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Article

Intensity Parameters and Physical Damage in Buildings Due to the Mass Movements Occurred between 3 and 5 November 2019, in Jericó, Antioquia, Colombia

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Abstract: Between 3 and 5 November 2019, mass movements occurred in Jericó, Antioquia, Colombia. Fortunately, no fatalities were reported during the events; however, five houses collapsed, two houses had damaged facade walls, and one power pole collapsed. Based on this, an analytical, probabilistic methodology is used to quantify the hazard intensity that occurred and affected the buildings. Initially, a technical description of the buildings and the damage caused is made. Three critical events are detected for hazard analysis, i.e. two related to landslides and one to debris flow. The hazard intensity is then quantified by determining the probabilistic parameters of velocity, dynamic thrust, momentum flux and overturning moment of the flow that caused damage to the different structures. These data are contrasted with the damage state thresholds for the overall behaviour of structures available in the literature. A structural fragility model in the out-of-plane direction in unreinforced masonry infill walls is used to obtain local complete damage thresholds. In addition, a complete damage threshold is calculated for the power pole. This study provides additional data that can strengthen knowledge related to the assessment of infrastructure risks associated with mass movements.

Keywords: mass movements hazard intensity; mass movements buildings' resistance; mass movements vulnerability; mass movements losses; mass movements risk; mass movements fragility curves; damage thresholds; unreinforced masonry

1. Introduction

Jericó is located to the southwest of the city of Medellín in the department of Antioquia, Colombia. There are reports compiled by the Colombian Geological Service where, since 1922, and on several occasions, events due to mass movements have been reported, repeatedly affecting the municipality's rural and urban areas [1–4]. From November 3 to 5, 2019, mass movements occurred, which caused significant damage to the population, private property and infrastructure [4]. Considering this event, an analytical and probabilistic methodology is used to quantify the mass movements' intensity and the affected buildings' physical vulnerability. There were two types of mass movements associated with the event: a debris flow from Las Nubes Hill, which was transported by the Valladares stream, saturated the sewage system and spread along Sixth Street to the municipal park, causing, among other damage, the collapse of a power pole. On Seventh and Ninth Streets, there were two landslides, which caused the collapse of five houses and damage to the facades of two others. The research considered the type of mass movements to calculate the velocity, dynamic thrust, momentum flux and overturning moment against the buildings. The Monte Carlo simulation technique was used to consider the uncertainty in the variables. The hazard intensity

obtained was compared with the damage state thresholds for the overall behaviour of structures in the literature. For masonry walls subjected to out-of-plane loads and for a power pole, complete damage thresholds were obtained. These thresholds were compared with the hazard intensity to which they were subjected. Quantifying the intensity of mass movements related to the damage state of buildings is scarce and necessary information to obtain damage state thresholds and validate methodologies for calculating physical vulnerability and risk.

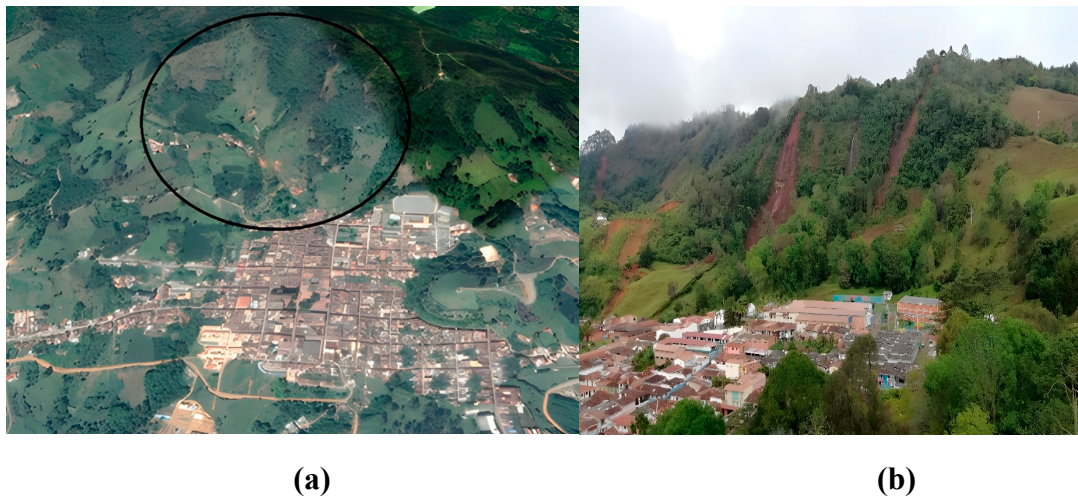


Figure 1. (a) Risk area due to mass movements on the slope of Las Nubes Hill. Source: www.elmundo.com.co; (b) Mass movements November 3, 2019.

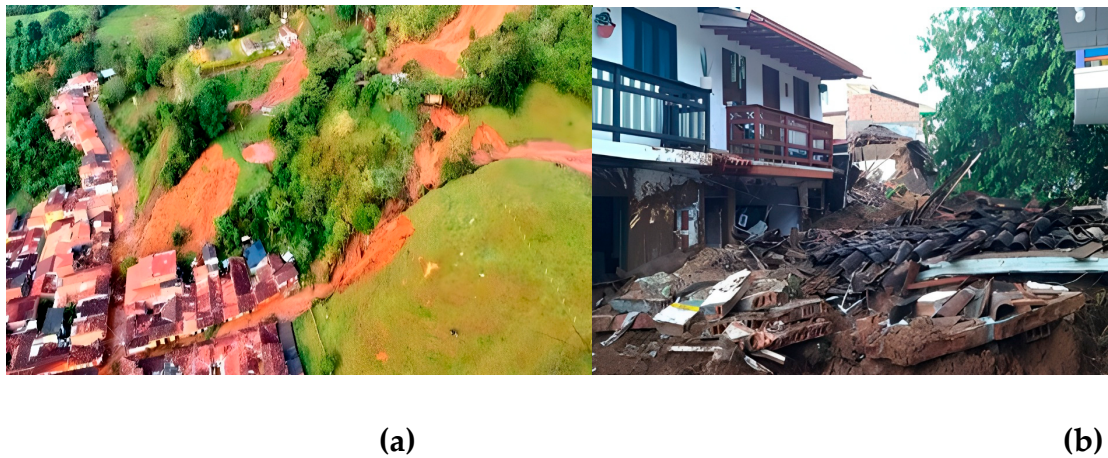


Figure 2. (a) Landslide. 1st Avenue - 6th – 7th Streets. www.eltiempo.com.co; (b) Landslide 1st avenue – 7th Street. Source: www.caracol.com.co.



Figure 3. (a) Debris flow. 1st Avenue – 6th Street. Source: twitter.com/Jericóantioq; (b) Debris flow 1st Avenue - 6th Street. www.eluniversal.com.co.

2. Damages Description to Affected Buildings

2.1. Damages Description House 1

House 1, shown in Figure 4, was directly impacted by the landslide to such an extent that the building collapsed, presenting a complete damage state considering references [5,6]. The single-storey dwelling was constructed of unreinforced clay brick masonry (URM) using horizontal perforated blocks of fired clay and a wooden roof with clay tiles. This building dissipated some of the energy that could reach House 2.



Figure 4. (a) Affected buildings. 1st Avenue – 7th Street, right side; (b) Buildings before the event. 1st Avenue – 7th Street, right side.



Figure 5. (a) The reinforced first storey with reinforced concrete frames. Interior view. house 2; (b) Rear facade. House 2. Reinforced with reinforced concrete wall in the first storey.

2.2. Damages Description House 2

A three-storey house (Figure 4) was built in an initial system of partially reinforced masonry. The walls comprise horizontal perforation blocks 10 cm wide, 20 cm high, 40 cm deep, 3.5 cm thick

mortar, and a 1 cm one-sided plaster. At the time of impact, they were remodelling the first story of the building, for which they built a frame system with 25 x 25 cm columns and beams and a hollow clay block, reinforced concrete slab, as shown in Figures 4 and 5. The building is in a light damage state based on [21,22]. The first-story infill walls were supported transversely on the new columns, and some walls collapsed due to their lack of flexural capacity when subjected to out-of-plane loads (Figures 5 and 6). The span between columns is 2.9 m, and the height of the walls is 2.4 m. After the phenomenon, and probably as a solution to possible future stress due to mass movement, the construction of reinforced concrete walls on the first floor can be observed (Figure 5). These elements help in this type of event, but seismically, they are not necessarily favourable. It is interesting to note that the only infill wall that did not collapse, although cracked, of the four requested spans was the one that was transversely stiffened by the partitions that formed the kitchen of the neighbouring house (house 1) (Figure 6b).



Figure 6. (a) Side facade, infill walls total collapse, House 2; (b) Side facade. Infill walls without total collapse. House 2.

2.3. Damages Description House 3

Figures 4 and 7 show House 3. The house was built with horizontal perforation bricks; the structural system is partially reinforced with masonry. Due to the event, 50% of the building collapsed, including the kitchen and dining room areas. The dwelling damage is classified as extensive, considering references [21,22]. It can also be seen that the building was not hit head-on.



Figure 7. (a) Partially confined masonry structure. Side facade. House 3; (b) Partially confined masonry structure. Front facade. House 3.

2.4. Damages Description House 4

Figure 8 shows the remains of the collapsed house. The single-storey building was structurally made of unreinforced clay brick masonry (URM). The bricks used were horizontal perforation blocks. The roof was made of wood and baked clay tiles. The building before the event is shown in Figure 9. This house was located at the intersection of 2nd Avenue and 9th Street. Based on [21,22], the present dwelling is classified as a complete damage state.



Figure 8. (a) House 4 Collapsed by the landslide; (b) Debris from House 4 due to landslide.



Figure 9. (a) Building before the event. The image about 2nd Avenue. House 4. Source: Google Earth; (b) Building before the event. Image of the intersection of 2nd Avenue and 9th Street. House 4. Source: Google Earth.

2.5. Damages Description House 5 to House 7

Figure 10 shows the only house that remained standing of the three houses across the street (left side) that were impacted head-on by the landslide. However, it is essential to recognise that the collision may have been mitigated, in part, by House 1, as shown in Figure 4. Plus, there is some degree of inclination, possibly favourable. This three-storey building, including the basement, whose predominant structural system is partially reinforced masonry, only damaged its main facade, Figure 10b. The facade consisted of wooden windows and masonry made of hollow horizontal cavity bricks without reinforcement. The collapsed wall had a span of 3.5 meters, as shown in Figures 10 and 11. The damage in this dwelling, based on [5,6], is associated with a light damage state.

Figure 11a shows the rear of lot 6, the only uncollapsed portion of the building visible in Figure 11b. Eighty per cent of the building collapsed, and only vestiges of the roof are visible. About the part that remained standing, three floors of unreinforced masonry (URM) are observed. The walls are made of hollow clay bricks with the following measurements: 10 cm wide by 20 cm high and 40 cm deep, joined with mortar about 3.5 cm thick. Figure 12 shows in detail the remains of House 6. The two-storey collapsed section was supported by 20 cm x 20 cm concrete columns and an earth wall 50

cm thick (Figures 12 and 13); on these elements rested a wooden mezzanine, which, being loose and subjected to the pressure of a landslide, contributed to the collapse of a large part of the building. In Figure 12b, some remains of the front part of the building can be seen along some wooden steps, a wooden wall, and an unreinforced masonry bathroom. Classifying the damage to the dwelling is associated with the complete damage state, according to [5,6]. House 7 (Figures 11b and 12a) is associated with the complete damage state, taking into account [5,6]. This two-storey building was structurally supported by unconfined masonry (URM).



Figure 10. (a) Affected building 1st Avenue – 7th Street, left side. House 5; (b) The facade affected, house 5, 1st Avenue – 7th Street, left side.



Figure 11. (a) Affected buildings 1st Avenue – 7th Street, left side. Houses 5, 6 and 7; (b) Buildings original state 1st Avenue – 7th Street, left side. House 5, 6, and 7. Source: Google Earth.



Figure 12. (a) Houses 6 and 7 collapsed. Left side. 1st Avenue – 7th Street; (b) Affected building 1st Avenue – 7th Street, left side. house 6.



Figure 13. (a) Affected building 1st Avenue – 7th Street, left side. House 6. Earth wall detail; (b) Affected building detail 1st Avenue – 7th Street, left side. house 6.

2.6. Damage Description to Houses Located on Sixth Street and the Lower Part of the Slope of Cerro las Nubes

Since a large part of the debris flow coming from Las Nubes hill was channelled through the Valladales stream, entering from the front on Sixth Street, the road served as a channel dissipating a large amount of energy along the street until almost reaching the principal Park (Figure 3, and 15). A large amount of mud penetrated the first houses through doors and windows, which the community extracted. Nevertheless, although there are economic losses at the finishes and additional works level, there is no evidence of structural damage in the dwellings (Figures 15b and 16). A power pole collapsed due to the impact of the debris flow, Figure 14. The damage classification of the houses located on Sixth Street and the lower part of the slope of Las Nubes Hill, based on [5,6], is associated with the light damage state.



Figure 14. (a) A power pole collapsed on 6th Street, lower slope of las Nubes Hill; (b) Collapsed power pole on 6th Street, lower slope of las Nubes Hill.



Figure 15. (a) Architectural view of houses located on 6th Street and the lower part of the slope of Las Nubes Hill. Source: Google Earth; (b) View of affected houses on the hillside of Las Nubes Hill, Valladares Stream, 6th Street. The photo was taken after evacuating the debris flow.



Figure 16. (a) Affected houses on the hillside of Las Nubes Hill, Valladares stream. 6th Street; (b) Debris level measurement of houses affected hillside of Las Nubes Hill, Valladares stream. 6th Street. The photo was taken after evacuating the debris flow.

3. Theoretical Framework for the Mass Movements Velocity Calculation

For decades, several professionals, due to the socio-environmental and economic problems caused by mass movements, have been concerned with understanding and reducing the phenomenon, so researchers such as [7–12] have published several empirical formulations correlated with different mass movement phenomena in specific places. In these researches, the study of parameters such as the potential volume of debris, mean flow velocity, maximum discharges, and the distance or path of the flow gained significant interest. Mass movements can carry different materials; therefore, determining the appropriate roughness coefficients is difficult. It is essential to understand that the friction between the materials that make up the mass movements and the supporting surface causes the energy to dissipate faster than water flow circulation [13].

Deducing the mass movement velocity at the instant of collision is essential for calculating the stresses acting on any surface. Taking into account the type of flow and its dynamic behaviour along the path, applicable experimental deductions have been made in analytical and numerical methodologies [9,11,13–15], **Error! Reference source not found.** and Eq. (13).

Table 1. Equations to estimate mass movements velocity.

Reference	Equation	
Newtonian laminar flow	$\vec{V} = \frac{\rho gh^2 S}{k\mu}$	(1)
Hungr's equation [7,16]	$\vec{V} = \frac{2}{3}\xi h^{3/2} S^{1/2} \quad \xi = 2.17m^{-1/2} s^{-1}$	(2)
Manning – Strickler equation	$\vec{V} = \frac{1}{\eta} h^{2/3} S^{1/2}$	(3)
Yang's equation [11,17]	$\vec{V} = \frac{1}{\eta_1} h^{2/3} S^{1/2} \quad \eta_1 = 0.054h^{0.42}$	(4)
Du's equation [13]	$\vec{V} = \frac{1}{\eta_2} h^{2/3} S^{1/2} \quad \eta_2 = 0.035h^{0.34}$	(5)
Chézy equation [8]	$\vec{V} = \frac{h^{1/2} S^{1/2}}{C^{1/2}}$	(6)
Empirical equation [8]	$\vec{V} = C_1 h^{0.3} S^{0.5}$	(7)
Lo'equation [16,18]	$\vec{V} = k_1 h^{2/3} S^{1/5}$	(8)
Prochaska's equation [19]	$\vec{V} = 0.35h^2 S + 5.36$	(9)
Hu's equation [10]	$\vec{V} = 8.94h^{0.15} b^{0.35} S^{0.5}$	(10)
Yang's equation [11]	$\vec{V} = 6.54p^{0.39} h^{1/2} S^{1/3} \quad 2\% < p < 14\%$	(11)
Wang's equation [12]	$\vec{V} = 7.451Cv^{0.391} h^{0.5} S^{0.011 \ln(Cv) + 0.054}$ $0.1 < Cv < 0.9$	(12)

Note: The abbreviation and symbol used in Table 1 have been described at the manuscript's end.

Table 2. Relationship between the coefficient k1 and the depth of the debris flow.

H (m)	<2.5	2.75	3	3.5	4	4.5	5	>5.5
K1	10	9.5	9	8	7	6	5	4

Note: Taken from [18]. The abbreviation and symbol used in Table 2 are described at the manuscript's end.

Table 3. Chézy coefficient, for Newtonian or near Newtonian flows.

Type	C
Water, smooth channel	0.0025
Mudflow	0.002
Pinatubo - mudflow	0.0024
Sediment laden flow	0.005
Pinatubo - hyper-concentrated flow	0.009-0.014
Mangatoetoenui - lahar	0.02 - 0.1
Pinatubo - lahar	0.01 - 0.3
Lahars	0.01 - 1
Debris flow	0.06 - 0.577
Wet landslide	0.184

Note: Taken from [20]. The abbreviation and symbol used in Table 3 are described at the manuscript's end.

Eq. (13) calculates the landslide's velocity [21,22]. This expression is an analytical deduction based on kinematics under the sliding block model, which models a landslide's movement as a block's movement on a curved surface with a constant frictional strength.

$$\vec{V} = \sqrt{2h'g\left(1 - \frac{\tan(\phi)}{S}\right)}$$

(13)

4. Theoretical Framework for the Calculation of Mass Movements Dynamic Thrust against Buildings

Hungr et al. (1984) [7] present perhaps the most famous hydrodynamic formulation to quantify mass movement hitting against a vertical barrier [23]. The authors determine that the mass movements dynamic thrust can be calculated with Eq. **Error! Reference source not found.** for barriers almost perpendicular to the flow direction. The hydrodynamic model's dimensionless impact coefficient (k) is 1.50. This value depends on the grain size distribution of the flow [24,25].

$$F=C_d\rho A_c\vec{V}^2\sin\beta$$

(14)

Below are some experimentally developed hydrostatic and hydrodynamic models for calculating the pressure from mass movements against vertical barriers.

Table 4. Hydrodynamic and hydrostatic hydraulic models.

Reference	Equation		
Zhang (1993)	$P=C_d\rho V^2\cos^2(\alpha)$	$c_d=3\sim5$	(25)
Armani (1997)	$P=c_s\rho gh$	$c_s=4.50$	(16)
Scotton and Deganutti (1997)	$P=c_s\rho gh$	$c_s=2.50\sim7.50$	(17)

Note: Debris flow impact pressure [N/m²]. Taken from [23,24,26]. The abbreviation and symbol used in Table 4 are described at the manuscript's end.

A dynamic pressure coefficient (k) equal to 2.5 is adjusted to the mean impact pressure due to mass movement, considering boulders with diameters up to 0.5 meters [18,27]. If larger diameters are present, the effect of the dynamic impact of mass movement and boulders should be calculated separately.

Table 5 shows experimentally developed mixed models for calculating mass movement pressure in vertical barriers. After identifying the strengths and weaknesses of hydrostatic and hydrodynamic models, researchers conclude that mixed models seem to be the best method to predict the pressure exerted by mass movements on a barrier [14]; they establish that the impact pressure can be calculated using Eq. **Error! Reference source not found.**

Table 5. Mixed hydraulic models.

Reference	Equation		
Arattano and Franzi (2003)	$P=C_m(0.5\rho gh+\rho V^2)$	$C_m=1.0$	(38)
Hübl and Holzinger (2003)	$P=C_m\rho(gh)^{0.6}V^{0.8}$	$C_m=5.0$	(19)
Cui et al (2015)	$P=C_mF_r^{-1.5}\rho V^2$	$C_m=5.3$	$F_r=\frac{V}{\sqrt{gh}}$ (20)
Gong, 2020	$P=2.07F_r^{1.64}\rho gh$	$F_r=\frac{\vec{V}}{\sqrt{gh}}$	(21)

Note: Mass movements impact pressure [N/m²]. Taken from [14,23]. The abbreviation and symbol used in Table 5 are described at the manuscript's end.

According to the recommendations of the regulation FEMA, 2017 [6], used by Prieto et al., 2018 [28]; Kean et al., 2019 [29], the acting force can be calculated with Eq. (22).

$$F_a=\frac{K_d}{2}C_d\rho B(hV^2)$$

(22)

5. Theoretical Framework for Structural fragility curves

Fragility curves represent the probability of reaching or exceeding a specified limit damage state when a structure is subjected to a given hazard intensity. In the following definition, momentum flux

was used as the intensity parameter (Eq. (23)). Nevertheless, other variables, such as height (h) or overturning moment (h^2v^2), can also be used. Log-normal functions are proposed as mass movement fragility curves using the momentum flux, hv^2 (where h and v are the height and velocity of mass movement at a given site, respectively) as the hazard intensity parameter [30]. Each curve is characterised by a median value and its log-normal standard deviation (β). Therefore, the probability of reaching or exceeding a specific damage state, given a structural response due to a defined hazard (mass movements), can be calculated as follows:

$$P[DS/hv^2]=\Phi\left[\frac{1}{\beta_{DS}}\ln\left(\frac{hv^2}{\overline{hv^2}_{DS}}\right)\right] \tag{23}$$

Which denotes a cumulative logarithmic normal distribution, where:
 hv^2 : the mass movement impact index represents the intensity of the hazard.
 $\overline{hv^2}_{DS}$: it is the median value of the impact index at which the building reaches the Damage State (DS).
 β_{DS} : it is the standard deviation of the natural logarithm of the impact index associated with a Damage State (DS).
 Φ : it is the standard normal cumulative distribution function.
These curves are defined by two parameters: the median value $\overline{hv^2}_{DS}$ and the standard deviation β_{DS} . The median value defines the point at which the probability of equaling or exceeding the damage state equals 50%, and the standard deviation gives an idea of the scatter.

6. Calculations and Results Analysis

This item aims to find measures of velocity, dynamic thrust, momentum flux, overturning moment, and structural fragility parameters. The research refers to three events. The one on First Avenue with Seventh Street related to the landslide of a slope collapsing houses 1, 6, and 7 referenced in item 2 (Figures 4 and 11). The one that occurred at the junction of Second Avenue with Ninth Street due to the landslide of a slope collapsing a house (Figures 8 and 9), and what happened at the intersection of Sixth Street with Las Nubes hill regarding debris flows channelled over the Valladales stream, reaching Sixth Street, and travelling to the vicinity of the central municipal park (Figure 3).

6.1. Calculation of Flow Velocity in Collapsed Houses

The events that occurred at First Avenue and Seventh Street and the one at the intersection of Second Avenue and Ninth Street are related to the landslide of a block of soil adjacent to the houses (Figures 4 and 13), triggered, among other reasons, by the high rainfall in the area. For this reason, Eq. (13) consistently calculates the velocity. Due to the uncertainty of the phenomenon, a probabilistic analysis using Monte Carlo simulation is required. According to the different variables visible in Eq. (13), this research chooses to use the continuous uniform probability distribution function since, among other functions, it provides maximum entropy when only extreme data are available. Table 6 shows the variables referred to. For the dynamic soil friction coefficient (φ), this research uses values referenced in RM Iverson, 1997 [31].

Table 6. Field parameters for velocity calculation.

Variable	Minimum	Maximum	Setting function
φ (°)	2.29	14	uniform
β (°) Houses 1, 6 y 7	14	15	uniform
β (°) House 4	16	17	uniform
h' (m) Houses 1, 6 y 7	5	7	uniform
h' (m) House 4	3	4	uniform

The adjustment was performed based on the Kolmogorov-Smirnov statistical criterion (K-S test), obtaining the parameters shown in Tables 7 and 8. This information is relevant to continuing the probabilistic analysis of the thrust acting on the houses studied (Table 9).

Table 7. Statistical parameters for the calculation of velocity, houses 1, 6 and 7.

Setting function	Triangular
Minimum	0.53
Maximum	10.78
Mode	9.15
Mean	6.82
Median	7.18
Standard deviation	2.25

Note: Units are in m/s.

Table 8. Statistical parameters for the calculation of velocity, house 4.

Setting function	Pert
Minimum	1.75
Maximum	8.32
Mode	6.22
Mean	5.83
Median	5.92
Standard deviation	1.21

Note: Units are in m/s.

6.2. Calculation of Thrust and Acting Momentum Flux Collapsed Houses

Following recommendations of FEMA, 2017 [6], using Eq. (22), the variables with their respective setting functions are recognised in Table 9. The variables and their uncertainties referring to the mass movements, such as density (ρ), drag coefficient (C_d), and impact coefficient due to debris size (k_d), are obtained according to [6,30]. The flow height during impact (h) is a time-varying measure. The research uses a continuous uniform fit function for its representation, which expresses the maximum entropy.

Under the Kolmogorov-Smirnov statistical criterion (K-S test), the Lognormal and general Beta functions efficiently fit the actual data for calculating thrust and momentum flux. The statistical data are reported in Tables 10 and 11.

Table 9. Field parameters for dynamic thrust calculation.

Input parameter	Minimum	Probable	Maximum	Median	Standard deviation	Setting function
v (m/s), Houses 1, 6 y 7	0.53	9.15	10.78			Triangular
v (m/s), House 4	1.75	6.22	8.32			Pert
h (m), Houses 6 y 7	1		2.5			Uniform
h (m), House 4	1		2			Uniform
B (m)	6		8			Uniform
ρ (kg/m ³)				1700	204.74	Log normal
K_d				1.2	0.67	Log normal
C_d				2	0.77	Log normal

Table 10. Statistical parameters for dynamic thrust calculation.

Event	Setting function	Mean	Median	Mode	Standard deviation
Houses 1, 6 y 7	Lognormal	1327	841.8	315.53	1622.9
House 4	Lognormal	761	556.64	294.26	713.51

Note: Units are in kN.

Table 11. Statistical parameters for momentum flux calculation ($h v^2$).

Setting function	General Beta (houses 1,6,7)	General Beta (houses 4)
$\alpha 1$	1.35	2.65
$\alpha 2$	2.91	5.53
Minimum	0.56	4.3
Maximum	282.71	155.05
Mean	89.91	53.14
Median	81.26	50.89
Mode	44.15	44.56
Standard deviation	57.22	23.28

Note: Units are in m^3/s^2 . $\alpha 1$ and $\alpha 2$ continuous shape parameters.

6.3. Collapsed Infill Walls First Floor, House 2

House 2 had no significant structural overall damage; however, some facade lateral walls collapsed in the first story, Figure 4. Unreinforced masonry infill walls (Figure 6) were forced by the landslide to an out-of-plane stress phenomenon, as shown in Figure 18. Although unconfined and unreinforced masonry offers little resistance to this event, damage thresholds will be calculated below. The first-story partition walls in house 2 collapsed a few meters away from houses 1, 6, and 7, analysed previously. Therefore, the magnitudes and other probabilistic data will be helpful.

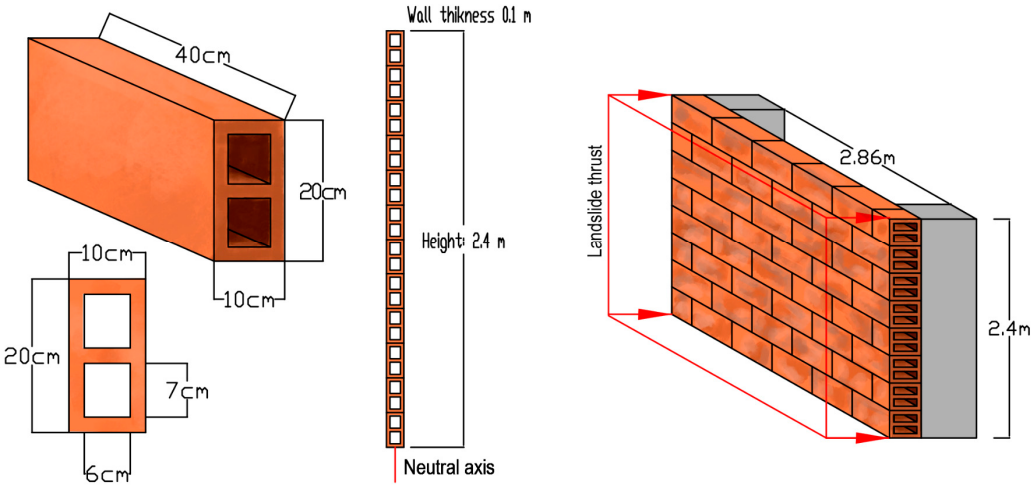


Figure 18. Infill wall, subjected to dynamic lateral thrust due to landslide. 1st Avenue / 7th Street. Dwelling 2.

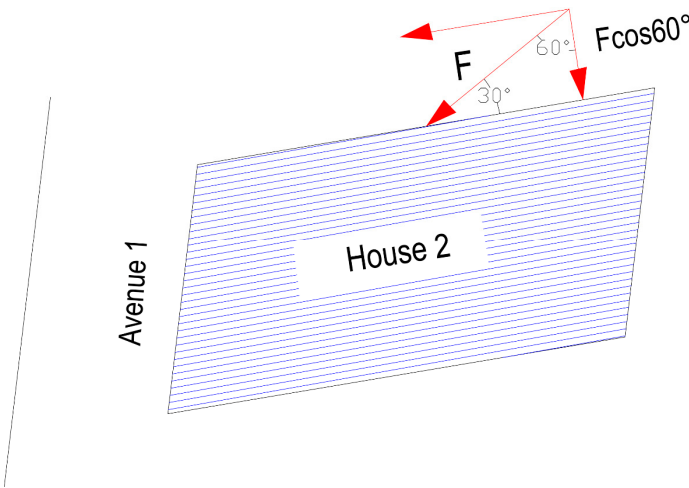


Figure 19. Location of house 2 and landslide angle of attack. 1st Avenue, 7th Street.

6.3.1. Calculation of Acting Momentum Flux in Collapsed Infill Walls, House 2

The landslide did not push the house and its partitions perpendicularly, and there was an angle of attack of 60°, Figure 19. Using the information in Table 11 and the angle of attack on the wall, an acting median momentum flux of 40.63 m³/s² and a standard deviation of 28.61 m³/s².

6.3.2. Infill walls fragility curve due to out-of-plane loads by the landslide

Since the 50s, different analytical, numerical, and experimental studies have been carried out regarding the out-of-plane direction strength of the unreinforced masonry walls [32–48]. Consistent with [49] y [37], the damage thresholds in walls subjected to out-of-plane loads in the present research are calculated considering the study carried out by [41]. Abrams et al., 1996 [41] assumed the wall resists a uniform lateral load through a one-way arch mechanism. Therefore, researchers determine the ultimate strength of the out-of-plane walls, as seen in Eq. (24). Asteris et al., 2017 [50] present a best-fitting equation for calculating the coefficients for fixed H/t ratios; see Eq. (25).

$$q_{ult} = \frac{0.7 f' m \lambda}{\frac{H}{t}} (LH)$$

(24)

$$\lambda = 1.38 \left(\frac{H}{t} \right)^{-1.41}$$

(25)

The ultimate capacity of the wall is equated; see Eq. (24), with the request due to the landslide visible in Eq. (22). If all field parameters are known, see Tables 12 and 14. Through techniques such as Monte Carlo, a function log-normal analytical is obtained regarding momentum flux (hv²), determining complete damage thresholds in walls subjected to out-of-plane loads (Tables 13 and 15).

Table 12. Field parameters, ultimate out-of-plane load capacity for infill walls by landslide.

Input parameter	Minimum	Probable	Maximum	Median	Standard deviation	Setting function
f'm (MPa)				3	0.9	Log normal
H (m)	2.3		2.6			Uniform
B (m)	2.7		2.9			Uniform
t (m)	0.1		0.12			Uniform

Table 13. Statistical parameters, ultimate out-of-plane load capacity for infill walls by landslide.

Event	Setting function	Mean	Median	Mode	Standard deviation
House 2	Lognormal	11.3	10.75	9.72	3.73

Note: Units are in kN.

Table 14. Field parameters, infill walls fragility curve due to out-of-plane loads by landslide, complete damage state.

Input parameter	Minimum	Probable Maximum	Median	Standard deviation	Setting function
Fu (kN)			10.75	3.73	Log normal
Kd			1.2	0.67	Log normal
Cd			2	0.77	Log normal
q (kg/m ³)			1700	204.74	Log normal
B (m)	2.7	2.9			Uniform

Table 15. Statistical parameters for the calculation of the infill walls fragility curve due to out-of-plane loads by landslide, complete damage state.

Event	Setting function	Mean	Median	Mode	Standard deviation
House 2	Lognormal	0.47	0.46	0.45	0.08

Note: Units are in m³/s².

The median value capacity in terms of momentum flux for a complete damage state in infill walls house 2 is approximately 0.46 m³/s² (Table 15), which is essential to explain the collapse of these structures when compared to the median value of momentum flux acting on the infill walls of 40.63 m³/s², as referred in item 6.3.1.

6.4. Collapsed Power Pole Analysis

The only structure that collapsed at the intersection of Sixth Street and Las Nubes Hill was a power pole. This element is used as a calibration to obtain parameters of velocity, dynamic thrust, momentum flux, and overturning moment (Figure 14) to generate knowledge that helps objectively interpret this kind of event.

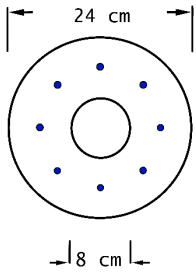


Figure 21. Cross section of the power pole located on 6th Street on the slope of Las Nubes Hill.

The power pole was 8 m high and had a reinforced concrete cross-section, as shown in Figure 21; the reinforcement consisted of 8 longitudinal bars ½ in each and 4 mm diameter stirrups (wire) located every 11 cm.

6.4.1. Calculation of Flow Velocity, Collapsed Power Pole

A probabilistic analysis using Monte Carlo simulation was performed to calculate the debris flow velocity at 40 meters from Sixth Street's intersection and Cerro Las Nubes's slope. The

formulations shown in Table 1 are used for channelised debris flows such as the one that occurred on Sixth Street (see Figure 3), considering equal probabilistic weight for each equation. Table 16 shows the variables used in the velocity calculation, their randomness, and the respective setting functions.

Table 16. Parameters for calculating the debris flow velocity over 6th street coming from Las Nubes Hill.

Variable	Minimum	Maximum	Setting function
Cv	0.1	0.9	uniform
h (m)	1.0	2.0	uniform
p (%)	2.0	14	uniform
C	0.0025	0.014	uniform

Table 17. Statistical data for debris flow velocity calculation.

Setting function	General Beta
$\alpha 1$	16.80
$\alpha 2$	18.56
Minimum	3.29
Maximum	6.42
Mean	4.78
Median	4.78
Mode	4.77
Standard deviation	0.26

Note: Units are in m/s.

The contact width of the debris flow over pole (B) equals 0.38 m, deduced as half perimeter, and the slope of Sixth Street (S) equals 0.054. The above are known parameters. According to the Kolmogorov-Smirnov statistical criterion (K-S test), the General Beta function is the one that best fits the actual data for the calculation of the velocity, obtaining the statistics shown in Table 16. This information is relevant to continue the probabilistic analysis of the thrust acting on the collapsed power pole (Table 17).

6.4.2. Calculation of the Debris Flow Dynamic Thrust on the Collapsed Power Pole

Following the recommendations of FEMA, 2017 [6], and using Eq. (22), Table 18 shows the variables used with their respective setting functions..

Table 18. Field parameters for calculating debris flow dynamic thrust on the collapse of a power pole.

Input parameter	$\alpha 1$	$\alpha 2$	Minimum	Maximum	Median	Standard deviation	Setting function
v (m/s)	16.80	18.56	3.29	6.42			General Beta
h (m)			1.0	2.0			Uniform
q (kg/m ³)					1700	204.74	Log normal
Kd					1.2	0.67	Log normal
Cd					2	0.77	Log normal

The variables in Table 18 referring to density (q), drag coefficient (Cd), and impact coefficient due to debris size (kd) are obtained according to [6,30]. The debris flow height at the moment of impact (h) is a time-varying measure; in the present research, a continuous uniform fit function is used to represent maximum entropy. Under the Kolmogorov-Smirnov statistical criterion (K-S test), the Lognormal and Pert functions efficiently fit the actual data for the calculation of thrust, momentum flux, and overturning moment, respectively, obtaining the statistical data shown in Tables 19–21.

Table 19. Statistical data for calculating the debris flow dynamic thrust on the power pole.

Setting function	Log normal
Mean	26.58
Median	21.01
Mode	13.14
Standard deviation	20.58

Note: Units are in kN.

Table 20. Statistical data for calculating the power pole's debris flow momentum flux ($h v^2$).

Setting function	Pert
Minimum	17.04
Maximum	59.93
Mean	34.46
Median	33.98
Mode	32.44
Standard deviation	7.96

Note: Units are in m^3/s^2 .**Table 21.** Statistical data for calculating the debris flow overturning moment ($h^2 v^2$).

Setting function	Pert
Minimum	17.71
Maximum	119.16
Mean	53.41
Median	51.09
Mode	41.96
Standard deviation	20.43

Note: Units are in m^4/s^2 .

6.4.3. Development of the Power Pole Complete Damage Threshold due to Debris Flow

$$V = \frac{\sqrt{f'c}}{6} bd \quad (26)$$

The power pole is impacted at the base by the debris flow and response in terms of shear strength, according to Eq. (26). This expression is used following recommendations of ACI 318 2014 for circular sections in reinforced concrete [51]. Where b is equal to the diameter of the cross-section and d corresponds to $0.8b$. Since the transverse reinforcement found was insignificant, its contribution to shear strength is not considered. Continuing a probabilistic analysis, Table 22 shows the variables used, knowing that the cross-section of these power poles is hollow. Using the Monte Carlo technique, a cumulative log-normal function representative of the shear capacity is obtained, see Table 23, transcendental information to match with hazard and find a cumulative log-normal function in terms of momentum flux ($h v^2$). Look at Tables 24 and 25.

Table 22. Field parameters, ultimate power pole load capacity.

Input parameter	Minimum	Probable	Maximum	Median	Standard deviation	Setting function
$f'c$ (MPa)				14	4	Log normal
De (m)	0.2		0.21			Uniform
Di (m)	0.06		0.08			Uniform

Table 23. Statistical parameters, ultimate power pole load capacity.

Event	Setting function	Mean	Median	Mode	Standard deviation
Power pole	Lognormal	18.33	18.13	17.75	2.66

Note: Units are in kN

Table 24. Field parameters, power pole complete damage threshold due to momentum flux.

Input parameter	Minimum	Probable Maximum	Median	Standard deviation	Setting function
Fu (kN)			18.13	2.66	Log normal
Kd			1.2	0.67	Log normal
Cd			2	0.77	Log normal
q (kg/m ³)			1700	204.74	Log normal
B (m)	0.375	0.375			Uniform

Table 25. Statistical parameters, power pole complete damage threshold due to momentum flux.

Event	Setting function	Mean	Median	Mode	Standard deviation
Power pole	Lognormal	36.15	28.87	17.54	26.31

Note: Units are in m³/s².

To check the bending capacity of the power pole according to [51] Eq. (27) is used, considering that the gravitational axial load applied to the power pole is less than 10% of Agf^c .

$$Mn = AsfyZ \tag{27}$$

Where Mn represents the nominal bending strength in the section. As it represents the area of the longitudinal reinforcement. fy is the specified yield strength of the reinforcement. Z , equal to 0.7b, is the distance between the points of application of the resulting forces tensile and compression.

Equating capacity with demand makes it possible to obtain an analytical expression regarding overturning moment (h^2v^2). Table 26 shows the variables used. Through Monte Carlo simulation, a log-normal cumulative function is obtained that represents a complete damage threshold for power poles such as the one found in Jericó, having as intensity the overturning moment due to debris flows (see Table 27).

Table 26. Field parameters, power pole complete damage threshold due to overturning moment.

Input parameter	Minimum	Probable Maximum	Median	Standard deviation	Setting function
fy (MPa)			240	15	Log normal
Kd			1.2	0.67	Log normal
Cd			2	0.77	Log normal
q (kg/m ³)			1700	204.74	Log normal
B (m)	0.375	0.375			Uniform
As (cm ²)	3	5			Uniform

Table 27. Statistical parameters, power pole complete damage threshold due to overturning moment.

Event	Setting function	Mean	Median	Mode	Standard deviation
Power pole	Lognormal	70.79	56.46	35.91	53.55

Note: Units are in m⁴/s².

7. Discussion

This research provides information on flow intensity parameters, including velocity, dynamic thrust, momentum flow and overturning moment, between 3 and 5 November 2019 in Jericó,

Antioquia, Colombia. It also provides a technical description of the structural damage to the impacted buildings. In addition, it includes information on the structural fragility of unreinforced masonry buildings in the municipality due to mass movements.

The median thrust for houses 1, 6, and 7 is 841.8 kN, and for house 4, it is 556.64 kN (Table 10). The median momentum flux for houses 1, 6, and 7 is $81.26 \text{ m}^3/\text{s}^2$, and for house 4, it is $50.89 \text{ m}^3/\text{s}^2$ (Table 11). This is contrasted with the median momentum flux threshold of $23.30 \text{ m}^3/\text{s}^2$ for a complete damage state in URM Colombian structures [30], which supports the collapse of the unreinforced masonry houses studied.

Although the damage to house number two was slight, some facade walls collapsed because they were forced to flex out-of-plane due to the landslide. The median momentum flux that caused the walls to collapse was $40.63 \text{ m}^3/\text{s}^2$, contrasted with a complete damage threshold equal to $0.46 \text{ m}^3/\text{s}^2$. This analysis reiterates the inability of unreinforced masonry to assume flexion out-of-plane. Although these types of local failures in a building must be analysed, it is essential to appreciate that the partially confined masonry building's overall stability was maintained. The three-story building also has a reinforced concrete frame system at the first-story level, giving it additional strength. It must be recognised that part of the lateral load with which this building was analysed (house 2) was dissipated by the collapsed house, number 1.

Electricity, among other services, is vital even in atypical situations such as those generated by debris flows. However, for the event that occurred in Jericó, the collapse of a power pole was observed under a medium thrust of 21.01 kN, a median momentum flux of $33.98 \text{ m}^3/\text{s}^2$, and a median overturning moment of $51.09 \text{ m}^4/\text{s}^2$. Contrasting complete damage thresholds with a shear median capacity of 18.13 kN, a median momentum flux of $28.87 \text{ m}^3/\text{s}^2$, and a median overturning moment of $56.46 \text{ m}^4/\text{s}^2$. According to what was observed on the ground, the hydraulic concrete of the power pole failed at the base when the shear force of the debris flow impacted it.

Considering the different variables and the uncertainty in calculating intensity and structural fragility, it was decided to do a probabilistic analysis using Monte Carlo simulation. It is necessary to know the different variables to reduce uncertainty by taking advantage of prior knowledge and field data. The technique illustrated in this work allows the probability calculation of hazard intensity, structural fragility, and risk against mass movements.

8. Conclusions

The research offers field data, hazard intensity measurement, damage auscultation, and thresholds of structural damage due to mass movements, according to what happened in Jericó, Antioquia, Colombia. This information is expected to help advance the probabilistic quantification of the hazard intensity, vulnerability, and risk due to mass movements, contributing to risk reduction through knowledge ownership.

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Symbols

As	Area of longitudinal tensile reinforcement
$\overline{hv^2}_{DS}$:	The median value of the impact index at which the building reaches the threshold of a damage state
b	The diameter of the cross-section
B	Barrier element width. The mass movement direction is perpendicular to this dimension
C	Chezy coefficient
cd	Drag coefficient
Cv	Sediment volumetric concentration
d	Corresponds to 0.8b
db	The diameter of the longitudinal reinforcement
De	Cross external diameter
Di	Cross internal diameter
f'c	Specified compressive strength of the concrete
f'm	Specified compressive strength of the masonry
Fu	The ultimate strength
fy	Yield strength of the longitudinal reinforcement
h	Mass movement depth
H	Wall effective height
h'	Vertical measurement of the landslide
hv ²	Momentum flux or impact index
h ² v ²	Overturning moment
Kd	Impact coefficient
L	Wall length
Mn	The nominal bending strength in the section
p(%)	The clay content of sedimentary material
qult	The ultimate strength of the out-of-plane walls
S	The bed slope where the stream flows
t	The effective thickness of the wall
v	Mass movement frontal velocity
V	Concrete shear strength
Z	Distance between the points of application of the resulting forces tensile and compression
β	The standard deviation of the natural logarithm of a variable
β _{DS}	Standard deviation of the natural logarithm of the impact index associated with a damage state
q	Mass movement density
Φ	The standard normal cumulative distribution function
Abbreviations	
URM	Unconfined, unreinforced clay brick masonry
sd	The standard deviation of a variable
P[DS/hv ²]	Probability of reaching or exceeding a specific damage state, given a structural response due to a defined hazard (mass movements)

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