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Article

Tensile Yield Strength Prediction for Polypropylene Using Cowper-Symonds Model in the Low Range of Strain Rates

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Abstract: This study investigates by hybrid approach of classical calculations and numerical explicit FEM simulation the strain rate sensitive hardening of Polypropylene Sabic 83MF10 under dynamic tension loads. The Cowper-Symonds model is employed to characterize the non-linear increase in yield strength with strain rate, within the range of 0,01 to 1 [1/s]. For lower strain rates, a drastic decrease in yield strength is observed, suggesting the significant influence of creep and relaxation phenomena. The study proposes further research incorporating viscoelastic properties for a more comprehensive material model. Additionally, the study observes a disproportionate increase in yield strength for samples with smaller radius, indicating a dependency on triaxiality which suggests further research on the Drucker-Prager model for this material. The study concludes by recommending a broader range of input parameters for future studies, including the Johnson-Cook model and comparison of tensile test results with compression test results.

Keywords: Polypropylene; Cowper-Symonds; strain rate; yield strength

1. Introduction

Polymer materials such as polypropylene, which was originally introduced in 1951 [1], are widely used in many industries. They require good strength properties, resistance to aging, dimensional stability throughout the product life cycle, high resistance to cracking, and importantly, the ability to be used in mass production processes such as extrusion or injection molding [2–5].

Table 1. Basic mechanical properties for Polypropylene [6].

Density	0,89 – 0.93 [g/cm ³]
Young’s modulus	1100 – 1800 [MPa]
Poisson ration	0,38 – 0.42 [–]
Yield strength in RT	20 – 40 [MPa]
Shore hardness	45 – 83 [D]
Melting point	140 – 165 [°C]

Due to the above advantages, Polypropylene has found wide application in the automotive industry, where it is used not only to manufacture components contained within the car’s interior, but also to produce parts exposed to mechanical factors and responsible for human safety [7]. An example of such a solution is a brake fluid reservoir that is part of the braking systems of passenger

cars. In the entire product life cycle, critical mechanical stress occurs once during the factory process of first filling, when a special filling head exerts significant load on the filler neck simultaneously in many directions.



Figure 1. Example of brake fluid reservoir mounted on brake system's pump. Rys. 1. Przykład zbiornika na płyn hamulcowy, zamontowanego na pompie układu hamulcowego

Because of the ongoing topological optimization of the above component, it is crucial to examine and validate the tank's strength before production. For many years, numerical testing methods based on the Finite Element Method (FEM) have been leading in such solutions due to their advantages, such as speed or accuracy of the results obtained. However, to fully base the validation of the structure on numerical methods, it is necessary to apply the most accurate material model of the simulated object.

2. Cowper-Symonds Model

Due to the nature of the applied force, i.e., the occurrence of loads at a relatively small but variable speed of their application, it is necessary to examine the basic properties of the material used, such as flow stress depending on the strain rate. One of the proposed constitutive models, which is able to reflect that change of parameter, is the Cowper-Symonds model [8], which is typically used for metallic materials and their wide spectrum of strain rates during tension or compression tests [9–11].

The Cowper-Symonds model parameterizes the dynamic flow stress using equation:

$$\sigma_d = \sigma_s \left(1 + \left(\frac{\dot{\epsilon}}{C} \right)^{1/q} \right) \quad (1)$$

where σ_d, σ_s represents the dynamic and static yield strength obtained from, among others, tensile tests. $\dot{\epsilon}$ is a strain rate and C, q are the constant parameters of the model. Because of the form of equation (1), the Cowper-Symonds model is characterized by a non-linear, in practice close to logarithmic, dependence of flow stress (σ_d) on strain rate ($\dot{\epsilon}$).

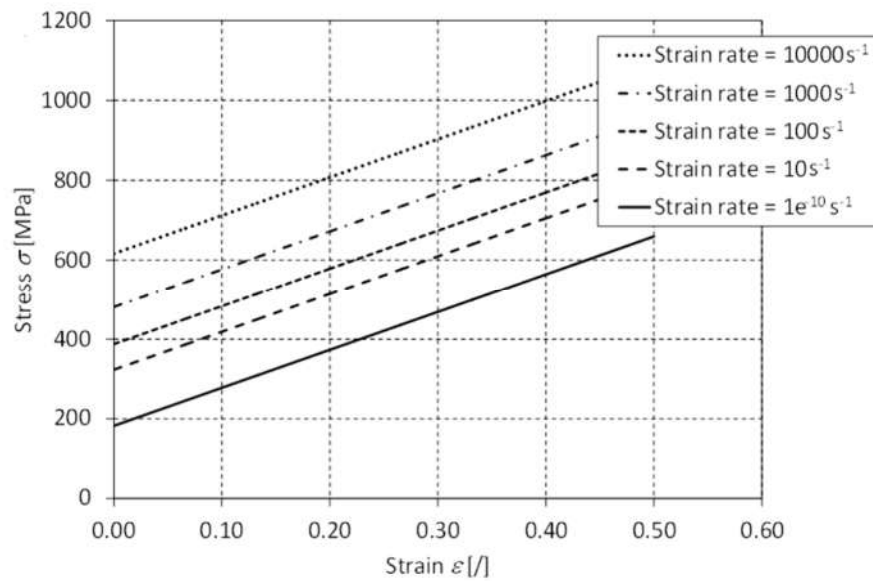


Figure 2. Example of flow stress curve for different strain rates using Cowper-Symonds model [11].

Rys. 2. Przykład krzywej wytrzymałości plastycznej dla różnych wartości prędkości odkształcenia używając modelu Compera-Simondsa [11].

It is worthy to mention that we could expect that for tension and compression test, the parameter will be different [8,9].

3. Material, Samples and Experimental Techniques

The material subjected to analysis on a Zwick type universal testing machine was Polypropylene with the trade name Sabic 83MF10, obtained in the form of flat plates with a thickness of 2,2 [mm]. The samples were machine cut to obtain different values of the rounding radius (R_1), which allowed for a wider range of strain rates ($\dot{\epsilon}$), with a limited number of speed settings for the travel head of the strength machine (v). This also allows for the assessment of the impact of other parameters, including the state of material strain, i.e., triaxiality (η) on the results obtained. The characteristic points, whose behavior is reflected in the stress-travel curves studied in the further part of the study, have been marked in the figure below.

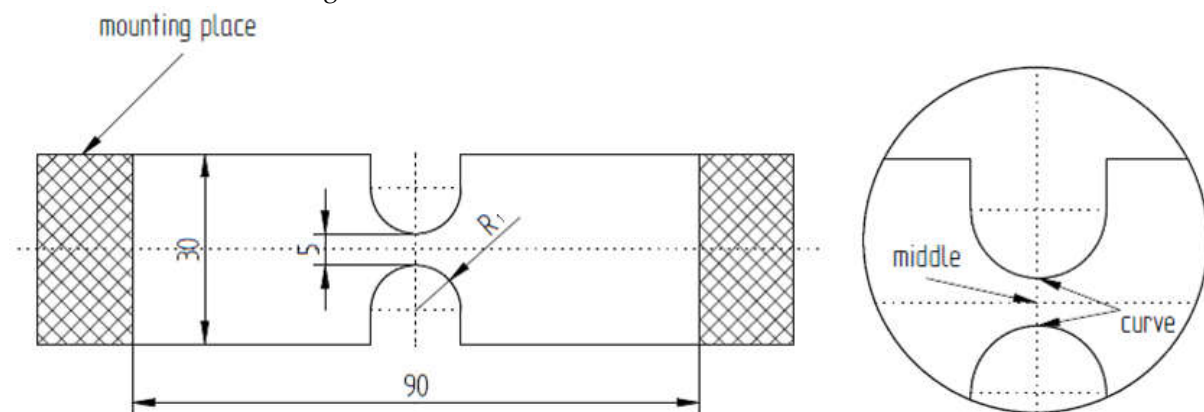


Figure 3. Characteristic dimension (in [mm]) of samples for tension test. Rys. 3. Wymiary charakterystyczne (w [mm]) próbek do badań na rozciąganie.

The twelve prepared samples were tension until the upper limit of plasticity (R_{eH}) was reached using a strength machine with a controllable head movement speed, using a swivel mounting system.

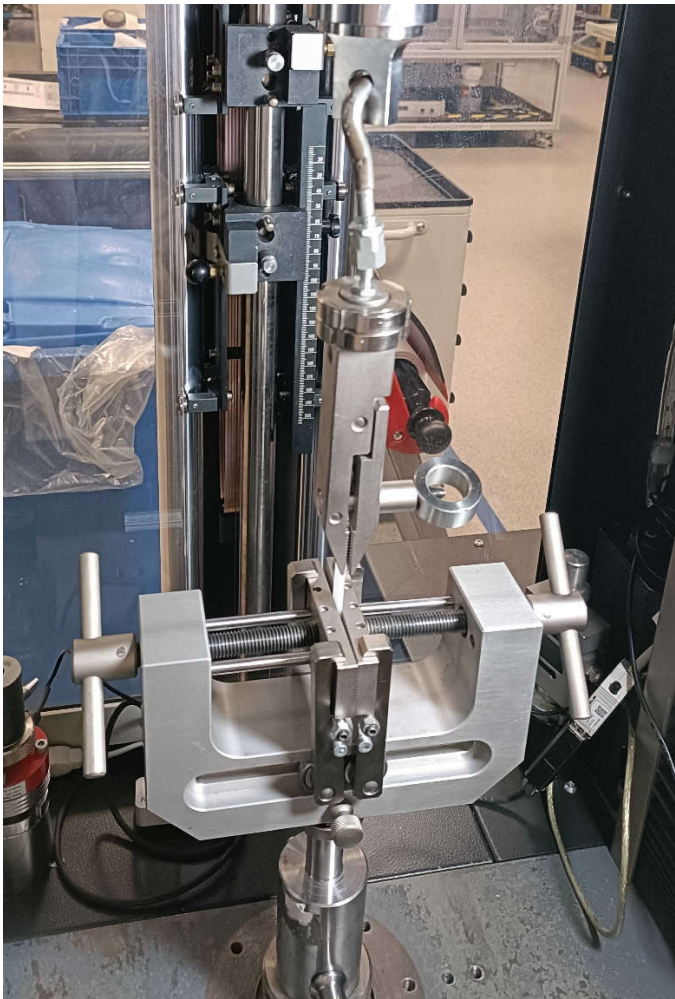


Figure 4. Mounting set for samples on universal testing machine. Rys. 4. System mocujący próbki na maszynie wytrzymałościowej.

In order to read the values of triaxiality (η) and strain rate ($\dot{\epsilon}$), a dynamic explicit FEM simulation was carried out simultaneously using a linear-elastic material model with Young’s modulus $E = 1200 \text{ [MPa]}$ and Poisson’s ratio $\nu = 0,40[-]$. The lack of consideration of material hardening does not have a significant impact on the result due to the limited scope of the study, i.e., observations until the appearance of significant plastic deformations.

4. Experimental Data Processing and Result

A series of twelve tests was conducted according to the combination below. The input values and already calculated output results for each sample were presented simultaneously.

Table 2. Tension test parameter scheme.

Input data			Output data			
No	$R_1 \text{ [mm]}$	$v \text{ [mm/s]}$	$R_{p0,2} \text{ [MPa]}$	$R_{eH} \text{ [MPa]}$	$\eta \text{ [-]}$	$\dot{\epsilon} \text{ [1/s]}$
1	3	0,1	16,75	21,55	0,52	0,00583
2		1	19,43	25,13		0,05830
3		5	19,47	24,79		0,29150
4	5	0,1	14,94	20,09	0,45	0,00499

5		1	18,97	24,11		0,04985
6		5	19,02	25,08		0,24925
7	10	0,1	12,49	20,36	0,40	0,00404
8		1	18,69	22,94		0,04040
9		5	19,14	24,81		0,20200
10	20	0,1	9,52	20,23	0,37	0,00335
11		1	18,47	23,05		0,03345
12		5	19,01	24,53		0,16725

The values of the conventional yield strength ($R_{p0,2}$), the upper yield strength(R_{eH}) and the below engineering stress curve as a function of head travel (presented on Figure 5) were determined according to the relationship:

$$\sigma = \frac{F}{A}$$

(2)

where the current force (F) read from the tensometric sensor was divided by the original cross-sectional area (A). The strain rate ($\dot{\epsilon}$) was obtained thanks to the knowledge of the change in the value of logarithmic elastic deformation ($\Delta\epsilon$) at the smallest possible time increment (Δt), which reached values in the range from 0,04 to 0,06 [s]:

$$\dot{\epsilon} = \frac{\Delta\epsilon}{\Delta t}$$

(3)

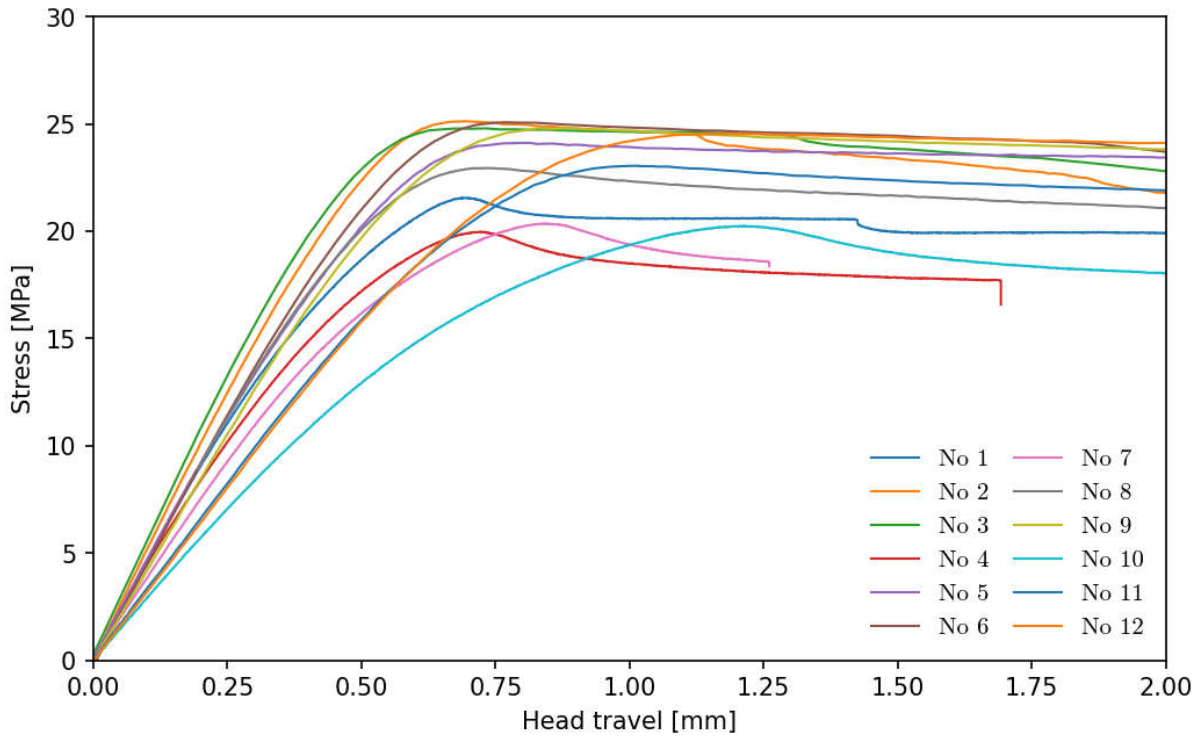


Figure 5. Engineering stress-head travel curves. Rys. 5. Krzywe naprężeń w funkcji drogi głowicy.

The values of triaxiality (η) and strain rate ($\dot{\epsilon}$) were read at the location marked as a curve in Figure 3 at the moment of reaching the conventional yield strength ($R_{p0,2}$).

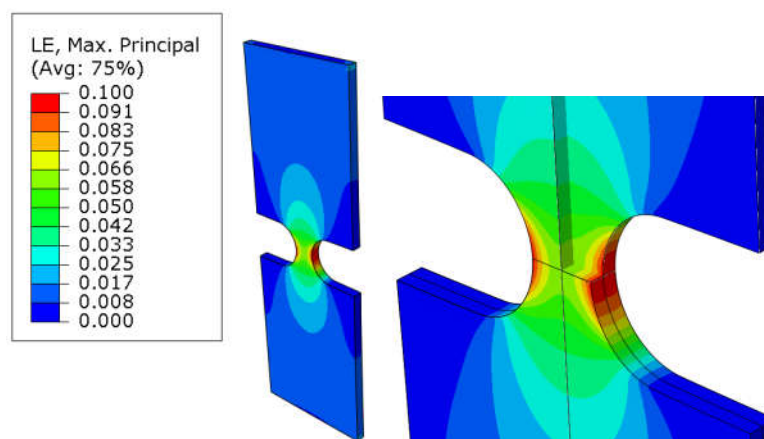


Figure 6. Distribution of logarithmic elastic strains in the critical cross-section for sample no 6. Rys. 6. Rozkład logarytmicznych odkształceń elastycznych w krytycznym przekroju dla próbki nr 6.

The base values obtained in this way were used to construct a graph of the dependence of the conventional yield strength ($R_{p0,2}$) and the upper yield strength (R_{eH}) as a function of strain rate ($\dot{\epsilon}$).

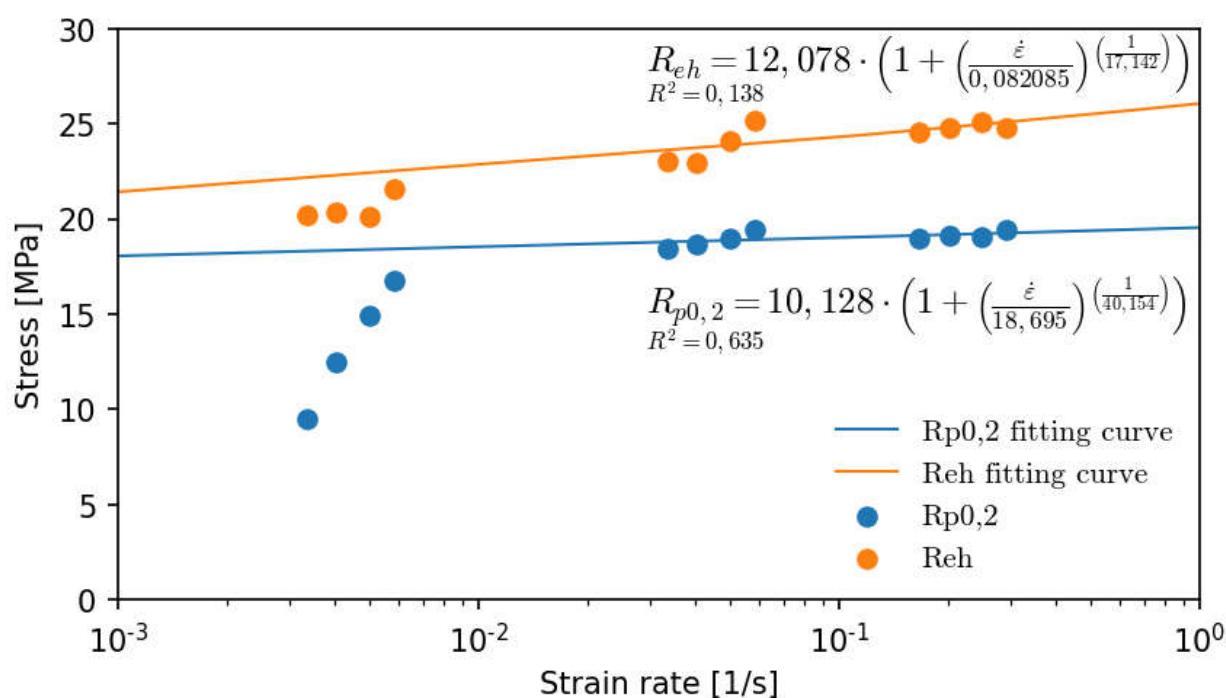


Figure 7. $R_{p0,2}$ and R_{eH} data as a function of elastic stress strain rate ($\dot{\epsilon}$). Rys. 7. Wartości $R_{p0,2}$ i R_{eH} oraz w funkcji prędkości odkształcenia elastycznego ($\dot{\epsilon}$).

Thanks to presenting the results on a logarithmic axis, it was possible at a later stage to justify the exclusion of results for the four lowest strain rate ($\dot{\epsilon}$) values from the regression curves. Their task is to propose the values of coefficients C and q according to relation (1) based on optimization by the least squares method (LSM). Due to the nature of the Cowper-Symonds model, it is possible to adopt flow stress (σ_d) based on the conventional yield strength ($R_{p0,2}$) while maintaining a satisfactory value of the coefficient of determination (R^2), according to the following relationship:

$$\sigma_d = 10,128 \left(1 + \left(\frac{\dot{\epsilon}}{18,695} \right)^{1/40,154} \right) \quad (4)$$

5. Summary, Conclusions and Limitations

The strain rate sensitive hardening of the Polypropylene Sabic 83MF10 under dynamic tension loads were discussed in this article. Based on presented investigation it is possible to highlight that:

- A noticeable non-linear increase in the values of the conventional yield strength ($R_{p0,2}$) and the upper yield strength (R_{eH}) is shaped according to the Cowper-Symonds model for elastic strain rate ($\dot{\epsilon}$) values ranging from 0,01 to 1 [1/s]. For a lower range, a drastic drop in both values is observed, especially the conventional yield strength ($R_{p0,2}$), which suggests a significant influence of the creep and relaxation phenomena. To define them, it is necessary to conduct further research for material models that include, among others, viscoelastic properties [12–14]. For further research, larger values of elastic strain rate ($\dot{\epsilon}$), are suggested, which would allow for additional validation of the proposed model [15].
- Among samples with a similar elastic strain rate ($\dot{\epsilon}$), those with a smaller rounding radius obtain disproportionately higher values of the conventional yield strength ($R_{p0,2}$) and the upper yield strength (R_{eH}). This highlights the existence of a dependency of both these values and flow stress (σ_d) on triaxiality (η). This suggests a high value of further research on the Drucker-Prager model for the aforementioned material [16].
- The proposed hybrid approach, which includes classical calculations and numerical reading of values, despite its advantages in the form of simplified procedures, introduces a noticeable error in reading, among others, the values of current stresses. In order to construct a full true stress-strain curve, it is possible to proceed, among others, in accordance with the Bridgman procedure [17].
- For further research, it is suggested to consider a wider range of examined input parameters. This includes, for example, following the Johnson-Cook model [18,19] and comparing the proposed model for stretched samples with the results of a compression test [20].

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