

Multi-channel Precision Voltage Source for Experiments on Quantum dots

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Abstract:

To realize precise control of single quantum dots (Qdots) device, the high-performance bias source play the key role. In this paper, the 16-channel high precision voltage bias source prototype for Qdots device with 18-bit resolution was designed. The prototype was made and its performance was tested. The short time fluctuations can reach 50 μ V. The up-step and the down-step response time can achieve less than 3 μ s. The stability, linearity and setting time of the bias source exhibits good performance. What's more, the voltage bias source can be controlled by local and online. The results show that it is one effective and feasible topology for the high precision voltage bias source in Qdots device application.

Keywords: quantum dots; *bias source*; *Multi-channel*, *high precision*

Introduction:

Recently, as many fundamental properties are size dependent in the nanometer range, a great deal of attention has been focused on the optoelectronic properties of quantum dots (Qdots)[1-4]. Qdots is one of most significant basic structures of nano-electronics which is regarded as development direction of the next generation semiconductor devices to replace traditional semiconductor technology[5, 6]. The Qdots device was widely investigated for quantum computing[7, 8], quantum detection[9, 10], quantum communication[11, 12] and quantum measurement[13-16].

In general, it is necessary to apply bias voltage on the gate of quantum dots to empty the two-dimensional electron gas below them and form quantum dots or quantum dot contact channels[17]. The Qdots device is mostly general driven by electric including current and voltage bias[18, 19]. The stability, linearity and setting time of bias source are key factors to affect the Qdots device performance[20-23]. In order to realize precise control of single quantum dots and quantum channels, it is meaningful to investigate on the high precision and quality bias source for Qdots device.

To our knowledge, the existing instruments are large volume with few channels or with limited accuracy[24, 25], meanwhile multi-channel and high precision bias voltage source is rarely reported in the literature. ADI recommends to use high resolution DAC chip to design the bias voltage source[26, 27]. Although precision DAC components are already on the market, building a multi-channel high-resolution system is not easy and cannot be treated hastily. The sources of error must be fully considered, which occur

The output voltage expression[29] of 18bit DAC is:

$$V_{out} = \frac{(V_{refp} - V_{refn}) * D}{2^{18} - 1} + V_{refn} \quad (1)$$

where:

V_{refn} provides a negative reference voltage for the DAC;

V_{refp} provides a positive reference voltage for the DAC;

D is an 18-bit binary programming value.

2) Output voltage accuracy and temperature drift analysis

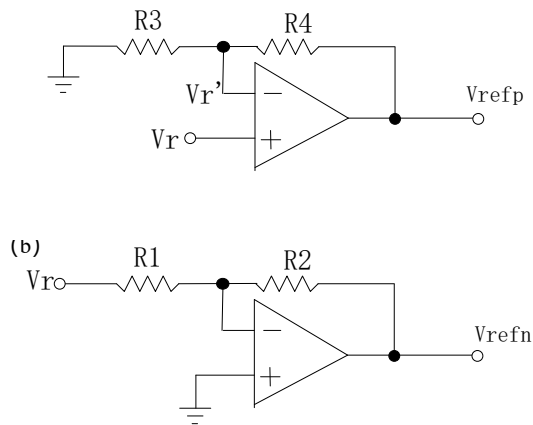


Fig.2. (a) Positive polarity reference voltage generating circuit ;(b) Negative polarity reference voltage generating circuit

As shown in Fig 2(a), V_r is the reference voltage, we choose the ultralow noise, LDO XFET voltage references with current sink and source(adr445B, ADI), temperature coefficient is 2ppm, the output voltage is $5V \pm 2mV$.

Regardless of the influence of the op amp bias current, assuming that the op amp offset voltage is V_{os1} , let $V_r' = V_r + V_{os1}$, according to the “virtual disconnection” principle, the following formula:

$$\frac{V_r'}{R_3} = \frac{V_{refp} - V_r'}{R_4} \quad (2)$$

So that,

$$V_{refp} = \left(1 + \frac{R_4}{R_3}\right) V_r' \quad (3)$$

As shown in Fig 3(b), assuming that the op amp offset voltage is V_{os2} , let $V_r'' = V_r + V_{os2}$, and the same can be obtained:

$$\frac{V_r''}{R_1} = \frac{-V_{refn}}{R_2} \quad (4)$$

$$V_{refn} = -V_r'' * \frac{R_2}{R_1} \quad (5)$$

Where :

V_{refn} provides a negative reference voltage for the DAC;

V_{refp} provides a positive reference voltage for the DAC.

Substituting formula (2), (3), (4), (5) into formula (1), we can get:

$$V_{out} = \left(\left(1 + \frac{R_4}{R_3} \right) * (V_r + Vos1) + \frac{R_2}{R_1} * (V_r + Vos2) \right) * \frac{1}{2^{18}-1} * D - \frac{R_2}{R_1} * (V_r + Vos2) \quad (6)$$

Assuming that R_2/R_1 , R_4/R_3 , V_r , $Vos1$, $Vos2$ do not change with temperature and time, V_{out} can be simplified to:

$$V_{out} = a * D + b \quad (7)$$

Here, R_1 , R_2 , R_3 , R_4 use Vishay bulk metal thin film voltage divider resistor series 300144Z and 300145, its resistance tracking temperature coefficient is 0.1 ppm/°C.

It can be seen from the above formula that the bias output voltage will be affected by the drift of the DAC, resistance, reference voltage, and operational amplifier.

The reference voltage source adopts ADR445BRZ to output 5V, and the temperature drift is about 2ppm/°C, which is 10 uV/°C.

The temperature drift of the voltage divider resistance is about 2ppm, and the temperature drift of the voltage divider resistance is required to be consistent, and the tracking temperature coefficient is less than 5 uV/°C.

The offset drift of AD8676 is about 0.6 μ V/°C. AD5781 has a very low temperature coefficient of about 0.05ppm/°C, which is much lower than the drift of the reference voltage source.

Ignoring the temperature drift of the op amp and DAC, it is mainly affected by the reference voltage source, and the drift is about 20 uV/°C.

Generally speaking, for a 20V voltage range, 18-bit system, the temperature drift is required to be controlled within 80uV, and the temperature cannot change more than 4 degrees.

3) Capacitive load analysis

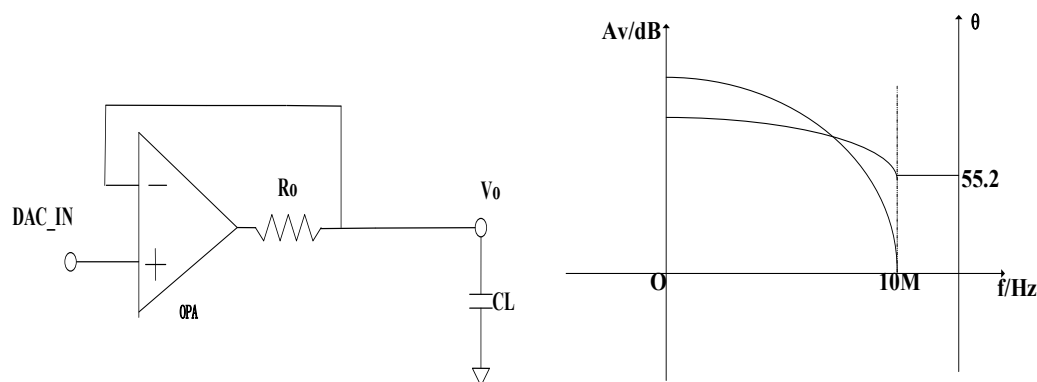


Fig.3. (a) DAC BUF design (b) AD8676 Bode Plots

The ideal operation state of the operational amplifier is that the output voltage and the input voltage are in phase, that is, when the input voltage at the negative input causes the output to increase, the operational amplifier can correspondingly reduce the increased voltage. However, the input and output phases of operational amplifiers are always different. When the phase difference between the output and the output is

180 ° The negative input is exactly the same as the positive input, but the output that should be reduced is enhanced (It becomes a state of positive and negative collapse.) If it falls into this state in a certain frequency band and remains the original amplitude, the output frequency and oscillation state will continue.

$$A_{Cl} = \frac{U_o}{U_i} = \frac{Z_o}{R_o} = -j * \frac{1}{2 * \pi * CL * f * R_o} \quad (6)$$

While $A_{cl} = 1$, $f_p = \frac{1}{2 * \pi * CL * R_o} > 10 \text{ MHz}$;

While $f_p > 10 \text{ MHz}$, $R_o > 40 \Omega$, $CL < 400 \text{ pF}$, there will be no shock.

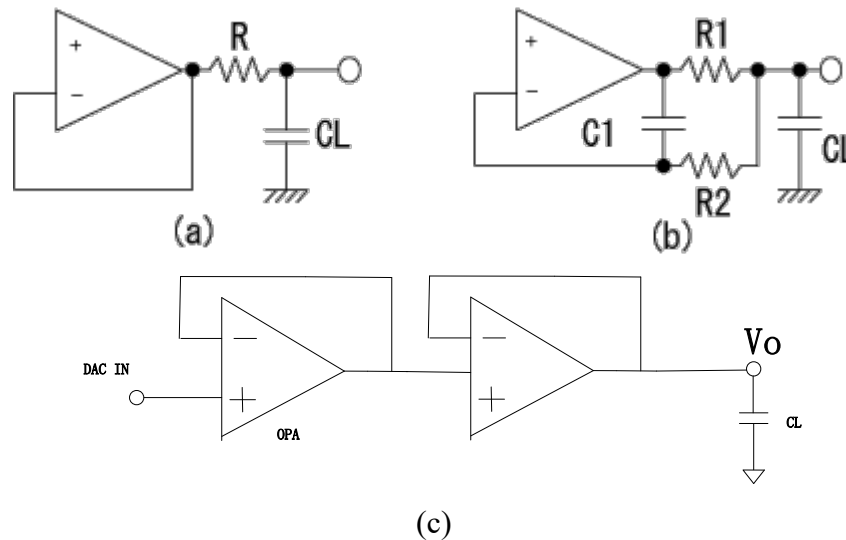


Fig.4 (a) Insert resistance R (b). Miller effect compensation (c) Stretch bandwidth

Fig.4(a) R is inserted in the figure to eliminate the phase lag of feedback loop due to CL

In high frequency region, R is shown as the load of operational amplifier replaces CL. Although R is added to the outside of the feedback loop, the series resistance R can act on the transfer function of the feedback network by the additional zero frequency FZ generated by the load capacitance, thus reducing the phase shift of the high frequency loop. In order to ensure the stability of the circuit, the value of R should make the additional zero frequency at least 10 times lower than the closed-loop bandwidth of the op amp circuit.

Fig.4(b) Miller effect compensation

The phase lag caused by CL is eliminated by pre-correction and C1 insertion.

Fig.4(c) Two stage OPA extended bandwidth

The phase delay caused by CL is compensated by the advanced correction, which is equivalent to adding a buffer at DAC output stage, and responding in time to the first stage operational amplifier response.

Results and discussion:

The multi-channel precision voltage source (MPVS-X) prototype was shown in Fig.5. The LCD screen and controller were distributed in the front panel layout. The Input-Power, power controller, multi-output, RS232 output interface and network interface were distributed in the rear panel layout. The size of prototype is 437mm*420mm*133mm (3U chassis size).

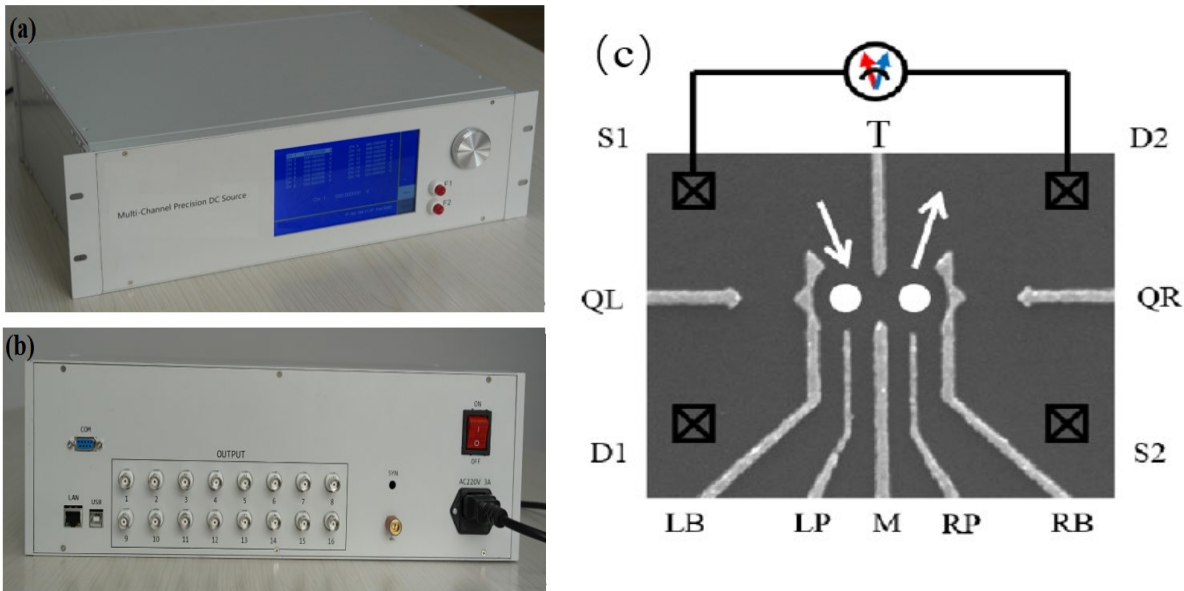


Fig. 5. (a), the front panel layout of prototype; (b) the rear panel layout of prototype; (c) bias source test in Qdots device application

1) Linearity

Set the output of the voltage source in the program, from the minimum value that can be set to the maximum value that can be set, in steps of 10 mV. Wait for 0.5s after setting the voltage value each time, and then use the 8.5-digit digital multi-meter (Agilent 3458A) to read the actual output voltage value. The whole process is repeated 5 times. Save the data of the original set voltage value—the actual voltage value, and perform curve fitting as shown in Fig 6.

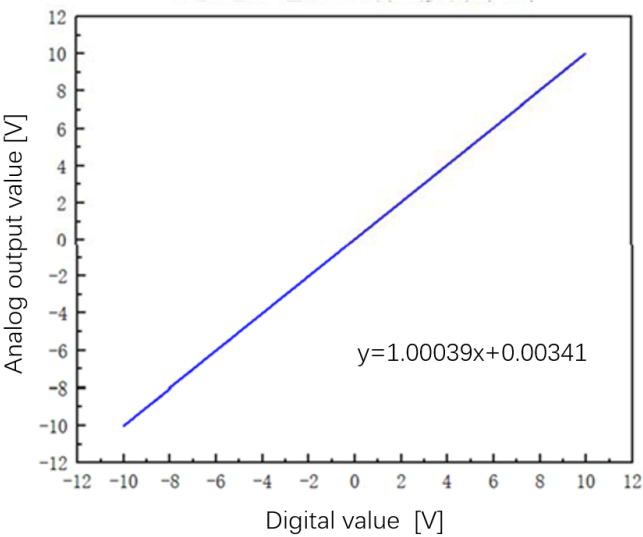


Fig 6 Linear fitting of output voltage

2) Short time fluctuations

Set different voltage output in the program, wait for 0.5s after setting the voltage value each time, and then read the actual output voltage value with an 8.5-digit digital multi-meter (Agilent 3458A), continuously measure 100 s, and count the peak-to-peak voltage jitter. The whole process is repeated 5 times.

Table 1. Output voltage fluctuations under different voltage

Vout/V	-10	-7.5	-5	-2.5	0	2.5	5	7.5	10
Fluctuations / μ V	45.8	36.8	26.6	13.3	1.4	11.3	32.7	28.1	39.2

The voltage output range of this system is -10V~10V. For 18-bit system, 1 LSB is 76 μ V, and the maximum voltage jitter does not exceed 50 μ V in the full voltage range.

3) Uniformity between two channels

As shown in Fig.7, the two channels have the same set voltage of - 5.5V and - 1V respectively, and read the actual output voltage value with an 8.5-digit digital multi-meter (Agilent 3458A), continuously measure for a long time.

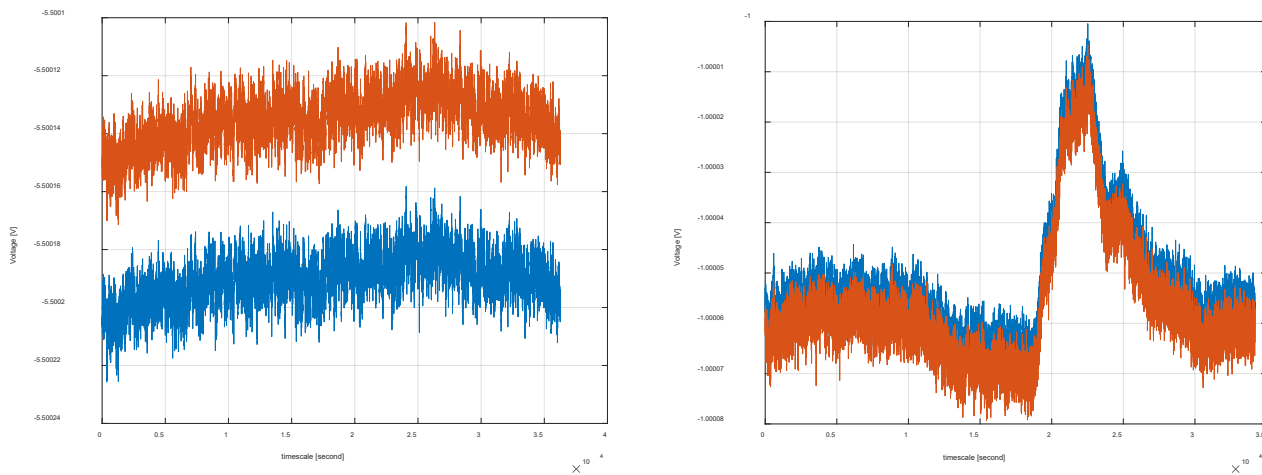


Fig.7 the uniformity between different channels

4) Step response

As shown in Fig.8, The step is set from -5V to +5V. According to the test results of the oscilloscope, the 10V step has a settling time of about 2.4~2.7 μ s.

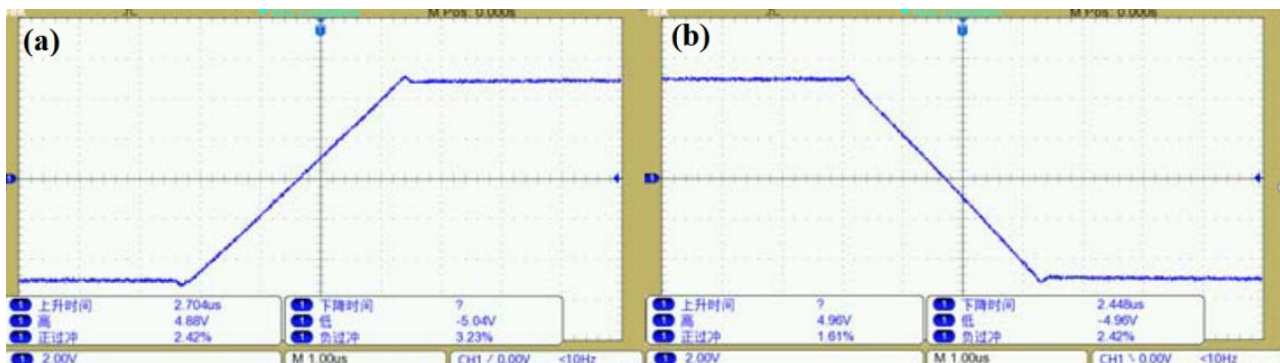


Fig 8 (a)-5V~+5V step response (b)+5V~-5V step response

5) Long-term stability

Turn on the output of 16 test channels at the same time and set their voltage output to 10 V at the same time, test the voltage value of random channels among them, read it every 10s, and the test duration is 24 hours. The output voltage change curve with time is as follows:

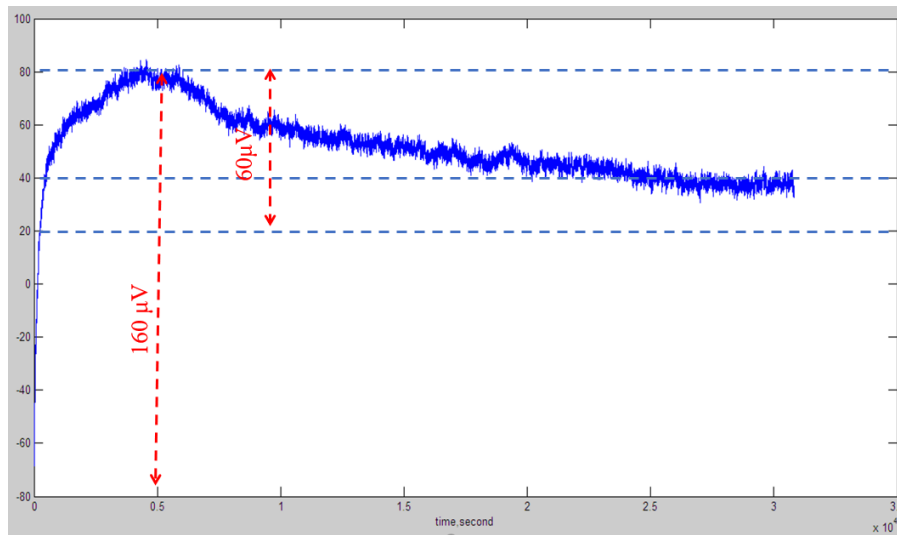


Fig. 9 the output voltage stability test

The output stability of the system was shown in Fig. 9. After starting up and running for about 2 hours, the internal temperature of the instrument gradually rises, and the output voltage will drift by $160\mu\text{V}$, and then the internal environment of the instrument gradually stabilizes. When multiple channels work at the same time, the system has excellent long-term stability of voltage output and maximum fluctuation. The range is less than $20\mu\text{V}$.

Conclusion:

Multi-channel bias voltage source technology is a typical technology of low noise circuit design, involving resolution, noise, accuracy, linearity, temperature, channel consistency, bias, long-term stability, low complexity and other aspects. The project research focuses on these problems closely, and achieves 4ppm conversion accuracy by designing high-resolution digital to analog conversion circuit; Through scientific exploration, a series of low noise circuit design problems such as power supply, grounding processing and signal isolation are solved; Through closed-loop measurement and digital correction, accurate voltage output is obtained; The problem of capacitive load and linearity is solved by two-stage op amp output; Through careful heat dissipation, the whole machine controls the temperature change on the one hand; On the other hand, the temperature drift of components is very low, which minimizes the temperature drift coefficient of the system and improves the working temperature range through temperature compensation; Through careful structure design of the whole machine, the complexity of the system is reduced, and the humanized man-machine interface is realized. The results show that it is one effective and feasible topology for the high precision voltage bias source in Qdots device application.

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