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Article

Performance-Based Seismic Resistance Assessment of Reinforced Slopes Using the Force-Equilibrium Finite Displacement Method

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Abstract

Performance-based evaluation of reinforced soil retaining structures often relies on numerical analyses that demand substantial time and expert effort, largely due to the complex interactions among soils, reinforcements, facings, and seismic loading. This study introduces an efficient approach for developing seismic-resisting capacity curves for geosynthetic-reinforced slopes with rigid facings, using a computer program built on the Force-Equilibrium-based Finite Displacement Method (FFDM). Positioned between conventional, non-performance-based limit-equilibrium methods (LEM) and the more computationally intensive finite element method (FEM), the FFDM offers a practical platform for performance-based seismic assessment in engineering design. The method is demonstrated through a re-examination of the Tanada Wall, a geosynthetic-reinforced soil retaining wall with a full-height rigid panel facing (GRS-FHR) that experienced strong shaking during the 1995 Hyogoken-Nambu earthquake ($M_L = 7.2$). Using only parameters available in published databases, the FFDM generates realistic seismic-resistance curves and directly computes seismic displacements. Three advantages distinguish the FFDM from traditional LEM-based Newmark approaches: (1) explicit incorporation of peak soil strength and post-peak degradation along the slip surface, eliminating the need for empirical “operational” strength adjustments; (2) direct use of peak ground acceleration (HPGA/g) as input, avoiding reliance on empirically selected seismic coefficients; and (3) capability for back-analysis, enabling soil strength and deformation parameters to be calibrated from small observed displacements (on the order of 10^{-3} m) during medium-scale earthquakes and subsequently used to predict structural response under more severe ground shaking.

Keywords: finite displacement method (FFDM); performance-based seismic evaluation; geosynthetic-reinforced soil structures; nonlinear soil model; seismic resistance curves

1. Introduction

In conventional engineering practice, the seismic stability of slopes is commonly evaluated using the safety factor (F_s) derived from prescribed seismic coefficients (k_h) through limit equilibrium methods (LEM). To estimate seismic-induced slope displacements, Newmark's hybrid approach—described in [1]—combines LEM with sliding-block dynamics and remains widely adopted. A key requirement for applying Newmark's method is the determination of a calibrated critical seismic coefficient (k_{hc}), obtained from the F_s – k_h relationship at the condition $F_s = 1.0$. Identifying this k_{hc} typically involves iterative trial-and-error adjustments to determine an “operational” internal friction angle (ϕ) that produces a satisfactory F_s – k_h curve.

To reduce the empiricism and iterative calibration inherent in this conventional workflow, Huang's Force-equilibrium-based Finite Displacement Method (FFDM), described in [2,3], was developed. By integrating soil stress–displacement behavior and displacement compatibility within

the sliding mass into the fundamental force and moment equilibrium framework of LEM, the FFDM provides a more direct and rational means of evaluating displacement-based slope performance. The method has since been successfully applied to groundwater induced landslides and reinforced slopes subjected to pseudo static seismic loading. Its capability has further been demonstrated through back-calculation of displacement-based soil and weathered-rock parameters [4,5] as well as through predictions of slope displacements [6].

Building on these developments, the present study aims to derive displacement-based seismic resisting capacity curves for a full scale geosynthetic reinforced railway embankment with a rigid concrete facing (referred to as the Tanada wall). The analyses are performed using SLOPE ffdm 2.0 [7], a computer program that integrates both conventional LEM-based and displacement-based FFDM analytical tools.

2. Methodology and Materials

2.1. Hyperbolic Soil Stress-Displacement Model

As illustrated in Figure 1, a hyperbolic model describing the normalized shear stress (τ/τ_f)–shear displacement (Δ) response along the potential failure surface was proposed in [2]. This model is an adaptation of the well known hyperbolic relationship for shear stress–strain behavior developed in [8].

$$\tau/\tau_f = \Delta / (a + b \cdot \Delta) \quad (1)$$

Where, $a = \tau_f / k_{\text{initial}}$, $b = R_f$, $R_f = \tau_f / \tau_{\text{ult}}$

k_{initial} : Initial shear stiffness of soils

τ_{ult} : Asymptote strength at infinite displacement

τ_f : Shear strength of soil according to the Mohr-Coulomb failure criterion

R_f : Asymptote strength ratio ($= \tau_f / \tau_{\text{ult}}$)

The shear strength of soils (τ_f) is defined by the Mohr-Coulomb failure criterion:

$$\tau_f = c + \sigma'_n \cdot \tan \varphi \quad (2)$$

σ'_n : Effective normal stress

c : Cohesion intercept

φ : Internal friction angle of soils

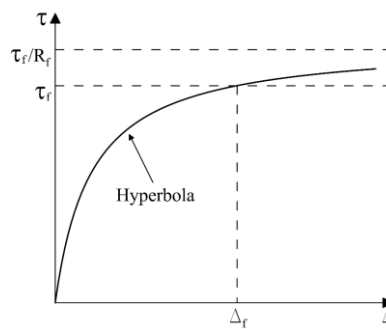


Figure 1. A hyperbolic normalized stress and shear displacement relationship.

2.2. Multi-Wedge Failure Mechanism

Figure 2 illustrates the multi wedge failure mechanism adopted in this study. This mechanism evolved from the classical “two-wedge” or “bi-linear” failure model, which has long been used to simulate the failure of engineered slopes with steep faces, such as mechanically stabilized earth (MSE) walls and geosynthetic reinforced slopes with rigid or near vertical facings. An enhanced version of the two wedge mechanism was proposed in [9], comprising two active wedges (Wedges 1 and 2), a facing column, and – when present – a passive wedge located beneath the toe of the facing. This multi wedge formulation provides deeper insight into the contribution of the facing system to overall slope

stability. Its advantages are further amplified when combined with the FFDM, which enables displacement based performance evaluation of the slope. Figure 3 presents the body forces and reaction forces acting on a generalized polygon wedge configuration. Triangular wedges, exemplified by Wedges 1 and 4, constitute special cases where the soil strength and reaction forces along one boundary are assumed to be negligible or zero.

By applying force equilibrium in both horizontal (x) and vertical (y) directions, the reaction force on the left side of each wedge can be expressed as:

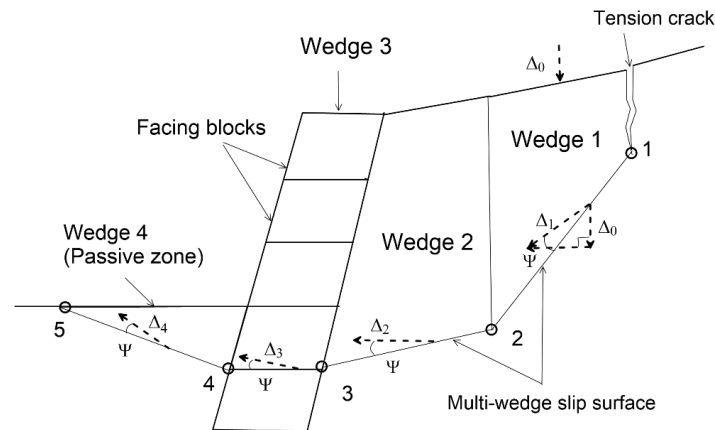


Figure 2. The multi-wedge failure mechanism.

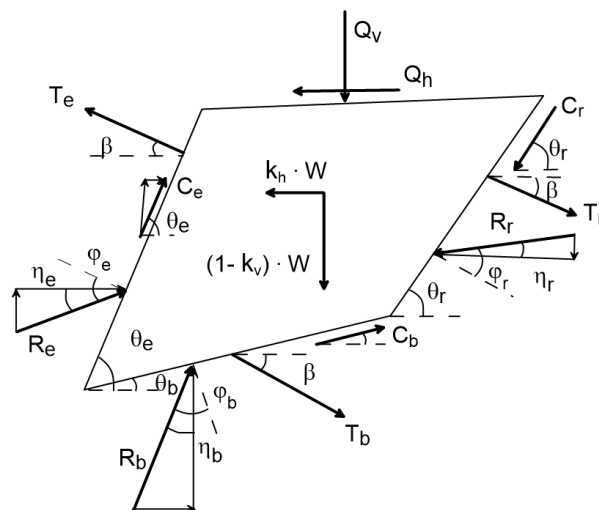


Figure 3. Force equilibrium for a generalized wedge.

$$R_e = f(R_b, R_r, T_r, T_b, T_e, C_e, C_r, C_b, C_e, \varphi_r, \varphi_b, \varphi_e, k_h, k_v, Q_v, Q_h) \quad (3)$$

$$\text{Where, } C_r = c \cdot l_r / FS_i, C_b = c \cdot l_b / FS_i, C_e = c \cdot l_e / FS_i$$

$$\varphi_r = \tan^{-1}(\tan \varphi / FS_i), \varphi_b = \tan^{-1}(\tan \varphi / FS_i), \varphi_e = \tan^{-1}(\tan \varphi / FS_i)$$

C_r, C_b, C_e : cohesive resistance along soil-block interfaces

l_r, l_b, l_e : lengths of soil-block interfaces

$\varphi_r, \varphi_b, \varphi_e$: mobilized internal friction angles at interfaces

T_r, T_b, T_e : reinforcement force at at interfaces

R_r, R_b : reaction forces at interfaces

To determine the reaction force acting on the left side of each wedge in the LEM analysis, the computation advances sequentially from wedge 1 to wedge 3 (or wedge 4, if present). A constant

safety factor, F_s , is assumed and applied uniformly to all wedges. With this assumption, all terms on the right-hand side of the governing force-equilibrium relationship are known except for the base reaction force R_b . Because both horizontal and vertical force equilibrium are imposed, the system is statically determinate. The safety factor is updated through iterative equilibrium calculations, typically starting with an initial trial value of $F_s = 1.0$, and is adjusted until the virtual external force R_e on the left side of wedge 3 (or wedge 4) becomes negligibly small, e.g., $R_e < 0.1$ kN.

In contrast, when the same governing relationship is solved within the FFDM framework, the safety factor for each soil block (F_{Si}) and the mobilized reinforcement force (T_r , T_b , T_e) depends on its displacement (Δ_i). The system remains statically determinate, but the safety factor is updated continuously according to the displacement field at the block base and along the interfaces. The computation begins by imposing a small vertical displacement at the crest of wedge 1 (Δ_0), e.g. a vertical displacement of 0.001m, and proceeds until all force equilibrium requirements are satisfied.

2.3. Post-Peak Stress-Displacement Relationship

The post-peak segment of the shear stress–displacement (τ – Δ) curve is modeled using the *Versoria* (or *Witch of Agnesi*) curve [6,10], schematically illustrated in Fig. 4. For efficient integration into the overall stress–displacement framework, a normalized local coordinate system (X – Y) is adopted. The X -axis origin ($X = 0$) aligns with the peak stress point (τ_f). The Y -axis origin ($Y = 0$) corresponds to the asymptotic value of the residual stress (τ_r). A distinctive feature of this curve is that the residual state (τ_r) is theoretically reached at an infinite Δ . In practice, however, a finite displacement (Δ_r), observed experimentally at the onset of the residual state (defined at $X = 1$), can be used to approximate τ_r with a negligibly small error (normally less than 1% error). The shear strength in the post-peak regime ($\tau_{post-peak}$) can be expressed as:

$$\tau_{post-peak} = \tau_f - \tau_f \cdot (t - Y) = \tau_f \cdot (1 - t + Y) \quad (4)$$

$$Y = t^3 / (t^2 + X^2) \quad (5)$$

$$X = (\Delta - \Delta_f) / (\Delta_r - \Delta_f) \quad (6)$$

$$t = (\tau_f - \tau_r) \cdot \tau_f \quad (7)$$

$$\Delta_r = \Delta_f \cdot \Delta_{ratio} \quad (8)$$

t : normalized strength reduction between peak and residual states

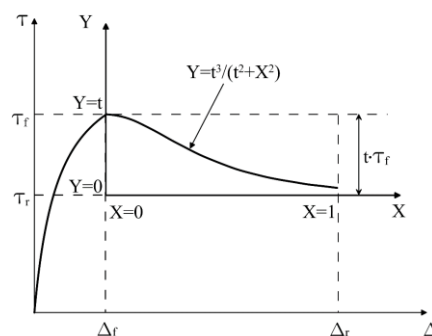
Y : normalized post-peak shear stress

X : normalized post-peak shear displacement

Δ_f : shear displacement at peak stress state

Δ_r : shear displacement at the entrance of residual state

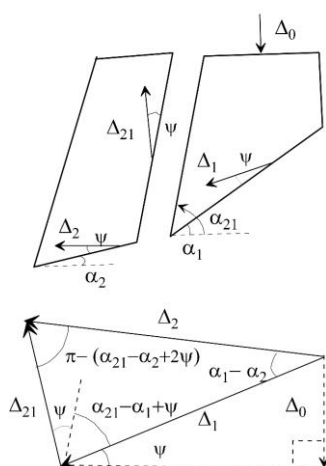
Δ_{ratio} : residual-to-peak displacement ratio



2.4. Displacement Compatibility

$$\Delta_i = \Delta_0 \bullet f(\alpha_i) \quad (9)$$

$$f(\alpha_i) = \cos(\alpha_1 - 2\Psi) / [\sin(\alpha_1 - \Psi) \cdot \cos(2\Psi - \alpha_1)] \quad (10)$$



2.5. Displacement Increment

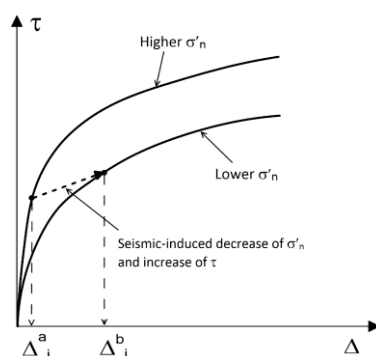
$$\Delta_i = \Delta^{b_i} - \Delta^{a_i} \quad (11)$$


Figure 6. Schematic stress path in response to seismic-induced stress changes.

2.6. The Tanada Wall

The Tanada wall is a geosynthetic-reinforced soil retaining wall with a full-height rigid panel facing (GRS-FHR), also known as a RRR wall. It formed part of a railway embankment located in a severely shaken area during the 1995 Hyogoken-Nambu earthquake (sometimes referred to as the Kobe earthquake; $M_L = 7.2$). Despite severe damage to nearby houses and soil-retaining structures, the Tanada wall demonstrated remarkable seismic resistance, with recorded displacements of only 0.1 m at the toe and 0.26 m at the top, as illustrated in Fig. 8. Comprehensive post-earthquake investigations and analyses were conducted in [12,13]. Based on site observations, the horizontal peak ground acceleration (HPGA) in the vicinity of the Tanada wall was estimated to be approximately 0.8 g in [12] (where g denotes gravitational acceleration).

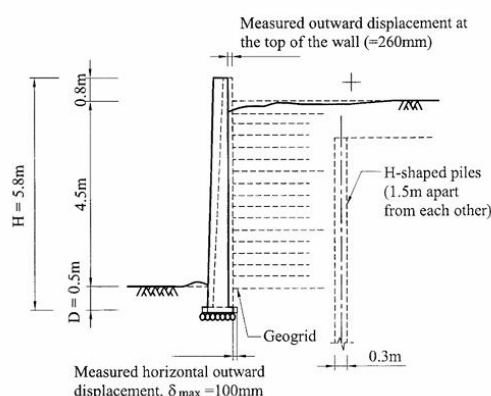


Figure 7. Cross-section of the Tanada wall following the earthquake [12].

2.7. Material Properties

The material properties used in the subsequent FFDM analyses of the Tanada wall are summarized in Table 1. Key evaluations for several primary input parameters that significantly influence seismic displacements are outlined below:

(1) Peak strengths of soils, c_{peak} , ϕ_{peak} : High-quality, cohesionless backfill ($c_{peak} = 0$) was clearly used in constructing the Tanada wall, a crucial component of the railway embankment. When applying the hyperbolic soil model, the design value of internal friction angle, $\phi = 40^\circ$ is adopted [12]. This value is considered as an 'operational' internal friction angle, slightly conservative in nature. In contrast, when incorporating the post-peak model for slope displacement evaluation, a higher $\phi_{peak} = 45^\circ$ - approximately 10% greater than the design value - is used to reflect the superior backfill quality and compaction during embankment construction. In the post-peak condition, cohesion is consistently zero, and the residual friction angle is taken as $\phi_{res} \cong 0.9 \phi_{peak}$ in the case study.

(2) Shear stiffness number, K: The analysis adopts stiffness values of $K = 200$ and $K = 400$, derived from a database of large- and medium-sized direct shear tests [6,15]. These values represent the lower-bound and median values for $\phi = 40^\circ$ within the dataset.

(3) **Displacement-dependent reinforcement pullout model:** The mobilized reinforcement force at the soil–block interface is determined using the hyperbolic reinforcement pullout model described in [3]. The peak adhesion at the soil–reinforcement interface is $c_{s-r} = 0$, and the peak friction angle is $\phi_{s-r} = 40^\circ$. It is assumed that this interface friction angle is not less than the internal friction angle of the backfill, as the reinforcement is a geogrid with woven junctions. The hyperbolic model parameters for reinforcement pullout - derived from a pullout test database - include pullout stiffness number $K_t = 10$, stress dependency exponent $n_t = 0.1$, and strength ratio $R_t = 0.7$ (failure strength / asymptotic strength).

(4) **Tie-Break Strength of Reinforcement:** In the FFDM hyperbolic reinforcement pullout model, the tie-break strength $T_{tie-break} = 30$ kN/m is defined as the unfactored ultimate tensile strength of the geogrid, reflecting the high-quality construction practices employed during the original project. This

definition contrasts with the factored allowable tensile strength $T_{allowable}$ commonly used in conventional limit-equilibrium methods.

(5) **Post-Peak Soil Stress–Displacement Model:** The post-peak cohesion is consistently zero ($c_{res}=0$), while the residual friction angle is taken as $\varphi_{res}\approx0.9\varphi_{peak}=41^\circ$ in the case study. A residual displacement ratio of $\Delta_r/\Delta_f=5.0$ is used, following the post-peak soil stress–displacement studies reported in [6,15]. Results of the studies reveal that typical dense sand exhibit Δ_r/Δ_f between 2.5 and 6.0.

(6) The H-piles located behind the wall at 1.5-meter center-to-center spacing were excluded. Due to their slenderness and wide spacing, they permit effective transmission of seismic earth pressure and thus do not significantly influence the results.

(7) The inter-block strength ratio ($f_{inter-block}$) defined as the ratio between the full shear strength to the shear strength available at the block-block interface in the force equilibrium calculations is set as 1.0 to account for the high-quality backfill and the fact that no tension crack has been observed at the crest in the post-earthquake investigation.

Table 1. Material properties used in the FFDM analysis for Tanada wall.

Soil		Reinforcement		Facing-related	
Hyperbolic model		Hyperbolic pullout model		strength parameters	
c	0 kPa	c_{s-r}	0	c_{b-r}	-
φ	40°	φ_{s-r}	40°	φ_{b-r}	-
K	10, 400	K_t	10	$\Gamma_{connect}$	0 kN/m
n	0.4	n_t	0.1	c_{back}	0
R_f	0.83	R_t	0.7	φ_{back}	30°
ψ	5°	$T_{tie-break}$	0 kN/m	c_{base}	0
				φ_{base}	40°
Post-peak model		Post-peak model		Post-peak model	
c_{peak}	0	Not available		Not available	
φ_{peak}	45°				
c_{res}	0				
φ_{res}	41°				
Δ_r/Δ_f	5.0				

* c_{s-r} , φ_{s-r} : adhesion and friction angle, respectively, at soil-reinforcement interface. * c_{b-r} , φ_{b-r} : adhesion and friction angle, respectively, at facing block-reinforcement interface. In the case of rigid panel facing, these values are not required. * c_{back} , φ_{back} : adhesion and friction angle, respectively, at the back-face of facing. * c_{base} , φ_{base} : adhesion and friction angle, respectively, at the base of facing. * $T_{tie-break}$: tie-break of reinforcement. In the FFDM displacement analysis, this value can be different from the design tensile strength of reinforcement ($T_{allowable}$) used in the LEM analysis. * $T_{connect}$: connecting force at facing-soil interface. This input is exclusively for the case of rigid panel facing which is equal to $T_{tie-break}$ in this case study of the Tanada wall.

Figure 8 presents an example of the stress–displacement curves visualized with integrated pre-peak and post-peak parameters ($\varphi_{peak}=45^\circ$, $\varphi_{res}=41^\circ$, $\Delta_r/\Delta_f=5.0$, $K=400$, $n=0.4$, $R_f=0.83$) as summarized in Table 1. For reference, the experimental data reported in [14] from direct shear tests on dense, remolded Chi-Chi sand—classified as SW-SM under the Unified Soil Classification System (USCS)—are also included.

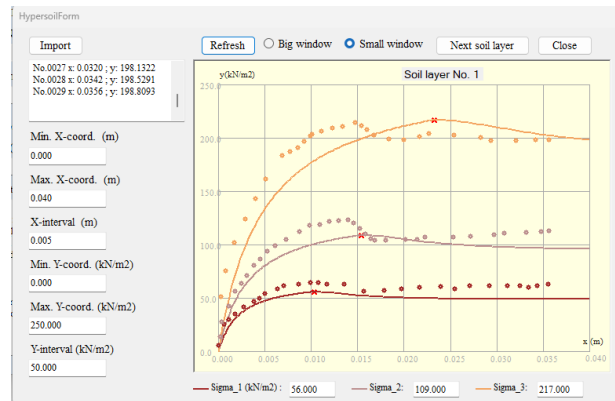


Figure 8. Integrated pre- and post-peak stress-displacement curves for the displacement analyses.

Figure 9 illustrates the visualized hyperbolic pullout curves for reinforcement ($c_{s-r} = 0$, $\phi_{s-r} = 40^\circ$, $T_{tie-break} = 30$ kN/m, $K_t = 10$, $n_t = 0.1$, and $R_t = 0.7$). For comparison, experimental pullout data for woven geogrids embedded in recycled construction material classified as SM (USCS), as reported in [15], are also shown. It is observed that the theoretical curves exhibit a stronger dependence on confining pressure than the experimental results, likely because the tests were conducted under relatively low confining pressures (10 and 25 kPa), where material uncertainties and measurement errors tend to have relatively large effects.

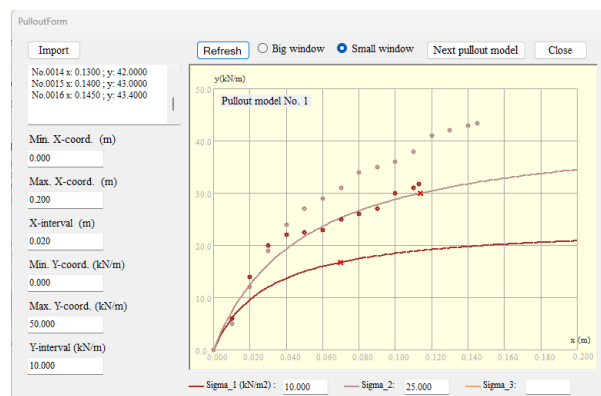


Figure 9. Stress-displacement curves for reinforcement pullout in the displacement analyses.

2.9. FFDM Displacement Analysis

In the Type-4 (multi-wedge) FFDM analysis implemented in SLOPE-ffdm 2.0, a total of 5,389 trial-and-error facing surfaces is employed to identify critical failure mechanisms characterized by the minimum safety factor (F_s) and the maximum vertical displacement at the slope crest (d_0), for a specified pseudo-static seismic coefficient k_h ($= HPGA/g$; g : gravitational acceleration). Figure 10 presents the initial configuration of the multi-wedge analysis, including the trial-and-error search grids for wedge points 1, 2, and 3. In this example, wedge point 3 is fixed at the heel of the rigid facing panel. Once the analysis begins, trial-and-error facing surfaces are systematically generated by connecting all grid combinations, as illustrated in Figure 11. Upon completion of the search, the resulting critical failure mechanisms are displayed in Figure 12. The corresponding failure modes of the reinforcing layers associated with the critical failure surface are also shown in Figure 12, where the symbol “ $\times$ ” denotes tie-break failure and “ $\rightarrow$ ” denotes pullout failure.

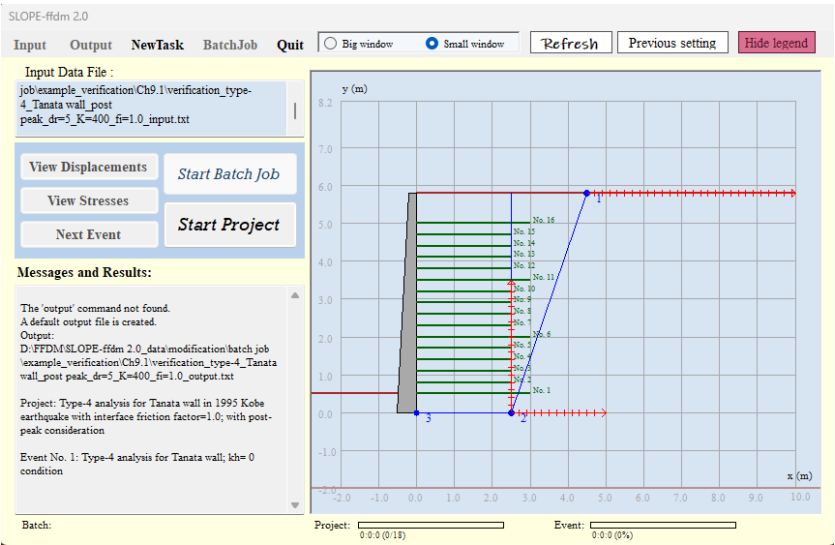


Figure 10. Initial configuration for the multi-wedge analysis in SLOPE-ffdm 2.0.

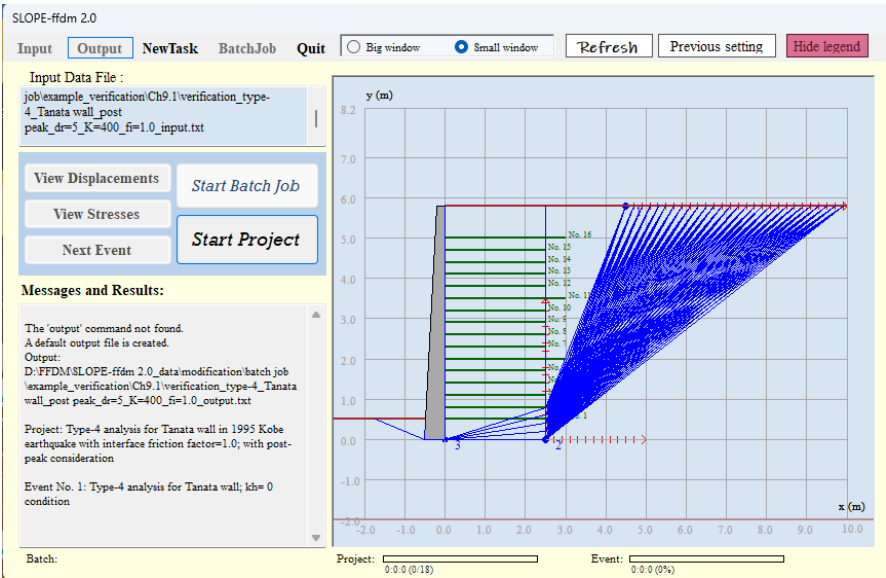


Figure 11. Searching for the critical failure mechanism using a trial-and-error procedure.

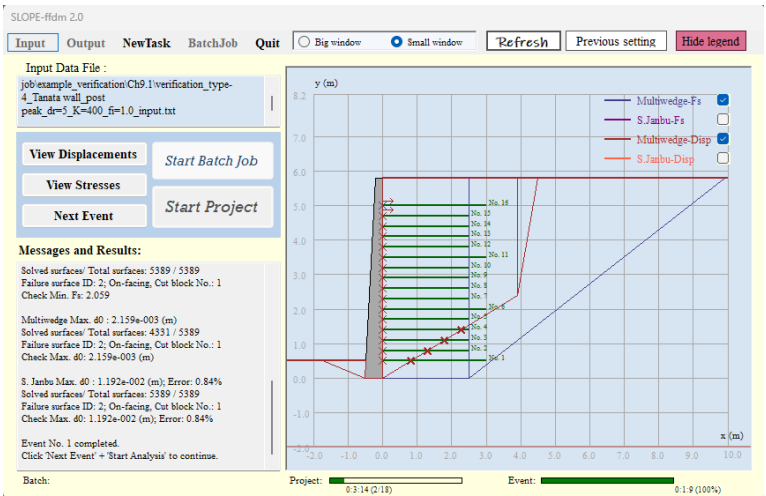


Figure 12. Critical failure mechanisms identified from the limit-equilibrium and displacement analyses, characterized by the minimum F_s and maximum d_0 (vertical crest settlement).

3. Results

Figure 12 shows the analytical result of FFDM analysis using the multiwedge method (or Type-4 analysis). In this figure, “Low” and “High” soil strength refer to $\phi = 40^\circ$ and 45° , respectively, listed in Table 1. Every data point in the figure represents a critical (or maximum) value of facing displacement found in 5,389 trial-and-error multiwedge searches. All curves exhibit consistent response to the increase of input $HPGA/g$ in the range of $0.0 - 0.85$. In the case $\phi = 40^\circ$ and hyperbolic soil behavior, the response curves exhibit rapid increases in facing displacement at $HPGA \approx 0.5g$. When the post-peak model is considered in the analysis, the response curves show a clear tendency toward failure state at $HPGA/g \approx 0.7 - 0.8$. In general, the curves with $K = 400$ and high soil strength effectively simulate the observed seismic displacement of the Tanada wall, regardless of the incorporation of post-peak strength. The analysis with a post-peak model verifies not only the earthquake-resisting capacity of the Tanada wall but also the capability of **SLOPE-ffdm 2.0** in calculating seismic displacements of geosynthetic-reinforced soil retaining walls. It is also noted that the calculated slope displacements span a wide range between 10^{-3} to $10^{-1} m$, reflecting their engineering significance and accuracy of the computational scheme of the computer program.

To compare the effectiveness of the FFDM with hybrid Newmark-type methods, conventional limit-equilibrium slope stability analyses were conducted to obtain F_s - k_h curves for $\phi = 40^\circ$ and $\phi = 45^\circ$, using soil, reinforcement, and facing parameters consistent with those adopted in the displacement analyses. The resulting critical horizontal seismic coefficients are $k_{hc} = 0.367$ and $k_{hc} = 0.528$ for $\phi = 40^\circ$ and $\phi = 45^\circ$, respectively. The value $k_{hc} = 0.367$ agrees well with the lower-bound regression relationship reported in reference [16]. Regression equations relating k_{hc} to seismic displacement for GRS-FHR systems subjected to strong ground motions—such as the El Centro, Loma Prieta, Hyogo-ken-Nambu, and Chi-Chi earthquakes—are also provided in reference [16]. Using the regression equation for the Hyogo-ken-Nambu earthquake, the predicted seismic displacements of the GRS-FHR are 132 mm and 30 mm for $\phi = 40$ degrees and $\phi = 45$ degrees, respectively. The displacement of 132 mm for $\phi = 40$ degrees again indicates that, when an operational friction angle of $\phi = 40$ degrees is adopted and an appropriate ground-motion record is selected, a conventional Newmark sliding-block analysis can yield reasonable estimates of seismic displacement for GRS-FHR systems. Nevertheless, this approach has inherent limitations, which will be discussed later.

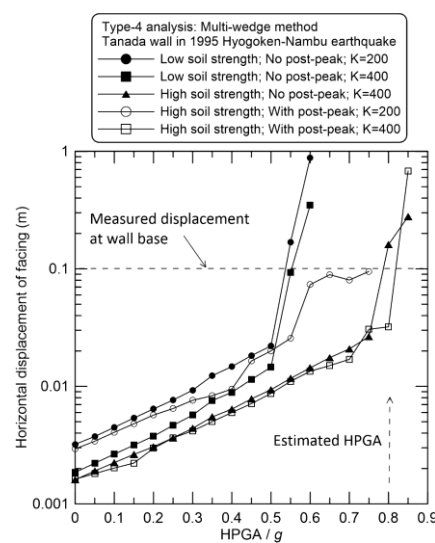


Figure 12. Seismic resistance curves for Tanada wall using Type-4 (multi-wedge) analysis

4. Discussion

By integrating soil behavior, reinforcement interaction, and seismic demand within a unified computational platform, the FFDM provides capabilities that extend beyond those of conventional

limit-equilibrium methods (LEM). Advantages and limitations of the LEM-based Newmark's and the pseudo-static-based FFDM approaches are:

1. Direct incorporation of peak strength and post-peak degradation: The FFDM explicitly accounts for both peak soil strength and its post-peak degradation along the slip surface. This eliminates the trial-and-error process traditionally required to estimate “operational” strength parameters, thereby streamlining the evaluation of seismic displacements in soil and reinforced-soil systems.

2. Direct use of peak ground acceleration (HPGA/g): Unlike LEM-based seismic analyses that rely on empirically selected seismic coefficients (k_h), the FFDM allows HPGA normalized by gravitational acceleration (g) to be used directly as input. This reduces dependence on empirical assumptions and enables more transparent, physically grounded seismic displacement assessments.

3. **Limitations of the Newmark approach in pre-earthquake assessments:** In a post-earthquake study, a ground excitation recorded at a nearby seismograph may help, to some extent, in reducing the uncertainty of input ground excitations. By using calibrated soil strengths, the LEM-based Newmark's approach is valid in estimating seismic displacement of GRS-FHR. However, this may not be the case in a pre-earthquake assessment. When a broad spectrum of potential ground motions is considered, the predicted seismic displacements may span an excessively wide range. Such variability can obscure the true seismic response of the system and hinder sound engineering judgment. As reported in [16], for a geosynthetic-reinforced soil wall with a non-detectable wall displacement during the 1999 Chi-Chi earthquake, the use of LEM-based Newmark's approach rendered $k_{hc} = 0.247\text{--}0.278$ and $\delta_h = 34\text{--}311$ mm based on various regression curves for normalized δ_h vs. k_{hc} / k_m ($k_m = \text{HPGA} / g$) relationships reported in [17,18].

4. **Contrasting complexity in soil parameters and ground-motion inputs:** The LEM-based Newmark approach employs simplified soil strength parameters (primarily cohesion c and ϕ), yet requires ground-motion inputs of considerable complexity, including period characteristics, maximum velocity, and HPGA. In contrast, the FFDM approach incorporates a richer set of soil deformation-related parameters (c , ϕ , K , n , R_f) while using a simplified ground-motion input in which HPGA is the primary concern. This inversion of complexity highlights the more mechanistic nature of the FFDM framework.

5. **Capability for back-analysis and parameter calibration:** A major advantage of the FFDM is its ability to perform back-analysis to derive soil deformation-related parameters (c , ϕ , K , n , R_f) from small-to-medium earthquake events (for example, $\text{HPGA} = 0.35 g$) in which the retaining structure experiences only minor damage (such as 10 mm of wall displacement). As illustrated in Figure 12, calibrated soil parameters can be inferred from the displacement versus HPGA/ g curves. These calibrated parameters can then be used to predict wall displacements under more intense ground shaking. The conventional LEM-based Newmark approach does not offer this capability, as its inherent uncertainties the uncertainties typically exceed several tens of millimeters (that is, on the order of 10^{-2} m), making reliable back-analysis impractical.

5. Conclusions

This study, implemented through the SLOPE-ffdm 2.0 program, establishes a displacement-based framework for evaluating the seismic performance of geosynthetic-reinforced slopes using the Force-Equilibrium Finite Displacement Method (FFDM). A performance-based re-evaluation of the Tanada Wall, which experienced intense shaking during the 1995 Hyogoken-Nambu earthquake ($M_L = 7.2$), further validates the effectiveness of the FFDM. The results show that using seismic coefficients derived directly from peak ground acceleration—rather than scaled or empirically adjusted values—eliminates a major source of uncertainty inherent in conventional LEM-based seismic stability analyses. The FFDM also produced realistic and reliable seismic-resistance curves using soil parameters within practically acceptable ranges.

Overall, the study demonstrates that the FFDM, as implemented in SLOPE-ffdm 2.0, provides a robust and practical framework for performance-based seismic evaluation of geosynthetic-reinforced

slopes and walls with rigid facings. Its ability to integrate soil behavior, reinforcement interaction, and seismic demand in a displacement-based manner represents a significant advancement over traditional methods and offers a valuable tool for modern geotechnical engineering practice.

This study also highlights key differences between the FFDM and the conventional LEM-based Newmark sliding-block method. The Newmark approach relies on simplified soil strength parameters while requiring consideration of widely varying ground-motion characteristics, which can lead to large variability in predicted seismic displacements. In contrast, the FFDM incorporates a richer set of soil deformation-related parameters while using a simplified ground-shaking input (HPGA), resulting in more transparent and physically grounded predictions.

A major advantage of the FFDM is its capability for back-analysis. For structures that experience only small displacements (for example, on the order of 10^{-3} m) during a medium-scale earthquake, the FFDM can be used to back-calculate soil strength and deformation parameters. These calibrated parameters can then be applied to predict the potential response of the structure under more severe ground shaking. The conventional LEM-based Newmark method does not offer this capability, as its inherent uncertainties typically exceed several tens of millimeters, making reliable back-analysis impractical.

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