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Article

Reactivity and Heavy Metal Adsorption Behaviour of Graphene Oxide Nanoparticle from First Principle Investigations: Case of Pb and Cd

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Abstract: Graphene oxide (GO) is considered as one of the promising adsorbents for the removal of various heavy metal contaminants in aquatic environment, due to its beneficial structural, chemical and electronic properties. Using the density functional theory (DFT) approach, we investigate the reactivity of a model GO nanoparticle ($C_{30}H_{14}O_{15}$) toward neutral and charged lead (Pb) and cadmium (Cd) atoms. We found the model metal-free GO to have a high chemical reactivity. To study the adsorption of the metal atoms on the GO nanoparticle, we have used a single and doubly-adsorbed neutral (Pb^0 and Cd^0) and charged (Pb^{2+} , Cd^{2+}) atoms. After identified possible adsorption sites on the GO, we found that a single charged metal ion binds more strongly than a neutral atom of the same type. To determine the possibility of multiple adsorptions of GO nanoparticle, two metal atoms of the same species are co-adsorbed on its surface. Our calculations reveals a site-dependent adsorption energy such that when two atoms of the same specie are adsorbed at sites S_i and S_j , the binding energy per atom depends on the whether one of the two atoms is adsorbed firstly on the S_i or S_j sites. It is also found that the binding energy per atom for two co-adsorbed atoms of the same specie is less than the binding energy of a singly-adsorbed atom which suggests that atoms may become less likely to be adsorbed on the GO nanoparticle when their concentrations increase. This applies to both neutral and charged atoms. We adduce the origin of this observation to be interplay between metal-metal interaction on the one hand and GO-metal on the other, with the former resulting in a less binding for the charged adsorbed metals in particular, due to repulsive interaction between two positively charged ions. The frontier molecular orbitals analysis and the calculated global reactivity descriptors of the respective GO-metal complexes revealed that all the GO-metal complexes have a smaller HOMO-LUMO gap (HLG) relative to that of pristine metal-free GO nanoparticle. This suggests that although the GO-metal complexes are stable, they are less stable compared to metal-free GO nanoparticles. The negative values of the chemical potentials obtained for all the GO-metal complexes further confirms their stability. Our work calculates parameters that will be crucial to rational design of GO nanoparticles for Pb and Cd ions contaminants removal, and may find application in water purification for example.

Keywords: graphene oxide; density functional theory; heavy metals; adsorption

1. Introduction

With the industrial revolution, the issues related to the management and control of mining waste have increased. These mining wastes, mainly heavy metals, constitute a real source of pollution to the ecosystem since they are not generally biodegradable [1]. Present in soils, waters and air, heavy metals can also be found in many uses such as paints, dyes, in some fertilizers, soaps as well in certain medicines [2]. Also, the bioaccumulation of metals such as Pb and Cd in the body is one of the causes

of carcinogenic, cardiovascular and kidney diseases, and can lead to death when absorbed in high concentrations [2,3].

Recent researches have indicated that two-dimensional nanomaterials containing oxygen, epoxy, hydroxyl, carboxylic groups [4] have a great potential for the adsorption of heavy metals [5–10]. In this context, graphene oxide (GO) nanoparticles have shown a great potential due to its high adsorption capacity, large surface area and solubility. It can also serve as an electrode material for monitoring contaminants [11]. They are hydrophilic in nature and have large negative charge surfaces that help to effectively remove cationic impurities such as heavy metal cations and cationic dyes by electrostatic interactions. Furthermore, due to their unique physico-chemical characteristics, they have the potential of becoming excellent adsorbents [12]. Indeed, Weijun *et al* have shown that GO nanoparticles can be superior adsorbents for the removal of heavy metal ions from water [13]. They can also act as excellent catalysts or further hybridize with effective catalysts to convert harmful gases and organic species in wastewater [14,15].

Recently, many experimental works have been carried out in the field of wastewater treatment [9,16,17]. These include the use of treatment techniques to remove heavy metal ions from wastewater such as chemical precipitation, membrane separation, ion exchange, electrochemical treatment as well metal adsorption, etc. Out of all these techniques, metal adsorption has been found to show remarkable effectiveness. Besides, due to its low cost, it is considered as a relatively cheap and fast approach for wastewater treatment. Also, to our knowledge, only a few theoretical works have been reported on this topic [13,18–20].

In this study, we use DFT calculations to investigate the structural and electronic properties of the GO nanoparticle from Ref. [21], having chemical the formula $C_{30}H_{14}O_{15}$, to heavy metals adsorption. Specifically, we consider the structural and electronic response of the nanoparticles to Cd and Pb in their neutral gas-phase, i.e., Pb^0 and Cd^0 respectively, as well as in their cationic state, i.e., Pb^{2+} and Cd^{2+} . We determine the active sites on the GO nanoparticle surface and the binding mechanisms underpinning metal adsorption. Furthermore, we provide deep insight into electronic interactions between the GO substrate and the adsorbed metal. The rest of the paper is organized as follows: In section II, we present the computational details and atomic models use in the study. Fundamental structural and electronic properties of the GO nanoparticle are then presented in section IIIA which are followed by adsorption and binding mechanism of Cd and Pb on GO as well as underlying electronic interactions (section IIIB).

2. Computational Details

All the results presented in this work have been obtained with the density function theory (DFT) as implemented in the Gaussian 16 package [22]. We used the B3LYP exchange-correlation functional with LANL2DZ basis set [23,24] and 6-31g for the calculation of GO vibrational frequencies. Figure 1(a) shows the atomic model of GO nanoparticle used in the study. It has the chemical formula $C_{30}H_{14}O_{15}$ and is made up of 59 atoms which also contains carboxylic ($-COOH$), alcohol ($-OH$) and epoxy ($-O-$) chemical groups. [21] In fact, the GO nanoparticle has to be constructed in such a way that the overall charge is zero by passivating the residual dangling bonds with H atoms. To simulate the metal-adsorption behaviour of GO nanoparticle, a metal atom in a gas-phase is placed on its most nucleophilic sites, which are denoted as S_1 and S_2 . Each Pb or Cd atom is placed about 2.0 Å above the GO surface. Such a separating distance is sufficient for metal atom to interact with the GO nanoparticle. Furthermore, the placement of the metal atom at the nucleophilic S_1 and S_2 sites is informed by the fact that they have the highest electrophilic condensed Fukui functions [25–28] as will be shown in the later section of this paper. It is worthwhile to state at this point that the condensed Fukui functions at a particular site, measures its chemical reactivity to an external perturbation. Three different types of condensed Fukui functions for a particular atom or site k have been defined, depending upon the type of electron transfer,

$$f_k^+(\mathbf{r}) = \rho_{N+1}(\mathbf{r}) - \rho_N(\mathbf{r}) \text{ for nucleophilic attack,} \quad (1)$$

$$f_k^-(\mathbf{r}) = \rho_N(\mathbf{r}) - \rho_{N-1}(\mathbf{r}) \text{ for electrophilic attack,} \quad (2)$$

$$f_k^0(\mathbf{r}) = \frac{1}{2}(\rho_{N+1}(\mathbf{r}) - \rho_{N-1}(\mathbf{r})) \text{ for radical attack,} \quad (3)$$

where $\rho_{N+1}(\mathbf{r})$, $\rho_{N-1}(\mathbf{r})$ and $\rho_N(\mathbf{r})$ are the gross electronic population of the atom or site k , calculated from the +1, -1 and 0 charged molecule. It should be noted that, the greater the value of condensed Fukui function, the more reactive is the particular atomic site in the molecule [27].

Three separate models of metal-adsorbed GO have been considered. These are named as GO-M/S₁, GO-M/S₂ and GO-2M/S₁S₂. In the model termed as GO-M/S₁, a single metal atom M is adsorbed on the S₁ site (Figure 1(a)) while S₂ is the adsorption site of M in the model GO-M/S₂ (Figure 1(b)). In the case of GO-2M/S₁S₂, two metal atoms of the same type occupy the adsorption sites S₁ and S₂ (Figure 1(c)). The structural model of GO-2M/S₁S₂ enables us to determine if metal atoms can be co-adsorbed at the two adsorption sites. To determine the minimum energy configuration for each of the three models, GO with neutral metal atoms of Pb⁰ and Cd⁰ as well as GO with metal cations of Pb²⁺ and Cd²⁺, each attached at their respective sites were optimized. The chemical stability and reactivity were determined through the global reactivity descriptors, using the frontier molecular orbitals which are the HOMO (*Highest Occupied Molecular Orbital*) and LUMO (*Lowest Unoccupied Molecular Orbital*) with the Koopmans theorem [29]:

$$E_g = E_{\text{LUMO}} - E_{\text{HOMO}}, \quad (4)$$

$$\mu = \frac{E_{\text{LUMO}} + E_{\text{HOMO}}}{2}, \quad (5)$$

$$\eta = \frac{E_{\text{LUMO}} - E_{\text{HOMO}}}{2}, \quad (6)$$

$$\omega = \frac{\mu^2}{2\eta}, \quad (7)$$

where E_g , μ , η and ω are defined as the HOMO-LUMO gap (HLG), chemical potential, chemical hardness and global electrophilicity index, respectively. It has been demonstrated that, a high HOMO energy corresponds to a more reactive molecule in the reactions with electrophiles, while a low LUMO energy favors molecular reactions with nucleophiles [30,31]. Note that a large HOMO-LUMO gap implies high kinetic stability and low chemical reactivity because it is energetically unfavorable to add electrons to a high-lying LUMO or to extract electrons from a low-lying HOMO [28,32–36]. A negative chemical potential suggests that a chemical compound or an atomic system is stable and will not decompose spontaneously into its constituent elements [37,38]. The chemical hardness may be interpreted as a measure of resistance toward the deformation of electron cloud of a chemical system under small perturbations encountered during chemical process. The global electrophilicity index is related to the ability of an electrophile to acquire additional electronic charge and the resistance to exchange electronic charge with the environment [31,39,40].

Following the energy minimization process, we calculated the binding energies per metal atom on the metal-free GO as well as the GO-metal complexes as:

$$E_b = \frac{1}{n}(E_{n-1} + n \times E_a - E_n), \quad n = 1, 2, \dots \quad (8)$$

where E_n and E_{n-1} are the minimum energies of GO nanoparticles having n and $n - 1$ numbers of adsorbed metal atoms respectively, while E_a is the total energy of the isolated metal. In this convention, the positive value of E_b means the adsorption process is favorable. Moreover, for a binding energy

lower than 0.5 eV, the adsorbate (i.e, the metal atom) is generally considered to be physisorbed on the adsorbent. A higher binding energy indicates chemisorption [41]. Finally, to confirm that the optimized GO system is in the minimum energy configuration, which is chemically stable, we performed vibrational frequency calculations. It has to be noticed that, imaginary frequencies in the vibrational modes will indicate an unstable molecule.

3. results and discussion

3.1. Stability and reactivity of GO nanoparticle

The molecule $C_{30}H_{14}O_{15}$ composed of 59 atoms has 174 normal modes of vibration. Depending on whether the vibration modes are given by the formula $3N-6$ (N :number of atoms). The results of the frequency calculation have revealed no imaginary frequency, so we can deduce that our GO is stable see supplementary information. Also, we have found that the paramagnetic ground-state is the preferred magnetic state for the GO nanoparticle, a result which is consistent with previous experimental and theoretical investigations of GO nanoparticles [42]. Also, we have found that the paramagnetic ground-state is the preferred magnetic state for the GO nanoparticle, a result which is consistent with previous experimental and theoretical investigations of GO nanoparticles [42].

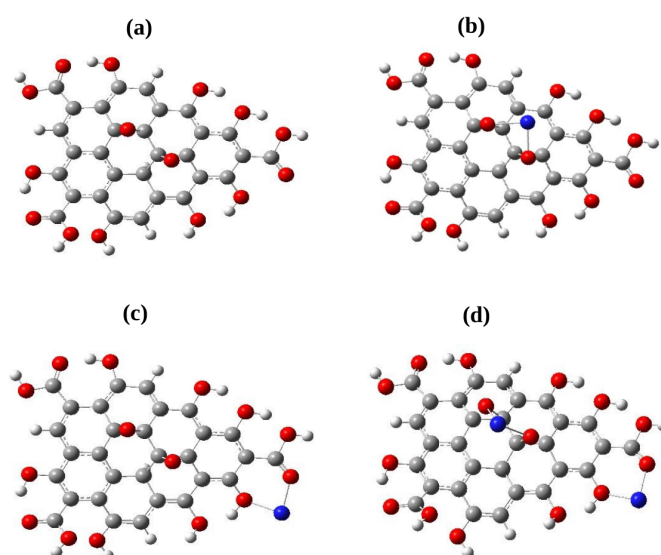


Figure 1. (a) Graphene oxide nanoparticle (GO), (b) GO nanoparticle with the metal atom adsorbed at the S_1 site, i.e., GO-M/ S_1 model, (c) GO nanoparticle with the metal atom adsorbed at the S_2 site, i.e., GO-M/ S_2 model, (d) GO-2M/ S_1S_2 model where two metal atoms are co-adsorbed at the S_1 and S_2 sites. In each of the models, $M = Pb^0, Cd^0, Pb^{2+}$ and Cd^{2+} . Carbon, hydrogen, oxygen and metal atoms are represented as gray, white, red and blue spheres.

Table 2 shows our calculated values for the LUMO-HOMO gap (E_g), chemical potential (μ), chemical hardness (η), and global electrophilicity index (ω). The HOMO–LUMO gap is found to be about 1.61 eV. It should be noted that, chemical systems with large E_g are hard and much less polarizable compared to systems with small E_g . A HOMO–LUMO gap (HLG) greater than 1.0 eV may be considered large [43]. Therefore, our model GO nanoparticle of relatively high E_g can be considered to have a high chemical stability and chemical hardness, and thus will be less polarizable. Its electron cloud will be resistive to small perturbations which will result in low chemical reactivity [31]. The chemical potentials (η) is found to be -4.37 eV. This negative η also suggests that the GO nanoparticle is stable and does not undergo decomposition into elements. The chemical hardness of about 0.805 eV may be large enough to consider the GO nanoparticle relatively resistant toward the deformation of its electron clouds under small perturbations, which is further affirmed by the relatively high E_g ,

i.e., greater than 1.0 eV. The global electrophilicity index of about 11.872 eV, which is small enough to consider that the GO nanoparticle may be subject to electrophilic attacks.

In order to map out nucleophilic sites onto the GO nanoparticle, we plot the molecular electrostatic potential (MEP) isosurface. The plot is displayed in Figure 2. The figure shows variation in the electron density in the GO nanoparticle. The blue colored regions for example, show low electronic densities while white colored regions indicate medium electronic densities. The orange colored regions indicate high electron densities and may be considered as nucleophilic sites, and are thus potential sites for electrophilic attacks.

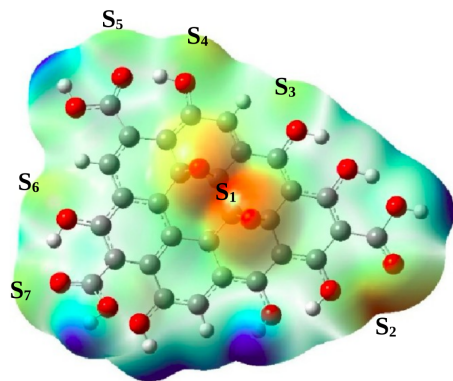


Figure 2. Molecular electrostatic potential (MEP) isosurfaces of the GO nanoparticle. The blue color indicates low electronic density, the white color indicates medium electronic density, and the orange color indicates high electron density region. S₁, S₂, S₃, S₄, S₅, S₆ and S₇ are the most prominent sites for electrophilic attacks.

Also, Figure 2 clearly shows that the most prominent nucleophilic sites are mainly localized around epoxy groups (site S₁), and the vicinity of carboxylic and alcohol groups (sites S₂, S₃, S₄, S₅, S₆, S₇). For a better understanding of local reactivity properties, we calculated the condensed dual descriptors of atoms localized at the potential nucleophilic sites, defined as $f_k^{(2)}(\mathbf{r}) = f_k^+(\mathbf{r}) - f_k^-(\mathbf{r})$. The negative value of $f^{(2)}(\mathbf{r})$ indicates the site is favoured for an electrophilic attack while the positive value indicates that the site may be favorable for a nucleophilic attack [25–28]. The calculated values of $f_k^{(2)}(\mathbf{r})$ are presented in Table 1, where we have demonstrated the variation of Fukui function values in the molecule by choosing the corresponding values for the sites S_k (k = 1-7). Here, S_k (k = 1-6) have negative condensed dual descriptors while the site S₇ has a positive condensed dual descriptor. The latter indicates that the electrophilicity of the site S₇ prevails over its nucleophilicity, which may be explained by the proximity with a highly electrophilic site as shown by the MEP isosurface. Furthermore, the ranking of the electrophilic Fukui condensed functions of potential nucleophilic sites is as follows : $f_1^-(\mathbf{r}) > f_2^-(\mathbf{r}) > f_4^-(\mathbf{r}) > f_3^-(\mathbf{r}) > f_6^-(\mathbf{r}) > f_5^-(\mathbf{r}) > f_7^-(\mathbf{r})$. This clearly suggests that the site S₁ has higher ability to attract electrophilic ions, followed by the site S₂. For this reason, the following section will be devoted to the adsorption behaviour of both sites S₁ and S₂.

Table 1. Nucleophilic $f_k^+(\mathbf{r})$ and electrophilic $f_k^-(\mathbf{r})$ condensed Fukui functions, and the condensed dual descriptor $f_k^{(2)}(\mathbf{r})$ for different adsorption sites onto the free GO nanoparticle.

Structure	Site	$f_k^-(\mathbf{r})$	$f_k^+(\mathbf{r})$	$f_k^{(2)}(\mathbf{r})$
GO	S ₁	0.112	0.005	−0.106
	S ₂	0.087	0.051	−0.036
	S ₃	0.043	0.007	−0.036
	S ₄	0.053	0.012	−0.041
	S ₅	0.034	0.020	−0.014
	S ₆	0.036	−0.002	−0.038
	S ₇	0.027	0.028	0.001

3.2. Adsorption of Pb and Cd

To determined the stability of metal at the various sites, we calculated the binding energy E_b^i ($i = 1, 2$) of adsorbed metal on the sites S_1 and S_2 of GO nanoparticle using the relaxed minimum energy structures of GO-M complexes. The resulting values are presented in Table 2. For a single metal adsorption, the E_b^i is positive in all the cases, which indicates that the adsorption of a single Cd or Pb as a neutral atom or in ionic form is stable. Also, to be noted from the table is that, the Pb^0 adsorption at the S_1 and S_2 sites of GO nanoparticle leads to a chemisorption with $E_b^1 = 5.93$ eV and $E_b^2 = 2.54$ eV respectively. These are much stronger adsorption compared to Cd^0 , which is also chemisorbed at the S_1 site with a much lower binding energy of $E_b^1 = 1.55$ eV, but physisorbed at the S_2 site with $E_b^2 = 0.06$ eV. Our results are in agreement with theoretical investigations conducted by Sara M. Elgengehi et al [20] in the case of graphene and GO as adsorbents for Cd and Pb heavy metals. They also found the same trend, namely, neutral Pb atom absorbs strongly than Cd.

Table 2. HOMO-LUMO gap (E_g), chemical potential (μ), chemical hardness (η) and global electrophilicity index (ω) of GO nanoparticle and GO-M complexes ($M = Pb^0, Cd^0$). Mulliken charge transfers δQ_i for the metal atom adsorbed at the site S_i ($i = 1, 2$). E_b^i is the adsorption energy per metal atom adsorbed on the GO nanoparticle. Similarly, E_b^{ij} ($(i, j) = (1, 2), (2, 1)$) represents the binding energy per adsorbed metal atom when two atoms are co-adsorbed in such a way that the first atom is adsorbed at the S_i prior to the adsorption of a second atom at S_j site. In other words, a metal atom pre-exists at the S_i before the second atom is adsorbed S_j .

Site	Structure	E_g (eV)	μ (eV)	η (eV)	ω (eV)	δQ_i	E_b^i (eV)	E_b^{ij} (eV)
	GO	1.61	−4.37	0.81	11.87	—	—	—
S_1	GO-Pb ⁰	0.30	−3.62	0.15	44.17	0.99	5.93	3.11
	GO-Cd ⁰	0.89	−4.30	0.45	20.76	0.76	1.55	1.08
	GO-Pb ²⁺	1.08	−10.42	0.54	100.68	−0.86	12.34	1.31
	GO-Cd ²⁺	0.96	−10.33	0.48	110.99	−0.90	12.18	1.16
S_2	GO-Pb ⁰	1.23	−3.63	0.613	10.77	0.60	2.54	1.42
	GO-Cd ⁰	1.34	−4.34	0.68	13.89	−0.04	0.06	0.04
	GO-Pb ²⁺	0.82	−9.96	0.41	121.52	−0.71	8.97	−0.37
	GO-Cd ²⁺	0.61	−10.26	0.31	172.20	−1.27	10.22	0.18

The aforementioned results can be related to Mulliken charge transfer between the GO nanoparticle and the adsorbed metal [44]. Table 2 presents different values of δQ_i (where i is the site index), defined as the Muliken charge difference between the electronic charge on the metal before and after adosorption on the GO surface. According to our definition, a negative value of δQ_i implies that the metal adsorbate loses charges to the GO surface while the positive value corresponds to a gain of electronic charges by the metal. We calculated a higher charge transfers from Pb^0 to the GO nanoparticle ($\delta Q_1 = -0.99e^-$ and $\delta Q_2 = -0.60e^-$) compared to those occurring from Cd^0 ($\delta Q_1 = -0.76e^-$ and $\delta Q_2 = 0.04e^-$), for the S_1 and S_2 sites respectively. Thus, neutral Pb^0 at the S_1 and S_2 sites act as electron donors while Cd^0 at the S_2 acts as electron acceptor. Interestingly, Cd^0 with a positive δQ has the lowest binding energy of all the single neutral metal atoms considered. Furthermore, the difference in charge transfers between Pb^0 and Cd^0 can be understood through the difference between their ionization energies (IE) [45–47]. Neutral Pb and Cd has IE of 7.42 eV and 8.99 eV respectively [46]. Thus, it is easier to extract electronic charge from Pb^0 compared to Cd^0 due to the former’s lower IE. Hence, Pb^0 transfers electrons more easily than Cd^0 to GO nanoparticle. Indeed, similar trend in IE

and charge transfer were obtained via first-principle investigations of adsorption properties of toxic heavy metals (i.e., Cd, Hg, Pb) on graphene quantum dots and infinite graphene structure [48].

We also calculated the harmonic vibration frequencies of both GO and GO-M with M being adsorbed on S_1 and S_2 sites. The results show that both GO and GO-M are stable, while the vibration frequencies range from 25.8716 cm^{-1} to 3694.89 cm^{-1} for GO nanoparticle and 19.6641 cm^{-1} to 3722.71 cm^{-1} , 24.8106 cm^{-1} to 3719.83 cm^{-1} respectively for GO-Pb⁰ and GO-Cd⁰ concerning the adsorption on the site S_1 , and from 15.9952 cm^{-1} to 3709.68 cm^{-1} and 15.0921 cm^{-1} to 3711.59 cm^{-1} for GO-Pb⁰ and GO-Cd⁰ concerning the site S_2 (see supplementary information for more details).

The adsorption of a single cationic adsorbate Pb²⁺ or Cd²⁺ at the S_1 and S_2 sites leads to a stronger chemisorption compared to those of a single neutral atoms (see Table 2). The binding energies of a single Pb²⁺ on the S_1 and S_2 sites are $E_b^1 = 12.34\text{ eV}$ and $E_b^2 = 8.97\text{ eV}$ respectively. Also, Cd²⁺ is adsorbed with $E_b^1 = 12.18\text{ eV}$ and $E_b^2 = 10.22\text{ eV}$ at the S_1 and S_2 sites respectively. These binding energies are order of magnitude higher than those obtained for corresponding neutral Pb⁰ and Cd⁰ adsorptions as shown in the Table 2. In general, charged metal ions, irrespective of the adsorption sites, binds more strongly compared to neutral atom of the same type. This result is in agreement with previous findings by Shtepliuk *et al* [48].

Muliken charge analysis shows a positive charge transfer, i.e., positive δQ , and thus electron transfer from the GO to the cations. Thus, each of Pb²⁺ and Cd²⁺ cations act as an electron acceptor from the GO nanoparticle. Therefore, positively charged ions reverse the direction of charge transfer compared to the charge-donating neutral atoms which is consistent with previously reported results by Shtepliuk *et al* [48].

We also investigated the adsorption of two neutral or charged Pb or Cd atoms on the S_1 and S_2 sites. Only co-adsorption of atoms of the same species are considered. Thus, we examined two models of adsorption which are the following : (i) The first metal atom pre-exists at the the S_1 site while the second atom adsorption occurs on the site S_2 . Here, the binding energy of doubly-adsorbed Pb or Cd is termed $E_b^{ij} \{(i, j) = (1, 2)\}$, where $(i, j) = (1, 2)$ indicates that metal atom pre-exists at site S_1 before the adsorption of another atom of the same specie occurs at S_2 ; (ii) The second adsorption occurs on the S_1 site while the first one pre-exists on the S_2 site. In this case, the binding energy of doubly-adsorbed Pb or Cd is termed $E_b^{ij} \{(i, j) = (2, 1)\}$ where $(i, j) = (2, 1)$ indicate that metal atom pre-exists at site S_2 before the adsorption of another atom occurs at S_1 . These binding energies per atom (E_b^{ij}) are presented in the last column of Table 2. If these are compared to the binding energies of a singly adsorbed metal atoms (E_b^i), it is clear that the atoms becomes less binded to the GO nanoparticle with increasing number of adsorbed atoms. As an example, for a single Pb⁰ adsorption, $E_b^i = 5.93\text{ eV}$ where for a doubly adsorbed atom of the same specie, $E_b^{ij} = 3.11\text{ eV}$. The same trend can be observed for all the metals, neutral or charged. In the case of Pb²⁺ ion, the binding energy per atom becomes negative (i.e, an unstable configuration or desorption) when the two charged ions are are co-adsorbed. Another observation from Table 2 is that the magnitude of $E_b^{1,2}$ is not the same as $E_b^{2,1}$. In all cases (for neutral and cations atoms adsorption) $E_b^{2,1}$ is larger than $E_b^{1,2}$. For example, $E_b^{2,1} = 3.11\text{ eV}$ for Pb⁰ while $E_b^{1,2} = 1.42\text{ eV}$ for the same atom specie. Similar trend is observed for all the atoms as show in Table 2. Thus, when a metal atom is initially adsorbed at the S_2 site, it attracts and binds more strongly an atom of the same specie at the S_1 site. In this case, the co-adsorption is thus energetically more favoured. However, when a metal atom is initially adsorbed at the S_1 site, the second atom adsorbed on the S_2 site experiences less binding. In actual fact, the co-adsorption may not be energetically favoured (that is, an unstable co-adsorption or desorption) as shown in the case of Pb²⁺ where $E_b^{2,1}$ is positive , i.e., 1.31 eV whereas $E_b^{1,2}$ is negative, i.e., -0.37 eV . Thus, the lattice site of a pre-exisitng or an adsorbed metal atom on GO has strong influence on subsequent binding or attraction of another atom of the same specie.

Furthermore, in order to gain deeper insight into the electronic origin of stability of adsorbed metal atoms on the GO nanoparticle, we performed frontier molecular orbitals analysis and calculated the global reactivity descriptors of the respective complexes (see Table 2). We found that the HLG

of all GO-M complexes are smaller than that of pristine metal-free GO nanoparticle, which suggests that when GO adsorbs metal, the GO-M complexes are still energetically stable, although less stable compared to metal-free GO. Also, the lower HLG of GO-M complexes indicates that they are chemically soft, more polarized and have higher chemical reactivity compared to the GO nanoparticle. However, we found the chemical potentials to be negative for all the metal adsorption on both the S_1 and S_2 sites, suggesting that the resulting complexes are stable and may not spontaneously decompose into separate metal ions and GO nanoparticle. Also, the chemical hardness of GO-metal complexes are smaller relative to that of pure GO, which indicates that GO-metal complexes are less resistant toward the deformation of their electron clouds under small perturbations. Furthermore, metal adsorption on GO leads to a higher global electrophilicity indexes compared to that of metal-free GO nanoparticle. This indicates the reduction of nucleophilic character of GO nanoparticle following metal adsorptions.

Based on the analyses of the binding energy and frontier molecular orbitals, we conclude that in general, multiple adsorption of metal atoms on GO is favoured, i.e., preponderance of positive binding energy for the co-adsorbed atom. However, as the number or concentration of adsorbed atom increases, the metal atom becomes less bonded to the GO. Such a behaviour, in the case of charged ions in particular may be rationalized as due to repulsive interaction between atoms of the same charge type, i.e., positive charge Cd^0 and Pb^0 ions. Indeed, Shtepliuk postulated that the competition between metal-metal interaction on the one hand and that of GO-metal on the other [48] is the origin of less binding experienced by multiple metal atoms when adsorbed on the GO nanoparticle. This important observation will be useful to evaluate the adsorption and retention of ions capability of GO nanoparticle as a medium to sequester heavy metal cations, in particular, those investigated in this work.

4. Summary and Conclusions

Density-functional theory (DFT) calculations were employed to investigate the reactivity and interaction of a graphene oxide (GO) nanoparticle with neutral metal atoms Pb^0 and Cd^0 as well as charged ions Pb^{2+} and Cd^{2+} ions. Binding energy and global reactivity descriptors such as HOMO-LUMO gap (HLG) chemical potential (μ), chemical hardness (η) and global electrophilicity index (ω) were used to characterize the interaction and reactivity of the metal atoms with the GO nanoparticle. We demonstrated that our model GO nanoparticle is stable and has high chemical reactivity. We identified seven potential nucleophilic sites on the GO nanoparticle, however only two of these were selected due to their greater occurrences, to study the adsorption of metal atoms. Using a single and doubly-adsorbed neutral and charged metal atoms on GO as our model of GO-metal complexes, we found that the adsorption characteristics of charged metal ions, i.e., Pb^{2+} and Cd^{2+} differs significantly from those of neutral atoms Pb^0 and Cd^0 . Firstly, we found that charged metal ions bind more strongly than a neutral atoms of the same specie for single adsorptions. Also, we investigated the adsorption and binding capability of GO nanoparticles by considering model systems consisting of two Pb or Cd in a neutral or charged atoms. Only co-adsorption of atoms of the same type have been considered. We found site-dependency of the adsorption energy. Specifically, the binding energy of one atom at a nucleophilic site S_i when one other atom of the same specie is adsorbed firstly at another site S_j , differs significantly to the binding energy of the same atom when the adsorption order on the two sites is reversed. Furthermore, it was observed that the binding energy per atom for two co-adsorbed atoms of the same specie is less than the binding energy of a singly-adsorbed atom. This may suggest that with increasing number or concentration of the adsorbed atoms, they become less likely to be adsorbed on the GO surface. The observed behaviour may be ascribed to the metal-metal interaction in one hand and GO-metal on the other. The former, in particular, may result in less binding for the charged metal system due to repulsive interaction between two positively charged ions. Furthermore, we performed frontier molecular orbitals analysis and calculated the global reactivity descriptors of the respective GO-metal complexes in order to gain deeper insight into the electronic origin of their stability. Our analyses revealed that all the GO-metal complexes have smaller HLG relative to that of

pristine metal-free GO nanoparticle, which indicates that although the GO-metal complexes are stable, they are less stable compared to metal-free GO nanoparticles. Furthermore, we found the chemical potentials to be negative for all the studied GO-metal complexes, which confirms their stability. Our work provides a basis for rational design of GO for harmful metal ions capturing which may be important in water purification when these are present as water pollutants.

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