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Posted Date: 24 October 2024

doi: 10.20944/preprints202410.1798.v1

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## Article

# Synthetic Jet Actuators for Active Flow Control: A Review

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**Abstract:** A synthetic jet actuator (SJA) is a fluidic device often consisting of a vibrating diaphragm that alters the volume of a cavity to produce a synthesized jet through an orifice. The cyclic ingestion and expulsion of the working fluid leads to a zero-net mass-flux and the transfer of linear momentum to the working fluid over an actuation cycle, leaving a train of vortex structures propagating away from the orifice. SJAs are a promising technology for flow control applications due to their unique features, such as no external fluid supply or ducting requirements, short response time, low weight, and compactness. Hence, they have been the focus of many research studies over the past few decades. Despite these advantages, implementing an effective control scheme using SJAs is quite challenging due to the large parameter space involving several geometrical and operational variables. This article aims to explain the working mechanism of SJAs and provide a comprehensive review of the effects of SJA design parameters in quiescent conditions and crossflow.

**Keywords:** synthetic jet actuators; flow control; boundary layer control; micro-fluidic device; flow separation

## 1. Introduction

Synthetic jet actuators enhance flow mixing, control turbulence, and manage separation in fluid systems. In aerospace, these devices offer the potential for boundary layer control on aircraft wings, directly impacting flight efficiency and safety [1]. Flow separation can be described as the breakaway or detachment of the boundary layer from its bounding surface, often leading to a significant decline in the efficiency and performance of fluid systems [2]. Flatt [3] defined the term boundary layer control (BLC) as any mechanism or process through which the boundary layer is caused to behave differently than it usually would. However, flow control can generally be described as an attempt to drive the character or disposition of a flow field through flow control devices to a more favorable one [1,4]. To put this definition in context, consider the flow separation phenomenon, commonly regarded as detrimental. Control devices, such as flaps and slats, delay flow separation on a commercial aircraft's wing, reducing drag and improving lift. However, in some cases, inducing separation can be advantageous, such as when spoilers are used to minimize ground-effect lift during landing [2].

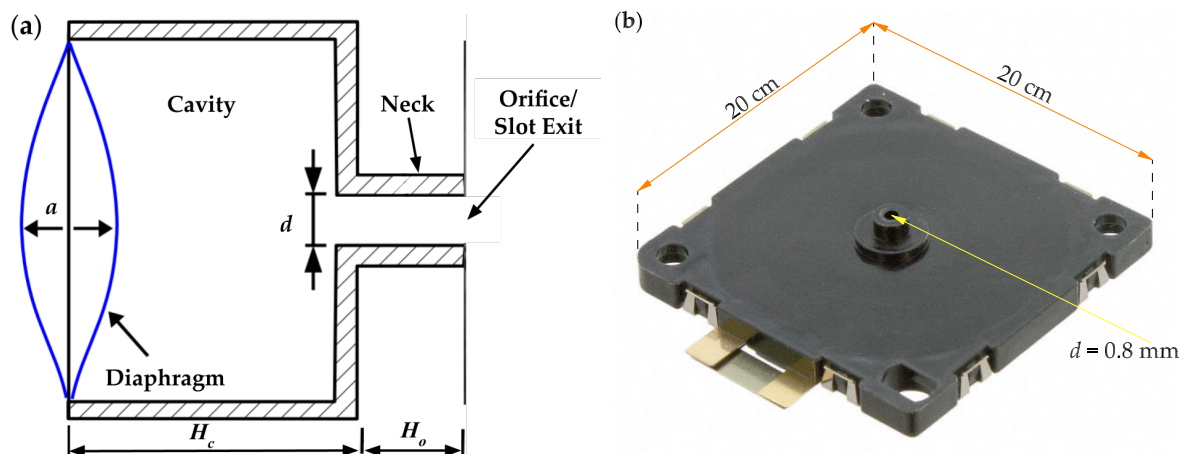
Flow control devices are categorized into two main types: passive and active. Passive devices, such as vortex generators on commercial aircraft wings, function without external energy input by leveraging the flow's inherent characteristics through geometric modifications. In contrast, active flow control (AFC) devices require energy input, typically adding momentum to the flow [5]. This fundamental distinction in energy requirements defines their operational principles and applications in fluid dynamics. Despite requiring input power, AFC devices may be advantageous as they adapt to off-design flow conditions, do not introduce a drag penalty common with passive control devices, or restore aerodynamic performance when passive devices fail [6,7]. AFC can be used in various

applications, such as increasing lift and reducing drag, enhancing mixing for more efficient combustion, aeroacoustic noise attenuation, and vibration reduction [8–10]. Traditional active control devices are operated based on the injection or removal of fluid from the control surface. Suction was the first method ever proposed for separation control to deflect the high-momentum freestream flow towards the surface by removing decelerated fluid near it [11]. Alternatively, steady blowing can be employed to add momentum directly to the retarded boundary layer near the surface and delay flow separation [12]. In general, the steady blowing and suction devices increase the mechanical complexity and weight of the system. Therefore, aerodynamic gains made by these techniques may not counterbalance the power required to operate the suction or blowing devices [13]. Instead of a steady momentum addition, modern AFC devices rely on excitation, often regarded as an oscillatory momentum addition. The periodic addition of momentum can achieve the same level of control authority as traditional steady methods with one primary advantage: the momentum input required is lower, ranging from factors to even orders of magnitude [14]. Furthermore, it is feasible for flight vehicles. Recent studies have shown that periodic flow control can be more effective than steady methods for a given momentum input [15–17]. Although there have been some attempts to deploy AFC in real-world scale models [18–21], most applications of AFC remain experimental and confined to laboratory settings, which is also a testament to the challenges involved in designing and implementing AFC systems.

Excitation can be achieved through various means, such as acoustic drivers [22–27] or hydrodynamic devices [28–31]. The present review paper focuses on hydrodynamic excitation, primarily by synthetic jet actuators. A synthetic jet actuator (SJA) is a device often consisting of a vibrating diaphragm or piston that alters the fluid volume within a cavity to eject a quasi-steady jet through an orifice. An actuator is a device, such as a vibrating diaphragm, capable of generating oscillatory momentum. A comprehensive review on actuators has been carried out by Cattafesta and Sheplak [32]. A fluidic jet is a high-momentum stream of fluid ejected from a nozzle, aperture, orifice into the surrounding medium. By definition, a steady jet has negligible temporal variations. A pulsed jet, however, is an unsteady jet that alternates between being fully on or off and can be generated through various methods, such as using a fast-acting solenoid valve or a rotating orifice assembly [31,33]. However, unlike pulsed jets, synthetic jets are formed entirely from the working fluid within the flow system where they are employed. As a result, they can transfer momentum to the flow system without injecting any net mass-flux across the flow boundary [34], and thereby sometimes referred to as zero mass blowing (ZMB) or zero-net mass-flux (ZNMF) jets. SJAs have become more prevalent in the past few decades as a technology for AFC applications as they require no external fluid supply or ducting [34–36]. This feature alone significantly reduces the mechanical complexity and weight of the flow control system. Additionally, SJAs are easy to miniaturize through microfabrication [37–39], allowing them to be seamlessly integrated into the flow surface.

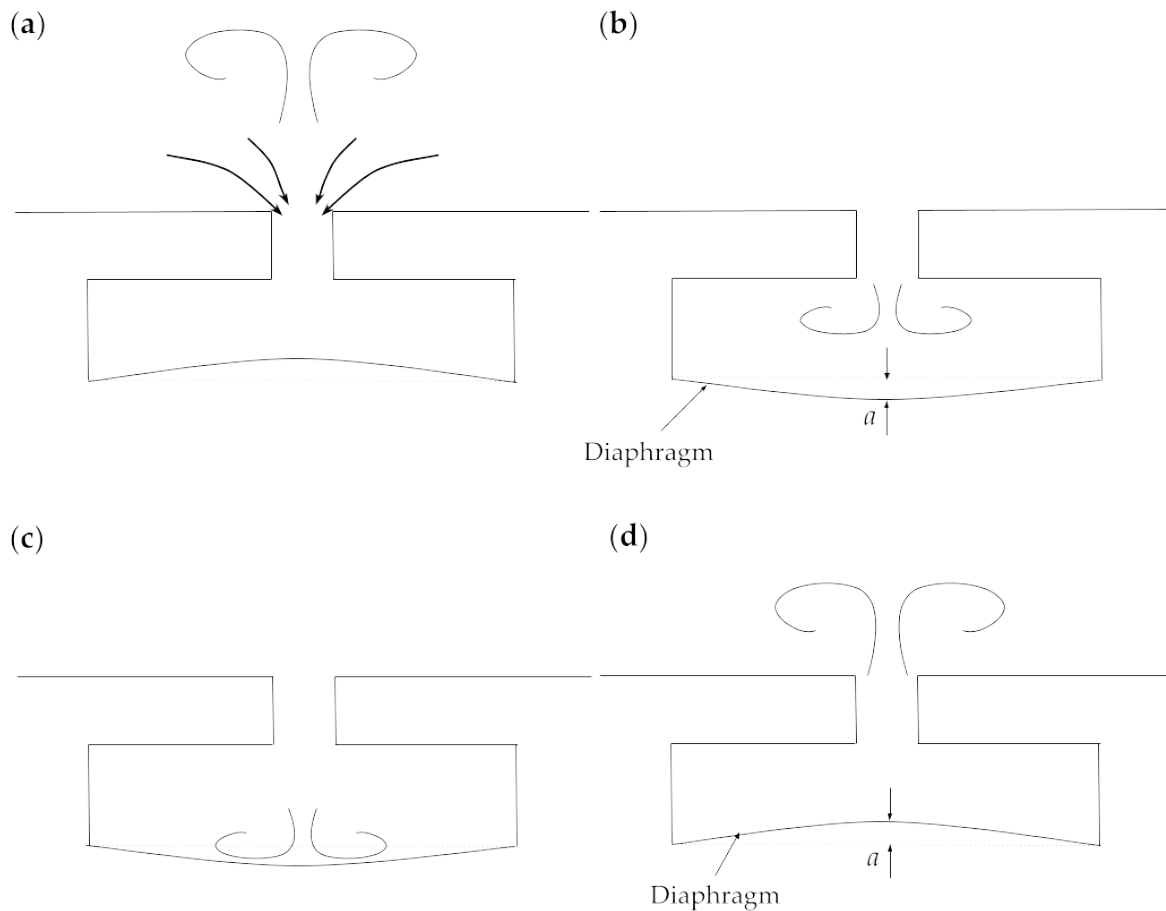
## 2. SJA Mechanism

A schematic drawing and photograph of an SJA are displayed in Figure 1. Although a variety of devices, such as mechanical pistons [29,40–44] and speakers [45–47], have been used as an actuator, the classical SJA comprises a vibrating diaphragm with an amplitude  $a$  located at the base of a cavity with a height of  $H_c$ . A neck with height  $H_o$  and diameter  $d$  connects the cavity to an exit (either an orifice or a jet slot) on the controlled surface.



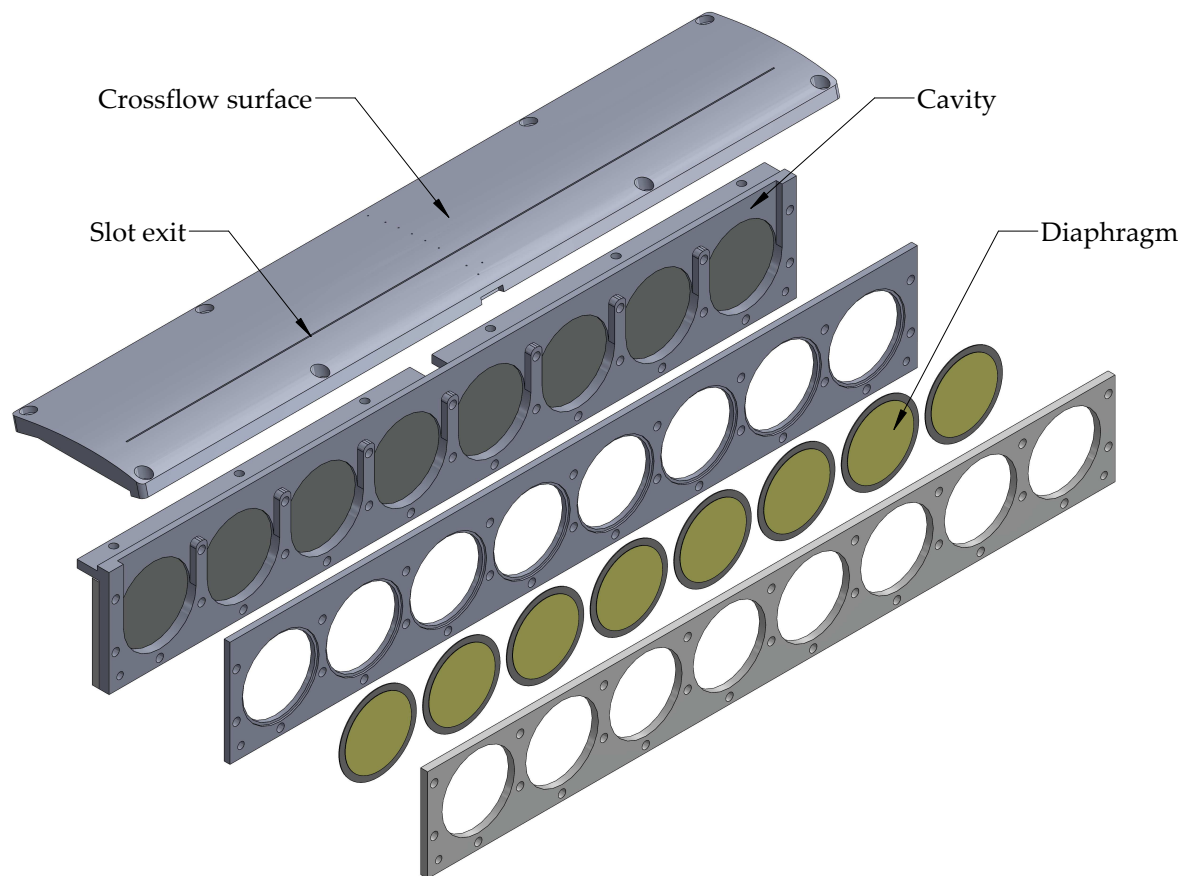
**Figure 1.** (a) A schematic drawing of an SJA in quiescent flow (adapted from Feero [48]) and (b) a Murata MZB1001T02 microblower (adapted from Machado et al. [49]).

The periodic movement of the diaphragm generates a jet cycle, alternating between the ingestion and expulsion cycle of the working fluid as it enters and exits the cavity. The actuation cycle begins with the ingestion cycle (Figures 2a–b), where flow is drawn into the cavity, followed by the expulsion cycle (Figures 2c–d), where the diaphragm forces the increased volume of flow to exit the cavity through the neck and jet slot. Alternating between the ingestion and expulsion cycles, linear momentum is intermittently transferred to the bulk flow. The net momentum arises from the ejection of discrete vortical structures from the slot exit, such as vortex rings for a circular orifice or vortex pairs for a two-dimensional slot.



**Figure 2.** Schematic drawing of an SJA in quiescent flow during expulsion and ingestion phase, (a) Initiation of ingestion cycle; (b) Peak ingestion phase ;(c) Initiation of expulsion cycle and (d) Peak expulsion phase.

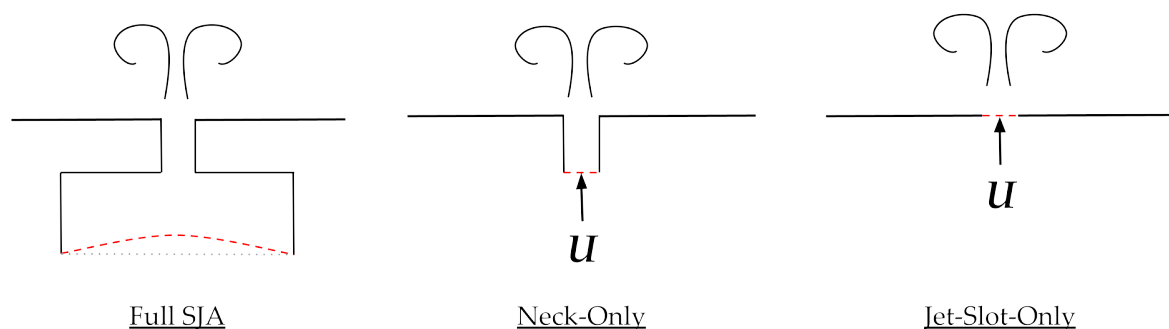
A traditional circular SJA is typically axisymmetric, but it can be modified to create a slot-based SJA with an aspect ratio at the jet exit. Another method of modifying SJAs involves altering the nozzle geometry and adjusting the lip thickness and profile. The working mechanism of SJAs does not vary significantly when an array of actuators, such as when multiple circular diaphragms placed within the same cavity, is employed to create a slot-based SJA [48]. An example is shown in Figure 3, where an array of actuators are integrated to operate a rectangular SJA. Note how multiple discrete cavities are partially connected near the slot exit.



**Figure 3.** Schematic drawing of a rectangular SJA having an array of circular actuators (adapted from Feero [48]).

### 2.1. SJA Modelling Methods

Extensive research has been carried out to characterize and optimize SJAs using both experimental and numerical methods [50–52]. One of the main challenges in numerical approaches is accurately modeling the periodic expulsion of synthetic jets to match experimental results. Three primary modeling techniques were used most frequently: full SJA modeling, neck-only, and jet-slot-only method, as shown in Figure 4.



**Figure 4.** Schematic drawing of different SJA modeling methods, red dotted line indicates where the boundary condition is applied, adapted from Ho et al. [53].

Raju et al. [54] conducted a series of numerical simulations with three different modeling techniques for two-dimensional SJAs in attached grazing flow and canonical separated crossflow. They compared the full SJA method with a radius-based jet profile, applying both a uniform jet  $U = f(t)$  and a sink-like jet  $U, V = f(r, t)$  to a neck-only model, as well as a uniform jet to a



jet-slot-only model. The study concluded that the sink-like jet profile applied to the neck-only model provided the best agreement with the full SJA method while significantly reducing computational costs. However, although the jet-slot-only model captured the correct trend in separation control, it under-predicted the separation bubble, with the deviation increasing rapidly as the jet Reynolds number was increased. The numerical work by Ho et al. [53] also compared the three methods by applying unsteady Reynolds-averaged Navier-Stokes (URANS) simulations to a three-dimensional circular SJA, with the analytical Womersley solution for the jet profile, previously used by Palumbo et al. [50] in a Direct Numerical Simulation (DNS):

$$U(r, t) = U_m \text{Real} \left[ \left( 1 - \frac{J_0(i^{\frac{3}{2}} r Wo)}{J_0(i^{\frac{3}{2}} Wo)} \right) e^{i\omega t} \right] \quad (1)$$

where  $U_m$  is the maximum jet centerline velocity,  $\omega = 2\pi f$  is the angular actuation frequency,  $J_0$  is the zeroth-order Bessel function, and  $Wo$  is the Womersley number:

$$Wo = d\sqrt{\omega/4\nu} \quad (2)$$

It was found that when the modelled neck volume is greater than the total ingested flow volume over the ingestion cycle, the neck-only method can yield comparable results to the full SJA method with a dynamic mesh approach. Meanwhile, the results from insufficient neck volume or the jet-slot-only method might only be accurate further downstream.

### 3. Synthetic Jet Actuators in Quiescent Flow

SJAs implemented in crossflow control applications are often characterized in quiescent flow conditions prior to deployment. But there are also purely quiescent flow applications, such as cooling applications. This preliminary assessment aims to characterize important input parameters, such as blowing velocity  $\overline{U}_j$ , actuation frequency  $f$ , and the peak-to-peak voltage  $V_{pp}$  applied to the diaphragm [55–57]. Smith and Swift [58] proposed that the Reynolds number of the synthetic jet could be determined using the average jet velocity during the expulsion phase, as shown in Equation (3) below:

$$Re_d = \frac{\overline{U}_j d}{\nu} \quad (3)$$

where the average velocity  $\overline{U}_j$  over the expulsion phase, also known as the blowing velocity, is obtained as:

$$\overline{U}_j = \frac{1}{T} \frac{1}{A_j} \int_{A_j} \int_0^\tau U_j dt dA \quad (4)$$

In Equation (4),  $A_j$  is the cross-sectional area of the orifice,  $T$  is the period of the actuation, and  $\tau$  is the duration of expulsion, typically set to  $\tau = T/2$ . There are other definition for the average velocity, but for the sake of consistency, only the blowing velocity  $\overline{U}_j$  will be used in this manuscript.

In the remainder of this section, a review of the criteria for synthetic jet formation is presented, followed by an analysis of its development in quiescent conditions, considering the influence of various geometrical and operational parameters on flow evolution. Note that the effects of clustering, concerning an array of multiple SJAs, will not be addressed in this section as it is discussed in detail in Section 4.5.

#### 3.1. Synthetic Jet Formation Criterion

The formation and evolution of synthetic jets were studied by Smith and Glezer [57] for a rectangular SJA having an aspect ratio  $AR = 150$ , by applying the slug model proposed by Glezer [59] for axisymmetric vortex rings, in which a cylindrical volume of fluid moves at constant

velocity  $\overline{U}_j$  for a time  $T$  through a circular orifice of  $d$ . Hence, the slug length  $L$  represents the length of the column (slug) of fluid ejected during the expulsion phase of the cycle and is expressed as:

$$L = \overline{U}_j T \equiv \frac{\overline{U}_j}{f} \quad (5)$$

Based on the slug model, Smith and Glezer [57] proposed two key dimensionless parameters: the Reynolds number  $Re_d$  and the stroke ratio  $L^+ = L/d$ , which can be used to characterize each vortex pair. Jabbar et al. [60] proposed a different variant of the Reynolds number, which was defined based on the stroke length as  $Re_L = Re_d L^+$ . Further studies by Utturkar et al. [61] and Holman et al. [62] showed that the synthetic jet formation is governed by the jet Strouhal number  $Sr$  or, alternatively, by both Reynolds number  $Re_d$  and Stokes number  $Sk$ :

$$\frac{1}{Sr} = \frac{Re_d}{Sk^2} > \frac{\tau}{T} K \quad (6)$$

where  $K$  is the formation threshold, and the Strouhal number  $Sr$  and Stokes number  $Sk$  are defined as:

$$Sr = \frac{\omega d}{\overline{U}_j} \quad (7)$$

$$Sk = \sqrt{\omega d^2 / \nu} \quad (8)$$

The formation criterion proposed by Holman et al. [62] outlines the conditions necessary for successful synthetic jet formation, and is related to the stroke ratio according to:

$$\frac{1}{Sr} = \frac{L^+}{2\pi} > \frac{\tau}{T} K \quad (9)$$

Note that, for instances where  $\tau = T/2$ , Equation (9) simply reduces to  $L^+/\pi > K$ . Generally, a synthetic jet forms when each vortex structure ejected during the blowing stroke propagates downstream at a speed fast enough to escape the influence of the sink-like flow during the suction stroke, which occurs when the stroke ratio  $L^+$  exceeds a certain threshold proportional to  $K$  [58,62–64]. Dimensional analysis led to the definition of the synthetic jet formation constant  $K$ , as follows:

$$K = \frac{32C^2(1+\epsilon)^p}{\kappa\pi^2} \quad (10)$$

where the constant  $C$  is defined as the ratio of the average velocity, that is  $2\overline{U}_j$  when  $\tau = T/2$ , to the centerline velocity  $U_c$  during the peak expulsion phase. The non-dimensional exit radius of curvature  $\epsilon$  is given by  $2r_l/d$ , where  $r_l$  is the lip radius of curvature and  $d$  is the jet orifice diameter or width. The constant  $\kappa$  is influenced by the vortex dimensions, while the exponent  $p < 1$  approximates the flow separation due to the exit curvature. The constant  $K$  was proposed for both two-dimensional and axisymmetric synthetic jets, with values of 1 and 0.16 [62], respectively. The former value was derived from computational results, while the latter is empirical. Both values were validated against other experimental studies. For example, Shuster and Smith [63] examined three primary stroke ratios,  $L^+ = 1, 2$ , and 3, for a circular SJA across a range of Reynolds numbers, using dye visualization and particle image velocimetry (PIV), observing that the vortex rings could not escape the orifice when  $L^+ < 0.6$ , which aligned closely with the criterion  $L^+ > 0.16 \times \pi \approx 0.5$  proposed by Utturkar et al. [61] (see Figures 3 and 6 in Reference [63]). Overall, the synthetic jet formation criterion constant is not universal and is highly dependent on the geometry of the SJA.



### 3.2. Synthetic Jet Evolution

Once synthetic jets are formed, the flow field in quiescent conditions consists of a train of vortex structures, generally divided into three distinct regions: the near, transitional, and far-field. However, many studies simplify this classification by omitting the transitional region [29,57]. The near-field region is dominated by the time-periodic formation and advection of the vortex structures [56,57]. The coherent vortical structures continue to convect downstream and, in the far-field region, break down into smaller vortical structures, eventually transitioning into a fully turbulent state. For  $L^+ = 1, 2$ , and 3, Shuster and Smith [63] reported that vortex ring trajectories scaled exclusively on the stroke ratio  $L^+$  within the near-field, similar to the observations by Smith et al. [65]. Their study demonstrated that the convective velocity of the vortex rings scales, at most, with the slug model velocity  $\bar{U}_j$  (see Figures 3 and 14 in Reference [63]). The study by Jabbal et al. [60] on circular synthetic jets in quiescent conditions revealed that above a threshold value of  $L^+ = 4$ , the circulation contained in the primary vortex rings reach a maximum, and secondary eddies are shed as  $L^+$  increases further (see Figures 7 and 8 in Reference [60]).

The similarities and differences between synthetic and conventional steady jets in both near- and far-field regions are intriguing. Cater and Soria [29] examined the evolution of a round SJA, while Smith and Swift [58] studied high-AR rectangular SJAs. Both studies confirmed that the far-field behavior was comparable to steady jets, with time-averaged velocity profiles becoming self-similar. A higher spreading rate and decay constant were observed from synthetic jets, particularly in the near-field region. This was attributed to the increased entrainment caused by the unsteady vortex formation at the synthetic jet origin. The faster-spreading rate accompanied by a more rapid decline in centerline velocity was also confirmed by Shuster and Smith [63]. For a circular SJA, Cater and Soria [29] defined the near-field as extending from the orifice to an axial distance of  $30d$ , with the far-field starting beyond this point. Shuster and Smith [63] used the stroke length in their classification, noting that vortex ring dynamics dominated the flow field for distances less than  $L$  from the orifice. In contrast, beyond  $L$ , the flow entered a short transitional region before resembling a steady round turbulent jet. The transition from vortex rings to a steady jet occurred over a longer streamwise distance when  $L^+ > 3$ . Smoke visualization by Smith and Glezer [57] for high-AR rectangular SJAs revealed that, within the transitional region, instabilities caused the formation of rib-like secondary vortical structures wrapped around the cores of the primary vortex pairs, eventually leading to loss of coherence and their breakdown into smaller scales (see Figure 4 in Reference [57]). Cater and Soria [29] described this phenomenon as analogous to the inviscid azimuthal instability responsible for the breakup of vortex rings, as observed by Widnall et al. [66].

### 3.3. Effects of Orifice Shape

Considerable efforts have been devoted to understanding the effect of jet exit shape on the mixing and turbulent characteristics of SJAs [29,67–72]. During the initial expulsion phase, the vortex rings emanating from a slotted orifice have a distorted cross-section that approximates the shape of the orifice. However, as the vortex ring moves downstream, its cross-section expands in the direction of the short axis and contracts in the direction of the long axis, a phenomenon which is referred to as axis switching (see Figure 2 in Reference [73]). Axis switching enhances mixing in both steady and synthetic jets, making non-circular SJAs particularly intriguing for AFC [74,75]. Non-circular SJAs are typically divided into low-AR, finite-span, and high-AR, though there is currently no standardized classification, with various criteria proposed by different researchers [40,76,77].

Lindstrom and Amitay [78] examined three orifice shapes: rectangular, trapezoidal, and triangular, all with the same aspect ratio  $AR = 19$  and area, at a hydraulic diameter-based Reynolds number  $Re_d = 7000$  using stereoscopic PIV and hot-wire anemometry (HWA). The time-averaged flow fields demonstrated that jet structural vectoring occurred toward the larger cross-sectional areas for the triangular and trapezoidal geometries, which was attributed to asymmetric vortex structures. In contrast, the jet associated with the rectangular orifice was ejected perpendicular to the orifice (see

Figures 5 and 6 in Reference [78]). While significant differences were observed in the near-field region among the three orifice shapes, with velocity profiles displaying undulations along the span, all cases eventually attained a bell-shaped velocity profile, as expected in a free jet. Lindstrom and Amitay [78] also proposed a criterion for the location of axis switching, defining it as the point where the averaged wall-normal vorticity exceeds the spanwise vorticity. Garcillan et al. [72] conducted a series of PIV experiments to investigate the effect of aspect ratios  $AR = 1\text{--}16$  for slotted SJAs while maintaining a constant jet exit area across the different cases. The vortex ring ejected from the slotted SJA initially emerged with a cross-section similar to the shape of the jet exit and appeared two-dimensional. However, as it convected downstream, it underwent axis switching, with this phenomenon becoming more rapid and intense as the aspect ratio of the jet slot increased. It was found that high- $AR$  SJAs generated vortex rings with greater initial jet momentum than circular SJAs. However, the subsequent axis switching led to more rapid structural dissipation and a faster momentum drop-off than circular SJAs. A similar conclusion was reached by Oren et al. [79], who experimentally investigated various nozzle geometries, including triangular, circular, square, and rectangular ( $AR = 3.7$ ) SJA nozzles using PIV.

Several numerical studies have also investigated the effects of SJA orifice shape on determining the optimal configuration for flow control. Lee and Goldstein [80] conducted DNS to examine the effects of SJA neck and lip geometry on flow characteristics in a quiescent environment, focusing on two-dimensional SJAs with flat, round, and cusp lips. It was reported that the flat lip SJA achieved a higher peak streamwise jet velocity. In contrast, the round lip SJA entrained more fluid during the ingestion cycle, increasing spanwise jet velocity. However, this effect was localized near the jet exit and had a limited impact on the external flow. Miró et al. [81] numerically investigated two different SJA configurations using DNS and large eddy simulation (LES) for jet impingement for a two-dimensional slot-based SJA and a circular SJA over a range of  $50 < Re_d < 500$ . The study reported that the circular SJA exhibited greater jet momentum at the center and more coherent structures than the slot-based SJA.

### 3.4. Effects of Actuation Frequency

The effect of SJA actuation frequency is a critical parameter in flow separation control and has been widely studied in quiescent environments [82–85]. An essential feature of any SJA is its frequency response, which dictates the output quantities of interest, such as velocity, in relation to the input signal. For an SJA, the frequency response of the jet velocity is influenced by the cavity and orifice geometry, fluid properties, and actuator characteristics [62]. Since an SJA operates similarly to a Helmholtz resonator, the Helmholtz frequency plays a crucial role in its frequency response, which is theoretically given by:

$$f_H = \frac{U_s}{2\pi} \sqrt{\frac{A_j}{H_n V_c}} \quad (11)$$

where  $V_c$  is the cavity volume,  $H_n$  is the effective height of orifice neck ( $H_n = H_o$  in case of Figure 1a), and  $U_s$  is the speed of sound. As highlighted by Arafa et al. [86], the Helmholtz frequency, as shown in Equation (11), is formulated for an ideal spherical volume in which sound wave propagation matches the volume boundaries. Gallas et al. [87] implemented a lumped element model for piezoelectric-driven SJAs, observing a good agreement between the analytical and measured frequency responses. The model revealed that a piezoelectric-driven SJA functions as a fourth-order coupled oscillator, with one oscillator being the cavity acting as a Helmholtz resonator and the other being the piezoelectric diaphragm. The system, therefore, may exhibit one or two resonant frequencies, depending on the proximity of the cavity's Helmholtz frequency to the piezoelectric diaphragm's natural frequency. It has been shown that an SJA with a high coupling ratio produces a single resonant peak velocity that is greater in magnitude than that of an SJA with a low coupling ratio [87–90]. The studies mentioned above highlight a significant limitation of piezoelectric actuators: the bandwidth over which acceptable

velocity magnitudes can be achieved is often confined to frequencies near resonance. One solution to this limitation is to modulate the input signal, which will be discussed in more detail in Section 4.3.

Mallinson et al. [91] conducted experimental and numerical investigations into the effects of actuation frequency on SJA performance, revealing that operation at the Helmholtz resonance frequency yielded the most significant response, a finding later corroborated by the numerical studies of Lv et al. [92]. Mallinson et al. [91] also proposed that the maximum jet centerline velocity is determined by a balance between the inertia of the membrane forcing and the viscous forces from the jet slot boundary layer. The effect of different modulation signals was investigated by Lu and Wang [93] using URANS, comparing them to a steady jet. The modulation signals included triangular, sinusoidal, trapezoidal, square, bi-frequency, and varying duty cycles. It was reported that the varying duty cycle modulation resulted in significantly stronger jet momentum with proper optimization than conventional sinusoidal modulation.

### 3.5. Effects of Cavity Shape

SJA cavity shape optimization has been studied both experimentally [86,88,94–96] and numerically [69,97–99]. Feero et al. [100] employed HWA to examine the influence of three cavity shapes, cylindrical, conical, and contracted, on SJAs producing circular synthetic jets in a quiescent flow operated near the Helmholtz frequency. A pressure probe within the cavity was utilized to ensure that the normalized frequency and cavity pressure remained constant across all three cases. Noticeable differences in the radial velocity profile and jet momentum flux were observed across the different cavity shapes. While the jet profile shape was consistent among the three cases, the magnitudes varied. Feero et al. [100] concluded that the basic cylindrical shape maximizes momentum flux. However, they also suggested that the more complex geometry of contracted cavity was able to achieve a lower resonant frequency, and can be used if the goal is to reduce power consumption and enhance efficiency. Ziadé et al. [101] conducted three-dimensional compressible laminar simulations using similar SJA cavities and test conditions as those in Feero et al. [102]. They found that conical and contracted cavities exhibited strong blockage effects, while cylindrical cavities demonstrated more efficient vortex formation.

The experimental work by Jabbar et al. [103] investigated the effect of neck and cavity height on the formation of vortex rings in circular SJAs using PIV. A shorter neck height was observed to result in more rapid vortex circulation when  $H_o/d < 1$ , while  $H_o/d > 1$  yielded consistent results. A compressible numerical model developed by Tang and Zhong [104] was also employed to support this finding. The numerical work by Chiatto et al. [105] investigated the flow inside a three-dimensional double orifice SJA. The study featured a cylindrical cavity, with the two orifices equally spaced from the center of the cavity. By analyzing Q-criterion contours and streamline plots of the flow, it was proposed that the flow within a double orifice SJA behaves like two sub-cavities, provided the jet slots are sufficiently spaced apart. A lumped model for predicting the behavior of a double orifice SJA, validated experimentally, was subsequently proposed, treating the frequency response as a force-damped spring-mass system.

## 4. Synthetic Jet Actuators in a Crossflow

For effective flow control, it is essential to thoroughly understand the vortical structures formed by the synthetic jet and boundary layer interaction (SJBLI), their effects near the surface, and their overall effectiveness in altering the flow dynamics [106,107]. Several experiments have demonstrated that synthetic jets effectively delay flow separation on aerodynamic bodies of various shapes [108–114]. The complex SJBLI phenomenon is illustrated schematically in Figure 5. An in-depth understanding of the SJBLI presents several challenges, including accurately characterizing the boundary layer, measuring the high-velocity gradients generated by the synthetic jets, and resolving small-scale rotational coherent structures [115]. In addition to the complex flow physics, ample parameter space must be considered when designing an effective control strategy using SJAs. To establish a systematic approach for

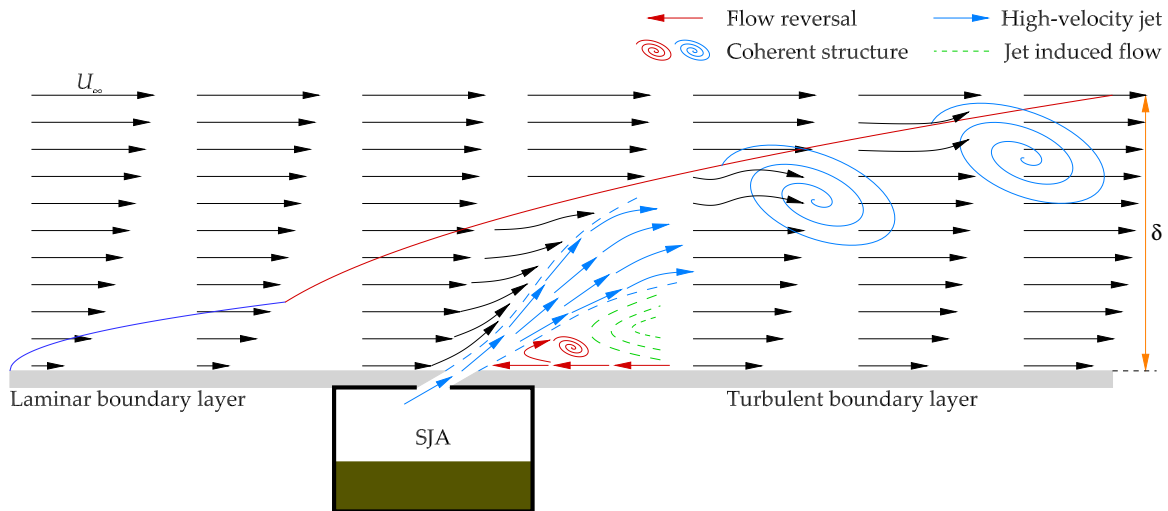
characterizing the effects of various geometrical and operational parameters, Jabbal and Zhong [107] applied Buckingham's  $\Pi$ -theorem to an SJA embedded in a crossflow boundary layer. This analysis identified the following dimensionless parameters:

$$\begin{aligned}\pi_1 &= \frac{fd}{U_\infty} & \pi_2 &= \frac{U_\infty \delta}{\nu} & \pi_3 &= \frac{\delta}{d} \\ \pi_4 &= \frac{\tau_w}{\frac{1}{2}\rho U_\infty^2} & \pi_5 &= \frac{\bar{U}_j}{U_\infty}\end{aligned}\quad (12)$$

where  $\pi_1$  represents the Strouhal number  $St$ ,  $\pi_2$  the freestream Reynolds number  $Re_\delta$ ,  $\pi_3$  the ratio of boundary layer thickness to orifice diameter,  $\pi_4$  the skin friction coefficient  $C_f$ , and  $\pi_5$  the blowing ratio  $C_b$  (also known as jet-to-freestream velocity ratio  $VR$ ). The following inter-dependencies exist between these dimensionless groups and the key dimensionless parameters for an SJA in quiescent conditions:

$$St = \frac{C_b}{L^+} \quad (13)$$

$$Re_L = \frac{C_b L}{\delta} Re_\delta \quad (14)$$



**Figure 5.** A schematic showcasing the complexities in understanding the interaction between a synthetic jet and a boundary layer (based on Ramasamy et al. [115]).

It is important to note that this parametric study did not include all parameters relevant to flow control applications, essentially neglecting factors such as surface curvature, orifice shape or aspect ratio, and clustering effects [116]. Moreover, quantifying momentum addition as a measure of the overall blowing strength was historically common, rather than using the jet-to-freestream velocity ratio [117]. For a two-dimensional configuration, the momentum coefficient  $C_\mu$  may be defined as a ratio of the time-averaged expelled momentum by all the operating SJAs  $\bar{I}_j$  to the momentum of the freestream:

$$C_\mu = \frac{\bar{I}_j}{\frac{1}{2}\rho_\infty U_\infty^2 A_f} \quad (15a)$$

$$\bar{I}_j = \frac{1}{T} \int_{A_j} \int_0^T \rho_j \langle U_j^2 \rangle dt dA \quad (15b)$$

where  $A_f$  is a reference area for the body under consideration and  $T$  is the actuation period [108,118]. The definition of the momentum coefficient is inconsistent in the literature, with various definitions proposed by different researchers [45,47,76,119,120]. Researchers have often assumed a uniform velocity distribution across the jet exit cross-section or ignored spatial variations by relying solely on the centerline velocity. Furthermore, these definitions often consider only the expelled momentum, integrating over the expulsion phase, which by also assuming a top-hat velocity distribution, leads to the following expression:

$$\bar{I}_j = \frac{1}{\tau} \rho_j A_j \int_0^\tau \langle U_j^2 \rangle dt \quad (16)$$

Also note the denominator in Equation (15b) and compare it with Equation (16). Greenblatt and Wygnanski [120] further simplified Equation (16) by decomposing the jet velocity into mean and oscillatory components as  $U_j = \bar{U}_j + u_j$ , deriving the following relation for the momentum coefficient:

$$C_\mu = \frac{2A_j}{A_f} \left( \frac{\bar{U}_j}{U_\infty} \right)^2 + \frac{2A_j}{A_f} \overline{\left( \frac{u_j}{U_\infty} \right)^2} \quad (17)$$

The second term on the right-hand side of Equation (17) may be neglected when it is relatively small compared to the first term. As highlighted by some researchers, the spatial velocity distribution can deviate significantly from the ideal top-hat profile under certain conditions [58,99,100]. Therefore, if the top-hat profile is assumed, the uniformity of the velocity distribution should be validated.

It is interesting to examine how SJA operational and geometric parameters affect their performance in crossflow conditions. The flat plate has been the most commonly used geometrical model in numerous experimental [107,121–128] and numerical [129–131] studies, as it eliminates curvature effects, effect of flow separation, and can produce a zero pressure gradient. Consequently, where applicable, discussing these parameters begins with this geometry before considering more complex shapes.

#### 4.1. Effects of Jet Strength

The strength of a synthetic jet relies on both  $C_b$  and  $Re_L$ . As with SJAs in quiescent conditions, a threshold criterion exists for SJAs in crossflow to effectively enhance fluid mixing (see Figures 10 in Reference [124]). Experimental evidence shows that the interaction of the vortices produced by a circular synthetic jet with a boundary layer leads to the formation of streamwise vortical structures, which can delay flow separation by drawing faster-moving fluid from the freestream into the near-wall region [96,132]. As these vortex rings enter the boundary layer, they experience combined effects from shear forces, boundary layer vorticity, and the Magnus force resulted from interactions with the crossflow [112,126,133,134]. These influences cause the vortex rings to tilt and deform at varying degrees, depending on their strength and residence time within the boundary layer, resulting in complex three-dimensional vortical structures.

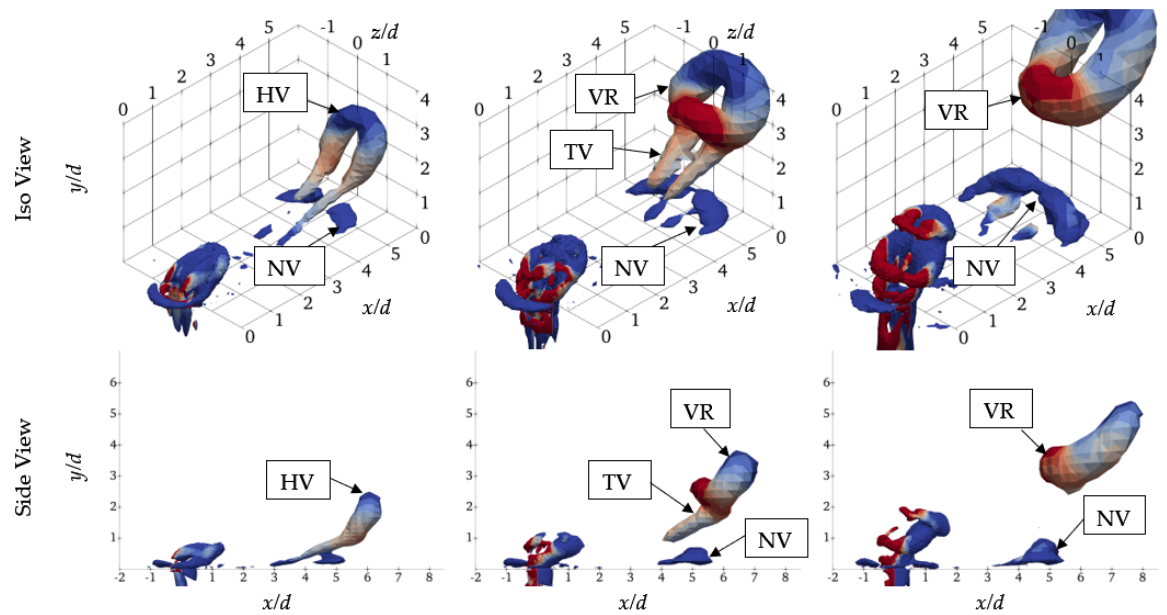
The dye flow visualization by Zhong et al. [126], with  $Re_L$  ranging from 16 to 245 and  $L^+$  from 0.56 to 1.4, in a laminar boundary layer at blowing ratio  $C_b$  from 0.06 to 0.7, revealed three distinct behaviors:

1. At low blowing ratios  $C_b$  and jet Reynolds numbers  $Re_L$ , the vortical structures generated by synthetic jets appeared as hairpin vortices attached to the wall.
2. At intermediate  $C_b$  and  $Re_L$  values, the vortex sheet formed at the orifice rolled up into vortex rings, which experienced significant tilting and stretching as they entered the boundary layer.
3. At high  $C_b$  and  $Re_L$  values, the vortex rings exhibited some tilting but little to no stretching, quickly penetrating the edge of the boundary layer.

Jabbal and Zhong [107] observed the same three types of vortical structures using stereoscopic dye flow visualization. They also performed surface visualization of the vortex footprints by applying a



temperature-sensitive liquid crystal (TLC) coating on the test surface. Interestingly, only two distinct types of thermal footprints were observed. Both hairpin vortices and stretched vortex rings produced two streamwise streaks of high heat transfer, corresponding to high-momentum fluid transfer toward the wall outboard of the streamwise counter-rotating legs based on the Reynolds analogy. In contrast, the tilted vortex rings generated only a single streamwise streak of high heat transfer, which was hypothesized to result from an induced vortex adjacent to the wall (see Figure 6 in Reference [107] or Figure 7 in Reference [124]). Q-criterion contours displaying the hairpin vortices, vortex rings, and near-wall vortices are presented in Figure 6.



**Figure 6.** Q-criterion contours of hairpin vortices and vortex rings as a result of the interaction between a synthetic jet and a boundary layer, showcasing hairpin vortex (HV), vortex ring (VR), trailing vortex pair (TV), and the near-wall vortex (NV) (adapted from Ho et al. [131]).

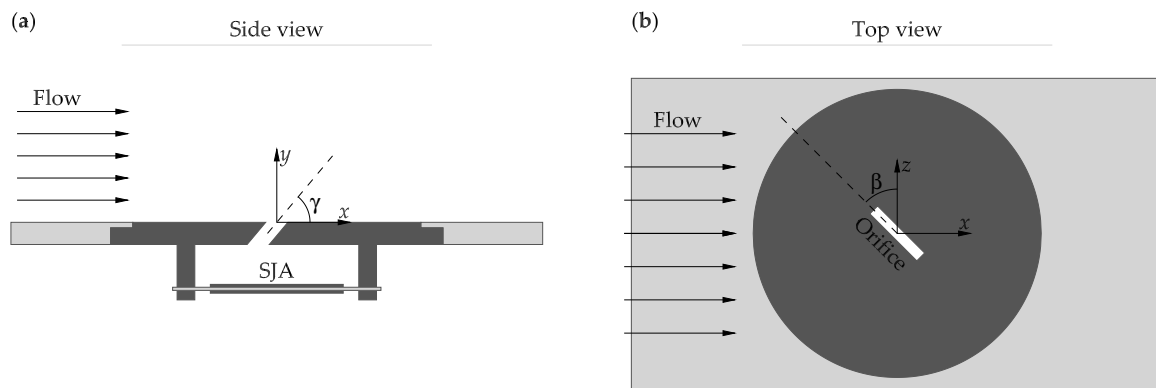
To understand the underlying flow mechanism, Jabbal and Zhong [107] used two-dimensional PIV to study the flow fields of the three above-mentioned vortical structures. Hairpin vortices ( $C_b = 0.32$  and  $L^+ = 1.6$ ) and stretched vortex rings ( $C_b = 0.27$  and  $L^+ = 2.7$ ) exhibited characteristics similar to a streamwise vortex pair with a common upwash. In contrast, tilted vortex rings ( $C_b = 0.54$  and  $L^+ = 2.7$ ) featuring a common downwash induced a tertiary streamwise vortex pair in the near-wall region. Wall shear stress measurements revealed that stretched vortex rings provided the best performance in terms of higher near-wall fluid mixing, greater persistency, and reduced spatial fluctuations. The numerical work of Ho et al. [131] investigated the effect of varying SJA jet momentum ( $0.32 < C_b < 1.10$ ) in a turbulent boundary layer crossflow with three-dimensional URANS. An increase of jet momentum resulted in greater boundary layer penetration under the same actuation frequency. Note that, although in this study the increase of jet momentum resulted in a significant increase of wall shear stress along the streamwise direction, it also reduces the spanwise control authority of the SJA. Classification of structures emerging due to SJBLI is not unique and depends on the considered parameter space. For example, Zhong and Zhang [112] described these vortical structures only based on blowing ratio  $C_b$  given a constant actuation frequency  $f$ , first as hairpin-like vortices that are located close to the wall, and then, as  $C_b$  increases, as tilted vortex rings with a pair of trailing legs that penetrate the edge of the boundary layer shortly downstream. The numerical work of Zhou and Zhong [123] of a rounded SJA in a laminar boundary layer provided a similar conclusion. For a constant value of orifice width and wall shear stress, parametric maps are available in the literature that classify synthetic jet or pulsed jet flow behavior based on the blowing



ratio  $C_b$  (VR) and the jet Reynolds number  $Re_L$ , or its alternative, the stroke ratio  $L^+$  [121,124,135]. The generated vortex rings will undergo deformation due to the resident shear in the boundary layer for both pulsed and synthetic jets. For a synthetic jet, however, an additional suction effect is expected to be confined to the upstream branch of the vortex, leading to the formation of an asymmetric structure. According to Jabbal and Zhong [124], a hairpin vortex forms as the upstream branch of the vortex ring produced by the synthetic jet is weakened by the suction cycle as it passes over the orifice and is then canceled out by resident vorticity of the opposite sign as it propagates downstream. Supposing the initial strength of the vortex ring at the orifice exit is relatively strong, the vortical structures may first appear as a stretched vortex ring with a weak upstream branch in the near-field before evolving into a hairpin structure further downstream. At higher blowing ratio  $C_b$  and stroke ratio  $L^+$  values, the vortex rings produced by synthetic jets can escape the influence of the suction cycle and the boundary layer's resident shear, emerging as fully formed rings that appear tilted relative to the wall. Above a threshold stroke ratio  $L^+$ , the vortex rings generated by synthetic jets become increasingly incoherent over time, and secondary vortices can eventually be seen shedding from the primary vortex ring, similar to the observations by Jabbal et al. [60] for SJAs in quiescent condition (see Figure 7 in Reference [124]).

#### 4.2. Effects of Orifice Shape and Orientation

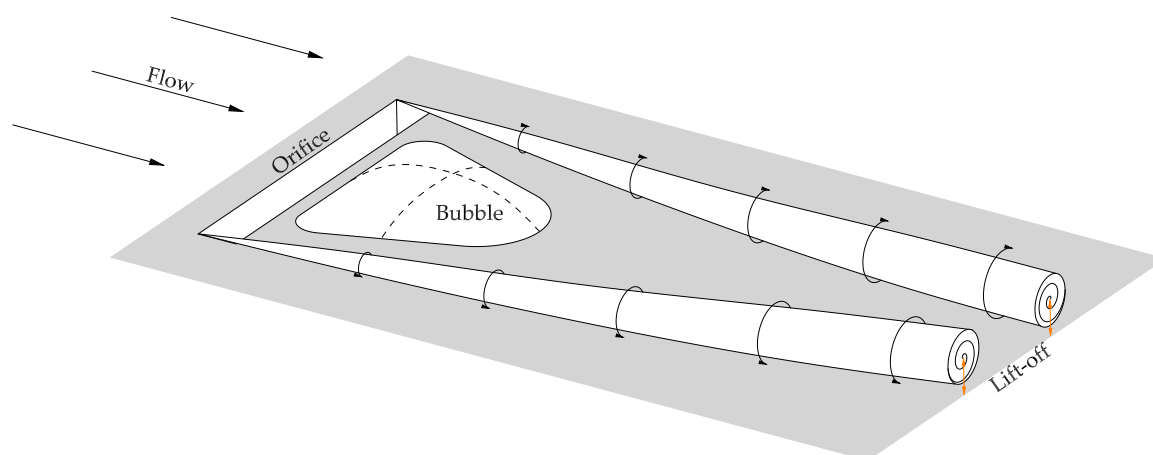
Flow control with synthetic jets from non-circular orifices is of interest because of their enhanced entrainment and mixing capability compared to circular and two-dimensional synthetic jets. A schematic of an SJA with a rectangular orifice in crossflow is shown in Figure 7. In addition to the pitch angle  $\gamma$ , for only a non-circular orifice, a skew angle  $\beta$  must be defined to fully determine the orientation of the orifice with respect to the crossflow. Shuster et al. [43] examined the orifice pitch angle for perpendicular ( $\gamma = 90^\circ$ ) and inclined ( $\gamma = 60^\circ$ ) circular synthetic jets subjected to a laminar boundary at two stroke ratios,  $L^+ = 1$  and 2. At the stroke ratio  $L^+ = 1$ , flow structure differences were significant between the perpendicular and inclined orifice orientations. For the perpendicular orifice, the vortex ring that formed at the orifice during the expulsion portion of the actuator cycle did not escape the near vicinity of the orifice and was subsequently ingested during the suction phase of the cycle. The incoming boundary layer diverted over and around this stationary vortex, creating a wake in the boundary layer downstream of the orifice. In contrast, for an inclined orifice at the same stroke length, a train of vortex rings originating from the orifice penetrated the crossflow (see Figures 5 and 8 in Reference [43]). At the stroke ratio  $L^+ = 2$ , large discrete vortices were formed at the orifice for both orifice orientations that penetrated deep into the crossflow, well beyond the boundary layer edge. In general, the mean interaction from the perpendicular orifice was shorter in the streamwise direction but extended further into the crossflow, causing a slight deflection of the mean streamlines away from the wall. In contrast, the mean interaction from the inclined orifice extended farther downstream, though it remained confined to a region closer to the wall. Zhao et al. [46] studied the flow over a national advisory committee for aeronautics (NACA) 0021 airfoil, instrumented with circular SJAs, at a maximum Reynolds number of  $Re_c = 300\,000$  for a range of angle of attacks  $-6^\circ < \alpha < 30^\circ$ . They observed that, for most configurations, when the momentum coefficient of SJAs was small, a larger pitch angle  $\gamma$  was more effective in improving the maximum lift coefficient of the airfoil. Conversely, when the SJAs had a more significant momentum coefficient, a smaller pitch angle  $\gamma$  was more effective (see Figure 11, Table 3, and Figure 16 in Reference [46]).



**Figure 7.** A schematic illustrating (a) pitch angle  $\gamma$  and (b) skew angle  $\beta$  for a rectangular SJA in a crossflow (based on Van Buren et al. [136]).

As highlighted by Kim et al. [137], the flow fields generated by circular orifices are significantly different from rectangular orifices, suggesting that their interactions with a boundary layer might also differ. Smith [138] conducted a wind-tunnel experiment for an  $AR = 45$  rectangular SJA array expelled normally into a turbulent boundary layer at  $C_b = 1.2$ , examining two orifice orientations, with the rectangular long side normal to ( $\beta = 0^\circ$ ) and aligned with the crossflow direction ( $\beta = 90^\circ$ ), respectively. The boundary layer in the former case exhibited a wake-like region due to the blockage effect, while in the latter, evidence suggested the presence of longitudinal vortices embedded in the boundary layer. Van Buren et al. [139] used stereoscopic PIV to study  $AR = 6, 12$ , and  $18$  rectangular synthetic jets issued normally into a laminar boundary layer of  $Re_\delta = 2000$  at  $C_b = 0.5, 1.0$ , and  $1.5$ . The flow field was characterized by two salient structures: a recirculation region downstream of the orifice and a steady streamwise vortex pair farther downstream, akin to the findings in Smith [138] and Cui et al. [140]. A conceptual model of these structures is shown in Figure 8. These vortices interact with each other, as well as with the wall [141], to eventually lift off of the surface. The spacing of the edgewise vortices, produced due to the finite span of the orifice, and the virtual blockage of the jet were reduced with the decreased  $AR$ .

Van Buren et al. [136] used stereoscopic PIV to study  $AR = 18$  rectangular synthetic jets issued into a boundary layer of  $Re_\delta = 2000$  at three momentum coefficients  $C_\mu = 0.08, 0.33$ , and  $0.75$ . The apparatus could accommodate different orifice pitch angles  $\gamma = 20^\circ, 45^\circ, 65^\circ$ , and  $90^\circ$  through separate inserts and could also be fixed at skew angles of  $\beta = 0^\circ$ – $90^\circ$  every  $15^\circ$ . It was found that orifice orientation significantly influenced both steady and unsteady flow structures. Different combinations of orifice skew and pitch angles led to the formation of various types of vortical structures downstream, including the absence of coherent vortex structures, a single strong vortex (either positive or negative), or a symmetric vortex pair. The phase-averaged  $Q$ -criterion iso-surfaces revealed that orifice pitch angles more aligned with the crossflow produced less coherent vortical structures as they contributed less to generating transverse velocities. In the time-averaged flow field, when the orifice pitch angle was less than  $90^\circ$ , the upstream lengthwise vortex dominated the interaction, leading to a single negative vortex downstream. However, when the orifice had a wall-normal pitch, the downstream lengthwise vortex became dominant, as the upstream vortex was constrained by the jet blockage, resulting in a single positive streamwise-oriented vortex downstream (most clearly seen for  $\beta = 45^\circ$  case, Figure 5 or Figure 6 in Reference [136]). In general, the more wall-normal transverse jets had more blockage, which resulted in a large wake deficit downstream, while the lower-pitch angled jets were more aligned with the flow, generating only regions of higher velocity with no wake. Additionally, the virtual blockage of the jet decreased as the aspect ratio was reduced.



**Figure 8.** A conceptual model of the vortical structures generated by a rectangular synthetic jet within a boundary layer, depicting the recirculation region and the streamwise vortex pair (based on Van Buren et al. [139]).

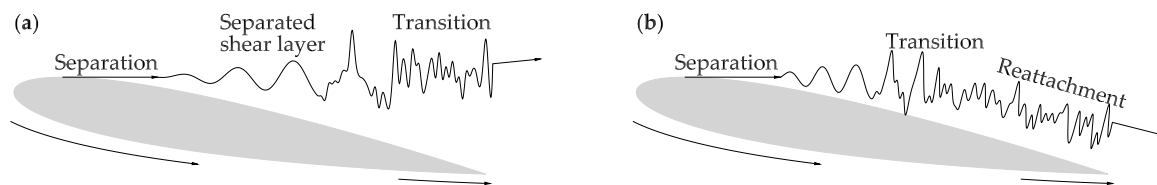
Wang and Feng [40] employed time-resolved tomographic PIV to investigate the three-dimensional flow fields of an  $AR = 3$  rectangular synthetic jet and its interaction with a laminar boundary layer of  $Re_\delta = 1317$  at a fixed blowing ratio  $C_b = 1$ . Two typical orifice orientations, namely spanwise ( $\beta = 0^\circ$ ) and streamwise ( $\beta = 90^\circ$ ) configurations, were examined to analyze the evolution of the vortical structures and the relevant flow physics. The flow field was composed of three major structures: a tilted vortex ring, a secondary trailing vortex, and a tertiary near-wall vortex. This suggested different flow scenarios from those for high-AR cases in Van Buren et al. [139] and Van Buren et al. [136]. Compared with the tilted and distorted vortex rings for circular cases observed by Jabbar and Zhong [107], the legs of the secondary trailing vortex were jointed in the spanwise direction at two different wall-normal heights. In contrast, the tertiary near-wall vortex was a crescent-shaped spanwise vortex instead of a streamwise vortex pair as in Jabbar and Zhong [107] (see Figure 5 in Reference [40]). Additionally, axis switching, a phenomenon typically observed in non-circular vortex rings as described in Section 3.3, was also detected in low-AR rectangular synthetic jets in crossflow. The orientation of the orifice had a direct influence on the timing and location of the axis switching. As for the two different orientations, their observations suggested that the spanwise orientation is more efficient in energizing the boundary layer.

Elimelech et al. [142] and Vasile and Amitay [143] performed stereoscopic PIV to study the interaction of a high-AR rectangular SJA with a three-dimensional boundary layer over a finite  $30^\circ$  swept-back NACA 4421 airfoil at a Reynolds number of  $Re_c = 100\,000$  and several angles of attack, where the SJA was operated at  $C_b = 0.8$  and  $1.2$  and several frequencies. High-frequency pairs of spanwise vorticity rollers were generated and shed away from the SJA, while streamwise vortices formed at both edges of the SJA orifice, rotating in opposite directions. The streamwise vortices primarily influenced the time-averaged flow field, as the impact of the spanwise rollers was largely diminished through averaging, with the higher blowing ratio causing deeper penetration into the crossflow (see Figure 10 in Reference [142]). The streamwise structures, along with the three-dimensional boundary layer, disrupt the coherence of the spanwise rollers, causing them to tilt and warp, eventually breaking them down into streamwise vorticity concentrations (see Figure 15 in Reference [142]).

#### 4.3. Effects of Forcing Frequency and Signal Waveform

The prior work indicates that active control schemes may become more effective by targeting the inherent flow instabilities [120,144]. For example, in the case of a flat plate, given that turbulent flow is less susceptible to separation, laminar separation can be delayed by prematurely triggering the

transition to turbulence through the excitation of Tollmien-Schlichting waves [145,146]. As illustrated in Figure 9, for separated flow over an airfoil, as the inherently unstable separated shear layer undergoes a laminar-to-turbulent transition, it may or may not reattach to the airfoil surface, leading to two distinct flow regimes [147]. Hence, the post-separated flow is dominated by three instabilities: the global instability for the von Karman-like vortex shedding in the wake, the Kelvin-Helmholtz instability associated with the vortex roll-up in the separated shear layer, and the bubble flapping or shedding frequency in the event that laminar separation bubble (LSB) is present [148,149]. The frequencies of the shear layer and wake instabilities are coupled non-linearly and differ by an order of magnitude, which aligns with traditional scaling arguments as the characteristic length scale of the shear layer is an order of magnitude smaller than that of the wake [150].

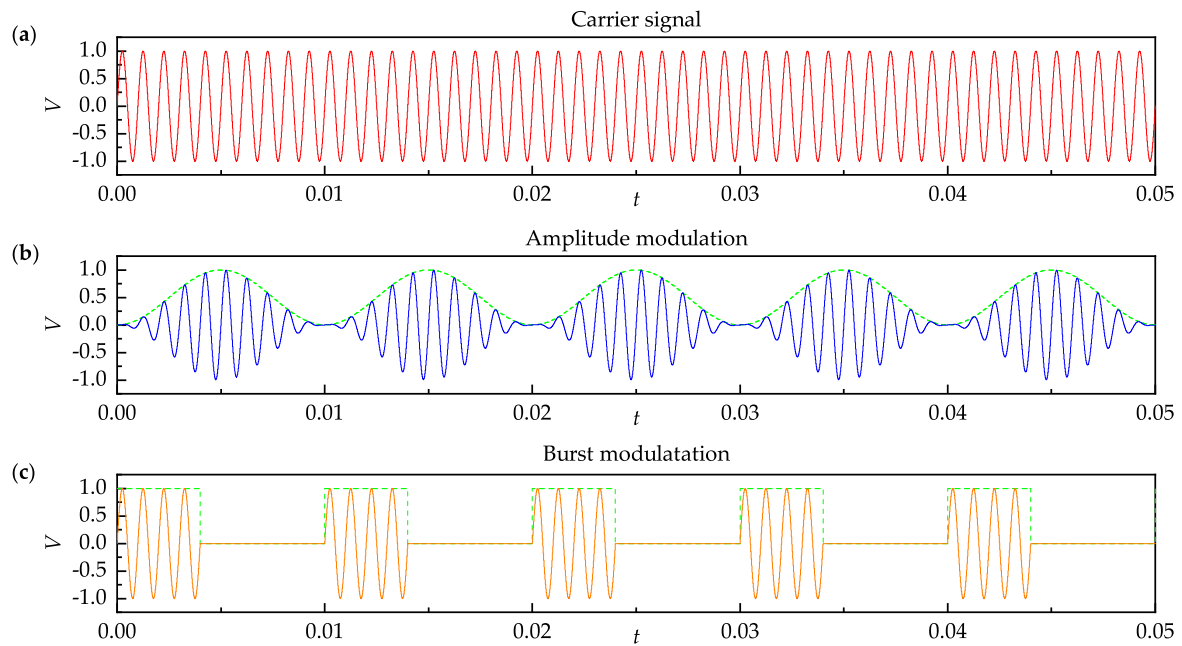


**Figure 9.** Separated flow over an airfoil at low Reynolds numbers undergoing (a) shear layer transition without reattachment and (b) flow reattachment and separation bubble formation (based on Yarusevych et al. [147]).

SJAs should ideally be operated at their optimal frequency, typically identified under quiescent conditions, to maximize jet velocity and momentum output. In many control scenarios, targeting the natural flow instabilities requires the SJA to operate at a sub-optimal excitation frequency. In such cases, a solution proposed by Amitay and Glezer [151] is to use pulse-modulated actuation. This method allows the SJA to be driven at a carrier frequency that maximizes the jet velocity, while the modulation frequency of the source signal is used to specifically target and trigger the desired flow instabilities. It is noteworthy to mention that, although uncommon for SJAs, it is possible to modulate the carrier signal using non-square pulse envelopes or employ amplitude modulation. Examples of modulation for a sinusoidal carrier wave is shown in Figure 10. Equations (15b) and (16) may also be equivalently applied to modulated SJAs, though in such cases,  $\tau$  should be set to the active duration of the SJA. Typically,  $\tau$  is assigned as  $\tau = DC \times T$ , although an SJA may still generate momentum during the off-phase of the cycle, depending on its response characteristics. Overall, Equation (15b) is more appropriate for burst modulation as Equation (16) does not adequately account for the duty cycle. This can be easily verified by assuming a uniform velocity distribution during the active phase, which is sometimes a reasonable assumption for burst-modulated SJAs (see Figure 4 in Reference [152] or Figure 2 in Reference [153]). It then becomes clear that Equation (16) remains unchanged, whereas Equation (15b) varies linearly with the duty cycle. In any case, the effect of forcing frequency is characterized by the reduced frequency  $f^+$ , defined below:

$$f^+ = \frac{f X_f}{U_\infty} \quad (18)$$

where  $X_f$  is an appropriate length scale for the flow under consideration and  $f$  is either the excitation, or the modulation frequency if the carrier signal is modulated. As a rule of thumb, an appropriate characteristic length is typically determined by the length scale of flow instabilities [154]. Nevertheless, it is also common to estimate the reduced frequency  $f^+$  using a reference geometrical length, such as the diameter of a cylinder or the chord length of an airfoil.



**Figure 10.** Examples showcasing the modulation of (a) a sinusoidal carrier signal at  $f_c = 1000$  Hz with (b) a sinusoidal envelope at  $f_m = 100$  Hz and (c) a square pulse envelope at  $f_m = 100$  Hz and DC = 40 %, over a duration of 0.05 s.

Goodfellow et al. [155] considered the effects of excitation at  $f^+ = 40$ , corresponding to the SJA Helmholtz resonant frequency, on the separated shear layer and wake of a NACA 0025 airfoil at a chord-based Reynolds number of  $Re_c = 100\,000$  and an angle of attack of  $\alpha = 5^\circ$ . Their results demonstrated that applying excitation above a threshold  $C_\mu$  leads to flow reattachment, which in turn significantly alters the wake topology. Although an initial increase in  $C_\mu$  above the threshold level resulted in an almost 50 % reduction in drag, the positive impact on airfoil performance plateaued at higher  $C_\mu$  values, highlighting the limitations of relying solely on  $C_\mu$  as a control input. The significance of the forcing frequency and waveform in achieving optimal control becomes evident when comparing the findings of Goodfellow et al. [155] with those of Feero et al. [102], who studied the effects of both the momentum coefficient  $C_\mu$  and reduced frequency  $f^+$  of a high-AR rectangular SJA on flow separation over a NACA 0025 airfoil at  $Re_c = 100\,000$  and  $\alpha = 10^\circ$ . Similar to Goodfellow et al. [155], Feero et al. [102] identified a threshold value for an effective momentum coefficient  $C_\mu = 0.34\%$  at a reduced frequency of  $f^+ = 58$ , which corresponded to the SJA resonant peak. For a burst-modulated input at  $f^+ = 0.84$  and DC = 50 %, however, flow reattachment occurred at  $C_\mu = 0.12\%$ , which was 63 % less than the threshold  $C_\mu$  required for high-frequency harmonic excitation at  $f^+ = 58$ . Interestingly, as the modulation frequency was increased to  $f^+ = 9.9$ , the flow reattached at  $C_\mu = 0.08\%$ , which was an order of magnitude smaller than what was required for high-frequency harmonic excitation. The effectiveness of low- and high-frequency forcing for an airfoil has been studied by several other researchers, in conjunction to different flow conditions, airfoil geometries, and SJA parameters [41,156–160]. Amitay and Glezer [144] conducted wind-tunnel experiments on an unconventional airfoil model at  $Re_c = 310\,000$ , studying the effects of the reduced frequency ranging from  $\mathcal{O}(1)$  to  $\mathcal{O}(10)$  on aerodynamic forces. They observed that forcing at  $f^+ \sim \mathcal{O}(1)$ , corresponding to the wake shedding frequency, leads to the formation of large vortical structures that persist well beyond the trailing edge of the airfoil, resulting in unsteady reattachment and aerodynamic forces. In contrast, actuation at  $f^+ \sim \mathcal{O}(10)$ , corresponding to the shear layer frequency, led to a complete flow reattachment, marked by the absence of large organized vortical structures. Similar observations were made by Amitay and Glezer [151] and Glezer et al. [119] who investigated the same two ranges of reduced frequency  $f^+$  for the same airfoil model as in Amitay and Glezer [144]. Amitay and



Glezer [151] focused on flow transients and observed that the transients following the initiation or termination of pulse-modulated control were quite similar for cases where  $f^+ \sim \mathcal{O}(1)$  and  $f^+ \sim \mathcal{O}(10)$ . After the initial transition, the shedding of organized vortical structures gradually diminished for  $f^+ \sim \mathcal{O}(10)$  case, whereas  $f^+ \sim \mathcal{O}(1)$  case was characterized by the coherent shedding of a train of large vortices. Similar observations were reported by Amitay and Glezer [161]. For a NACA 0025 airfoil at  $Re_c = 100\,000$ , both Feero et al. [162] and Xu et al. [163] showed that forcing at the shear layer instability  $f^+ \sim \mathcal{O}(10)$  maximizes the lift-to-drag ratio, while forcing at the wake instability  $f^+ \sim \mathcal{O}(1)$  leads to maximum lift increase. Glezer et al. [119] investigated the fundamental differences in the response of separated flow over a two-dimensional circular cylinder at a diameter-based Reynolds number of  $Re_D = 75\,500$  to both low- and high-frequency actuation. By measuring the changes in circulation around the cylinder, the study confirmed the earlier findings of Amitay and Glezer [144,151]. Low-frequency actuation at  $f^+ \sim \mathcal{O}(0.1)$ , coupled with the global shedding frequency of the wake, produced strong oscillations in circulation and, as a result, in the aerodynamic forces. In contrast, under high-frequency actuation at  $f^+ \sim \mathcal{O}(1)$ , the circulation experienced a brief transient before stabilizing to a quasi-steady state, indicating that the aerodynamic forces became relatively time-invariant. These results underscored the fundamental distinction between low- and high-frequency actuation, that is the latter is decoupled from the unsteady base flow frequencies, leading to aerodynamic forces that are nearly constant and a damping of global flow oscillations.

The second part of the study by Amitay and Glezer [151] focused specifically on the efficiency of SJAs using pulse-modulated forcing at a constant duty cycle  $DC = 25\%$  and across a range of reduced frequencies  $0.27 < f^+ < 5$ , compared to time-harmonic excitation. A comparison of both methods at  $f^+ = 3.3$ , while maintaining the same  $C_\mu$  level, revealed that time-harmonic actuation did not produce the same levels of lift coefficient as pulse-modulated excitation. Remarkably, pulse modulation resulted in a 400 % increase in the lift coefficient once steady state was achieved, compared to continuous high-frequency  $f^+ \sim \mathcal{O}(10)$  actuation, while using only 25 % of the jet momentum coefficient. Taylor and Amitay [108] investigated the effects of pulse-modulated SJA flow at varying  $C_\mu$  and  $f^+$  values on the global forces and moments of a dynamically pitching finite-span national renewable energy laboratory (NREL) S809 blade at  $Re_c = 220\,000$ . Remarkably, at a reduced modulation frequency of  $f^+ = 1.2$  and a duty cycle  $DC = 40\%$ , a 50 % reduction in lift hysteresis was observed compared with the continuous sinusoidal actuation. Moreover, at a constant  $f^+$ , the reduction in hysteresis was very similar between  $DC = 60\%$  and  $DC = 100\%$  cases. The effectiveness of pulse-modulated forcing at a constant  $C_\mu = 1.2\%$  and various  $f^+$  values was also confirmed by Rice et al. [153,164,165] for an NREL S817 airfoil at  $Re_c = 375\,000$ . Notably, these studies demonstrated the efficacy of pulse modulation in deep stall conditions, such as at  $\alpha = 25^\circ$ , using a duty cycle of only  $DC = 35\%$ , significantly reducing power consumption. All of these works highlight the potential for reducing power requirements for synthetic jets while achieving similar flow reattachment effects or hysteresis reductions through pulse modulation at lower duty cycles.

Margalit et al. [166] conducted a series of tests on a balance-mounted  $60^\circ$  swept-back semi-span delta wing model with a sharp leading edge, and a 5.7 % thickness-to-root-chord ratio for a range of Reynolds numbers  $117\,000 < Re_c < 350\,000$  and post-stall angles of attack  $25^\circ < \alpha < 45^\circ$ , studying several SJA parameters, including the modulation wave form. Their analyses revealed that the most effective reduced frequencies in improving the normal force were an order of  $\mathcal{O}(1)$ , regardless of the modulation waveform or momentum coefficient  $C_\mu$ . Interestingly, high-frequency non-modulated signals resulted in no improvement, or even a slight degradation, of aerodynamic performance (see Figures 4 and 5 in Reference [166]). Furthermore, the square pulse and chainsaw envelopes were somewhat superior to the triangle and sine envelopes in terms of normal force enhancement, for the range of effective frequencies considered (see Figure 6 in Reference [166]). It was found that a square envelope with a duty cycle as low as  $DC = 5\%$  was more effective than an amplitude-modulated signal, despite the latter having a larger peak excitation velocity and an order of magnitude greater



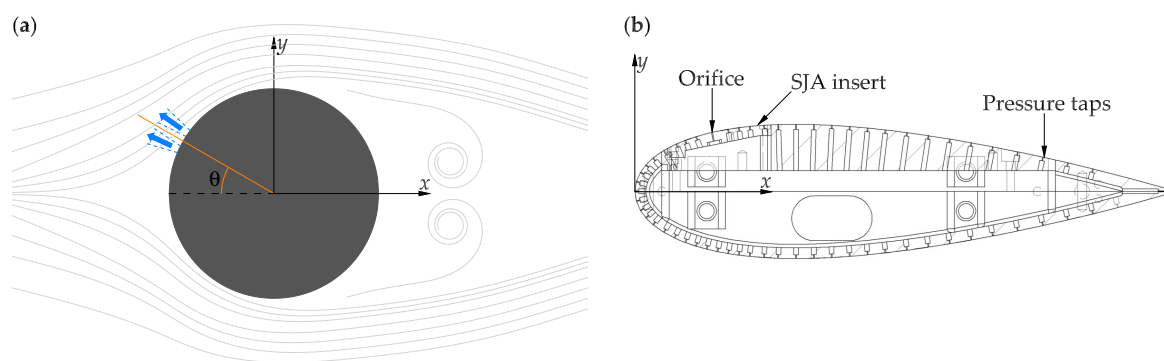
momentum input. The study by Margalit et al. [166] demonstrates the role of modulation envelope in enhancing the performance of SJAs.

#### 4.4. Effects of Actuator Location

Although not explicitly included in the dimensional analysis presented in Section 4, the location of the SJAs, denoted by  $x^+$  when non-dimensionalized, implicitly influences other parameters, such as the boundary layer thickness  $\delta$ , wall shear stress  $\tau_w$ , and the local wall curvature. Amitay et al. [159] investigated the effect of SJA location on the reattached flow over an unconventional airfoil across a range of angles of attack  $5^\circ < \alpha < 25^\circ$  at a Reynolds number of  $Re_c = 310\,000$ . The results showed that less power was required to reattach the flow as the control was positioned closer to the natural separation point on the unforced airfoil (see Figure 7 in Reference [159]). Surprisingly, reattachment was still achieved in some cases even when the actuators were positioned downstream of the stagnation point on the pressure side of the airfoil. Amitay et al. [159] emphasized that, despite the relatively high levels of  $C_\mu$  necessary to affect the flow far upstream of the separation point, the interaction between the jets and the crossflow can yield a higher lift-to-drag ratio that may not be achievable when the jets are closer to the separation point. Zhao et al. [46] considered two chordwise locations  $x^+ = 15\%$  and  $40\%$  for a NACA 0021 airfoil. They explained that the rear location was more effective than the front location in increasing the lift coefficient at pre-stall angles of attack  $\alpha$  as little flow separation occurs near the rear location, allowing the induced jet to directly inject momentum into the separated flow. As  $\alpha$  increased, the flow separation point moved toward the leading edge of the airfoil and, consequently, the front SJA location proved superior for controlling leading-edge flow separation, resulting in enhanced aerodynamic characteristics of the airfoil (see Figure 12 in Reference [46]). Overall, the upstream location was reported to be more efficient in delaying the stall of airfoil. Tang et al. [167] also studied two chordwise SJA locations  $x = 23\%$  and  $43\%$  for a national aeronautics and space administration (NASA) straight-wing model at a Reynolds number of  $Re_c = 120\,000$  and a range of angles of attack  $5^\circ < \alpha < 25^\circ$ , where the SJA was operated at several reduced frequencies  $f^+$ , reporting that the front SJA array was more effective than the rear one (See Figure 7 in Reference [167]).

Amitay et al. [114,168] investigated the manipulation of global aerodynamic forces on a two-dimensional circular cylinder model having a pair of surface-mounted SJAs, for a range of Reynolds numbers up to  $Re_D = 131\,000$  and SJA locations at circumferential angles  $0 < \theta < 180^\circ$ . A schematic of their experimental setup is shown in Figure 11a. The smoke visualizations revealed that the interaction between the synthetic jet and the boundary layer led to the formation of closed recirculation regions, which could displace the local streaklines above the cylinder's top surface, delaying flow separation (see Figures 5 and 7 in Reference [114]). When the SJAs were positioned at  $\theta = 0^\circ$ , the circumferential pressure distribution remained nearly unchanged, indicating that the momentum coefficient was too low to affect the flow significantly. As  $\theta$  increased, the effect of the SJAs on the pressure distribution became more pronounced, with a local minimum appearing in the pressure coefficient distribution around the SJAs location compared to the baseline flow (see Figure 2 in Reference [168]). For  $\theta < 90^\circ$ , the static pressure between the front stagnation point and the separation point continued to decrease as  $\theta$  increased. Of particular note were the changes in the base pressure of the cylinder between the top and bottom separation points, signifying the effect of actuation on the pressure drag (see Figure 10 in Reference [114]). For  $\theta > 90^\circ$ , downstream of the separation point of the baseline flow, the pressure distribution shifted, exhibiting a second local minimum in the static pressure upstream of the separation zone on the unforced lower half of the cylinder. When  $\theta = 110^\circ$ , the two minima in the pressure distribution were nearly identical and symmetric, indicating an approximately zero lift force at this angle. For large enough values of  $\theta$ , the pressure distribution near the separation point on the forced side became nearly indistinguishable from that of the baseline flow. The SJAs seemed to influence only the unforced lower half of the cylinder, indicating a reversal in the direction of the lift force (see Figure 11 in Reference [114]). Eventually, for substantially large values of  $\theta$ , when

the SJAs were located near the wake, the pressure distributions for both the forced and unforced flows became nearly identical. A remarkable finding from the studies by Amitay et al. [114,168] is that the lift force can be entirely nullified or reversed simply by altering the circumferential position of the SJAs. These studies also confirm that when excitation is applied to the stable flow, the disturbances decay before becoming unstable. In contrast, applying excitation near the separation point proves to be an effective control strategy. Tensi et al. [44] studied the flow over a two-dimensional circular cylinder at a Reynolds number of  $Re_D = 100\,000$ , with two SJAs positioned at  $\theta = \pm 112.5^\circ$ , operating at reduced frequencies up to  $f^+ = 0.2$ , close to the natural shedding frequency. Surface oil visualizations showed that the separation line shifted downstream. When only one actuator was active, the trends in the pressure distributions were similar to those reported by Amitay et al. [114,168]. However, when both SJAs were activated, separation was delayed on both sides of the cylinder, resulting in two distinct local minima in the pressure distribution. These minima were nearly identical and symmetric, indicating an almost zero lift force (see Figures 7 and 11 in Reference [44]).



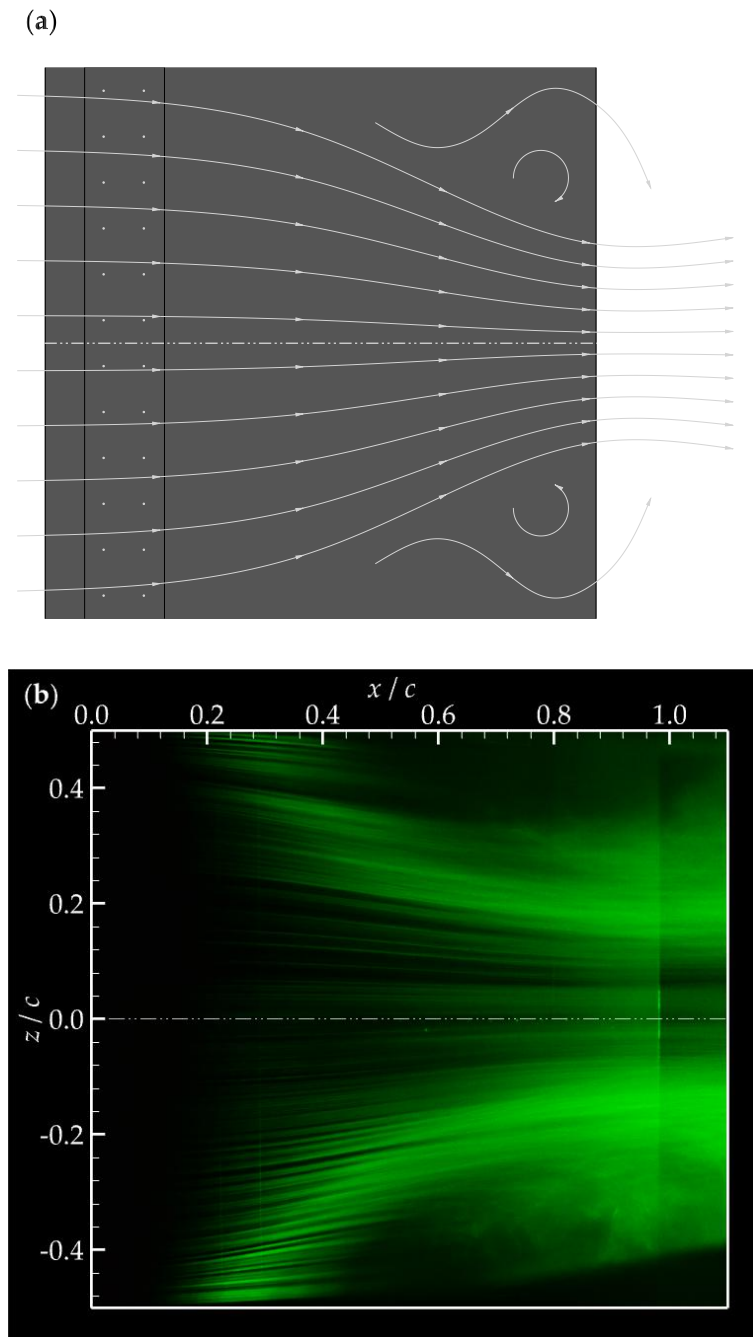
**Figure 11.** Schematic drawings of SJA location for (a) a two-dimensional circular cylinder, studied by Amitay et al. [114,168] and Glezer et al. [119], and (b) an instrumented NACA 0025 airfoil model used by Feero et al. [169].

The study by Feero et al. [162] on a NACA 0025 airfoil, shown in Figure 11b, considered four chordwise SJA locations  $x^+$  around the mean separation point  $x_s^+$ , specifically  $x^+ - x_s^+ = -4.3\%$ ,  $-1.3\%$ ,  $1.3\%$ , and  $4.3\%$ . The results indicated that once a certain blowing ratio was achieved, the benefits of control saturated for both drag reduction and lift increase. A monotonic decrease in the threshold blowing ratio required to fully reattach the flow, along with an increase in the lift-to-drag ratio, was observed as the slot location moved upstream, with the most upstream location proving to be the most effective, both by requiring the lowest threshold blowing ratio and producing the largest lift-to-drag ratio. Zhao et al. [46] investigated two chordwise SJA locations,  $x^+ = 15\%$  and  $40\%$ , for a NACA 0021 airfoil, again concluding that the jet positioned closer to the leading edge of the airfoil was more effective in delaying stall. The analyses by Taylor and Amitay [108] for the pitching NREL S809 blade, with two chordwise SJA locations at  $x^+ = 10\%$  and  $20\%$ , revealed that the forward jet location consistently performed better in reducing hysteresis at any given momentum coefficient  $C_\mu$  and reduced frequency  $f^+$  (see Figure 8 in Reference [108]). Still, the rear SJA location produced a higher lift coefficient during most of the pitching cycle. Therefore, if the goal is to enhance the lift coefficient, the rear jet location was recommended (see Figure 7 in Reference [108]).

#### 4.5. Effects of Clustering

SJAs are typically smaller than the geometric scales of the body they are intended to control, so they are often arranged in arrays to cover longer spans for more effective flow control [170,171]. For an array of SJAs, the stability of flow structures is crucial for enabling effective mixing of low- and high-momentum fluid across the entire span of the controlled geometry. Feero et al. [169] employed tuft and oil visualizations to examine the shape and spanwise extent of the reattached flow over

a NACA 0025 airfoil caused by a high-AR rectangular SJA across a range of reduced excitation frequencies  $f^+$  and blowing ratios  $C_b$  at a constant  $\alpha = 12^\circ$  and  $Re_c = 125\,000$ . The surface flow visualizations showed that the spanwise extent of the reattached flow narrows toward the trailing edge of the airfoil, a phenomenon described as flow contraction toward the airfoil centerline, which is also illustrated in Figure 12.



**Figure 12.** Contraction of the controlled flow towards the airfoil centerline showcased by (a) a schematic drawing of the SJA array and the streamlines and (b) a smoke visualization image adapted from Ho and Machado [172].

In the work of Feero et al. [169], the size and shape of the reattached region remained unchanged with varying  $f^+$  at  $C_b = 1$ . However, at a constant  $f^+ = 47$ , as  $C_b$  increased from 1 to 2.5, the contraction of the attached flow decreased, resulting in a larger spanwise extent of the attached flow.

These observations suggest that measurement techniques examining lift and drag improvements solely at the mid-span may fail to capture the full effects occurring across the entire span, which could result in inaccurate assessments of parameters. Also, note that the blowing ratio  $C_b$  was used by Feero et al. [169] as a measure of jet strength instead of the momentum coefficient  $C_\mu$  since the SJA was essentially two-dimensional. Machado et al. [49,173] utilized smoke wire visualization to investigate the three-dimensionality of the reattached flow over the same NACA 0025 airfoil model as in Feero et al. [169] at  $\alpha = 10^\circ$  and  $Re_c = 100\,000$ . The airfoil was equipped with an array of circular SJAs instead, operating at a constant momentum coefficient of  $C_\mu = 0.2\%$  and two burst-modulated reduced frequencies  $f^+ = 1.18$  and  $f^+ = 11.76$ . Although the contraction phenomenon was observed at both frequencies, in the low-frequency case, the contraction was sharper and occurred at various chordwise locations. In contrast, the high-frequency case resulted in a more gradual contraction along the span. The results indicated that the effective control length is confined to about 40% of the array width, significantly decreasing the sectional lift coefficient as the distance from the mid-span increases.

Clustering SJAs introduces additional parameters, such as phase differences and spacing between individual SJAs, further expanding the complex parameter space. The studies by Liddle et al. [174], Liddle and Wood [175], Wen et al. [176], and Wen and Tang [177] explored the impact of phase differences,  $\Delta\phi = 0^\circ$ – $270^\circ$  in  $90^\circ$  increments, between in-line twin circular SJAs in laminar and turbulent boundary layers over a flat plate. These investigations employed a variety of experimental techniques, including constant temperature anemometry (CTA) [174,175], oil-flow visualization [174], stereoscopic dye visualization [176,177], and PIV [176,177]. In both studies by Liddle et al. [174] and Liddle and Wood [175], power spectral analysis of the downstream velocity time-histories revealed a distinct difference in  $\Delta\phi = 270^\circ$  case, where the prominent peak occurred at twice the actuation frequency, as opposed to the three other instances in which the prominent peak occurred at the actuation frequency. Additionally, the time-averaged streamwise velocity contours for  $\Delta\phi = 90^\circ$  featured more abrupt changes, indicating greater penetration into the boundary layer (see Figure 10 in Reference [174] or Figure 4 in Reference [175]). These findings were confirmed later by Wen et al. [176], Wen and Tang [177]. Both studies identified, three types of vortex structures: one combined vortex at  $\Delta\phi = 90^\circ$ , two completely separated hairpin vortices at  $\Delta\phi = 270^\circ$ , and partially interacting vortex structures at  $\Delta\phi = 0^\circ$  and  $180^\circ$  (see Figure 5 in Reference [176] or Figure 4 in Reference [177]). The strongest structure was the single combined vortex at  $\Delta\phi = 90^\circ$ , which exhibited the greatest penetration into the boundary layer. At  $\Delta\phi = 270^\circ$ , the resulting flow structures resembled a train of completely separated hairpin vortices, effectively doubling the frequency of the hairpin vortices produced by a single SJA. Overall, the results from the above studies indicate the potential for phase angle manipulation to improved flow control. It should be noted that the most effective phase difference between in-line SJAs also depends on the dimensionless jet-to-jet spacing  $s^+$  (usually spacing is normalized by the orifice width). For clarity, consider the study by Zhao et al. [46], where the effects of phase delay and combinations of pitch angles for in-line dual arrays on a NACA 0021 airfoil were investigated. At the angle of attack  $\alpha$  just after stall, the phase difference of  $\Delta\phi = 180^\circ$  could significantly increase the lift coefficient and help prevent flow separation (see Figure 13 in Reference [46]). On the other hand, the control effects due to combined pitch angles were more complex. However, overall, when the pitch angle of the upstream SJA was lower, the dual jet actuators provided better control over airfoil stall compared to a single actuator (see Figure 16 in Reference [46] for a detailed report on combined pitch angles).

Fewer studies have explored the effects of spacing  $s^+$  and phase difference  $\Delta\phi$  in the parallel clustering of SJAs within a crossflow. For steady round jets having a parallel twin-jet configuration in a flat plate boundary layer, a detailed investigation was conducted by Zang and New [178], examining various spacing  $s^+$  and velocity ratio values, using laser-induced fluorescence (LIF) and PIV. The study demonstrated that each jet in the cluster achieved greater entrainment and larger jet half-widths compared to a single jet in crossflow. Reducing  $s^+$  caused the twin jets to interact with each other closer to the orifice exit. Similar to the enhancement mechanism in quiescent flow [114], the inner vortices

were observed to move toward each other, neutralizing due to their oppositely signed vorticity and merging into a single counter-rotating vortex pair, which prevailed further downstream (see Figures 9 and 10 in Reference [178]). The study by Vasile and Amitay [143] on a  $30^\circ$  swept-back NACA 4421 wing equipped with three parallel rectangular SJAs with a spanwise spacing of  $s^+ = 43$  also demonstrated that, when the spanwise spacing between the jets is sufficiently large, there is minimal interaction between the jets. The resulting flow field, formed by the simultaneous activation of all three jets, was essentially a superposition of the flow fields produced when each jet was activated individually. More recently, Jankee and Ganapathisubramani [179] investigated the interaction of parallel  $AR = 13$  rectangular twin jets with a turbulent boundary layer over a flat plate, for a range of spacing  $s^+$  and phase differences  $\Delta\phi$ , while keeping all other geometrical and operational parameters constant. A limit in spacing was identified, beyond which any further increase causes the twin jets to behave as two independent synthetic jets, which also aligned with the findings of Watson et al. [180] observed under quiescent conditions. Similar to the observations of Zang and New [178], when the spacing  $s^+$  was sufficiently small, the jets interacted with each other, with the inner vortex of each counter-rotating vortex pair canceling out due to their opposite vorticity signs and the remaining part of the vortices coalescing into a single vortex pair (see Figure 4 in Reference [179]). For the smallest spacing of  $s^+ = 2$  with a phase difference  $\Delta\phi \neq 0$ , the jets exhibited vectoring toward the actuator leading in phase, similar to the behavior observed in quiescent flow conditions [114,181,182] (see Figure 6 in Reference [179]). At a phase difference of  $\Delta\phi = 78^\circ$ , the influence of the crossflow caused the vortical structures from the leading SJA to convect downstream before the lagging SJA reached peak blowing. As a result, the interactions were minimal, and the flow field of the twin jets in this scenario became analogous to that of a single SJA operating at twice the actuation frequency, the doubling effect. The studies mentioned above highlight the potential of clustering parameters  $s^+$  and  $\Delta\phi$  for enhanced control schemes. A notable example can be found in the work by Amitay et al. [114] on a circular cylinder. When the SJAs were positioned on the downstream edge at  $\theta = 180^\circ$ , substantial momentum was necessary to influence the wake. However, with the SJAs operated at  $\Delta\phi = 120^\circ$ , the downward vectoring of the jets caused a downward shift in the entire wake and a simultaneous displacement of the front stagnation point. This led to a decrease in spacing between the streaklines above the cylinder and an increase in spacing below it, indicating a change in circulation and lift generation (see Figures 8 and 9 in Reference [114]).

#### 4.6. Open- and Closed-loop Control

Given the focus on flow control applications, experimental and numerical studies involving airfoils and wing models with open-loop control were reviewed and presented in Table 1 for comparison. In studies employing an open-loop control system, the SJA parameters are preset and performance is evaluated afterward. In many real-world scenarios, the control scheme must be robust to variations in design conditions and, in some cases, even adaptive to ensure optimal performance. Implementing closed-loop systems is an emerging trend in AFC, both in experimental [4,183] and numerical [184, 185] works. An effective sensing strategy is essential for expanding open-loop control systems to closed-loop configurations. Researchers have proposed several approaches for this, including visual feedback [4,28,186], pressure sensing [4,183,187,188], and shear sensing [5]. Closed-loop control studies using either model-based or model-free methods hold significant promise for the field. While a detailed examination of these approaches is beyond the scope of this article, readers interested in machine learning approaches for AFC are directed to the recent review by Li et al. [189].



**Table 1.** Summary of the test parameters for some studies on flow control over airfoils and wings using SJAs.

Reference	Geometry	Method	Airfoil parameters	SJA parameters <sup>1</sup>
Zhao et al. [46]	AR = 1.8 NACA 0021	Experimental, Force measurement, PIV	$Re_C < 300\,000$ $-6^\circ < \alpha < 30^\circ$	$0.1\% < C_\mu < 0.9\%$ $30^\circ < \gamma < 90^\circ$ <sup>2</sup> $1.6 < f^+ < 8$ $x^+ = 15\%, 40\%$ $\Delta\phi = 0^\circ, 180^\circ$
Sahni et al. [76]	AR = 5.33 NACA 4421	Experimental and numerical, Stereoscopic PIV	$Re_C = 100\,000$ $\alpha = 0^\circ$	$0.2 < C_b < 1.2$ AR = 21.33 <sup>3</sup> $f^+ = 38.1$ $x^+ = 17\%$ $s^+ = 17.87$
Elimelech et al. [142]	AR = 4 30° swept-back NACA 4421	Experimental, Stereoscopic PIV	$Re_C = 100\,000$ $\alpha = 9^\circ, 15.5^\circ$	$C_b = 0.8, 1.2$ AR = 28.8 $f^+ = 46.67$ $x^+ = 17\%$
Vasile and Amitay [143]	AR = 4 30° swept-back NACA 4421	Experimental, Stereoscopic PIV	$Re_C = 100\,000$ $\alpha = 13.5^\circ$	$C_b = 1.2$ AR = 19 $f^+ = 45.33$ $x^+ = 17\%$ $s^+ = 43$
Amitay and Glezer [144]	Unconventional symmetric airfoil with circular leading edge	Experimental, Pressure measurement, PIV, HWA	$Re_C = 310\,000$ $\alpha = 17.5^\circ$	$C_\mu = 0.35\%$ AR = 280 $0.95 < f^+ < 20$ $\theta = 60^\circ$ $s^+ = 5$
Amitay and Glezer [151]	Unconventional symmetric airfoil with circular leading edge	Experimental, Smoke visualization, Pressure measurement, PIV	$Re_C = 310\,000$ $\alpha = 17.5^\circ, 20^\circ$	$0.35\% < C_\mu < 0.54\%$ AR = 280 $0.27 < f^+ < 10$ DC = 25% <sup>4</sup> $\theta = 42^\circ, 60^\circ$ $s^+ = 5$
Glezer et al. [119]	Unconventional symmetric airfoil with circular leading edge	Experimental, Smoke visualization, HWA	$Re_C = 310\,000$ $\alpha = 15^\circ$	$C_\mu = 0.18\%$ AR = 280 $0.7 < f^+ < 10$ $\theta = 60^\circ$ $s^+ = 5$
Amitay and Glezer [161]	Unconventional symmetric airfoil with circular leading edge	Experimental, Smoke visualization	$Re_C = 310\,000$ $\alpha = 17.5^\circ$	$C_\mu = 0.35\%$ AR = 280 $f^+ = 10$ $x^+ = 6.2\%$
Goodfellow et al. [155]	AR = 2.95 NACA 0025	Experimental, Smoke visualization, Pressure measurement, HWA	$Re_C = 100\,000$ $\alpha = 5^\circ$	$0 < C_\mu < 1.2\%$ AR = 280 $30 < f^+ < 90$ $x^+ = 33.67\%$
Feero et al. [102]	AR = 2.95 NACA 0025	Experimental, Smoke visualization, Pressure measurement, HWA	$Re_C = 100\,000$ $\alpha = 10^\circ$	$0 < C_\mu < 3.72\%$ AR = 280 $f^+ = 0.84, 9.9, 58$ DC = 50% $x^+ = 19\%$
Buchmann et al. [41]	AR = 5.1 NACA 0015	Experimental, Time-resolved PIV	$Re_C = 30\,000$ $\alpha = 18^\circ$	$C_\mu = 0.14\%$ AR = 3066.67 $f^+ = 1.3$ $x^+ = 0$
Taylor and Amitay [108]	AR = 3.1 NREL S809	Experimental, Force measurement, Stereoscopic PIV	$Re_C = 220\,000$ $\bar{\alpha} = 8^\circ, 14^\circ, 20^\circ$ $\alpha_a = 3^\circ, 5.5^\circ, 10^\circ$ <sup>5</sup> $0.0015 < k_f < 0.015$ <sup>6</sup>	$0 < C_\mu < 0.44\%$ AR = 20 $f^+ = 1.2, 2.5, 3.7$ $20\% < DC < 100\%$ $x^+ = 10\%, 20\%$
Rice et al. [164]	AR = 1.64 NREL S817	Experimental, Force measurement, pressure measurement, Stereoscopic PIV	$Re_C = 375\,000$ $-5^\circ < \alpha < 25^\circ$	$C_\mu = 1.2\%$ $\gamma = 45^\circ$ AR = 12 $f^+ = 1, 4$ DC = 35% $x^+ = 35\%$
Rice et al. [165]	AR = 1.64 NREL S817	Experimental, Force measurement, pressure measurement, Stereoscopic PIV	$Re_C = 375\,000$ $\bar{\alpha} = 15^\circ, 19^\circ$ $\alpha_a = 3^\circ, 5^\circ, 7^\circ$ $k_f = 0.025, 0.05$	$C_\mu = 1.2\%$ $\gamma = 45^\circ$ AR = 12 $f^+ = 0.7, 25$ DC = 35% $x^+ = 35\%$
Rice et al. [153]	AR = 1.64 NREL S817	Experimental, Force measurement, pressure measurement, Stereoscopic PIV	$Re_C = 375\,000$ $\bar{\alpha} = 15^\circ, 19^\circ$ $\alpha_a = 3^\circ, 5^\circ$ $k_f = 0.025$	$C_\mu = 1.2\%$ $\gamma = 45^\circ$ AR = 12 $f^+ = 1.4, 22.4$ DC = 35% $x^+ = 15\%, 35\%$
Margalit et al. [166]	60° swept-back semi-span delta wing	Experimental, Force measurement, pressure measurement, PIV	$Re_C = 117\,000, 234\,000, 350\,000$ $25^\circ < \alpha < 45^\circ$	$0 < C_\mu < 3.8\%$ $0 < f^+ < 82$ $0 < DC < 100\%$ $x^+ = 0$ <sup>7</sup> $0^\circ < \Delta\phi < 360^\circ$
Amitay et al. [159]	Unconventional symmetric airfoil with circular leading edge	Experimental, Pressure measurement, HWA	$Re_C = 310\,000, 525\,000, 725\,000$ $5^\circ < \alpha < 20^\circ$	$0 < C_\mu < 0.35\%$ AR = 280 $0.95 < f^+ < 20$ $-60^\circ < \theta < 60^\circ$ $s^+ = 5$



Table 1. Cont.

Tang et al. [167]	AR = 1.42 NASA/Langley LS(1)-0421MOD wing	Experimental, Force measurement, Tomographic PIV, HWA	$Re_C = 120\,000$ $5^\circ < \alpha < 25^\circ$	$C_b = 0.12, 0.15, 0.22$ $f^+ = 3.6, 7.2, 10.8$ $x^+ = 23\%, 43\%$ $s^+ = 2^8$
Salunkhe et al. [190]	AR = 1.42 NASA/Langley LS(1)-0421MOD wing	Experimental, Tomographic PIV	$Re_C = 120\,000$ $\alpha = 19^\circ$	$C_\mu = 0.0042\%$ $C_b = 0.22$ $f^+ = 7.2$ $x^+ = 23\%$ $s^+ = 2^8$
Holman et al. [191]	AR = 1.92 NACA 0025	Experimental, PIV, Laser Doppler velocimetry (LDV)	$Re_C = 100\,000$ $\alpha = 12^\circ$	AR = 203.2 $f^+ = 19.05$ $x^+ = 3\%, 30\%$ $0^\circ < \Delta\phi < 360^\circ$
Yen and Ahmed [192]	AR = 1.45 NACA 0020	Experimental, Pressure measurement	$Re_C = 125\,000$ $\bar{\alpha} = 0^\circ, 5^\circ, 10^\circ, 20^\circ$ $\alpha_a = 20^\circ, 25^\circ, 30^\circ, 40^\circ$ $\lambda = 1.6, 2, 2.4, 2.9^9$	$C_\mu = 0.043\%, 7.5\%, 10\%$ $f^+ = 1$ $x^+ = 2.8\%$
Feero et al. [162]	AR = 2.95 NACA 0025	Experimental, Pressure measurement, PIV, HWA	$Re_C = 100\,000$ $\alpha = 12^\circ$	$0 < C_b < 3$ AR = 588 $f^+ = 1, 2, 14, 58$ DC = 50 % $x^+ = 8.7\%, 11.7\%, 14.3\%, 17.3\%$
Feero et al. [169]	AR = 2.95 NACA 0025	Experimental, Smoke, tuft, and oil flow visualizations, Pressure measurement	$Re_C = 125\,000$ $\alpha = 12^\circ$	$C_b = 1, 2, 2.5$ AR = 588 $f^+ = 0.5, 1, 2, 12, 47$ $x^+ = 11.7\%$
Machado et al. [49]	AR = 2.95 NACA 0025	Experimental, Smoke visualization	$Re_C = 125\,000$ $\alpha = 10^\circ$	$C_\mu = 0.2\%$ $f^+ = 1.18, 11.76$ DC = 50 % $x^+ = 10.7\%$
Machado et al. [173]	AR = 2.95 NACA 0025	Experimental, Smoke visualization, PIV, HWA	$Re_C = 100\,000$ $\alpha = 10^\circ$	$C_\mu = 0.2\%$ $f^+ = 1.18, 11.76$ DC = 50 % $x^+ = 10.7\%$
Ciobaca et al. [52]	DLR-F15	Numerical, URANS - SA & $k-\omega$ SST	$Re_C = 1\,000\,000$ $\alpha = 3^\circ$	$C_\mu = 0.56\%$ DC = 50 % $f^+ = 0.5$
Zhao et al. [193]	VR-7B & OA212	Numerical, URANS - $k-\omega$ SST	$Re_C = 2\,700\,000$ $\alpha = 10^\circ-25^\circ$	$C_\mu = 0.01\%-0.9\%$ $f^+ = 40$ $x^+ = 10\%, 50\%$
Shahrabi [194]	NACA 0015	Numerical, URANS - $k-\omega$ SST & LES	$Re_C = 250\,000-1\,000\,000$ $\alpha = 0^\circ-22^\circ$	$C_\mu = 0-11\%$ $f^+ = 0-2$ $x^+ = 10\%, 66\%$
Tousi et al. [195]	SD7003	Numerical, URANS-SA & LES	$Re_C = 60\,000$ $\alpha = 14^\circ$	$C_\mu = 0.3\%-0.53\%$ $f^+ = 1, 1.6, 2.6$ $x^+ = 0.5\%-1\%$
Li and Yi [196]	NREL S809	Numerical, LES	$Re_C = 1\,000\,000$ $\alpha = 3^\circ-17^\circ$	$f_m = 25\text{ Hz}-200\text{ Hz}$ DC = 1 %-100 % $x^+ = 2\%$
You and Moin [197]	NACA 0015	Numerical, LES	$Re_C = 896\,000$ $\alpha = 16.6^\circ$	$C_\mu = 1.23\%$ $f^+ = 1.284$ $x^+ = 12\%$
Itsariyapinyo and Sharma [198]	NACA 0015	Numerical, LES	$Re_C = 110\,000$ $\alpha = 0^\circ-12^\circ$	$C_\mu = 0.44\%-6.88\%$ $f^+ = 3.0$ $x^+ = 13\%$
Kitsios et al. [199]	NACA 0015	Numerical, LES	$Re_C = 30\,000$ $\alpha = 18^\circ$	$C_\mu = 0.0213\%$ $f^+ = 1.3$ $x^+ = 0\%$
De Giorgi et al. [200]	NACA 0015	Numerical, DNS	$Re_C = 896\,000$ $\alpha = 16.6^\circ$	$C_\mu = 1.23\%$ $f^+ = 0.65-1.4$ $x^+ = 12\%$
Zhang and Samtaney [201]	NACA 0018	Numerical, DNS	$Re_C = 10\,000$ $\alpha = 10^\circ$	$C_\mu = 0.0213\%$ $f^+ = 0.5, 1, 4$ $x^+ = 13\%$

<sup>1</sup> Trivial SJA parameters, such as  $\gamma = 90^\circ$  or  $\Delta\phi = 0^\circ$ , are not reported.

<sup>2</sup> Parameters focused on in each study are Highlighted in blue.

<sup>3</sup> Aspect ratio is reported for rectangular SJAs in this table.

<sup>4</sup> Duty cycle is only reported for burst modulation studies.

<sup>5</sup> In the case of pitching airfoils, both mean and amplitude of  $\alpha$  may be reported.

<sup>6</sup> For pitching airfoils, the reduced angular pitch frequency  $k_f = \pi f X_f / U_\infty$  may be reported.

<sup>7</sup> In this case, SJAs were distributed along the leading edge of the wing.

<sup>8</sup> Due to nested SJA clustering, only the smallest spacing is reported here.

<sup>9</sup> For turbine blades, blade speed ratio  $\lambda$  may be reported.

## 5. Conclusions

SJAs offer significant advantages for flow control due to their ability to inject momentum without an external fluid supply, reducing system complexity, and weight. Technological advancements have made them lightweight, easy to maintain, and highly responsive, spurring increased research and publications on SJAs. This article reviewed SJA working mechanisms and how operational and geometrical factors influence flow fields in quiescent and crossflow conditions. Key studies were summarized, highlighting their contributions.

**Author Contributions:** Conceptualization, A.S., H.H., E.E., P.E.S.; formal analysis, A.S., H.H.; investigation, A.S., H.H.; resources, E.E., P.E.S.; data curation, A.S., H.H.; writing—original draft preparation, A.S., H.H.; writing—review and editing, A.S., H.H., E.E., P.E.S.; supervision, E.E., P.E.S.; project administration, E.E., P.E.S.; funding acquisition, P.E.S. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by Natural Sciences and Engineering Research Council of Canada (NSERC) grant number RGPIN-2022-03071 and the Digital Research Alliance of Canada (4752).

**Data Availability Statement:** No new data were created or analyzed in this study.

**Conflicts of Interest:** The authors declare no conflicts of interest.

## Abbreviations

The following abbreviations are used in this manuscript:

AFC	Active Flow Control
AR	Aspect Ratio
BLC	Boundary Layer Control
CTA	Constant Temperature Anemometry
DC	Duty Cycle
DNS	Direct Numerical Simulation
HWA	Hot-Wire Anemometry
LDV	Laser Doppler Velocimetry
LES	Large Eddy Simulation
LIF	Laser-Induced Fluorescence
LSB	Laminar Separation Bubble
NACA	National Advisory Committee for Aeronautics
NASA	National Aeronautics and Space Administration
NREL	National Renewable Energy Laboratory
PIV	Particle Image Velocimetry
SJA	Synthetic Jet Actuator
SJBLI	Synthetic Jet and Boundary Layer Interaction
TLC	Temperature-sensitive Liquid Crystal
URANS	Unsteady Reynolds-Averaged Navier-Stokes
VR	Velocity Ratio
ZMB	Zero Mass Blowing
ZNMF	Zero-Net Mass-Flux

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