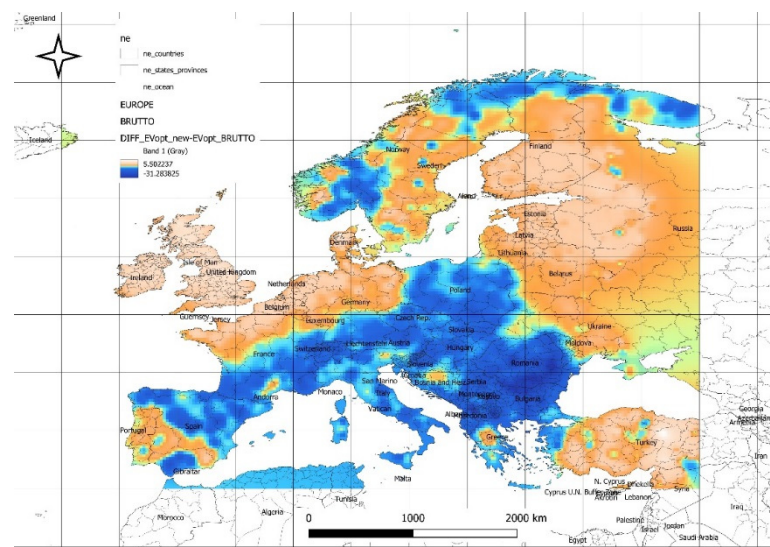


Figure 9. The difference between forecasted and historical calculated optimal expected gross power values [W/m²].

Figure 10 illustrates the spatial distribution of optimal expected values of available net power density (at minimal risk) from the solar and wind power plant energy mix based on forecasted data. The maximum values of available optimal power reach 33 [W/m²], while the minimum values are 4 [W/m²]. The highest values are located in the northern part of Central and Eastern Europe, including England, France, Germany, Belgium, the Netherlands, Poland, and western Spain. The spatial distribution in Figure 10 shows that forecasted optimal net power densities remain highest in northern and central Europe, particularly in regions like England, Germany, and the Netherlands, reflecting their robust hybrid energy potential. These findings emphasize the importance of these areas for future energy infrastructure development, leveraging their favorable climatic conditions to optimize the solar and wind energy mix.

Figure 11 illustrates the spatial distribution of the difference between forecasted and historical calculated optimal expected net power values from the solar power plant energy mix. The maximum values of available optimal power reach 6 [W/m²], while the minimum values are -7 [W/m²]. Positive values, indicating an improvement in optimal net power values over the next decade, are observed in northern France, Germany, Belgium, the Netherlands, Denmark, Turkey, Portugal, Finland, Latvia, Lithuania, Estonia, southern Sweden, and northern Norway. In other areas, a decline in optimal power values is expected. The spatial distribution in Figure 11 highlights regional shifts in forecasted net power values for solar energy, with positive trends observed in northern and central Europe, including Germany, the Netherlands, and southern Sweden, suggesting increasing solar efficiency in these areas. Conversely, declines in other regions underscore the need for targeted adaptation strategies to address potential reductions and optimize energy production where improvements are forecasted.

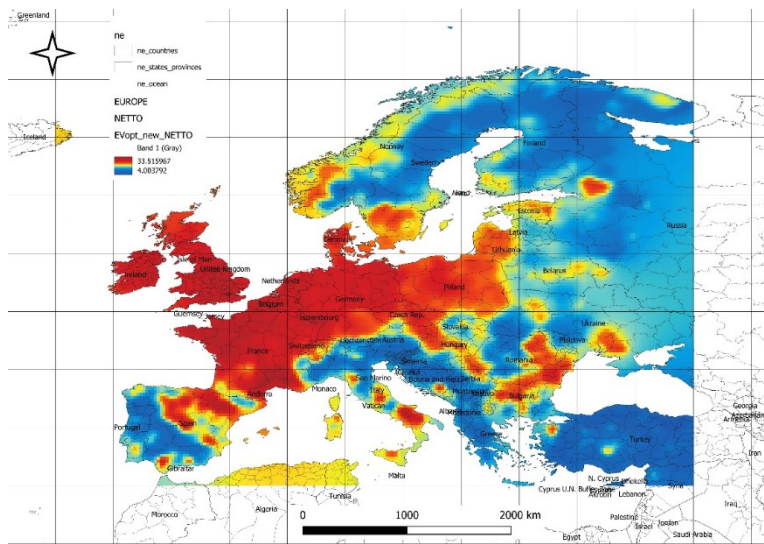


Figure 10. The value of optimal expected forecasted net power values (at minimal risk) from the energy mix $[\text{W/m}^2]$.

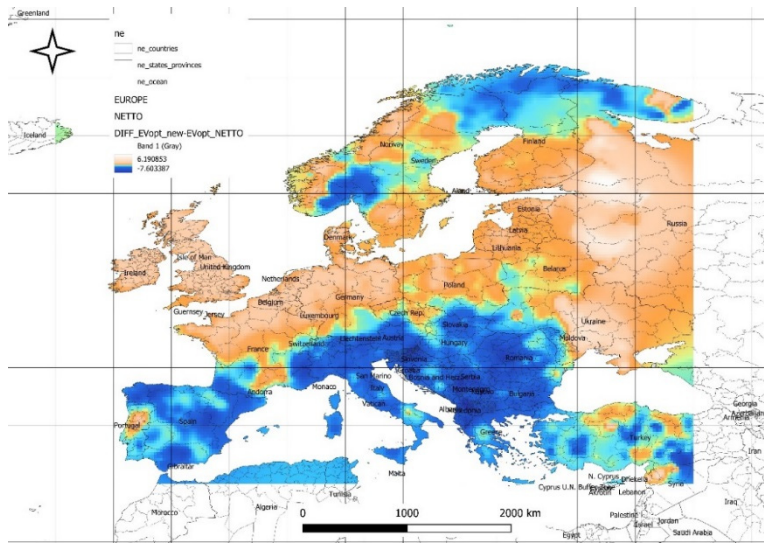


Figure 11. The difference between forecasted and historical calculated optimal expected gross power values $[\text{W/m}^2]$.

Figure 12 illustrates the spatial distribution of maximum expected values of available gross power density from the solar and wind power plant energy mix for the forecasted data. The maximum values of available optimal power reach $200 \text{ [W/m}^2]$, while the minimum values are $50 \text{ [W/m}^2]$. The highest values are located in the latitude band up to the 45° parallel, primarily due to high solar radiation intensity. The spatial distribution in Figure 12 underscores the significance of regions within the 45° latitude band for hybrid energy systems, where solar radiation intensity plays a dominant role in driving maximum gross power density. This distribution highlights the importance of focusing renewable energy investments in these areas to capitalize on their strong solar potential and ensure efficient energy generation under forecasted conditions.

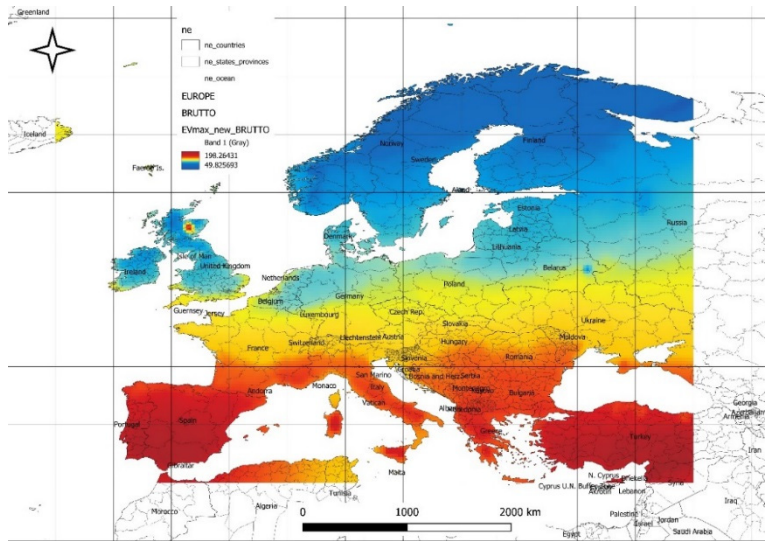


Figure 12. The value of maximum expected forecasted gross power values (at minimal risk) from the energy mix [W/m²].

Figure 13 illustrates the spatial distribution of the difference between forecasted and historical calculated maximum expected gross power values from the solar power plant energy mix. The maximum values of available optimal power reach 20 [W/m²], while the minimum values are -183 [W/m²]. Negative values, indicating a decline in maximum gross power values over the next decade, are observed along the northern coasts of France, Germany, Belgium, and the Netherlands, as well as in the British Isles. In other areas, an improvement in optimal power values is expect. The spatial distribution, Germany, and the British Isles, likely linked to reduced solar intensity or increasing variability. Conversely, areas with positive changes highlight opportunities for strategic investments and technological adaptations to optimize solar energy potential in regions expected to see improvement.

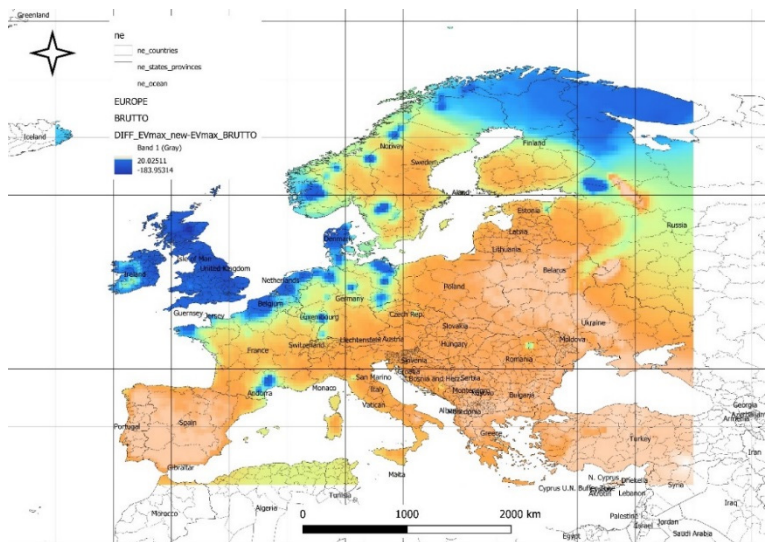


Figure 13. The difference between forecasted and historical calculated maximum expected gross power values [W/m²].

Figure 14 illustrates the spatial distribution of maximum expected values of available net power density (at minimal risk) from the solar and wind power plant energy mix for forecasted data. The maximum values of available optimal power reach 111 [W/m²], while the minimum values are 14 [W/m²]. The highest values are located in the northern part of Central Europe, including England,

France, Germany, Belgium, the Netherlands, central and southern Spain, as well as Portugal and Turkey. The spatial distribution in Figure 14 emphasizes the continued dominance of northern and central Europe in achieving high net power densities, reflecting their favorable conditions for hybrid solar and wind energy systems. Additionally, the inclusion of regions like central and southern Spain, Portugal, and Turkey highlights the potential for broader geographic diversification of renewable energy investments under forecasted conditions.

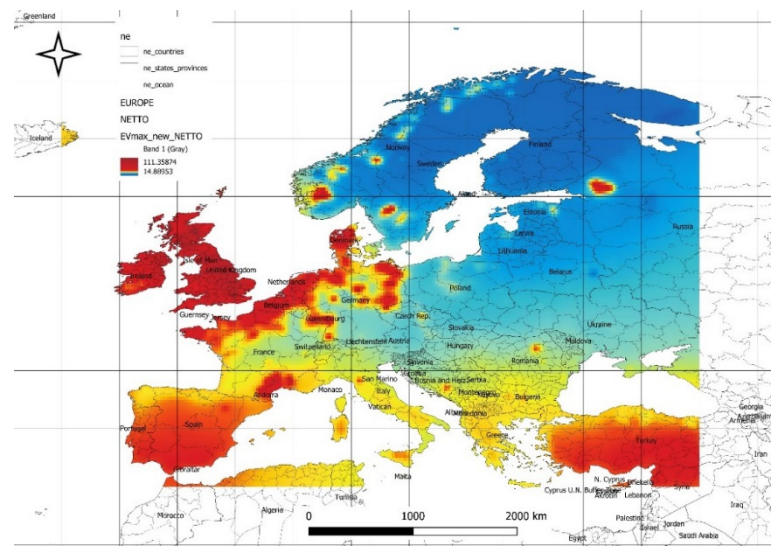


Figure 14. The value of maximum expected forecasted net power values (at minimal risk) from the energy mix [W/m²].

Figure 15 illustrates the spatial distribution of the difference between forecasted and historical calculated maximum expected net power values from the solar power plant energy mix. The maximum values of available maximum power reach 20 [W/m²], while the minimum values are -10 [W/m²]. An improvement, indicating an increase in maximum net power values over the next decade, is expected along the northern coasts of France, Germany, Belgium, and the Netherlands, as well as in Denmark, the British Isles, western Sweden, and Norway. The spatial distribution in Figure 15 highlights promising improvements in maximum net power values for regions like northern France, Germany, and the British Isles, suggesting enhanced solar efficiency and better resource utilization in these areas over the next decade. This positive trend underscores the potential for strategic expansion of renewable energy infrastructure in these regions, particularly to leverage their increasing solar power contributions alongside existing wind energy potential.

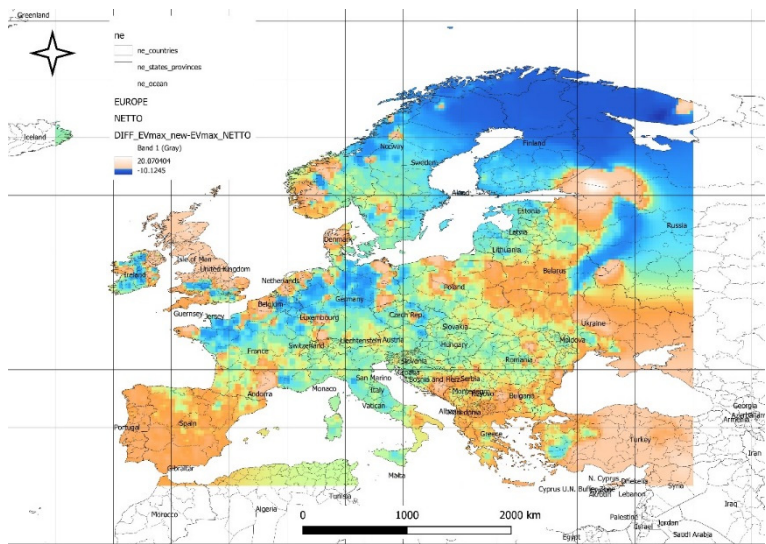


Figure 15. The difference between forecasted and historical calculated maximum expected net power values [W/m²].

Analyzing the maps of wind energy share coefficients (Figures 16 and 17), it is important to note that the solar energy share coefficients will complement these to a total of 1. The greatest potential for wind energy is concentrated in the areas of the British Isles, Ireland, Spain, and the northern coasts of France, Belgium, the Netherlands, as well as the entire area of Denmark and the northeastern region of Germany. Central Europe is less endowed with wind energy resources.

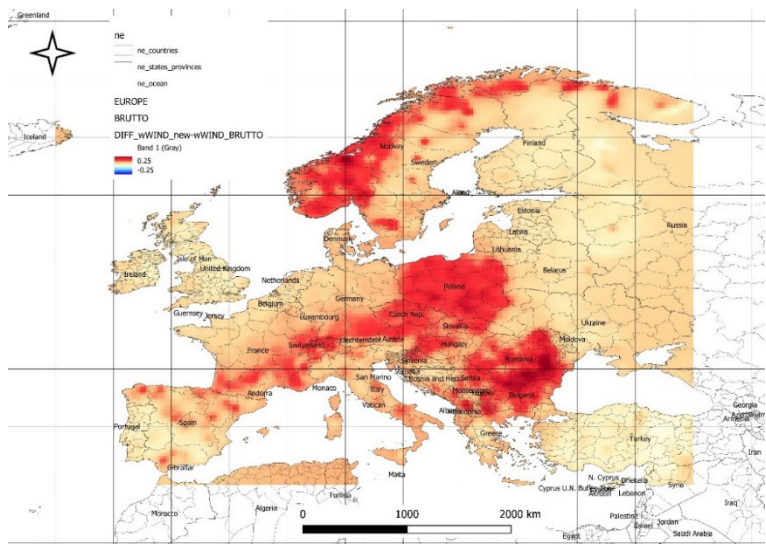


Figure 16. Change in the optimal share coefficients of the wind energy component under forecasted gross energy mix conditions compared to historical conditions.

Figure 16 illustrates the spatial distribution of changes in the optimal share coefficients for the wind energy component under forecasted gross energy mix conditions compared to historical conditions. An increase in the wind energy share is observed in Poland, the southern regions of Germany and France, as well as in Romania, Bulgaria, Albania, and Serbia. A decrease in the wind energy share is noticeable in the British Isles and Portugal.

Figure 17 illustrates the spatial distribution of changes in the optimal share coefficients for the wind energy component under forecasted net energy mix conditions compared to historical conditions. An increase in the wind energy share is observed in Switzerland, Austria, the Czech Republic, Slovakia, Slovenia, Serbia, Albania, Romania, Bulgaria, and northern Italy.

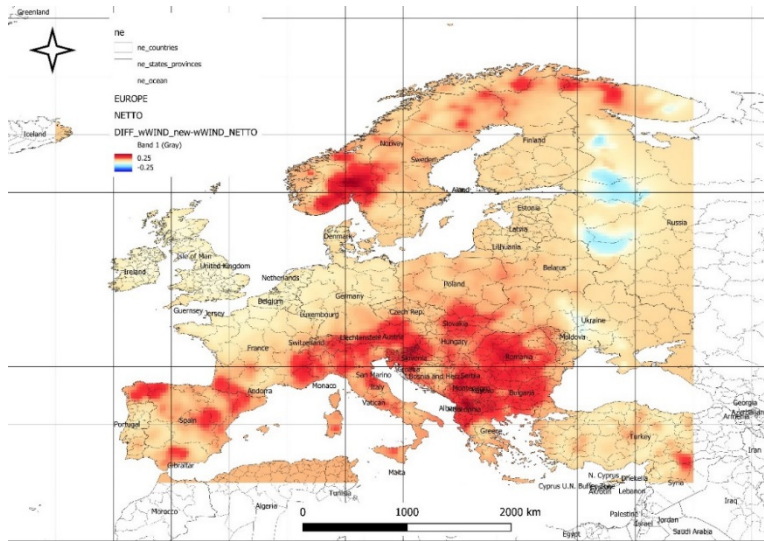


Figure 17. Change in the optimal share coefficients of the wind energy component under forecasted net energy mix conditions compared to historical conditions.

The spatial distribution in Figures 16 and 17 highlight the dynamic shifts in the spatial distribution of wind energy share coefficients under forecasted conditions for both gross and net energy mixes. While regions traditionally strong in wind energy, such as the British Isles and Portugal, show a decline in wind energy share, areas like Poland, southern Germany, and parts of the Balkans experience notable increases. The rise in wind energy share in Central and Eastern Europe, including Austria, the Czech Republic, and northern Italy, emphasizes the growing importance of these regions in the future renewable energy landscape. These shifts underline the need for adaptive energy strategies that account for regional potential and forecasted changes, ensuring optimal integration of wind and solar energy to maintain balance and efficiency in the energy mix.

From the MPT analysis for the solar and wind power plant/potential energy mix, the optimal expected power value at minimal energy portfolio risk was obtained. Additionally, for the upper branch of Markowitz’s parabola, the maximum expected power value was determined. Analyses were conducted for both historical and forecasted data. Table 1 summarizes the characteristics of the relationships between optimal and maximum net power values.

Across the analyzed European region, various cases of relationships between optimal and maximum expected energy values, gross and net risks, were identified in both historical and forecasted dimensions. The study describes all possible cases of relationships between optimal expected power values at minimal risk and maximum expected power values for both historical and forecasted data. An effort was made to standardize and characterize these possible relationships in terms of:

- Interpretation of relationships from the perspective of climate change,
- Implications for the energy mix,
- Diversification of the energy portfolio,
- Adaptability of energy infrastructure,
- Climate policy and regulations,
- Short-term and long-term planning.

The corresponding cases are indicated in Table 1:

E_{opt}^{HIS} - [W/m²] – Optimal power value from the solar and wind power plant energy mix calculated based on historical data,
 E_{opt}^{PRO} - [W/m²] – Optimal power value from the solar and wind power plant energy mix calculated based on forecasted data,

E_{max}^{HIS} - [W/m²] – Maximum power value from the solar and wind power plant energy mix calculated based on historical data,
 E_{max}^{PRO} - [W/m²] – Maximum power value from the solar and wind power plant energy mix calculated based on forecasted data.

Table 1. Analysis of Relationships and Their Implications for the Energy Mix in the Context of Climate Change.

$E_{opt}^{HIS} < E_{opt}^{PRO}$ oraz $E_{max}^{HIS} < E_{max}^{PRO}$
The relationship indicates that the optimal expected power value at minimal risk is higher in forecasts than in historical data. This suggests that in the future, even at minimal risk, renewable energy production (solar and wind) could be more efficient than in the past. Interpretation in the Context of Climate Change: • Improvement in conditions for renewable energy: Climate change may enhance the availability of solar and wind energy, for example, by extending periods of sunlight or increasing wind consistency. • Increased energy stability: A rise in optimal power values at minimal risk implies that the energy system might operate more predictably and reliably, boosting its resilience to weather variability. The maximum expected power value in forecasts being higher than in historical data indicates that future climate changes could increase the maximum production potential of renewable energy under extreme conditions, such as very strong winds or exceptionally intense sunlight. Implications for the Energy Mix: • Growth in extreme production potential: The increased forecasted maximum power value could result from predicted extreme weather conditions, such as more intense sunlight or stronger, more regular winds in specific regions. • Improved utilization of peak potential: The energy system could better capitalize on periods of peak renewable resource availability, provided appropriate investments in infrastructure are made. • Implications for the Energy Mix: • Increased renewable energy potential: The rise in both optimal and maximum power values in forecasted data highlights a positive impact of predicted climate changes on the availability of solar and wind energy. • Potential for greater renewable energy share: Higher optimal and maximum values enable a larger share of renewable energy in the energy mix without increasing risk or reducing system flexibility. • Investments in storage and transmission infrastructure: The increase in forecasted maximum power values suggests a need for advanced energy storage technologies and flexible transmission networks to efficiently utilize peak production periods. Adaptive Planning: • Long-term energy planning: Energy strategies should consider the predicted increase in solar and wind energy availability while monitoring local climate changes. • Regional differences: Forecasts may indicate variability in resource availability across different regions. Detailed regional analyses would be valuable for optimizing local energy mixes. The relationship indicates that climate change could positively impact the availability and maximum potential of renewable energy. Forecasts suggest greater efficiency in the energy system both at minimal risk and under maximum resource utilization conditions. This opens the possibility of increasing the share of renewables in the energy mix and implementing new storage and network management technologies. Recommendations: • Development of renewable energy sources: Maximize the forecasted increase in solar and wind energy efficiency through continued investments in these sectors. • Infrastructure expansion: Deploy energy storage facilities and intelligent network management systems to effectively utilize periods of peak production. • Regional climate forecasts: Identify regions where predicted climate changes will provide the greatest benefits for renewable energy. • Transmission system adaptation: Enhance the flexibility of transmission networks to accommodate increased variability in wind and solar energy availability.
$E_{opt}^{HIS} < E_{opt}^{PRO}$ oraz $E_{max}^{HIS} > E_{max}^{PRO}$
The optimal expected power value at minimal risk is higher in forecasted data than in historical data. This suggests that in the future, renewable energy (solar and wind) may exhibit greater stability and predictability at minimal risk.

Interpretation in the Context of Climate Change: • Positive changes in renewable resources: Climate change may lead to better resource availability, such as increased sunlight or more consistent winds, improving the predictability and efficiency of the energy portfolio. • Increased portfolio stability: Higher optimal power values in forecasted data indicate greater resilience of the energy system to weather variability, which is beneficial for the energy mix. The maximum expected power value in historical data is higher than in forecasted data. This indicates that the peak potential for renewable energy production may be lower in the future, potentially due to more extreme or unpredictable climatic conditions. Interpretation in the Context of Climate Change: • Constraints from instability: Forecasted climate changes may lead to greater variability in extreme events, such as excessively strong winds or high temperatures, limiting the maximum potential of renewable energy production. • Flattening of peak potential: Lower forecasted maximum power values could indicate challenges in fully utilizing extreme conditions favorable for energy production, necessitating appropriate technical solutions such as energy storage. Implications for the Energy Mix: • Increased share of renewable energy: Higher forecasted optimal power values suggest favorable conditions for integrating renewable energy sources, especially in stable, long-term scenarios. • Adaptation to lower forecasted maximum power values: Reduced peak potential in the future underscores the need to develop energy storage technologies to ensure availability during periods of low production. • Investments in system flexibility: Lower maximum power values in forecasts may require greater flexibility in transmission and storage infrastructure to manage production variability effectively. • Long-term planning amid climate change: Preparing for lower peak production values necessitates strategic energy mix planning, taking into account regional differences in resource availability. Recommendations for the Future Energy Mix: • Development of energy storage technologies: Mitigate the impact of lower forecasted maximum power values through investments in batteries and other energy storage solutions. • Diversification of energy sources: Beyond solar and wind, place greater emphasis on other renewable energy sources such as biomass or geothermal energy to offset declines in peak production potential. • Improved infrastructure management: Modernize transmission networks to adapt to more diverse production conditions in the future. • Incorporation of climate variability: Predictive energy mix models should account for dynamic changes in climatic conditions and their impact on the stability and peak potential of renewable energy. Summary: The relationship highlights the beneficial impact of climate change on the stability of renewable energy sources while limiting their maximum potential. Energy system development should focus on adapting to changing conditions and investing in technologies that enable effective resource management and reduce the impact of weather variability on energy production.
$E_{opt}^{HIS} < E_{opt}^{PRO}$ oraz $E_{max}^{HIS} = E_{max}^{PRO}$
A lower optimal expected power value in historical data compared to forecasted data indicates that predicted climate changes may improve conditions for renewable energy production at minimal risk. This suggests a greater potential for stable production in the future, likely due to projected climate trends such as increased wind intensity or longer periods of sunlight. Interpretation in the Context of Climate Change: • Improved conditions: Forecasts suggest more favorable climatic conditions for renewable energy production compared to historical data. • Future stability: Higher optimal forecasted power values imply that future energy production at minimal risk will be more stable, supporting long-term planning for a renewable energy-based mix. The equality of maximum expected power values between historical and forecasted data indicates that the peak potential for renewable energy production remains unchanged. This means that in the future, it will still be possible to achieve maximum production levels similar to those observed in the past during optimal weather conditions. Interpretation in the Context of Climate Change:

• Consistency of peak potential: Maximum potential will remain unaffected despite forecasted climate changes, suggesting that extreme weather conditions (e.g., very strong winds or periods of intense sunlight) will occur with similar frequency and intensity. • Adaptive limitations: While maximum potential remains the same, utilizing this potential will require appropriate energy storage and management strategies. Implications for the Energy Mix: • Improved system stability: Higher optimal forecasted power values indicate that future climate changes may favor more stable renewable energy production, increasing its competitiveness against traditional energy sources. The energy mix could be optimized for a greater share of renewables. • Utilization of peak potential: Consistency in maximum power values requires continued investment in energy storage and transmission technologies to fully capitalize on periods of maximum production. • Long-term planning: Improved forecasted conditions for optimal power emphasize the need for further development of infrastructure supporting renewable energy, such as smart grids and resource management systems. • Investments in system flexibility: Higher stability at minimal risk for optimal power supports the development of energy systems resilient to climate variability. Maintaining peak potential requires considering local climatic conditions and investing in adaptive technologies. • Regional differences: Forecasted climate changes may vary regionally, necessitating adjustments to the energy mix based on local wind and solar conditions. Summary: The relationship between higher forecasted optimal power and unchanged maximum power suggests that future climate conditions could enhance the stability of renewable energy production at minimal risk, benefiting the development of a renewable energy-based mix. Meanwhile, unchanged peak potential highlights the need for further advancements in storage technologies and effective energy use during peak production periods. Recommendations: • Increase renewable energy share: Improved forecasts for optimal power suggest the potential for greater integration of renewables into the energy mix. • Invest in energy storage: The consistency of maximum power values necessitates the development of adequate infrastructure for storing and distributing energy. Develop adaptive technologies: Climate changes demand flexible resource management strategies. - Local planning: Incorporate specific regional climate forecasts to optimize the energy mix. $E_{opt}^{HIS} > E_{opt}^{PRO} \text{ oraz } E_{max}^{HIS} < E_{max}^{PRO}$ A higher optimal expected power value in historical data compared to forecasted data suggests that future conditions may involve greater risks associated with energy production. This implies that the stability of renewable energy supply in the future could be lower compared to historical observations. Interpretation in the Context of Climate Change: • Variability in weather conditions: Climate changes may lead to increased irregularities in sunlight and wind speed, limiting the ability to achieve stable and predictable energy supplies at minimal risk. • Seasonal variability and extreme weather events: Forecasts might indicate more frequent extreme weather conditions, such as prolonged windless periods or storms, which disrupt renewable energy availability. • Impact on energy security: This relationship suggests that future energy systems will require greater safeguards to minimize risk and ensure stable energy supplies. A higher maximum expected power value in forecasted data suggests that the future maximum potential for energy production from wind and solar will exceed historically observed values. This indicates an opportunity for greater use of renewable energy during peak production periods. Interpretation in the Context of Climate Change: • Increased renewable energy potential: Climate models may predict a rise in wind and solar energy potential in certain regions due to changes in atmospheric circulation or increased sunlight. • Technological advancements: Future technologies may better harness available renewable resources, improving efficiency during favorable conditions. • System flexibility opportunities: Higher maximum values suggest that the energy system could better manage temporary demand peaks with adequate infrastructure. Implications for the Energy Mix: • Managing stability: The decline in forecasted optimal expected power values indicates a need to increase the share of stable energy sources (e.g., hydropower, energy storage, or gas) in the energy mix to offset the
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instability of renewables. Strategies integrating renewable sources with storage systems, such as batteries or pumped hydroelectric stations, will be crucial to minimizing risks. - Utilizing renewable energy potential: Higher maximum expected power values suggest an opportunity to capitalize on favorable periods for renewable energy. However, this requires investments in flexible transmission networks and mechanisms to export or store energy surpluses. Predictive technologies will improve the management of wind and solar variability, maximizing forecasted potential. - Adapting to climate change: The forecasted instability of renewable energy supply necessitates advanced infrastructure planning that considers climate dynamics and regional resource availability. High forecasted maximum power values highlight the need for modern energy management systems capable of responding to extreme climate conditions. - Long-term planning: The higher future maximum potential requires the development of advanced energy storage technologies and expanded transmission infrastructure to fully exploit this potential. The evolution of the energy mix must account for climate change dynamics and potential shifts in regional production capacity. Summary: Higher historical optimal power values indicate greater risks of instability in future renewable energy supplies, while higher forecasted maximum power values emphasize increased future production potential. Climate change and technological advancements could enhance maximum production capabilities but also introduce greater variability and uncertainty. To effectively manage these changes, it is essential to: - Increase investments in energy storage and transmission infrastructure. - Balance the energy mix with stable sources and flexible management mechanisms. - Adapt to climate change by incorporating forecasting and long-term climate scenarios into energy planning.
$E_{opt}^{HIS} > E_{opt}^{PRO}$ oraz $E_{max}^{HIS} > E_{max}^{PRO}$ A higher optimal expected power value at minimal risk in historical data (HIS) compared to forecasted data (PRO) indicates that achieving the same level of production stability in the future may be more challenging. This suggests that climate changes or other factors (e.g., infrastructural or technological) anticipated in PRO data may lower the minimal expected power of the energy portfolio while maintaining minimal risk. Interpretation in the Context of Climate Change: - Climate variability: Forecasts may reflect increased instability in weather conditions, such as more irregular sunlight or reduced wind intensity, which lowers the expected minimal power of renewables. - Instability risk: The decline in forecasted optimal power suggests that managing renewable energy sources to ensure system stability may become more difficult in the future. A lower maximum expected power value in forecasted data compared to historical data suggests that the future maximum potential of renewable energy may be constrained. This implies that climate or environmental changes could reduce the peak generation capacity of wind and solar energy. Interpretation in the Context of Climate Change: - Decline in renewable resource availability: Forecasted climate changes, such as prolonged windless periods, increased cloud cover, or shifts in seasonal sunlight distribution, could negatively impact peak production capacity. - Impact of extreme events: More frequent extreme events (e.g., storms, droughts) could limit renewable infrastructure’s ability to achieve maximum production levels. Implications for the Energy Mix: Enhancing system stability: The higher historical optimal power highlights the need to increase the share of stable energy sources, such as hydropower, gas, or energy storage systems, to compensate for declining stability in renewables. Integrated energy management: Ensuring energy security will require improved management of energy mixes by integrating diverse sources. Development of Adaptive Technologies: - Addressing reduced maximum power: Investments in technologies that enhance the efficiency of existing renewable resources, such as advanced wind turbines, high-efficiency photovoltaic cells, or energy storage solutions, will be essential. - Adapting to irregular production: Systems must incorporate predictive technologies and better demand planning to manage more irregular renewable energy production. - Compensating for lost peak potential: Lower forecasted maximum power values suggest that future energy infrastructure may need greater redundancy to offset declines in peak production potential. This requires modernization and greater diversification of energy sources.

Transmission and Storage Infrastructure Planning: • The decline in both (E_{opt}) and (E_{max}) in forecasted data emphasizes the importance of investments in infrastructure capable of managing production and transmission variability effectively. • Expanding energy storage systems and flexible transmission networks will be critical to maximizing the use of available renewable resources. Climate Change as a Key Factor: • The decline in both optimal and maximum power in forecasts highlights the necessity of incorporating climate changes into long-term energy mix planning. Models must account for dynamic shifts in resource availability. Summary: The relationships of lower optimal and maximum power values in forecasts point to challenges in managing the future energy system in the context of climate change. Declines in stability and maximum production capacity suggest that the future energy mix must include greater diversification, infrastructure investments, and adaptive technologies. Recommendations: • Investments in stable energy sources: Increase the share of energy storage, hydropower, and flexible transmission systems. • Improved planning: Forecast models should account for climate dynamics, seasonal variability, and regional differences. • Technology development: Invest in technologies that enhance the efficiency and flexibility of renewable energy sources to maintain energy security. • Long-term strategies: Develop integrated infrastructure planning that addresses climate variability and anticipated limitations in renewable energy production potential.
$E_{\text{opt}}^{\text{HIS}} > E_{\text{opt}}^{\text{PRO}}$ oraz $E_{\text{max}}^{\text{HIS}} = E_{\text{max}}^{\text{PRO}}$ A higher optimal expected power value at minimal risk in historical data ($E_{\text{opt}}^{\text{HIS}}$) compared to forecasted data ($E_{\text{opt}}^{\text{PRO}}$) indicates that predicted future stability in energy production may be lower. This suggests that climate changes or other forecasted factors may lead to greater variability in the availability of renewable energy. Interpretation in the Context of Climate Change: • Lower stability: Climate changes could result in more irregular weather patterns, such as reduced wind frequency or increased cloud cover, negatively affecting forecasted energy production. • Increased operational risk: A decline in forecasted optimal power values suggests that future energy portfolios may face higher instability risks, especially during periods of low renewable resource availability. The equality of maximum expected power values in historical and forecasted data ($E_{\text{max}}^{\text{HIS}} = E_{\text{max}}^{\text{PRO}}$) suggests that the maximum potential for renewable energy production will remain unchanged under forecasted climatic conditions. This indicates that despite projected instability, peak production capabilities will remain the same. Interpretation in the Context of Climate Change: • Steady peak potential: The lack of change in maximum power values suggests that favorable weather conditions (e.g., strong winds or high sunlight) will still enable maximum energy production. • Limited diversity in peak production: This could mean that maximum production will continue to depend on the same conditions observed historically, potentially limiting the flexibility of resource management in the future. Implications for the Energy Mix: • Managing system stability: The decline in forecasted optimal power values highlights the need to increase the share of stable energy sources in the energy mix, such as nuclear, gas, or energy storage systems. This would help compensate for the reduced stability of renewable energy production in the future. Better integration of forecasting and variability management technologies will be essential. • Efficient use of peak potential: The stability of maximum power values means the energy system must be prepared to utilize high production periods effectively, such as through energy storage or transferring surpluses to other regions. • Adapting to variability: A decline in forecasted optimal power values suggests greater uncertainty in future energy supplies. Advanced adaptive strategies, including investments in transmission infrastructure and energy storage, will be critical. Implications for Energy Policy Design: • Flexibility in the energy mix: The stability of peak potential indicates opportunities to increase the flexibility of the energy mix through better management of production peaks. • Regional resource differences: Strategies should account for regional differences in renewable resource availability and adapt development plans to specific climatic conditions.

- Technological investments: Developing technologies that enhance production efficiency and optimize the use of renewable energy in unstable conditions is crucial. Summary: The relationship points to forecasted instability in future renewable energy supplies, while suggests that maximum production potential will remain unchanged under forecasted climatic conditions. Recommendations: - Enhancing stability: Integrate stable energy sources and develop energy storage solutions. - Utilizing peak potential: Invest in transmission infrastructure and energy storage technologies. - Considering climate variability: Adapt the energy mix to regional forecasts of climate changes. - Developing technologies: Focus on improving renewable energy efficiency and technologies that enable adaptation to variable weather conditions.
$E_{opt}^{HIS} = E_{opt}^{PRO}$ oraz $E_{max}^{HIS} < E_{max}^{PRO}$ The relationship of unchanged optimal power values indicates that the optimal expected power at minimal energy portfolio risk is the same for both historical and forecasted data. This reflects stability in minimal risk in both cases, suggesting that predicted climate changes do not significantly impact the minimal risk of ensuring optimal portfolio power. Interpretation in the Context of Climate Change: - Stability of forecasted optimal power: This may stem from the fact that minimal energy risk in the model is more dependent on the structure of the energy mix (the share of wind, solar, and other sources) and less on variability in historical and forecasted data. - Risk mitigation strategies: It is also possible that optimization strategies for minimal risk account for variability in renewable energy production (e.g., compensating for weaker wind or solar periods), minimizing the impact of climate changes on this parameter. The relationship of a higher maximum expected power value for forecasted data suggests that the potential for energy production in the future is greater than observed in historical data. This indicates that climate changes may increase the availability of wind and solar energy in the analyzed period. Interpretation in the Context of Climate Change: - Wind: Forecasts may assume stronger or more frequent winds in regions with high wind potential, potentially due to climate models predicting changes in atmospheric circulation. - Solar: Forecasts may anticipate changes in cloud cover and increased sunlight in certain regions, boosting energy potential. - Technology: This relationship could also result from anticipated advancements in technologies that more effectively utilize available renewable resources, enhancing energy conversion efficiency. Implications for the Energy Mix: - Increased renewable energy potential: Higher forecasted maximum power values suggest that the share of renewable energy in the mix should be increased to fully utilize the predicted capabilities of wind and solar. The potential to achieve higher maximum power levels implies that the energy system can be more flexible and better equipped to handle peak demand. - Balancing stability and maximization: The stability of optimal power indicates the need to balance the energy mix. Stable sources, such as hydropower, gas, or energy storage, should counterbalance the variability of renewable sources. Future infrastructure planning should consider the anticipated increase in maximum renewable potential while ensuring grid stability. Long-Term Planning: - Investments in storage and transmission: Forecasts indicating higher maximum potential require investments in energy storage technologies (e.g., batteries, hydrogen) and transmission networks to effectively manage energy during periods of overproduction. - Adaptation to Climate Change: - As climate changes affect the availability of renewable energy, countries and regions should adapt their energy strategies to account for dynamic changes in resource availability. Summary: - The relationship of unchanged optimal power values highlights stability in minimal energy risk, while the higher forecasted maximum power value emphasizes the increased future potential of renewable sources. - Climate change and technological advancements create new opportunities for renewable energy development, which should be incorporated into long-term energy mix planning strategies.

Investments in energy storage and transmission infrastructure will be essential to effectively capitalize on anticipated changes in renewable potential.
$E_{opt}^{HIS} = E_{opt}^{PRO}$ oraz $E_{max}^{HIS} > E_{max}^{PRO}$
The equality in the optimal expected power value at minimal risk for historical and forecasted data indicates that the stability of renewable energy production under minimal risk conditions will not change in the future. This suggests that the potential for renewable energy under these conditions remains unaffected by predicted climate changes. Interpretation in the Context of Climate Change: - Stability under minimal risk: Climate changes do not negatively impact the minimal risk energy portfolio, which is crucial for planning a stable energy system. - Unchanged baseline potential: A system based on forecasted data will operate at a similar level to the past under minimal risk conditions. - A lower maximum expected power value in forecasts compared to historical data indicates that climate changes may limit the maximum production potential of renewable energy. Possible reasons include reduced intensity of extreme weather conditions, such as very strong winds or exceptionally long periods of sunlight, which were significant in historical data. Interpretation in the Context of Climate Change: - Reduced peak potential: Forecasts suggest that achieving maximum energy production levels may be more challenging in the future due to reduced intensity of extreme weather conditions. - Geographical variation: In some regions, predicted climate changes may reduce the availability of renewable energy resources during peak conditions. Implications for the Energy Mix: - Stability at minimal risk: The unchanged optimal power value relationship suggests that the energy system can maintain renewable energy production stability even with climate changes, which is key for long-term energy planning. - Challenges in peak potential: The decline in forecasted maximum power highlights the need for investments in energy storage technologies and better management of peak production periods to minimize losses from reduced potential. - Adapting the energy mix: A decline in maximum potential requires a more diversified energy mix, less reliant on extreme weather conditions and more flexible to renewable resource variability. - Investments in adaptive technologies: Implementing technological solutions that enhance the efficiency of renewable energy utilization under forecasted conditions, such as advanced energy storage systems and smart energy grid management, will be essential. - Incorporating climate variability into regional planning: Regional climate forecasts should be analyzed to identify areas where reduced maximum potential will have the greatest impact on the energy system. Summary: - Unchanged optimal power value: Indicates stability in expected power at minimal risk, suggesting that climate changes will not negatively affect the baseline stability of renewable energy production. - Decline in maximum power forecasts: Highlights that future climate changes may limit the maximum production potential of renewable energy, necessitating adaptive actions in the energy mix. Recommendations: - Balanced energy mix development: Increase the share of energy sources less dependent on extreme weather conditions, such as hydropower, nuclear, or geothermal energy. - Development of energy storage technologies: Essential for efficiently utilizing renewable energy during peak periods. - Invest in climate research: Improve understanding of the impact of forecasted climate changes on regional renewable energy resources. - Adaptive energy management: Implement systems capable of adapting to reduced maximum potential, such as flexible energy transmission systems and dynamic demand management.
$E_{opt}^{HIS} = E_{opt}^{PRO}$ oraz $E_{max}^{HIS} = E_{max}^{PRO}$
The relationship of consistency in the optimal expected power value at minimal risk between historical and forecasted data indicates that the stability of renewable energy production will not change in the future, even in the context of predicted climate changes. Energy production under minimal risk conditions will thus remain as effective as in the past. Interpretation in the Context of Climate Change: Energy system stability: Climate changes do not negatively impact the stability and expected production of renewable energy under minimal risk conditions.

- Long-term planning: Continue investments in renewable energy as a stable component of the energy mix.
- Development of storage infrastructure: Utilize the stability of maximum potential to optimize energy storage and transmission during peak production periods.
- Monitoring regional changes: While global forecasts are stable, analyzing regional climate trends could reveal local deviations that should be considered in planning.
- Energy system flexibility: Implement smart grid management systems to effectively respond to potential changes in production patterns.

- Revenue changes due to differences in optimal power (forecasted vs. historical, Figure 18): Fluctuations range from -150 to +40 EURO/day. The largest declines are observed in western and northern Spain, southern France, Italy, Switzerland, and southern Germany. Increases are anticipated in the British Isles, northern France, Belgium, and the Netherlands.
- Revenue changes due to differences in maximum power (forecasted vs. historical, Figure 19): Fluctuations range from -44 to +135 EURO/day. The largest increases are expected in the British Isles, eastern Germany, Spain, and Portugal, while declines are anticipated in northeastern Sweden and northern Finland.

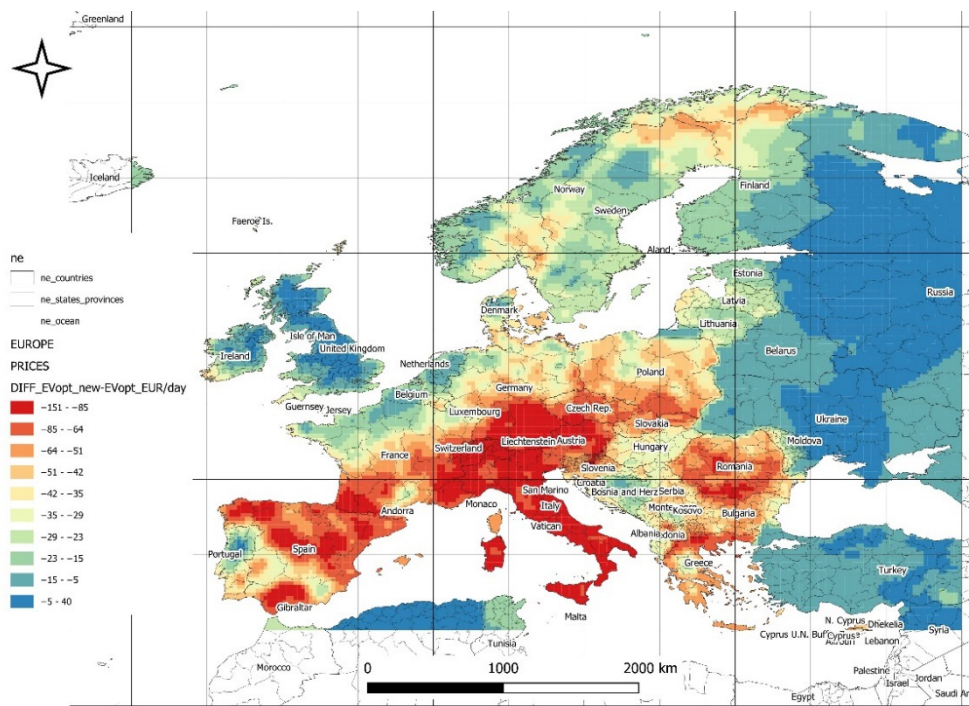


Figure 18. Changes in EUR/day resulting from climate condition variations at the level of optimal expected net power density values for the minimum risk level.

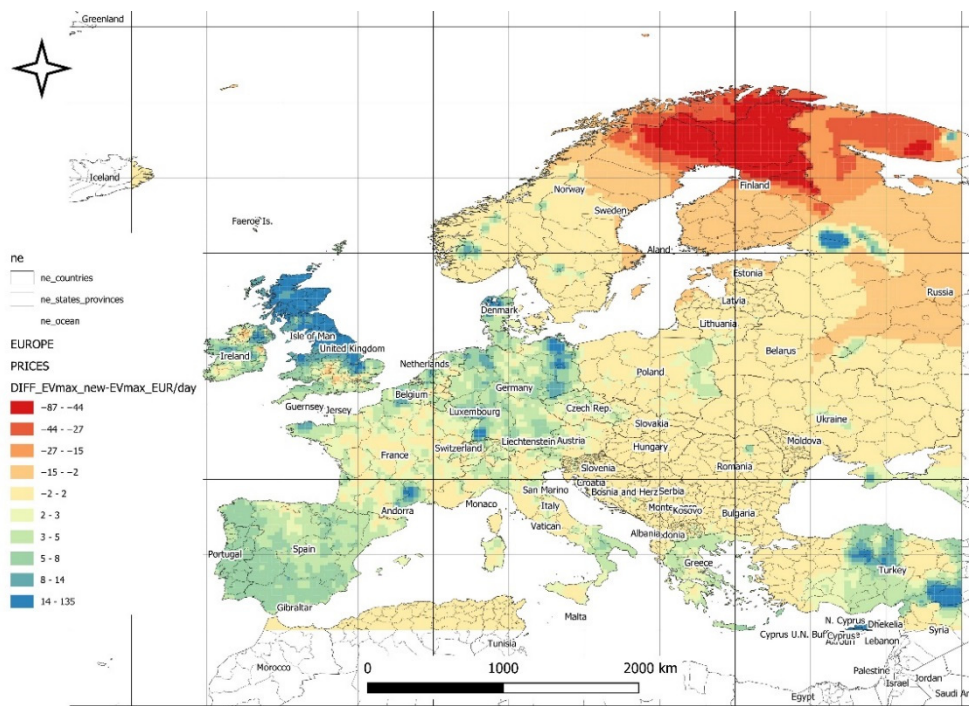


Figure 19. Changes in EUR/day resulting from climate condition variations at the level of maximum expected net power density values.

- Regional Differences:
- Optimal Power (Figure 18): Regions such as western Spain, southern France, and Italy are more exposed to losses, while northern France and the British Isles may benefit from revenue increases.

- Maximum Power (Figure 19): The British Isles, eastern Germany, and Portugal show positive financial prospects, highlighting their adaptive potential.

Recommendations:

The analysis emphasizes the need for localized energy strategies that:

- Minimize losses in regions vulnerable to adverse climatic changes.
- Maximize benefits in regions with improving conditions.
- Ensure a balanced economic impact at the regional level, supporting adaptation to evolving climatic conditions.

10. Summary

The analysis conducted for the European region considered differences in the optimal and maximum gross and net power values based on historical and forecasted data. Using daily data allowed for modeling climate variability and planning adaptive strategies for hybrid energy systems. Climate variability leads to significant fluctuations in the production potential of solar and wind energy, requiring adjustments to the proportions of these technologies based on seasonal and annual changes. The results of the analysis, based on Monte Carlo methods, highlight the critical role of flexibility in planning investments in hybrid power plants. Dynamically adjusting the shares of PV and wind energy enables a response to changing climatic conditions, which is essential for both existing and planned systems. Addressing risks and uncertainties arising from climate forecasts supports long-term planning.

The high-resolution data reveals regional differences across Europe, emphasizing the importance of local climatic conditions in shaping the optimal shares of PV and wind technologies. The results can serve as a foundation for developing adaptive strategies tailored to specific regional conditions and potential changes in the availability of renewable energy sources.

The analysis provides valuable insights for policymakers, supporting the development of decarbonization and energy mix diversification policies. Scenarios accounting for climate changes aid in planning the sustainable development of the energy sector. The application of Modern Portfolio Theory (MPT) promotes a flexible approach to planning, fostering the creation of efficient and resilient energy systems capable of meeting future challenges.

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