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Article

Entropy as First Principle: Deriving Quantum and Gravitational Structure from Thermodynamic Geometry

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Abstract: This paper introduces the Total Entropic Quantity (TEQ) framework, a structural reformulation of quantum theory grounded in two foundational axioms. **Axiom 0** posits entropy as a generative constraint: a geometric principle that determines which configurations can stably distinguish themselves, independent of space, time, or dynamics. Here, entropy refers to a curvature-functional over distinguishability configurations, maintaining only those structural patterns that remain stable or well-posed under finite informational resolution—that is, structures that are not destroyed or dissolved by coarse-graining or limited observability. **Axiom 1**, the Minimal Principle (MP), selects from these configurations those that remain maximally resolvable under finite entropy resolution. From this entropic foundation, core features of quantum theory—including the Born rule, Schrödinger dynamics, quantization, and gravitational structure—emerge as consequences of variation within an entropy-curved geometry. TEQ unifies quantum coherence, classical emergence, and spacetime curvature under a single informational principle, replacing conventional postulates with entropy-stabilized structure. The framework predicts deviations in high-curvature regimes and reinterprets physical law as the geometry of distinguishability rather than imposed dynamics.

Keywords: entropy-weighted path integral; thermodynamic quantization; minimal principle; entropy geometry; entropy curvature; emergent quantum theory; distinguishability; information-theoretic physics; quantum foundations; gravitational thermodynamics

Prelude: Entropy as Generative Principle

This prelude introduces the core inversion of TEQ: entropy is not a consequence of physical law, but its origin. Not a statistical residue, entropy is the generative structure that defines which distinctions are possible, and which configurations persist. From this perspective, physics does not begin with space, time, or quantization—it begins with resolvability. Axiom 0 defines entropy as a geometric constraint on distinguishability; Axiom 1 (the Minimal Principle) selects maximally stable patterns within that structure. Together, they replace classical and quantum postulates with a single condition: stability under entropy curvature. (See Section 4 for how entropy curvature deforms canonical structure and induces quantization.)

This reframes the deepest question—Why does the world unfold as it does?—as a question of dimensionality. In TEQ, causality is not fundamental but emergent: it arises only when entropy flow becomes rich enough to stabilize distinctions across configurations. Our universe appears causal because it inhabits a regime— $D_S \ge 4$ —where distinctions align, persist, and order themselves in time. Causality, in this view, is a structural consequence of high-dimensional entropy geometry.

This paper proposes a simple but radical idea: *entropy is the structural foundation of physics*. Rather than treating entropy as a byproduct of classical or quantum systems, we reverse the hierarchy: entropy determines which structures are physically realized.

The Total Entropic Quantity (TEQ) framework formalizes this shift through two structural axioms:

Formal Statement of Core Axioms

Axiom 1 (Axiom 0 — Entropy Geometry as Generative Constraint). There exists a pre-geometric configuration space C equipped with an entropy functional $\tilde{S}: C \to \mathbb{R}$, such that physical structure arises from the local curvature of \tilde{S} . Configurations $\phi \in C$ are said to be resolvable if they correspond to local minima or stationary points of entropy curvature, defined by the second variation:

$$\delta^2 \tilde{S}[\phi] := \frac{\delta^2 \tilde{S}}{\delta \phi^2}.$$

Only those configurations with non-negative, finite entropy curvature are stable and physically meaningful.

Remark 1 (Conceptual Meaning of Axiom 0). *Axiom 0 asserts that entropy is not merely a secondary property—such as disorder—but the fundamental structure determining what distinctions are physically possible. It defines a geometric landscape: a map of what can and cannot be resolved.*

This reverses the conventional hierarchy: physical law emerges not from postulated dynamics but from entropy geometry. The novelty lies here: structure precedes evolution, and resolution precedes spacetime.

Axiom 2 (Axiom 1 — Minimal Principle (MP)). Let $\mathcal{P} \subset \mathcal{C}$ denote the set of resolvable trajectories. The physically realized subset $\mathcal{P}_{phys} \subset \mathcal{P}$ consists of those paths that extremize entropy-weighted distinguishability. Formally, they minimize the entropy-weighted action:

$$S_{eff}[\phi] = S[\phi] - i\hbar\beta\tilde{S}[\phi],$$

where $S[\phi]$ is the classical action and $\beta \in \mathbb{C}$ is a structural Lagrange multiplier. These paths are entropy-stationary:

$$\delta S_{eff}[\phi] = 0.$$

Remark 2 (Conceptual Meaning of the Minimal Principle). The Minimal Principle (MP) posits that nature favors configurations that remain maximally distinct under entropy flow. It replaces assumptions about dynamics with a single criterion: the stability of distinctions. Classical paths, quantum amplitudes, and gravitational curvature all arise as consequences of this entropic variational condition.

Distinguishability arises from the geometry of entropy. Configurations are distinct if their differences remain resolvable under finite resolution. As resolution fades, distinctions dissolve. There is no absolute separability—only relative persistence. Particles, observers, and events are not fundamental entities but stabilized patterns within this entropy-defined structure.

Together, these axioms replace the postulates of classical and quantum mechanics with a single geometric principle: resolvability under entropy curvature. The Minimal Principle plays the role of a variational condition—not over action, but over the stability of distinction itself.

From this constraint, core features of quantum theory emerge:

- The **Born rule** arises from entropy-weighted path selection;
- The **Schrödinger equation** from entropy-curved variation of action;
- Commutation relations as geometric deformations induced by entropy structure;
- Quantization as a condition of entropic stability, not a postulate;
- Measurement and decoherence as entropy redistribution across latent and realized structure;
- Gravity as curvature in entropy geometry where gradients become irreversible.

The constants \hbar , β , and k_B are reinterpreted as structural multipliers linking phase coherence to entropy resolution. Their interrelations are derived from geometry—not imposed. Each of these results is developed from first principles in Sections 5, 6, and 7.

Not how entropy emerges from quantum mechanics, but how quantum mechanics emerges from entropy.

This reorientation makes quantum theory a special case of entropic structure and predicts deviations in strongly curved entropy regimes—where coherence, dynamics, and gravitation converge.

1. Introduction

Quantum mechanics (QM), despite its unrivaled empirical success, is traditionally introduced through axioms whose deeper origins remain opaque [1,2]. Core elements—the Born rule, wavefunction collapse, and quantization—are postulated rather than derived, leaving foundational questions unresolved [3–5].

The *Total Entropic Quantity* (TEQ) framework proposes a reversal of this structure: quantum behavior is not fundamental, but emerges from entropy. Rather than treating entropy as a secondary thermodynamic quantity, TEQ reinterprets it as the generative constraint governing all physical evolution. Quantum coherence, measurement, and classicality arise from a variational principle in which entropy and action jointly constrain viable trajectories.

At the core of TEQ is a decomposition of entropy into three dynamically coupled components:

- Realized entropy local macroscopic disorder;
- Latent entangled entropy nonlocal quantum correlations;
- Latent classical entropy quasi-stable, decohered structure encoding memory.

This triadic view reframes the quantum-to-classical transition as a continuous redistribution of entropy, eliminating the need for discontinuous collapse or observer-centric postulates. TEQ further introduces the concept of **entropy dimensions** D_S , classifying the effective dimensionality of entropy flow:

- $D_S = 0$: nonlocal entangled phase space;
- $D_S \in [2,3)$: latent classical correlations (e.g., pointer states);
- $D_S \ge 4$: realized macroscopic structure and spacetime irreversibility.

We reformulate TEQ around a single meta-constraint that replaces traditional axioms:

Minimal Principle (MP):

Physical trajectories are those that remain maximally distinguishable relative to the entropy dimensionality D_S of their domain. (See Section 8 for a unified summary of the principle and its structural consequences.)

This principle defines physical evolution through geometric constraints. Entropy structure and resolution together determine which configurations persist. From this, we derive:

- Derivation of an entropy-weighted path integral from first principles;
- The emergence of β as a Lagrange multiplier governing entropy weighting;
- The Born rule and its entropy-curvature corrections;
- The Schrödinger equation and quantization as stability conditions;
- Classicality as the smooth-limit behavior of entropy geometry.

The path integral evaluates relative distinguishability among trajectories, with entropy gradients acting as geometric filters that select thermodynamically viable paths; the associated entropy curvature, which governs deformation of phase structure, is defined formally in Section 4.

Unlike other entropy-based approaches—such as Entropic Dynamics [6] or Jaynesian inference [7]—TEQ does not assume standard quantum structure. It predicts testable deviations in regimes of strong entropy curvature, including:

- Gravitational and cosmological quantum systems [8–10];
- Ultra-isolated and far-from-equilibrium quantum systems;
- Nonlinear decoherence and entropy-sensitive corrections to standard dynamics [4,5].

These include modified Born statistics, altered coherence times, and constraints on quantization tied to entropy geometry. TEQ thus opens a new route to probing the entropic foundations of quantum theory.

We refer to the *geometrothermodynamic limit* as the regime in which entropy curvature governs the dominant structural behavior, allowing simplified descriptions where local fluctuations are subordinated to large-scale thermodynamic geometry. Many of the results in this manuscript, such as quantization, classical emergence, and gravitation, are derived as structural consequences within this regime.

Remark 3 (Conceptual Intuition and Broader Significance). At its core, the TEQ framework proposes that physical structure arises from the geometry of entropy itself. Instead of treating quantum laws and gravitational dynamics as fundamental, TEQ starts with a simpler idea: systems evolve along paths that remain maximally distinguishable under entropic constraints. This guiding principle leads to the emergence of quantum amplitudes, spacetime structure, and even fundamental constants, as consequences of a deeper entropic geometry.

This perspective matters beyond physics. It suggests that the very notion of "what exists" depends on what can be resolved or distinguished—an idea with deep resonance in information theory, complexity science, and the philosophy of measurement. In TEQ, quantization is not imposed but arises from structural limits on distinguishability. Entropy is not a measure of ignorance, but a generative principle that shapes what can be known, stabilized, or predicted. This reorientation offers a new foundation for understanding coherence, irreversibility, and the emergence of classical reality.

Structure of the manuscript. Section 2 introduces the entropy-weighted path integral and defines the effective action. Section 3 derives structural relations among \hbar , β , and k_B , identifying a two-dimensional dynamical surface. Section 4 interprets quantization as a geometric stability condition. Section 5 derives the Born rule and formulates corrections in high-curvature regimes. Section 6 presents the Schrödinger equation as a limit of entropy-stabilized evolution. Section 7 proposes an entropic basis for spacetime and gravity.

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Navigating TEQ

For orientation, we provide two reference tools: a structural overview diagram and a glossary of key terms. Figure 1 illustrates how the core axioms generate the major results of the theory, clarifying the dependency structure between assumptions, derivations, and physical consequences. The accompanying table summarizes central concepts, helping to reduce interpretive load–especially for interdisciplinary readers.

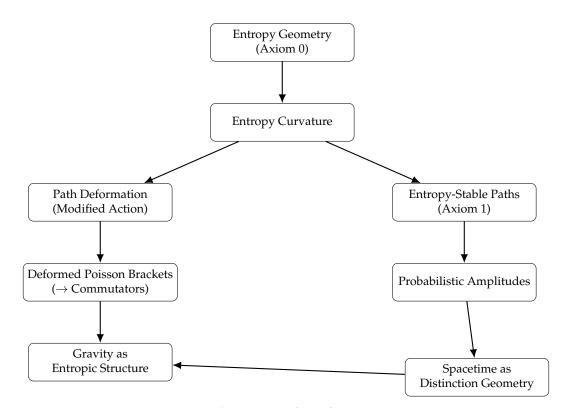


Figure 1. Structural generation of TEQ from entropy geometry

To further support conceptual clarity, Table 1 summarizes key terms used throughout the manuscript, with a focus on their operational meaning within the TEQ framework.

Table 1. Key terms and their definitions in the TEQ framework.

Term	Definition
Entropy Curvature	Second variation of the entropy functional; determines stability and induces metric structure.
Distinguishability	Degree to which configurations or paths are resolvable under entropy gradients.
TEQ Flow	Dynamical evolution along entropy-weighted gradients; generalizes classical geodesics.
Entropy-Dominant Regime	Regime where entropy curvature dominates over local fluctuations, allowing emergent structure to be described by thermodynamic geometry.
MP2 Paths	Trajectories selected by the principle of minimal entropy-stable distinction.
Entropy Functional	The core action-like quantity: $S[\phi] = \int g(\phi, \dot{\phi}) dt$; generates the entropy geometry.
Deformed Commutator	Modified algebraic bracket induced by entropy curvature; source of quantization.
TEQ Path Integral	Functional integral over entropy-weighted paths; selects dominant histories via curvature.
Entropic Metric	Effective metric on configuration space derived from entropy curvature.

Dynamical Regimes in TEQ. To clarify how standard physical behavior emerges from the TEQ framework, we introduce a structural taxonomy of dynamical regimes based on the dominance of

entropy versus action and the geometry of entropy flow. This classification helps distinguish the quantum limit, classical behavior, and novel entropy-dominant phases predicted by TEQ. Table 2 below summarizes these regimes and their associated features.

Table 2. Full regime typology in TEQ, indexed by dominant constraint, entropy type, entropy dimension D_S , entropy curvature κ , and selector angle θ .

Regime Name	Dominant Constraint	Dominant Entropy Type	D_S	К	θ	Description
Entropy-Dominant	Entropy Geometry	Any	Any	High	$ heta ightarrow \pi/2$	Entropy curvature dominates; standard variational methods fail.
Action-Dominant	Action Extremization	Any	Any	Low	heta o 0	Classical mechanics or standard Feynman path integrals.
Quantum Coherent Limit	Mixed	Entangled	$D_S \approx 0$	Variable	$ heta pprox \pi/2$	Nonlocal coherence dominates; supports interference.
Thermal/Pointer	Mixed	Latent Classical	$D_S \in [2,3)$	Moderate	$\theta \in (0,\pi/4)$	Partial decoherence; semi-stable classical structure.
Classical Macroscopic	Action Dominant	Realized	$D_S \geq 4$	Very Low	$\theta pprox 0$	Irreversible, decohered evolution; classical limit.
Entropy-Curvature Transition	Transition	Mixed	$D_S \approx 2$	Increasing	$\theta \in (\pi/4, \pi/2)$	Instability zone; TEQ effects begin to dominate.

Overview of Results

The Total Entropic Quantity (TEQ) framework rederives the foundational structures of quantum mechanics, thermodynamics, and spacetime from a single entropic variational principle: the *Minimal Principle* (MP). Rather than assuming conventional postulates, TEQ shows that quantum and classical behavior **emerge** from entropy-weighted selection among resolvable configurations.

This section summarizes the main results and contrasts standard quantum postulates with their derivations or reinterpretations under TEQ.

Key Contributions

- Entropy-Weighted Path Selection: TEQ replaces the classical action principle with a variational principle derived from the Minimal Principle (Axiom 1): *physical trajectories are those that remain maximally distinguishable under entropy flow.* This yields:
 - The Born rule as a statistical consequence of entropy-stabilized trajectories,
 - The Schrödinger equation from entropic deformation of classical action,
 - Commutation relations and quantization from entropy-curved geometry.
- Entropy Dimensions D_S : A classification of entropy flow regimes:
 - $D_S = 0$: Nonlocal entanglement,
 - $D_S \in [2,3)$: Latent classical correlations,
 - $D_S \ge 4$: Realized macroscopic structure and time-asymmetry.
- **Unified Constants**: The constants \hbar , k_B , and G emerge as structural multipliers across distinct entropic regimes, linking phase coherence, resolution, and curvature.
- Minimal Principle as Structural Generator: All physical structure—quantization, coherence, decoherence, and classicality—arises from the Minimal Principle (Axiom 1). This replaces conventional dynamical and measurement postulates with a single entropic variational condition.

Postulates Reinterpreted via TEQ

Table 3 contrasts standard quantum postulates with their TEQ counterparts, all derived from the Minimal Principle. Rather than assuming structures such as unitary evolution or canonical quantization, TEQ reconstructs them as emergent features of entropy geometry. This unifies quantum and thermodynamic reasoning and reframes quantization as a consequence of constrained resolution.

Table 3. Standard quantum postulates vs. TEQ derivations from the Minimal Principle (MP). These results rely on Axiom 0, which defines the entropy-curved configuration space within which MP selects physically viable trajectories.

Standard Postulate or Structure	Derived or Reframed via TEQ Status in TEQ (via M	
Born Rule $P = \psi ^2$	Emerges from entropy-weighted path integral in the large- β limit	Derived (under MP)
Unitary Evolution $U(t) = e^{-iHt/\hbar}$	Emerges as a limiting case for $\beta = \frac{i}{\hbar}$; generalized to complex entropy weights	Emergent (in limit)
Superposition Principle	Results from interference among entropy-stable paths	Emergent (via entropy paths)
Schrödinger Equation	Derived from entropy-stabilized variation of the action	Derived (from stability)
Canonical Commutation $[x, p] = i\hbar$	Emerges from entropy-curvature de- formation of symplectic geometry	Emergent (via geometry)
Quantization	Results from stability filtering under entropy gradients	Emergent (under MP)
Hilbert Space	Appears as an effective approximation from entropy-stable interference; linearity is not fundamental	Emergent (under MP)
Measurement Axiom	Replaced by entropy-defined distinguishability and observer resolution	Reframed (observer- based)
Partition Function $Z = \sum e^{-\beta E}$	Recovered from path integral via imaginary-time continuation	Derived (in thermody- namic form)
Thermodynamic Ensembles	MaxEnt over constrained path distributions derived from MP	Derived (via MaxEnt)
Arrow of Time / Irreversibility	Emerges from the structure of entropy flow for $D_S \ge 4$	Emergent (from D_S)

2. The Entropy-Weighted Feynman Path Integral from a Minimal Principle

This section derives the Feynman path integral as a consequence of TEQ's structural axioms. Rather than postulating quantum behavior, we show that entropy-weighted amplitudes emerge from the Minimal Principle (MP), which governs stability under finite resolution. Classical action is generalized into a geometric entropy functional, and the resulting dynamics favor entropy-resilient trajectories. The standard quantum amplitude arises in the limit of vanishing entropy curvature. By embedding thermodynamic stability into the variational structure, this approach recasts quantization as a response to entropy-induced instability in trajectory space.

In TEQ, quantum structure is not assumed—it is derived from a single variational constraint:

Minimal Principle (MP):

Physical trajectories maximize distinguishability of entropy flow under structural constraints.

This principle unifies path selection, thermodynamic stability, and quantum amplitudes. The Feynman path integral emerges naturally as a statistical expression of entropy-weighted distinguishability, generalizing classical action into entropy geometry.

2.1. Standard Amplitude Formulation

In standard quantum mechanics, the transition amplitude is given by:

$$\mathcal{A} \propto \int \mathcal{D}[\phi] \, e^{iS[\phi]/\hbar},$$
 (1)

where $S[\phi]$ is the classical action, and $\mathcal{D}[\phi]$ integrates over all histories. All paths contribute equally in magnitude; only phase varies [11]. This implicitly assumes no entropy-based preference among paths.

In TEQ, uniform amplitude is recovered only when entropy curvature vanishes. In general, entropy-instability leads to suppression: paths with higher entropy production contribute less. This is not added by hand—it arises directly from the Minimal Principle. Decoherence hints at this mechanism: paths differing significantly in entropy production interfere less, biasing evolution toward entropy-stable trajectories.

2.2. Entropic Weighting as a Consequence of MP

Lemma 1 (Entropy Bias from the Minimal Principle). *The Minimal Principle selects trajectories based on entropy stability. This weighting parallels the Feynman–Vernon influence functional* [12]:

$$\mathcal{A} \propto \int \mathcal{D}[\phi] e^{iS[\phi]/\hbar} \mathcal{F}[\phi], \quad \mathcal{F}[\phi] = e^{-\mathcal{I}[\phi]},$$
 (2)

where $\mathcal{I}[\phi]$ encodes entropy-producing interactions, structurally analogous to decoherence functionals in opensystem quantum theory [4,13].

TEQ does not postulate this suppression—it derives it (see Appendix A). Entropy weighting follows naturally from constrained optimization of distinguishability under MP, introducing the Lagrange multiplier β . The entropy functional $\tilde{S}_{apparent}[\phi]$, defined below, captures the observer-resolvable entropy flow.

2.3. Entropy-Weighted Amplitudes from MP

In Appendix A.5, we derive:

Theorem 1 (Path Amplitudes from the Minimal Principle). *The effective amplitude for a path* ϕ *is:*

$$\mathcal{A}_{eff}[\phi] \propto \exp\left(\frac{i}{\hbar}S[\phi] - \beta \,\tilde{S}_{apparent}[\phi]\right),$$
 (3)

where $\beta \in \mathbb{C}$ arises from constrained variation. The classical Feynman integral is recovered in the limit $\beta \to 0$.

The parameter β interpolates between dynamical regimes. When $\beta = \frac{1}{\hbar}$, standard unitary evolution emerges; when $\beta = \frac{1}{k_B T}$, the system enters a thermal regime. These are not independent assumptions but limiting cases of a unified structure.

As derived in Appendix B, the effective action becomes:

$$S_{\rm eff}[\phi] = \int dt (L(\phi, \dot{\phi}) - i\hbar\beta \, g(\phi, \dot{\phi})), \tag{4}$$

where $g(\phi, \dot{\phi})$ is the entropy flux functional, arising naturally from the local geometry of the entropy metric.

Remark 4 (Entropy Weighting, Measure Instability, and Path Selection). *In standard quantum mechanics, all paths contribute equally to the path integral, differing only by phase. TEQ introduces entropy flow as a geometric constraint that modifies this principle. Trajectories are no longer treated symmetrically: paths that lead to steep entropy gradients are exponentially suppressed, as they imply a loss of stable, resolvable distinctions. The*

entropy weighting term $e^{-\beta \tilde{S}_{apparent}[\phi]}$ breaks the uniformity of the measure, introducing exponential sensitivity to entropy curvature.

In regimes of strong entropy variation, the unmodified path integral becomes unstable: infinitesimally close trajectories can differ exponentially in weight due to high entropy curvature, rendering the standard measure ill-defined. TEQ resolves this by selecting only entropy-stationary trajectories, around which the weighting becomes sharply peaked and stable. This eliminates the singular behavior and motivates a deformation of the variational geometry itself. Quantization thus emerges not as an axiom, but as a structural response to entropy-induced instability in trajectory space.

2.4. Interpretation and Structural Role of β

The constants \hbar and β emerge as dual Lagrange multipliers (see Appendix A.5):

- β suppresses entropy-unstable paths;
- \hbar preserves phase coherence;
- Together, they govern entropy-weighted quantum dynamics.

Corollary 1 (Born Rule from the Minimal Principle). *The Born rule arises naturally in the large-* β *limit from suppression of entropically unstable paths. Probabilities reflect stability, not fundamental indeterminism. See Section 5.*

Paradigm Shift. Quantum amplitudes emerge as structural consequences of entropy-weighted distinguishability. The Minimal Principle selects viable trajectories. β and \hbar are thus structural multipliers—not independent parameters.

2.5. Modified Euler-Lagrange Equation

Theorem 2 (Entropy-Corrected Dynamics from MP). *Variation of the entropy-weighted action* (4) *yields:*

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\phi}} - i\hbar \beta \frac{\partial g}{\partial \dot{\phi}} \right) - \left(\frac{\partial L}{\partial \phi} - i\hbar \beta \frac{\partial g}{\partial \phi} \right) = 0. \tag{5}$$

This extends classical extremality by introducing geometric bias favoring entropy-stable trajectories.

Remark 5 (Intuitive Meaning of Entropy Curvature). Entropy curvature measures how rapidly entropy production changes as we move between different paths. Intuitively, high entropy curvature corresponds to regions where small changes in trajectory lead to large changes in distinguishability. The Minimal Principle favors paths that remain stable under these variations—effectively selecting trajectories that avoid steep entropy gradients. Thus, entropy curvature functions like a landscape of stability: physical paths settle into entropy-stable valleys rather than entropy-unstable peaks.

In the limit $\beta \to 0$, standard quantum or classical mechanics is recovered.

Corollary 2 (Entropy-Stabilized Classical Emergence). *As* $\hbar \to 0$, the classical Euler–Lagrange equation reemerges, but entropy curvature continues filtering viable macroscopic paths. Classicality is thus a stabilized limit of entropy geometry.

Paradigm Shift. The least-action principle is generalized by the Minimal Principle. Physical evolution selects entropy-resilient paths. Classical mechanics is thus not fundamental but emerges naturally as the stable, entropy-filtered limit of quantum dynamics.

3. Geometric Structure of Fundamental Constants

This section analyzes how the apparent constants of nature—Planck's constant \hbar , the inverse temperature parameter β , and Boltzmann's constant k_B —emerge within TEQ as projections of a

unified entropy-action geometry. Rather than being fixed, irreducible inputs, these quantities reflect structural relationships that govern resolvability and coherence under entropy curvature. By making this geometry explicit, we show that these constants are neither fundamental nor independent, but arise as limiting behaviors within a minimal two-dimensional framework. The result is a principled reinterpretation of physical constants as emergent from the same entropic structure that underlies quantum and thermal dynamics.

In the Total Entropic Quantity (TEQ) framework, the constants \hbar , β , and k_B are not fundamental. They emerge as structural parameters governing entropy-resolved path distinguishability.

Remark 6 (Why Constants Are Not Fundamental). In traditional physics, constants such as \hbar , β , and k_B are taken as irreducible inputs—fixed quantities defining the behavior of quantum, thermal, and statistical systems. In TEQ, these constants instead emerge from the geometry of entropy and action. They are not intrinsic to the universe, but arise as structural parameters that encode how finely distinctions can be resolved, and how entropy suppresses or stabilizes certain paths. Their apparent constancy reflects the stability of entropy geometry under specific regimes, not fundamental necessity.

This structure follows from two generative assumptions:

- Axiom 0: Entropy defines a geometric field over possible configurations, establishing resolvability;
- **Axiom 1 (Minimal Principle):** Physical paths remain maximally distinguishable within this entropy geometry.

From this foundation, the constants \hbar , β , and k_B emerge as interdependent projections within a unified geometric structure.

Minimal Principle and Entropic Selector

Consider first the entropy-weighted amplitude introduced in TEQ:

$$\mathcal{A}[\phi] = \exp\left(\frac{i}{\hbar}S[\phi] - \beta \tilde{S}_{\mathrm{apparent}}[\phi]\right).$$

This amplitude structurally distinguishes two fundamental aspects:

- an *imaginary* component, governing quantum coherence via the action $S[\phi]$;
- a *real* component, encoding thermodynamic irreversibility via entropy $S_{\text{apparent}}[\phi]$.

This duality strongly suggests a simple geometric representation in terms of a two-dimensional entropy-action plane. Specifically, we represent amplitudes through linear projections onto this plane using a complex *selector vector* $\vec{\xi} \in \mathbb{C}^2$:

$$\vec{\xi} = \lambda \begin{bmatrix} e^{i\theta} \\ -e^{-i\theta} \end{bmatrix} = \lambda \begin{bmatrix} \cos \theta + i \sin \theta \\ -\cos \theta + i \sin \theta \end{bmatrix},$$

where the magnitude $\lambda \in \mathbb{R}^+$ sets the overall scale, and the selector angle $\theta \in [0, \frac{\pi}{2}]$ modulates the balance between quantum coherence (imaginary) and entropy-driven dissipation (real).

Remark 7 (Rationale for the Linear Geometric Assumption). The choice of a linear two-dimensional geometry to represent the entropy-action structure is not arbitrary, but is motivated by simplicity and direct correspondence to the inherently real and imaginary decomposition of amplitudes. While nonlinear or higher-dimensional generalizations could be considered—particularly in regimes of strong entropy curvature or complex multi-scale interactions—the linear geometric assumption constitutes the simplest, conceptually transparent, and analytically tractable choice that fully captures the dual role of entropy and action. Future extensions might explore nonlinear geometric structures or higher-dimensional selectors, particularly where empirical deviations from standard quantum predictions necessitate more complex geometries.

Matching this geometric selector explicitly to the amplitude structure:

$$\frac{i}{\hbar} = \lambda(\cos\theta + i\sin\theta), \qquad -\beta = \lambda(-\cos\theta + i\sin\theta),$$

we immediately recover the fundamental parameters in geometric form:

$$\frac{1}{\hbar} = \lambda \sin \theta, \qquad \beta = \lambda \cos \theta.$$

Thus, the dimensionless entropy-resolution parameter emerges as:

$$\alpha := \beta \hbar = \cot \theta$$
.

This parameterization gives a direct geometric interpretation of θ as a fundamental dial tuning the balance between quantum coherence and entropic dissipation:

- **Quantum-coherent limit** ($\theta \to \pi/2$): entropy curvature vanishes; dynamics become unitary.
- Classical-thermal limit ($\theta \to 0$): entropy dominates, coherence is suppressed, and dynamics become fully dissipative.

The selector vector, therefore, is not introduced as an independent postulate. Rather, it explicitly encodes a structure *already implicitly present* in the TEQ amplitude. Making this structure explicit clarifies the underlying geometric unity, illustrating clearly how the constants \hbar , β , and k_B emerge naturally from a minimal geometric assumption.

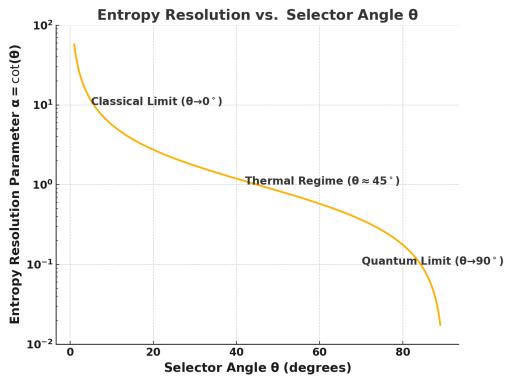


Figure 2. Entropy resolution parameter $\alpha = \cot(\theta)$ as a function of selector angle θ . The quantum limit corresponds to $\theta \to \pi/2$, the classical/thermal limit to $\theta \to 0$.

Dimensional Consistency and the Role of k_B

To restore thermodynamic units, define:

$$\alpha := \beta \hbar = \frac{\hbar}{k_B T} \quad \Rightarrow \quad \beta = \frac{\hbar}{\alpha k_B}.$$

Theorem 3 (Unified Constants from Entropy Geometry). *The constants* \hbar , β , and k_B arise from a two-dimensional entropy-action geometry:

$$\frac{1}{\hbar} = \lambda \sin \theta, \qquad \beta = \lambda \cos \theta, \qquad \alpha = \cot \theta.$$

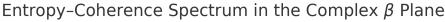
Corollary 3 (Entropy-Coherence Scaling and Limiting Regimes). *The dimensionless parameter* $\alpha = \cot \theta$ *governs the balance between entropy suppression and phase coherence. It defines the dynamical regime of the system, with limiting behaviors:*

- Quantum (unitary): $\alpha = i \Rightarrow \beta = \frac{i}{\hbar}$;
- Thermal: $\alpha = \frac{\hbar}{k_B T} \ll 1$;
- *Intermediate:* $\beta \in \mathbb{C}$, partial coherence regimes.

Feynman and Boltzmann weights emerge as limits of the same entropy-weighted structure, and the constants \hbar and k_B act as scale-setting factors for phase coherence and entropy resolution. Representative values are summarized in Table 4.

Table 4. Representative values of β across physical regimes, illustrating the entropy–coherence spectrum. See Appendix C for derivation details.

Regime	Representative β	Interpretation
Room temperature ($T \approx 300 \mathrm{K}$)	$\sim 2.4 \times 10^{20} J^{-1}$	Classical-thermal
Quantum limit (unitary)	$\beta = \frac{i}{\hbar} \sim i \times 10^{34} \mathrm{J}^{-1}$	Coherence-dominated
CMB temperature ($T \approx 2.7 \text{K}$)	$\sim 2.7 \times 10^{22} \text{J}^{-1}$	Weak entropy flow
Planck temperature ($T_P \sim 1.4 \times 10^{32} \mathrm{K}$)	$\sim 10^{-9} \mathrm{J}^{-1}$	Action-dominated



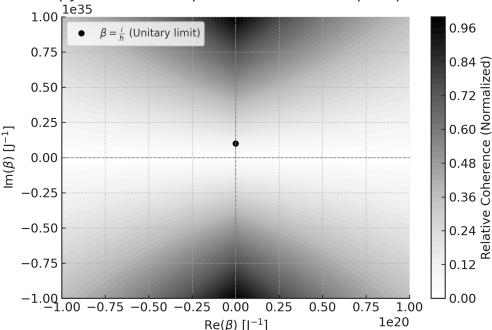


Figure 3. Entropy—coherence spectrum in the complex β plane. The grayscale intensity encodes relative coherence strength, with higher values corresponding to stronger phase coherence. The imaginary axis captures coherent dynamics ($\beta = \frac{i}{\hbar}$), while the real axis corresponds to entropy-dominated suppression regimes ($\beta \in \mathbb{R}^+$). The plot illustrates how TEQ interpolates between quantum and thermodynamic behavior through variations in entropy geometry.

Remark on the Emergence of Unitarity. In TEQ, unitarity is not a fundamental postulate but an emergent behavior in the flat-curvature, coherence-dominated limit of the entropy-weighted action. It arises when entropy flow vanishes and the system approaches maximal resolution, with $\beta = \frac{i}{\hbar}$. In this regime, amplitudes evolve purely oscillatory and probability is conserved through unitary dynamics.

As entropy gradients activate and curvature grows, coherence is lost and evolution becomes non-unitary. Dissipation, decoherence, and irreversibility are thus not anomalies to be explained away, but intrinsic consequences of entropy-weighted structure. Conservation is not violated, but generalized: replaced by structural distinguishability across entropy-curved paths.

TEQ implies that unitarity is not generic, but a special case realized only when entropy curvature vanishes. In strongly curved regimes—such as early cosmology, black hole evaporation, or macroscopic decoherence—non-unitary evolution is structurally expected. See Appendix F for standard approaches to handling non-unitarity.

Observer Resolution and Gauge Structure

The parameter $\alpha = \beta \hbar$ encodes the entropy resolution available to the observer—how finely entropy-distinguishable structure can be resolved. Shifts in θ act as gauge transformations in the entropy geometry [14,15], leaving the underlying dynamics invariant but altering the resolution scale.

Structural Role of Axiom 0. The geometric relationships among \hbar , β , and k_B are not imposed. They arise from a prestructured entropy geometry (Axiom 0), constrained by the Minimal Principle (Axiom 1). Constants are projections of resolution and coherence within this geometry.

4. Quantization as Entropic Deformation of Symplectic Geometry

This section derives quantization as a geometric consequence of entropy-stabilized dynamics. In TEQ, classical symplectic geometry becomes unstable under entropy curvature, and the variational structure deforms to preserve distinguishability. This deformation leads to modified conjugate momenta, noncanonical Poisson brackets, and ultimately to quantum commutators. Quantization thus arises not from postulates or operator formalism, but from the failure of classical resolution in entropy-curved phase space. By tracing how entropy flow modifies the effective action and phase structure, we show that noncommutativity encodes the minimal distinguishability permitted by entropy geometry.

In TEQ, quantization and noncommutativity are not postulated but arise as necessary geometric consequences of entropy structure. The central idea is that entropy flow governs the resolvability of trajectories. When entropy curvature $\kappa \neq 0$, the underlying geometry of phase space is no longer flat and classical symplectic structure fails to describe stable evolution. Instead, TEQ imposes a variational constraint that selects only those trajectories which remain distinguishable under entropy deformation.

This modifies the effective phase space geometry, leading to a generalized conjugate momentum, deformed Poisson brackets, and eventually noncommutative operator structure. Quantization thus becomes a stability condition rooted in thermodynamic distinguishability, not an externally imposed axiom.

4.1. Entropy-Weighted Dynamics and Effective Momentum

Lemma 2 (Entropy-Weighted Momentum). Given the entropy-weighted effective action

$$S_{eff}[\phi] = \int dt [L(\phi,\dot{\phi}) - i\hbar\beta g(\phi,\dot{\phi})],$$

the effective momentum is

$$\Pi_{e\!f\!f}=rac{\partial L}{\partial \dot{\phi}}-i\hbar eta rac{\partial g}{\partial \dot{\phi}},$$

generalizing classical conjugate momentum by incorporating entropy flow as a stabilizing term.

Remark on Hermitian and Non-Hermitian Structure. In TEQ, the effective action is complex-valued, with entropy flow contributing an imaginary deformation. The resulting Euler–Lagrange equation naturally incorporates dissipative structure, and the effective Hamiltonian may become non-Hermitian in regimes of strong entropy curvature. Hermiticity is not postulated, but emerges in the entropy-coherent limit where entropy flow is symmetric or negligible. Thus, both Hermitian and non-Hermitian dynamics are unified within a single variational principle, reflecting local geometry of entropy stability rather than arbitrary assumptions. Dissipation, decoherence, and resolvability loss correspond directly to non-Hermitian deformation.

Definition 1 (Entropy Curvature). *Entropy curvature is defined as*

$$\kappa := \frac{\partial^2 g}{\partial \dot{\phi}^2},$$

characterizing local constraints on distinguishability in velocity space.

This quantity measures how rapidly entropy flow $g(\phi,\dot{\phi})$ changes with respect to variations in velocity $\dot{\phi}$. A nonzero κ indicates that small fluctuations in trajectory velocity lead to measurable changes in entropy flow, thus affecting the stability and resolvability of the path. When $\kappa=0$, entropy suppression is uniform across paths; when $\kappa>0$, entropy acts as stabilizing curvature, filtering out rapidly diverging trajectories. This curvature term deforms the canonical phase structure, underpinning TEQ's generalized quantization conditions.

Remark 8 (Structure and Interpretation of the Entropy Functional $g(\phi, \dot{\phi})$). The entropy functional $g(\phi, \dot{\phi})$ plays a central role in the TEQ framework. It defines the local entropy flux along a trajectory, determining how resolvability varies under coarse-grained evolution. Unlike thermodynamic entropy, which is usually state-dependent, g is a rate-functional—it encodes how entropy is produced or dissipated during transitions between configurations.

Minimal Requirements:

- $g(\phi, \dot{\phi}) \ge 0$: entropy is not locally reversed under coarse-graining;
- g is at least C^2 in $\dot{\phi}$: ensures that curvature $\kappa = \partial^2 g / \partial \dot{\phi}^2$ is well-defined;
- g is observer-dependent: it encodes resolution limits, hence may vary with effective coarse-graining scale.

Illustrative Example: Free Particle with Resolution Cost. Consider a simple entropy functional:

$$g(\phi,\dot{\phi}) = \frac{1}{2}\dot{\phi}^2,$$

which penalizes high-velocity transitions due to their instability under coarse resolution. This choice implies:

$$\kappa = \frac{\partial^2 g}{\partial \dot{\phi}^2} = 1,$$

and leads directly to entropy-curvature-induced deformation of the momentum and commutator structure (see *Section 4*).

Generalizations: More complex systems may involve higher-order or non-quadratic forms of g, such as:

$$g(\phi,\dot{\phi}) = \frac{1}{2}A(\phi)\dot{\phi}^2 + B(\phi)\dot{\phi} + C(\phi),$$

where $A(\phi)$ acts as an entropy metric tensor. This form parallels Lagrangians with configuration-dependent mass and introduces spatially modulated entropy curvature.

Interpretive Note: The functional g does not depend on a prior thermodynamic system. It is emergent from the distinguishability structure and encodes the entropy penalty for transitioning between configurations at finite resolution. In this way, TEQ generalizes the notion of entropy flow into a purely geometric field over phase space trajectories.

Remark 9 (Intuitive Origin of Quantization from Entropy Geometry). *Quantization in TEQ emerges* because entropy curvature modifies how distinct states in phase space relate to each other. Classically, positions and momenta commute, reflecting infinite resolution of phase space structure. Entropy curvature introduces a fundamental resolution limit: states cannot be infinitely distinguished due to thermodynamic constraints. As a result, positions and momenta no longer commute exactly, manifesting as quantization. Conceptually, quantization is not an imposed rule, but a geometric necessity arising from the limited resolvability of paths under entropy constraints.

4.2. Deformation of Symplectic Structure

In classical mechanics, the Poisson bracket reflects the flat, globally resolvable geometry of phase space—each trajectory is distinguishable, and the symplectic structure remains uniform. But under entropy weighting, this assumption breaks down. When entropy curvature varies rapidly, the effective measure in the path integral becomes sharply nonuniform: trajectories arbitrarily close in configuration space can differ exponentially in entropic weight. This leads to a singular, ill-defined measure and signals a geometric instability in the classical variational framework. Classical resolution fails not due to stochasticity, but because the space of trajectories no longer supports uniform distinguishability. The path integral becomes dominated by a sparse set of entropy-stationary configurations, and the underlying symplectic structure must deform accordingly. Quantization thus emerges as a structural repair—restoring coherent dynamics in the presence of entropy-induced degeneracy.

To preserve well-defined evolution under these conditions, TEQ deforms the symplectic structure itself. This deformation ensures that path stability, distinguishability, and phase volume all remain consistent with the entropy-weighted action. The result is a curved, thermodynamically-constrained geometry of phase space.

In Appendix D.1, we derive:

Theorem 4 (Entropy-Deformed Poisson Bracket). *Entropy curvature modifies the classical Poisson bracket:*

$$\{\phi, \Pi_{eff}\}_{TEQ} = 1 - \frac{\beta}{m}\kappa.$$

This deformation reflects the shift from pure Hamiltonian dynamics to entropy-constrained trajectory space. The classical bracket is recovered as $\kappa \to 0$ or $m \to \infty$.

Theorem 5 (Quantization from Entropy-Curved Geometry). *From the entropy-weighted action (Eq.* (4)) and the resulting deformation of symplectic structure (Appendix D), the canonical commutator becomes:

$$[\hat{\phi},\hat{\Pi}_{\it eff}]=i\hbarigg(1-rac{eta}{m}\kappaigg),$$

where $\kappa := \frac{\partial^2 g}{\partial \dot{\phi}^2}$ is entropy curvature. The classical commutator emerges when $\kappa \to 0$.

Corollary 4 (Thermodynamic Origin of Noncommutativity). *Quantization is not postulated but structurally required: noncommutativity arises naturally as a geometric constraint from entropy-curved phase space. It encodes minimal resolvability of trajectories under entropy-driven stability.*

Remark 10 (Structural Role of Mass). The parameter m acts not as inertial mass per se, but as a buffer against entropy curvature. Canonical behavior is preserved if:

$$\frac{\beta}{m}\kappa \ll 1.$$

This suggests a thermodynamic interpretation of mass as resistance to entropic deformation, analogous to how mass resists spacetime curvature in general relativity (see Section ??).

Structural Insight. In TEQ, quantization is not imposed but derived. Entropy curvature makes classical phase space structure unstable to perturbations. The only trajectories that remain well-resolved under entropy-weighted variation are those consistent with a deformed, quantized geometry. Quantization thus arises as the only viable structure compatible with entropy-stabilized evolution.

4.3. Quantization from Entropic Mode Stability

Theorem 6 (Discrete Modes from Entropy Stationarity). In the entropy-weighted path integral

$${\cal A}_{\it eff}[\phi] = \int {\cal D}[\phi] \, e^{iS[\phi]/\hbar} \, e^{-eta ilde{S}_{\it apparent}[\phi]}$$
 ,

dominant contributions come from entropy-stationary paths. First-order stationarity yields:

$$p = \frac{\partial S}{\partial x} = i\hbar\beta \frac{\partial \tilde{S}_{apparent}}{\partial x},$$

showing quantized momenta arise as entropy-optimized configurations.

Remark 11 (Derivation and Intuition). *Extremizing the effective action yields:*

$$\delta S[\phi] = i\hbar\beta \,\delta \tilde{S}_{apparent}[\phi],$$

balancing dynamical cost against entropy distinguishability. Interpreting $p = \partial S/\partial x$ leads directly to quantized momenta as conditions ensuring stable distinguishability.

Corollary 5 (Entropy-Curvature Uncertainty Relation). *Entropy curvature modifies the uncertainty bound:*

$$\Delta\phi\,\Delta\Pi_{e\!f\!f}\gtrsim rac{\hbar}{1-rac{eta}{m}\kappa}.$$

Positive curvature increases the lower bound, reflecting thermodynamic limits on resolution.

Structural Insight. The uncertainty principle is entropy-sensitive. In TEQ, thermodynamics and quantization unify as constraints on stable distinguishability.

Remark on Hilbert Space Emergence. In TEQ, the Hilbert space formalism of quantum theory is not assumed but emergent. In the flat entropy-curvature limit and high-resolution regime ($\beta \gg 1$), the space of distinguishable amplitudes becomes effectively linear, with interference defining a well-behaved inner product. Hilbert space thus emerges naturally as the coherence-maximized, flat-curvature limit of entropy geometry. It encodes distinguishable, resolvable configurations under maximal resolution. Outside this regime—where

entropy curvature is strong or observer resolution limited—the Hilbert space description breaks down, and TEQ provides a more general variational structure.

5. Derivation of the Born Rule from the Minimal Principle

This section derives the Born rule not as a postulate but as a consequence of TEQ's Minimal Principle. In standard quantum theory, probabilities are assigned by fiat through squared amplitudes. In TEQ, these probabilities arise from entropy-weighted variation: only distinguishable, entropy-stable paths contribute significantly to the path integral. By expanding around entropy-stationary trajectories, we recover the Born rule as the entropy-flat limit and obtain explicit corrections from entropy curvature. The result grounds probabilistic outcomes in thermodynamic geometry, linking quantum statistics to structural resolvability.

In standard quantum mechanics, the Born rule is postulated:

$$P(B_i) = |\psi(B_i)|^2, \tag{6}$$

assigning probabilities to outcomes B_i via the squared wavefunction amplitude [2,16]. In TEQ, this rule is not assumed but derived: probabilities emerge from the entropy-weighted stability of distinguishable paths under the Minimal Principle.

5.1. Path Probabilities from Entropy-Constrained Variation

Lemma 3 (Minimal Principle and Path Probability). *Let* $\Pi(B_i)$ *denote the unnormalized path weight for outcome* B_i :

$$\Pi(B_i) := \left| \int_{\phi \in B_i} \mathcal{D}[\phi] \, e^{\frac{i}{\hbar} S[\phi]} e^{-\beta \tilde{S}_{apparent}[\phi]} \right|^2. \tag{7}$$

Then the normalized probability is:

$$P(B_i) := \frac{\Pi(B_i)}{\sum_i \Pi(B_i)}.$$
 (8)

Entropy weighting reflects the requirement that only entropy-stable paths contribute. Thermodynamically unstable trajectories are filtered out by the Minimal Principle.

5.2. Saddle-Point Expansion and Entropy-Stable Variation

This expansion parallels the saddle-point and Gaussian path integral techniques used in semiclassical quantum mechanics and statistical field theory [17–19].

Theorem 7 (Born Rule from Entropy-Stabilized Paths). *Expanding* $\tilde{S}_{apparent}[\phi]$ *near an entropy-stationary path* ϕ_{st} :

$$\tilde{S}_{apparent}[\phi] = \tilde{S}_{st} + \frac{1}{2} \int dt \, dt' \, \delta\phi(t) \, H(t,t') \, \delta\phi(t') + \mathcal{O}(\delta\phi^3), \tag{9}$$

$$H(t,t') := \frac{\delta^2 \tilde{S}_{apparent}}{\delta \phi(t) \delta \phi(t')} \bigg|_{\phi_{st}}, \tag{10}$$

leads to:

$$\Pi(B_i) \approx e^{-2\beta \tilde{S}_{st}} \left[\det \left(\frac{\beta H}{\pi} \right) \right]^{-1/2} \left(1 + \mathcal{O}(\beta^{-1}) \right). \tag{11}$$

The Hessian H(t,t') encodes local entropy curvature and quantifies distinguishability in path space.

Corollary 6 (Minimal Principle Correction to Born Rule). The effective amplitude becomes:

$$\psi(B_i) := e^{\frac{i}{\hbar}S_{st}}e^{-\beta \tilde{S}_{st}},\tag{12}$$

yielding probability:

$$P(B_i) = \frac{|\psi(B_i)|^2 \cdot (\det H)^{-1/2}}{\sum_i |\psi(B_i)|^2 \cdot (\det H_i)^{-1/2}}.$$
(13)

In the limit of flat entropy curvature:

$$P(B_i) \approx \frac{|\psi(B_i)|^2}{\sum_i |\psi(B_i)|^2},\tag{14}$$

recovering the standard Born rule.

Interpretive Note: The curvature H modulates path amplitude normalization. TEQ predicts observable corrections in regimes where entropy gradients are strong, nonuniform, or non-negligible.

5.3. Entropy Curvature and Logarithmic Expansion

From Eq. (13):

Lemma 4 (Path Probabilities in the Large- β Limit).

$$\ln P(B_i) = -2\beta \tilde{S}_{st} - \frac{1}{2} \ln \det H + \mathcal{O}(\beta^{-1}), \tag{15}$$

$$\tilde{S}_{st} = -\frac{1}{2\beta} \ln P(B_i) - \frac{1}{4\beta} \ln \det H + \mathcal{O}(\beta^{-2}). \tag{16}$$

Probabilities encode not only amplitudes but entropy curvature. This links statistical outcomes to the geometry of distinguishability.

5.4. Born Rule as Entropy-Flat Limit

Theorem 8 (Born Rule from Minimal Principle). *When entropy curvature is flat* ($H \rightarrow const$):

$$P(B_i) \to |\psi(B_i)|^2. \tag{17}$$

More generally:

$$P(B_i) \propto |\psi(B_i)|^2 \cdot (\det H)^{-1/2}.$$
 (18)

Corollary 7 (Thermodynamic Correction Factor). *Probabilities acquire a curvature-sensitive normalization:*

$$P(B_i) = |\psi(B_i)|^2 \cdot Z(B_i)^{-1}, \qquad Z(B_i) = \sqrt{\det(\beta H/\pi)}.$$
 (19)

Paradigm Shift. The Born rule is no longer a postulate. It emerges as the entropy-flat limit of the Minimal Principle. Probabilities reflect structural distinguishability shaped by entropy curvature.

Empirical Implication. The correction factor $Z(B_i)^{-1}$ provides a concrete falsifiability criterion. Controlled deviations from $|\psi(B_i)|^2$ in entropy-curved systems would offer direct evidence for or against TEQ.

- 5.5. Experimental Implications and Regimes of Deviation
- **Entropy-flat regime:** det $H \approx \text{const} \Rightarrow P(B_i) \approx |\psi(B_i)|^2$. Standard quantum behavior holds.
- **Entropy-curved regime:** Variations in *H* introduce measurable corrections, particularly in systems with strong gradients or nonequilibrium dynamics.
- **Testable domains:** High-precision interferometry [20], gravitational decoherence [21], and nonequilibrium quantum thermodynamics [22] offer experimental windows for detecting curvature-induced deviations.

6. Emergence of the Schrödinger Equation via the Minimal Principle

This section derives the Schrödinger equation from the Minimal Principle, without assuming it as a foundational postulate. In TEQ, quantum dynamics emerge from entropy-weighted variation: only those trajectories that remain both phase-coherent and entropy-stable contribute to physical evolution. By analyzing the effective momentum arising from the entropy-weighted action and applying a gradient approximation, we recover the Schrödinger equation as the unique evolution law consistent with entropy-constrained distinguishability. This reframes unitary quantum dynamics as a limiting behavior of entropy-stabilized variational structure.

In conventional quantum theory, the Schrödinger equation

$$i\hbar\frac{\partial\psi}{\partial t} = \hat{H}\psi\tag{20}$$

is introduced axiomatically (see, e.g., [1,23]). In TEQ, it arises from the Minimal Principle: physical trajectories must remain entropy-distinguishable under constrained variation within the entropy geometry defined by Axiom 0. Only entropy-stable, phase-coherent paths satisfy this condition.

6.1. Entropy-Constrained Action and Effective Momentum

We begin with the entropy-weighted action (4):

$$S_{\mathrm{eff}}[\phi] = \int dt (L(\phi,\dot{\phi}) - i\hbar\beta \, g(\phi,\dot{\phi})),$$

where *L* is the classical Lagrangian, *g* encodes apparent entropy flow, and $\beta \in \mathbb{C}$ governs entropic suppression.

Variation of this action yields the modified Euler–Lagrange equation (Theorem 5), extending classical dynamics with an entropic stabilizer term.

Definition 2 (Entropy-Weighted Momentum). *The conjugate momentum becomes:*

$$p_{eff} = \frac{\partial L}{\partial \dot{x}} - i\hbar \beta \frac{\partial g}{\partial \dot{x}},\tag{21}$$

introducing a complex deformation of phase space governed by entropy flow.

Example 1 (Free Particle with Entropy Flow). For $L = \frac{1}{2}m\dot{x}^2$ and $g = \frac{1}{2}\dot{x}^2$:

$$p_{\it eff} = (m - i\hbar eta)\dot{x}, \qquad \dot{x} = rac{p_{\it eff}}{m - i\hbar eta}.$$

This alters trajectory structure and embeds entropic filtering directly into kinematics.

Entropy Gradient Approximation

Lemma 5 (Entropy Gradient Approximation). *Because* $\beta \gg 1$ *in typical physical regimes* (see Appendix C), and assuming $\tilde{S}_{apparent}$ has bounded curvature in \dot{x} , we have

$$\left\langle \frac{\partial \tilde{S}_{apparent}}{\partial \dot{x}} \right\rangle \approx \frac{\partial \tilde{S}_{apparent}}{\partial x}$$
 up to $\mathcal{O}(\beta^{-1/2})$.

This justifies replacing velocity gradients with spatial ones, enabling a configuration-space representation of entropy-weighted dynamics. A full derivation appears in Section H.

Minimal Principle and Schrödinger Dynamics

Theorem 9 (Schrödinger Equation from the Minimal Principle). Given the entropy-weighted momentum

$$p_{eff} = \frac{\partial L}{\partial \dot{x}} - i\hbar\beta \frac{\partial g}{\partial \dot{x}},$$

from Definition 2, and applying the entropy gradient approximation (Lemma 5), we find that in the large- β regime:

$$\left\langle \frac{\partial g}{\partial \dot{x}} \right\rangle \approx \frac{\partial g}{\partial x}.$$

This allows us to express p_{eff} as a differential operator in configuration space. In the entropy-stabilized regime, this operator takes the form:

$$p_{eff}\mapsto -i\hbar\nabla$$
,

reflecting stable phase-resolved entropy flow in configuration space.

Substituting into the effective Hamiltonian

$$H=\frac{p_{eff}^2}{2m},$$

we obtain:

$$H\psi = -\frac{\hbar^2}{2m}\nabla^2\psi,$$

and hence the evolution law

$$i\hbar\frac{\partial\psi}{\partial t} = H\psi. \tag{22}$$

Corollary 8 (Schrödinger Equation as Stability Condition). *The Schrödinger equation arises as the unique configuration-space dynamics compatible with entropy-constrained distinguishability. It reflects the selection of stable, phase-coherent trajectories under the Minimal Principle.*

Paradigm Shift. The Schrödinger equation is not a foundational axiom. It is the dynamical signature of entropy-stabilized, phase-coherent evolution, selected by the Minimal Principle within the entropy geometry defined by Axiom 0.

6.2. From Classical Action to Entropic Coherence

TEQ extends classical extremality by embedding entropy stability into the variational structure. At quantum scales, entropy curvature alters trajectory viability, selecting only phase-coherent, entropy-stable paths. This generalization is summarized in Table 5.

Table 5. Comparison between classical least-action principles and the entropy-weighted formulation of TEQ. The latter incorporates entropy geometry through a complex deformation of the action, leading to quantization and emergent Schrödinger dynamics.

Classical Least Action	Entropy-Weighted Action (TEQ)
Action: $S = \int L(\phi, \dot{\phi}) dt$	Entropy-constrained action: $S_{\text{eff}} = \int [L - i\hbar \beta g] dt$
Variation: $\delta S = 0$	Entropy-constrained variation: $\delta S_{\mathrm{eff}} = 0$ under MP
Euler-Lagrange: $\frac{d}{dt}\frac{\partial L}{\partial \dot{\phi}} - \frac{\partial L}{\partial \phi} = 0$	Entropy-stabilized dynamics: $\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\phi}} - i\hbar \beta \frac{\partial g}{\partial \dot{\phi}} \right) - \left(\frac{\partial L}{\partial \phi} - i\hbar \beta \frac{\partial g}{\partial \phi} \right) = 0$
Momentum: $p = \frac{\partial L}{\partial \bar{x}}$	Entropy-deformed momentum: $p_{\mathrm{eff}} = rac{\partial L}{\partial \dot{x}} - i\hbar eta rac{\partial g}{\partial \dot{x}}$
No quantum structure: Phase space is real-valued	Quantization as entropy coherence: Phase space is complexified via entropy
No evolution law: Hamilton's equations	Emergent Schrödinger dynamics: Schrödinger equation from entropy-stable variation

7. Toward Gravitation from Entropic Geometry

This section develops the emergence of gravity in TEQ as a structural response to entropy geometry. Rather than postulating spacetime curvature, we show that gravitational phenomena arise from entropy gradients that bias which configurations remain distinguishable. Axiom 0 introduces curvature into configuration space via entropy flow, while the Minimal Principle filters for stability. Together, these generate effective geometric structure: energy—momentum flow becomes linked to entropy curvature, and mass emerges as resistance to entropic deformation. Gravitation, in this framework, is not a fundamental interaction but the thermodynamic stabilization of resolvable structure.

See also Jacobson [8], Padmanabhan [9], and Verlinde [10] for related views of gravity as emergent from entropy gradients.

Remark 12 (Conceptual Summary: Gravity from Entropy Structure). In TEQ, gravity is not a fundamental force but a structural response to irreversible entropy flow. Where gradients become non-reversible, curvature arises as resistance to redistributing distinctions—an effect rooted in the entropy-dimensional analysis of Section 2. Spacetime is not a backdrop but an emergent bias: a geometry that favors stable, distinguishable paths. Gravitational phenomena arise when entropy structure becomes rich enough to sustain localized, persistent configurations.

In TEQ, gravitation is not a property of predefined spacetime. It emerges from the interaction of two structural principles. **Axiom 0** defines entropy as a generative constraint on the geometry of possible configurations. It endows configuration space with curvature, resolution limits, and the potential for structure. **The Minimal Principle (MP)** then selects those configurations that remain maximally distinguishable under entropy flow. Together, they imply that classical curvature arises as the entropy-preserving deformation of trajectory space.

7.1. Entropy Dimensionality and Curvature Activation

Entropy redistribution behaves qualitatively differently across regimes of entropy dimensionality:

Definition 3 (Entropy Dimensional Regimes).

1. **Entangled Regime** ($D_S = 0$): Fully nonlocal entropy. No classical support; no spatial geometry.

- 2. Latent Regime ($D_S \in [2,3)$): Stable quasi-classical correlations (e.g., pointer states); approximate geometry.
- 3. **Realized Regime** ($D_S \ge 4$): Entropy gradients become irreversible and geometric. Spacetime structure emerges.

Remark 13 (Conceptual Meaning of Entropy Dimensional Regimes). These dimensional regimes classify how much structure entropy can support. In the entangled regime, distinctions are fully nonlocal—nothing is individually identifiable. In the latent regime, approximate classicality begins to stabilize, allowing emergent structure. Only in the realized regime does entropy flow become irreversible enough to generate robust, geometric features like spacetime and curvature. These transitions mark structural thresholds: from quantum coherence to classical decoherence to gravitational geometry.

Only for $D_S \ge 4$ does entropy curvature take geometric form. Below this threshold, distinguishability remains delocalized or latent.

7.2. Noether Balance and Entropy-Stress

The following result extends Noether's theorem [24] to complex, entropy-weighted actions. Although Noether's original formulation assumed real-valued Lagrangians, the symmetry argument still yields conservation laws—now encoding the joint flow of energy and entropy.

Lemma 6 (Diffeomorphism Invariance under Entropic Constraint). *Let the entropy-weighted effective action be*

$$S_{eff} = S - i\hbar\beta \, \tilde{S}_{apparent}.$$

Under an infinitesimal coordinate shift $x^{\mu} \mapsto x^{\mu} + \delta x^{\mu}$, we obtain:

$$\delta S_{eff} = \int d^4x \, (T^{\mu\nu} - i\hbar\beta \, \Sigma^{\mu\nu}) \nabla_\mu \delta x_
u,$$

where:

- $T^{\mu\nu} := \delta S/\delta g_{\mu\nu}$ is the energy–momentum tensor,
- $\Sigma^{\mu\nu} := \delta \tilde{S}_{apparent} / \delta g_{\mu\nu}$ is the entropy-stress tensor.

Remark. This generalizes the one-dimensional action (4), where entropy flow enters through a scalar functional $g(\phi,\dot{\phi})$. In the covariant setting, entropy geometry gives rise to the tensor $\Sigma^{\mu\nu}$, which structurally biases the dynamics toward distinguishable paths.

Corollary 9 (Entropy-Balanced Continuity). From invariance under the Minimal Principle:

$$\nabla_{\mu}T^{\mu\nu}=0, \qquad \nabla_{\mu}\Sigma^{\mu\nu}=0.$$

These continuity conditions express a simple idea: energy and entropy are not arbitrarily exchanged—they must flow in ways consistent with the underlying structure. Rather than being imposed, this balance follows naturally from the entropy-weighted geometry and the variational principle.

7.3. Entropy Curvature as Geometric Source

Definition 4 (Entropy Curvature Tensor). *Define:*

$$\kappa^{\mu\nu} := \nabla^{\mu}\nabla^{\nu}\tilde{S}_{apparent},$$

as the second-order entropy curvature. This tensor captures how entropy flow deforms the surrounding structure—it measures how curved the entropy landscape is at a given point.

Relation to Local Curvature: In the one-dimensional or trajectory-based formulation, entropy curvature appears as

 $\kappa := \frac{\partial^2 g}{\partial \dot{\phi}^2},$

which quantifies local constraints on distinguishability in velocity space. The tensor $\kappa^{\mu\nu}$ generalizes this to spacetime, encoding how distinguishability constraints vary in all directions and contribute to the emergent geometry.

Theorem 10 (Emergent Geometry from Entropic Equilibrium). *The Minimal Principle requires a local match between energy flow and entropy gradient. In simplified terms:*

$$T^{\mu\nu}\xi_{\nu}=T\nabla^{\mu}\tilde{S}_{apparent}$$
,

where ξ^{μ} represents a small shift in the local frame—a kind of "preferred direction" used to compare changes. From this balance it follows that:

$$\kappa^{\mu\nu} \propto T^{\mu\nu}$$
.

In other words, the curvature of the entropy structure acts as the source of geometry—replacing the role played by the Einstein tensor in general relativity. Gravity, on this view, is not a background condition but a thermodynamic response to structured entropy flow.

Structural Insight. In TEQ, spacetime is not presupposed. It emerges from the structure defined by Axiom 0 and the constraint imposed by the Minimal Principle. Gravity arises as the thermodynamic geometry of resolvable distinctions—curvature is not a backdrop, but the outcome of constrained entropy flow.

Theorem 11 (Mass as Entropy-Curvature Resistance). *To preserve distinguishability under entropy curvature, a system must remain stable against entropic deformation. This sets a structural constraint:*

$$\frac{\beta}{m}\kappa\ll 1$$
,

where:

- κ denotes the entropy curvature—i.e., the second derivative of apparent entropy,
- β is the entropy-sensitivity parameter,
- and m represents the system's effective mass.

This expresses the requirement that mass must be large enough to suppress destabilizing entropy gradients. To relate this to spacetime structure, consider the entropy-weighted action's invariance under infinitesimal coordinate transformations. Applying the principle of stationary action (as in Noether's theorem) leads to a generalized balance condition between entropy-induced stress and entropy curvature:

$$\delta S_{\it eff} = \int d^4x \, (T^{\mu
u} - i\hbar eta \, \Sigma^{\mu
u})
abla_\mu \delta x_
u.$$

If we assume the stress tensors are approximately aligned with the entropy curvature in the high- β regime, then structurally:

$$\Sigma^{\mu\nu} \propto \frac{m}{\beta} \nabla^{\mu} \nabla^{\nu} \tilde{S}_{apparent}.$$

Solving for mass gives:

$$m \sim eta \cdot \left(rac{\Sigma^{\mu
u}}{
abla^{\mu}
abla^{
u} ilde{S}_{apparent}}
ight).$$

Interpretation: Mass arises not as a fundamental quantity but as a measure of a system's resistance to deformation by entropy gradients. It quantifies how much entropy-stress is needed to sustain a given curvature in the entropy landscape. In this view, inertial mass is a geometrically emergent property linked to entropic stability.

Remark 14 (Mass as Curvature Buffer). *In TEQ, mass quantifies resistance to entropy curvature. Like inertia in GR, it reflects how a system buffers structural deformation—but here it arises from entropy geometry, not spacetime metrics.*

Outlook: Toward a Field-Theoretic Formulation

While the present manuscript focuses on semiclassical and particle-based configurations, the TEQ framework extends naturally to field-theoretic domains. In this generalization, entropy is no longer a functional of trajectory variables alone, but becomes a functional over field configurations: $\tilde{S}[\phi(x)]$, with ϕ representing matter or gauge fields over spacetime. Entropy curvature then defines a local geometric structure over field space, suggesting that the TEQ variational principle can be formulated as an extremization over sections of fiber bundles equipped with an entropy metric.

This opens a path to incorporating gauge fields, fermions, and local symmetries into TEQ, potentially aligning with existing entropy-gradient formalisms in gravity and quantum information [8, 9,25,26]. The entropy-stress tensor $\Sigma^{\mu\nu}$, introduced here in the gravitational context, may generalize to an entropy current $\Sigma^{\mu}[\phi(x)]$, whose divergence governs the emergence of effective spacetime structure and renormalization behavior in field theories. Such developments are reserved for future work, but they indicate the broader scope of the TEQ framework beyond its point-particle foundations.

This completes the structural unification. Spacetime, curvature, and inertia are not independent elements, but emergent consequences of entropy geometry. Axiom 0 provides the generative field; the Minimal Principle selects the stable distinctions within it.

8. Core Principles from the Minimal Principle (MP)

This section articulates the Minimal Principle (MP) as the sole generative condition from which all physical structure in TEQ emerges. Rather than positing separate principles for quantization, dynamics, or measurement, TEQ derives them as consequences of a single requirement: stability of distinguishable structure under entropy flow. The MP replaces traditional axioms with a geometric criterion of resolvability. From this, the core architecture of physics—dynamics, probability, quantization, and curvature—unfolds as structurally necessary. The result is a radically minimal foundation, in which the diversity of physical phenomena reflects variations in entropy geometry, not multiplicity of laws.

TEQ does not begin with quantum postulates. It derives physical structure from a single generative constraint:

Minimal Principle (MP):

Physically realizable trajectories are those that maximize entropy distinguishability under structural constraints.

From this, all features of TEQ follow. Quantization, decoherence, probabilistic measurement, and curvature emerge as structural consequences of entropy-constrained variation.

MP1. Entropy-Action Coupling from Variational Structure

Applying MP to a constrained ensemble of paths yields amplitudes:

$$\mathcal{A}[\phi] = \exp\left(\frac{i}{\hbar}S[\phi] - \beta \tilde{S}_{\mathrm{apparent}}[\phi]\right),$$

where $S[\phi]$ is the classical action, $\tilde{S}_{apparent}$ is observer-resolvable entropy, and \hbar^{-1} , β arise as Lagrange multipliers.

MP2. Entropy-Weighted Path Selection

The effective amplitude becomes:

$$\mathcal{A}_{ ext{eff}} = \int \mathcal{D}[\phi] \, \mathcal{A}[\phi],$$

favoring entropy-stationary trajectories. Destructive interference suppresses unstable paths; coherence emerges from thermodynamic filtering (see Appendix G for related dynamics in entropy-gradient systems).

MP3. Quantization from Entropy Geometry

Canonical commutation relations are deformed by entropy curvature:

$$[\hat{\phi}, \hat{\Pi}_{\text{eff}}] = i\hbar \left(1 - \frac{\beta}{m}\kappa\right),$$

with κ the local entropy curvature. Quantization is thus a geometric stability condition—not an imposed algebra.

MP4. Entropy Resolution as Structural Gauge

The parameter $\alpha = \beta \hbar$ defines observer resolution. Shifts in α interpolate between coherent and dissipative regimes, acting as a gauge on entropy distinguishability.

MP5. Probability as Entropic Flatness

In the large- β limit, path probabilities approach:

$$P(B_i) = |\psi(B_i)|^2 + \mathcal{O}(\beta^{-1}),$$

with corrections from entropy curvature. Probability reflects geometric distinguishability—not intrinsic randomness.

Conclusion:

All structure in TEQ—quantization, measurement, decoherence, gravity—emerges from a single structural condition: the Minimal Principle. This unifies geometry, thermodynamics, and quantum theory within a coherent variational framework.

Postlude: Entropy as a Structural First Principle

With the entropy-geometry framework now assembled, we can step back to assess its structural scope and implications.

Scope and Limits. While this manuscript explicitly rederives key structures of quantum theory, thermodynamics, and elements of gravitational structure, it does not exhaust the full implications of TEQ. Several domains—including quantum field theory, holography, quantum information, and early-universe cosmology—are structurally implicated by the entropy geometry and the Minimal Principle but are reserved for future work. To avoid speculative overreach, this manuscript halts explicitly at the first closure of the entropy-action-gravity arc. Further developments may proceed modularly from this established foundation

The Total Entropic Quantity (TEQ) framework repositions entropy not as a thermodynamic byproduct, but as the structural foundation of physical law. At its core lie two generative axioms. **Axiom 0** posits entropy as a prior constraint: a curvature-bearing structure over configuration space

that defines which distinctions can, in principle, exist. **Axiom 1**, the Minimal Principle (MP), then selects those configurations that remain maximally distinguishable under finite entropy resolution.

This shift is both physical and philosophical. It reframes quantization, measurement, and spacetime not as postulates, but as emergent consequences of a more primitive condition: resolvability under entropy geometry. The constants \hbar , β , and k_B are no longer fundamental givens, but structural responses to this underlying constraint geometry.

From this perspective, the entropy-weighted path integral is not merely a computational tool. It defines a structural interface between ontology and epistemology: between what exists and what can be resolved. It encodes which distinctions are physically meaningful under constraints of entropy flow, resolution, and coherence.

This structural polarity—between emergence and collapse—is summarized in Table 6, contrasting the forward and reverse flow of entropy in TEQ, from resolved structure to undifferentiated entanglement.

Table 6. Structural contrast in TEQ between the forward (emergent) and reverse (collapse) flow of entropy. Forward flow yields quantum and classical structure; reverse flow leads to global entanglement and dissolution of spacetime.

Quantity	Forward Flow (Emergence)	Reverse Flow (Collapse)	
Entropy dimension D_S	Increases toward resolvable structure	Tends to zero; structureless entanglement	
Distinguishability	Increases under entropy resolution	Vanishes; configurations merge	
Observer resolution α	Finite resolution selects stable paths	Tends to zero; no discernible paths	
Quantization	Emerges from entropy-stabilized coherence	Dissolves as entropy gradients flatten	
Geometry	Emerges from entropy curvature	Collapses into nonlocal structure	
Time	Becomes ordered and resolvable	Undefined; no temporal distinctions	
Space	Structured via distinguishable records	Nonlocal; spatial relations collapse	

In this light, TEQ belongs to a broader movement toward information-based formulations of physics, but diverges by grounding information not in observers, bits, or priors, but in the geometric structure of entropy itself. The foundational question is not *what evolves*, but *what distinctions persist* within the generative limits set by entropy curvature.

Further extensions of this framework may address the emergence of time, the arrow of causality, and the role of observers. But the structural stance is clear: entropy is not a result of dynamics—it is the precondition for their emergence. Axiom 0 creates the space of possible structure; Axiom 1 selects its realized form.

Concluding Perspective: Entropy as Foundation

The Total Entropic Quantity (TEQ) framework proposes a fundamental shift in how physical structure is understood. Rather than treating entropy as a byproduct of known dynamics, TEQ reverses the logic: structure, dynamics, and quantization *emerge* from entropy. At its core are two principles: a geometric field of entropy that defines which distinctions can be resolved (Axiom 0), and a minimal principle that selects the most stable among them (Axiom 1). From this, the familiar landscape of

quantum mechanics—amplitudes, commutators, and unitary evolution—arises as a special case of entropy geometry.

This perspective reframes core questions in physics. Quantization is no longer a postulate, but a consequence of structural stability. The constants \hbar , β , and k_B are not inputs, but projections of coherence and resolution within an entropy-defined space. Decoherence, measurement, and even gravitation are reinterpreted as outcomes of entropy flow and curvature.

Beyond physics, this framework opens new connections to information theory, complexity, and the limits of distinguishability. It invites rethinking not only what physical systems do, but what it *means* for something to exist as a stable, resolvable structure.

Open Directions. This manuscript halts at the structural core. Many consequences of TEQ remain to be developed:

- Entropic reformulations of quantum field theory and statistical mechanics;
- Generalizations of entropy curvature in high-dimensional and strongly non-equilibrium regimes;
- Connections to information-theoretic bounds and complexity constraints;
- Further exploration of gravity as entropy-induced deformation, including black hole structure and cosmological evolution;
- Operational formulations of observer resolution and entropy dimension transitions.

These directions are not peripheral extensions but follow naturally from the foundational principle: what is resolvable under entropy, becomes real. The TEQ framework provides a general and conceptually unified structure for exploring this principle across the full spectrum of physics and beyond.

Remark 15 (On Axioms and the Nature of Truth). Even if Axiom 0 and Axiom 1 do not name the ultimate source of reality—even if they are not "true" in an ontological sense—their power to generate quantum structure, gravitational curvature, and classical stability suggests something deeper. They function not as declarations of what is, but as constraints on what can coherently be resolved. In this role, they may be less foundations than fixed points in a shifting sea of structure.

Philosophically, we may never know what is ultimately "true." Ontology eludes us. But epistemology offers a different measure: truthiness. A structural principle that explains much, connects widely, and resists contradiction earns a high degree of epistemic plausibility. TEQ does not claim metaphysical certainty; it claims that from two simple axioms, an entire scaffold of physics falls into place—coherently, compactly, and without ad hoc assumptions.

In that light, even if the axioms one day yield to more refined insights, their truthiness remains. They may not be the last word, but they frame the question with uncommon clarity.

9. Conclusions and Outlook

This manuscript has introduced the Total Entropic Quantity (TEQ) framework, grounded in two structural axioms. **Axiom 0** posits entropy as a generative principle—a geometric constraint defining which configurations can stably distinguish themselves. In TEQ, entropy refers to a curvature-functional over distinguishability configurations, governing which structures persist under resolution. **Axiom 1**, the Minimal Principle (MP), selects among these those that remain maximally distinguishable under finite entropy resolution. Together, these axioms define a geometry of resolvability that replaces conventional postulates with structural constraints.

From this foundation, canonical features of quantum theory—including the Born rule, Schrödinger dynamics, quantization, and elements of gravitational structure—emerge as consequences of entropy-weighted variation. The result is a unified framework in which quantum coherence, classical emergence, and spacetime curvature arise from the same entropic structure.

Though this work focuses on TEQ in semiclassical regimes, several natural extensions remain open. In quantum field theory, entropy gradients may generalize to field configurations via entropy currents on fiber bundles. In quantum information, entropy-tensor flows may offer geometric analogues

to entanglement, particularly in decohering systems. The role of entropy dimensionality D_S in governing causal structure—and potential connections to holographic or thermodynamic gravity models—warrants further exploration.

These directions are not proposed as a personal research program, but as natural extrapolations of the structural logic presented here. This manuscript is offered as one formulation of a deeper principle, to be evaluated, refined, or reinterpreted by others.

Acknowledgments: This research was undertaken informally and independently during an ongoing period of cognitive and physical rehabilitation following a brain hemorrhage. It should be understood as part of a personal recovery process, not a professional research output. In that context, ChatGPT was used for grammar refinement, structural clarity, and conceptual dialogue. All theoretical developments, derivations, and conclusions are solely the author's. This work is offered in the hope that, whatever its origin, the structural clarity it seeks may be of value. Any credit belongs not to the author, but to the ideas themselves, to those able to advance them, and to the long tradition of thinkers—male and female—whose work made this one possible.

Appendix A. Entropy-Weighted Path Integral Derivation

This appendix derives the entropy-weighted path integral as a variational solution, showing that the standard Feynman path integral emerges as a special case. Rather than postulating the exponential weighting of paths by classical action, we obtain this structure by maximizing path entropy under a constraint on average action. This approach extends Jaynes' MaxEnt formalism [7,27] to the space of trajectories, and connects to earlier work exploring the thermodynamic and information-theoretic interpretation of path integrals [28,29]. In this view, the path integral reflects an entropy-maximizing inference over distinguishable trajectories, weighted by both dynamical and entropic constraints.

Appendix A.1. Path Distribution and Entropy Functional

Let q(t) be a configuration path and $\mathcal{P}[q(t)]$ a probability distribution over such paths. Define the entropy functional:

$$S[P] := -\int P[q(t)] \log P[q(t)] \mathcal{D}q. \tag{A1}$$

We seek the distribution \mathcal{P} that maximizes this entropy, subject to:

- Normalization: $\int \mathcal{P}[q(t)] \mathcal{D}q = 1$,
- Average Action: $\int \mathcal{P}[q(t)]S[q(t)] \mathcal{D}q = \bar{S}$,

where S[q(t)] is the classical action functional associated with each path.

Appendix A.2. Variational Derivation

We introduce Lagrange multipliers $\lambda \in \mathbb{R}$ and $\beta \in \mathbb{C}$, and define the constrained entropy functional:

$$\Phi[\mathcal{P}] = \mathcal{S}[\mathcal{P}] - \beta \int \mathcal{P}[q(t)] \mathcal{S}[q(t)] \mathcal{D}q$$

$$-\lambda \left(\int \mathcal{P}[q(t)] \mathcal{D}q - 1 \right). \tag{A2}$$

Taking the functional derivative and setting $\delta \Phi = 0$, we obtain the stationary condition:

$$\log \mathcal{P}[q(t)] + 1 + \beta S[q(t)] + \lambda = 0. \tag{A3}$$

Solving for $\mathcal{P}[q(t)]$, we find the Gibbs-like distribution:

$$\mathcal{P}[q(t)] = \frac{1}{Z} \exp(-\beta S[q(t)]), \quad Z = \int \exp(-\beta S[q(t)]) \mathcal{D}q$$
(A4)

Remark A1 (Beyond Jaynesian Inference). While the form of the distribution resembles Jaynes' MaxEnt derivation [7], in TEQ the entropy functional is not epistemic or informational in origin. Instead, it reflects a

geometric constraint on resolvability itself, derived from the underlying entropy curvature. Thus, the exponential form arises not from inference under uncertainty, but from structural stability under entropy flow.

Appendix A.3. Path Integral Formulation

Given the distribution $\mathcal{P}[q(t)]$, the expectation value of an observable $\mathcal{O}[q(t)]$ is:

$$\langle \mathcal{O} \rangle = \int \mathcal{O}[q(t)] \, \mathcal{P}[q(t)] \, \mathcal{D}q.$$
 (A5)

This defines the entropy-weighted path integral, where β regulates the contribution of high-action (low-probability) paths.

Lemma A1 (Entropy-Weighted Path Distribution). Let S[q(t)] be the classical action functional. The distribution $\mathcal{P}[q(t)]$ that maximizes path entropy subject to normalization and average action constraints is:

$$\mathcal{P}[q(t)] = \frac{1}{Z} \exp(-\beta S[q(t)]), \qquad Z = \int \exp(-\beta S[q(t)]) \,\mathcal{D}q.$$

Corollary A1 (Recovery of the Feynman Path Integral). *Setting* $\beta = \frac{i}{\hbar}$ *yields:*

$$\langle \mathcal{O} \rangle = \frac{1}{Z} \int \mathcal{O}[q(t)] \, e^{iS[q(t)]/\hbar} \, \mathcal{D}q,$$

which recovers the Feynman path integral [17–19,30].

Appendix A.4. Entropy-Action Correspondence in TEQ

In the TEQ framework, the parameter β is not fixed a priori. Rather:

- $\beta = \frac{1}{\hbar}$: yields standard unitary quantum mechanics.
- $\beta \in \mathbb{R}^+$: encodes dissipative entropy suppression, relevant in decoherence and thermodynamic limits [4,5,12].
- $\beta \in \mathbb{C}$: allows interpolations between unitary and non-unitary regimes, depending on the entropy balance.

TEQ generalizes the Feynman path integral by embedding it in a broader entropy-weighted variational structure. This connects coherent quantum dynamics to entropy-driven path selection, and reveals \hbar as the scale at which action and entropy intersect. The influence functional formalism of Feynman and Vernon [12] plays a key conceptual role here. It shows how tracing out environmental degrees of freedom induces effective damping of interference between alternative paths. In TEQ, this suppression is generalized: entropy curvature plays the structural role of biasing path weights, with decoherence arising as a special case of entropy-driven distinguishability loss.

Appendix A.5. Derivation of β as a Lagrange Multiplier from Entropy-Constrained Path Selection

In the TEQ framework, the parameter β emerges naturally as a Lagrange multiplier enforcing entropy constraints in the path selection process. This derivation shows how β arises from maximizing path entropy subject to constraints on both action and apparent entropy.

Entropy-Constrained Path Variational Principle

Let $\rho[\phi]$ be the path probability density functional over histories $\phi(t)$. We impose the following constraints:

$$\int \mathcal{D}[\phi] \, \rho[\phi] = 1,\tag{A6}$$

$$\int \mathcal{D}[\phi] \, \rho[\phi] \, S[\phi] = \bar{A},\tag{A7}$$

$$\int \mathcal{D}[\phi] \, \rho[\phi] \, \tilde{S}_{\text{apparent}}[\phi] = \bar{S}, \tag{A8}$$

where $S[\phi]$ is the classical action and $\tilde{S}_{apparent}[\phi]$ is the entropy functional associated with each path. We define the entropy of the path distribution as:

$$S[\rho] := -\int \mathcal{D}[\phi] \,\rho[\phi] \ln \rho[\phi], \tag{A9}$$

and extremize it with Lagrange multipliers β and λ :

$$\delta \left\{ S[\rho] + \beta \left(\bar{S} - \int \rho[\phi] \tilde{S}_{\text{apparent}}[\phi] \right) + i\lambda \left(\bar{A} - \int \rho[\phi] S[\phi] \right) \right\} = 0. \tag{A10}$$

Taking the functional variation yields:

$$\ln \rho[\phi] + 1 + \beta \tilde{S}_{\text{apparent}}[\phi] + i\lambda S[\phi] = 0, \tag{A11}$$

so that:

$$\rho[\phi] = \frac{1}{Z} \exp(-\beta \tilde{S}_{\text{apparent}}[\phi] - i\lambda S[\phi]), \tag{A12}$$

with normalization factor:

$$Z = \int \mathcal{D}[\phi] \exp(-\beta \tilde{S}_{\text{apparent}}[\phi] - i\lambda S[\phi]). \tag{A13}$$

Recovery of the TEQ Amplitude and Born Rule

Identifying $\lambda = 1/\hbar$, we obtain:

$$\rho[\phi] = \frac{1}{Z} \exp\left(\frac{i}{\hbar} S[\phi] - \beta \tilde{S}_{\text{apparent}}[\phi]\right). \tag{A14}$$

Thus, the TEQ path amplitude

$$\mathcal{A}[\phi] = \exp\left(\frac{i}{\hbar}S[\phi] - \beta\tilde{S}_{\text{apparent}}[\phi]\right) \tag{A15}$$

is the exponential of the Lagrangian dual function. The modulus squared of this amplitude,

$$|\mathcal{A}[\phi]|^2 = e^{-2\beta \tilde{S}_{\text{apparent}}[\phi]},\tag{A16}$$

recovers the path probability density. This confirms that *the Born rule arises naturally* from the entropy-constrained variational principle, with β enforcing the entropy constraint and \hbar setting the scale of phase sensitivity.

Appendix B. Appendix: Deriving the Entropy Metric $g(\phi,\dot{\phi})$ from Entropy Geometry

The entropy-weighted action in TEQ introduces a deformation term:

$$S_{\text{eff}}[\phi] = \int dt (L(\phi, \dot{\phi}) - i\hbar\beta \cdot g(\phi, \dot{\phi})), \tag{A17}$$

where $g(\phi, \dot{\phi})$ quantifies entropy flux accessible to a finite-resolution observer along the trajectory $\phi(t)$. To derive a general, assumption-minimizing form for g, we impose the following structural constraints:

- **(G1) Locality:** *g* depends only on the instantaneous state $(\phi, \dot{\phi})$.
- **(G2) Positivity:** $g \ge 0$, encoding directional entropy production or suppression.
- **(G3) Covariance:** *g* transforms as a scalar under coordinate reparametrizations of configuration space.
- **(G4) Distinguishability Geometry:** The entropy curvature defines a local metric structure over the tangent bundle.

Appendix B.1. Geometric Form from Entropy Curvature

Assume that entropy flow defines a Riemannian structure on configuration space \mathcal{M} , captured by a positive-semidefinite tensor field $G_{ij}(\phi)$. This defines a quadratic form on the velocity space:

$$g(\phi, \dot{\phi}) := \frac{1}{2} G_{ij}(\phi) \dot{\phi}^i \dot{\phi}^j. \tag{A18}$$

This expression is:

- Minimal: Involves no higher-order or nonlocal assumptions;
- Coordinate-invariant: A scalar under general reparametrizations;
- Structurally familiar: Analogous to kinetic terms in classical mechanics, but with the metric now encoding entropy curvature.

Appendix B.2. Interpretation as an Entropic Fisher Metric

This construction connects to information geometry, where the Fisher information metric quantifies statistical distinguishability between infinitesimally nearby distributions:

$$G_{ij}(\phi) = \mathbb{E}\left[\partial_i \log p(x;\phi)\partial_i \log p(x;\phi)\right],\tag{A19}$$

for a family of distributions $p(x;\phi)$ on observable configurations [28,31,32]. In this analogy, G_{ij} captures how entropy curvature governs resolvability limits in velocity space. This perspective echoes ideas in thermodynamic geometry [33,34] and recent reconstructions of quantum theory from information-geometric foundations [29].

Appendix B.3. Curvature and Entropic Stability

The second variation of *g* defines the entropy curvature:

$$\kappa := \frac{\partial^2 g}{\partial \dot{\phi}^2} = G_{ij}(\phi),\tag{A20}$$

which appears directly in the entropy-deformed Poisson bracket and generalized quantization conditions (see Section 4). Thus, G_{ij} functions as an entropic analogue of an inertial tensor: it biases trajectory weights according to local geometric stability.

Appendix B.4. Summary and Outlook

We conclude that the entropy deformation term $g(\phi, \dot{\phi})$ should, under general structural and geometric constraints, take the form:

$$g(\phi, \dot{\phi}) = \frac{1}{2} G_{ij}(\phi) \dot{\phi}^i \dot{\phi}^j, \tag{A21}$$

with $G_{ij}(\phi)$ an emergent entropy-derived metric tensor encoding local distinguishability. This form supports rigorous derivations of entropy-weighted dynamics, deformation of canonical structures, and quantization from entropy geometry.

Appendix C. Order-of-Magnitude Estimate for β in TEQ

We estimate the physical magnitude of the entropy–action coupling parameter β , assuming entropy is measured in units of the Boltzmann constant k_B . The parameter β plays a central role in the TEQ framework as a Lagrange multiplier that governs the weighting of paths by entropy relative to action (see Appendix A).

Lemma A2 (Canonical Estimates of β). Let entropy be expressed in units of k_B . Then in three key physical regimes, β takes the following characteristic values:

1. Thermal Regime (Statistical Mechanics):

$$\beta = \frac{1}{k_B T}$$
, where T is temperature.

For $T \approx 300$ *K, this yields:*

$$\beta \approx 2.4 \times 10^{20} \, J^{-1}$$
.

2. Quantum Regime (Unitary Limit):

$$\beta = \frac{i}{\hbar} \approx i \times 9.5 \times 10^{33} J^{-1},$$

where $\hbar \approx 1.05 \times 10^{-34}$ Js. This corresponds to fully coherent quantum evolution.

3. **Entropy–Action Balance:** The dimensionless ratio $\alpha = \beta \hbar = \frac{\hbar}{k_B T}$ quantifies the relative influence of entropy and action. At room temperature:

$$\alpha \approx 2.5 \times 10^{-14} \ll 1$$
.

indicating that entropy strongly suppresses quantum interference at macroscopic scales [5].

Corollary A2 (Thermodynamic Dominance in Classical Regimes). *In the limit* $\alpha \ll 1$, *TEQ reduces to classical deterministic behavior. The smallness of* α *explains the empirical absence of macroscopic superpositions and the stability of classical trajectories.*

These estimates align with canonical results from statistical mechanics [35], thermodynamic inference [7], and quantum theory [23], and provide the empirical foundation for interpreting TEQ's scale-dependent behavior.

Gravitational and Cosmological Limits of β

In the TEQ framework, the Lagrange multiplier β encodes the relative weight of entropy versus action in selecting physical trajectories. Extremal values of β correspond to regimes where entropy geometry dominates—such as gravitational singularities, black hole horizons, and the early universe—where standard thermodynamic and quantum approximations may break down.

Theorem A1 (Gravitational Limit of Entropy Weighting). *In the high-temperature limit,* $\beta \to 0$, *entropy weighting becomes negligible and classical dynamics dominate. As* $T \to T_P$ (*Planck temperature*), *entropy curvature becomes dominant, signaling the breakdown of standard path integral approximations. A unified entropy-weighted geometry is required to describe such regimes* [36].

Corollary A3 (Cosmological and Black Hole Regimes). *In black hole thermodynamics* [37,38], *gravitational decoherence* [21,39], *and early-universe cosmology* [8,9], *the entropy flow exhibits extreme curvature. In these limits, TEQ predicts observable corrections to the Born rule and commutation structure.*

The Planck temperature $T_P \sim 1.42 \times 10^{32}$ K yields:

$$\beta_P = \frac{1}{k_B T_P} \sim 7.0 \times 10^{-10} \, \mathrm{J}^{-1},$$

defining the lower bound of entropy sensitivity. In contrast, cosmological cooling or ultra-isolated systems yield large β , favoring entropy-stable and classically emergent dynamics.

Remark A2. TEQ interpolates between coherent quantum mechanics ($\beta = \frac{i}{\hbar}$) and gravitational thermodynamics ($\beta \to 0$). Entropy curvature serves as the geometric link, supporting a unified variational structure across quantum, thermodynamic, and gravitational domains [10].

Appendix D. Derivation of Entropy-Deformed Symplectic Structure

This appendix derives the entropy-induced deformation of symplectic structure and its quantum counterpart. Starting from the entropy-weighted action, we show how both the Poisson bracket and commutator acquire entropy-curvature corrections. These results support the main discussion in Section 4.

Appendix D.1. Poisson Bracket from Entropy-Weighted Momentum

We begin with the entropy-weighted action functional:

$$S_{\text{eff}}[\phi] = \int dt (L(\phi, \dot{\phi}) - i\hbar\beta \, g(\phi, \dot{\phi})), \tag{A22}$$

where $g(\phi, \dot{\phi})$ encodes entropy flux along the path (see Appendix B).

The corresponding effective momentum is:

$$\Pi_{\text{eff}} := \frac{\partial L}{\partial \dot{\phi}} - i\hbar \beta \, \frac{\partial g}{\partial \dot{\phi}}.\tag{A23}$$

To assess deformation of the symplectic structure, we compute:

$$\{\phi, \Pi_{\rm eff}\}_{\rm TEQ} = \frac{\partial \Pi_{\rm eff}}{\partial \dot{\phi}} = \frac{\partial^2 L}{\partial \dot{\phi}^2} - i\hbar\beta \frac{\partial^2 g}{\partial \dot{\phi}^2}. \tag{A24}$$

Assuming a standard quadratic kinetic term $L = \frac{1}{2}m\dot{\phi}^2 - V(\phi)$, and $g = \frac{1}{2}\dot{\phi}^2$, we find:

$$\{\phi, \Pi_{\text{eff}}\}_{\text{TEQ}} = m - i\hbar\beta \kappa, \quad \text{with } \kappa := \frac{\partial^2 g}{\partial \dot{\phi}^2} = 1.$$
 (A25)

Here, κ characterizes local entropy curvature in velocity space, i.e., how distinguishability varies with infinitesimal changes in velocity.

Normalizing by mass and taking the real part:

$$\{\phi, \Pi_{\text{eff}}\}_{\text{TEQ}} = 1 - \frac{\beta}{m}\kappa.$$
 (A26)

This deformation recovers the canonical bracket in the limit $\kappa \to 0$ or $\beta \to 0$, and encodes the suppression of unstable paths under entropy-weighted dynamics.

Appendix D.2. Effective Commutator via Path Variation

To derive the entropy-corrected commutator without assuming canonical quantization, consider the entropy-weighted amplitude:

$$\mathcal{A}[\phi] = \exp\left(\frac{i}{\hbar}S[\phi] - \beta\tilde{S}_{\text{apparent}}[\phi]\right),\tag{A27}$$

and expand the effective action to second order near a stable path:

$$\delta^2 S_{\text{eff}} = \int dt \left(\delta \phi \, \frac{\partial^2 L}{\partial \phi^2} \, \delta \phi + \delta \dot{\phi} \, \frac{\partial^2 L}{\partial \dot{\phi}^2} \, \delta \dot{\phi} - i \hbar \beta \, \delta \dot{\phi} \, \frac{\partial^2 g}{\partial \dot{\phi}^2} \, \delta \dot{\phi} \right). \tag{A28}$$

This modifies the curvature of path fluctuations in momentum space, inducing an effective noncommutativity of the form:

$$[\hat{\phi}, \hat{\Pi}_{\text{eff}}] \sim i\hbar \left(1 - \frac{\beta}{m}\kappa\right),$$
 (A29)

where the coefficient reflects reduced distinguishability between nearby paths under entropy-weighted evolution. This scaling arises from stability analysis of path fluctuations, analogous to the role of fluctuation-action curvature in effective action formalisms [40–43].

Thus, both the classical bracket and its quantum deformation emerge from entropy geometry rather than canonical assumptions. TEQ thereby unifies dynamical and statistical constraints in a variationally coherent framework, extending quantization to entropy-curved configuration spaces.

Appendix E. Evaluation of the Entropy-Weighted Gaussian Path Integral

This appendix derives the leading-order approximation to the entropy-weighted path integral via a Gaussian expansion around the entropy-stationary path ϕ_{st} , paralleling saddle-point methods in semiclassical quantum mechanics [17,18]. Similar Gaussian expansions have long played a role in semiclassical methods [44,45], while here they are adapted to entropy-weighted variational structure. This derivation supports Lemma 5, used in the Schrödinger derivation to justify replacing entropy gradients in velocity space with configuration-space gradients.

Appendix E.1. Quadratic Expansion Around Entropy-Stable Trajectory

Let the path be expanded as $\phi(t) = \phi_{st}(t) + \delta\phi(t)$, where ϕ_{st} minimizes the entropy functional. A second-order expansion yields:

$$\tilde{S}_{\text{apparent}}[\phi] = \tilde{S}_{\text{apparent}}[\phi_{\text{st}}] + \frac{1}{2} \int dt \, dt' \, \delta\phi(t) \, H(t, t') \, \delta\phi(t') + \mathcal{O}(\delta\phi^3), \tag{A30}$$

where the kernel H(t, t') is the functional Hessian:

$$H(t,t') := \frac{\delta^2 \tilde{S}_{\text{apparent}}}{\delta \phi(t) \, \delta \phi(t')} \bigg|_{\phi = \phi_{\text{st}}}.$$
(A31)

Lemma A3 (Leading-Order Approximation of the Entropy-Weighted Path Integral). *To leading order, the entropy-weighted path integral becomes:*

$$\mathcal{Z} pprox e^{-2eta ilde{S}_{apparent}[\phi_{
m st}]} \cdot \int \mathcal{D}[\delta\phi] \, e^{-eta \int dt \, dt' \, \delta\phi(t) H(t,t') \delta\phi(t')}.$$

Appendix E.2. Reduction via Discretization

Discretizing time into N intervals, the path integral reduces to a Gaussian over \mathbb{R}^N :

$$\mathcal{Z} \approx e^{-2\beta \tilde{S}_{\text{apparent}}[\phi_{\text{st}}]} \cdot \int d^N \vec{\delta \phi} \, \exp\left(-\beta \vec{\delta \phi}^\top H \vec{\delta \phi}\right),$$
 (A32)

where $H \in \mathbb{R}^{N \times N}$ is the discretized Hessian matrix, with entries

$$H_{ij} := \left. rac{\partial^2 ilde{S}_{ ext{apparent}}}{\partial \phi_i \partial \phi_j}
ight|_{\phi = \phi_{ ext{st}}}.$$

Theorem A2 (Gaussian Evaluation of Entropy-Weighted Integral). Let $H \succ 0$ be a positive-definite entropy curvature matrix. Then:

$$\mathcal{Z} \approx e^{-2\beta \tilde{S}_{apparent}[\phi_{\rm st}]} \cdot (\det H)^{-1/2}$$

up to a normalization factor absorbed during probability normalization [45,46].

Corollary A4 (Entropy-Curvature Dominance in Path Probability). *The dominant contribution to path probability scales as:*

$$P(B_i) \propto e^{-2\beta \tilde{S}_{apparent}[\phi_{st}]} \cdot (\det H)^{-1/2},$$

where $\tilde{S}_{apparent}$ is minimized and H quantifies local curvature in entropy geometry.

Appendix E.3. Interpretation and Structural Significance

This result is structurally analogous to the semiclassical stationary phase approximation in conventional path integrals, but here weighted by entropy geometry rather than oscillatory phase. It highlights two factors:

- Dominant Suppression: The exponential term reflects entropy minimization across histories.
- Fluctuation Curvature: The determinant encodes the local "stiffness" or curvature of entropy geometry around the dominant path.

Remark A3. The curvature correction modifies quantum probabilities and contributes directly to the generalized Born rule derived in Section 5. This reveals a direct link between entropy stability and the statistical structure of quantum measurement.

Paradigm Shift. In TEQ, the dominant contribution to quantum probabilities arises not from phase coherence alone, but from entropic stability. The Gaussian path integral reveals that both entropy minimization and entropy curvature govern the likelihood of quantum outcomes. This reframes quantum amplitudes as structurally constrained by thermodynamic geometry, embedding the Born rule within a variational entropy-weighted framework.

Appendix F. Workarounds for Nonunitarity in Standard Quantum Theory and Their Structural Resolution in TEQ

While conventional quantum theory assumes unitary evolution, many physical processes exhibit apparently nonunitary behavior—such as measurement, decoherence, dissipation, and decay. These phenomena are typically addressed through a range of pragmatic workarounds that preserve unitary evolution at the formal level, while introducing auxiliary mechanisms—whether interpretive, phenomenological, or effective—to account for observable loss of coherence or probability.

In contrast, the Total Entropic Quantity (TEQ) framework treats nonunitarity as structurally emergent. The entropy-weighted variational principle introduces a complex deformation of the action,

allowing for non-Hermitian dynamics whenever entropy flow disrupts phase coherence. In TEQ, unitarity is not a foundational postulate but a limiting case: it arises when entropy curvature vanishes and resolution is maximal ($\beta = \frac{i}{\hbar}$). This formulation permits a unified treatment of quantum coherence, decoherence, and dissipation as geometric consequences of entropy flow.

Table A1. Standard treatments of nonunitarity compared to their structural resolution in the TEQ framework.

Standard Method	Mechanism / Assumption	TEQ Structural Resolution	
Density Matrix Formalism [47]	Encodes uncertainty via mixed states. Unitary evolution is retained for isolated systems.	Mixedness arises directly from entropy curvature. Unitarity holds precisely only when entropy flux vanishes $(\beta = \frac{i}{\hbar})$.	
Collapse Postulate [48]	Measurement induces nonunitary projection. Adds extrinsic, non-dynamical rule.	Collapse is emergent. It results from entropy- gradient suppression of unstable paths under coarse-grained resolution.	
Lindblad Master Equa- tion [49]	Effective dissipator models nonunitary evolution in open systems.	Lindblad dynamics correspond to high-entropy- curvature regimes. Entropy geometry replaces phenomenological dissipators.	
Non-Hermitian Hamiltonians [50,51]	Decay and absorption modeled via complex potentials. Effective nonunitary behavior.	Non-Hermitian terms arise from first principles when entropy flow is nonzero. No manual prescription needed.	
Quantum Trajectories [52,53]	Stochastic path simulations reproduce averaged Lindblad dynamics.	TEQ provides deterministic path ensembles from a variational entropy principle. Stochastic elements are replaced by entropy constraints.	
Environment-Induced Decoherence [4,54]	Entanglement with environment leads to effective loss of phase coherence.	Environment and observer resolution limits are internal to entropy geometry. Decoherence reflects limited distinguishability, not tracing.	
Many-Worlds Interpretation [55,56]	Unitary evolution preserved by branching of global wavefunction.	Branching and collapse are limiting regimes of entropy flow. TEQ requires no ontological proliferation, only structural curvature.	

Appendix G. Entropy Gradients, Entropic Forces, and Attractors in Closed Systems

This section formalizes how entropy gradients give rise to deterministic flows and attractor structures within the TEQ framework. These flows are emergent from the geometry of entropy, not from any optimization or agency assumption. Entropic forces represent structural tendencies toward more resolvable macrostates, and attractors correspond to entropy-stationary configurations.

Appendix G.1. Preliminary Assumptions

Consider a dynamical system evolving in continuous time:

$$\frac{d\mathbf{x}}{dt} = f(\mathbf{x}),\tag{A33}$$

with $\mathbf{x} \in \mathbb{R}^n$, and f continuously differentiable [57].

Assumption 1 (Lyapunov Stability [58]). There exists a scalar function $V(\mathbf{x})$ such that $\frac{dV}{dt} \leq 0$ along trajectories. Then $\mathbf{x}(t) \to \mathbf{x}_*$ as $t \to \infty$, for some attractor $\mathbf{x}_* \in \mathbb{R}^n$.

Assumption 2 (Entropy Gradient Flow). The system evolves along the gradient of an entropy-derived potential:

$$f(\mathbf{x}) = -\nabla \Phi(\mathbf{x}), \qquad \Phi(\mathbf{x}) := -TS(\mathbf{x}),$$
 (A34)

where $S(\mathbf{x})$ is a coarse-grained entropy function and T an effective temperature [59,60].

Assumption 3 (Local Convexity Near Equilibrium). The entropy potential satisfies $\nabla \Phi(\mathbf{x}_*) = 0$ and $\nabla^2 \Phi(\mathbf{x}_*) \succ 0$, implying local stability near the attractor [7].

Appendix G.2. Gradient Flow Interpretation

Theorem A3 (Monotonic Entropy Increase). *Under the above assumptions, the system evolves monotonically toward higher entropy:*

 $\frac{dS}{dt} = -\frac{1}{T} \|\nabla \Phi(\mathbf{x})\|^2 \le 0.$

Corollary A5 (Stability of Entropic Attractors). *If* $\nabla \Phi(\mathbf{x}_*) = 0$ *and* $\nabla^2 \Phi(\mathbf{x}_*) \succ 0$, *then the trajectory satisfies* $\mathbf{x}(t) \to \mathbf{x}_*$, a local entropy maximum.

Remark A4. This generalizes the second law of thermodynamics into a local dynamical principle, where entropy increase is a structural outcome of the system's geometry rather than a probabilistic trend or imposed constraint.

Appendix G.3. Extension to Open Systems

In open systems, entropy exchange with the environment modifies the internal entropy potential.

Definition A1 (Time-Dependent Entropy Potential). Let

$$\Phi(\mathbf{x},t) := -T(t)S(\mathbf{x},t), \qquad \mathbf{F}_{entropic} := -\nabla\Phi(\mathbf{x},t),$$

define the dynamic entropy landscape.

Theorem A4 (Non-Equilibrium Steady State (NESS) [61]). A NESS satisfies

$$\sigma = rac{dS_{system}}{dt} + rac{dS_{environment}}{dt} = 0$$
, with $rac{dS_{system}}{dt}
eq 0$,

where σ is the total entropy production rate.

Corollary A6 (Moving Entropic Attractors [62]). *In time-dependent landscapes, dynamic attractors evolve as local minima of* $\Phi(\mathbf{x}, t)$ *, leading to entropy-guided adaptation.*

Appendix G.4. Implications for TEQ

- Entropy gradients define vector fields over configuration space, determining structural flows without invoking optimization.
- Attractors correspond to entropy-stationary configurations under coarse-grained evolution.
- The arrow of time emerges as an internal feature of entropy geometry, not an externally imposed boundary condition.

Paradigm Shift. In TEQ, attractors are emergent geometric fixed points in entropy-weighted flow, not imposed equilibrium constraints. This unifies thermodynamic, dynamical, and informational evolution under a single variational principle based on entropy geometry.

Appendix H. Justification of the Entropy Gradient Approximation

In the TEQ framework, the entropy-weighted action modifies the classical variational principle:

$$S_{\text{eff}}[x] = \int (L(x, \dot{x}) - i\hbar\beta g(x, \dot{x}))dt, \tag{A35}$$

where $g(x, \dot{x})$ is the local entropy flux density, derived from entropy geometry (see Appendix B). The resulting Euler–Lagrange equation becomes:

$$\frac{d}{dt}\frac{\partial L}{\partial \dot{x}} - \frac{\partial L}{\partial x} = i\hbar\beta \left(\frac{d}{dt}\frac{\partial g}{\partial \dot{x}} - \frac{\partial g}{\partial x}\right). \tag{A36}$$

To obtain a corresponding Hamiltonian structure, one typically replaces the velocity-space entropy gradient with its configuration-space counterpart. This section provides a rigorous justification for the approximation:

$$\left\langle \frac{\partial g}{\partial \dot{x}} \right\rangle \approx \frac{\partial g}{\partial x}.$$
 (A37)

Appendix H.1. Entropy-Weighted Expectation

Given the entropy-weighted path integral distribution:

$$\mathcal{P}[x(t)] \propto \exp\left(\frac{i}{\hbar}S[x] - \beta \int g(x,\dot{x})dt\right),$$

the expectation of an observable $\mathcal{O}[x]$ is:

$$\langle \mathcal{O} \rangle = \frac{\int \mathcal{D}[x] \, \mathcal{O}[x] \, e^{iS[x]/\hbar - \beta \int g dt}}{\int \mathcal{D}[x] \, e^{iS[x]/\hbar - \beta \int g dt}}.$$
 (A38)

For $\mathcal{O} = \partial g/\partial \dot{x}$, we compute:

$$\left\langle \frac{\partial g}{\partial \dot{x}} \right\rangle = \frac{\int \mathcal{D}[x] \frac{\partial g}{\partial \dot{x}} e^{iS/\hbar - \beta \int g dt}}{\int \mathcal{D}[x] e^{iS/\hbar - \beta \int g dt}}.$$
 (A39)

Using the chain rule:

$$\frac{dg}{dt} = \frac{\partial g}{\partial x}\dot{x} + \frac{\partial g}{\partial \dot{x}}\ddot{x},\tag{A40}$$

and taking the expectation:

$$\left\langle \frac{dg}{dt} \right\rangle = \left\langle \frac{\partial g}{\partial x} \dot{x} \right\rangle + \left\langle \frac{\partial g}{\partial \dot{x}} \ddot{x} \right\rangle. \tag{A41}$$

Appendix H.2. Fluctuation Suppression

Lemma A4 (Entropy-Curvature Suppression). Let $g(x, \dot{x})$ be locally convex in \dot{x} , with:

$$g(x,\dot{x}) \approx g(x,\dot{x}_{st}) + \frac{1}{2}\kappa(x)(\delta\dot{x})^2$$
, where $\kappa(x) := \frac{\partial^2 g}{\partial \dot{x}^2} > 0$.

Then velocity fluctuations satisfy:

$$\left\langle |\ddot{x}|^2 \right\rangle \le \frac{C}{\beta \kappa(x)},\tag{A42}$$

for some finite constant C depending on system scale and local smoothness.

Sketch. This follows from standard Gaussian path integral suppression: large $\beta \kappa$ exponentially dampens off-path fluctuations in \dot{x} , bounding the variance of second derivatives [18,19].

Appendix H.3. Main Result

Theorem A5 (Entropy Gradient Approximation). Let $\beta \gg 1$, and assume $g(x, \dot{x})$ is C^2 in \dot{x} with local entropy curvature $\kappa(x) := \partial^2 g/\partial \dot{x}^2$. Then:

$$\left| \left\langle \frac{\partial g}{\partial \dot{x}} \right\rangle - \frac{\partial g}{\partial x} \right| \le \frac{C}{\sqrt{\beta \kappa(x)}},\tag{A43}$$

where $C \in \mathbb{R}^+$ depends on the system's resolution scale and fluctuation amplitude.

Corollary A7 (Stability of the Hamiltonian Limit). *In the limit* $\beta \to \infty$, *the approximation*

$$\left\langle \frac{\partial g}{\partial \dot{x}} \right\rangle \approx \frac{\partial g}{\partial x}$$

becomes asymptotically exact. Entropy-weighted Hamiltonian dynamics remains well-posed and converges to classical form.

Appendix H.4. Interpretation

This result justifies the substitution used in deriving entropy-deformed Hamiltonian dynamics and Schrödinger evolution in TEQ. It confirms that under strong entropy weighting, configuration gradients dominate over velocity gradients, effectively compressing the entropy geometry into configuration space.

Paradigm Shift. In TEQ, velocity-space entropy gradients collapse to configuration gradients in the high- β regime. This enables entropy-weighted classical and quantum mechanics to emerge as coarse-grained limits of a unified entropy geometric variational principle.

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