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Article

Estimation of Uncertain Parameters in Single and Double Diode Models of Photovoltaic Panels Using Frilled Lizard Optimization

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Abstract: Renewable energy sources are increasingly crucial for sustainable development. Photovoltaic (PV) systems, which convert solar energy into electricity, offer an environmentally friendly solution. Enhancing energy efficiency and minimizing environmental impacts in these systems heavily rely on parameter optimization. In this study, the Frilled Lizard Optimization (FLO) algorithm is proposed as a novel approach, integrating the newton-raphson method into the root mean square error (RMSE) objective function process to address nonlinear equations. Extensive analyses conducted on RTC France, STM6-40/36, and Photowatt PWP201 modules demonstrate the superior performance of the FLO algorithm. The RMSE values were calculated as SDM: 0.0030375 and DDM: 0.011538 for RTC France; 0.012036 for STM6-40/36; and 0.0097545 for Photowatt-PWP201, indicating significantly lower error margins compared to other optimization methods. Additionally, comprehensive evaluations were carried out using error metrics such as IAE, RE, and MAE, supported by detailed graphical representations of measured and predicted parameters. Current-voltage (I-V) and power-voltage (P-V) characteristic curves, as well as convergence behaviors, were systematically analyzed. This study introduces an innovative and robust solution for parameter optimization in PV systems, contributing to both theoretical and industrial applications.

Keywords: Artificial Intelligence; Frilled Lizard Optimization; parameter estimation; Single and Double Diode

1. Introduction

In the recent past, investments in renewable energy (RE) resources have been increasing due to the increasing energy supply and the risk of depletion of fossil fuels and their environmental impacts. In addition to energy sources such as wind, geothermal, biomass and hydroelectricity, which are among the sustainable energy sources, the use of solar energy is increasing rapidly on a global scale with its high accessibility and easy installation advantages [1–3]. In this regard, photovoltaic (PV) panel systems stand out as renewable, environmentally friendly and clean energy sources that convert light from the sun directly into electrical energy [3,4]. PV systems provide a powerful alternative to fossil fuels by facilitating our access to renewable energy and make a significant contribution to a sustainable energy future [5,6]. The widespread use of PV systems worldwide has had a multiplier effect on the increase in scientific research in this field. The main aim of all these researches is to obtain the highest efficiency from the PV module. Therefore, it is critical to understand the electrical dynamics behaviour of PV systems and to optimise them with an accurate mathematical model to obtain maximum power [7,8]. In this respect, it is aimed to estimate the optimal parameters by simulating an electrical model [7].

In the literature, single diode model (SDM) and double diode model (DDM) are widely used electrical models [9]. SDM is the simplest and most practical model of PV cell. This model has 5 unknown parameters, namely photogeneration current (I_{ph}), shunt resistance (R_{sh}), series resistance (R_s), diode saturation current (I_d) and ideality factor (a). The DDM, obtained by connecting a second

diode in parallel, is the electrical model used for more complex and precise calculations with 7 unknown parameters [10]. In this context, the main objective of the calculation of unknown parameters is to design a PV cell model that will provide high accuracy and maximum power efficiency [7,10,11]. One of the main challenges is to solve the nonlinear equation provided by these designed models and to determine the unknown parameters. Several methods including analytical, deterministic and meta-heuristic (MH) have been proposed in the literature to improve the efficiency of PV systems [12]. Although analytical methods give fast results, they cause deviations in measured and calculated parameter values due to their dependence on initial values. Deterministic methods such as Newton-Raphson (NR), Gauss-Seidel have disadvantages such as high computation times [13,14]. Despite the disadvantages of analytical and deterministic approaches, MH optimisation methods have come to the fore [15].

In recent years, MH optimisation algorithms have been frequently used to solve many engineering problems. Optimisation algorithms in PV cells provide the most efficient and optimal results by analysing the interrelationships of the basic parameters of the cell in depth. This enables PV systems to be used more effectively by increasing energy efficiency [16–18]. There are some MH optimisation algorithms proposed in the literature such as atomic orbital search algorithm [19], bald eagle search (BES) [20], harris hawks optimization (HHO) [21], improved jaya optimization algorithm (IJAYA) [22], bacterial foraging algorithm (BFA) [23], tunicate swarm algorithm (TSA) [24], grey wolf optimization (GWO) [25], differential evolution (DE) [26], artificial bee swarm optimization (ABSO) [27], honey badger algorithm (HBA) [28], whale optimization algorithm (WOA) [29], farmland fertility optimizer (FFO) [30], ranking teaching learning based optimization (RTLBO) [31], wind driven optimization (WDO) [32], generalized oppositional teaching learning-based optimization (GOTLBO) [33], weighted mean of vectors algorithm (INFO) [34] etc. These algorithms provide solutions for parameter estimation in PV cells. However, current MH algorithms need to be investigated in more detail. In this context, it is important to introduce new optimisation algorithms for solar PV parameter extraction [35]. In this study, a novel frilled lizard optimisation (FLO) algorithm is proposed as an efficient method for estimating PV model parameters.

The FLO algorithm is inspired by the hunting and defence behaviour of the frilled lizard in nature and is devised to be used in solving complex problems. This optimisation algorithm is widely used in engineering, finance, energy management and health sciences [36–38]. The FLO algorithm has a population-based approach and works with an initially randomly generated solution set. The objective function, which evaluates how good the solution is to achieve the target value, is critical for optimisation algorithms [39–41]. In the optimisation of PV system parameters, the statistical term root mean square error (RMSE) is often used as the objective function. In this process, the decrease of the RMSE value in each iteration is an indication of improved performance. Since the relationship between current and voltage is nonlinear, the Newton-Raphson (N-R) numerical method is integrated to determine the solution points of the equations in the objective function [41–43]. In this paper, a novel FLO algorithm is integrated with the N-R numerical method and used for the first time in the literature to solve the problem of estimating unknown parameters in PV cells.

This paper contributes to the literature both theoretically and practically by developing a new methodology for the optimisation of PV cells. The first use of the FLO algorithm in this field fills an important gap in the literature and breaks new ground to inspire future studies. In this context, the study offers an innovative perspective both theoretically and practically. The main contributions of this study can be listed as follows:

- A novel and efficient FLO algorithm is used to estimate the unknown parameters in PV systems.
- In particular, the N-R numerical method is integrated to analyse the nonlinear equation of RMSE more efficiently.
- The performance of the proposed FLO algorithm is also calculated in detail with error metrics such as IAE, RE, MAE.
- A comprehensive comparison of the obtained results with various algorithms found in the literature has been made.

In the following Section 2, the mathematical formulation of the electrical models to be analysed and the objective function are introduced. Section 3 further details the proposed FLO algorithm. In Section 4, the experimental results obtained are evaluated and discussed. The last Section 5 is organised in such a way that a conclusion is presented.

2. Mathematical Model of Solar Cells

In the literature, although there are different PV solar cell models, SDM and DDM are widely used. [44]. In this study, two models given in Figure 2 will be used to analyse the current-voltage characteristics of PV cell models in depth. The mathematical expressions of these models and the objective function are analysed in detail in the following sections.

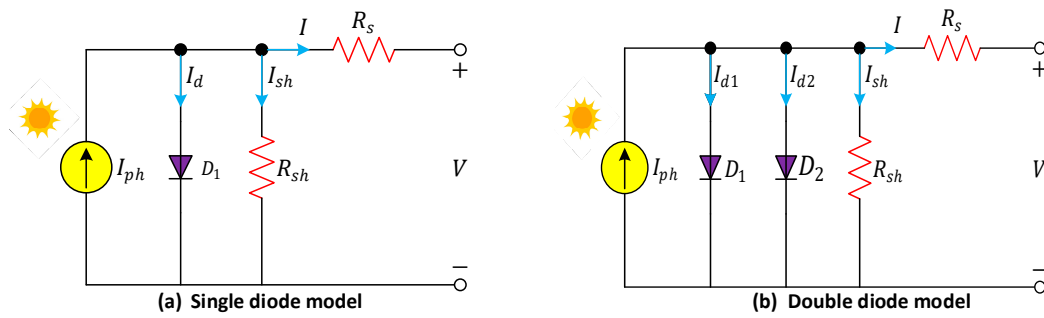


Figure 1. Equivalent circuit of photovoltaic models.

2.1. Single Diode Model

The SDM is a model often used to analyse PV cell characteristics [45]. As the electrical circuit is shown in Figure 1 (a), the general cycle formula of the model is expressed in equation (1) with Kirchhoff Current Law (KCL) [46].

$$I = I_{ph} - I_d - I_{sh} \quad (1)$$

Also, R_s , R_{sh} , V , and I represent the series resistance, shunt resistance, output voltage and output current of the solar cell, respectively.

$$I_d = I_0 \left(e^{\frac{V + (I * R_s)}{a * V_t}} - 1 \right) \quad (2)$$

$$V_t = \frac{k * T}{q} \quad (3)$$

In Equation (2), the diode current I_d is expressed mathematically. I_0 and a are defined as diode saturation current and diode ideality factor, respectively. Equation (3), V_t is the thermal voltage. k , T , and q are Boltzmann's constant ($1.3806503 \times 10^{-23}$ J/K), cell temperature in kelvin (K), and electron charge ($1.60217646 \times 10^{-19}$ C), respectively. The shunt resistor current I_{sh} is mathematically defined in equation (4).

$$I_{sh} = \frac{V + (I * R_s)}{R_{sh}} \quad (4)$$

The output current of the SDM model can be rewritten as expressed in equation (5) [47].

$$I = I_{ph} - I_0 \left[e^{\frac{V + IR_s}{aV_t}} - 1 \right] - \left[\frac{V + IR_s}{R_{sh}} \right] \quad (5)$$

Here, five unknown parameters (I_{ph} , I_0 , a , R_s , R_{sh}) must be extracted to obtain the I-V characteristic of the SDM accurately.

2.2. Double Diode Model

As the electrical circuit is shown in Figure 1 (b), the DDM model is formed by connecting a second diode in parallel. The output current of the model is mathematically expressed by equation (6) by applying KCL [46].

$$I = I_{ph} - I_{d1} - I_{d2} - I_{sh} \quad (6)$$

Where I_{d1} is the first diode current and I_{d2} is second diode current. Equations (7) and (8) describe these diode currents mathematically [46,47].

$$I_{d1} = I_{01} \left(e^{\frac{V+(I \cdot R_s)}{a_1 \cdot V_t}} - 1 \right) \quad (7)$$

$$I_{d2} = I_{02} \left(e^{\frac{V+(I \cdot R_s)}{a_2 \cdot V_t}} - 1 \right) \quad (8)$$

Here, we denote the saturation currents of the first and second diodes as I_{01} and I_{02} respectively, and the ideality factors as a_1 and a_2 respectively. V_t was previously expressed in equation (3). Thus, the output current may be mathematically reformulated as presented in equation (9) [46,47].

$$I = I_{ph} - I_{01} \left(e^{\frac{V+(I \cdot R_s)}{a_1 \cdot V_t}} - 1 \right) - I_{02} \left(e^{\frac{V+(I \cdot R_s)}{a_2 \cdot V_t}} - 1 \right) - \frac{V + (I \cdot R_s)}{R_{sh}} \quad (9)$$

Equation (9) expresses the output current of the DDM. Here, seven unknown parameters (I_{ph} , I_{01} , I_{02} , a_1 , a_2 , R_s , R_{sh}) must be extracted for optimum operating conditions.

2.3. Objective Function

In the literature, there are various efficiency measures for parameter extraction in PV solar cells. The main purpose of the objective function is to minimise the difference between the estimated and measured parameter values. In this study, the root mean square error (RMSE) is used as the objective function. The error function of the model is expressed mathematically in equations (10) and (11) [46,48]. Furthermore, the model performance was rigorously evaluated using error metrics such as individual absolute error (IAE), relative error (RE) and mean absolute error (MAE), which are widely used in the literature. Through these error metrics, expressed mathematically in Equations (12), (13), (14), (15) and (16), the differences between the measured and estimated parameter values are examined in detail and the accuracy of the model is analysed comprehensively [1].

$$\text{Objective Function} = \sqrt{\frac{1}{N} \sum_{i=1}^N J(V, I, x)^2} \quad (10)$$

$$\text{RMSE}(x) = \sqrt{\frac{1}{N} \sum_{i=1}^N J(I_i^{\text{measured}} - I_i^{\text{estimated}})^2} \quad (11)$$

$$\text{IAE}_I = \sum_{i=1}^N |I_{\text{measured}} - I_{\text{estimation}}| \quad (12)$$

$$\text{IAE}_P = \sum_{i=1}^N |P_{\text{measured}} - P_{\text{estimation}}| \quad (13)$$

$$\text{RE}_I = \left| \frac{I_{\text{measured}} - I_{\text{estimation}}}{I_{\text{measured}}} \right| * 100 \quad (14)$$

$$RE_P = \left| \frac{P_{measured} - P_{estimation}}{I_{measured}} \right| * 100 \quad (15)$$

$$MAE = \frac{1}{N} \sum_{i=1}^N |I_{measured} - I_{estimation}| \quad (16)$$

3. Frilled Lizard Optimization (FLO)

Frilled lizard optimisation (FLO) is an optimisation algorithm inspired by the behaviour of frilled lizards in hunting, moving towards prey and protecting against predators. This algorithm, which aims to solve complex problems, consists of 2 independent basic parts. These are exploration and exploitation phases [37,39].

3.1. Exploration Phase

This phase starts by imitating the ambush and movement of frilled lizards towards their prey. The main goal here is to find better solutions to solve the problem by looking at various regions. Then, using the hunting strategy of frilled lizards, the positions of individuals are updated by observing their positions and objective function values. In other words, individuals update their own positions by targeting other individuals that perform the best according to their own situation. By this design, the frilled lizard algorithm determines the potential prey points according to equation (17) [37,39].

$$C_{FL_i} = \{X_i \mid F_k < F_i \text{ ve } k \neq i\} \quad (17)$$

In this equation, C_{FL_i} represents the location of the prey of the i 'th individual. Here, it is aimed not to move away from the best value by taking into account the objective function values of other individuals. The position update in the next step is expressed by the following equation [37,39].

$$X_{i,j}^* = x_{i,j} + r_{i,j} \cdot (SP_{i,j} - I_{i,j} \cdot x_{i,j}) \quad (18)$$

In this equation, $X_{i,j}^*$ is the new updated position value, $x_{i,j}$ is the current position value, $SP_{i,j}$ is the target position value, $r_{i,j}$ is a random factor, $I_{i,j}$ is a factor determining the influence of other individuals. In equation (19), a mathematical representation of the conditions under which the new position value will be accepted is given [37,39].

$$X_i = \begin{cases} X_{i,j}^*, & F_{i,j}^* < F_i \\ X_i, & \text{otherwise} \end{cases} \quad (19)$$

In the above equation, $F_{i,j}^*$ and F_i refer to the target function of the new position and the target function of the existing function respectively.

3.2. Exploitation Phase

This phase mimics the behaviour of a frilled lizard after being hunted, climbing a nearby tree to find a safe area. The main objective of this phase is to optimise the parameters found in the exploration phase. For this purpose, it is aimed to obtain more efficient solutions by analysing the previously found regions in depth. In this phase, each position update is represented by the following mathematical equation [37,39].

$$X_{i,j}^{(t+1)} = x_{i,j} + (1 - 2r) \cdot (U_{\text{best}} - L_{\text{best}}) \quad (20)$$

In the above equation $X_{i,j}^{(t+1)}$ is the updated position in the second stage, $x_{i,j}$ is the current position, U_{best} is the best solution found, L_{best} is the worst solution found and r is a random factor. The following equation is then used to determine whether or not to accept the new found position [37,39].

$$X_i = \begin{cases} X_{i,j}^{(t+1)}, & F_{i,j}^{(t+1)} < F_i \\ X_i, & otherwise \end{cases} \tag{21}$$

Figure 2 shows the overall process of the study, which systematically describes an optimised methodology for PV parameter estimation. The proposed FLO algorithm integrates the N-R mathematical approach, which is often preferred for solving nonlinear equations. Accurate calculation of I-V characteristics is an extremely significant criterion in solar cell modelling and parameter estimation. In this regard, the FLO+NR method combines strong global optimisation capabilities and fast convergence to determine the parameters with high accuracy. [41,42]. The flowchart of the FLO algorithm is presented in Figure 3.

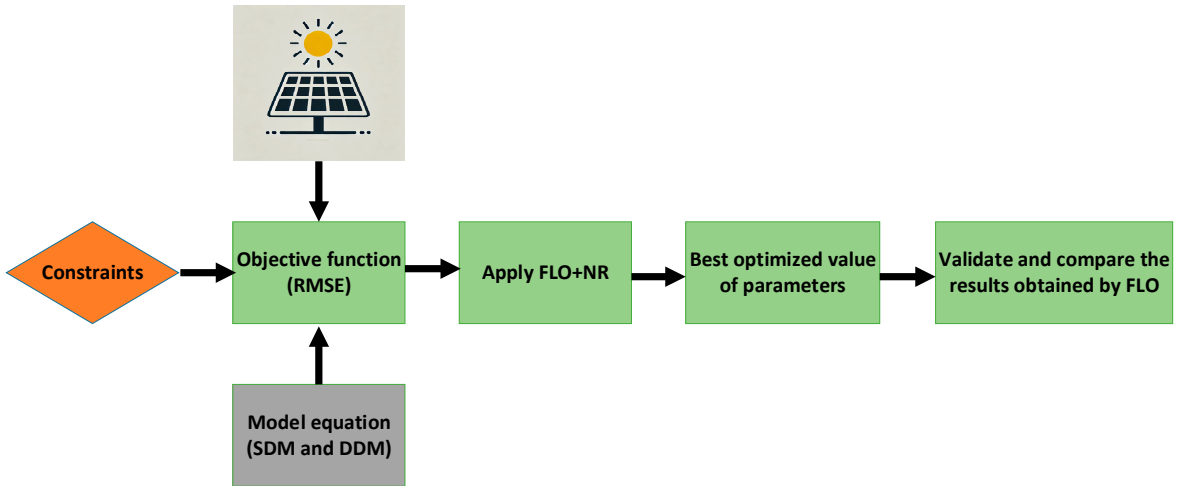


Figure 2. An overview of FLO algorithm-based parameter estimation of PV models.

Table 1. The upper and lower bounds of each parameter.

	R.T.C France Module		STM6-40/36 Module		Photowatt-PWP201 Module	
Parameters	Upper Bound	Lower Bound	Upper Bound	Lower Bound	Upper Bound	Lower Bound
$I_{ph}(A)$	1	0	2	0	2	0
$R_s(\Omega)$	0,5	0	0,36	0	2	0
$R_{sh}(\Omega)$	100	0	1000	0	2000	0
a, a_1	2	1	60	1	50	1
$I_0, I_{01}(\mu A)$	1	0	50	0	50	0

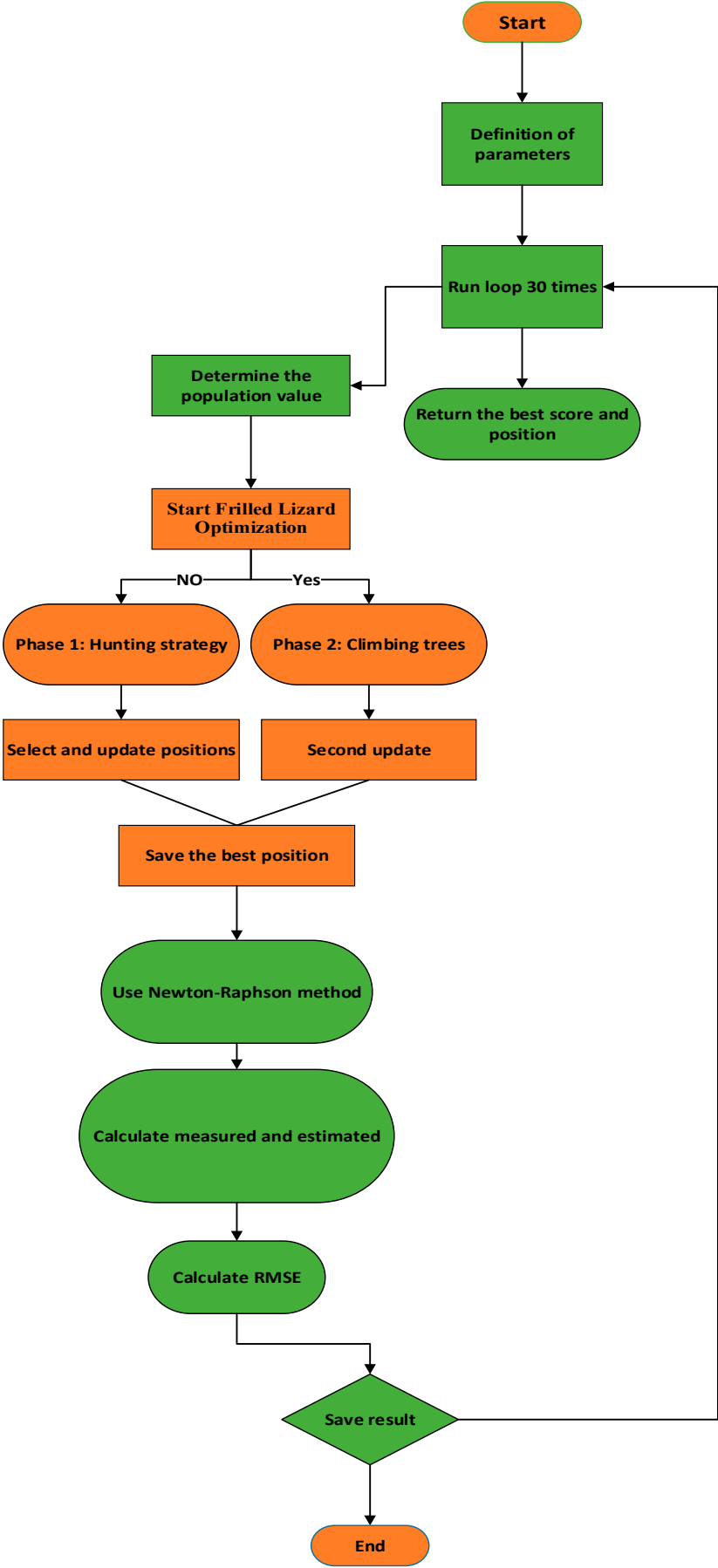


Figure 3. FLO flowchart.

4. Result And Discussion

In this section, the results obtained with the proposed FLO algorithm for the parameter estimation problem of solar PV cells are presented. In order to verify the effectiveness of the FLO algorithm, real current-voltage data from the literature were used. These data sets include R.T.C. France commercial silicon solar cell with a diameter of 57 mm, measured at 1000 W/m² irradiance and 33 °C, monocrystalline STM6-40/36 module measured at 51 °C and Photowatt-PWP201 module consisting of 36 cells connected in series measured at 45 °C [49,50]. All these analyses were performed using the electrical circuits of the SDM and DDM models, especially the lower and upper parameter limits of the data sets are given in Table 1. These bound values are critical values that determine the performance and efficiency characteristics of the modules [51]. The measured and predicted current-voltage (I-V), power-voltage (P-V) graphs, convergence curves and maximum power point (MPP) are given in detail with the proposed FLO algorithm. In addition, statistical metrics such as maximum (max), minimum (min), standard deviation (std), mean (mean), variance (var) and scatter plots are presented. In order to make a more powerful analysis, error metrics such as IAE, RE, MAE were calculated in addition to the RMSE used as the objective function, and the differences between the measured and estimated parameter values were analysed comprehensively. All these experiments were analysed using MATLAB R2022a software with Intel(R) Core(TM) i7-7500U CPU @ 2.70GHz 2.90 GHz and 8 GB RAM. In addition, the FLO algorithm proposed in the study was tested in 30 runs, 40 population sizes and 800 iterations.

4.1. Result for R.T.C. France

Table 2 shows that the FLO algorithm exhibits superior performance in optimisation accuracy for the SDM model. The lowest RMSE value of 0.0030375 was obtained when compared with multi-verse optimization (MVO), hybrid particle swarm optimization and simulated annealing (HPSOSA), bacterial foraging algorithm (BFA), genetic algorithm (GA), simulated annealing (SA), pattern search (PS), whale optimization algorithm (WOA), butterfly optimization algorithm (BOA) optimisation algorithms in the literature. Table 3 presents the optimisation results of the DDM model. The lowest RMSE value with 0.011538 was obtained compared to particle swarm optimization (PSO), opposition-based sine cosine algorithm (OBSCA), GA, SA, PS, WOA, BOA optimisation algorithms in the literature. These results demonstrate the superior performance of the proposed method in parameter estimation on SDM and DDM models.

Table 2. Comparison of result obtained from the FLO with other optimization techniques in the literature for SDM.

Algorithm	I_{ph} (A)	I_o (μ A)	R_s (Ω)	R_{sh} (Ω)	α	RMSE
FLO (Proposed)	0.761598	0.384977	0.0381659	68.8525	1.49892	0.0030375
MVO [44]	0.7616	0.32094	0.0365	59.5884	1.5252	0.1268
HPSOS [44]	0.7608	0.3117	0.0365	52.8898	1.4753	0.0071
BFA [52]	0.7602	0.8000	0.0325	50.8691	1.6951	0.029
GA[52]	0.7619	0.8087	0.0299	43.3729	1.5751	0.019
SA [53]	0.762	0.4798	0.0345	43.1034	1.5172	0.019
PS [54]	0.7617	0.998	0.0313	64.1026	1.6	0.2863
WOA [55]	0.76405	0.28588	0.0484	59.9940	1.4702	0.0132
BOA [56]	0.760234	0.80980	0.023287	30.53997	1.585917	0.16641

Figure 4 (a) and (b) show the I-V and P-V characteristic curves of the SDM model, respectively. When these curves are analysed, it is clearly seen that the measured and predicted values agree with a high accuracy. Likewise, Figure 5 (a) and (b) show this agreement in the I-V and P-V characteristic curves of the DDM model, respectively. In this regard, these graphs strongly support the accuracy and reliability of both the model and the FLO algorithm used. In Figure 6 (a) and (b), the convergence curves of SDM and DDM are presented respectively. The fact that the fitness values for both models

reach low levels proves that the solution accuracy of the algorithm is high. It is also evident that the FLO algorithm performs reliably and efficiently for both simple and complex models.

Table 3. Comparison of result obtained from the FLO with other optimization techniques in the literature for DDM.

Algorithm	I_{ph} (A)	I_{o1} (μA)	R_s (Ω)	R_{sh} (Ω)	α_1	I_{o2} (μA)	α_2	RMSE
FLO (Proposed)	0.752239	0.592485	0.0342579	38.0587	1.55789	0.646782	1.9019	0.011538
PSO [57]	0.7623	0.4767	0.0325	43.1034	1.5172	0.01	2	0.0166
GA [52]	0.7608	0.0001	0.0364	53.7185	1.3355	0.0001	1.481	0.36040
SA [53]	0.7623	0.4767	0.0345	43.1034	1.5172	0.01	2	0.01664
PS [54]	0.7602	0.9889	0.032	81.3008	1.6	0.0001	1.192	0.01518
WOA [55]	0.7658	2.9957E-07	0.0493	59.0196	1.4795	3.9438E-07	1.9201	0.0154
OBSCA [56]	0.794380	0.528673	0.03468	23.9696	1.527530	0.04440	2	0.024067
BOA [56]	0.78077	0.89987	0.03875	34.5559	1.47604	0.29385	1.99100	0.013564

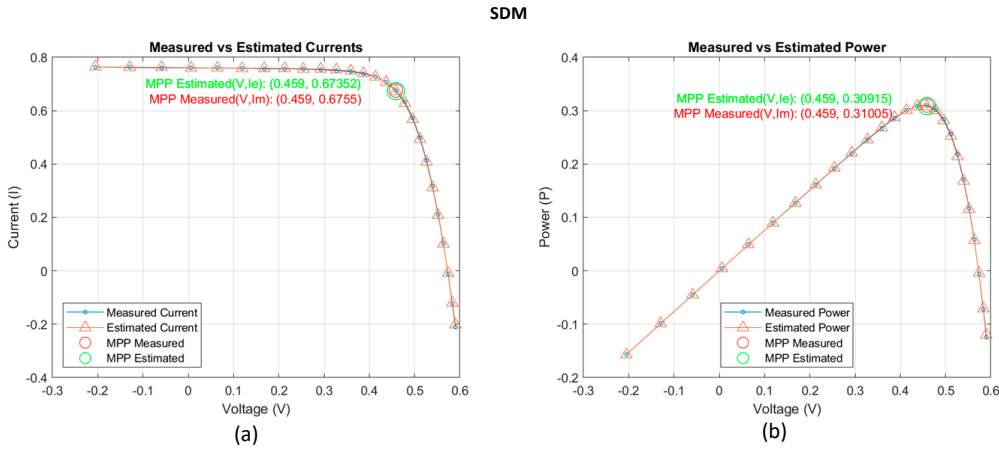


Figure 4. Comparison between the measured and the estimated data obtained by FLO algorithm for R.T.C France model (a) I-V of SDM, (b) P-V of SDM.

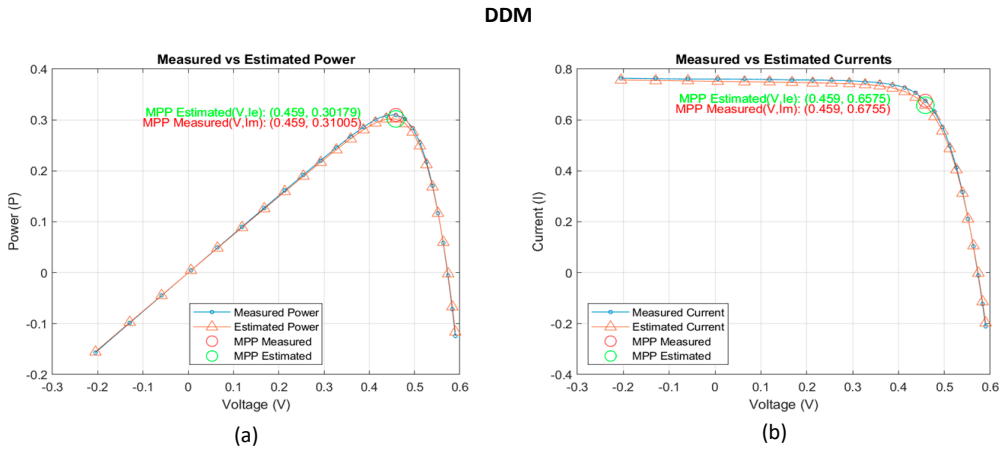


Figure 5. Comparison between the measured and the estimated data obtained by FLO algorithm for R.T.C France model (a) I-V of DDM, (b) P-V of DDM.

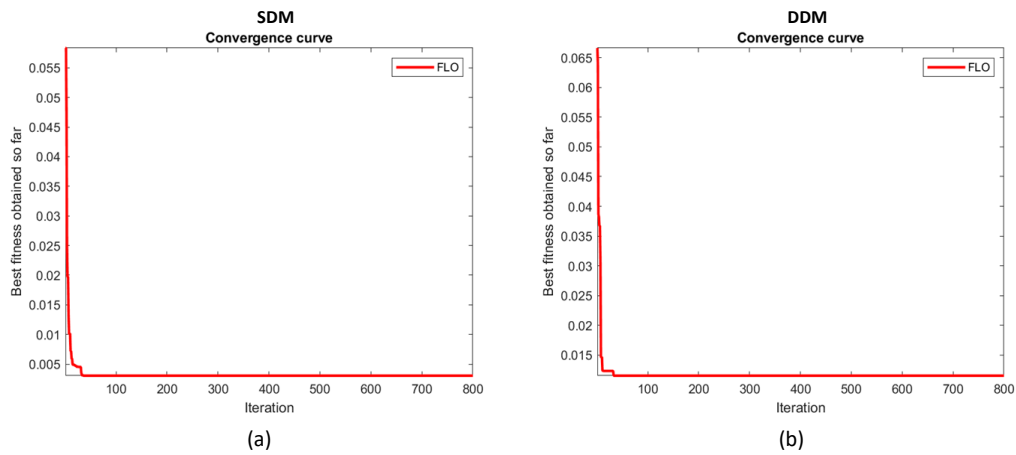


Figure 6. Convergence graph of proposed FLO algorithm for R.T.C France model: (a) SDM, (b) DDM.

Table 4 presents the measured and estimated current and power values of the SDM model and the error metrics such as IAE, RE, MAE between these values in a comprehensive manner. In this regard, it is clearly seen that I_m and P_m values agree with I_e and P_e values with a high level of accuracy. Analysing the determined error metrics, the total IAE error value in the SDM model was calculated as 0.06194 and 0.02812 for current and power, respectively. The MAE error value was calculated depending on the IAE values for each data line in order to analyse the change in the process, and the total MAE error value was obtained as 0.00238 for current.

Table 5 shows the error metrics of the DDM model. Here, the total IAE error value is calculated as 0.27738 and 0.10030 for current and power, respectively. The MAE error value was calculated depending on the IAE values for each data line in order to analyse the change in the process, and the total MAE error value was obtained as 0.01067 for current. The low error values for SDM and DDM model are important indicators of the consistency of the algorithm. Figure 7 (a) and (b) show that the agreement between measured and estimated I-V/P-V values at all data points for the SDM and DDM models is clearly observed. In Figure 7 (c), a graphical representation of the IAE and MAE error performance for both models is presented. In addition, although the RE error metric results calculated for the current and power shown in Tables 4 and 5 are quite consistent, deviations are experienced at certain data points. This situation can be interpreted as a need for improvements in the optimisation process of the proposed FLO algorithm. Considering all the analyses, SDM offers a simpler and faster modelling approach, while DDM stands out as an option that can be used in more complex situations. In terms of overall performance, it is evident that the FLO algorithm provides precise solutions to the parameter optimisation problem in PV cells by providing highly effective results in both models.

Table 4. Statistical error tests for SDM of R.T.C. France.

No	Measured Data			Estimation Data		IAE		RE		MAE
	$V(V)$	$I_m(A)$	$P_m(W)$	$I_e(A)$	$P_e(W)$	IAE_I	IAE_P	RE_I	RE_P	MAE_I
1	-0.2057	0.7640	-0.1572	0.7642	-0.1572	0.00016	0.00004	0.0209	-0.0255	0.00016
2	-0.1291	0.7620	-0.0984	0.7631	-0.0985	0.00105	0.00014	0.1378	-0.1382	0.00060
3	-0.0588	0.7605	-0.0447	0.7620	-0.0448	0.00153	0.00009	0.2012	-0.2013	0.00091
4	0.0057	0.7605	0.0043	0.7611	0.0043	0.00059	0.00000	0.0776	0.0784	0.00083
5	0.0646	0.7600	0.0491	0.7602	0.0491	0.00023	0.00002	0.0303	0.0306	0.00071
6	0.1185	0.7590	0.0899	0.7594	0.0900	0.00044	0.00005	0.0580	0.0589	0.00067
7	0.1678	0.7570	0.1270	0.7587	0.1273	0.00168	0.00029	0.2219	0.2283	0.00081
8	0.2132	0.7570	0.1614	0.7579	0.1616	0.00091	0.00020	0.1202	0.1239	0.00082
9	0.2545	0.7555	0.1923	0.7570	0.1927	0.00148	0.00038	0.1959	0.1976	0.00090
10	0.2924	0.7540	0.2205	0.7556	0.2210	0.00163	0.00048	0.2162	0.2177	0.00097

11	0.3269	0.7505	0.2453	0.7533	0.2463	0.00283	0.00092	0.3771	0.3750	0.00114
12	0.3585	0.7465	0.2676	0.7491	0.2686	0.00261	0.00094	0.3496	0.3512	0.00126
13	0.3873	0.7385	0.2860	0.7415	0.2872	0.00295	0.00114	0.3995	0.3986	0.00139
14	0.4137	0.7280	0.3012	0.7280	0.3012	0.00002	0.00001	0.0027	0.0033	0.00129
15	0.4373	0.7065	0.3090	0.7065	0.3090	0.00003	0.00001	0.0042	0.0032	0.00121
16	0.4590	0.6755	0.3101	0.6735	0.3092	0.00198	0.00090	0.2931	0.2903	0.00126
17	0.4784	0.6320	0.3024	0.6277	0.3003	0.00432	0.00207	0.6835	0.6846	0.00144
18	0.4960	0.5730	0.2842	0.5676	0.2815	0.00540	0.00268	0.9424	0.9430	0.00166
19	0.5119	0.4990	0.2554	0.4942	0.2530	0.00481	0.00246	0.9639	0.9630	0.00182
20	0.5265	0.4130	0.2174	0.4080	0.2148	0.00498	0.00262	1.2058	1.2049	0.00198
21	0.5398	0.3165	0.1709	0.3124	0.1686	0.00415	0.00224	1.3112	1.3111	0.00208
22	0.5521	0.2120	0.1171	0.2086	0.1152	0.00338	0.00187	1.5943	1.5976	0.00214
23	0.5633	0.1035	0.0583	0.1013	0.0571	0.00220	0.00124	2.1256	2.1303	0.00215
24	0.5736	-0.0100	-0.0057	-0.0081	-0.0046	0.00194	0.00111	-19.4080	-19.4090	0.00214
25	0.5833	-0.1230	-0.0717	-0.1200	-0.0700	0.00300	0.00171	-2.4390	-2.3764	0.00217
26	0.5900	-0.2100	-0.1239	-0.2024	-0.1194	0.00764	0.00451	-3.6381	-3.6400	0.00238
Sum of IAE						0.06194	0.02812			

Table 5. Statistical error tests for DDM of R.T.C. France.

No	Measured Data			Estimation Data		IAE		RE		MAE
	$V(V)$	$I_m(A)$	$P_m(W)$	$I_e(A)$	$P_e(W)$	IAE_I	IAE_P	RE_I	RE_P	MAE_I
1	-0.2057	0.7640	-0.1572	0.7570	-0.1557	0.00704	0.00144	0.9215	-0.9163	0.00704
2	-0.1291	0.7620	-0.0984	0.7550	-0.0975	0.00705	0.00091	0.9252	-0.9250	0.00705
3	-0.0588	0.7605	-0.0447	0.7531	-0.0443	0.00739	0.00043	0.9717	-0.9705	0.00716
4	0.0057	0.7605	0.0043	0.7514	0.0043	0.00909	0.00005	1.1953	1.1950	0.00764
5	0.0646	0.7600	0.0491	0.7499	0.0484	0.01014	0.00066	1.3342	1.3341	0.00814
6	0.1185	0.7590	0.0899	0.7484	0.0887	0.01058	0.00125	1.3939	1.3931	0.00855
7	0.1678	0.7570	0.1270	0.7471	0.1254	0.00994	0.00166	1.3131	1.3069	0.00875
8	0.2132	0.7570	0.1614	0.7457	0.1590	0.01131	0.00241	1.4941	1.4933	0.00907
9	0.2545	0.7555	0.1923	0.7442	0.1894	0.01133	0.00288	1.4997	1.4979	0.00932
10	0.2924	0.7540	0.2205	0.7422	0.2170	0.01183	0.00346	1.5690	1.5694	0.00957
11	0.3269	0.7505	0.2453	0.7391	0.2416	0.01136	0.00372	1.5137	1.5163	0.00973
12	0.3585	0.7465	0.2676	0.7341	0.2632	0.01240	0.00445	1.6611	1.6628	0.00996
13	0.3873	0.7385	0.2860	0.7256	0.2810	0.01290	0.00499	1.7468	1.7446	0.01018
14	0.4137	0.7280	0.3012	0.7115	0.2944	0.01649	0.00682	2.2651	2.2645	0.01063
15	0.4373	0.7065	0.3090	0.6899	0.3017	0.01665	0.00728	2.3567	2.3564	0.01103
16	0.4590	0.6755	0.3101	0.6575	0.3018	0.01800	0.00826	2.6647	2.6641	0.01147
17	0.4784	0.6320	0.3024	0.6134	0.2934	0.01861	0.00891	2.9446	2.9469	0.01189
18	0.4960	0.5730	0.2842	0.5561	0.2758	0.01692	0.00839	2.9529	2.9520	0.01217
19	0.5119	0.4990	0.2554	0.4862	0.2489	0.01283	0.00657	2.5711	2.5720	0.01220
20	0.5265	0.4130	0.2174	0.4038	0.2126	0.00921	0.00484	2.2300	2.2259	0.01205
21	0.5398	0.3165	0.1709	0.3117	0.1682	0.00483	0.00261	1.5261	1.5277	0.01171
22	0.5521	0.2120	0.1171	0.2109	0.1164	0.00113	0.00063	0.5330	0.5382	0.01123
23	0.5633	0.1035	0.0583	0.1056	0.0595	0.00208	0.00117	2.0097	2.0085	0.01083
24	0.5736	-0.0100	-0.0057	-0.0027	-0.0016	0.00729	0.00418	-72.9430	-72.9428	0.01068
25	0.5833	-0.1230	-0.0717	-0.1146	-0.0669	0.00838	0.00489	-6.8130	-6.8171	0.01059
26	0.5900	-0.2100	-0.1239	-0.1974	-0.1165	0.01260	0.00743	-6.0000	-5.9968	0.01067
Sum of IAE						0,27738	0,10030			

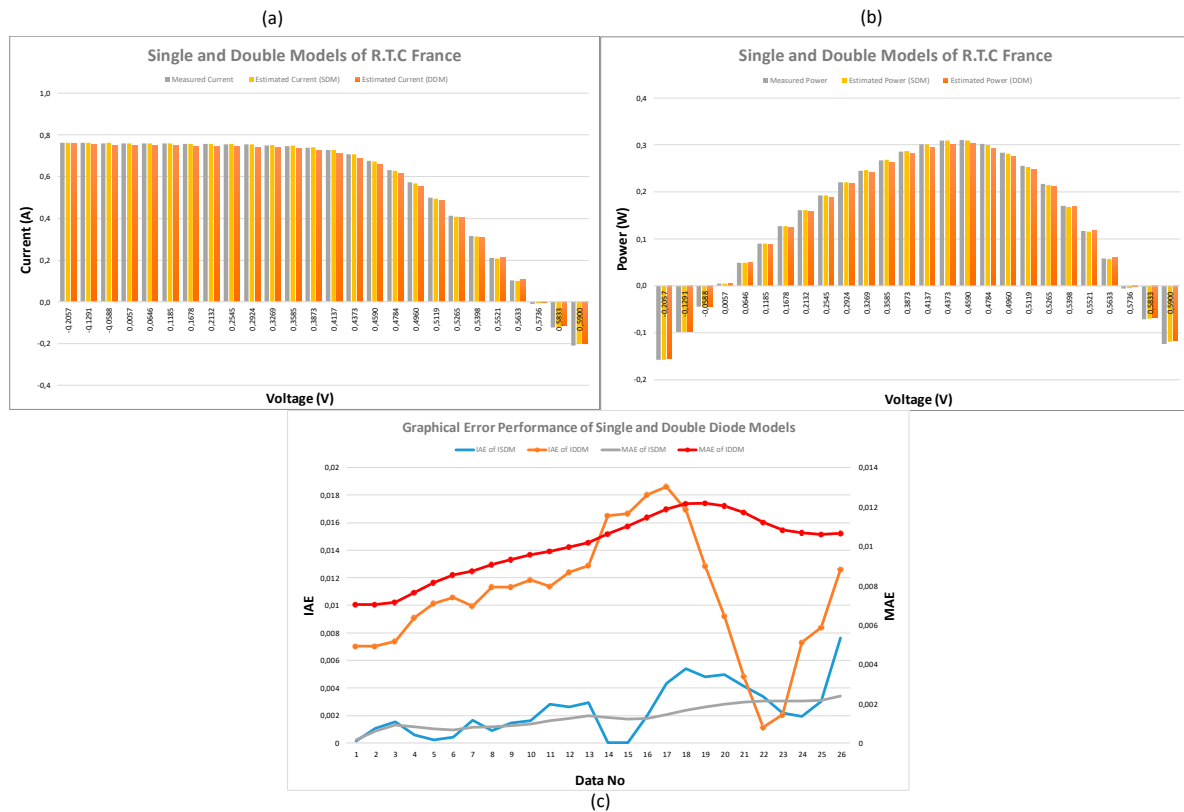


Figure 7. Performance Comparison of Single and Double Diode Models Using FLO algorithm (a)I-V, (b)P-V and (c) Error Metrics for Each Data Point.

4.2. Results For STM6-40/36 and Photowatt-PWP201

In this subsection, the optimal parameters obtained with the FLO algorithm using the STM6-40/36 data set are presented in Table 6. The lowest RMSE value of 0.012036 was obtained when compared with triple archives particle swarm optimization (TAPSO), artificial bee colony (ABC), chaotic improved artificial bee colony (CIABC), PSO, sine-cosine algorithm (SCA), wind driven optimization (WDO) optimisation algorithms in the literature. In particular, this shows that the estimated parameter values are highly accurate. The I-V and P-V characteristic curves in Figure 8 (a) and (b) show that the agreement between the measured and estimated values is very strong. In Table 7, the lowest RMSE value with 0.012036 was obtained in the analysis using Photowatt-PWP201 module compared to whale optimization algorithm (WOA), SCA, firefly algorithm (FA), atom search optimization (ASO), newton, WDO. As shown in Figure 9 (a) and (b), the measured and estimated values are quite consistent. The convergence curves of STM6-40/36 and Photowatt-PWP201 are presented in Figure 10 (a) and (b), respectively. In both models, the FLO algorithm showed a fast convergence with early iteration. This proves that the algorithm has a strong exploration capability and can effectively scan the solution space. As a result, it shows that the FLO algorithm exhibits a strong performance in both convergence speed and solution accuracy and works effectively in parameter estimation tasks for different PV modules.

Table 6. Comparison of result obtained from the FLO with other optimization techniques in the literature for STM6-40/36.

Algorithm	I_{ph} (A)	I_o (μ A)	R_s (Ω)	R_{sh} (Ω)	α	RMSE
FLO (Proposed)	1.664394	1.955187	0.1534515	950.3287	58.27311	0.012036
TAPSO [58]	1.66180	12.8424	0.00053	190.1861	1.77407	0.013423
ABC [59]	1.5	1.6644	0.1796	547.416	53.5176	0.19253
CIABC [59]	1.6642	1.676	0.1584	562.212	53.9136	0.02518
PSO [60]	1.64	0.151	0.28	200.94	55.82	0.0241
SCA [60]	1.74	0.252	0.86	100.52	54.51	0.0295
WDO [61]	0.827900	42.22415	0.312870	772.4239	28.6336	0.0934228

Table 7. Comparison of result obtained from the FLO with other optimization techniques in the literature for Photowatt-PWP201.

Algorithm	I_{ph} (A)	I_o (μ A)	R_s (Ω)	R_{sh} (Ω)	α	RMSE
FLO (Proposed)	1.0308692	2.5494649	1.2662524	1408.5111	49.181231	0.0097545
WOA [55]	1.3135	0	0.0622	16.229	49.4231	0.2838
SCA [62]	1.03364	0.118	0.930711	1268.463	53.72168	0.0117780
FA [63]	1.0424	4.6816	1.2042	1204.0547	497875	0.0103
ASO [64]	1.2145	1.0826	0.2298	59.6881	44.3904	0.16898
Newton [59]	1.0318	3.2875	1.2057	555.5556	48.45	0.7805
WDO [61]	0.31735	3.682679	0.978698	184.19173	8.215487	0.104839

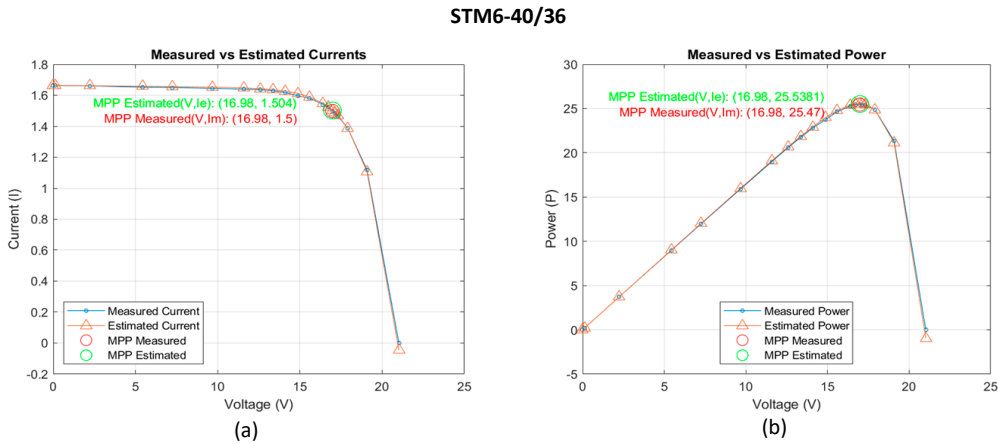


Figure 8. Comparison between the measured and the estimated data obtained by FLO algorithm for STM6-40/36 model (a) I-V curve. (b) P-V curve.

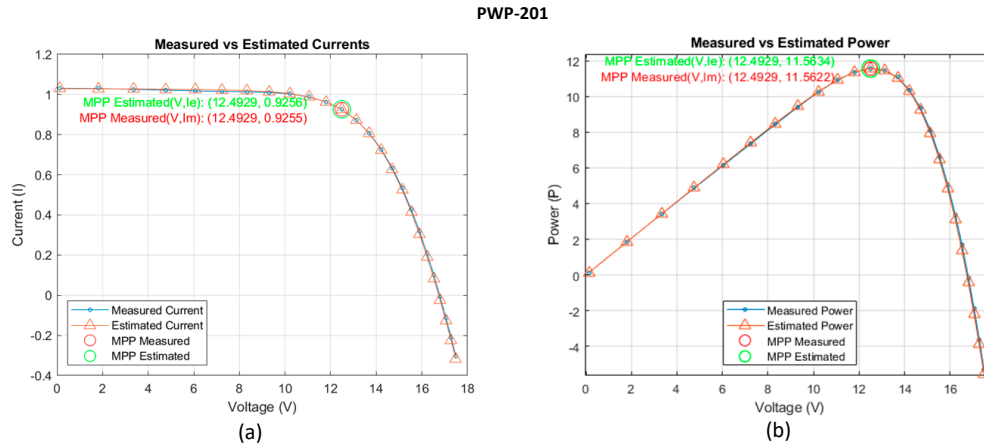


Figure 9. Comparison between the measured and the estimated data obtained by FLO algorithm for Photowatt PWP-201 model (a) I-V curve. (b) P-V curve.

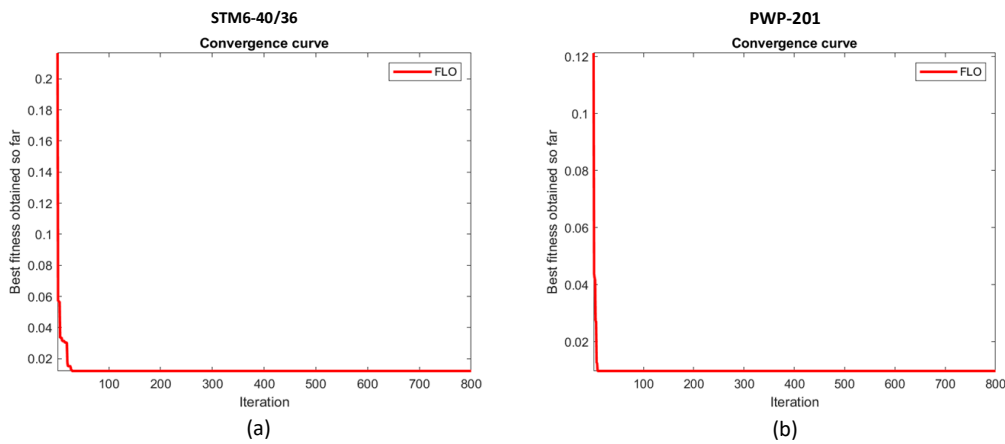


Figure 10. Convergence graph of proposed FLO algorithm for: (a) STM6-40/36. (b) Photowatt PWP-201.

In Tables 8 and 9, measured and predicted current and power values of STM6-40/36 and Photowatt-PWP201 models, respectively, as well as calculated error metrics are given. As shown in Table 8, the calculated total IAE is 0.1529 and 2.4106 for current and power error values, respectively. The MAE error value was calculated depending on the IAE values for each data line in order to analyse the change in the process, and the total MAE error value was obtained as 0.0076 for current. In Table 9, the total IAE error values for current and power are calculated as 0.1856 and 2.6810, respectively, and the total MAE error value for current is calculated as 0.0074. Figure 11 (a) and (b) shows the consistency between measured and predicted I-V/P-V values at all data points for STM6-40/36 and Photowatt-PWP201 modules. In Figure 11 (c) and (d), a graphical approach including the IAE and MAE error performance for both models is presented. Furthermore, Tables 8 and 9 show the error metric results of these models for current and power. The low error values obtained clearly demonstrate that the proposed FLO algorithm produces highly consistent and reliable solutions for different PV module data sets.

Table 8. Statistical error tests for SDM of STM6-40/36.

	Measured Data			Estimation Data		IAE		RE		MAE
No	V (V)	I_m (A)	P_m (W)	I_e (A)	P_e (W)	IAE_I	IAE_P	RE_I	RE_P	MAE_I
1	0	1.663	0	1.6641	0	0.0011	0.0000	0.0661	-	0.0011
2	0.118	1.663	0.196234	1.664	0.196352	0.0010	0.0001	0.0601	0.0601	0.0010
3	2.237	1.661	3.71566	1.6618	3.71737	0.0008	0.0017	0.0482	0.0460	0.0010
4	5.434	1.653	8.9824	1.6583	9.01137	0.0053	0.0290	0.3206	0.3225	0.0020
5	7.26	1.65	11.979	1.6562	12.0242	0.0062	0.0452	0.3758	0.3773	0.0029
6	9.68	1.645	15.9236	1.6527	15.9981	0.0077	0.0745	0.4681	0.4679	0.0037
7	11.59	1.64	19.0076	1.6476	19.0957	0.0076	0.0881	0.4634	0.4635	0.0042
8	12.6	1.636	20.6136	1.6425	20.6957	0.0065	0.0821	0.3973	0.3983	0.0045
9	13.37	1.629	21.7797	1.6363	21.8772	0.0073	0.0975	0.4481	0.4477	0.0048
10	14.09	1.619	22.8117	1.6273	22.929	0.0083	0.1173	0.5127	0.5142	0.0052
11	14.88	1.597	23.7634	1.6118	23.9834	0.0148	0.2200	0.9267	0.9258	0.0061
12	15.59	1.581	24.6478	1.5896	24.7824	0.0086	0.1346	0.5440	0.5461	0.0063
13	16.4	1.542	25.2888	1.5489	25.4018	0.0069	0.1130	0.4475	0.4468	0.0063
14	16.71	1.524	25.466	1.5269	25.515	0.0029	0.0490	0.1903	0.1924	0.0061
15	16.98	1.5	25.47	1.504	25.5381	0.0040	0.0681	0.2667	0.2674	0.0059
16	17.13	1.485	25.4381	1.4895	25.5151	0.0045	0.0770	0.3030	0.3027	0.0058
17	17.32	1.465	25.3738	1.4691	25.4441	0.0041	0.0703	0.2799	0.2771	0.0057
18	17.91	1.388	24.8591	1.3878	24.8556	0.0002	0.0035	0.0144	0.0141	0.0054
19	19.08	1.118	21.3314	1.1081	21.1423	0.0099	0.1891	0.8855	0.8865	0.0057
20	21.02	0	0	-0.045221	-0.950544	0.0452	0.9505	-	-	0.0076
Sum of IAE						0.1529	2.4106			



Figure 11. Performance Comparison I-V, P-V and Error Metrics for Each Data Point; (a), (c) STM6-40/36 and (b), (d) Photowatt-PWP201.

Table 9. Statistical error tests for SDM of Photowatt-PWP201.

No	Measured Data			Estimation Data		IAE		RE		MAE
	$V(V)$	$I_m(A)$	$P_m(W)$	$I_e(A)$	$P_e(W)$	IAE_I	IAE_P	RE_I	RE_P	MAE_I
1	0.1248	1.0315	0.128731	1.0298	0.128525	0.0017	0.0002	0.1648	0.1600	0.0017
2	1.8093	1.03	1.86358	1.0286	1.86111	0.0014	0.0025	0.1359	0.1325	0.0016
3	3.3511	1.026	3.43823	1.0275	3.44318	0.0015	0.0050	0.1462	0.1440	0.0015
4	4.7622	1.022	4.86697	1.0263	4.88742	0.0043	0.0204	0.4207	0.4202	0.0022
5	6.0538	1.018	6.16277	1.0249	6.20464	0.0069	0.0419	0.6778	0.6794	0.0032
6	7.2364	1.0155	7.34856	1.023	7.40273	0.0075	0.0542	0.7386	0.7372	0.0039
7	8.3189	1.014	8.43536	1.0198	8.48403	0.0058	0.0487	0.5720	0.5770	0.0042
8	9.3097	1.01	9.4028	1.0144	9.44363	0.0044	0.0408	0.4356	0.4342	0.0042
9	10.2163	1.0035	10.2521	1.0049	10.2659	0.0014	0.0138	0.1395	0.1346	0.0039
10	11.0449	0.988	10.9124	0.98884	10.9216	0.0008	0.0092	0.0850	0.0843	0.0036
11	11.8018	0.963	11.3651	0.96341	11.37	0.0004	0.0049	0.0426	0.0431	0.0033
12	12.4929	0.9255	11.5622	0.9256	11.5634	0.0001	0.0012	0.0108	0.0104	0.0030
13	13.1231	0.8725	11.4499	0.87318	11.4588	0.0007	0.0089	0.0779	0.0777	0.0028
14	13.6983	0.8075	11.0614	0.80525	11.0305	0.0022	0.0309	0.2786	0.2793	0.0028
15	14.2221	0.7265	10.3324	0.72283	10.2802	0.0037	0.0522	0.5052	0.5052	0.0029
16	14.6995	0.6345	9.32683	0.62823	9.23473	0.0063	0.0921	0.9882	0.9875	0.0031
17	15.1346	0.5345	8.08944	0.52465	7.94044	0.0099	0.1490	1.8428	1.8419	0.0035
18	15.5311	0.4275	6.63955	0.41547	6.45275	0.0120	0.1868	2.8140	2.8134	0.0039
19	15.8929	0.3185	5.06189	0.30363	4.82563	0.0149	0.2363	4.6688	4.6674	0.0045
20	16.2229	0.2085	3.38247	0.19168	3.10956	0.0168	0.2729	8.0671	8.0684	0.0051
21	16.5241	0.101	1.66893	0.081626	1.3488	0.0194	0.3201	19.1822	19.1818	0.0058
22	16.7987	-0.008	-0.13439	-0.024974	-0.419524	0.0170	0.2851	-212.1750	-212.1691	0.0063
23	17.0499	-0.111	-1.89254	-0.12747	-2.1733	0.0165	0.2808	-14.8378	-14.8351	0.0068
24	17.2793	-0.209	-3.61137	-0.22501	-3.88806	0.0160	0.2767	-7.6603	-7.6616	0.0071
25	17.4885	-0.303	-5.29902	-0.31709	-5.5455	0.0141	0.2465	-4.6502	-4.6514	0.0074
Sum of IAE						0,1856	2,6810			

Table 10 statistically evaluates the modelling performance using the RMSE values calculated by the FLO algorithm with SDM, DDM, STM6-40/36 and Photowatt-PWP201 module data. Max, Min, Mean, Std and Var values are presented for each data set. Also, a graph showing the error distribution of these metrics is given in Figure 12. In STM6-40/36, the max. error value (1.54332) is higher than the other data sets. In Photowatt-PWP201, the max. RMSE value (0.43731) is higher than SDM and DDM models. In this respect, high max. values can be interpreted as the algorithm should be improved on these data sets. The minimum RMSE values are 0.01153 and 0.01203 for DDM and STM6-40/36, respectively, and although these values are higher compared to SDM and Photowatt-PWP201 (0.00303 and 0.00975, respectively), the RMSE values in all analysed module data remain at a low level in general. This indicates that the model has a high accuracy capacity. Mean RMSE is the lowest in the SDM (0.08168) and DDM (0.08529) models. This indicates that the errors for the two models are in a narrow range. The error values are slightly higher for the STM6-40/36 (0.69211) and Photowatt-PWP201 (0.21988) models. In this respect, it may indicate that the proposed optimisation method should be improved in order to increase the performance of the models. Std. and var. values (0.33856 and 0.11462, respectively) are the highest for the STM6-40/36 module. This indicates that the errors are distributed in a wider range for this data set. All these results show that the proposed FLO algorithm performs well in terms of overall accuracy and consistency, but the optimisation process can be improved for some data sets (STM6-40/36 and Photowatt-PWP201).

Table 10. The statistical metrics of RMSE values provided by FLO algorithm for SDM, DDM, STP6-120/36 and Photowatt-PWP201.

RMSE	Data Sets			
Statistical metrics	SDM	DDM	STM6-40/36	PWP-201
Max	0.12876	0.13501	1.54332	0.43731
Min	0.00303	0.01153	0.01203	0.00975
Mean	0.08168	0.08529	0.69211	0.21988
Std	0.03582	0.03090	0.33856	0.149
Var	0.00128	0.00095	0.11462	0.0222

In Table 11, the FLO algorithm obtained high accuracy results compared to hybrid firefly algorithm and pattern search algorithm (HFAPS) bird mating optimization (BMO), firefly algorithm (FA) comparing the maximum power point (MPP) parameters (V_{MP} , I_{MP} , P_{MP}) to evaluate its performance. For the R.T.C France dataset, V_{MP} , I_{MP} , P_{MP} values (respectively: 0.459, 0.67352, 0.30915) were estimated with very small deviation compared to the measured values. Similarly, the values obtained for STM6-40/36 dataset (respectively: 16.98, 1.504, 25.5381) produced more accurate results than the other algorithms compared. In the Photowatt PWP-201 dataset, the values estimated by the proposed FLO algorithm (respectively: 12.4929, 0.9256, 11.5634) proved its potential with the closest deviation to the measured values compared to other algorithms. Since BMO, FA and HFAPS algorithms exhibit higher deviations, the proposed FLO algorithm stands out as a promising alternative in terms of its overall performance in estimating MPP parameters accurately and reliably.

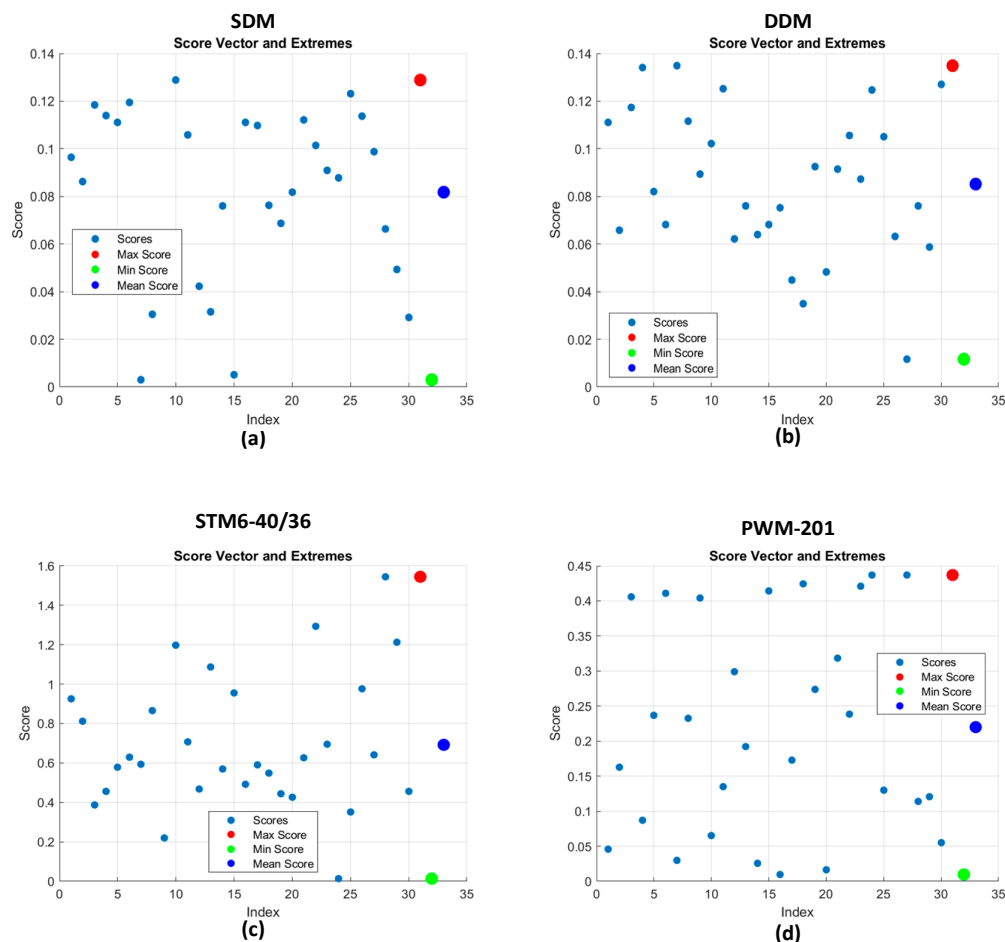


Figure 12. Statistical scores (RMSE) of all runs (30) by FLO algorithm: (a) SDM. (b) DDM. (c) STM6-40/36 and (d) Photowatt PWP-201.

Table 11. Comparison of I_{MP} , V_{MP} and P_{MP} for proposed FLO algorithm.

Data Sets	Parameter	Measured data	FLO (Proposed)	BMO [59]	FA [59]	HFAPS [59]
R.T.C France	$V_{MP}(v)$	0.459	0.459	0.449	0.4509	0.4506
	$I_{MP}(I)$	0.6755	0.67352	0.692	0.6894	0.6894
	$P_{MP}(w)$	0.31005	0.30915	0.3107	0.31085	0.31064
STM6-40/36	$V_{MP}(v)$	16.98	16.98	-	17.045	16.973
	$I_{MP}(I)$	1.5	1.504	-	1.494	1.500
	$P_{MP}(w)$	25.47	25.5381	-	25.477	25.459
PWM-201	$V_{MP}(v)$	12.4929	12.4929	-	12.618	12.645
	$I_{MP}(I)$	0.9255	0.9256	-	0.9085	0.9125
	$P_{MP}(w)$	11.5622	11.5634	-	11.463	11.539

4.4. Discussion

The performance of the FLO algorithm is evaluated, and various analyses are performed in this study. In these analyses; 3 reference PV models, namely R.T.C France, STM6-40/36, Photowatt-PWP201 data sets, were used. The FLO algorithm stands out with its low RMSE values obtained for both SDM and DDM models tested with R.T.C France module data. In the SDM model, FLO outperformed the other compared algorithms with a very low RMSE value of 0.0030375. It is especially more successful compared to methods such as HPSOS (0.0071) and BFA (0.029). In the DDM model, FLO's RMSE value of 0.011538 is lower than popular optimisation methods such as SA (0.01664) and PSO (0.0166). These results show that the proposed algorithm is effective for parameter optimisation in PV systems. In addition, in the comparative analysis with the SDM model with STM6-40/36 module data, more successful results were obtained than the compared algorithms (such as TAPSO: 0.013423, CIABC: 0.02518) with an RMSE value of 0.012036. In the analysis performed with Photowatt-PWP201 module data, FLO has been strongly proven to achieve much more successful results compared to algorithms such as WOA (0.2838) and SCA (0.0117780) by providing the lowest error rate with an RMSE value of 0.0097545. It is evident that the proposed FLO algorithm provides more consistent and accurate parameter extraction than MVO, HPSOSA, BFA, GA, SA, PS, WOA, BOA, PSO, OBSCA, TAPSO, ABC, SCA, CIABC, WDO, FA, ASO, newton optimisation techniques. Although these methods are successful in specific parameter extraction, the overall performance of FLO is stronger in terms of accurate estimation of all parameters. Moreover, in order to test the accuracy of the measured and estimated parameter values, error metrics such as IAE, RE, MAE are also calculated and given in Tables 4, 5, 8 and 9. Furthermore, for each analysed model, the measured and estimated parameter values are compared in Figures 4, 5, 8 and 9 and the convergence curves of the proposed FLO algorithm are presented in Figures 6 and 10. All these analysis results show that the proposed algorithm provides accurate solutions in both theoretical and practical applications.

5. Conclusions

In this paper, a novel FLO algorithm is proposed to estimate the unknown parameters in PV cells and N-R numerical method is integrated to improve the efficiency of the algorithm. In order to reveal the potential of the algorithm, analyses were performed on single and dual diode electrical models using R.T.C France, STM6-40/36 and Photowatt-PWP-201 real module data. In addition, IAE, RE and MAE error metrics were calculated. These error metric results, the lowest RMSE value obtained compared to other compared algorithms, consistent statistical metrics (such as max, min, mean, std, var) and highly accurate matched MPP point, suggest that the proposed FLO algorithm offers a powerful alternative that increases efficiency with precise parameter estimation, especially in PV cells. Furthermore, it is shown that the proposed FLO algorithm provides a strong agreement and parallelism between the I-V and P-V characteristics of the measured and estimated parameter values. As a result, FLO has a wide application potential in the design and performance analyses of solar energy systems. Especially, it is an effective tool for efficiency analyses of photovoltaic modules,

simulation of panel performance and improving accuracy in system design. In addition, FLO's low error rates and results compatible with physical parameters support its use in the industrial field. This algorithm is expected to be useful in industrial applications to provide optimum design and efficiency in solar energy systems. The following topics are planned to be focussed in future studies.

- The FLO algorithm will make significant contributions to the development of PV cell models in a more dynamic way through hybrid approaches created by integration with different algorithms.
- Experimental studies will be carried out with module data including different operating conditions in order to verify the practical effectiveness of the FLO algorithm.
- Studies will be carried out on the applicability of FLO algorithm to the solution of optimisation problems in various fields.

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