

## Article

# Challenges with Harmonic Compensation at a Remote Bus in Offshore Wind Power Plant

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**Abstract:** The interaction between the grid network and the offshore wind power plant (WPP) network can lead to the amplification of certain harmonics and potentially resonant conditions. Offshore WPP should limit the increment of harmonic voltage distortion at the point of connection to the grid network as well as within their internal network. The harmonic distortion should be limited within the planning level limits using harmonic compensation, which is usually achieved by using static filters. In this paper an active damping compensation strategy with a STATCOM using emulation of resistance at the harmonic frequencies of concern is analysed. Such a compensation is effective for the local bus, though the performance is not guaranteed at the remote bus. This paper investigates the challenges associated with remote harmonic compensation in the offshore WPP, which is connected to the onshore grid through long high-voltage cables and transformers. First, the harmonic distortion and the compensating effects of the filter are theoretically assessed. Afterwards, they are demonstrated using harmonic propagation studies and time domain simulations in PSCAD.

13

**Keywords:** harmonic distortion; active power filter; resonance; damping; wind power plants

## 15 1. Introduction

16 Several large offshore wind power plants (WPP) have been installed in Europe and many more  
17 are under different stages of development. These usually comprise of type III or type IV wind turbines  
18 (WT) with power electronic converters and are connected to the ac network through High Voltage AC  
19 (HVAC) or High Voltage DC (HVDC) transmission systems. HVAC transmission systems are widely  
20 used in large scale WPPs closer to the shore, within 50-100 km from the shore [1], due to simple  
21 installation and maintenance, higher reliability and less complexity in comparison to HVDC systems.  
22 Anholt, Horns Rev and Nysted WPPs in Denmark and Barrow wind farm in United Kingdom are  
23 some of the WPPs HVAC connection to the grid [2,3].

24 HVAC connection of Offshore Wind Power Plants (WPPs) typically comprise of long submarine  
25 and underground HVAC cables up to the point of grid connection and step up transformers.  
26 Meanwhile, huge number of medium voltage (MV) submarine cables of network collection of  
27 wind turbines should not be overlooked. The combination of the transformer inductance and the  
28 submarine cable capacitance might produce a resonant circuit, which may cause amplification of  
29 harmonics [4]. Harmonic emission level of power electronic based generation sources should meet

30 the requirements mentioned in the relevant standards including recommended (IEEE and IEC) and  
31 planning (G5/4-1) limits [5–7].

32 Power electronic converters and non-linear loads produce the major part of grid harmonics. Grid  
33 background harmonic at a particular terminal reflects the overall impact of aforementioned harmonic  
34 sources at that specific bus, e.g. the Point of Connection (POC). Existence of harmonics in the grid is  
35 inevitable even in the absence of WPP. Connection of WPP to the grid, influences the effective grid  
36 impedance at POC. Depending on the interaction between the WPP and grid impedances, there may  
37 be an amplification or an attenuation of the harmonic voltage distortion. New resonant modes may  
38 appear and/or the existing resonant modes may move to undesirable frequencies, thereby amplifying  
39 the harmonic distortion leading to poor power quality at the POC exceeding the permissible levels of  
40 harmonic distortion. Moreover, the injection of harmonics by built-in power electronic converters of  
41 WPPs, may also worsen the situation.

42 Current work addresses magnification of grid background harmonic due to the interaction  
43 between the WPP and grid impedances. The main focus is devoted to the grid background harmonics  
44 as the main source of harmonics and the share of Wind Turbines (WTs) in current harmonic injection is  
45 considered as future works. Later on, active damping of harmonics is performed by the emulation of  
46 resistive behaviour by the STATCOM at particular frequencies. The research findings confirm that the  
47 harmonic compensation is efficient at the local bus. However, its performance is not guaranteed at the  
48 remote buses. Due to practical considerations and current state of the art of STATCOM technology,  
49 the STATCOM is not connected to the high voltage buses (POC and PCC) close to the grid. To meet the  
50 requirements of grid codes associated with harmonics, the harmonic level should be within the limits  
51 specified at the PCC or POC which appear to be the remote bus with respect to the point of connection  
52 of the STATCOM. This paper investigates the challenges and difficulties in harmonic mitigation and  
53 compliance with the power quality at such remote buses.

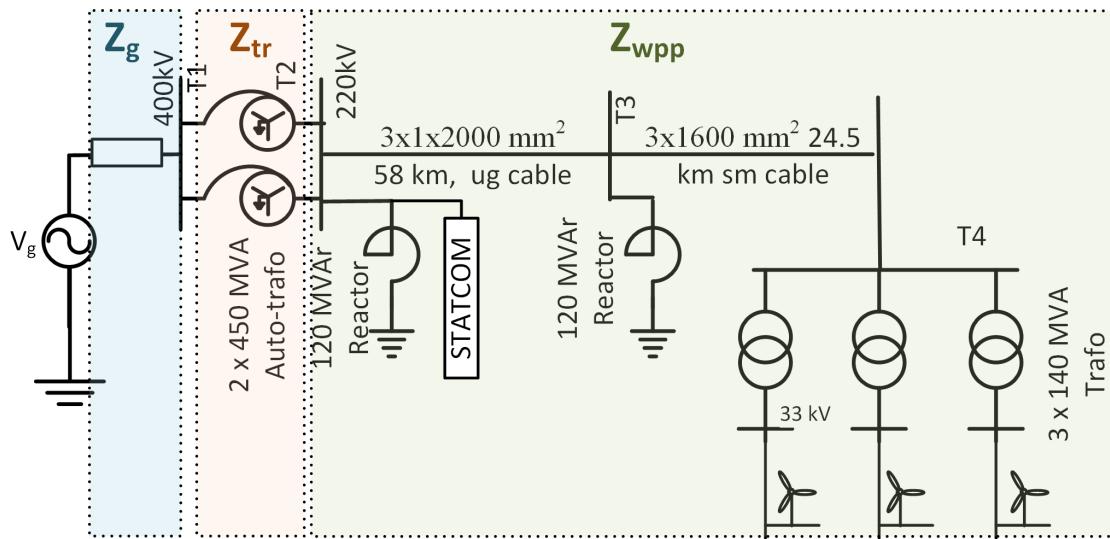
54 This paper is organized as follows. The test WPP grid network is presented along with the  
55 mathematical analysis of the amplification or attenuation of harmonics and the effect of harmonic  
56 compensation in section 2. The effect of harmonic compensation upon the harmonic impedance of  
57 WPP network is illustrated in section 3. The Nyquist criterion is applied to assess the overall  
58 stability of the compensation strategy in section 4. The results of the harmonic propagation studies  
59 and time domain simulation are presented in section 5. Finally, the paper is concluded in section 6.

## 60 2. Test WPP Grid Network

### 61 2.1. Wind power plant model

62 The Anholt offshore WPP in Denmark with the capacity of 400 MW is chosen as a case study  
63 for harmonic study of WPP network as shown in Figure 1 [8]. Three step up transformers (3x140  
64 MVA, 225/34 kV) connect the WPP collection network to the submarine cable. The submarine cable  
65 size and length are 3\*1600 mm<sup>2</sup> and 24.5 km respectively. It is connected to the underground cable  
66 (3\*2000 mm<sup>2</sup>) with the length of 58 km. The generated power is delivered to the onshore grid using  
67 two units of 450 MVA, 410/233 kV transformers in parallel. Two switched shunt reactors (120 and  
68 240 MVar) are employed to compensate the reactive power of cable capacitance in the submarine and  
69 underground cables, respectively. A STATCOM is connected to the 220 KV bus,  $T_2$  for the dynamic  
70 reactive power compensation as well as the active damping of resonance and mitigation of harmonic  
71 voltage distortion .

72 The medium voltage (MV) cables in the 34-kV collector network of the WPP is collectively  
73 represented by 3 sets of 4x11 km cable of 500 mm<sup>2</sup> at 34 kV voltage level. The capacitance of the MV  
74 cables is selected such that the overall capacitance of resultant cable network remains unchanged.



**Figure 1.** WPP electrical network model.

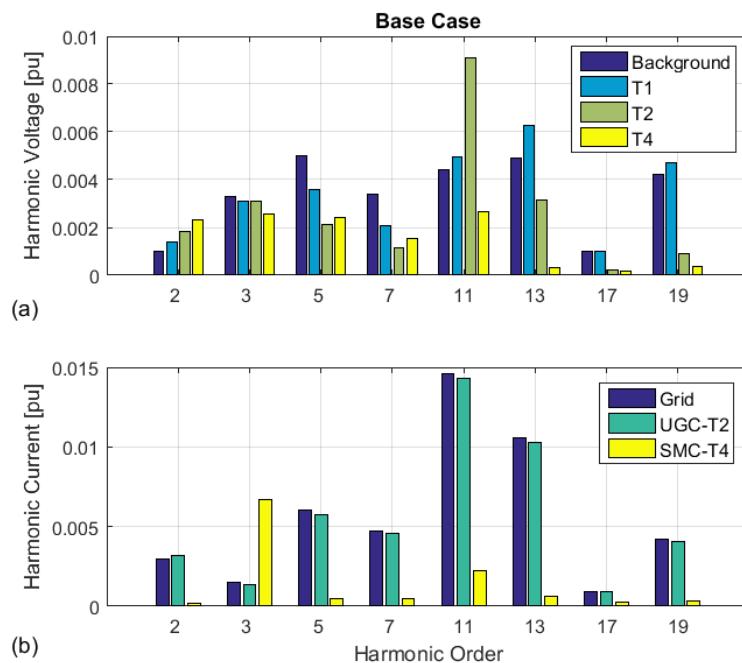
**Table 1.** Base Values.

	Unit	Grid and at $T_1$	At $T_2$ , $T_4$ , and HV Cables
Power	[MW]	400	400
RMS voltage	[kV]	400	220
RMS current	[kA]	577.4	1049.7
Resistance	[ $\Omega$ ]	400	121

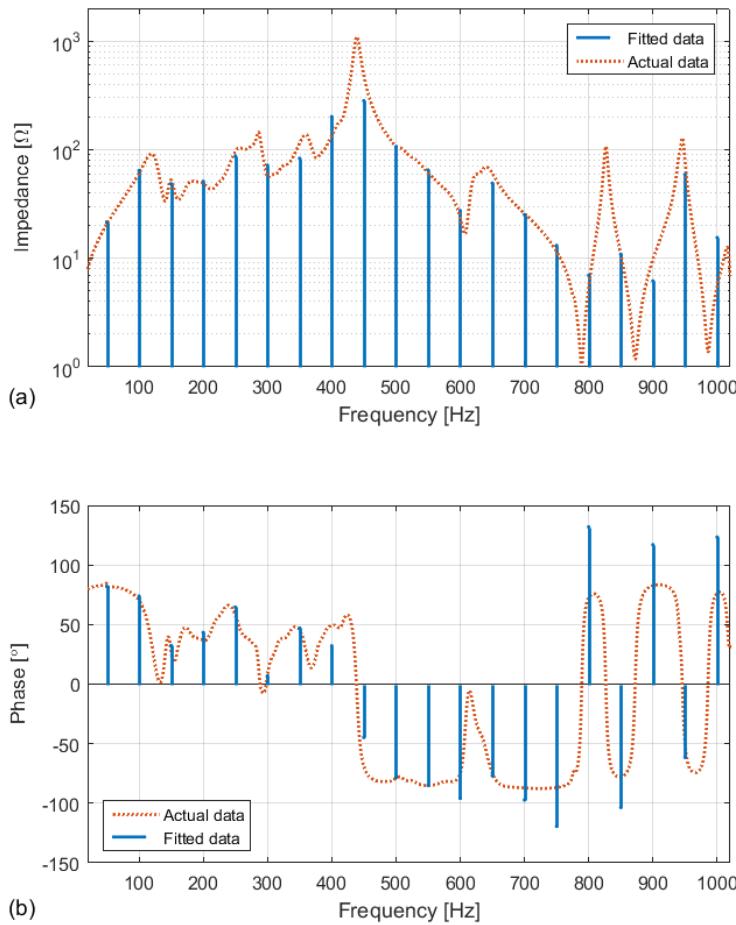
## 2.2. Grid

The main grid is modelled by three phase voltage sources with background voltage harmonics. The grid impedance is considered in series with the voltage source in accordance to the Thévenin equivalent circuit [9]. Figure 2-a represents the magnitude of voltage harmonics at the PCC and other buses ( $T_1$ ,  $T_2$  and  $T_4$ ). Figure 2-b indicates the current harmonic injected by the grid into the WPP in different locations. The bar values are shown in pu calculated according to the base values given in Table 1.

The frequency spectrum of grid impedance is available as magnitude and phase in term of frequency. Although, the aforementioned data can be directly utilized for frequency domain analysis, such as the harmonic propagation studies, it cannot be applied to the time domain simulation studies. In this case the data needs to be transformed to a frequency domain transfer function using vector fitting technique [10]. The frequency sweep data of grid impedance (actual grid impedance data) and the resultant Frequency Dependent Network Equivalent (FDNE) transfer function is shown in Figure 3.



**Figure 2.** . Base case. (a) Background harmonic levels, and the harmonic voltages at  $T_1$ ,  $T_2$  and  $T_4$ , and (b) Harmonic current flow in the grid and the HV cables (UGC: underground cables and SMC:submarine cables) at  $T_1$ ,  $T_2$  and  $T_4$ .



**Figure 3.** Grid impedance characteristics. (a) Magnitude, and (b) Phase angle.

89 2.3. Amplification/Attenuation of harmonic distortion

90 Magnification or attenuation of harmonics at different buses may happen due to the interaction  
 91 between the grid impedance in series with the equivalent impedance of the WPP and its submarine,  
 92 underground cables and collection network. In this study, the 400 kV bus , i.e.  $T_1$  is considered as  
 93 PCC, and thus the objective is to reduce the harmonic distortion at bus  $T_1$ .

94 By excluding the harmonic emission of WTs and considering the grid as the main source of  
 95 harmonic distortion, the amplification of harmonic voltage distortion at buses  $T_1$  and  $T_2$  are given by:

$$A_1 = \frac{V_{1h}}{V_{gh}} = \frac{Z_{tr,h} + Z_{wpp,h}}{Z_{g,h} + Z_{tr,h} + Z_{wpp,h}} \quad \left. \right\}, \quad (1)$$

$$A_2 = \frac{V_{2h}}{V_{gh}} = \frac{Z_{wpp,h}}{Z_{g,h} + Z_{tr,h} + Z_{wpp,h}} \quad \left. \right\},$$

96 where,  $Z_{tr,h}$ ,  $Z_{wpp,h}$  and  $Z_{g,h}$  are the impedance of transformer, WPP and the grid at the  $h^{th}$  harmonic  
 97 order represented in Figure 4. The amplification ratios  $A_1$  and  $A_2$  in (1) versus frequency are plotted  
 98 in Figure 5. Values greater/smaller than one is interpreted as amplification/attenuation. At bus  $T_1$ ,  
 99 the harmonic orders 2<sup>nd</sup>, 9-15<sup>th</sup>, 17<sup>th</sup> and the 19<sup>th</sup> are amplified. At bus  $T_2$ , the 2<sup>nd</sup>, 11<sup>th</sup> and the 12<sup>th</sup>  
 100 harmonic orders are amplified.

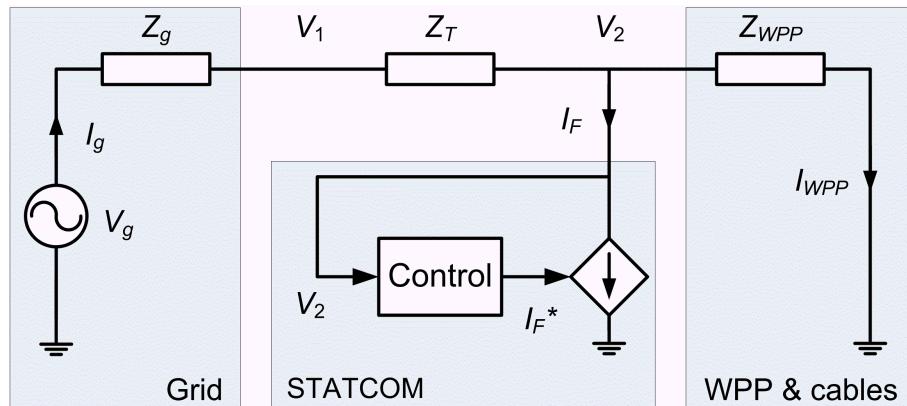


Figure 4. An equivalent single line drawing of the test system.

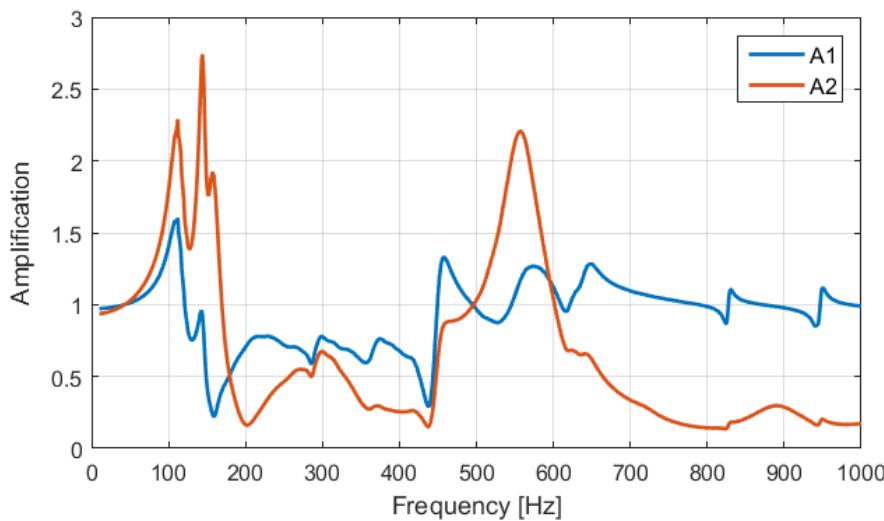
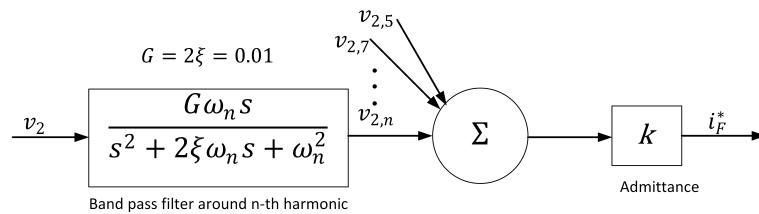


Figure 5. Amplification of the background harmonics in the grid.

101 The amplification of 13<sup>th</sup> harmonic order at  $T_1$  by 1.27 times makes sense due  
 102 to the positive sequence impedance values of,  $Z_{g,13} = (17 - j59) \Omega$  on the grid side and  
 103  $(Z_{tr,13} + Z_{wpp,13}) = (48 + j233) \Omega$  on the WPP side at the bus  $T_1$  when referred to the 400 kV voltage  
 104 base. Typically, the odd harmonics at the 5<sup>th</sup>, 7<sup>th</sup>, 11<sup>th</sup>, 13<sup>th</sup>, 17<sup>th</sup> and 19<sup>th</sup> have a relatively higher  
 105 content in the background harmonics in the grid. Hence, the amplification of these harmonics should  
 106 be checked to the extent feasible.

107 2.4. STATCOM controller for harmonic compensation

108 When a resistor is connected in shunt, it reduces the overall impedance and hence the voltage  
 109 drops. However, it would affect the harmonic as well as the fundamental frequency components.  
 110 Moreover, it leads to high losses and hence connecting a resistor for harmonic compensation is not  
 111 feasible. It is therefore emulated by a STATCOM, which provides reactive power compensation at  
 112 the fundamental frequency and selective harmonic filtering. Figure 6 shows the block diagram of  
 113 the STATCOM controller for the active power filter (APF) functionality. It will be in addition to the  
 114 reactive power regulation, which happens at the fundamental frequency. The aspect of reactive power  
 115 compensation is not described in this paper.



**Figure 6.** STATCOM controller for harmonic compensation.

116 The terminal voltage  $v_2$  is measured at  $T_2$  and the harmonic components are extracted using  
 117 band-pass filters tuned around the desired harmonic frequency orders. Afterwards, the harmonic  
 118 components are added together and multiplied by a constant admittance,  $k$ , to produce the harmonic  
 119 current reference,  $i_F^*$  to provide the harmonic compensation. The individual band pass filter around  
 120 the harmonic frequency,  $\omega_n$ , has the transfer function,

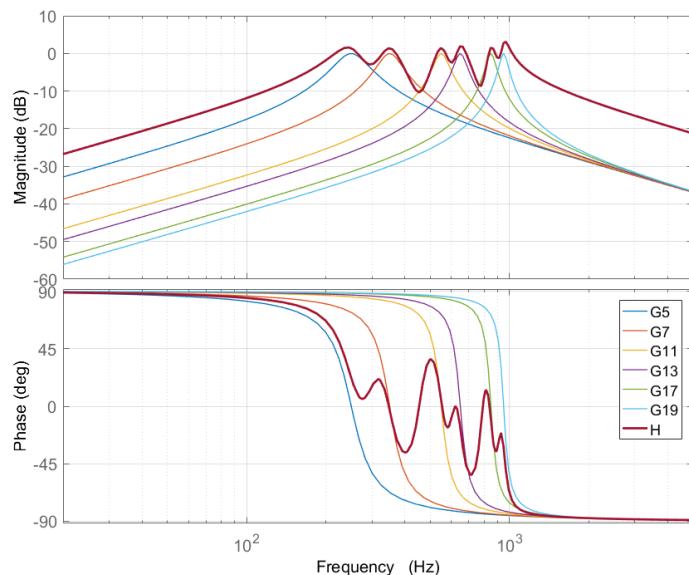
$$HF_n(s) = \frac{G \cdot \omega_n \cdot s}{s^2 + 2 \cdot \xi \cdot \omega_n \cdot s + \omega_n^2}. \quad (2)$$

121 Such a filter is required for each of the individual harmonic orders concerned. Therefore, the  
 122 resultant filter transfer function is,

$$HF(s) = \sum_n^N \frac{2 \cdot \xi \cdot \omega_n \cdot s}{s^2 + 2 \cdot \xi \cdot \omega_n \cdot s + \omega_n^2} \quad (3)$$

123 The frequency vs. magnitude and phase characteristic of the multiple harmonic band-pass filters  
 124 in parallel are shown in Figure 7. Here the individual filter characteristics are shown by the curves  
 125 for the legends  $G_n$ , where the subscript  $n$  denotes the corresponding harmonic order. The thick curve  
 126 for the legend  $H$  indicates the overall combination of all six harmonic filters used in this work. Once  
 127 the harmonic components are extracted, the harmonic current reference is given by (4),

$$I_{f,H}(s) = k \cdot HF(s) \cdot V_{2,H}(s), \quad (4)$$



**Figure 7.** Bode plot of the individual harmonic filter transfer functions and their parallel combination.

128 where,  $k$  has the unit of admittance. It may be the same for all the desired harmonic orders, or different  
 129 for each of the different harmonic components. Thus, the current references are proportional to the  
 130 corresponding harmonic voltages. Since  $k$  is a real constant number, the emulated impedance is  
 131 resistive.

132 Applying the superposition theorem, the resultant harmonic voltage at the terminal  $T_2$  due to  
 133 the background harmonic voltage in the grid,  $V_{g,h}(s)$ , and the harmonic current,  $I_{g,h}(s)$ , drawn by the  
 134 STATCOM as shown in Figure 4, is given by,

$$V_{2,h}(s) = \frac{Z_{wpp,h}(s) \cdot V_{g,h}(s) - Z_{wpp,h}(s) \cdot (Z_{g,h} + Z_{tr,h}(s)) \cdot I_{f,h}(s)}{Z_{\Sigma}(s)}, \quad (5)$$

135 where,  $Z_{\Sigma}(s) = Z_{g,h}(s) + Z_{tr,h}(s) + Z_{wpp,h}(s)$ . Substituting the harmonic current reference from (4),

$$V_{2,h}(s) = \frac{Z_{wpp,h}(s) \cdot V_{g,h}(s)}{Z_{\Sigma}(s) \cdot \left(1 + \frac{k \cdot HF(s) \cdot Z_{wpp,h}(s) \cdot (Z_{g,h}(s) + Z_{tr,h}(s))}{Z_{\Sigma}(s)}\right)}. \quad (6)$$

136 Thus, in comparison to the base case (i.e. without any compensation) the harmonic voltage is  
 137 changed by a factor of,

$$F_{2,h}(s) = \left(1 + \frac{k \cdot HF(s) \cdot Z_{wpp,h} \cdot (Z_{g,h} + Z_{tr,h})}{Z_{\Sigma}}\right) \quad (7)$$

138 Since, the harmonic voltage at  $T_1$  is given by,

$$V_{1,h}(s) = \frac{Z_{tr,h}(s) \cdot V_{g,h}(s) - Z_{g,h}(s) \cdot V_{2,h}(s)}{Z_{g,h}(s) + Z_{tr,h}(s)} \quad (8)$$

139 Using (6), (7) and (8), we get,

$$V_{1,h}(s) = \left( \frac{Z_{tr,h}(s) - \frac{Z_{g,h}(s) \cdot Z_{wpp,h}(s)}{Z_{\Sigma}(s) \cdot F_{2,h}(s)}}{Z_{g,h}(s) + Z_{tr,h}(s)} \right) \cdot V_{g,h}(s) \quad (9)$$

### 140 3. Harmonic compensation analysis

141 The WPP network is largely a radial network. When a compensating resistor is connected at a  
 142 bus, the equivalent impedance of the network, downstream from that bus, decreases. Thus the system  
 143 impedance characteristic gets changed. Consequently, the harmonic voltages at different buses in the  
 144 system would change. The resultant amplification ratios for different cases with two different values  
 145 of the harmonic filtering resistance connected at two different buses are numerically analyzed using  
 146 (1).

#### 147 3.1. Active damping using harmonic resistance at bus $T_2$

148 When a resistance is connected at  $T_2$ , it is in parallel to the WPP impedance. Hence, the effective  
 149 WPP impedance is lower in magnitude and its phase angle moves closer to  $0^\circ$ , implying that it is more  
 150 resistive as shown in Figure 8. The solid arrows indicate the 5<sup>th</sup>, 11<sup>th</sup> and the 13<sup>th</sup> harmonic impedance  
 151 when there is no compensation. The dotted lines indicate the locus of the tip of the impedance move  
 152 from the initial uncompensated values towards the origin, as the emulated resistance is decreased  
 153 from 10  $pu$  to 0.03  $pu$ . The asterisk marks indicate the points for 2, 1.5, 1, 0.5, 0.25  $pu$  resistive  
 154 compensation.

155 Physically, the resistors in harmonic power filters dissipate energy, and thus provide damping  
 156 to harmonic amplifications. Likewise, the APF can provide damping to harmonic amplifications by

157 emulating resistive behaviour at the selected harmonic frequencies [11]. This is the case for providing  
 158 harmonic compensation at the local bus.

159 For the frequency domain analysis, a shunt resistor is connected at bus  $T_2$ , in parallel to the WPP  
 160 impedance,  $Z_{wpp}$ . The resultant amplifications at bus  $T_1$  and bus  $T_2$  are shown in Figure 10. These  
 161 curves show that while the compensation works for the full range of harmonics at bus  $T_2$ , it is not  
 162 effective at the remote bus  $T_1$  as the 6<sup>th</sup>, 7<sup>th</sup>, 10<sup>th</sup>, and 11<sup>th</sup> harmonic voltages get amplified.

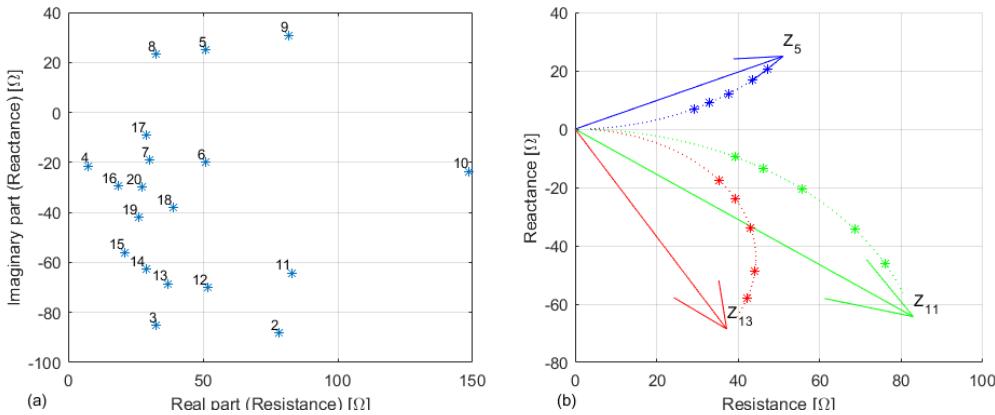


Figure 8. WPP impedance at  $T_2$ . (a) Impedance values at different harmonic orders. (b) 5<sup>th</sup>, 11<sup>th</sup> and 13<sup>th</sup> order Impedance locus as the compensating resistance at  $T_2$  is decreased from 10 pu to 0.03 pu (1 pu = 121  $\Omega$ )

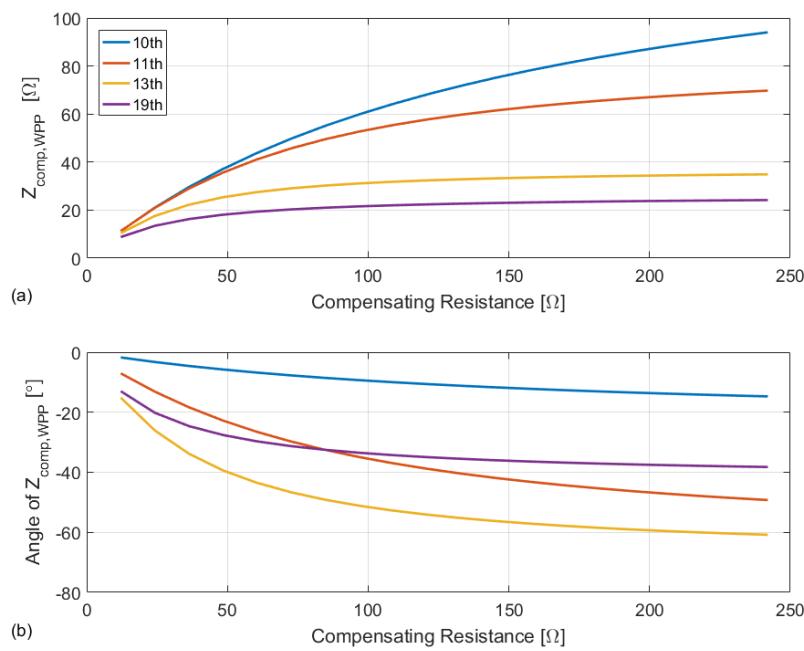
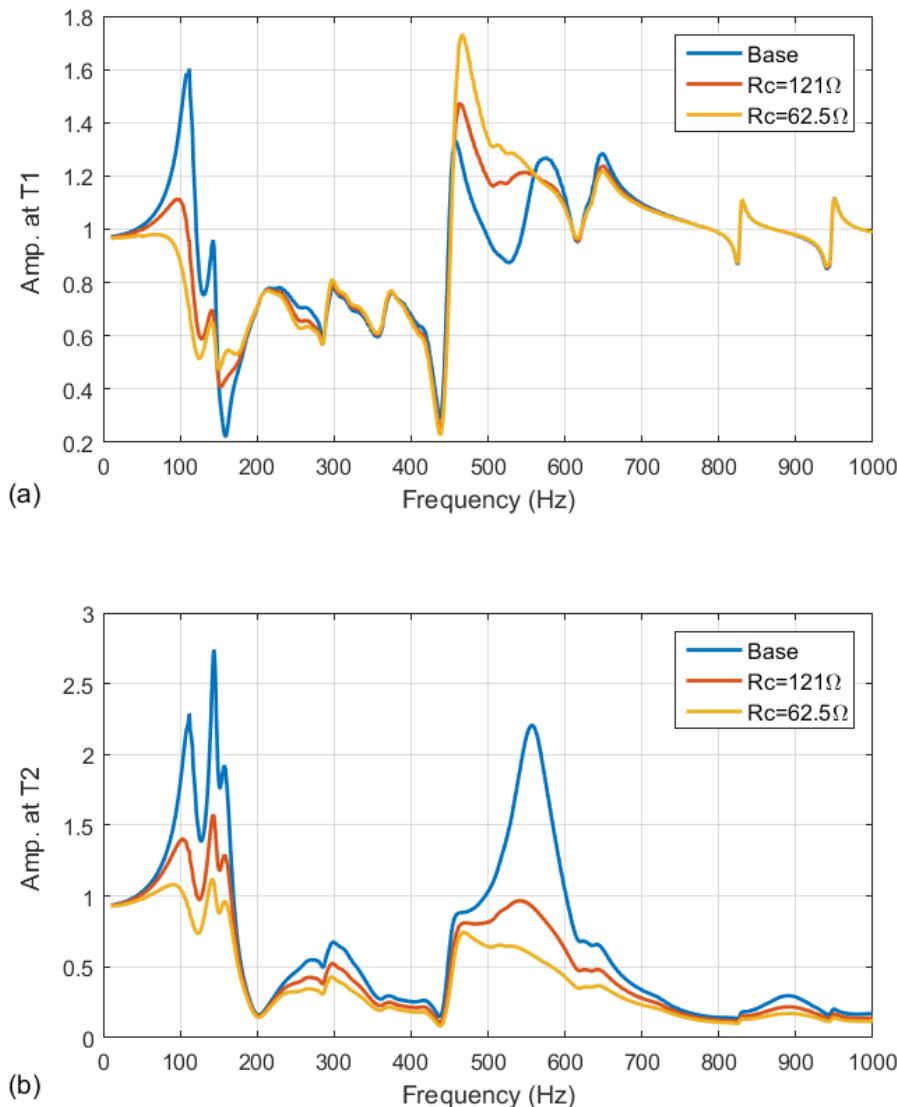


Figure 9. Variation of WPP impedance with resistance connected at  $T_2$ . (a) Magnitude. (b) Phase.

163 As shown in Figure 10, the harmonic compensation, provided by the resistances of sizes 1 pu  
 164 (121  $\Omega$ ) and 0.5 pu (62.5  $\Omega$ ) respectively at bus  $T_2$ , reduces the local amplification ratio. However,  
 165 it is not the same for the remote bus,  $T_1$ , which is upstream. An amplification is observed here, in  
 166 the base case, as the grid impedance is capacitive while the WPP side impedance is inductive largely

<sup>167</sup> due to the inductive impedance of the grid transformers. Even though there is an attenuation of the  
<sup>168</sup> 10<sup>th</sup> harmonic at the local bus  $T_2$ , it gets amplified in comparison to the base case at  $T_1$ . This can be  
<sup>169</sup> attributed to the reduced damping due to the reduction of the effective resistance of the WPP from  
<sup>170</sup> 424  $\Omega$  to 210  $\Omega$  and due to the compensation as shown in Table 2.



**Figure 10.** Amplification due to compensation at  $T_2$ .

**Table 2.** 10<sup>th</sup> harmonic impedance (referred to 400 kV) observed at  $T_1$  with 1pu resistive compensation at  $T_2$ .

	Unit	Real	Imaginary
$Z_g$	$[\Omega]$	20	-108
$Z_{tr}$	$[\Omega]$	3	261
$Z_{wpp}$	$[\Omega]$	421	-185
$Z_{wpp,comp}$	$[\Omega]$	207	-39
$Z_{wpp} + Z_{tr}$	$[\Omega]$	424	76
$Z_{wpp,comp} + Z_{tr}$	$[\Omega]$	210	222

171 3.2. Active damping using harmonic resistance at bus  $T_1$ 

172 As shown in Figure 11, when the harmonic compensating resistances of sizes 1 pu (i.e.  $400\Omega$ )  
 173 and 0.5 pu (i.e.  $200\Omega$ ) respectively are connected at bus  $T_1$ , the harmonic voltage gets reduced for  
 174 the local bus  $T_1$  as well as bus  $T_2$ , which lies downstream. It is expected, as the harmonic voltages are  
 175 appearing due to background harmonics in the grid.

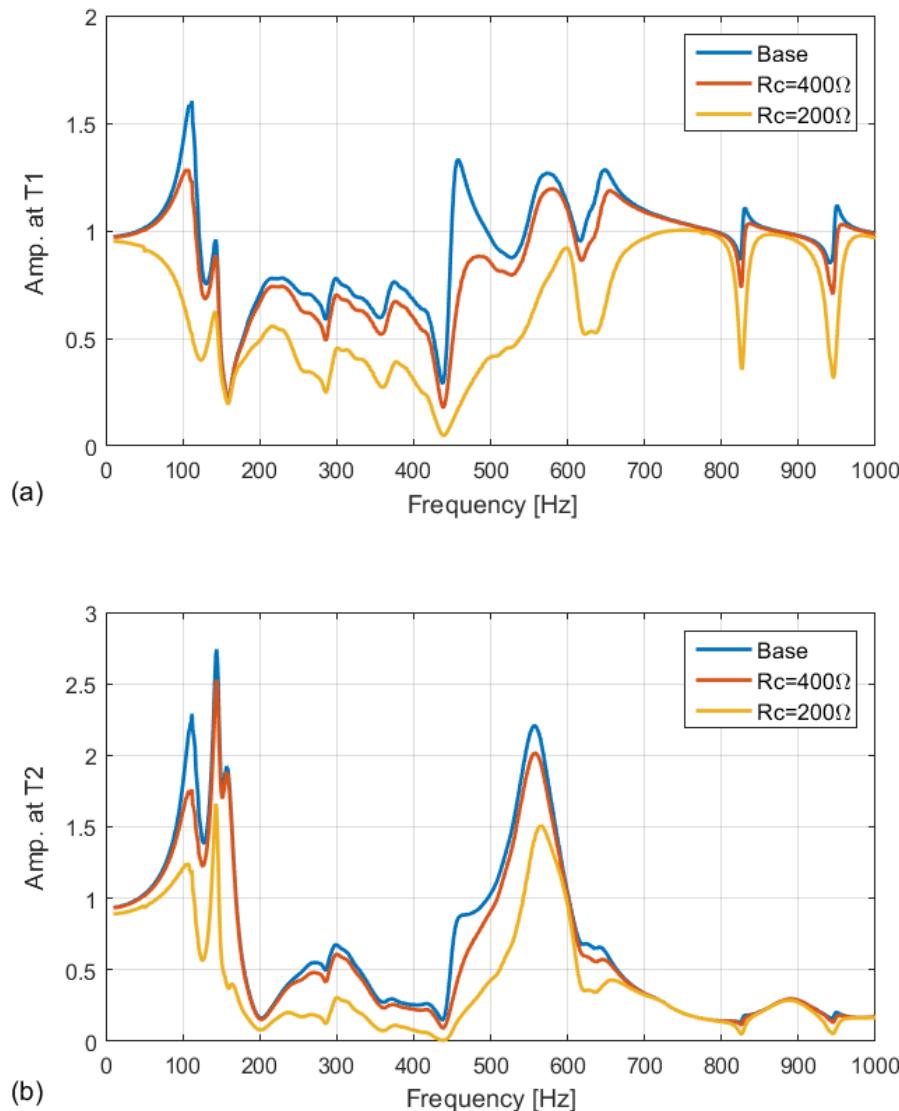


Figure 11. Amplification due to compensation at  $T_1$ .

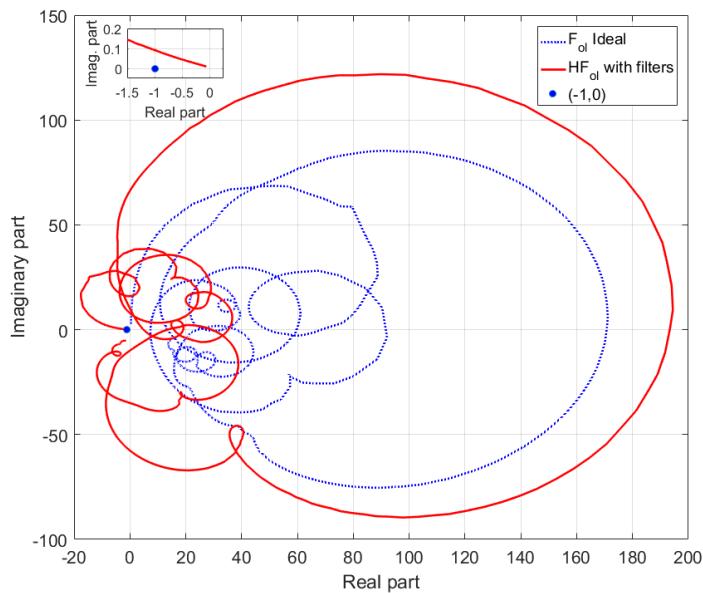
## 176 4. Nyquist Stability Analysis

177 Equation (7) for the harmonic voltage reduction factor is analogous to the characteristic equation  
 178 of a closed loop transfer function. Therefore, the stability of the proposed control algorithm can be  
 179 studied using Nyquist stability criterion on the loop gain,

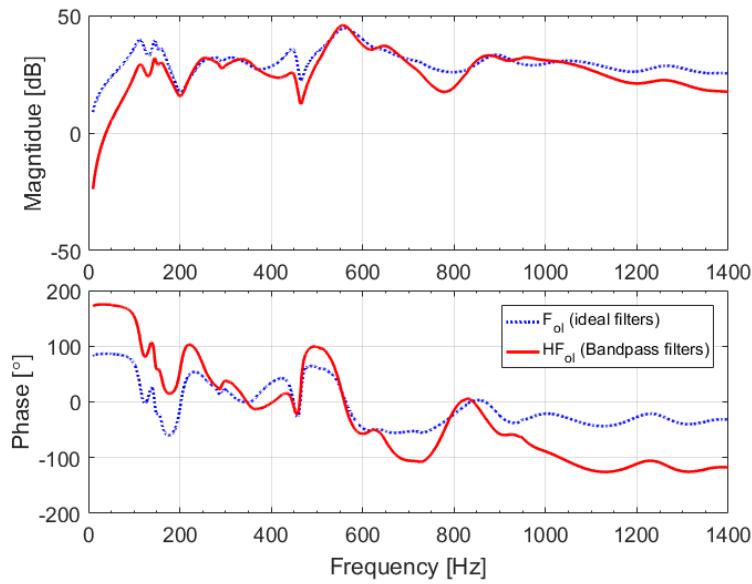
$$F_{ol}(s) = \frac{k \cdot HF(s) \cdot Z_{wpp,h} \cdot (Z_{gh} + Z_{tr,h})}{Z_{\Sigma}}. \quad (10)$$

180 If all the poles of (10) are on the right half plane, it will be stable for all values of the scalar gain  
 181 constant  $k$ . The Nyquist plot of this factor shown in Figure 12. It appears to be stable for all positive

182 values of  $k$  as it does not encircle the point  $(-1.0, 0)$ . The frequency characteristics of the harmonic  
 183 voltage reduction factor is further elaborated in Figure 13. The phase margin at the gain crossover  
 184 frequency of 240 rad/sec i.e. 38.2 Hz is 5 deg. This implies that there will be amplification of the  
 185 frequency components less than 38 Hz. The phase always remains within  $\pm 180$  deg.



**Figure 12.** Nyquist plot of the harmonic resistance emulation.



**Figure 13.** Bode plot of the of the harmonic voltage reduction factor at  $T_2$ .

## 186 5. Simulation Results

187 Harmonic propagation studies [12] is used to compare the harmonic voltage levels at different  
 188 buses and harmonic currents through different components in the system. Afterwards, the  
 189 performance of dynamic harmonic compensation is shown using time domain simulation in PSCAD.

190 *5.1. Harmonic propagation studies*

191 In harmonic propagation studies, the network model is created for a specific harmonic frequency  
 192 and the network equations are solved for that particular frequency. Since the power frequency is not  
 193 considered and only one frequency is considered at a time, the emulation of resistance at the specific  
 194 harmonic frequency by the STATCOM is simulated by a connecting a resistance in the network at  
 195 the concerned bus. In this work, a 1- $\mu$  resistance is separately connected to bus  $T_1$  and  $T_2$ . The  
 196 resultant harmonic voltages at buses  $T_1$ ,  $T_2$  and  $T_4$  are observed in the test system. The results are  
 197 then compared in Figure 14. In line with the amplification ratios described in the previous section, the  
 198 compensation at bus  $T_1$  leads to a reduction of voltage harmonics at all the aforementioned buses. The  
 199 compensation at bus  $T_2$  leads to the reduction of harmonics at bus  $T_2$  and  $T_4$ , which are downstream,  
 200 while there is an amplification of the 7<sup>th</sup> and the 11<sup>th</sup> harmonic at bus  $T_1$ . The results corroborate  
 201 the prediction made in the previous section as the distortion levels at bus  $T_2$  is decreased for all the  
 202 harmonic orders, whereas, for bus  $T_1$ , it gets decreased only for the 5<sup>th</sup> and the 13<sup>th</sup> harmonic orders.

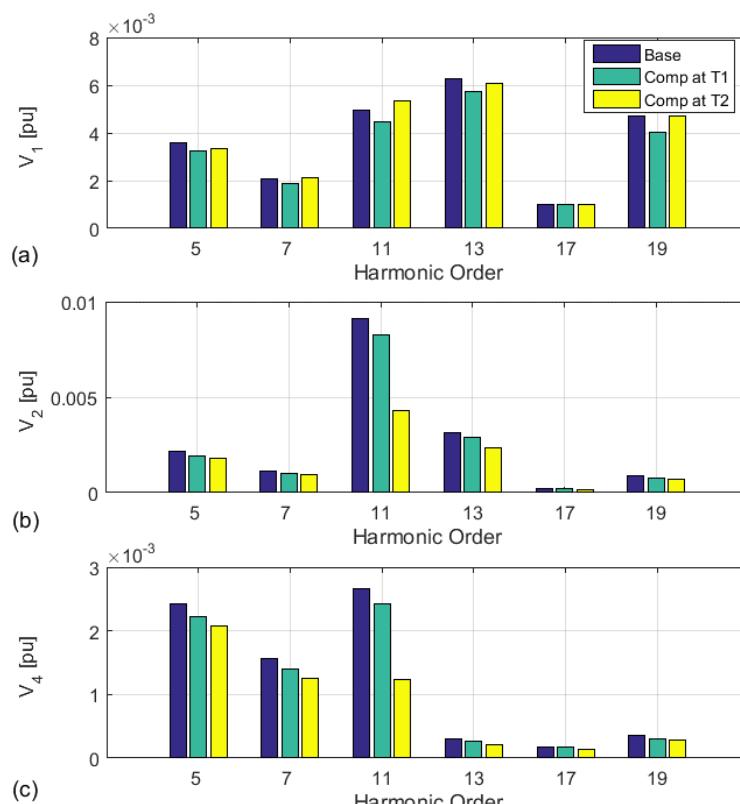
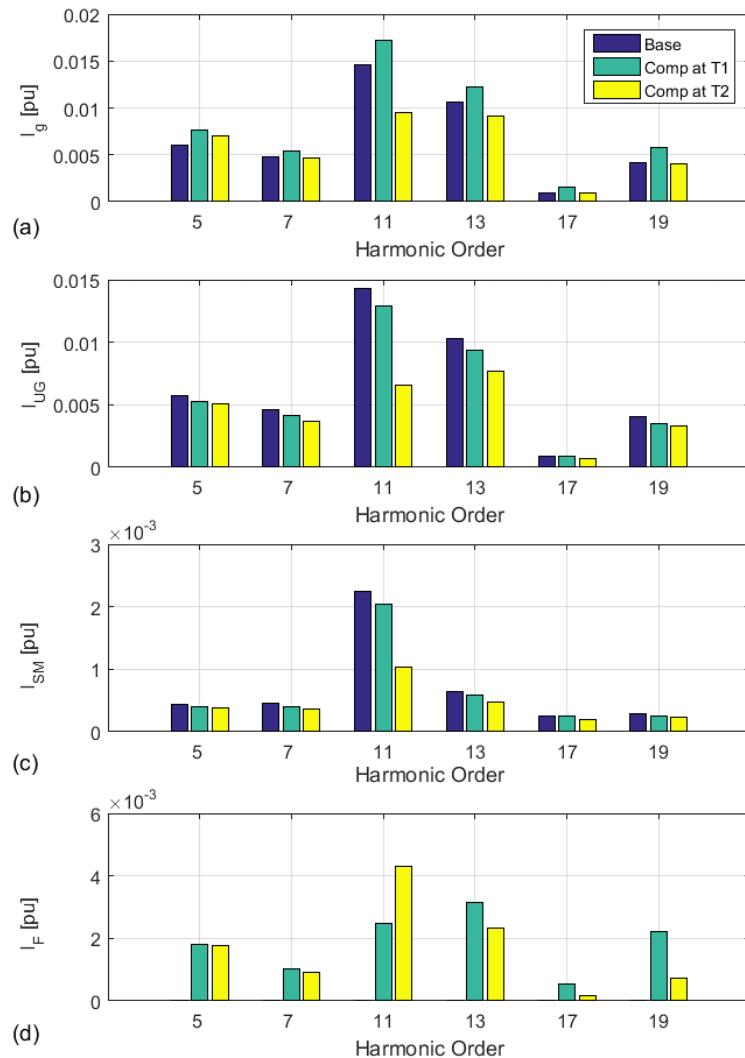


Figure 14. Harmonic voltages in pu at (a)  $T_1$ , (b)  $T_2$ , and (c)  $T_4$ .

203 The harmonic current flow in the different components as well as in the STATCOM is shown  
 204 in Figure 15. The harmonic current drawn from the grid is higher than that in the base case, when  
 205 the compensation is provided at bus  $T_1$ . By Kirchhoff's law, it is obvious that the grid has to supply  
 206 the current drawn by the WPP as well as the compensating resistance. Thus, the resultant harmonic  
 207 current in the grid will be the phasor sum of the WPP current and the STATCOM current. When the  
 208 compensation is provided at bus  $T_2$ , the grid currents are reduced by over 50% for the 11<sup>th</sup> harmonic,  
 209 while there is a smaller reduction for other harmonics, except the 5<sup>th</sup> harmonic, for which there is an  
 210 amplification. This amplification is due to the reduction of the total impedance for the 5<sup>th</sup> harmonic.



**Figure 15.** Harmonic currents in pu. (a) Grid at  $T_1$ , (b)Underground (UG) cable at  $T_2$ , (c) Sub-marine (SM) cable at  $T_4$  and (d) STATCOM.

### 5.2. Time domain simulation

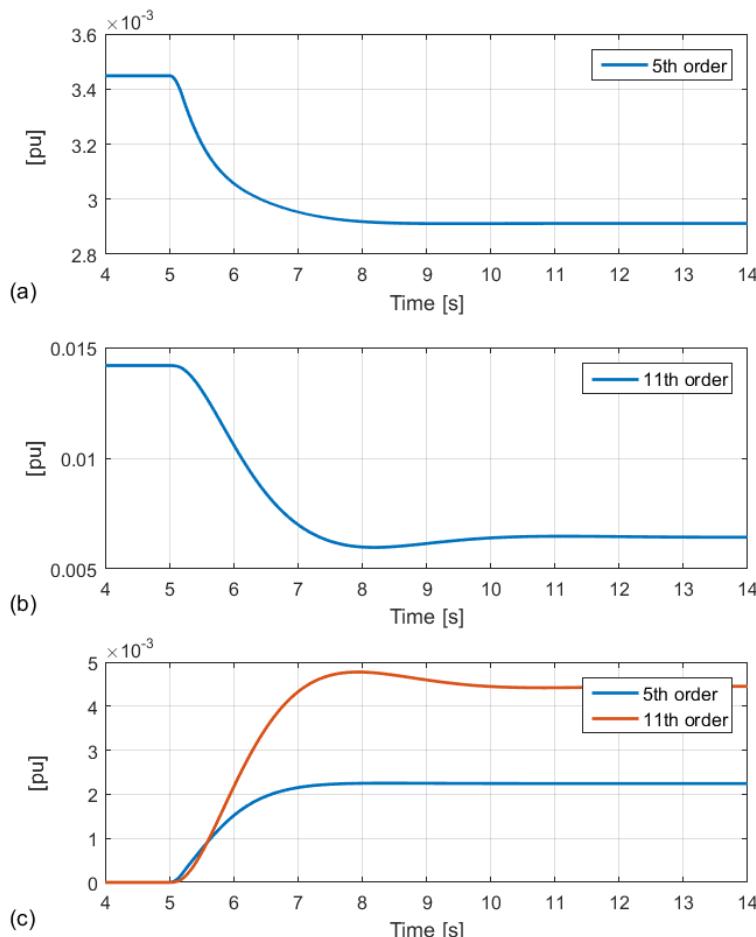
A time domain simulation model has been developed in PSCAD to show the STATCOM controller emulating the resistive behavior. The harmonic current source model of the STATCOM is connected to bus  $T_2$  as shown in Figure 4. Its controller measures the  $T_2$  bus voltage and extracts the 5<sup>th</sup>, 7<sup>th</sup>, 11<sup>th</sup>, 13<sup>th</sup>, and the 19<sup>th</sup> harmonic voltages. Then the corresponding harmonic current references are generated. When the voltage and currents are stated in pu values, setting the gain  $k = 1$  results in the emulation of 1pu resistance (i.e. 121  $\Omega$ ) at the selected harmonics.

The harmonic filtering functionality of the STATCOM is activated at 5s. The dynamics of the 5<sup>th</sup> and 11<sup>th</sup> order harmonic voltages and the filter currents at  $T_1$  and  $T_2$  are shown in Figure 16 and Figure 17. The harmonic components of the voltage decrease at the local bus  $T_2$ . The 5<sup>th</sup> harmonic component of the voltage at the local terminal  $T_2$  decrease from 0.34% to 0.29%. Similarly the 11<sup>th</sup> harmonic component decrease from 1.42% to 0.64%. The 5<sup>th</sup> and 5<sup>th</sup> harmonic currents from the STATCOM is 0.22% and 0.44% respectively. Table 3 shows that all the 5 selected harmonic voltage components get attenuated at the local bus  $T_2$  due to the compensating harmonic currents from the STATCOM. The total rms value of the selected harmonic compensating currents is 0.57% of the nominal.

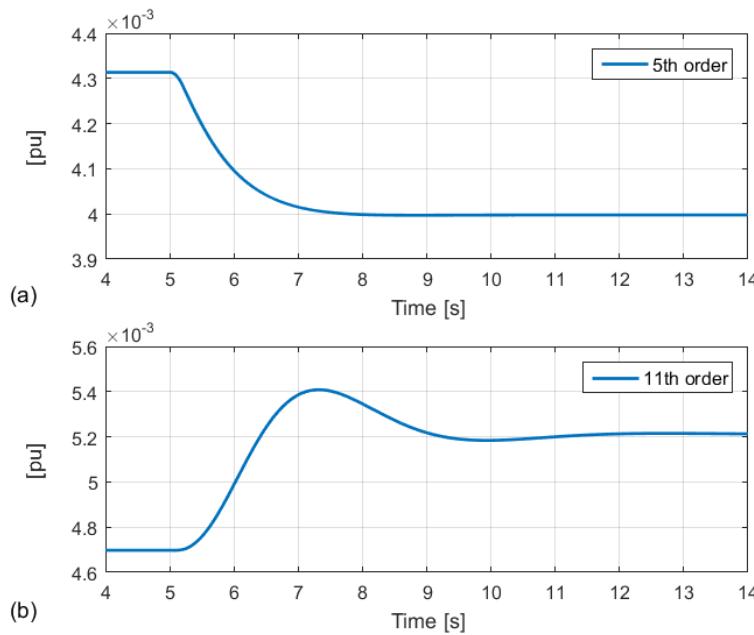
For the remote bus  $T_1$ , the 5<sup>th</sup> and the 13<sup>th</sup> harmonic orders show attenuation while the 7<sup>th</sup> and the 11<sup>th</sup> orders get amplified as shown in Table 3. The attenuation of the 5<sup>th</sup> harmonic voltage component from 0.43% to 0.40% and the amplification of the 11<sup>th</sup> harmonic voltage component from 0.47% to 0.51% as a result of the compensation from the STATCOM is shown in Figure 17. Though the numerical values in time domain simulation differ from the numbers obtained in the harmonic propagation studies, they exhibit similar trend.

**Table 3.** Harmonic voltages in the base case and after compensation (pu values are shown in percentage to reduce the leading zeros).

Harmonic order	5th	7th	11th	13th	19th
<b>Bus <math>T_1</math></b>					
Base (%)	0.43	0.23	0.47	0.60	0.47
Compensated (%)	0.40	0.23	0.52	0.58	0.47
Change (%)	7	-1	-11	2	0
<b>Bus <math>T_2</math></b>					
Base (%)	0.34	0.12	1.42	0.25	0.06
Compensated (%)	0.29	0.09	0.64	0.21	0.05
Change (%)	16	19	55	18	12
Current (IF in %)	0.22	0.10	0.44	0.24	0.06



**Figure 16.** (a) 5<sup>th</sup> harmonic voltage at  $T_2$ . (b) 11<sup>th</sup> harmonic voltage at  $T_2$ . (c) 5<sup>th</sup> and 11<sup>th</sup> harmonic resistive currents by the STATCOM.



**Figure 17.** Harmonic voltages at  $T_1$ . (a) 5<sup>th</sup> order. (b) 11<sup>th</sup> order.

## 233 6. Conclusion

234 This work investigates the amplification of the harmonic voltage distortion due to the  
 235 background harmonics in the grid at two different buses in a test WPP model. The effect of ideal  
 236 resistive compensation is numerically analysed and then corroborated using harmonic propagation  
 237 studies. Afterwards, a time domain simulation is used to validate the performance of this  
 238 scheme including the bandpass filters for the extraction of harmonic voltage components.

239 The resistive compensation is realized using a STATCOM, which emulates the resistive behavior  
 240 for the selected harmonic orders. Since the STATCOM controller determines the harmonic current  
 241 references, its effective resistance can be adapted dynamically in real time. Harmonic resistive  
 242 compensation has the following salient features:

- 243 • It can attenuate the harmonic voltages at its own bus, that is bus  $T_2$ . Since the WPP has a radial  
 244 network, the harmonic voltage level gets attenuated downstream from the point of compensation,  
 245 i.e. at the buses  $T_3$  and  $T_4$ .
- 246 • The attenuation at remote buses upstream from the point of compensation is not guaranteed.  
 247 Rather, in some cases, there may be an amplification of harmonic distortion levels. In the test  
 248 system, the 5<sup>th</sup> and 13<sup>th</sup> orders were attenuated while there was an amplification for the 7<sup>th</sup> and  
 249 11<sup>th</sup> orders at the bus  $T_1$ . Therefore, all different scenarios should be evaluated to ensure that  
 250 there is no undue amplification at the PCC and other buses upstream.
- 251 • This method is found to be stable for all values of the emulated resistance as per the Nyquist  
 252 stability criterion.

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