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Article

Regression-Assisted Ant Lion Optimisation of a Low-Grade-Heat Adsorption Chiller: A Decision-Support Technology for Sustainable Cooling

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Abstract

Growing cooling demand and environmental concerns surrounding mechanical vapour compression systems motivate research into alternative technologies capable of converting low-grade heat into useful cooling. Silica-gel/water single-stage dual-bed adsorption chillers (ADCs) are promising candidates, however, their design must balance conflicting performance targets. This study proposes a regression-assisted multi-objective optimisation framework for low-grade-heat ADC, combining statistically validated surrogate models with the Ant Lion Optimiser and its multi-objective variant. Three co-equal objectives, coefficient of performance (COP), cooling capacity (Q_{cc}) and waste-heat recovery efficiency (η_e) are jointly maximised to map an operational envelope for sustainable cooling. Two-dimensional Pareto-optimal solutions exhibit a one-dimensional ridge in which η_e declines, and COP and Q_{cc} increase simultaneously. Within the explored bounds, non-dominated ranges span COP=0.675–0.717, Q_{cc} =18.3–27.5 kW and η_e =0.118–0.127, with a practical compromise near COP \approx 0.695, $Q_{cc} \approx$ 24 kW and $\eta_e \approx$ 0.122–0.123. While mass flow rate decisions increase Q_{cc} at the expense of η_e , a one-at-a-time sensitivity analysis with re-optimisation identifies the hot- and chilled-water inlet temperatures and exchanger conductance as the dominant decision variables and maps diminishing-return regions. The proposed framework can effectively use low-grade heat in future low-carbon buildings and processes and supports the configuration of ADC systems.

Keywords: adsorption chiller; multi-objective optimisation; antlion optimiser (ALO); multi-objective antlion optimisation (MOALO); regression-based surrogate models; low-grade waste heat

1. Introduction

Recent decades have seen the transition of air conditioners from luxury to an integral part of modern standards of well-being and comfort. Aside from extreme heat-related illnesses like heat stroke, exhaustion and syncope, exposure to extremely low temperatures, particularly among infants and the aged, urbanisation, rising temperatures, and incomes are stoking the global demand for space cooling [1–3]. Human activities are gradually contributing to global warming and causing dramatic shifts in energy-use patterns [4]. The energy cost of cooling buildings steadily rises relative to other energy uses [5]. Projections show that 68% of the world's population will live in urban areas by 2050, implying an expansion of air conditioner ownership and electricity use this decade and beyond [6,7]. This emphasises the need to use modern digital tools and decision-support technologies to configure and optimise efficient, sustainable and low-carbon cooling solutions.

Typically, indoor spaces are cooled by electric fans or air conditioners, with air conditioners being the most energy-intensive choice. The most prevalent refrigeration and air conditioning systems are the Mechanical vapour compression (MVC) systems, and they require a substantial amount of high-grade

energy to power the compressor and initiate the cooling cycle [8,9]. Additionally, the refrigerants commonly used in MVC systems have been reported to have high ozone depletion potential (ODP) and global warming potential (GWP) and could be very poisonous [10,11].

It has been reported that the cooling of rooms accounts for almost a fifth of the electricity used by buildings. Currently, approximately 135 million air conditioners are sold annually, with projections of even higher sales figures in the coming years [12]. The increased usage of air conditioning has an instantaneous effect on electricity usage. This brings into question the long-term supply and sustainability of electricity resources [13]. Moreover, a 2 - 3% annual growth in electricity demand by 2030 is anticipated by the projections of the expanding world economy [13].

These drawbacks of mechanical vapour compression (MVC) systems have driven research efforts to explore and identify energy-efficient technological cooling alternatives [9]. The adsorption cooling chiller (ADC) represents a promising alternative to the conventional, high-energy-consuming MVC systems. Notably, multi-bed adsorption chillers have shown significant potential as a feasible solution. A key advantage of ADCs is their ability to operate fully or partially by low-grade energy sources like industrial solar, biomass and waste heat for heating and cooling [14]. Also, they use environmentally safe refrigerants with further benefits like durability, quiet functioning, lower energy requirements, and simple controls [15,16]. Thus, ADCs are presented as emerging sustainable cooling technologies that can be used for future low-carbon buildings and industrial operations. While adsorption chillers offer potential advantages, they also have notable limitations. These include suboptimal performance indicators like Specific Cooling Power (SCP), Coefficient of Performance (COP), high manufacturing costs, system complexity and sensitivity to operational parameters such as variations in flow rates, temperature, and working fluids. Addressing these limitations requires a robust research approach to optimise long-term dynamic performance, particularly when powered by waste or renewable heat sources [17].

This study optimises the performance of a single-stage dual-bed ADC, allowing the findings to be potentially extended to complex bed ADCs in the future. Specifically, it develops a framework that acts as a computerised decision-support tool for configuring such ADC systems.

Optimisation techniques such as single and multi-objective optimisation, which use advanced algorithms, can be employed to systematically analyse parametric interactions and serve as sub-models to improve the performance metrics and design criteria of ADCs. Optimisation techniques are computational methods used for finding ideal designs, and multi-objective optimisation specifically handles problems with several objectives, where the inherent conflicting nature of these objectives results in multiple solutions. Consequently, the multi-objective nature of most real-world engineering problems makes them appropriate for multi-objective optimisation applications due to the inherent trade-offs between performance metrics [18,19]. When combined with surrogate models, these techniques form useful digital tools for exploring high-dimensional design spaces and supporting engineering decisions.

Our earlier work on algorithmic optimisation of ADC systems [20] provides a detailed comparative summary of optimisation and control studies for silica-gel/water and multi-bed ADCs. This includes three-bed mass-recovery cycles, periodic optimal control, and integrated design and control frameworks. In this present study, we build on previous research by focusing on a single-stage dual-bed silica-gel/water ADC.

This study introduces η_e as a co-equal objective alongside COP and Q_{cc} rather than a derived metric. As a co-equal to COP and Q_{cc} , η_e is used consistently through modelling, single and multi-objective optimisation, plotting, validation with external literature and design guidance. This is to explicitly inform design source utilisation choices and quantify how low-grade heat can be effectively converted to useful cooling. In this way, waste heat recovery efficiency is treated as a core design target as opposed to a secondary indicator.

The structure of this paper is as follows: Section 2 discusses the materials and methods; Section 3 covers the adsorption chiller system optimisation details, along with the Antlion optimisation

technique and problem mathematical formulation; and Section 4 discusses the optimisation and sensitivity analysis results.

Thus, this research aims to achieve the following objectives:

- To introduce a regression-assisted multi-objective optimisation framework for a single-stage dual-bed adsorption chiller using Ant Lion algorithms.
- To maximise the Coefficient of Performance (COP), cooling capacity (Q_{cc}), and waste heat recovery efficiency (η_e) of the adsorption chiller using the Multi-Objective Ant Lion Optimisation technique.
- To conduct a sensitivity analysis with re-optimisation to determine the impacts of selected decision variables on COP, Q_{cc} and η_e and to identify regions of diminishing returns.

2. Materials and Methods

2.1. Overview of the Optimisation Framework

This study's optimisation framework treats the silica-gel/water adsorption chiller as a black-box that maps a set of design and operating variables to three performance indicators: coefficient of performance (COP), cooling capacity (Q_{cc}) and waste-heat recovery efficiency (η_e). It uses statistically validated regression models as quick substitutes for the complex thermo-physical behaviour, making it possible to extensively explore many design options without having to solve detailed dynamic models repeatedly.

We use a metaheuristic search algorithm to find the best combinations of decision variables that concurrently maximise all three objectives. This process creates a Pareto front, which shows the trade-offs between COP, Q_{cc} and η_e use. We then perform a one-at-a-time sensitivity analysis with re-optimisation to measure how key temperatures, mass flow rates, and heat-exchanger conductances affect performance and to identify where returns start to diminish. For a broader overview of metaheuristic optimisation strategies for adsorption chillers, see our previous work [20]. This paper focuses on the multi-objective Ant Lion Optimiser (MOALO) and how we use it to build and analyse the Pareto-optimal operating set.

2.2. Adsorption Chiller System and Operating Principle

This study considers a single-stage dual-bed silica-gel and water adsorption chiller that uses low-grade hot water as its energy source. Each bed alternates between adsorption and desorption depending on the pressure gains or losses and the opening and closing of the valves. The evaporator cools the chilled water, and the condenser handles heat dissipation. Figure 1 shows the main components and flow paths, with a summary of the operating cycle. The evaporator and condenser connect to the adsorbent bed via valves (V1–V4).

In Mode A, V1 and V4 are closed, whereas V2 and V3 are left open. The adsorption-evaporation process starts by connecting Adsorbent Bed 1. The heat supplied by the chilled water reduces the pressure and temperature of the adsorbate (water), causing it to boil in the evaporator. As a result, the refrigerant vapours from Bed 1 are adsorbed. The cooling water circuit receives the heat rejected during the adsorption process. The desorption-condensation process also happens concurrently in Bed 2 and the condenser. In Bed 2, heat is supplied to desorb the refrigerant in the adsorbent material, and the heat of condensation is sent to the cooling water circuit

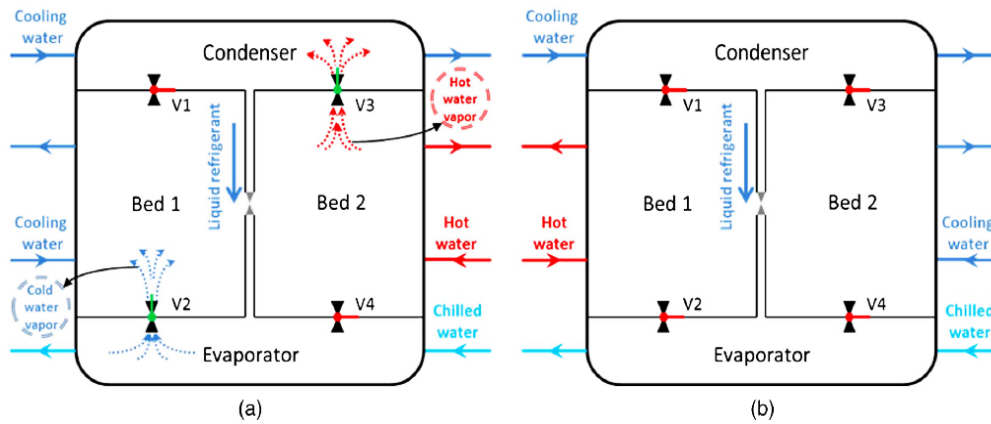


Figure 1. (a) Schematic diagram of a single-stage, dual-bed adsorption chiller (adsorption-desorption mode); (b) schematic diagram of a single-stage, dual-bed adsorption chiller (switching mode).

2.3. Regression-Based Objective Functions (COP, Q_{cc} , η_e)

Based on the system description in Figure 2 and Section 3.1, the three linear regression equations used as objective functions for the single-stage dual-bed adsorption chiller are shown as equations (2), (4) and (6) as follows:

1. Maximise COP: For adsorption cycles, COP is a primary indicator of performance calculated by estimating the cooling and heating taking place in the evaporator and condenser, respectively, according to [21]. The expression for the COP of the chiller can be represented as [22] in equation 1:

$$COP = \frac{\int_0^{t_{hc}} \dot{m}_{chw} c_{pw} (T_{chw,in} - T_{chw,out}) dt}{\int_0^{t_{hc}} \dot{m}_{hw} c_{pw} (T_{hw,in} - T_{hw,out}) dt} \quad (1)$$

where,

t_{hc} = half cycle time

\dot{m}_{chw} = chilled water mass flow rate

c_{pw} = specific heat capacity of water

$T_{chw,in}$ = chilled water inlet temperature

$T_{chw,out}$ = chilled water outlet temperature

$T_{hw,in}$ = hot water inlet temperature

$T_{hw,out}$ = hot water outlet temperature

The linear regression equations of COP, Q_{cc} and η_e with their adjusted coefficient of determination (R^2) values, are presented as follows according to Papoutsis et.al.[23].

The COP for the single-stage dual-bed ADC is shown in equation (2) as:

$$\begin{aligned} COP = & -1.1469 + 0.0014T_{hw,in} - 0.0085T_{cw,in} + 0.0124T_{chw,in} + 0.0050\dot{m}_{hw} \\ & + 0.0099\dot{m}_{cw,bed} + 0.0793\dot{m}_{chw} + 0.0092\dot{m}_{cw,cond} \\ & + 5.0687 \times 10^{-6}UA_{bed} \\ & + 5.2952 \times 10^{-6}UA_{evap} + 4.6260 \times 10^{-7}UA_{cond} \end{aligned} \quad (2)$$

with $R^2 = 0.8041$

where,

$T_{cw,in}$ = cooling water inlet temperature

\dot{m}_{hw} = mass flow rate of hot water

$\dot{m}_{cw,bed}$ = cooling water mass flow rate of the bed

$\dot{m}_{cw,cond}$ = cooling water mass flow rate of the condenser

UA_{bed} = adsorbent bed overall thermal conductance

UA_{evap} = evaporator overall thermal conductance

UA_{cond} = condenser overall thermal conductance

2. Maximize Cooling Capacity (Q_{cc}): Cooling capacity is another primary indicator of adsorption chiller performance. Q_{cc} is defined in equation (3) by [24] as:

$$Q_{cc} = \frac{\int_0^{t_{hc}} \dot{m}_{chw} c_{pw} (T_{chw,in} - T_{chw,out}) dt}{t_{hc}} \quad (3)$$

The linear regression representation of Q_{cc} for the single-stage dual-bed ADC is defined according to [23] as equation (4):

$$Q_{cc} = -64.6199 + 0.3107T_{hw,in} - 0.8625T_{cw,in} + 0.7601 + 0.6108\dot{m}_{hw} + 0.9944\dot{m}_{cw,bed} + 4.4533\dot{m}_{chw} + 0.5967\dot{m}_{cw,cond} + 0.0006UA_{bed} + 0.0003UA_{evap} + 2.6623 \times 10^{-5}UA_{cond} \quad (4)$$

with $R^2 = 0.9250$

3. Maximise waste heat recovery efficiency (η_e): Effective heat recovery strategies are pivotal in enhancing the overall system performance of ADCs (Wang and Chua, 2007). Following Papoutsis et al, η_e is defined as a cycle-averaged ratio of useful cooling to hot-water heat input according to [23] as equation (5):

$$\eta_e = \frac{\int_0^{t_{hc}} \dot{m}_{chw} c_{pw} (T_{chw,in} - T_{chw,out}) dt}{\int_0^{t_{hc}} \dot{m}_{hw} c_{pw} (T_{hw,in} - T_{hw,out}) dt} \quad (5)$$

All quantities are cycle-averaged at quasi-steady operation, and pump work is neglected.

To show how much low-grade heat is converted to useful cooling for a single-stage ADC, η_e , is optimized alongside COP, equation (2) and Q_{cc} , equation (4). Equation (6) is propagated through all the optimization processes, visualizations and validity checks.

The regression expression used for η_e [23] is:

$$\eta_e = -0.2347 - 0.0003T_{hw,in} - 0.0019T_{cw,in} + 0.0026T_{chw,in} + 0.0277\dot{m}_{hw} + 0.0034\dot{m}_{cw,bed} + 0.0150\dot{m}_{chw} + 0.0019\dot{m}_{cw,cond} + 2.0286 \times 10^{-6}UA_{bed} + 1.0279 \times 10^{-6}UA_{evap} + 6.8084 \times 10^{-8}UA_{cond} \quad (6)$$

with adjusted $R^2 = 0.8371$

Based on the objective functions from equations (2), (4) and (6), the decision variables and bounds are presented in Table 1.

Table 2. Decision variables and bounds.

Variable Description	Symbol	Range	Units
Hot water inlet temperature	$T_{hw,in}$	65 – 95	°C
Cooling water inlet temperature	$T_{cw,in}$	22 – 36	°C
Chilled water inlet temperature	$T_{chw,in}$	10 – 20	°C
Hot water mass flow rate	\dot{m}_{hw}	0.8 – 2.2	kgs ⁻¹
Bed cooling water mass flow rate	$\dot{m}_{cw,bed}$	0.8 – 2.2	kgs ⁻¹
Chilled water mass flow rate	\dot{m}_{chw}	0.2 – 1.4	kgs ⁻¹
Condenser cooling water mass flow rate	$\dot{m}_{cw,cond}$	0.8 – 2.2	kgs ⁻¹
Adsorbent bed overall thermal conductance	$U_{bed}A_{bed}$	2,000 – 10,000	W/K
Evaporator overall thermal conductance	$U_{evap}A_{evap}$	2,000 – 10,000	W/K
Condenser overall thermal conductance	$U_{cond}A_{cond}$	10,000 – 24,000	W/K

From the regression analysis equations of the selected variables (equations 2,4, and 6), the adjusted R^2 values of 0.8041 for COP, 0.9250 for Q_{cc} , and 0.8371 for η_e indicate that the chosen equations offer a good fit for the data. The high values of adjusted R^2 across all three objective functions (COP, Q_{cc} , and η_e) validate the suitability of the selected equations for modelling the relationships between the variables.

The regression equations will serve as the objective functions to be maximised using the Antlion Optimiser (ALO) and Multi-Objective Antlion Optimiser (MOALO) algorithms, with the decision variables bounded as presented in Table 1.

To eliminate occlusions inherent to static three-dimensional (3-D) Pareto fronts and perspective distortion, all Pareto solutions from MOALO are presented as two-dimensional (2-D) pairwise projections with a single marker colour for maximum clarity. It is important to emphasize that the observed trends reflect re-optimised Pareto points and may not correspond to the linear marginal coefficients.

2.4. Ant Lion Optimiser (ALO)

ALO is a single-objective optimizer algorithm. There is just one global optimum solution in single-objective optimisation due to the existence of only a single optimal solution and the unary objective in single-objective problems [19]. Antlions go through two main stages in their life cycle: larvae and adults. larvae mostly have a natural lifespan of three to five weeks, and the adults up to three years. They typically hunt as larvae and reproduce during their adulthood. To become adults, antlions undergo metamorphosis in a cocoon. Their unique hunting style and their favourite prey gave them their names. An antlion larva travels in a circle and throws out sand with its enormous jaws, digging a cone-shaped pit in the sand [25,26]. Figure 2 depicts multiple cone-shaped pits of varying diameters [27,28]. The antlion larva digs a cone-shaped trap and hides at the bottom, waiting for prey (ants) to be trapped. The cone's edge is sharp and easily traps the ant at the bottom. Should the prey attempt to flee, the antlion destabilizes it by flicking sand. Once captured, the prey is eaten underground, and the pit is cleared for the subsequent capture [29]. Interestingly, the hungrier the antlion, the larger the traps it digs [30] and/or when the moon is full [31]. Thus, the primary source of inspiration for the ALO algorithm comes from the foraging behaviour of antlions' larvae and emulates the interaction between antlions and ants in the trap [28].

Given that ants randomly travel when searching for food, a random walk is chosen to model the ants' movement as follows:

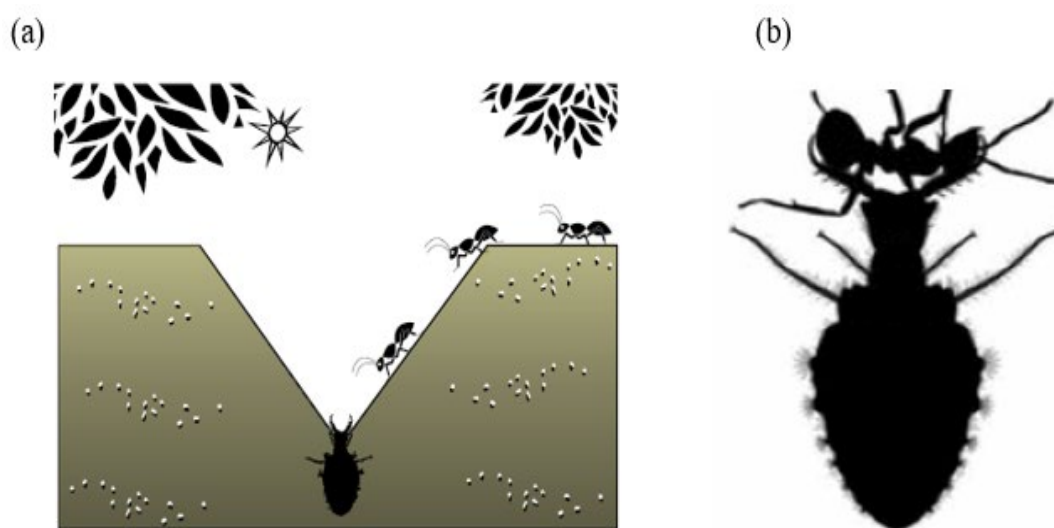


Figure 2. Cone-shaped traps and antlions' hunting behaviour.

$$Y(t) = [0, \text{cumsum}(2t(r_1) - 1), \text{cumsum}(2t(r_2) - 1), \dots, \text{cumsum}(2t(r_n) - 1)] \quad (7)$$

Equation (7) shows how the position vector, \vec{M} of antlions is calculated.

Here:

cumsum = cumulative summation operation

n = maximum number of epochs or iterations

r = the prey's step during a random walk

$t(r)$ is a stochastic function defined as:

$$t(r) = \begin{cases} 1 & \text{if } \text{rand} > 0.5 \\ 0 & \text{if } \text{rand} \leq 0.5 \end{cases} \quad (8)$$

where:

r = a single step within the iteration of the random walk process

rand = a randomly generated number with uniform distribution in the interval of [0, 1].

The position of the ants is stored in memory and used to guide the optimisation process in a matrix format as shown in equation (9):

$$M_{Ant} = \begin{bmatrix} A_{1,1} & A_{2,2} & \cdots & \cdots & A_{1,d} \\ A_{2,1} & A_{2,2} & \cdots & \cdots & A_{2,d} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ A_{n,1} & A_{n,2} & \cdots & \cdots & A_{n,d} \end{bmatrix} \quad (9)$$

where:

M_{Ant} = a matrix for storing the position of each ant

$A_{i,j}$ = value of the j^{th} variable of the i^{th} ant

n = number of ants

d = number of variables

Using the objective function $F(\cdot)$, each ant's decision vector is evaluated during optimisation and the resulting fitness values are stored in a column matrix as:

$$M_{OA} = \begin{bmatrix} F([A_{1,1} & A_{1,2} & \cdots & \cdots & A_{1,d}]) \\ F([A_{2,1} & A_{2,2} & \cdots & \cdots & A_{2,d}]) \\ \vdots \\ \vdots \\ F([A_{n,1} & A_{n,2} & \cdots & \cdots & A_{n,d}]) \end{bmatrix} \quad (10)$$

where:

M_{OA} = matrix for saving the fitness of each ant

$A_{i,j}$ = value of the j^{th} variable of the i^{th} ant

n = number of ants

d = number of variables

It is assumed the antlions hid in the search spaces, awaiting their prey. Their hiding positions and fitness values are saved in the matrices as equations (11) and (12), respectively:

$$M_{Antlion} = \begin{bmatrix} AL_{1,1} & AL_{2,2} & \cdots & \cdots & AL_{1,d} \\ AL_{2,1} & AL_{2,2} & \cdots & \cdots & AL_{2,d} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ AL_{n,1} & AL_{n,2} & \cdots & \cdots & AL_{n,d} \end{bmatrix} \quad (11)$$

$$M_{OAL} = \begin{bmatrix} F([AL_{1,1} & AL_{1,2} & \cdots & \cdots & AL_{1,d}]) \\ F([AL_{2,1} & AL_{2,2} & \cdots & \cdots & AL_{2,d}]) \\ \vdots \\ \vdots \\ F([AL_{n,1} & AL_{n,2} & \cdots & \cdots & AL_{n,d}]) \end{bmatrix} \quad (12)$$

where:

$M_{Antlion}$ = matrix holding the positional data for all antlions

M_{OAL} = matrix storing the fitness value of each antlion

$AL_{i,j}$ = value of the j^{th} dimension value of the i^{th} ant

n = total number of antlions

d = number of variables (dimensions)

F = objective functions

Conditions applied during optimisation are:

1. The ants explore the search space by random movements.
2. Random movements are applied to all dimensions of the ants
3. These random movements influence the traps set by the antlions
4. The size of the traps/pits built by the antlions is proportional to their fitness levels.
5. Antlions with large pits have a higher likelihood of trapping ants.

6. An elite (fittest) or random antlion is likely to catch an ant in each iteration.
7. An adaptive decrease in the range of the ants' random walks simulates the sliding of the ants towards the antlions.
8. An ant becoming fitter than the antlion implies that the ant is captured and drawn beneath the sand by the antlion.
9. After capturing the prey at each hunt, the antlion updates its position to align with the prey and digs a pit/trap to improve its chances of catching another prey.

2.4.1. Random Walks of Ants

Equation (8) is the basis of the random walks of ants. Ants update their positions at every stage of the optimisation process with random walks. To prevent random walks outside the search spaces, the min-max normalization scaling technique is used. This is given by:

$$Y_i^t = \frac{(Y_i^t - a_i) \times (d_i - c_i^t)}{(d_i^t - a_i)} + c_i \quad (13)$$

where:

a_i = minimum of the random walk of the i^{th} variable.

d_i = maximum of the random walk in the i^{th} variable

c_i^t = minimum of the i^{th} variable at the t^{th} iteration.

d_i^t = maximum of the i^{th} variable at the t^{th} iteration.

Equation (13) must be applied in each iteration to prevent random walks outside the search.

2.4.2. Building the Trap

A roulette wheel is used to model the antlion's hunting capabilities. As seen in Figure 3, the ant is assumed to be trapped by only one selected antlion. Thus, during the optimisation process, the roulette wheel operator in the ALO algorithm selects the antlions according to their fitness. This mechanism increases the fittest antlion's chance of capturing ants.

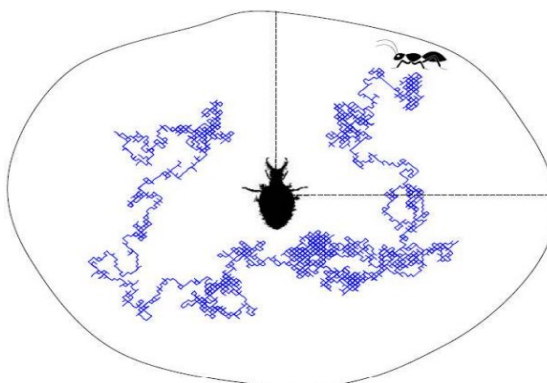


Figure 3. An ant walking randomly inside an antlion's trap.

2.4.3. Sliding Ants Towards the Antlion

Using the same roulette wheel mechanism, ants move arbitrarily, and antlions can build traps proportional to their fitness levels. Once the ant is trapped, the antlion throws sand towards the center of the pit, causing the trapped ant to slide down. This behaviour can be modelled mathematically by reducing the radius of the ant's hypersphere random movement and presented as equations (16) and (17).

$$c^t = \frac{c^t}{I} \quad (16)$$

$$d^t = \frac{d^t}{I} \quad (17)$$

where:

c^t = minimum variables at t^{th} iteration.

d^t = maximum variables at t^{th} iteration.

l = ratio

$$l = 10^w \frac{t}{T} \quad (18)$$

Where:

t = current iteration

T = maximum number of iterations

w = constant defined per the current iteration ($w = 1$ when $t > 0.1T$; $w = 3$ when $t > 0.5T$; $w = 4$ when $t > 0.75T$; $w = 5$ when $t > 0.9T$ and $w = 6$ when $t > 0.95T$)

2.4.4. Catching the Prey and Rebuilding the Pit

This is the final stage of the hunt. Here, the ant that falls to the bottom of the pit is trapped in the antlion's jaw and eaten up. From the eighth point in the conditions for optimisation, the prey is only caught when it becomes fitter than the antlion. Thus, the antlion needs to update its latest position to align with the hunted ant to improve its likelihood of catching new prey. In this regard, equation (19) follows as:

$$Antlion_j^t = Ant_i^t \quad \text{if } F(Ant_i^t) > F(Antlion_j^t) \quad (19)$$

where:

t = current iteration

$Antlion_j^t$ = position of the selected j^{th} antlion at the t^{th} iteration

Ant_i^t = position of the i^{th} ant at the t^{th} iteration

2.4.5. Elitism

Elitism is a fundamental characteristic of evolutionary algorithms that allows the storage of the best solution(s) obtained at every step of the optimisation process. For ALO, an elite refers to the best antlion saved from each iteration. This means the elite is the fittest antlion, so it should influence the movement of every ant during iterations. Therefore, it is assumed that the roulette wheel selects the antlion, and every ant randomly moves around the selected antlion and the elite concurrently, as depicted in equation (20) as:

$$Ant_i^t = \frac{R_A^t + R_E^t}{2} \quad (20)$$

where:

Ant_i^t = position of the i^{th} ant at the t^{th} iteration

R_A^t = random walk around the antlion chosen by the roulette wheel at the t^{th} iteration

R_E^t = random walk around the elite at the t^{th} iteration

2.5. Single-Objective Optimisation

The optimisation flowchart for the ALO for a single objective optimisation is illustrated in Figure 4. After initializing ants and antlions, fitness is evaluated, and the best antlion is set as the elite. For each iteration $t=T$, the Roulette wheel is used to select a guiding antlion, and the search bounds c , d are updated. Generate a normalized random walk around the selected antlion and elite, map it to the bounds c and d and update the ant's position to advance the loop index, i . Re-evaluate ants, let the fitter ant replace its paired antlion, and the elite if a better antlion is discovered. Repeat until $t = T$ and return the elite solution.

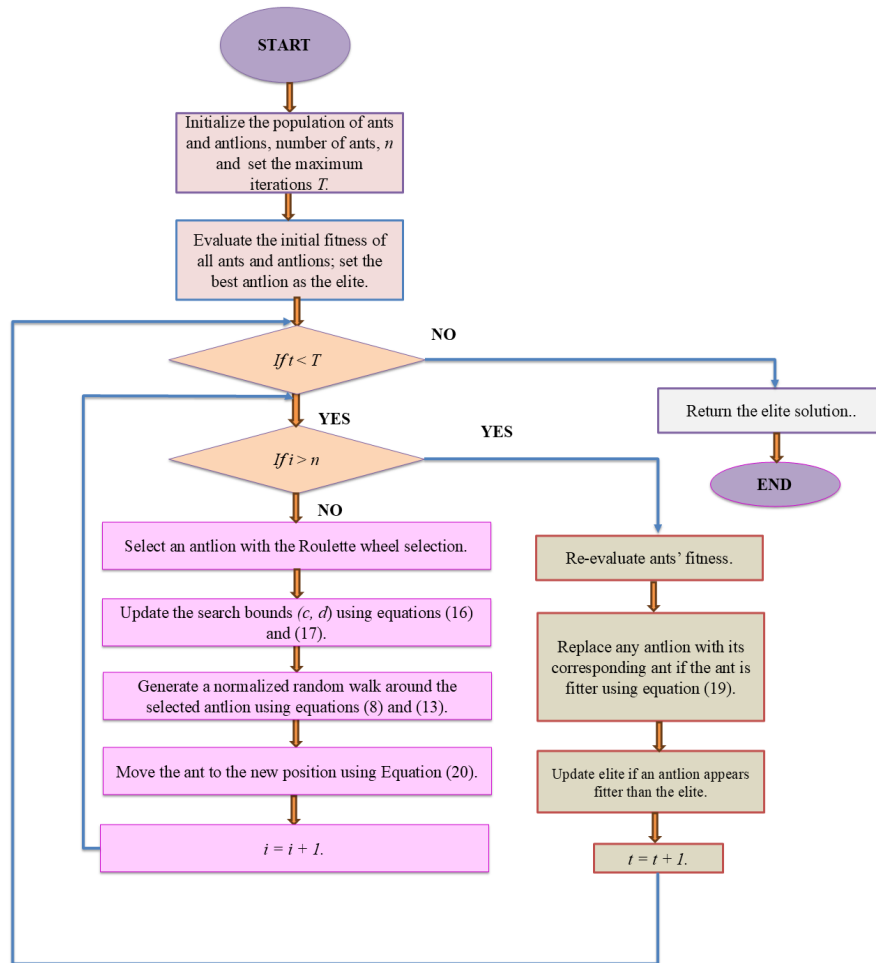


Figure 4. Flowchart of the single-objective Ant Lion Optimizer (ALO).

However, a problem can have multiple conflicting objective functions in energy systems. This will require a multi-objective optimisation approach to simultaneously generate viable solutions. The multi-objective antlion optimisation (MOALO), modelled after the multi-objective particle swarm optimisation (MOPSO), integrates a mechanism for archive management and leader selection. Solutions are selected from a pre-defined archive size to improve solution diversity. Using the niching technique, a specified radius is employed to study the area of each solution and count nearby solutions as a measure of distribution. This ensures well-spread solutions within the archive. MOALO adopts two strategies, like MOPSO, to further enhance the distribution of solutions.

Firstly, the antlion is selected based on the solution with the least crowded neighbourhood. Equation (21) determines the probability of selecting a particular solution from the archive [19].

$$P_i = \frac{c}{N_i} \quad (21)$$

c = constant value greater than 1

N_i = number of solutions in the neighbourhood for the i th solution.

The second strategy deletes solutions from the most crowded neighbourhood when the archive is full to make space for new solutions. Equation (22) is used to identify which solution is likely to be deleted from the archive.

$$P_i = \frac{N_i}{c} \quad (22)$$

Finally, equation (15) needs to be modified for multi-objective problems. Equation (17) must also be modified to select a non-dominated solution from the archive on the simultaneous selection of antlions and elites.

The flowchart for the resulting mathematical model for multi-objective ALO is shown in Figure 5. From Figure 5, the MOALO variant balances exploitation and exploration while preserving diversity using an external archive. At each iteration, the parent antlion and elites are pulled from the archive by the Roulette wheel selection. The ants take normalized walks around the selected antlion and the elite within adaptive bounds, advancing towards non-dominated regions. After each iteration, the newly found non-dominated solutions refresh and update the archive. When the archive is full, equation (21) is used to prune densely packed members to preserve spread along the Pareto front. The algorithm terminates at $t = T$ and returns the final nondominated archive, Pareto-optimal set.

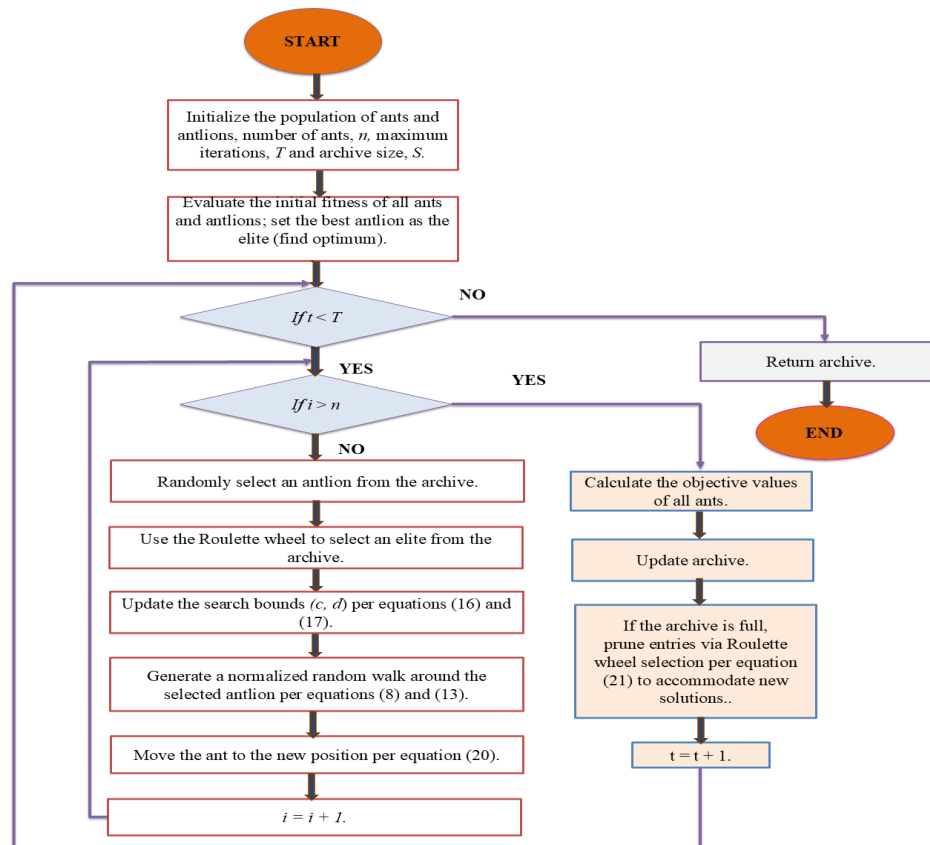


Figure 5. Workflow of the Multi-Objective Ant Lion Optimizer (MOALO).

2.6. Mathematical Formulation

The Ant Lion Optimiser (ALO) and its multi-objective version (MOALO) are utilised here to optimise the thermodynamic performance of a single-stage dual-bed silica gel–water ADC. ALO and MOALO are modelled on the hunting techniques of antlions in sand pits. Equations (2), (4) and (6) represent the regression-based models for the Coefficient of Performance (COP), Cooling Capacity (Q_{cc}), and Waste Heat Recovery Efficiency (η_e) [23]. ALO/MOALO employs a stochastic evolutionary approach that emulates ant–antlion interactions to explore and exploit the design space. The single-objective formulation of ALO optimises each objective independently.

- COP maximisation:

$$\mathcal{F}_1 = COP(T_{hw,in}, T_{cw,in}, T_{chw,in}, \dot{m}_{hw}, \dot{m}_{cw,bed}, \dot{m}_{chw}, \dot{m}_{cw,cond}, UA_{bed}, UA_{evap}, UA_{cond}) \quad (23)$$

Similarly, the optimisation of Cooling Capacity (Q_{cc}) is defined as:

- Cooling capacity maximisation:

$$\mathcal{F}_2 = Q_{cc}(T_{hw,in}, T_{cw,in}, T_{chw,in}, \dot{m}_{hw}, \dot{m}_{cw,bed}, \dot{m}_{chw}, \dot{m}_{cw,cond}, UA_{bed}, UA_{evap}, UA_{cond}) \quad (24)$$

- Waste heat recovery efficiency maximisation:

$$\mathcal{F}_3 = \eta_e(T_{hw,in}, T_{cw,in}, T_{chw,in}, \dot{m}_{hw}, \dot{m}_{cw,bed}, \dot{m}_{chw}, \dot{m}_{cw,cond}, UA_{bed}, UA_{evap}, UA_{cond}) \quad (25)$$

To preserve the diversity among solutions, MOALO extends the ALO framework by using Pareto dominance, elitism, and a crowding distance mechanism to converge toward a diverse and optimal set of non-dominated solutions.

The multi-objective formulation simultaneously combines the three objectives as equation (26):

$$\begin{aligned} & \text{Maximise } \mathcal{F} = \{\mathcal{F}_1, \mathcal{F}_2, \mathcal{F}_3\} & (26) \\ & \text{subject to the variable bounds:} \\ & 65 \leq T_{hw,in} \leq 95 \text{ [}^\circ\text{C]} \\ & 22 \leq T_{cw,in} \leq 36 \text{ [}^\circ\text{C]} \\ & 10 \leq T_{chw,in} \leq 20 \text{ [}^\circ\text{C]} \\ & 0.8 \leq \dot{m}_{hw} \leq 2.2 \text{ [kgs}^{-1}\text{]} \\ & 0.8 \leq \dot{m}_{cw,bed} \leq 2.2 \text{ [kgs}^{-1}\text{]} \\ & 0.2 \leq \dot{m}_{chw} \leq 1.4 \text{ [kgs}^{-1}\text{]} \\ & 0.8 \leq \dot{m}_{cw,cond} \leq 2.2 \text{ [kgs}^{-1}\text{]} \\ & 2000 \leq U_{bed}A_{bed} \leq 10000 \text{ [W/K]} \\ & 2000 \leq U_{evap}A_{evap} \leq 10000 \text{ [W/K]} \\ & 10000 \leq U_{cond}A_{cond} \leq 24000 \text{ [W/K]} \end{aligned}$$

3. Results

3.1. Single Objective Optimisation

The single-objective ALO algorithm implemented in this study was adapted from the original work by Mirjalili et al [32] which is available online. The algorithm was tailored to the characteristics of the three objective functions, the selected decision variables and implemented on the MATLAB R2021a platform using a 64-bit operating system, an x64-based processor, 8 GB RAM, and a 12th Gen Intel(R) Core (TM) i7-1255u CPU @ 1.70 GHz laptop.

Although the operating envelopes generated by ALO in this study are high, they are plausible given the sink and source temperatures and UA values. Depending on the design conditions, experimental single-stage silica-gel/water units generally report COP between 0.3 to 0.5 [33]. A review study on silica-gel water ADCs reported a COP of approximately 0.5 – 0.6 and beyond for optimized cases [34]. This validates the results from the SOO ALO of this study. The observed trends need not match the linear marginal coefficients since they reflect re-optimized Pareto set solutions.

The actions are to maximize each of the objectives discussed under setpoints, Loop flow controls, heat exchanger (HX) UA practices, and a prioritized sequence for constrained conditions.

3.1.1. Coefficient of Performance (COP) Maximization

The ALO algorithm was used to solve equation (23) to determine the conditions for maximum COP, using the decision variables and values presented in Table 2. Table 3 displays the optimum decision variables to maximise COP, Q_{CC} and η_e . Based on the ALO Maximize COP solution from Table 3; the following actions can be adapted to interpret the optimizer's choices into chiller-operable settings.

To achieve the optimal COP of 0.67412, the following control strategies were identified based on the direction of decision variables:

Setpoints to Target (COP Mode)

Moving the three temperature levers in the recommended favourable directions can immediately increase the COP.

- $T_{hw,in}$: increase toward 95 °C. Aim for the highest available driving temperature within limits [35].

- $T_{cw,in}$: minimize as cold as practicable (around 22 °C) using tower fan or flow [35].
- $T_{chw,in}$: increase to around 20 °C. A warmer chilled water setpoint can reduce lift [36]

Water-Loop Flows Setpoints

Driving the four water flow control loops towards the recommendations stated below can increase COP and UA effectiveness with diminishing returns. Flow meters with a Proportional Integral Derivative (PID) controller to command the Variable Frequency Drive (VFD) speed can be used to achieve each ALO specified flow rate.

- \dot{m}_{hw} : increase to around 2.20 kgs⁻¹ for stronger regeneration [37].
- $\dot{m}_{cw,bed}$: increase to around 2.20 kgs⁻¹ for better bed-side heat transfer [22].
- \dot{m}_{chw} : increase to around 1.40 kgs⁻¹ for stronger evaporator duty [22].
- $\dot{m}_{cw,cond}$: increase to approximately 2.20 kgs⁻¹ to ease heat dissipation [37].

Thermal Conductance (UA) Operational Levers

From Table 3, the ALO optimum shows high UA values. While UA is primarily design-fixed [22] effective UA depends on the following steps:

- maximize $U_{bed}A_{bed}$, $U_{evap}A_{evap}$, $U_{cond}A_{cond}$ or operate closer to high UA values [38].
- Open all HX circuits, balance flows and keep filters clean.
- Defoul evaporator and condenser surfaces on schedule.
- Maintain high tower airflow and adequate cooling water velocity.

Table 3. ALO single-objective optima for COP, Q_{cc} and η_e ; metrics on the right are the values for the same solution.

Optimization Objective	Decision Variable Values (from ALO)	Resulting COP [-]	Resulting Q_{cc} [kW]	Resulting η_e [-]
Maximize COP	$T_{hw,in} = 95^\circ\text{C}$, $T_{cw,in} = 22^\circ\text{C}$, $T_{chw,in} = 20^\circ\text{C}$, $\dot{m}_{hw} = 2.20 \text{ kgs}^{-1}$, $\dot{m}_{cw,bed} = 2.2 \text{ kgs}^{-1}$, $\dot{m}_{chw} = 1.4 \text{ kgs}^{-1}$, $\dot{m}_{cw,cond} = 2.2 \text{ kgs}^{-1}$, $U_{bed}A_{bed} = 10000 \text{ W/K}$, $U_{evap}A_{evap} = 10000 \text{ W/K}$, $U_{cond}A_{cond} = 24000 \text{ W/K}$	0.67412 (Max Value)	NR	NR
Maximize Q_{cc}	$T_{hw,in} = 95^\circ\text{C}$, $T_{cw,in} = 22^\circ\text{C}$, $T_{chw,in} = 20^\circ\text{C}$, $\dot{m}_{hw} = 2.20 \text{ kgs}^{-1}$, $\dot{m}_{cw,bed} = 2.135 \text{ kgs}^{-1}$, $\dot{m}_{chw} = 1.4 \text{ kgs}^{-1}$, $\dot{m}_{cw,cond} = 2.2 \text{ kgs}^{-1}$, $U_{bed}A_{bed} = 10000 \text{ W/K}$, $U_{evap}A_{evap} = 10000 \text{ W/K}$, $U_{cond}A_{cond} = 23999.66 \text{ W/K}$	NR	18.2235 (Max Value)	NR
Maximize η_e	$T_{hw,in} = 65^\circ\text{C}$, $T_{cw,in} = 22^\circ\text{C}$, $T_{chw,in} = 20^\circ\text{C}$, $\dot{m}_{hw} = 2.198 \text{ kgs}^{-1}$, $\dot{m}_{cw,bed} = 1.658 \text{ kgs}^{-1}$, $\dot{m}_{chw} = 1.396 \text{ kgs}^{-1}$, $\dot{m}_{cw,cond} = 1.244 \text{ kgs}^{-1}$	NR	NR	0.11829 (Max Value)

$$\begin{aligned}
 U_{bed}A_{bed} &= 10000 \text{ W/K}, \\
 U_{evap}A_{evap} &= 10000 \text{ W/K}, \\
 U_{cond}A_{cond} &= 23738.26 \text{ W/K}
 \end{aligned}$$

(NR = not reported here, sub-optimal at this solution since not the primary objective). COP and η_e are dimensionless [–].

Priority When Constrained (Most COP per Effort)

When it is impossible to achieve all targets (ambient and equipment limits), leverage the following steps for the biggest COP gain per step.

- $T_{cw,in}$: lower $T_{cw,in}$ to make the sink colder and reduce the tower approach to wet bulb.
- UA: increase all UA through cleaning HX or balancing flow.
- $T_{hw,in}$ and \dot{m}_{hw} : Push $T_{hw,in}$ and \dot{m}_{hw} further. Although this could reduce η_e , it can increase COP when sink and UA are in good shape.
- \dot{m}_{chw} : Fine-tune \dot{m}_{chw} . Too low \dot{m}_{chw} will starve the evaporator duty, and too high will reduce Logarithmic Mean Temperature Difference (LMTD), so it is better to stay near the ALO target of around 1.4 kgs^{-1} .

3.1.2. Cooling Capacity (Q_{cc}) Maximization

To identify the conditions for maximum Q_{cc} , the ALO algorithm was used to solve Equation (24) with the decision variables and values from Table 2. Table 4 displays the optimum decision variables to maximise Q_{cc} . To achieve a maximum Q_{cc} of 18.2235 kW, the following variable adjustments depicted in Table 3 are required.

Setpoints to Target (Q_{cc} Mode)

Moving the three temperature levers in the recommended favourable directions can immediately increase the Q_{cc} .

- $T_{hw,in}$: increase toward $95 \text{ }^\circ\text{C}$. Aim for the highest available driving temperature within limits [35,39].
- $T_{cw,in}$: minimize $T_{cw,in}$ (around $22 \text{ }^\circ\text{C}$) to reduce the condensation/adsorption process and boost Q_{cc} [37,39,40].
- $T_{chw,in}$: increase to around $20 \text{ }^\circ\text{C}$. This will reduce the temperature lift to increase Q_{cc} to its optimum [36,41].

Water-Loop Flows Setpoints

Driving the flow control loops towards the recommendations stated below can increase COP and UA effectiveness with diminishing returns.

- \dot{m}_{hw} : increase to around 2.20 kgs^{-1} for stronger regeneration [37].
- $\dot{m}_{cw,bed}$: increase to around 2.20 kgs^{-1} for better bed-side heat transfer [22].
- \dot{m}_{chw} : increase to around 1.40 kgs^{-1} increases the evaporator effectiveness to improve Q_{cc} up to diminishing returns [22,42].
- $\dot{m}_{cw,cond}$: Although optima may exist, increasing $\dot{m}_{cw,cond}$ to approximately 2.20 kgs^{-1} lowers the condensing temperature to enhance Q_{cc} [37].

Thermal Conductance (UA) Operational Levers

From Table 3, the ALO optimum shows high UA values. While UA is primarily design-fixed [22], effective UA depends on the following steps:

- maximize $U_{bed}A_{bed}$, $U_{evap}A_{evap}$, $U_{cond}A_{cond}$ or operate closer to high UA values [38].

Priority When Constrained (Most kW per Effort)

When it is impossible to achieve all targets (ambient and equipment limits), leverage the following steps for the biggest Q_{cc} gain per step.

- $T_{cw,in}$: lower $T_{cw,in}$ to reduce sink temperature [37,39,40].
- UA: increase all UA through cleaning HX or balancing flow.
- $T_{hw,in}$ and \dot{m}_{hw} : Increase $T_{hw,in}$ and \dot{m}_{hw} within limits to enhance the drive heat and increase Q_{cc} [35].
- \dot{m}_{chw} and $\dot{m}_{cw,cond}$: Raise \dot{m}_{chw} and $\dot{m}_{cw,cond}$ to increase evaporator throughput and lower condenser temperature, respectively. It is advisable to keep \dot{m}_{chw} close to the ALO target of around 1.4 kgs^{-1} . This can directly increase Q_{cc} [37].

3.1.3. Waste Heat Recovery Efficiency (η_e) Maximisation

Applying the ALO algorithm to Equation (25) with the decision variables and values from Table 2 yielded the results in Table 3. To achieve a maximum η_e of 0.11829 requires the following set points.

Setpoints to target (η_e mode)

Moving the three temperature levers in the recommended favourable directions can immediately increase the η_e .

- $T_{hw,in}$: reduce $T_{hw,in}$ toward $65 \text{ }^\circ\text{C}$ with other favourable settings to increase η_e . However, too low $T_{hw,in}$ weakens desorption to reduce η_e . This shows that to some extent, "higher is not always better" for η_e and there exists an optimum.
- $T_{cw,in}$: $T_{cw,in}$ should be low enough to keep the sink cold and support desorption, but not weaken it (around $22 \text{ }^\circ\text{C}$) [43].
- $T_{chw,in}$: increase $T_{chw,in}$ to around $20 \text{ }^\circ\text{C}$. This will reduce the temperature lift to increase η_e to its optimum [43].

Water-Loop flows setpoints

Combining the recommendations stated below with Proportional Integral Derivative (PID) and Variable Frequency Drive (VFD) speed flow meters can achieve each ALO specified flow rate to boost η_e .

- \dot{m}_{hw} : aim for moderate to high \dot{m}_{hw} ($2.198 - 2.20 \text{ kgs}^{-1}$) to sustain desorption at the lower $T_{hw,in}$ without "over-supplying" heat [35].
- $\dot{m}_{cw,bed}$: aim for a moderate flow rate (around 1.658 kgs^{-1}), just enough to maintain $U_{bed}A_{bed}$ without increasing the drive heat and number of transfer units (NTU), diminishing returns [44].
- \dot{m}_{chw} : increase \dot{m}_{chw} to around 1.40 kgs^{-1} increases the evaporator effectiveness to improve η_e up to diminishing returns [22,42].
- $\dot{m}_{cw,cond}$: moderate to low $\dot{m}_{cw,cond}$ (around 1.244 kgs^{-1}) to maintain consistent heat rejection and higher η_e [44].

Thermal Conductance (UA) Operational Levers

From Table 3, the ALO optimum shows high UA values. While UA is primarily design-fixed [22], effective UA depends on the following steps:

- $U_{bed}A_{bed}$ and $U_{evap}A_{evap}$: Keep $U_{bed}A_{bed}$ and $U_{evap}A_{evap}$ high around $10,000 \text{ kW/k}$. Better HX effectiveness directly relates to increased cooling for the same drive heat, thereby increasing η_e [44].
- $U_{cond}A_{cond}$: Optimum η_e is just below maximum $U_{cond}A_{cond}$, so run $U_{cond}A_{cond}$ only enough to increase the condenser NTU. Increasing $U_{cond}A_{cond}$ beyond that will mainly reduce condenser temperature and increase heat dissipation without a commensurate rise in η_e [44,45].
- Cleaning the condenser, adequate tube/channel velocity and balanced circuits can increase the effectiveness of UA without an excessive increment of the $U_{cond}A_{cond}$ operating values.



Priority When Constrained (Most η_e per Unit Drive Heat)

When it is impossible to achieve all targets (ambient and equipment limits), leverage the following steps for the biggest η_e gain per step.

- Enable a lower $T_{hw,in}$. Reduce the temperature lift by reducing $T_{cw,in}$ and increasing $T_{chw,in}$ [43]. Increasing $T_{chw,in}$ (within process limits) increases evaporating saturation pressure/temperature to reduce lift. The resulting LMTD is enough to maintain or slightly increase evaporator duty without suppressing η_e .
- $T_{hw,in}$: Aim for $T_{hw,in}$ between 65–75 °C at a minimum acceptable Q_{cc} . Efficiency has been reported to peak at moderate temperature drives [35].
- Set \dot{m}_{chw} at high, $\dot{m}_{cw,bed}$ moderate, $\dot{m}_{cw,cond}$ low to moderate and \dot{m}_{hw} moderate to high to η_e targets [42,44].
- Increase the effectiveness of UA through good housekeeping practices like opening all HX circuits to improve distribution, cleaning filters, descaling HXs to reduce fouling resistance and maintaining sensible water velocities to lift Reynolds number [44,45].

3.1.4. Conflicts in Single-Objective Optima (ALO)

From Table 4, the linear surrogate models indicate a monotone direction. Under box constraints, maximising a single objective drives all the positively signed coefficients to their upper bounds while dragging down all the negatively signed variables to their lower bounds. For instance, since $T_{hw,in}$ in shows opposite signs in

η_e versus COP/ Q_{cc} , the SOO optima are mutually incompatible and different. Varying $T_{hw,in}$ across its admissible bounds (65 - 95 °C) while holding other variables fixed, increased COP by +0.042 and Q_{cc} by +9.32 kW, while decreasing η_e by -0.009. This model-level antagonism necessitates an MOO approach to show a full Pareto front rather than isolating corner solutions.

Unlike MOALO, which constructs a Pareto front of all objectives [19], ALO conceals the continuous trade-off surface while exposing only the isolated extreme points of the decision variable bounds [28].

Table 4 reports the response model of the linear regression's directional preferences of each objective at its single-objective optimum in maximisation form. An upward arrow, "↑" indicates that the objective increases when the variable moves towards its upper bound and a downward arrow "↓" implies there is an improvement when the objective moves towards its lower bound. The conflicts column shows consensus, "✓" when all three objectives have the same direction and "≠" indicates conflict when at least one objective goes the opposite direction (e.g., ↑, ↑ ↓). For this model, $T_{hw,in}$ reduces η_e but increases COP and Q_{cc} , which is a conflict and requires a multi-objective (Pareto) treatment.

Table 4. Trend of Decision Variables under ALO-Based SOO.

Decision Variable	Symbol	COP	Q_{cc}	η_e	Conflict
Hot-water inlet temperature	$T_{hw,in}$	↑	↑	↓	≠
Cooling-water inlet temperature	$T_{cw,in}$	↓	↓	↓	✓
Chilled-water inlet temperature	$T_{chw,in}$	↑	↑	↑	✓
Hot-water mass flow rate	\dot{m}_{hw}	↑	↑	↑	✓
Bed cooling-water mass flow	$\dot{m}_{cw,bed}$	↑	↑	↑	✓
Chilled-water mass flow	\dot{m}_{chw}	↑	↑	↑	✓
Condenser cooling-water mass flow	$\dot{m}_{cw,cond}$	↑	↑	↑	✓
Bed overall conductance	$U_{bed}A_{bed}$	↑	↑	↑	✓
Evaporator overall conductance	$U_{evap}A_{evap}$	↑	↑	↑	✓
Condenser overall conductance	$U_{cond}A_{cond}$	↑	↑	↑	✓

Legend: ↑ increases at optimality; ↓ decreases; ≠ conflict.

Table 4 confirms that the best way to maximise one objective (e.g., η_e) differs from the optimal direction to maximise another (e.g., COP or Q_{cc}) for certain decision variables like $T_{hw,in}$ and \dot{m}_{hw} . This implies that no single set of operating parameters can simultaneously maximise all the three performance metrics. This necessitates determining the Pareto optimal solutions through multi-objective optimisation (MOO), such as the Multi-Objective Ant Lion Optimiser (MOALO). Using MOALO goes beyond merely finding isolated optimal points for individual objectives; it identifies a set of non-dominated solutions that represent the best trade-offs among these competing performance metrics [19].

3.2. Multi-Objective Optimisation

The multi-objective antlion optimisation algorithm implemented in this study was adapted from the original work by Mirjalili et al [46], which is available online. The algorithm was tailored to the characteristics of the three objective functions, the selected decision variables and implemented on the MATLAB platform using a 64-bit operating system, an x64-based processor, 8GB RAM, and a 12th Gen Intel(R) Core (TM) i7-1255u CPU@ 1.70 GHz laptop. The set values of the hyperparameters, as proposed by Mirjalili et al. [100] in the original MOALO algorithm, are provided in Table 5.

Table 5. Set values of the hyperparameters.

Hyperparameter	Value
Maximum Number of Iterations	100
Population Size (Number of Ants)	100
Number of Antlions	100
Archive Size	200
Search Space Dimension	10
Maximum Number of Iterations	100

3.2.1. Pairwise Pareto Front Trade-offs (2-D Projections)

Across the investigated bounds, the front is effectively one-dimensional (1-D) and collapses to form a ridge. Rather than a broad, multi-dimensional surface, the two-dimensional (2-D) plots show the data points as a narrow continuous linear curve. For panel (a), COP increases monotonically with Q_{cc} , yielding an almost continuous linear curve, whereas η_e is non-correlated with both capacity (panel b) and COP (panel c). Panels (b) and (c) show that η_e reduces as either COP or Q_{cc} increases, validating the plot in panel (a) and indicating a consistent trade-off between COP/cooling capacity and η_e . Altogether, the three projections demonstrate that aiming for a higher COP and Q_{cc} will be at the cost of η_e and vice versa. A practical design compromise is seen near the intersections of panels (a) to (c), as a balanced region is identified around COP \approx 0.695, $Q_{cc} \approx$ 24 kW, and $\eta_e \approx$ 0.122–0.123.

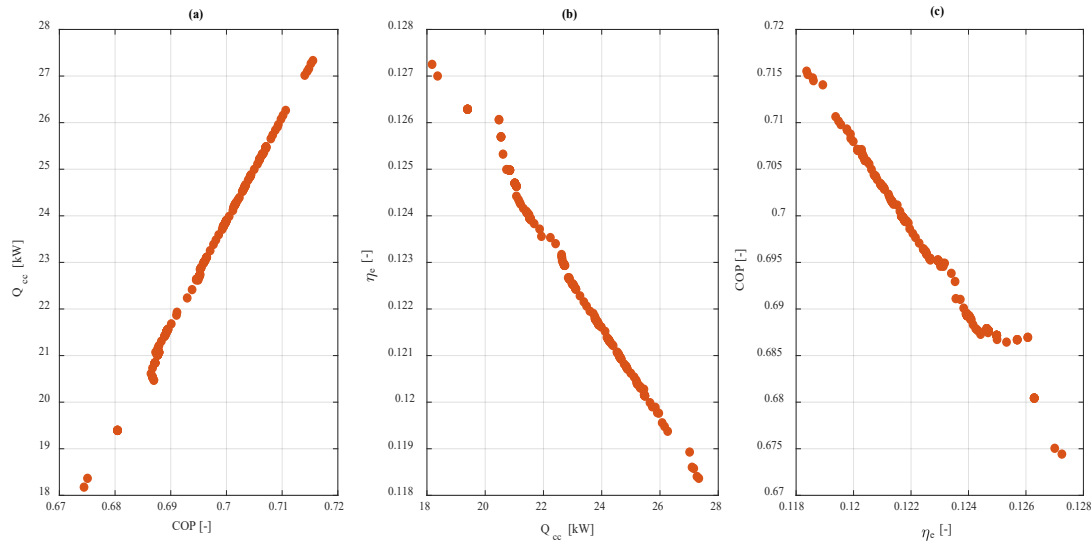


Figure 6. Pairwise 2-D projections of the MOALO non-dominated set ($N = 100$). (a) COP versus Q_{cc} ; (b) η_e vs Q_{cc} ; (c) COP vs η_e .

3.2.2. Validation of Objective Models and Pareto-Front Quality

Within the explored bounds, the COP, Q_{cc} , and η_e fronts compress towards an effective 1-D manifold because the objectives co-vary with the same hot-side driving temperature potential and heat-transfer conductance (UA). The performance of classic silica-gel/water systems ADCs is significantly affected by heat and mass flow rates [47], and both the COP and cooling capacity are very sensitive to operating water temperatures [48]. This coupling inherently results in a ridge-shaped front geometry. Nevertheless, a ridge-shaped front is expected because the objectives are correlated and partially redundant due to the degeneration of the Pareto fronts for such regimes [49,50]. This is why the results are presented in 2-D rather than 3-D to ensure the plots are clear and free from occlusion for quantitative comparison [47,49]. The observed trends in the 2-D projections are physically plausible and internally consistent with the working of silica-gel/water systems ADCs. Cooling capacity increases as hot water (desorption) temperature rises until an optimum efficiency, after which COP may decline [35,51–53]. As noted earlier, observed trends reflect re-optimized Pareto sets and do not necessarily correspond to linear marginal coefficients; therefore, moving from one Pareto-optimal solution to another indicates a trade-off [54,55].

All reported Pareto data points meet the imposed bound limits (temperatures, mass-flow rates, and UA products) and basic thermodynamics constraints, as the approach temperatures are realistic and there are monotonic responses to driving temperature and heat transfer area. There are no remaining infeasible or dominated points after re-evaluation [35].

Table 6 summarizes selected literature benchmarks for ADC performance and compares them with the MOALO Pareto set across COP, Q_{cc} , operating temperatures and system scale. The MOALO front yields COP from 0.69–0.71, Q_{cc} around 18–27.3 kW, and operating temperature from 65–95 °C for $T_{hw,in}$, $T_{cw,in}$ around 22 °C and 20 °C $T_{chw,in}$ aligning with reported values [56–59]. Even though η_e was derived from a prior formulation, it is seldom reported as a performance metric in ADC optimization. It is therefore reported explicitly for this MOALO Pareto solutions within the explored bounds as 0.118–0.1275 (11.8–12.75%) to provide a direct measure of utilization of waste heat for design and comparison. The reported ranges of η_e add useful context for future waste-heat integration studies while remaining consistent with the underlying thermodynamics principles. Overall, the reported literature aligns with the results from this study and supports the quality of the generated MOALO Pareto set and the reliability of the objectives.

Table 6. Comparison of Literature benchmarks studies for single-stage silica-gel/water ADCs versus this study's MOALO (This Work).

Parameter	Literature (Selected Anchors)	MOALO – This Work
COP range	Typical around 0.5–0.6 for single-stage silica-gel/water adsorption chillers; upper values ≤ 0.7 reported in manufacturer data [56,57]	Approximately 0.69–0.71 (Pareto set)
Q_{cc}	Laboratory or prototype report 2–10 kW [60]; product class 10 kW [57]; pilot/field 30–105 kW [58]; commercial 35–1180 kW [59]	Approximately 18–27.3 kW (Pareto set)
η_e	Seldom reported explicitly in product literature and many papers; emphasis typically on COP/capacity [61]	Approximately 0.118–0.1275 (11.8–12.75 %)
Operating temperatures	Single-stage silica-gel/water, typical temperature drive reviewed chilled-water temperature ranges 10–20 °C [56]	Envelope: $T_{hw,in} = 65\text{--}95$ °C; $T_{cw,in} \approx 22$ °C; $T_{chw,in} \approx 20$ °C
System context	Commercial silica-gel/water ADCs span tens of kW to >1 MW (35–1180 kW line) [59]	This work falls in the low-commercial or high-pilot scale.

3.3. Sensitivity Analysis

To assess the robustness of the MOALO results, a One-at-a-Time (OAT) approach sensitivity analysis (SA) was conducted to examine the impact of each decision variable on COP, Q_{cc} , and η_e . One variable was swept across the lower, midpoint, and upper bounds, while all other variables were held at their baseline values. For each OAT setting, the optimizer was re-run for twenty independent runs using the same hyperparameters to obtain a stable Pareto set [62,63]. After each run, the resulting non-dominated cloud of Pareto-optimal points for the objectives was summarized, with cubic polynomial fits. The trends are reported as three projections: Q_{cc} against COP, η_e against COP and η_e against Q_{cc} .

3.3.1. Effects of Varying Hot Water Inlet Temperature

Figure 7 illustrates the effects of $T_{hw,in}$ on the Pareto set. Three $T_{hw,in}$ levels are shown as 65 °C (low, blue circles), 80 °C (intermediate, red squares), and 95 °C (highest, green triangles). The markers represent the non-dominated solutions, and smooth curves are cubic fits drawn to guide the eye. In panel (a), COP increases with Q_{cc} across all $T_{hw,in}$. This shows a positive correlation between COP and Q_{cc} within the explored bounds, consistent with prototype and bench tests of silica-gel/water units [60,64].

For panels (b) and (c), η_e shifts upwards as $T_{hw,in}$ rises. Higher $T_{hw,in}$ usually improves the desorption process and increases the useful cooling per unit bed up to an intermediate optimum beyond which gains decline [60,65]. The η_e –COP relation is a concave curve with a maximum η_e occurring at a COP between 0.78 and 0.82, in line with the reported optimum driving temperature behaviour for silica-gel/water systems ADCs [60,66].

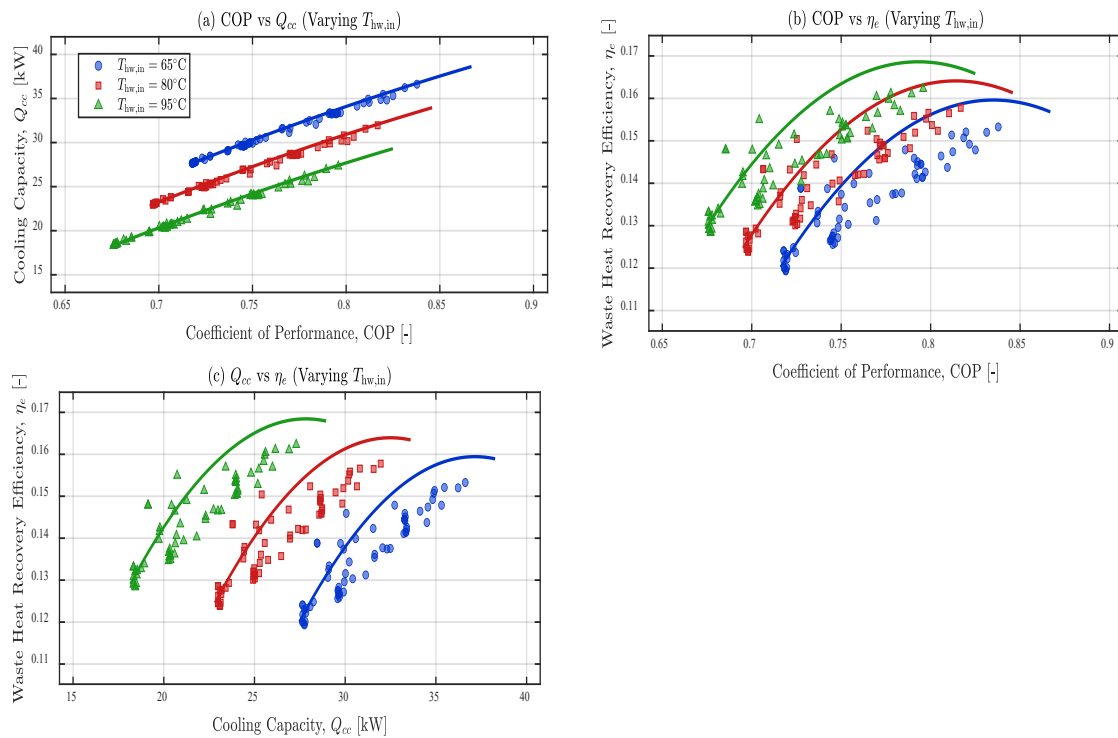


Figure 7. Sensitivity of the Pareto set to hot-water inlet temperature, $T_{hw,in}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

Panel (c) suggests diminishing returns in waste heat utilization as η_e initially increases with higher Q_{cc} , then saturates more prominently at 80–95 °C. Literature confirms that the performance of η_e declines beyond an optimum driving force at larger throughput [60,67]. Practically, datasheet operating windows support the use of 65–95 °C $T_{hw,in}$ for ADCs and highlights performance flattening at the upper end [68]

Within the MOALO envelope, if maximizing waste heat utilization is the priority, then the ADC should be operated at a higher $T_{hw,in}$ (80–95 °C) around the intermediate COP region where η_e peaks, as specified by the datasheet operating windows [68]. If cooling capacity is the main requirement, a trade-off is observed in panel (c) for Q_{cc} and η_e . Thus, 65 °C can deliver a higher Q_{cc} at the expense of η_e . Depending on the available source temperature, this study offers a balanced compromise around a COP of 0.80, with Q_{cc} between 28–34 kW and η_e , 0.150–0.170 at 95°C.

3.3.2. Effects of varying cooling water inlet temperature on the Pareto set

Figure 8 illustrates the effects of $T_{cw,in}$ on the Pareto set. Three OAT levels are shown as 22 °C (low, blue circles), 29 °C (intermediate, red circles), and 36 °C (highest, green circles). The markers represent the non-dominated solutions from re-optimised runs. In panel (a), Q_{cc} increases alongside COP for every $T_{cw,in}$ within the explored bounds. $T_{cw,in}$ clearly separates the Pareto clouds. The MOALO optimizer adjust the other degrees of freedom to compensate so the highest COP and Q_{cc} are observed at 36 °C, followed by 29 °C and 22 °C. In most fixed envelope silica-gel/water ADCs experimental settings, increasing $T_{cw,in}$ usually degrades Q_{cc} and COP, so the ordering of $T_{cw,in}$ here reflects re-optimization rather than a universal law [56,66,69,70].

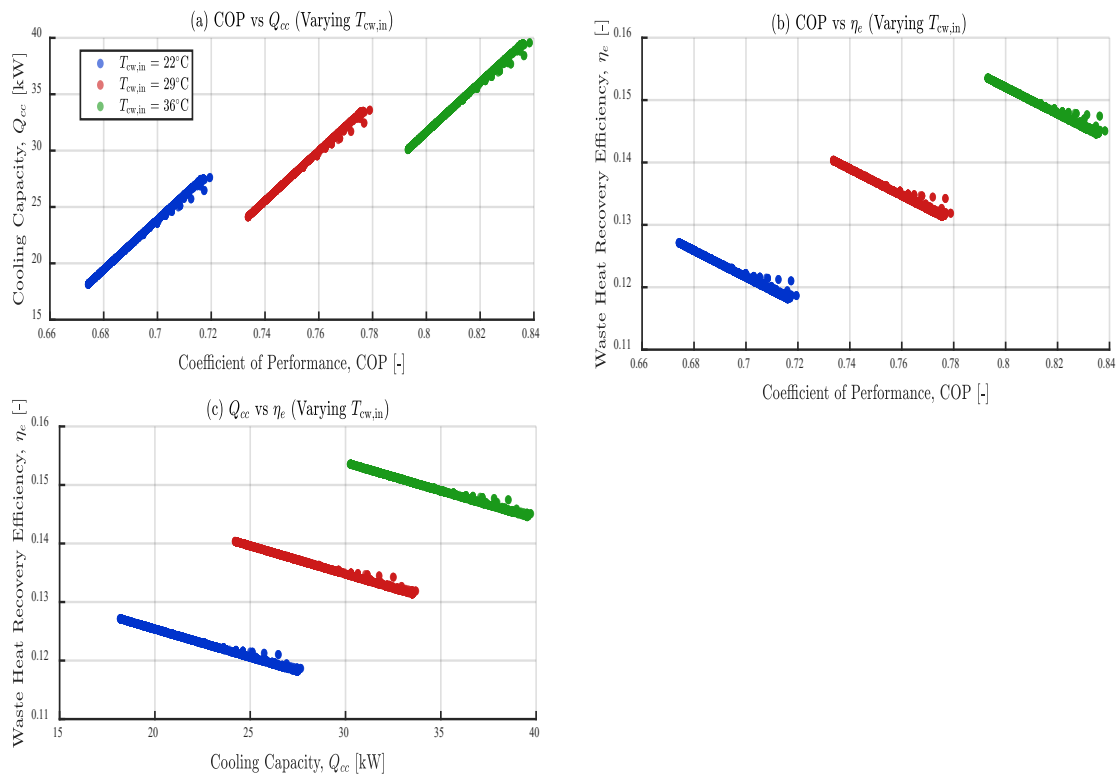


Figure 8. Sensitivity of the Pareto set to cooling water inlet temperature, $T_{cw,in}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

In panel (b), a negative correlation is observed within each level. η_e decreases as COP rises. The MOALO optimizer compensation shifts the entire η_e -COP curve upwards across all levels ($36^\circ\text{C} > 29^\circ\text{C} > 22^\circ\text{C}$). Under fixed conditions, increasing $T_{cw,in}$ is generally detrimental to the performance of the ADC [56,66,69]. The observed trends are specific to the explored bounds and OAT protocols, where the optimizer reallocates other variables as $T_{cw,in}$ varies. From panel (c), higher $T_{cw,in}$ corresponds to higher η_e across all levels, while η_e decreases with Q_{cc} .

Again, in these OAT runs, the MOALO optimizer adjusts responses to changes in $T_{cw,in}$. Thus, fixed-setting studies will report the opposite ordering when other variables are held constant [56,66,69,70]. These trends highlight the practical limitations and sensitivity to sink conditions as indicated in the datasheet windows [57,58,68].

In this MOALO envelope, a balanced design compromise is observed around COP 0.79–0.82, with Q_{cc} between 31 and 38 kW and η_e approximately 0.140–0.155.

3.3.3. Effects of Varying Chilling Water Inlet Temperature on the Pareto Set

Figure 9 illustrates the effects of $T_{chw,in}$ on the Pareto set. Three OAT levels are shown as 10°C (low, blue circles), 15°C (intermediate, red circles), and 20°C (highest, green circles). The markers represent the non-dominated solutions from re-optimised runs, and no curve fits are shown. In panel (a), Q_{cc} and COP increase together across all levels of $T_{chw,in}$. The fronts are ordered by $T_{chw,in}$. The highest $T_{chw,in}$ 20°C (blue), shows the highest COP- Q_{cc} , followed by 15°C (red) and 10°C (green). This ordering aligns with the behaviour of silica-gel/water ADC under fixed settings, where both COP and Q_{cc} improve due to a reduction in temperature lift from warmer chilled water law [56,60,69].

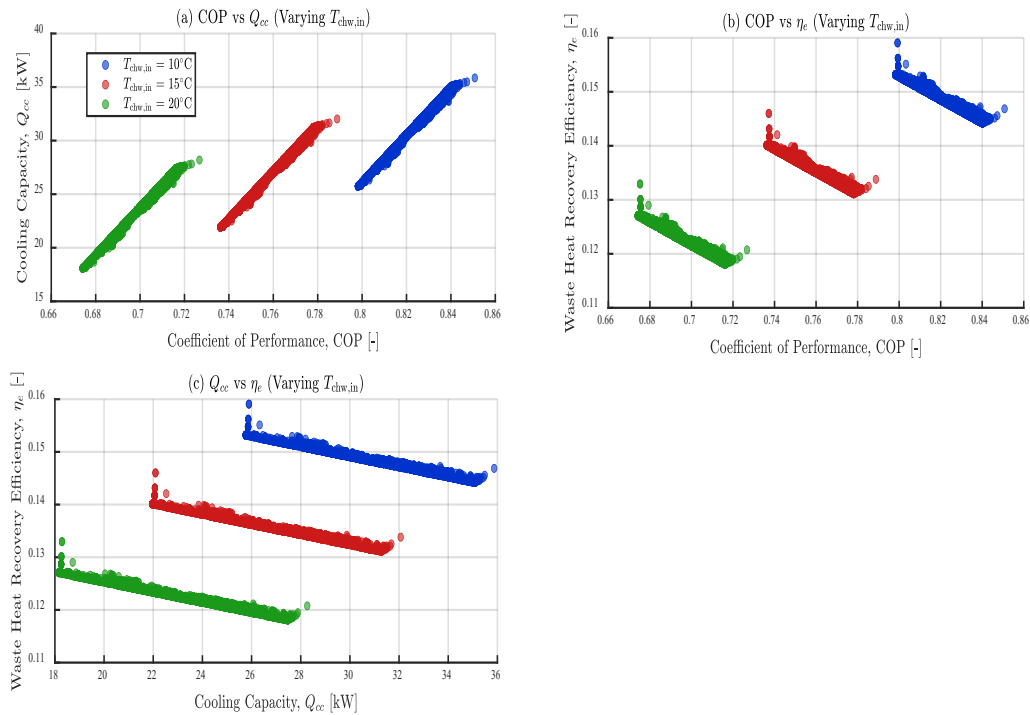


Figure 9. Sensitivity of the Pareto set to cooling water inlet temperature, $T_{chw,in}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

For panel (b), η_e slightly decreases as COP increases within each $T_{chw,in}$ level. Across levels, lower temperature lifts improve heat utilization at the hot side, so higher $T_{chw,in}$ swings the whole η_e -COP band upwards ($20^\circ\text{C} > 15^\circ\text{C} > 10^\circ\text{C}$) [56,66,69]. In panel (c), warmer chilled water produces higher η_e values, while η_e decreases with COP for each level of $T_{chw,in}$. Similar shifts and sensitivity of returning/leaving chilled water temperatures are documented in manufacturer datasheets [57,58,68].

For this MOALO study, the Pareto front is favourable for processes that can accept chilled water at higher temperatures to produce higher COP, Q_{cc} , and η_e . However, expect a reduction in the COP and η_e values if the requirement is a strict $T_{chw,in} = 10^\circ\text{C}$ set point. Within the explored bounds of this study, a practical compromise lies around a COP of 0.80, with Q_{cc} 29–35 kW and η_e 0.145–0.158.

3.3.4. Effects of Varying Hot Water Inlet Mass Flow Rate on the Pareto Set

Figures 10 (a-c) reveal how changing the hot water mass flow rate (\dot{m}_{hw}) at three different levels, 0.8 kgs^{-1} (black circles), 1.5 kgs^{-1} (orange squares), and 2.2 kgs^{-1} (green triangles), affects system performance. Panel (a) shows the COP against Q_{cc} across the tested flow rate range. The upper part of the plot is predominantly occupied by the highest-flow set ($\dot{m}_{hw} = 2.2\text{ kgs}^{-1}$, green triangles), suggesting a strong, positive linear correlation between COP and Q_{cc} , while the lowest-flow set ($\dot{m}_{hw} = 0.8\text{ kgs}^{-1}$, black circles) lies lower. However, the three MOALO clouds are tightly clustered.

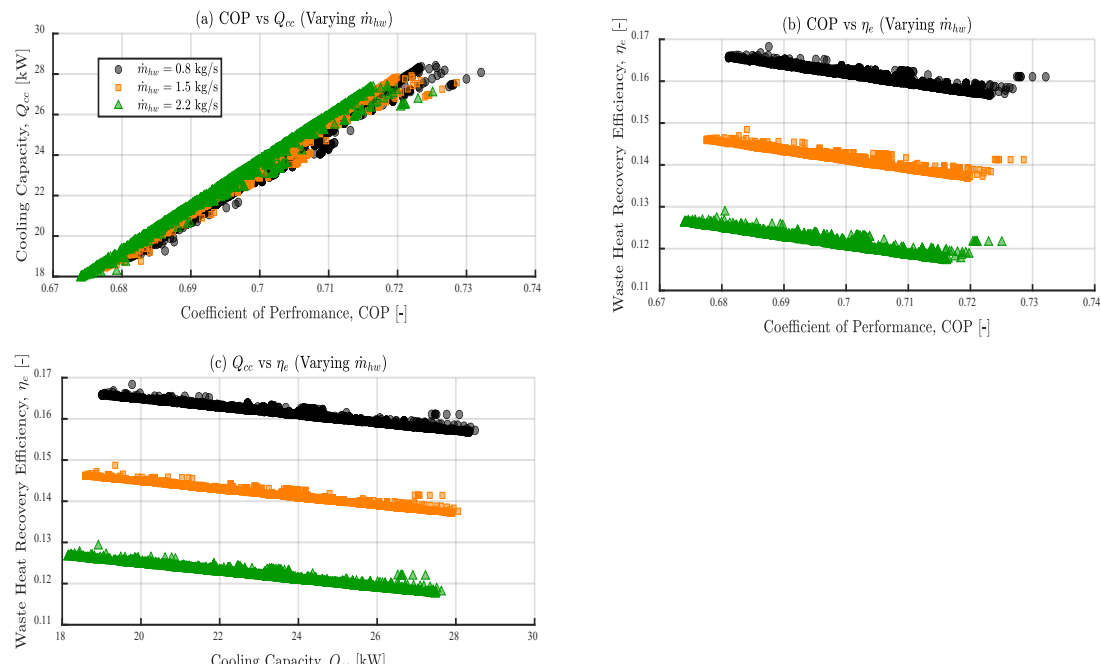


Figure 10. Sensitivity of the Pareto set to cooling water inlet temperature, \dot{m}_{hw} . Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

This indicates that the hot water mass flow rate has weak leverage on the core COP- Q_{cc} performance within the tested envelope. This agrees with Kalawa et al [71], who found that increasing the mass flow rate marginally improves COP/ Q_{cc} , albeit improving operational stability.

Theoretically, higher \dot{m}_{hw} improves heat transfer and desorption rate in silica gel-water ADC systems [24]. But, this MOALO optimizers likely compensate via other degrees of freedom, resulting in the observed weak sensitivity. Panel (b) shows η_e against COP, and panel (c) η_e against Q_{cc} . The plots show clear stratification based on the flow rate. η_e decreases as COP or Q_{cc} increases within each flow rate level. There is a significant monotonic decline in η_e as \dot{m}_{hw} increases across each level ($\dot{m}_{hw} : 0.8 > 1.5 > 2.2 \text{ kg s}^{-1}$). Theoretically, a higher \dot{m}_{hw} quickens the desorption process, resulting in a faster cooling cycle and potentially better cooling performance [24]. Nevertheless, they can also intensify irreversibilities and increase entropy generation, leading to losses in useful energy that decrease the quality of η_e [72]. This results in a trade-off: modest COP or Q_{cc} gains at high \dot{m}_{hw} at the cost of lower η_e . These trends mirror reoptimized solutions and are specific to this envelope. Operate at a lower \dot{m}_{hw} when waste heat is costly or limited to maintain a high η_e at a smaller Q_{cc} . A higher \dot{m}_{hw} is preferable if Q_{cc} is the limiting factor but expect a lower η_e . A practical compromise for a reasonable Q_{cc} and moderate η_e is to use the mid-flow level (1.5 kg s^{-1}) near the mid-COP region.

3.3.5. Effects of Varying Bed Cooling Water Mass Flow Rate on the Pareto Set

Panels (a-c) show the effects of bed cooling water mass flow on the Pareto set at three levels: 0.8 kg s^{-1} (black circles), 1.5 kg s^{-1} (orange squares), and 2.2 kg s^{-1} (green triangles). Markers represent non-dominated solutions.

Panel (a) Q_{cc} against COP shows an improvement in the ADC's primary cooling performance as $\dot{m}_{cw,bed}$ increase. The lowest performance occurs at the lower region ($\dot{m}_{cw,bed} = 0.8 \text{ kg s}^{-1}$), while the highest-flow band ($\dot{m}_{cw,bed} = 2.2 \text{ kg s}^{-1}$) occupies the upper region, with COP up to 0.73 and Q_{cc} around 28.5 kW. This is thermodynamically reasonable, as a higher bed cooling water mass flow facilitates effective removal of adsorption heat. This reduces the bed pressure during adsorption and maintains vapour uptake to increase throughput. Consequently, COP increases with Q_{cc} but with diminishing returns at higher flow rates [24].

Conversely, panels (b) η_e against COP and (c) η_e against Q_{cc} shows a decrease in waste heat efficiency (η_e) at higher $\dot{m}_{cw,bed}$ both within and across all levels. Maximum η_e occurs at the lowest flow rate (0.8 kgs⁻¹), while the highest flow rate (2.2 kgs⁻¹) results in the lowest η_e . At higher mass flow rates, the cooling water stream effectively dissipates more heat, but this increases irreversibilities too. Therefore, the quality of waste-heat utilisation falls even if Q_{cc} improves [24,72].

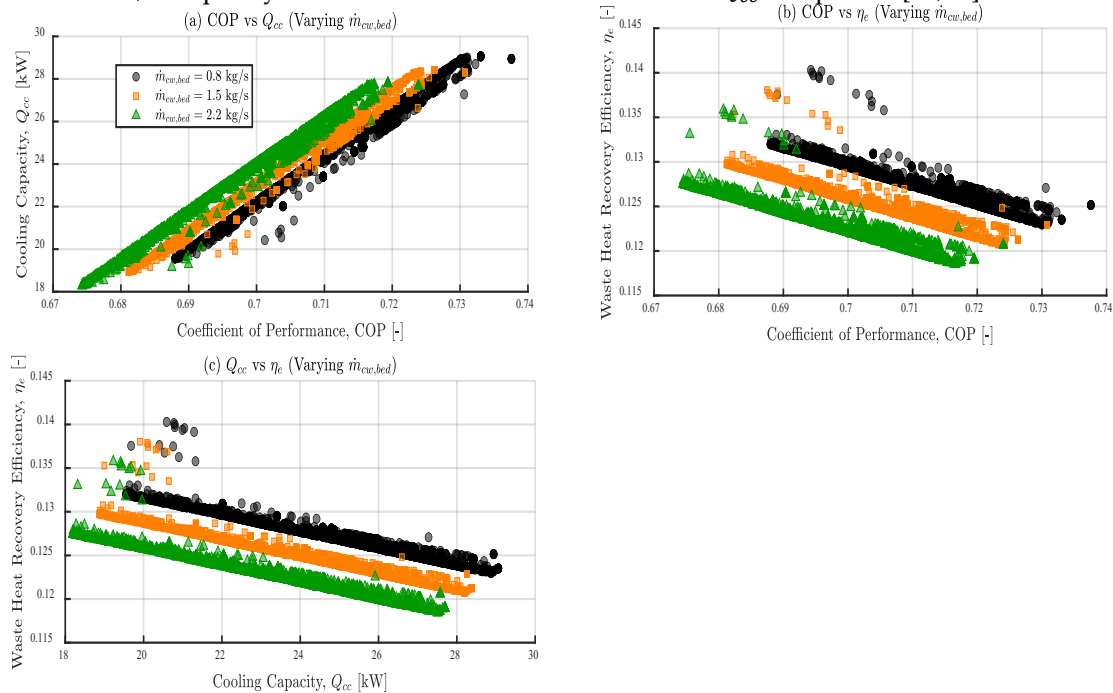


Figure 11. Sensitivity of the Pareto set to cooling water inlet temperature, $\dot{m}_{cw,bed}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

For these MOALO settings, increasing or decreasing $\dot{m}_{cw,bed}$ can maximize or reduce Q_{cc} or η_e , respectively. Therefore, choose $\dot{m}_{cw,bed}$ based on the required design outcome. A balanced compromise occurs at the intermediate flow case ($\dot{m}_{cw,bed}=1.5$ kg s⁻¹) around mid-COP between 0.70–0.72 for a moderate Q_{cc} with only a slight drop in η_e .

3.3.6. Effects of Varying Chilled Water Inlet Mass Flow Rate on the Pareto Set

Panels (a-c) show the effects of chilled water mass flow on the Pareto set at three levels: 0.2 kgs⁻¹ (black circles), 0.8 kgs⁻¹ (orange squares), and 1.4 kgs⁻¹ (green triangles). Markers are non-dominated solutions.

Panel (a) shows Q_{cc} against COP. The lowest \dot{m}_{chw} (0.2 kgs⁻¹) corresponds to the highest COP values (0.78 to 0.83) and the highest Q_{cc} (28 to 32 kW). The intermediate \dot{m}_{chw} (0.8 kgs⁻¹) shows mid-point values for both COP and Q_{cc} . And the least COP and Q_{cc} values are observed at high \dot{m}_{chw} (1.4 kgs⁻¹). Although increasing \dot{m}_{chw} generally improves heat transfer, the plots show the existence of a low to mid flow optimum on the evaporator side and going beyond that can have detrimental effects on the off-design operation of the components. Sah et al reported a near-flat trend of performance metrics at higher chilled water flow rates and improvement at low to moderate flow rates, indicating diminishing returns and an implied optimum [40].

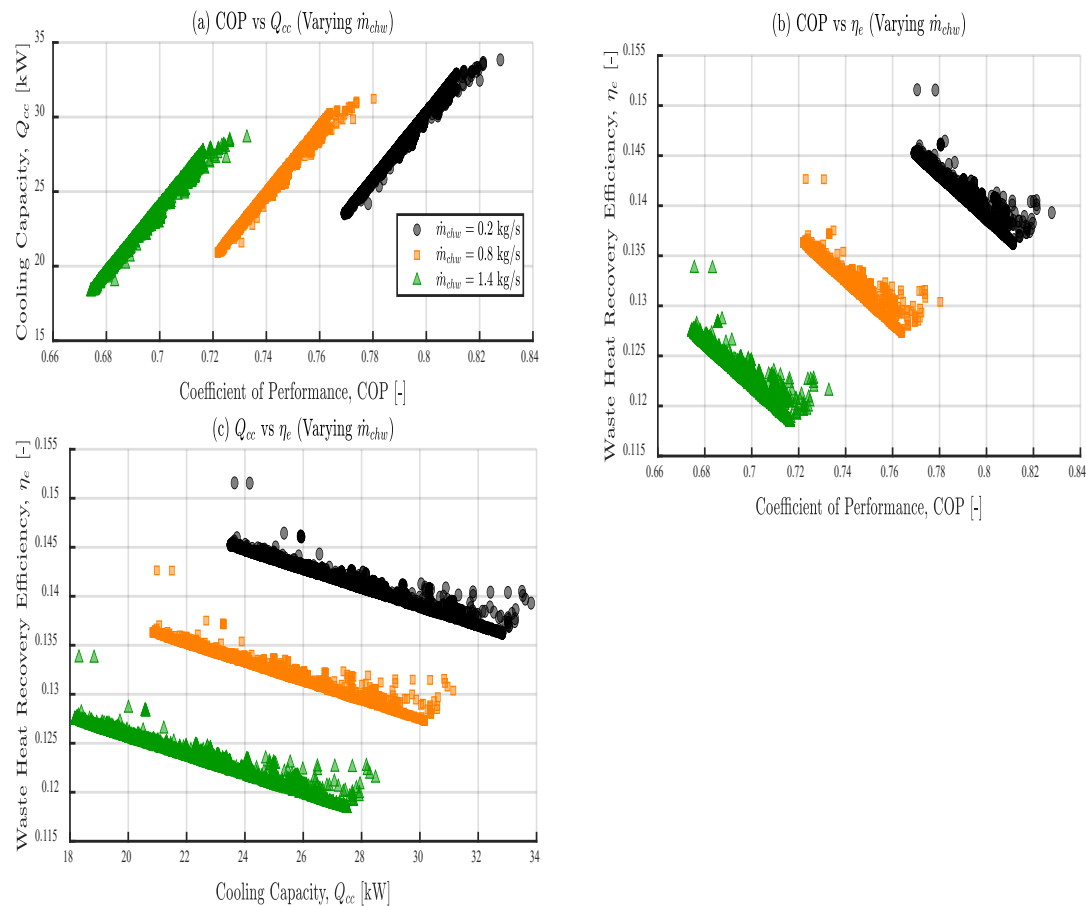


Figure 12. Sensitivity of the Pareto set to chilling water mass flow, \dot{m}_{chw} . Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

Panels (b) η_e against COP and (c) η_e against Q_{cc} . An inverse relationship is observed between η_e and COP or Q_{cc} within each level. η_e decreases as COP or Q_{cc} increases. Raising the chilled-water flow from 0.8 to 1.4 kg s^{-1} produced a lower COP and Q_{cc} . This is due to operating beyond the evaporator-side optimum, where the bedside heat/mass-transfer limits the performance. Beyond the optimal operating conditions, the effective LMTD/residence time reduces, declining evaporative duty cycle per cycle as increasing flow rate causes a marginal rise in thermal conductance. This behaviour is consistent with the finite time module and bed transport limits characteristics of adsorption modules [44,73] and saturation of gains at higher mass flow rates [20].

Within the explored bounds, choosing low to mid \dot{m}_{chw} when COP and Q_{cc} are the priorities can preserve η_e . However, operating at very \dot{m}_{chw} pushes the ADC beyond the evaporator-side optimum and penalizes both COP and η_e . Practically, a balanced compromise will be to run \dot{m}_{chw} at 0.8 kg s^{-1} close to COP of 0.76–0.80.

3.3.7. Effects of Varying Condenser Cooling Water Mass Flow Rate on the Pareto Set

Panels (a-c) show the effects of condenser-cooling mass flow on the Pareto set at three levels: 0.8 kg s^{-1} (black circles), 1.5 kg s^{-1} (orange squares), and 2.2 kg s^{-1} (green triangles). Markers are non-dominated solutions, and other variables are held at baseline and reoptimized.

Panel (a) Q_{cc} against COP. A clear positive coupling is observed for Q_{cc} and COP. Increasing $\dot{m}_{cw,cond}$ shifts the entire cloud upwards and Q_{cc} increases with COP. An increase in $\dot{m}_{cw,cond}$ improves heat dissipation from the condenser and reduces the average condensing temperature (smaller lift). This raises the Q_{cc} at a given COP. A modest separation is identified with diminishing returns at the highest $\dot{m}_{cw,cond}$. This is consistent with off-design limits and sink-side improvements characteristics for silica-gel/water ADCs [56,69].

Panel (b) shows η_e against COP, and (c) η_e against Q_{cc} . An inverse relationship is seen for η_e and $\dot{m}_{cw,cond}$ across all levels, while η_e decreases with COP or Q_{cc} as $\dot{m}_{cw,cond}$ increases within each level.

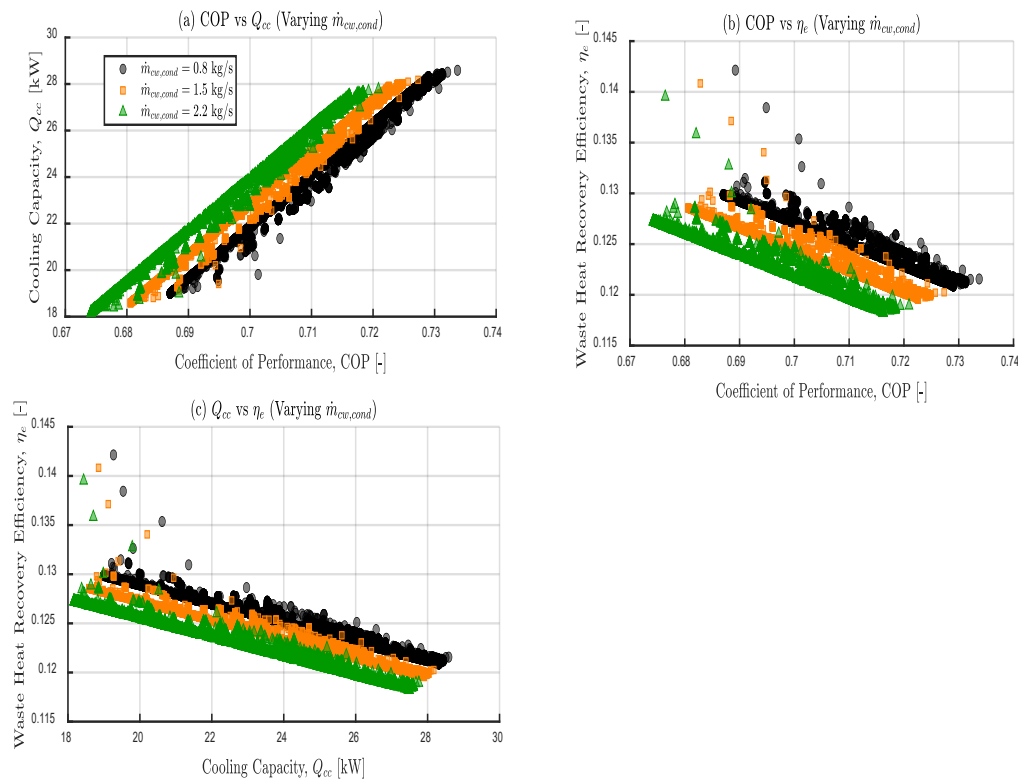


Figure 13. Sensitivity of the Pareto set to condenser cooling water mass flow, $\dot{m}_{cw,cond}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

Similarly to the $\dot{m}_{cw,bed}$ case, rejecting more heat in the sink increases entropy generation and thus, the quality of waste heat used falls while COP or Q_{cc} improves [40,56,72].

If Q_{cc} is the ADC's priority, then a higher $\dot{m}_{cw,cond}$ is beneficial, and if η_e is the main requirement, then a lower $\dot{m}_{cw,cond}$ is most preferable. Within the explored envelope, operating $\dot{m}_{cw,cond}$ at mid flow (1.5 kg s⁻¹) near the mid COP is a good compromise, which gives higher Q_{cc} at a moderate η_e penalty.

3.3.8. Effects of Varying Bed Overall Conductance on the Pareto Set

Panels (a-c) show the effects of overall bed thermal conductance on the Pareto set at three levels: 2,000 W/K (low, purple circles), 6,000 W/K (mid, teal diamonds), 10,000 W/K (high, red squares). Markers are non-dominated solutions, and other variables are held at baseline and reoptimized for each level.

Panel (a) shows Q_{cc} against COP. The three bands are almost parallel and increasing $U_{bed}A_{bed}$ shifts the cloud up and to the right to yield a higher COP at a given Q_{cc} and a higher Q_{cc} at a given COP. Physically, a higher UA increases the effectiveness of removing heat of adsorption.

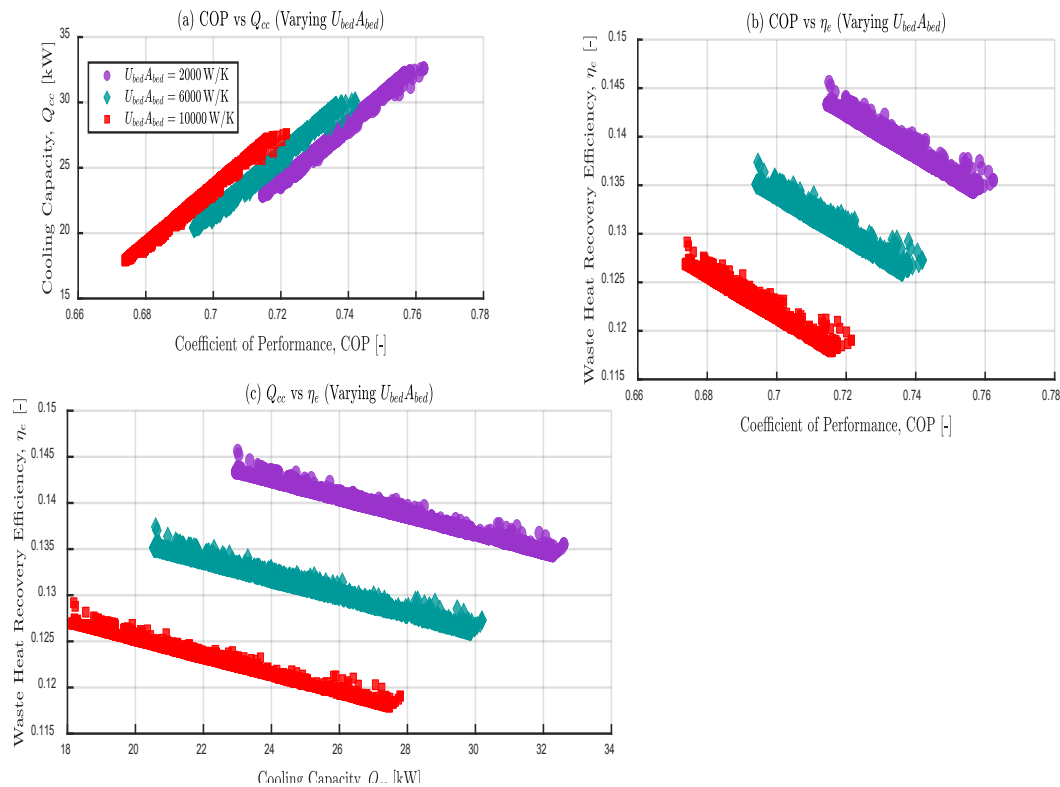


Figure 14. Sensitivity of the Pareto set to bed overall conductance, $U_{bed}A_{bed}$.

Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc}

This improves regeneration and reduces bed temperature during adsorption and temperature swings during desorption to increase the cycles' Q_{cc} and COP [24,52,56,74].

Panel (b) shows η_e against COP, and panel (c) shows η_e against Q_{cc} . Within each $U_{bed}A_{bed}$ lever, η_e reduces as COP or Q_{cc} rises but increases monotonically with $U_{bed}A_{bed}$ across all levels. Larger UA reduces the temperature approach differences, thereby reducing irreversibilities and improving the quality of heat utilization [72,74,75].

However, the spacing between each band narrows at high $U_{bed}A_{bed}$, suggesting internal limitations and diminishing of gains once the external HX resistance reduces [24,76].

Within the explored bounds, increasing $U_{bed}A_{bed}$ raises COP, Q_{cc} and η_e until internal limits set in. Practically, a balanced compromise will be at the mid to high $U_{bed}A_{bed}$ range of 6000–10000 W/K near the mid-COP region, which yields high Q_{cc} with a good η_e . Pushing $U_{bed}A_{bed}$ above 10000 W/K only improves Q_{cc} slightly relative to the size and/or cost constraints.

3.3.9. Effects of Varying Condenser Overall Conductance on the Pareto Set

Panels (a-c) illustrate the influence of condenser overall conductance on the Pareto set at three levels: 10,000 W/K (low, purple circles), 17,000 W/K (mid, teal diamonds), 24,000 W/K (high, red squares). Markers represent non-dominated solutions, with other variables held at baseline and reoptimized for each level.

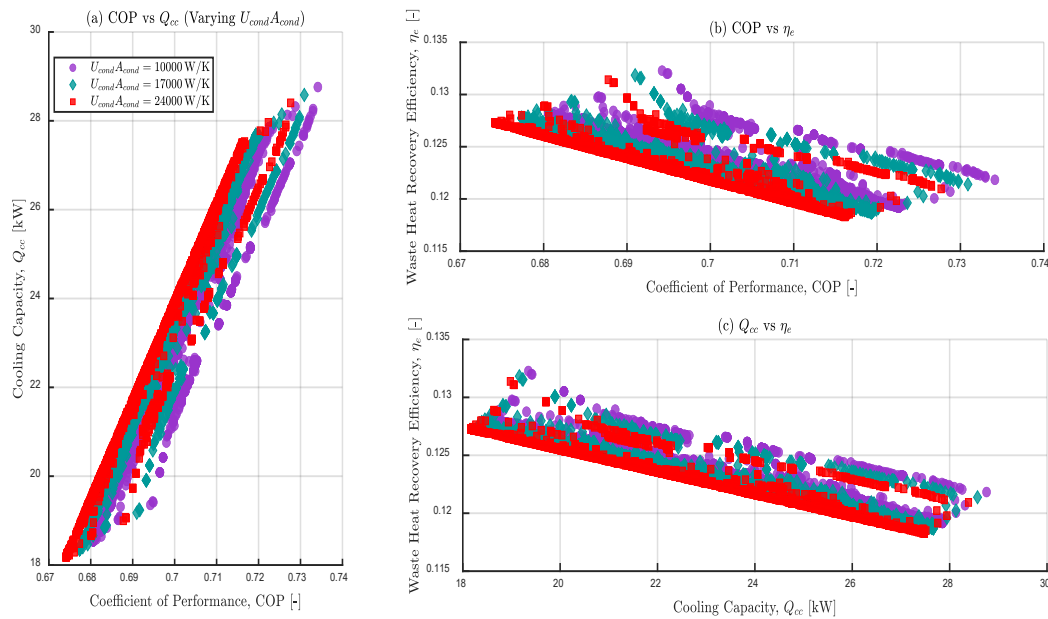


Figure 15. Sensitivity of the Pareto set to condenser overall conductance, $U_{cond}A_{cond}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

Panel (a) shows Q_{cc} against COP. The plots reveal three nearly parallel bands that shift upward and to the right as $U_{cond}A_{cond}$ increases. COP slightly improves for a given Q_{cc} , while Q_{cc} significantly increases for a given COP. Higher condenser UA reduces heat rejection, lowers the mean condensing temperature, and raises both Q_{cc} and COP [24,52,74]. The narrow spacing between bands at high $U_{cond}A_{cond}$ indicates diminishing returns.

Panel (b) depicts η_e versus COP, and panel (c) shows η_e against Q_{cc} . In each band, η_e decreases as COP or Q_{cc} rises. An inverse relationship exists between η_e and $U_{cond}A_{cond}$, because increasing $U_{cond}A_{cond}$ results in more heat being dumped into the sink, raising entropy generation. Therefore, although Q_{cc} improves, the quality of waste heat utilisation (η_e) declines [72,74].

When cooling capacity is paramount, a higher $U_{cond}A_{cond}$ is the optimal choice. Conversely, if waste heat utilisation is the priority, low to moderate $U_{cond}A_{cond}$ should be preferred to preserve η_e . For this envelope, if the design requires high Q_{cc} with a moderate penalty on η_e , $U_{cond}A_{cond}$ around 17000 W/K near the mid COP region would be a good compromise.

3.3.10. Effects of Varying Evaporator Overall Conductance on the Pareto Set

Panels (a-c) illustrate the influence of evaporator overall conductance on the Pareto set at three levels: 2,000 W/K (low, purple circles), 6,000 W/K (mid, teal diamonds), 10,000 W/K (high, red squares). Markers are non-dominated solutions, with other variables held at baseline and re-optimised for each level.

Panel (a) shows three nearly parallel bands that shift upward for Q_{cc} against COP as $U_{evap}A_{evap}$ decreases from 10,000 W/K to 6,000 W/K to 2,000 W/K. That is, for a given Q_{cc} , there is a moderately higher COP, and for a given COP, there is a noticeably higher Q_{cc} at lower $U_{evap}A_{evap}$. This implies that within this envelope, the evaporator is not the active bottleneck after re-optimisation, but MOALO compensate by reallocating the high-side temperatures and flow rates (other degrees of freedom) for a slightly lower COP and Q_{cc} at higher $U_{evap}A_{evap}$. A higher $U_{evap}A_{evap}$ usually raises the evaporation temperature (reduces lift) to increase Q_{cc} [24,52,74].

Panel (b) is η_e against COP. η_e reduces as COP increases within each band in the order of 2,000 W/K, 6,000 W/K and 10,000 W/K across the band. High $U_{evap}A_{evap}$ increases throughput and total heat dissipated to the sink, but raises irreversibilities, which lowers the quality of waste heat utilization [72,74].

Panel (c) displays η_e against Q_{cc} , following the same pattern as panel (b). η_e decreases as Q_{cc} increases within the bands across all levels. This reveals the inherent trade-offs between Q_{cc} and η_e . Raising $U_{evap}A_{evap}$ to 10,000 W/K results in diminishing returns on the re-optimised Pareto front due to compensation. Thus, a good compromise for this OAT envelope is lower to mid $U_{evap}A_{evap}$ (2000–6000 W/K) near the mid COP region for a higher Q_{cc} at a comparatively higher η_e .

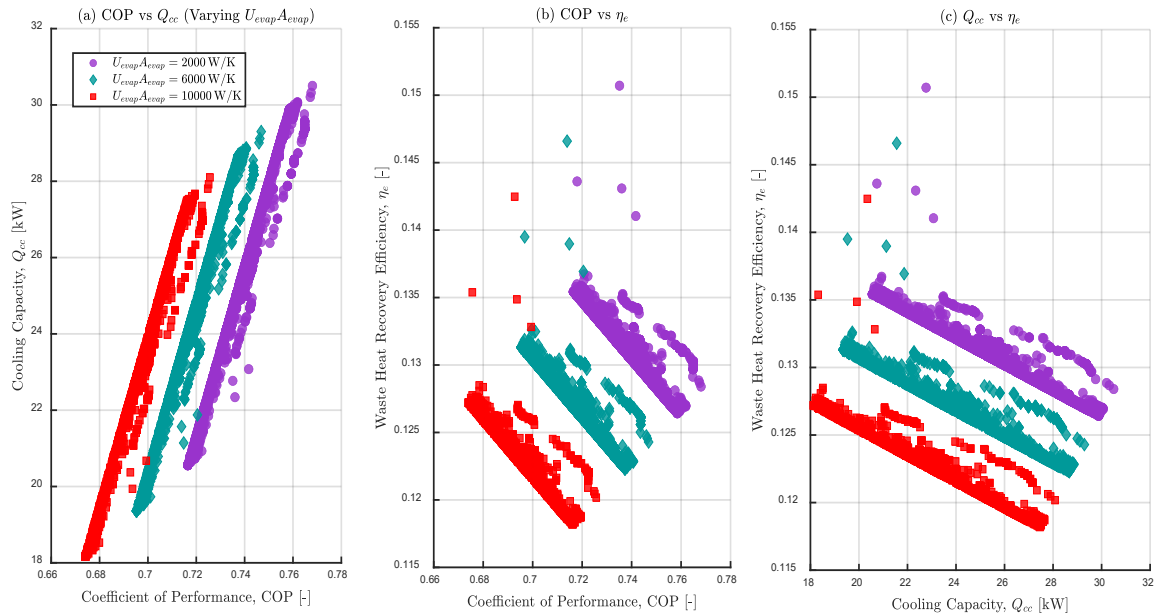


Figure 16. Sensitivity of the Pareto set to evaporator overall conductance $U_{evap}A_{evap}$. Panels: (a) Q_{cc} versus COP; (b) η_e versus COP; (c) η_e versus Q_{cc} .

4. Conclusions

This study developed a computational framework to maximise the performance of a silica gel–water single-stage dual-bed adsorption chiller using Antlion Optimiser (ALO) and Multi-Objective Antlion Optimiser (MOALO). Regression models that have been statistically validated were used to formulate objective functions for three key performance indicators: Coefficient of Performance (COP), cooling capacity (Q_{cc}), and waste heat recovery efficiency (η_e). η_e is introduced and treated as an equivalent objective (not a derived metric), just like COP and Q_{cc} , and it is consistently taken through modelling, optimisation, visualisation and validation along with COP and Q_{cc} . Furthermore, a structured validation and sensitivity analysis were carried out to ensure the optimisation framework's physical consistency and robustness.

The following is a summary of the study's findings and outcomes:

- MOALO identified the non-dominated set of decision variables influencing the performance of a single-stage dual-bed ADC. These included inlet temperatures, heat exchanger conductance, and mass flow rates.
- Three objective functions: COP, Q_{cc} , and η_e were formulated from statistically validated regressions and used to assess the performance of a single-stage dual-bed ADC. Treating η_e as a primary objective explicitly emphasises waste heat utilisation in addition to conventional performance metrics.
- The optimal or non-dominated solutions produced by ALO and MOALO provide actionable trade-offs to enhance performance with COP ranging from 0.675–0.717, Q_{cc} from roughly 18.3–27.5 kW, and η_e reaching an approximated maximum range of 0.131, clustering around intermediate COP and Q_{cc} values. The ALO and MOALO outcomes are consistent (and superior in some cases) to comparable literature benchmarks within the same operating window.
- References on experiments, commercial product datasheets, heat exchanger conductance and optimisation trade-offs were used to validate the objective functions and operating bounds.

- Although η_e is seldom explicitly reported in ADC studies and validation benchmark tests, the achieved η_e window demonstrates effective waste heat utilisation (recovery), contributing source-aware knowledge to existing literature.
- A one-at-a-time (OAT) sensitivity analysis was run, varying the focal variable at three levels (low, mid and high) while re-optimising all non-focal variables. Across objectives, \dot{m}_{chw} , $T_{hw,in}$, and heat exchanger conductance ($U_{evap}A_{evap}$ and $U_{cond}A_{cond}$), emerged as the most influential levers.
- Instead of 3-D projections of all three objectives, pairwise 2-D projections were used for visualisations to make interpretations of trade-offs easy and avoid occlusions of 3-D static projections. Within the explored bounds, the Pareto set is compressed to an effective 1-D ridge due to the inherent trade-offs between COP and Q_{cc} and η_e . η_e falls as COP and/or Q_{cc} rises.
- The results shown by each OAT panel are non-dominated solutions after re-optimising all non-focal decision variables. Therefore, the order by which results are presented at different lever levels must not be read as a fixed-point sensitivity where other variables are kept constant. The MOALO results reflect compensated design responses rather than simple single-parameter gradients and should be interpreted as such.
- If Q_{cc} is the priority, it is recommended to operate at a higher $T_{hw,in}$, allow a slightly warmer $T_{chw,in}$ if acceptable to the process to reduce the temperature lift, use adequately higher UA and avoid excessive heat dissipation that can penalise η_e .
- On the other hand, if the priority is effective waste heat utilisation, a balanced compromise will be to operate near the intermediate-COP region, where η_e peaks, while moderating sink side flow rates and UA. \dot{m}_{chw} should be tuned to get a balanced Q_{cc} and utilisation quality.
- Outside the explored envelope, linear regressions can exhibit non-physical intercepts, which require reciprocal transformation for SA convenience and interpretations. To ensure realistic performance predictions across the entire operating range, future research should focus on developing more physically constrained models, carrying out experimental validation at representative Pareto points, uncertainty quantification, and exploring alternative adsorbents and multi-bed recovery schemes.
- In conclusion, this study verifies the effectiveness of MOALO for improving ADC performance. Treating η_e as a co-equal objective alongside COP and Q_{cc} equips designers and decision makers with source-aware guidance to balance or prioritise cooling performance and waste heat utilisation within the established operating envelope. Thus, the regression-assisted MOALO framework may serve as a useful and practical digital technology for configuring low-grade heat ADCs and could be extended to other sustainable cooling processes.

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Abbreviations

The following abbreviations are used in this manuscript:

ADCs	Adsorption Chillers
MVC	Mechanical Vapour Compression
COP	Coefficient of Performance

GWO	Grey Wolf Optimizer
MOGWO	Multi-Objective Grey Wolf Optimizer
ALO	Antlion Optimiser
MOALO	Multi objective antlion optimiser
HFC	Hydrofluorocarbon
HCFC	Hydrochlorofluorocarbon
RAC	Refrigeration and Air Conditioning
GHG	Greenhouse Gas
SEER	Seasonal Energy Efficiency Ratio
KPI	Key Performance Indicators
PSO	Particle Swarm Optimization
thc	half cycle time
cp	Specific heat capacity ($\text{kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$)
k	Thermal conductivity ($\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$)
L	Latent heat of vaporization ($\text{kJ}\cdot\text{kg}^{-1}$)
m	Mass flow rate ($\text{kg}\cdot\text{s}^{-1}$)
Q_{cc}	Cooling capacity at the evaporator (kW)
t	Time (s)
T	Temperature ($^{\circ}\text{C}$; use K for ΔT)
UA	Overall heat conductance ($\text{kW}\cdot\text{K}^{-1}$)
$T_{hw,in}$	Hot-water inlet temperature to adsorber/desorber ($^{\circ}\text{C}$)
$T_{cw,in}$	Cooling-water inlet temperature to condenser/adsorber ($^{\circ}\text{C}$)
$T_{chw,in}$	Chilled-water inlet temperature to evaporator ($^{\circ}\text{C}$)
\dot{m}_{hw}	Hot-water mass flow rate ($\text{kg}\cdot\text{s}^{-1}$)
$\dot{m}_{cw,bed}$	Cooling-water mass flow rate through beds ($\text{kg}\cdot\text{s}^{-1}$)
\dot{m}_{chw}	Chilled-water mass flow rate ($\text{kg}\cdot\text{s}^{-1}$)
$\dot{m}_{cw,cond}$	Cooling-water mass flow rate through condenser ($\text{kg}\cdot\text{s}^{-1}$)
$U_{bed}A_{bed}$	Bed heat exchanger conductance ($\text{kW}\cdot\text{K}^{-1}$)
$U_{evap}A_{evap}$	Evaporator conductance ($\text{kW}\cdot\text{K}^{-1}$)
$U_{cond}A_{cond}$	Condenser conductance ($\text{kW}\cdot\text{K}^{-1}$)

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