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Posted Date: 15 January 2025

doi: 10.20944/preprints202410.1227.v3

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Article

# Tracking of Fin Whales Using Their Calls Recorded by Triplets of Hydrophones

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**Abstract:** Whale signals originating in the vicinity of a triplet of underwater hydrophones, 2 km distant from each other, and recorded at the three hydrophones, offer the opportunity to verify simple models of propagation applied in the immediate neighborhood of the triplet, by comparing arrival times and amplitudes between the three hydrophones. Examples of recordings of individual fin whales based on the characteristics of their vocalizations around 20 Hz, passing by hydrophone triplets are presented. Conclusions are drawn about waveform coherency and amplitudes of the signals recorded at the three hydrophones in the [10-50] Hz frequency band. A grid-search method of tracking the calls is presented based on time differences of arrivals between three hydrophones obtained with a combination of power detector time picking and cross-correlation. The spherical amplitude decay law of one over the distance is verified using amplitude ratios between two of the hydrophones, when the cetacean is in the immediate vicinity of the triplet, in a circle of radius 1.5 km sharing its center with the triplet. In turn, the measurement of the amplitude ratios between two hydrophones allows for an estimate of the depth of vocalization when the animal is within 250 m of horizontal distance of one of the hydrophones. Analysis of hundreds of calls leads to the possibility that more accurate coordinates and depth of the hydrophones are needed to unambiguously verify the laws of propagation, or that more elaborate non-isotropic models of propagation are needed.

**Keywords:** hydroacoustics; signal processing; location methods; whale tracking; whale vocalizations; acoustic monitoring; acoustic propagation models.

## 1. Introduction

Whale songs are frequently recorded on the hydrophones of the International Monitoring System (IMS) hydroacoustic network of the Comprehensive Nuclear-Test-Ban Treaty Organization (CTBTO) [1]. The larger whales, such as blue whales — *Balaenoptera musculus* — and fin whales — *Balaenoptera physalus* —, emit acoustic energy in the [15-50] Hz frequency range [3], which can be used to assess the suitability of simple ocean-acoustic wave propagation models to estimate the location of the whales. A lot is unknown about whale vocalization (acoustic signal emitted by whales). Such questions as: the depth at which they emit the sound; if they emit the sound when only at certain depths; the depth-dependent interference of the direct signal with the surface reflection; the possible frequency — and depth — dependent radiation pattern of the acoustic emission, etc. Attempts have been made to estimate the range from the in-water hydrophone IMS stations at which the signals are recorded. Even far ranges are considered in these attempts as it is well known that acoustic energy can travel very efficiently if it is guided in the Sound Fixing and Ranging (SOFAR) channel [4].

The locations of all IMS stations [2], including the hydroacoustic stations, are openly available. Five of the six in-water hydrophone IMS stations consist of pairs of triplets of hydrophones close to oceanic islands. These island stations have one triplet deployed to the north and the other to the south of the island with hydrophone deployment depths close to the generally considered depth of the SOFAR channel of 700 m to 1000 m. This hydrophone depth provides excellent detections of hydro-

acoustic signals originating from very far distances of thousands of kilometers if trapped in the SOFAR channel. The acquisition system of the hydrophones has a sampling frequency of 250 Hz. A filter is applied to the data compensating for the system response that makes the data above 100 Hz difficult to use as calibrated data. Less relevant to the study in this paper, the acquisition system also has limitation on the lower frequency end. This still allows recordings of signals almost undisturbed between 1 and 100 Hz. This bandwidth is mandated by Member States of the CTBTO [1] as specifications for the IMS hydrophones in the Operational Manual for Hydroacoustic Stations developed as required by the CTBT Treaty.

Previous works were concerned with whale tracking methods for basic understanding of animal behavior and mitigation of seismic air gun surveys on the animals. Methods have been developed to estimate the depth of a diving sperm whale – *Physeter macrocephalus* – from the time difference between the direct arrival and the surface reflection, using two or three elements vertical or horizontal hydrophone arrays [5]. Triangulation has been used to track the diving behavior of bowhead whales – *Balaena mysticetus* – in the noisy environment of a seismic air gun survey [5]. In both these examples, the signals emitted by the animal cover higher frequencies ([5-20] kHz and short duration < 25 ms) for sperm whales, and [0.2-2] kHz for bowhead whales). These higher frequencies are above the useful frequency range of the IMS hydrophones, and the present work studies signals emitted by likely fin whales, at frequencies below 0.1 kHz. Whale tracking has also been used to compare the source level of fin whale signals recorded at an in-water hydrophone location in the Pacific Ocean and an Ocean Bottom Seismometer (OBS) in the Atlantic Ocean [7]. Parabolic equation modeling is the central tool used to derive the source level of fin whales in the two regions [8].

Other works do not specifically track whales but rather use characteristics of their calls and spatial and temporal statistics of the calls, for instance to get information on the population of blue whales in the southeast Indian Ocean and southwest Pacific Ocean [9]. Temporal statistics have put in evidence that the dominant frequency of pygmy blue whales decreases with time over a period of 8 years [10], and that their range of detectability is between 50 km and 200 km from the HA01 triplet [11]. A range estimate of up to several tens of kilometers from the northern triplet of HA08 for blue whales in the Chagos archipelago in the Indian Ocean, was obtained using a method based on two parameters: back-azimuth estimates using the signals on the three hydrophones and amplitude decay estimates [12]. At these distances, based on modeling up to signal propagation ranges of 250 km, the amplitude of the whale signal decays roughly like the inverse of the square root of the distance to the hydrophone, as expected from a cylindrical geometrical spreading. The blue whale calls were detected in records from January 2003 with a Short-Term Average/Long-Term Average (STA/LTA) method using a ratio threshold of 2.5.

At closer range, it is possible to make the assumption that the whale is close to the surface (whale depth is assumed to be zero) and then use the differences in the times of arrivals between the three hydrophones to estimate a location. At further ranges, only the direction of the incoming signals is available. A grid-search method was used to trace the path of a likely fin whale crossing the waters above hydrophone station HA01, Cape Leeuwin, Australia [13]. In that work, the authors tracked the movement of the whale through the three hydrophones using the direct arrival from the whale signal. They also observed multiple scattered energetic arrivals – one directly from the ocean bottom, another from the sea surface after reflection from the ocean bottom – as the whale position was close to being in the area directly above the hydrophones. Similar multiple scattered arrivals from the ocean bottom and sea surface had previously been observed in bottom-moored hydrophones in the Southern Ocean [14]. In addition to water multiple reflections, crustal reflections were observed from fin whale calls recorded on ocean bottom seismometers in the straits of Juan de Fuca, between the USA and Canada [15].

Tagged animal studies on fin and blue whales [16] have been conducted and show some variability in the swimming depth of a fin whale between very shallow depth (10 m) and up to nearly 300 m. A deeper dive may occur amidst shallower ones. At shallow depths of vocalization of a fin whale, somewhere between the sea surface and 300 m depth, it may be difficult to differentiate in

time between the direct path from the animal to the hydrophone, and the reflection from the sea surface. In [13], a double peak in the autocorrelation and envelope of the first arrival may hint at this sea surface reflection. An elaborate approach [17] based on modeling Lloyd's mirror effect [18] estimated the depth of vocalizing fin whales using the hydrophone and vertical component seismometer channels of Ocean Bottom Seismometers (OBS) and estimated a depth of 72 m in one of the examples. A shallow depth of 15 m was also estimated, for an individual fin whale localization, based on the modeling of travel times of multiple bottom and surface reflections, at the three hydrophones of the southern triplet of IMS hydroacoustic station HA11 [19].

The purpose of the paper is to track and locate whales emitting low-frequency sound, such as blue whales, fin whales, and recorded on the existing deployed hydro acoustic network of the IMS sensor network. Because of the frequency bandwidth of the recordings, it is a challenge to separate arrivals in the time domain when they are close together, as is the case for the direct arrival and the surface reflection if the animal is close to the surface. It may be possible to gain information in the frequency domain, together with the three distances to the hydrophones, i.e., the Lloyd's mirror where the separation of fringes at a particular frequency depends on the distance of the source to the sea surface. The advantages of the IMS network are its quality, thanks to the calibration of the data, its spatial coverage, continuous acquisition system, and potential for automatic processing, for instance detecting specific features in the signal. In the present work, data processing and location methods are applied to a data set recorded at the same hydrophone triplet H11, on 19 and 20 February 2024. A fin whale passed close to the triplet, similarly to the 26 July 2017 at HA01 [13], and the multiple passages at HA11, between 2010 and 2022 [19].

After finding that a method purely based on cross-correlation to measure the time delays of the signal arrival time at different hydrophones — or Time Differences of Arrival (TDOA) — is inappropriate because of the presence of strong bottom and sea surface reflections, a method based on time pick differences combined with cross-correlation is presented and found to be appropriate for the case of this data set where the animal is close to the hydrophone triplet. A grid-search localization method is then presented and applied with the TDOAs as input.

A further contribution of this work is to take advantage of the passage of the whale close to two of the hydrophones to estimate its vocalization depth when above the hydrophones. It is assumed that the amplitudes decay linearly with (one over distance law) distance from the source when in the vicinity of the hydrophones, specifically within 1.5 km from the center of the hydrophone triplet. This is equivalent to the inverse square law of energy for a point source in free space. Energy is the square of the amplitude. It is also assumed that the amplitudes of the signals are spherically symmetrical and do not depend on the direction of motion of the whale.

## 2. Data Acquisition and Processing Methods

### 2.1. Data Acquisition

The data set analyzed in this work was acquired at IMS hydroacoustic stations HA11. Table 1 shows basic site location parameters for the hydrophones H11S1, H11S2, and H11S3 of the southern triplet of the station. For the remainder of this work, the identifiers S1, S2, S3, as shown in Table 1 will be used for respectively H11S1, H11S2, and H11S3. A local coordinate system has the S1 hydrophone location as its origin and Table 1 also shows the coordinates of the hydrophones in this local system. Figure 1d is a simple local map showing the geometry of the triplet.

**Table 1.** Basic geometry parameters for HA11S triplet. The water depth is 1174 m.

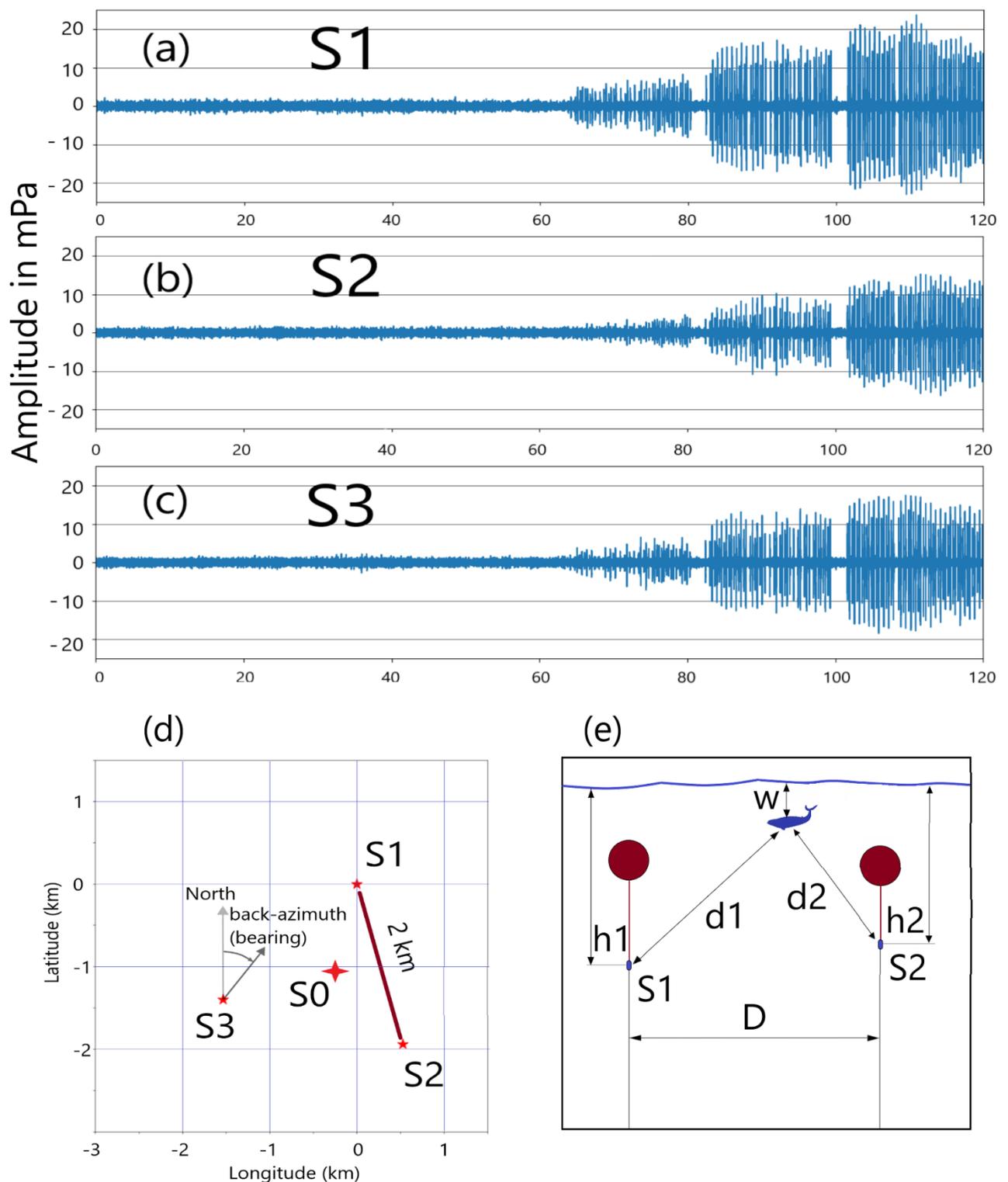
Hydrophone	Identifier	Latitude Longitude* (decimal degree)	Latitude Longitude (km from S1)	Depth (m)
H11S1	S1	18.50827 166.700272	0.000 0.000	<i>h1</i> 739** 750*

H11S2	S2	18.49082	-1.939	<i>h2</i>	739**
		166.705002	0.498		742*
H11S3	S3	18.49568	-1.399	<i>h3</i>	739**
		166.686462	-1.455		724*

\* Obtained from [20] \*\*Obtained from [21].

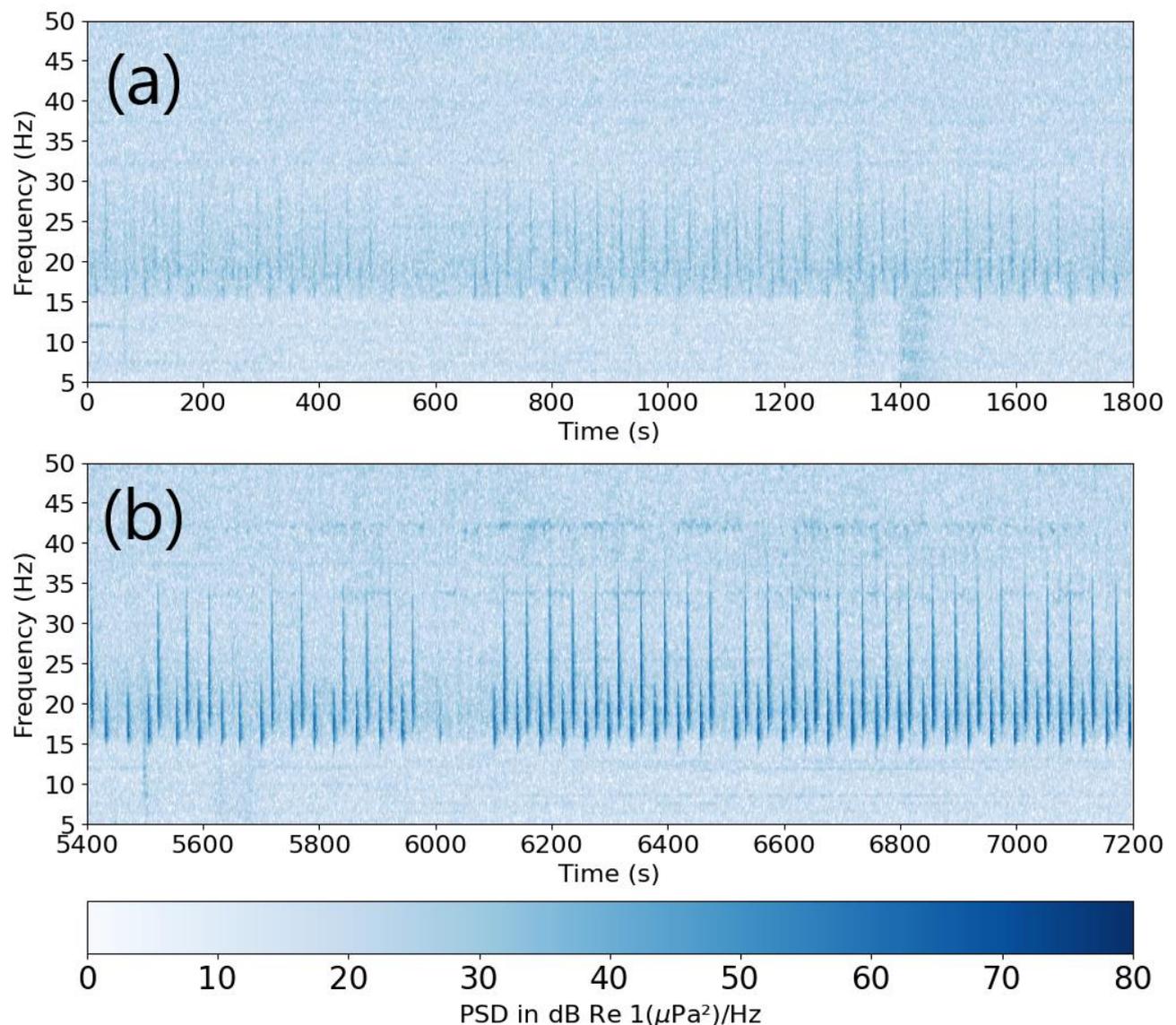
The data is openly available from the IRIS data center [20] with network code IM. Figures 1a, 1b, and 1c show two hours of the three hydrophone traces at respectively S1, S2, and S3 at the beginning of the sequence of interest, starting at 21:00 UTC on 19 February 2024. The data of interest is clearly visible on the raw waveform starting at around 22:05 UTC, sixty-five minutes after the beginning of the trace. Several observations can be made regarding the features of the signal on the three waveforms:

- The amplitude of the signal is increasing on all three waveforms starting from about one hour after time zero. This can easily be explained if the source is progressively getting closer to all three sensors until the end of the two-hour sequence.
- The amplitudes at S1 and S3 are slightly higher than at S2.



**Figure 1.** (a), (b), and (c) show two hours of unfiltered hydrophone data starting at 21:00 UTC on 19 February 2024 for, respectively, the S1, S2, and S3 hydrophones. At the one-hour mark approximately, frequent (approximately once every 25 seconds) impulsive signals are visible and increasing in amplitude towards the end of the section. The amplitudes are in mPa, and the horizontal lines are the -10, -20, 10, and 20 mPa levels. (d) Basic map with the S1 hydrophone being the origin of the local horizontal coordinate system. S0 marks the center of the triplet and the arrow next to S3 shows how the back-azimuth is measured from the North. The latitude and longitude differences are in kilometers. The absolute latitude and longitude of the S1 hydrophone are respectively 15.50827 degrees North and 166.700272 degrees East. (e) Vertical geometry in a cross-section including S1 and S2 and defines parameters used in the text. The whale may or may not be in the same plane as S1 and S2.

There appears to be interruptions of two to three minutes in the sequence of calls every fifteen to twenty minutes. Since it is well known that cetaceans surface at regular intervals to breathe, it seems natural to infer that these short interruptions correspond to the surfacing of a single individual, or several individuals surfacing in a synchronized fashion, and that the vocalizations happen while the animal dives between the surfacing. This pattern has previously been observed and the three minutes interruptions attributed to surfacing of the animal [22].



**Figure 2.** Spectrograms of the first 30 minutes (a), and the last 30 minutes (b) of the two hours of waveforms for S2 shown on Figure 1. An FFT length of 1024 points with 512 points overlap was used to compute the whole spectrogram over the 7200 s. The first 30 minutes and last 30 minutes were then windowed. The Nyquist frequency is 125 Hz. The frequency resolution is 0.244 Hz (512 intervals in [0-125] Hz) and the time resolution is 2.05 s.

On the spectrogram for the same time interval, the beginning of the trace also shows the large amplitude individual transient arrivals in the [15-50] Hz band. This is illustrated by Figure 2 showing the first and last 30 minutes of the two-hour interval. Observations beyond the previous ones can be made from the spectrograms:

- Two types of calls are clearly visible on the spectrogram. One type has a broader bandwidth [17-40] Hz and higher center frequency than the other one [15-25] Hz. The nomenclature type A for the lower frequency type and type B for the higher frequency have previously been used in the

literature[19]. The two types are separated by about 25 s and generally alternate, but not always. An exception can be seen in Figure 2 in an interval of about 100 s after 5600 s with three consecutive type B in that interval, and again twice at about 5800 s. Each call is picked individually, and the measurement of amplitudes shows a bimodal distribution corresponding to these two types.

- If the hypothesis that the interruptions in the calls are at the time of surfacing, and the calls originate with a single individual, the first call when the animal dives is generally the lower, narrower band, frequency pulse (type A), and the last call is the higher, broader band, frequency call (type B)

## 2.2. Waveform Signal Processing

To estimate the location of the whale calls when the signal is strong, we start by picking individual signals out of the background noise using the STA/LTA ratio method, explained in [23]. This method is often applied on seismic data (e.g. [24]) for the purpose of automatic picking of seismic phases. In the present work, the STA time interval is 0.1 s and the LTA time interval 1 s. This method is also part of the hydroacoustic processing chain at the International Data Centre (IDC) of the CTBTO, as explained in detail in [25]. In the present work, the STA/LTA method is used on the envelope,  $E$ , of the waveform  $W$  after bandpass filtering between [10-50] Hz, rather than directly on the waveforms themselves. The bandpass filter used is a fourth order Butterworth filter. If  $nsta$  is the number of samples in the STA interval and  $nlta$  the number of samples in the LTA interval, the power detector STA/LTA trace,  $Pd$ , is computed as:  $Pd[k] = \frac{\sum_{i=1}^{nsta} E[k-nsta+i]^2}{\sum_{i=1}^{nlta} E[k-nlta+i]^2}$ , where  $E[k] = \sqrt{W[k]^2 + H(W)[k]^2}$ , and  $H(W)$  is the Hilbert transform of  $W$ .

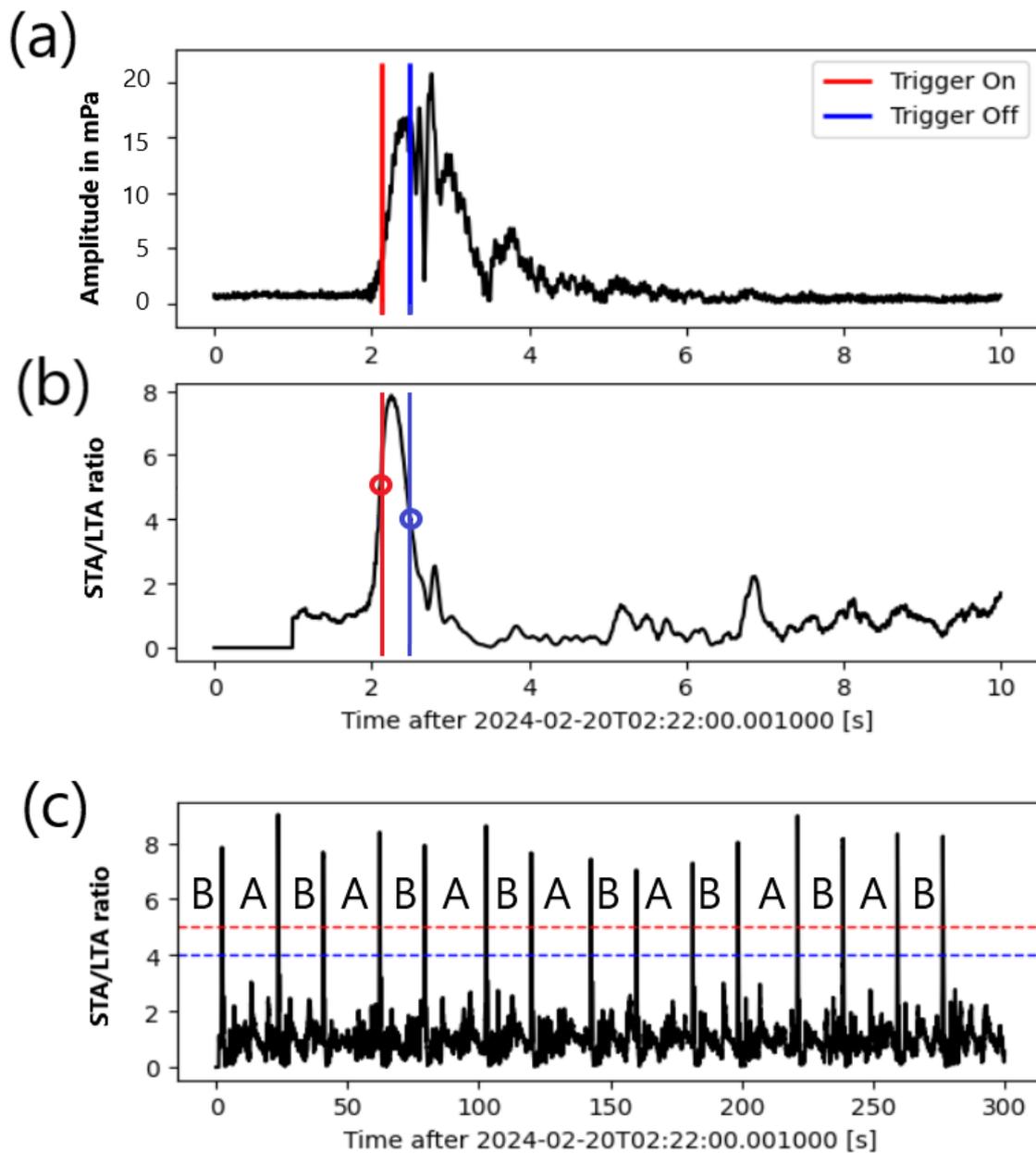
This is illustrated by Figure 3 where values of 5 for the trigger-on and 4 for trigger-off are used on a five-minute segment of data at hydrophone S1 starting at 2:20:00 UTC on the 20 February 2024. Fifteen detections are made in the time segment. Figure 3a shows a close-up of the envelope of the first call in the sequence, which is identified as a type B call. Figure 3b shows the STA/LTA function for that call. For the same time interval, the same number of detections is made on the other two hydrophones, S2 and S3. Figure 3c shows the fifteen calls, with the type A or B identification placed before each call.

Figure 4 shows signals for the same call as in Figure 3a at hydrophones S1 and S2 on 10-second segments starting 2.5 seconds before the STA/LTA on-trigger times at hydrophone S1. The TDOA between the direct arrivals is clearly visible and emphasized by the thin blue lines, which is labeled d12.

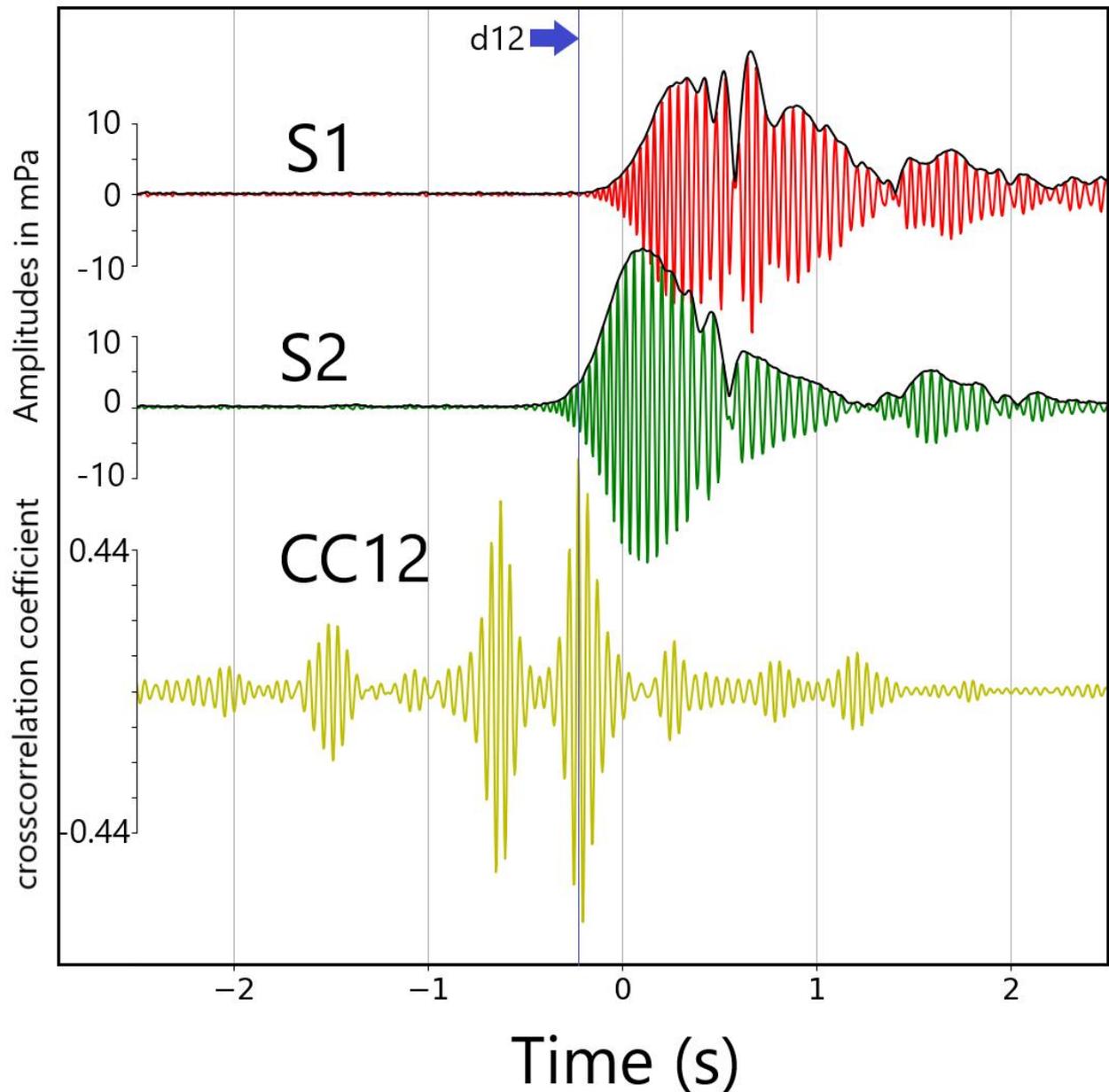
Two methods were tested to compute TDOAs between the three hydrophones to assess a location for the source of the signals in the case when the signal is strong enough to trigger the detector with the parameters specified above:

1 – The first method is to compute TDOAs from the cross-correlations between S1 and the other two traces for each detection made at S1. The cross-correlations are computed on ten-second segments and the detection is confirmed on the three traces when the maximum of the cross-correlation is larger than 0.5.

2 – The second method is to use detections made on the other hydrophones if they fall within a three-second interval from the S1 detection. The TDOAs are then simply the time differences between the detection times.



**Figure 3.** Illustration of the STA/LTA detection method on a 10 second interval with a single call at S1. (a) envelope of the first signal with red and blue timelines to show respectively the trigger-on and trigger-off times. (b) STA/LTA function of the first signal. In addition to the timelines showing the trigger-on and trigger-off, the circle markers show their respective threshold values of 5 and 4 (c) STA/LTA of the envelope of the five-minute interval with fifteen calls. Each call is labelled A or B according to its center frequency. The red and blue horizontal dotted lines show the trigger-on and trigger-off thresholds.

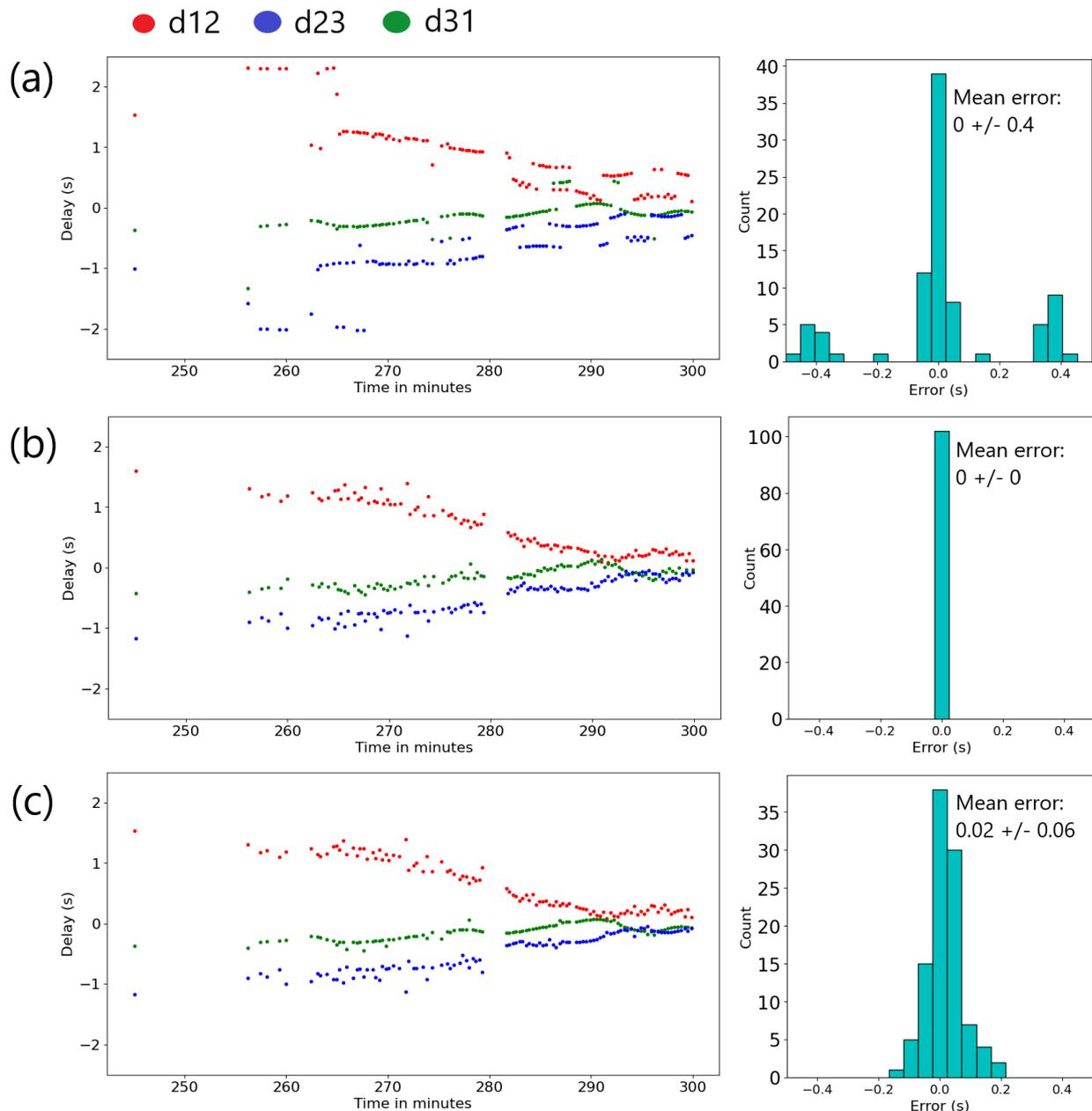


**Figure 4.** Traces S1, S2, and their cross-correlation function CC12 for the call shown in Figure 3. The zero on the time axis is the time of the STA/LTA pick on S1. The maximum value of the CC12 cross-correlation is 0.73 for a time shift of -0.23 s, emphasized by the thin blue line marked d12.

Figure 5 illustrates the difference in TDOA computation between the two methods on the two-hour interval shown on Figure 1. The STA/LTA detector found respectively 142, 124, and 131 detections on S1, S2, and S3 in that interval. Note that the first detection is made after 60 minutes, five more detections are made between 75 and 80 minutes, and between 80 minutes and 120 minutes, the detection density is higher than two per minute.

There are striking differences between the results of the two methods used to compute the delays. The cross-correlation based method 1 (Figure 5a) shows higher consistency between the estimated values of the TDOA for consecutive calls, however there are sudden jumps in these values from one call to the next. These can be attributed to the reflected arrivals following the first arrival, which can be as large as the first arrival (see for instance S3 trace on Figure 4). The picks-only method 2 (Figure 5b) does not show these sudden jumps in the values of the TDOAs likely because the method ensures that the TDOAs will be computed on the first arrival and not later reflected arrivals.

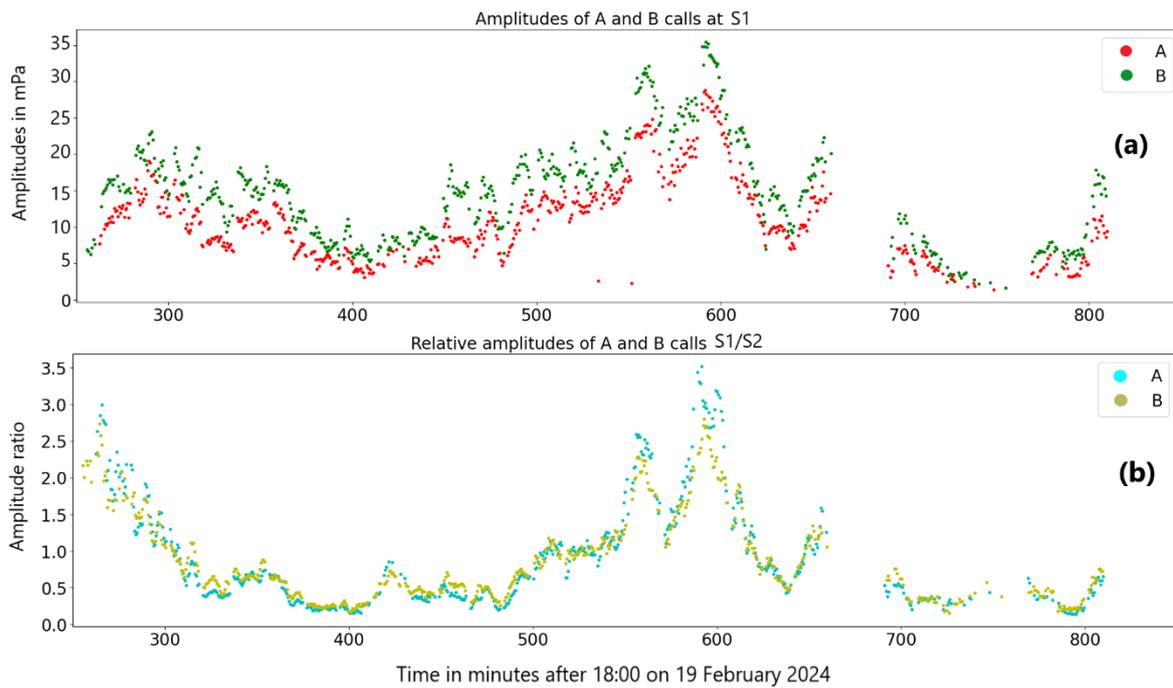
The consistency between two consecutive calls however is not as good as for method 1, partly because there is no guarantee that picks based on a value of STA/LTA optimize the alignment of waveforms. A natural improvement consists of using method 2 to get initial values and then refine the value of the TDOA via cross-correlation (Figure 5c). In the remainder of this study, it will be referred to as “improved method 2”. The histograms on the right of each panel show the distribution of closure errors for each panel. The errors are always zero by construction for method 2 and can be large for method 1. This may happen for instance when the maximum of the cross-correlation corresponds to a correlation between a direct arrival and a reflected arrival. Improved method 2 shows that introducing a small shift based on the cross-correlation TDOA values increases the errors. The errors remain within a value of 0.2 seconds, however.



**Figure 5.** Panel (a) shows the results of picking TDOAs based on method 1 (cross-correlation), and panel (b) is based on method 2 (STA/LTA picks only). Panel (c) shows the result of improved method 2, obtained by adjusting (b) with cross-correlation values when TDOAs obtained with the two different methods are within a tenth of a second of each other. Red dots are the delays (d12 or cd12) between S1 and S2, the green dots, the TDOAs (d31 or cd31) between S1 and S3, and the blue dots are the TDOAs between S2 and S3 (d23 or cd23). On

the right of each panel is a histogram of the errors estimated from the difference between the measured TDOAs  $e=(d_{12}+d_{23}+d_{31})$  which should theoretically be zero.  $|e|$  is called the closure and is described in detail in [26].

The amplitudes are computed as the maximum of the envelope in a 6 s interval starting 2.5 s before the detection trigger time on S1. Figure 6a illustrates the difference in amplitude between the A calls and the B calls. B calls have consistently higher amplitudes. When ratios are considered however, such as the ratio of the amplitude at S1 to the amplitude at S2, types A and B calls show a high degree of consistency. This will allow a comparison of this ratio to the ratio of distances once we have a location for each call.



**Figure 6.** (a) Illustration of the amplitude differences between A and B types of calls. The amplitude measure for type B is consistently higher than for type A. The amplitude scale is in mPa. (b) Shows the consistency of the relative amplitudes for types A and B, in this case amplitude at S1 divided by amplitude at S2.

A step-by-step summary of the feature extraction algorithm is provided in Algorithm 1:

Algorithm 1	DTOA and amplitudes extraction
<b>Input:</b> Three waveform segments from S1, S2, S3.	
<b>Output:</b> Three arrays of time differences $d_{12}$ , $d_{23}$ , $d_{31}$ and three arrays of amplitudes $a_1$ , $a_2$ , $a_3$ . All six arrays are of dimension $N_{det}$ , the number of groups of three detections (one each at S1, S2, S3) made.	
Step 1	Apply STA/LTA algorithm on all three waveforms. Get $N_1$ , $N_2$ , $N_3$ detections respectively on S1, S2, S3.
Step 2	For each detection at S1: Cross-correlate waveform 10 s segments (start time 2.5 s before $t_1[i]$ ) within each group, Extract $cd_{12}[i]$ , $cd_{23}[i]$ , $cd_{31}[i]$ , time difference estimates from the maximum of the cross-correlation. These are illustrated in Figure 5a.
Step 3	For each detection at S1: If detections exist for S2 and S3, compatible with a single call detected at all three hydrophones, group them with the S1 detection. This results in $N_{det}$ groups of detections where $N_{det} \leq N_1$ .
Step 4	For each group, calculate $N_{det}$ DTOA as $d_{12}[i] = t_2[i] - t_1[i]$ , $d_{23}[i] = t_3[i] - t_2[i]$ , $d_{31}[i] = t_1[i] - t_3[i]$ , time difference estimates from the STA/LTA pick times. These are illustrated in Figure 5b.
Step 5	Adjust DTOA as $d_{12}[i] = cd_{12}[i]$ if $abs(cd_{12}[i] - d_{12}[i]) < 0.1$ s., and similarly for 23 and 31. These are illustrated in Figure 5c.

Step 6 Extract amplitudes  $a_1, a_2, a_3$ , as the maxima of the envelopes on the 10 s segments. These are illustrated in Figure 6.

### 2.3. Location Method by Grid Search

Since with large amplitudes (above 5000  $\mu\text{Pa}$  in the [10-50] Hz band), it is likely that the whale is close to the triplet of hydrophones, we assume straight line propagation and that the whale is close to the surface (whale depth is assumed to be zero). With these assumptions, using three hydrophones is sufficient to unambiguously locate the vocalization source. The localization of each call is then accomplished by a simple grid search to minimize the time TDOA differences between measured and modeled TDOAs at each hydrophone, assuming straight ray propagation and a water velocity of 1480 m/s. The latitude and longitude grid spacing is 25 m and the depth difference between the source and receivers is set constant during the search. Specifically, the grid search for the first call is initially done over a 10 by 10 kilometers area to locate the first call. For later calls, the search is limited to an area 2.5 by 2.5 kilometers, since the animal cannot travel far from one call to the next. This provides a very substantial efficiency gain.

A step-by-step summary of the grid search algorithm is provided in Algorithm 2:

Algorithm 2	Grid search for optimal location
<b>Input:</b> Three DTOA scalar arrays $d_{12}, d_{23}, d_{31}$ of length $N_{\text{det}}$ .	
<b>Output:</b> Optimal locations of all $N_{\text{det}}$ calls for a given constant depth.	
Step 1	For the initial point $d_{12}[1]$ , assume whale depth of zero, water velocity $v = 1480$ m/s, and straight-line propagation. For each point of a horizontal $400 \times 400$ grid, with 25 m spacing (10 km by 10 km), compute the RMS of the difference between the observed and estimated DTOA: $res[p, q] = \sqrt{(d_{12} - td_{12})^2 + (d_{23} - td_{23})^2 + (d_{31} - td_{31})^2},$ where $td_{12}$ is the theoretical travel time difference between propagation to S2 and propagation to S1: $td_{12} = \frac{\ S_2 - X\  - \ S_1 - X\ }{v},$ where $\ B - A\ $ denotes the distance between points A and B.
Step 2	$X[1]$ is the grid point $[p, q]_{\text{opt}}$ with the lowest value of $res[p, q]$ over all $p$ and $q$ grid points.
Step 3	For later groups of detections, search a $40 \times 40$ grid around $X[i-1]$ , with the same 25 m spacing (1km by 1 km). The reason for a smaller grid is that the whale cannot move further than 0.5 km within the time between consecutive calls.

### 2.4. Amplitude Ratios When the Whale Is Directly Above a Hydrophone

Relative amplitudes of the signals when the whale is located above the S1 and S2 hydrophones is useful in assessing the depth of the whale when it passes above it. The relative amplitudes  $a_1/a_2$  when the whale is above S1 or S2 should be equal to the distance ratio  $d_2/d_1$  between the whale and each of the hydrophones. When it is above S1, the amplitude ratio is:

$$r_1 = \left(\frac{a_1}{a_2}\right)^{S_1} = \frac{d_2}{d_1} = \frac{\sqrt{(h_2 - w_1)^2 + D^2}}{h_1 - w_1} \quad (1)$$

Similarly, when it is above S2:

$$r_2 = \left(\frac{a_2}{a_1}\right)^{S_2} = \frac{d_1}{d_2} = \frac{\sqrt{(h_1 - w_2)^2 + D^2}}{h_2 - w_2}$$

Where  $D$  is the horizontal distance between S1 and S2,  $h_1$  is the depth of S1,  $h_2$  the depth of S2,  $w_1$  and  $w_2$  are the depths of the whale when respectively above S1 or S2,  $d_1$  and  $d_2$  are the distances between the whale and respectively S1 and S2. Figure 1c illustrates the definition of the geometrical quantities.

When the whale is shown to be directly above S1 or S2, its depth can then be computed by solving for  $w$  the quadratic equation resulting from Equation (1):

$$w_1 = \frac{(h_2 - r_1^2 h_1) \pm \sqrt{\Delta_1}}{(1 - r_1^2)} \quad (2)$$

$$\text{Where } \Delta_1 = (h_2 - r_1^2 h_1)^2 - (1 - r_1^2)(D^2 - r_1^2 h_1^2)$$

$$w2 = \frac{(h1 - r2^2 h2) \pm \sqrt{\Delta 2}}{(1 - r2^2)} \quad (2)$$

Where  $\Delta 2 = (h1 - r2^2 h2)^2 - (1 - r2^2)(D^2 - r2^2 h2^2)$

This expression simplifies when  $h1 = h2 = h$ , as is the case when using the values of  $h1$  and  $h2$  from [21],  $h = 739$  m.

$$w = h \pm \sqrt{\frac{D^2 - h^2}{r1^2 - 1}} \quad (3)$$

These formulas will be used to estimate the depth of the whale in the close proximity of S1 and S2 for results of the location algorithm are presented for the complete seventeen-hour interval starting at 21:00 UTC on 19 February 2024.

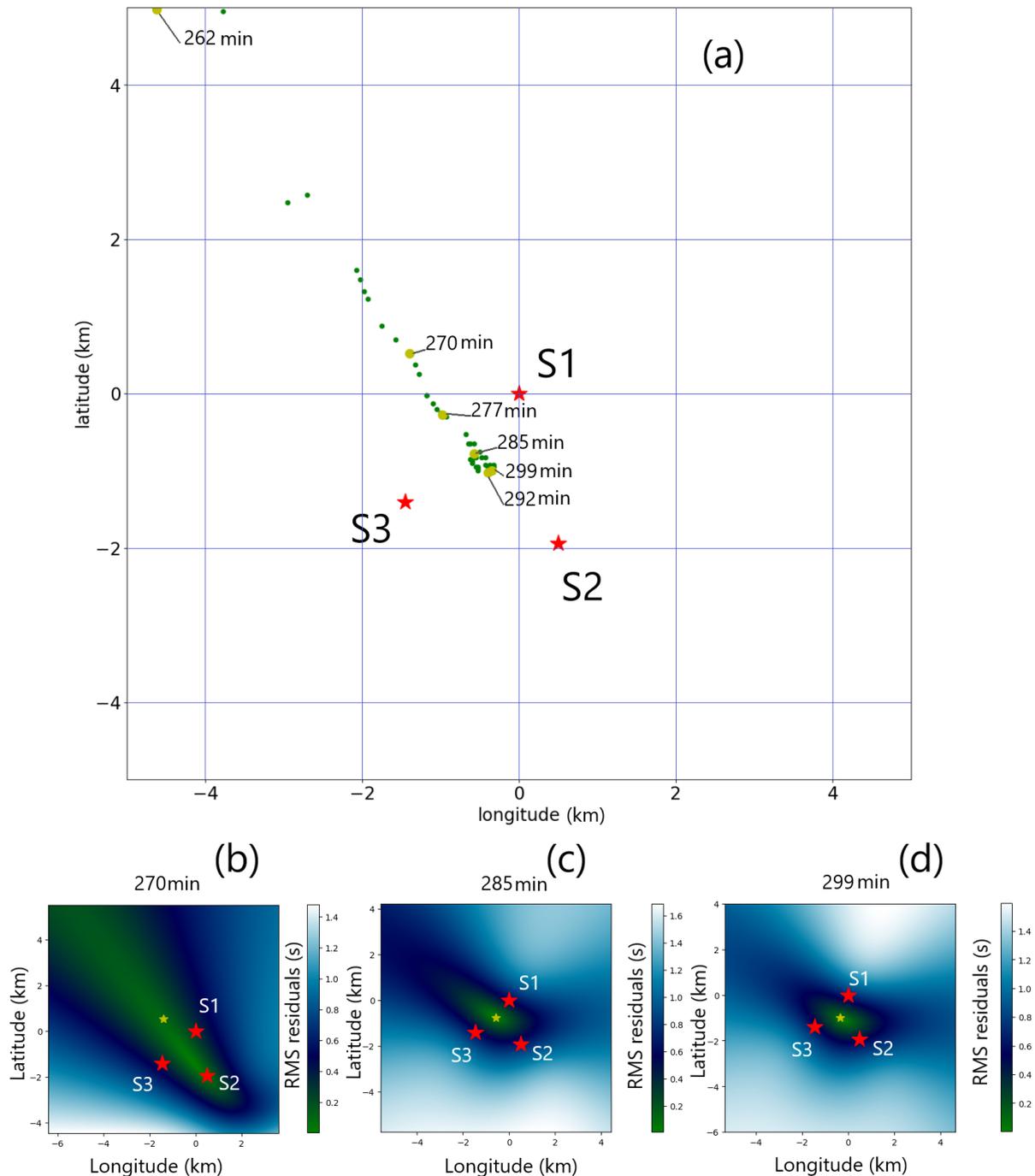
### 3. Results

#### 3.1. Location by Grid Search for the Initial Two-Hour Onset of Observations

While the depth at which the whale vocalizes is unknown, one can assume that it is shallower than the depth of the hydrophones. In a first attempt at tracking the motion of the vocalizing whale, it is assumed to be at the surface of the ocean. Improved method 2, explained in section 2.2, was used to extract the parameters of interest (absolute times of picks, TDOAs between hydrophones, amplitudes of the signal). The amplitudes are computed on the signal's envelopes such as the one shown on Figure 3(d). The depth will trade-off with the projection on the horizontal plane (epicenter in seismology). A way around this is when sensors are directly above the fault in seismology, or directly below the whale for the hydrophones, provided an estimate of the location and origin time are available.

Figure 7a shows a map with the results of the localization of all 49 A calls for the two-hour data set starting at 21:00 UTC on 19 February 2024 (shown on Figure 1). Note the progression of the whale from the northwest to the center of the triplet during this interval.

Figures 7b, 7c, and 7d are maps of the residuals for three of the points indicated by yellow dots on the map. The minimum of the residual is indicated by a yellow star and the value of the residual is shown on a 10 km by 10 km square. It is apparent that the two points (minutes 285 and 299) which fall inside the perimeter defined by the triplet have a better spatial resolution than the point (minute 270) which lays outside of the perimeter. The residual surface for that latter case has a shape elongated along the direction from the center of the triplet to its minimum. The back-azimuth from the center of the triplet is well constrained, but not the distance to the minimum.

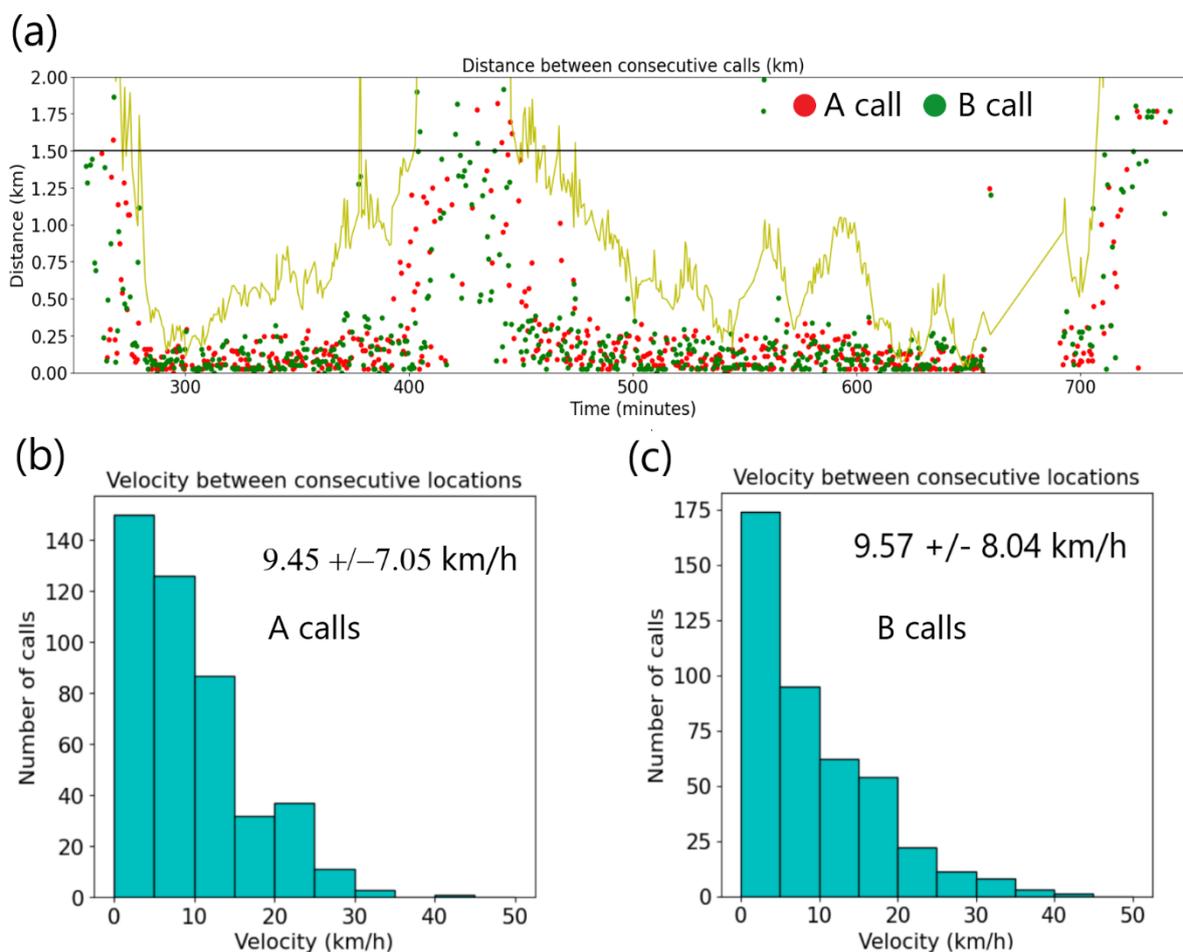


**Figure 7.** Panel (a) is a map showing the location of all A calls (small green dots) detected during the two-hour interval shown on Figure 1. Six of the calls are shown with larger yellow dots and labeled in minutes, corresponding to the detection time on S1 after 18:00 UTC on 19 February 2024, and show the progression of the whale from the northwest of the triplet to its center. The red stars are the locations of the hydrophones. Panel (b) to (d) are the surfaces of the time delay residuals at the time indicated. The yellow star shows the location of the minimum of the RMS of delay residuals for the three specific calls. Note that panels (b) to (d) show ten-kilometers squares centered on the yellow star.

### 3.2. Location and Amplitude Results on the Whole Seventeen Hours of Observations

All calls between 21:00 UTC on 19 February and 14:00 UTC on 20 February with a location close to the center of the hydrophone triplets were gathered into a single data set.

A value of 4 for the STA/LTA trigger-on value was used in this case, and a value of 2 for the trigger-off. A total of 597 A calls and 600 B calls were initially detected.

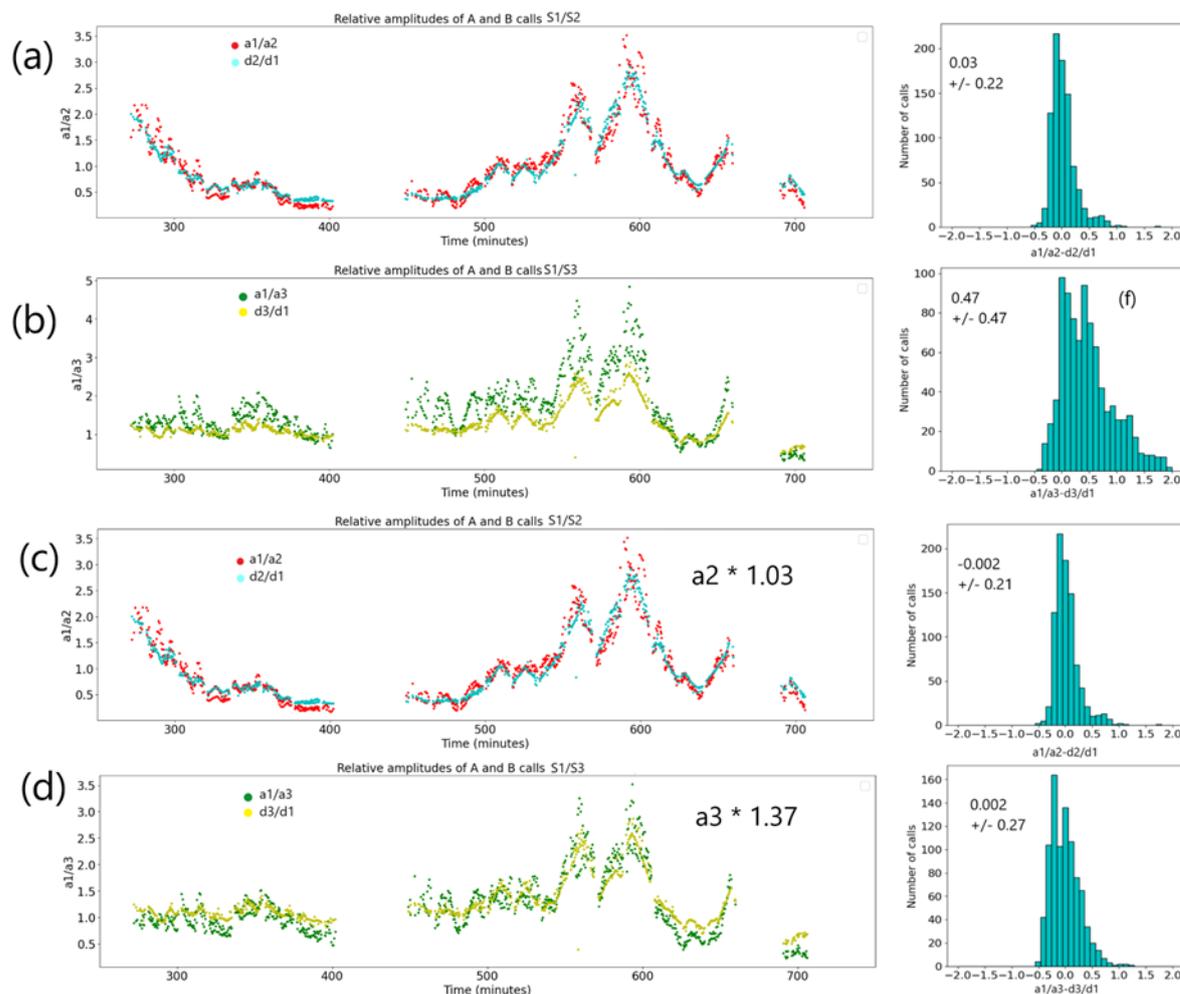


**Figure 8.** (a) Distances between consecutive calls of the same type based on locations derived from the TDOAs for the A and B calls. The red dots correspond to the A calls and the green dots to the B calls. The yellow line shows the distance from the B calls to the center of the triplet. Since the A and B calls are close to each other, the line derived from the A calls would be similar. The solid black indicates 1.5 km. (b) shows the histogram of estimated speed between two consecutive A calls when inside the 1.5 km line for the two different calls (c) shows the histograms of velocity estimates between consecutive B calls.

The assumption that the decay in amplitude is as  $1/R$ , where  $R$  is the distance between the source and the receiver, breaks down when the propagation becomes mostly horizontal for a source far away from the triplet. As demonstrated on Figure 7, the uncertainty on the location is greater when the whale is outside of the perimeter of the triplets. This is also reflected in the average distance between consecutive calls as shown in Figure 8. The yellow line is the distance of the location of calls to the center of the triplet. When that distance falls below 1.5 km, shown by the solid black line, the distance between consecutive calls is concentrated around or below 0.25 km, indicating that a more accurate location is obtained inside of the circle of 1.5 km. The distances between consecutive calls have large average values and standard deviation when outside of the 1.5 km radius circle, as can be seen on Figure 8a between approximately 400 and 450 minutes.

Figure 8 also shows the histograms of estimated swim velocity of the whale when inside the 1.5 km circle, eliminating non-physical outlier values of velocity larger than 50 km/h. This results in a reduced number of 447 A calls and 430 B calls on which velocity statistics are computed. An average value of  $9.45 \pm 7.05$  km/h between two consecutive A calls and  $9.57 \pm 8.04$  km/h between consecutive

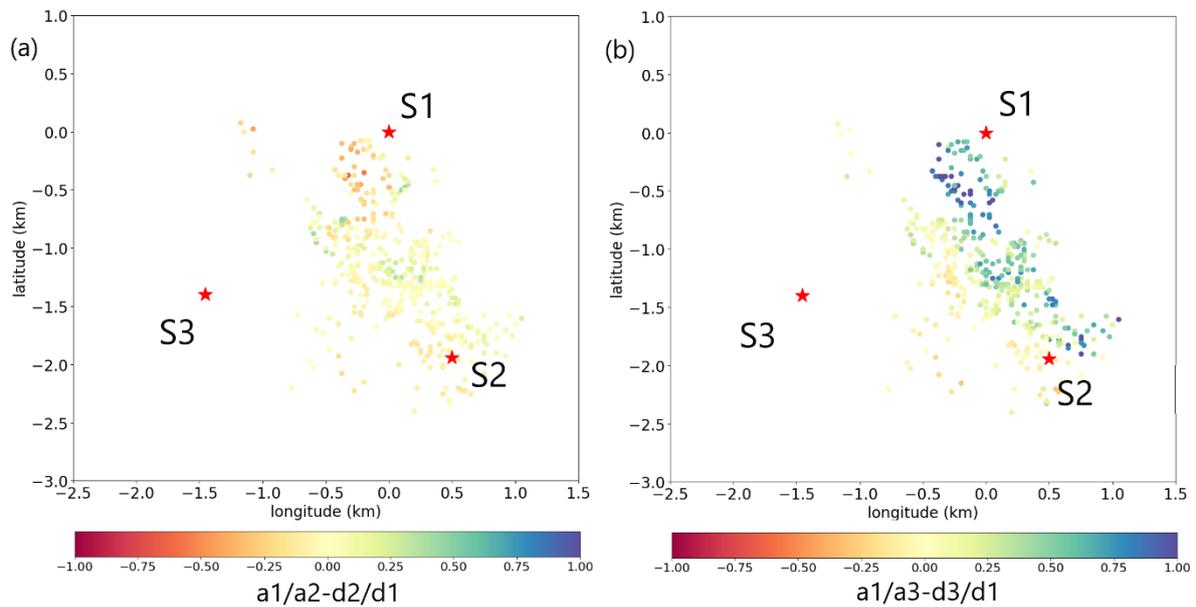
B calls is compatible with what is known about the swim velocity of fin whale, which have a maximum swim speed of 37 km/h, or about 20 knots [3].



**Figure 9.** Relative measured amplitudes  $a1/a2$  (a) and  $a1/a3$  (b) displayed as a function of time when the call location is within 1.5 km of the triplet center. The scale is in minutes from 18:00 on 19 February 2024. For comparison, the distance ratios  $d2/d1$  and  $d3/d1$  are displayed on the same graphs. When a constant bias of 1.03 and 1.37 are applied to respectively  $a2$  and  $a3$ , the graphs are displayed in (c) and (d). The histograms of the residuals ( $a1/a2-d2/d1$ ) and ( $a1/a3-d3/d1$ ) corresponding to each time series are shown to the right of each time series along with their mean and standard deviation.

The relative amplitudes were discussed in section 2.2, and it was concluded that the A and B calls, while exhibiting different absolute amplitudes in the frequency band considered, the relative amplitudes between hydrophones show consistency between the two types of calls. Figure 9 shows the variations and histograms of the relative amplitudes  $a1/a2$  and  $a1/a3$  where  $a1$ ,  $a2$ ,  $a3$  are respectively the amplitudes measured at S1, S2, and S3. The measured ( $a1/a2$ ) and theoretical ( $d2/d1$ ) values follow each other quite closely, while  $a1/a3$  and  $d3/d1$  depart from each other, as emphasized by the histogram of the differences. When using only the calls within the 1.5 km limit from the center of the triplet and eliminating outliers (residuals of  $|a1/a2-d2/d1|$  more than 1 and  $|a1/a3-d3/d1|$  more than 2), the biases are computed from the average ratios of ( $d2/d1$ ) to ( $a1/a2$ ). The biases are respectively 1.03 for  $a1/a2$ , and 1.37 for  $a1/a3$ . If the larger bias observed at S3 originates from the need to adjust the calibration of that hydrophone, it should be possible to observe the same kind of average differences for hydroacoustic arrivals propagating horizontally on large distances before

reaching the triplet, of which there is a very large database at the IDC. This is however beyond the scope of this study.

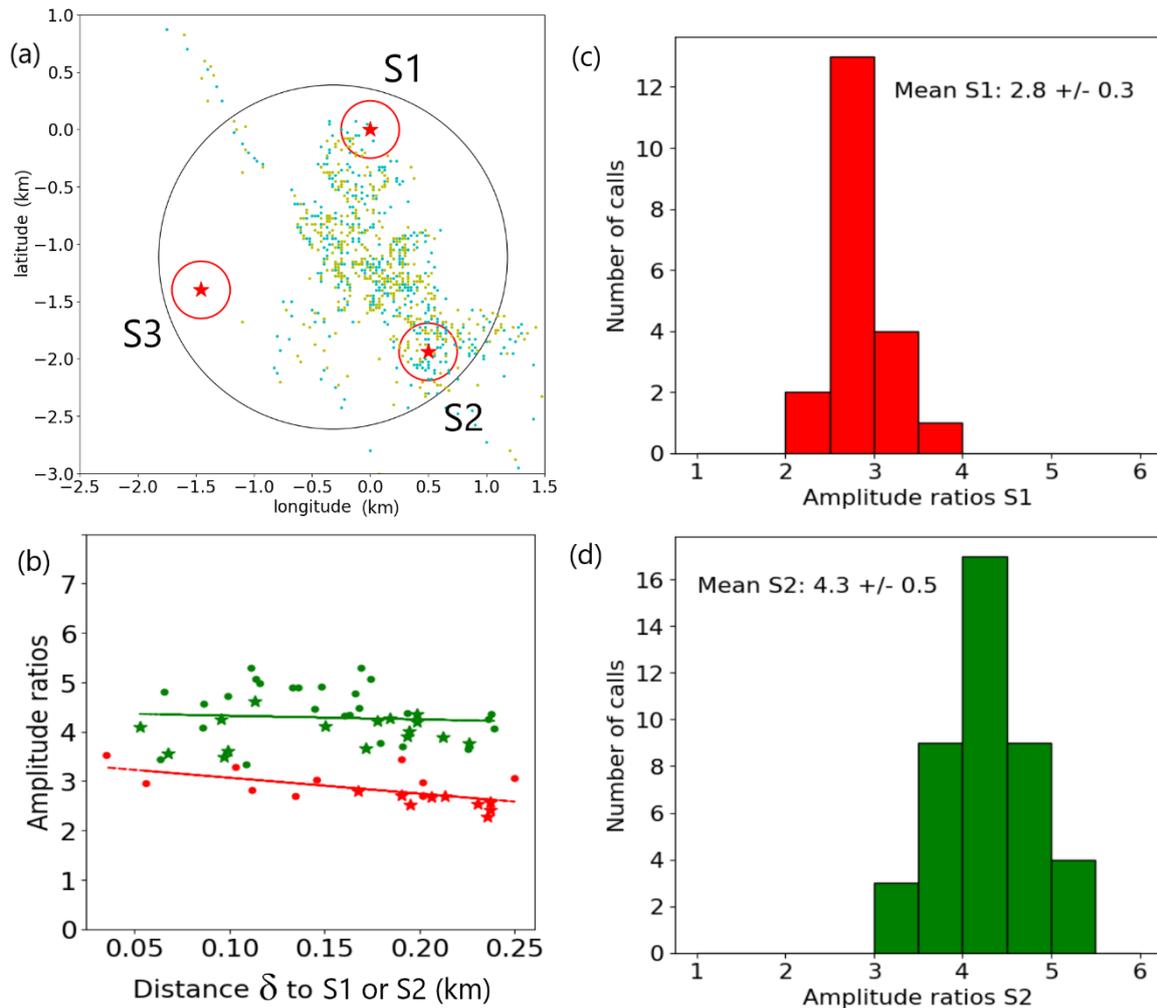


**Figure 10.** Spatial mapping of residuals  $a1/a2-d2/d1$  (a) and  $a1/a3-d3/d1$  (b). Note the higher amplitudes of the residuals in (b), which a plane sloping from the S1-S2 line towards S3 would fit.

Figure 10 shows a spatial mapping of the residuals. Figure 10a displays  $a1/a2-d2/d1$  with low absolute values of the residuals, slightly negative values around S1, and slightly positive values midway between S1 and S2. The  $a1/a3-d3/d1$  residuals show an apparent positive slope roughly from S3 to the S1-S2 line as illustrated by Figure 10b. A possible explanation for this discrepancy is given in the Discussion section.

### 3.2. Taking Advantage of Dense Coverage Close to S1 and S2 to Estimate Depths

The amplitude bias between S1 and S2 seems to be minimal, and therefore it should be possible to compare amplitudes of received calls with locations directly above the hydrophones. In that case, the distance to the closest hydrophone is the depth difference between the vocalization and the hydrophone. Assuming that the calls have the same source levels, and that the depth of the source is similar, the relative amplitudes  $a1/a2$  at S1 should be similar to the relative amplitudes  $a2/a1$  at S2. Figure 11a shows a map of call locations with a circle of 1.5 km in radius and circles of 250 m in radius around each of the three hydrophone locations.



**Figure 11.** (a) Map of all calls analyzed in the study. 597 A calls are in cyan, 600 B calls in yellow. The large circle is centered in the middle of the triplet and has a radius of 1.5 km. The small red circles are centered on each hydrophone and have a radius of 250 m. (b) Amplitude ratios  $a_1/a_2$  in red, and  $a_2/a_1$  in green, displayed as a function of distance for calls within 250 m of the hydrophones. (c) Histogram of the amplitude ratios  $a_1/a_2$  for calls close to S1. (d) Histogram of the amplitude ratios  $a_2/a_1$  for calls close to S2.

The relative ratios  $a_1/a_2$  are shown in red on Figure 11b for the calls within the 250 m circle at S1, and  $a_2/a_1$  are shown in green for the calls within the 250 m radius circle at S2, for a passage of the whale between 23:40 on the 19 February and 00:40 on the 20 February. The linear fit  $a_1/a_2 = 3.39 - 3.21 \delta$  with coefficient of determination  $r^2 = 0.37$  — extrapolates to a value of 3.39 at S1 and the linear fit  $a_1/a_2 = 4.40 - 0.75 \delta$  with coefficient of determination  $r^2 = 0.006$  — extrapolates to 4.40 at S2. A calls are marked as dots while B calls are marked as stars.

Using Equation (3) to determine the depth of the whale while above S1, we get the value of:

$$w_1 = 0.739 \pm \sqrt{\frac{4 - 0.74^2}{2.8^2 - 1}} = 0.739 \pm 0.711 \text{ km, when using the extrapolated value at } \delta=0 \text{ and the}$$

depth of hydrophones cited in [21]. Keeping the only solution above the hydrophone depth, the whale depth is estimated at 28 m when above S1. When the extrapolated value of 3.4 for the ratio is used, the corresponding whale depth is 167 m. A depth of 0 m for the whale at S1 would correspond to a ratio of 2.51.

When using Equation (2) with the values of hydrophone depths  $h_1 \neq h_2$  listed in [20] and the average value of  $r_1$  at S1:

$$w1 = \frac{0.742 - 2.8^2 \times 0.75}{1 - 2.8^2} \pm \sqrt{\frac{(0.75 - 2.8^2 \times 0.742)^2 - (1 - 2.8^2)(4 - 2.8^2 \times 0.742^2)}{(1 - 2.8^2)^2}} = 0.750 \pm 0.699 \text{ km}$$

Keeping the only solution above the depth of the hydrophones, the depth estimate is 51 m for this average value of the r1 ratio at S1. This illustrates the sensitivity of the estimate if the whale depths to the hydrophone depths using this method. Table 2 shows all the whale depth values for the two different sets of hydrophone coordinates and two different values of the r1 and r2 ratios. The first row for each hydrophone is the value of the average ratio, and the second is the value of the ratio when extrapolated directly above the hydrophone ( $\delta = 0$ ).

**Table 2.** Vocalization depths estimates when the whale is above S1 or S2.

Hydrophone	Amplitude ratios	h1 = 739 m	h1 = 750 m	h2 = 742 m
		h2 = 739 m		
S1	r1 = 2.8	w1 = 28 m	w1 = 51 m	
	r1 = 3.4	w1 = 167 m	w1 = 191 m	
S2	r2 = 4.3	w2 = 295 m	w2 = 284 m	
	r2 = 4.4	w2 = 305 m	w2 = 295 m	

These values are compatible with the range of depth of vocalization observed on tagged fin whales in the Southern California bight [16], which recorded a majority of shallow depth of less than 50 m, comparable with our estimate when the whale is above S1 when using the average ratio value, but up to 300 m, similar to our estimate when it is above S2. The estimates of depth using this method are more sensitive to the value of the amplitude ratio rather than the exact depth of the hydrophones.

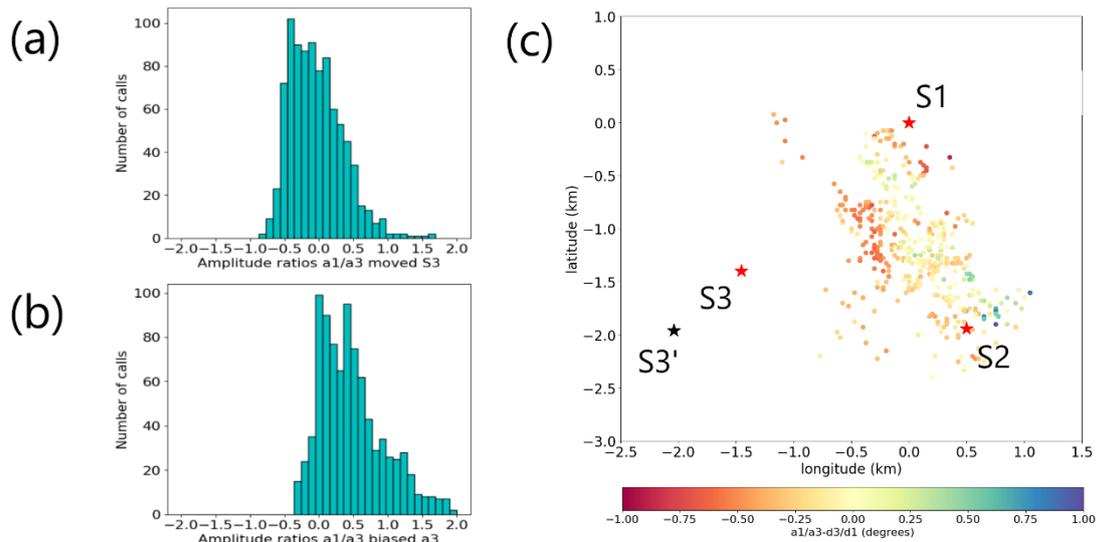
#### 4. Discussion

Waveforms originating from what is assumed to be vocalizing fin whales recorded on the IMS hydro acoustics station HA11S have been presented and analyzed to estimate optimal locations of the whales from the TDOAs between hydrophones. The waveforms recorded for each whale call on each hydrophone are rendered complex by the presence of the water surface reflection and multiple water bottom reflections when the whale is in the close vicinity of the triplet of hydrophones. This leads to issues with methods based purely on waveform cross-correlation such as the progressive multi-channel cross-correlation (PMCC) method [26], when the vocalization happens close to the hydrophone. Some reflections are as energetic as the first, direct arrival, causing confusion as to which peak in the cross-correlation functions are to be used. To counter this issue, a hybrid method was presented that avoids the ambiguity of pure cross-correlation methods yet takes advantage of its precise estimate of TDOAs. The measurement of amplitudes is likely affected by the multiplicity of the arrivals, and perhaps a more sophisticated method than the one used in this study could be used to pick the amplitude of the first arrival with confidence, rather than assuming it will be the highest value of amplitude within a six second segment.

The results presented in this paper regarding the depth of the vocalizations rely on the accuracy of the published depth of the hydrophones. It should be possible to extract the waveform of the source signal by assuming a spectral shape, pitch variation, and minimum phase for each of the A and B types of call, using wavelet deconvolution techniques from the seismic exploration industry [27]. Waveform modeling using a method that identifies individual arrivals, such as simple ray methods, should then become feasible, leading to estimations of the reflection coefficients, more exact whale depths estimates, and verification of the hydrophone depths.

It is likely that there are in fact differences of possibly up to a few tens of meters between the depths of the three hydrophones, as the mooring cable lengths were pre-established during deployment, but the exact water depth at which the hydrophones were dropped is likely to have deviated from the depth of the target locations, even though a very precise bathymetry was acquired before the deployment. The deployment of the hydrophones is a complex operation with a large

surface vessel trying to maintain position while kilometers long cable is deployed to the bottom of the ocean. Analysis of the amplitudes of the signals exploited in this work points to a possible need for either correcting the S3 location to a point further from S1 and S2. A possible explanation for the discrepancies observed in the residuals in Figure 10b is that the S3 hydrophone's position is not correct and that it is located further away from the S1-S2 line than the coordinates used in this study indicate. Testing this hypothesis for a point located as shown on Figure 12d as S3', it is found that the constant bias is indeed removed from the distribution for point S3' at coordinates (-2.04 km, -1.96 km, S3 hydrophone depth unchanged) on the S1-S3 line at a distance 1.4 times larger than the distance S1-S3.



**Figure 12.** (a) Histogram of the  $a_1/a_3 - d_3/d_1$  residuals with moved S3' (top). (b) Histogram of the  $a_1/a_3 - d_3/d_1$  residuals with original S3 (bottom). (c) Spatial mapping of residuals  $a_1/a_3 - d_3/d_1$  when S3 is moved to S3'.

The standard deviation of residuals after moving the location of S3 to S3' is higher than when a constant bias correction on S3 amplitudes is applied. One also has to keep in mind that the calculation of the vocalization locations itself depends on the location of S3, and that these locations have not been updated in this work before re-calculating the residuals.

Another possibility for the lack of consistency of the relative ratios of amplitudes and distances between S1 and S3 is that a calibration correction of the hydrophone at S3 is needed. A simple study of a large number of horizontally propagating signals recorded at the triplet should be able to confirm or infirm a calibration issue.

In analyzing the amplitude of the signals, the assumption was made that the source of sound is spherically symmetrical, with no azimuthally or vertically dependent radiation pattern. It may be possible, in a more refined analysis, to use the direction of motion of the whale as a substitute for the position of the animal and detect any variation in the strength of the signal depending on the position of the receiver with respect to the whale and its front to rear axis.

An inversion problem using both amplitudes and delay residuals to estimate potential corrections to the hydrophone locations may be possible if a very large number of calls are collected. It would be beneficial to search the data for additional similar sequences, providing better coverage especially close to the S3 hydrophone.

## 5. Conclusions

The sequence of calls studied in this work has a long duration and the tracks followed by the whale allow for good coverage of the area directly above the triplets. It was shown that using the amplitude ratios of the signal at two different hydrophones, when the source is in the near field, less than 1.5 km horizontally from the center of the triplet, can be of interest. The amplitude ratios between

S1 and S2 confirm that amplitudes follow the expected decay rule of being inversely proportional to the distance between source and receiver. This is however not the case for the amplitude ratios between S1 and S3. Several hypotheses may explain this, including that the relative location of S3 with respect to S1 and S2 needs to be corrected. Another possibility is that the amplitude radiation pattern of the calls is not isotropic, and there is a need to account for amplitudes decaying with the angle between the source-receiver line and the direction of propagation of the whale. Further collection of similar data with increased coverage may resolve which hypothesis explains the data best.

The estimated average swimming speed of the whale between A calls is  $9.45 \pm 7.05$  km/h, and  $9.57 \pm 8.04$  km/h between B calls. This is obtained when the cetacean is located less than 1.5 km from the center of the triplet, where locations and therefore distances swum are more accurately determined. The swim speed estimate is compatible with what is known about the maximum speed of 37 km/h (20 knots) for these cetaceans [3].

Given the very close relationship between the locations and relative amplitudes of A and B calls, it is expected that either the source of the calls is a single animal, at least in contiguous periods of time, or if they are from two distinct animals, their relationship must be quite symbiotic. A different conclusion was reached by the authors of [19], on very similar data from February 2019, also from HA11S. They concluded that A and B calls originated from two different animals. Our analysis could be repeated on the data set they used, with the addition of an analysis of the amplitudes in addition to the TDOAs and this will be the object of future work to attempt to resolve these differing interpretations.

According to [28], both triplets at HA11 were deployed around a seamount. It may not be a coincidence but rather directed by foraging around that seamount that initially, as shown on Figure 7, the whale appears to head towards the seamount and to slow down around it.

As a general conclusion amplitude may be a source of information additional to the travel times provided that sensor locations are estimated within a few meters and that more is known about the radiation pattern of the acoustic sources.

**Author Contributions:** Conceptualization, R.L. and P.N.; methodology, R.L.; software, R.L.; formal analysis, R.L.; data curation, R.L.; writing—original draft preparation, R.L.; writing—review and editing, P.N.; All authors have read and agreed to the published version of the manuscript.

**Funding:** This research received no external funding

**Data Availability Statement:** The data from IMS hydroacoustic station HA11 is openly available at the IRIS data center [18]. The data from HA01 as shown on Figure 1 can be obtained via the vDEC [25] mechanism of the CTBTO.

**Conflicts of Interest:** The authors declare no conflicts of interest.

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