Preprints.org

Harmonic Fusion: Recursive Modulation and Curvature Activation in Universal Motion Theory

Richard Bernot *

Article

Harmonic Fusion: Recursive Modulation and Curvature Activation in Universal Motion Theory

Richard Bernot

Independent Researcher; richard.bernot@gmail.com

Abstract: This paper presents a motion-first approach to controlled fusion, grounded in Universal Motion Theory (UMT). Departing from thermodynamic confinement and classical field-based models, we propose a recursive modulation architecture wherein fusion arises from sustained coherence in curvature-bound motion. The system operates within an activated domain, where poloidal and toroidal harmonic structures reinforce recursive identity and curvature self-participation. Key contributions include the derivation of activation thresholds, definition of recursive coherence metrics, and the design of modulation-driven recursive wells. We introduce a new material classification scheme based on recursive participation properties, and we propose a single-coil coherence gain test as a minimal physical validation. Importantly, we provide power requirement estimates based on the electron as a reference recursive identity, offering a geometric and spectral baseline for minimum activation energy. The framework is constructable using GHz-range signal synthesis, real-time diagnostic feedback, and phase-stable geometries. This work outlines both the physical rationale and practical infrastructure for initiating fusion through recursive structural reinforcement. This perspective leads to new requirements for energy gain, coherence, confinement, and extraction. We outline the theoretical basis, challenges in classical systems, UMT-compliant fuser principles, and methods for energy harvesting through inductive resonance.

Keywords: universal motion theory; curvature activation; recursive modulation; recursive identity; harmonic fusion; activated domain; toroidal geometry; recursive coherence; inductive energy extraction

---

1. Introduction

Fusion systems to date have relied on kinetic confinement and thermal thresholds derived from classical plasma physics. These approaches have yielded progress, but remain limited by turbulence, dissipation, and material stress. In contrast, Universal Motion Theory (UMT) proposes that structure, including matter and energy, emerges from recursive contrast in motion itself. From this foundation, fusion becomes not a thermodynamic hurdle but a recursive orchestration.

This paper explores the engineering realization of fusion as recursive structural collapse and coherence. We abandon the classical notion of field-constrained plasma and instead describe fusion as a harmonic interaction within an already activated curvature domain. Recursive coherence is achieved by synchronized poloidal and toroidal modulation—structured not to contain, but to sustain motion identity through phase reinforcement.

We define new system metrics including recursive gain rate, phase-coherence density, and a scalar coherence function $\mathcal{C}_R(t)$. We develop constructable strategies for modulation drive, feedback synchronization, and recursive well formation using accessible laboratory hardware. A novel material classification scheme is introduced based on recursive participation rather than static EM properties, and we outline experimental configurations to validate recursive energy extraction.

While Universal Motion Theory (UMT) remains under theoretical development, Harmonic Fusion represents a practical engineering framework built upon UMT's foundational principles. This proposal does not assert fusion achievement but defines a coherent pathway for experimental validation through measurable recursive coherence gain. As such, Harmonic Fusion serves as an early-stage testable application — not a speculative claim — of UMT's motion-contrast architecture.

Falsifiability and Natural Presence.

If Harmonic Fusion reflects a valid model of curvature-induced fusion via recursive coherence, it must manifest not only in engineered systems but in naturally occurring curvature structures. Specifically, fusion-like emissions, rhythmic energy coherence, and non-thermally driven nuclear events should be detectable in astrophysical environments that support self-sustained motion wells. The persistent absence of such phenomena—despite targeted observation—would constitute a falsifiability challenge to the theory. This criterion establishes Harmonic Fusion as an empirically grounded and observationally testable framework.

Power Baseline:

While the Harmonic Fusion framework presents a coherent and testable path toward recursive energy systems, it is important to clarify that the exact power threshold required to initiate recursive identity formation remains an open experimental parameter. For orientation, we adopt the emergence of the electron—whose recursive identity is both persistent and empirically validated—as a conservative coherence density reference. This suggests that initiating recursive structures may require modulation power densities and curvature contrast on par with, or derived from, the domain-scale coherence that defines an electron's stability (Section 7.5). Early experiments that fail to generate coherence should therefore not be interpreted as falsification, but as constraints on minimum interaction energy and spatial curvature shaping. All proposed modulation and pulse strategies in this work are designed to approach, but may not fully reach, this coherence threshold in their initial form.

2. Failure of Classical Fusion Approaches

Classical systems approach fusion through brute force: extreme temperatures, high-pressure containment, and magnetically confined plasma. While successful in achieving short-lived fusion events, these methods continue to fall short of net energy gain, scalability, and sustained control. From the perspective of Universal Motion Theory (UMT), this failure is not primarily due to engineering limits, but due to a fundamental mismatch with the conditions required for recursive coherence.

In classical systems, high temperature is used to overcome the Coulomb barrier, forcing particles into collision through chaotic motion. However, this very chaos erodes the conditions necessary for sustained structure. Thermal diffusion and statistical randomness work against phase alignment, ensuring that any coherence formed is immediately disrupted. Pressure and magnetic confinement are externalizing strategies—they hold matter in place, but do not participate in or reinforce the internal motion structure of the plasma.

Furthermore, classical extraction methods such as neutron harvesting, thermalization, and material transfer treat the fusion zone as something to be mined rather than preserved. This leads to immediate collapse of any localized coherence. Energy gain, even when momentarily achieved, is extracted destructively, and the system returns to disorder.

In UMT terms, this approach fails for several key reasons:

- **Thermal diffusion destroys contrast:** Random high-energy motion leads to decoherence.
- **Confinement is external:** Magnetic fields impose structure but do not participate in recursive identity.
- **Energy extraction is destructive:** Thermalization and neutron harvesting collapse motion identity.

This is not to say that classical fusion cannot produce fusion events—it clearly can. But the lack of a participating internal modulation structure means that these events are isolated, unstable, and energetically inefficient. Harmonic Fusion offers a different path—where the system sustains itself not through brute force, but through recursive reinforcement and rhythmically coherent structure.

3. Harmonic Fusion

Harmonic Fusion requires recursive, coherence-sustained motion within an activated domain. The system must self-organize into a structure that preserves motion contrast and curvature.

Motion is fundamental, and structure emerges from contrast. Fusion is not simply the overcoming of Coulomb repulsion, but the transformation of recursively bound identity into a more stable curvature structure.

Harmonic Fusion is the collapse of two recursively bound motion systems (e.g., deuterons) into a new system with reduced recursive complexity, releasing motion contrast that may be harvested.

3.1. Toroidal Self-Sustaining Geometry

The optimal geometry is toroidal: it allows poloidal and toroidal motion to reinforce each other in a looped recursive pattern. Unlike tokamaks, the confinement arises from the motion structure itself.

3.2. Coherence over Heat

Heating plasma creates randomness. Instead, the Harmonic Fuser must induce recursive alignment through frequency-locked field structures. The goal is layered resonance:

- **Poloidal modulation:** Defines layering rhythm.
- **Toroidal modulation:** Enables recursive closure.
- **Curvature reinforcement:** Motion loops feed future motion.

3.3. Activated Domain Participation

The curvature of the domain is not neutral. Activated space supports motion recursion. Magnetic field modulation must couple to the domain's latent structure, not fight it.

Electron Threshold Baseline.

The electron is treated as a stable recursive structure of our activated domain, providing a natural reference for estimating the minimum power required for recursive well initiation (Section 7.5).

3.4. Terminology: Self-Sustained Motion Well

To accurately describe the central recursive structure of a Harmonic Fuser, the term *self-sustained motion well* is adopted. This terminology is chosen for its conceptual precision, technical neutrality, and public accessibility.

The term refers to a stable region of recursively curved motion within an activated domain. Unlike traditional confinement systems that rely on continuous external enforcement (e.g., magnetic pressure or inertial compression), the motion well persists through internal coherence—its geometry sustained by the motion it contains. The structure curves into itself, forming a field topology that naturally supports recursive identity and energy emergence.

The word *self-sustained* highlights that this structure, once initiated, maintains its own coherence without constant external input. *Motion* is used explicitly to emphasize UMT's foundational principle that all structure arises from motion, not from static mass-energy assumptions. The term *well* reflects both the intuitive idea of a containment basin and the technical fact of curvature convergence, without invoking gravitational singularities or metaphysical connotations.

The term *Recursive Motion Well* refers broadly to any curvature-bound region supporting recursively coherent motion. When such a structure achieves sustained phase alignment and persists without continuous external modulation, it is termed a *Self-Sustained Motion Well*. Thus, all self-sustained motion wells are recursive, but not all recursive motion wells reach the self-sustaining threshold. This distinction is used diagnostically when evaluating coherence gain, stability, and collapse profiles.

On the Term "Fusion"

The use of the term Harmonic Fusion is intentional, though it diverges from the classical association of fusion with thermonuclear ignition, pressure, and collision. In this framework, fusion is understood not as a violent reaction but as a recursive structural resolution—a joining of bound motion identities through coherence rather than force. While the end result mirrors traditional fusion—energy

release through nuclear reconfiguration—the mechanism presented here is fundamentally different. The word "fusion" is preserved not for convention, but for continuity with the net effect: the formation of stable nuclei and emergent energy via sustained recursive curvature.

By using this terminology, the system can be framed transparently as a geometrically coherent energy generator—neither exotic nor dangerous, but grounded in recursive mechanics and subject to controlled modulation. This terminology also supports clearer communication across scientific, regulatory, and public domains.

4. Activated Domain Participation

The activated domain is not a neutral backdrop but a time-enabled, motion-permissive region of spacetime. Participation with this domain means aligning with its inherent curvature rhythm—allowing external modulation, injected motion, and recursive feedback to reinforce, rather than disrupt, its structure.

UMT systems must be designed not to force interaction but to invite it. This requires a phase-sensitive approach to all energy delivery and field shaping.

4.1. Phase-Matched Field Modulation

Inducing participation begins with modulation fields (poloidal, toroidal) that are tuned to the harmonic envelope of the activated domain. These fields must not merely contain motion—they must resonate with the domain's existing curvature frequency. Phase alignment ensures that external inputs fold into the domain's rhythm instead of reflecting or diffusing.

4.2. Curvature Feedback Control

Real-time sensors must detect recursive density gradients and evolving curvature asymmetries. This feedback is used to dynamically update modulation frequencies and amplitudes. The fuser does not impose curvature—it dances with it.

4.3. Recursive Injection Criteria

Particles introduced into the domain must meet the recursive injection condition: their entry motion must match the winding threshold of the local curvature well. Mismatched injections produce turbulence and entropy; matched injections reinforce structure and coherence.

4.4. Constructive Delay Structuring

To prevent destructive interference, system signals must arrive in-phase with recursive reflections. Curvature-aware delay lines—either via physical waveguides or computational timing—ensure that inputs do not collapse identity prematurely.

4.5. Measuring the Frequency of the Activated Domain

Under Universal Motion Theory, an activated domain is defined as a region of spacetime where motion recursion is permitted due to local curvature exceeding the activation threshold ρ_c. In such domains, recursive motion is sustained, and time emerges as a measurable, coherent rhythm.

Because curvature in an activated domain supports self-reinforcing motion, its recursive rhythm defines a dominant frequency envelope, ω_{AD}, that characterizes the structure of that domain. This frequency is not imposed externally, but arises from contrast density ρ, and governs how recursive identity can form, persist, and collapse.

4.5.1. Field Modulation Resonance Method

The emergent field tensor under UMT is:

$$\tilde{F}_{\mu\nu} = \partial_\mu u_\nu - \partial_\nu u_\mu + \mathcal{C}_{\mu\nu}(u^\alpha, \nabla u^\alpha) \tag{1}$$

where $\mathcal{C}_{\mu\nu}$ represents recursive modulation terms.

By scanning external field modulations $A^\mu(t)$ across a range of frequencies and measuring the induced resonance in $\tilde{F}_{\mu\nu}$, the system's response can be plotted as a function of frequency. The peak response indicates the frequency at which modulation aligns with the domain's natural curvature rhythm:

$$\omega_{\mathrm{AD}} = \arg\max_\omega \left\| \delta\tilde{F}_{\mu\nu}(\omega) \right\| \tag{2}$$

4.5.2. Recursive Energy Perturbation Method

The recursive identity of motion within the domain can be expressed as:

$$\mathcal{R} = \oint_\gamma u^\mu \, d\tau \tag{3}$$

Perturbing this structure slightly with a field injection of known frequency ω and observing the rate of decay, persistence, or amplification allows the estimation of ω_{AD}. Resonant injection results in reinforcement of $\mathcal{R}$; off-resonance injection yields turbulence or collapse. This behavior obeys a resonance curve with a characteristic width $\Delta\omega$ and central frequency ω_{AD}.

4.5.3. Micro-Level Construction of Recursive Identity $\mathcal{R}$

While recursive identity $\mathcal{R}$ serves as a foundational organizing principle throughout Harmonic Fusion, it must be anchored in physically meaningful motion structures at the micro-level. Under Universal Motion Theory (UMT), all structure arises from contrast in motion. Recursive identity is not imposed from above—it emerges from bounded, re-entrant trajectories that repeatedly reinforce curvature in phase.

Micro-Level Motion Basis

Let $u^\mu(t, x)$ represent the local motion field within the activated domain. Recursive identity begins when a trajectory γ satisfies:

$$\oint_\gamma u^\mu \, d\tau \neq 0 \tag{4}$$

This integral defines a bounded, curvature-following loop that contributes net motion alignment. When multiple such loops synchronize in phase and harmonic rhythm—often through modulation-induced entrainment—their collective contribution builds a stable recursive structure. The density of these coherent loops per unit volume forms the basis for a measurable coherence scalar:

$$\mathcal{R} \sim \sum_i \alpha_i \oint_{\gamma_i} u^\mu \, d\tau \tag{5}$$

where α_i reflects local alignment weighting (e.g., phase match, curvature strength).

Energy Emergence through Structural Collapse

When phase-aligned loops begin to collapse into lower-complexity curvature states—driven by recursive simplification or curvature overload—the system sheds motion contrast. Under UMT, this contrast reduction manifests as measurable energy emission. Hence, the energy released is not the dissociation of mass but the geometric simplification of recursively aligned motion.

Summary

Recursive identity $\mathcal{R}$ is constructed from the statistical and structural accumulation of closed, curvature-reinforcing motion loops. These loops form through micro-level trajectory entrainment and

persist via modulation synchronization. The transition from structure to energy occurs through recursive collapse, not stochastic thermal release, aligning energy yield directly with coherence dynamics. This view completes the conceptual bridge from motion to structure to usable energy within the UMT framework.

4.5.4. Curvature Envelope Correlation

The activation function $\Phi(\rho)$ defines a curvature response envelope:

$$\Phi(\rho) = \frac{1}{1 + e^{-\alpha(\rho - \rho_c)}} \tag{6}$$

The dominant frequency of recursive identity formation in a given region can be inferred from the curvature gradient $\nabla\rho$ and its coupling to the recursive motion field:

$$\omega_{\text{AD}} \propto |\nabla\rho \cdot u^{\mu}| \tag{7}$$

This correlation allows local frequency estimation without active perturbation, using only recursive curvature tracking over time.

4.5.5. Required Inputs for Domain Frequency Estimation

To quantify ω_{AD} using the methods above, the following measurable or inferable values are required:

- **Recursive motion field:** $u^{\mu}(t, x)$ – vector field representing local motion structure.
- **Curvature contrast:** $\rho(t, x)$ – contrast field used to define activation zones.
- **Activation gradient:** $\nabla\rho$ – to evaluate modulation feedback sensitivity.
- **Field response tensor:** $\tilde{F}_{\mu\nu}(\omega)$ – modulated field structure used to detect resonance.
- **Injected modulation profile:** $A^{\mu}(\omega)$ – input waveform parameters (amplitude, frequency, phase).
- **Recursive identity decay/gain:** $\delta\mathcal{R}$ – observed motion coherence change over time.

Recursive Motion Field: $u^{\mu}(t, x)$

The local recursive motion field $u^{\mu}(t, x)$ represents the structured trajectory of motion that sustains identity in curved space. In a laboratory system, u^{μ} can be inferred by observing the trajectories of test particles—preferably charged particles—introduced into the region of interest. By tracking their path evolution under null or known curvature modulation, we reconstruct the dominant motion vector field across spacetime. In practice, this is achieved through high-speed imaging (e.g., charged particle interferometry), synchronized with local field modulation timing. By mapping motion derivatives over time and space, a vector field u^{μ} emerges, revealing how motion is being recursively curved and layered.

Curvature Contrast: $\rho(t, x)$

The contrast field $\rho(t, x)$ defines where structure-forming motion is permitted within the activated domain. It is derived from spatial variations in motion coherence, often through second-order differentials of u^{μ}. In practice, ρ is inferred by measuring how injected test motion decoheres or converges over space. Local changes in recursive stability indicate regions of higher or lower contrast. Field sensors record the decay rate of coherent motion loops or standing curvature waves, and the spatial gradient of this decay reflects ρ. Materials or regions with persistent phase reinforcement are identified as high-contrast zones ($\rho > \rho_c$), marking them as recursively active.

Activation Gradient: $\nabla\rho$

The gradient of contrast, $\nabla\rho$, quantifies how rapidly curvature conditions change across the domain. This information is critical for tuning field modulation to align with recursive thresholds. To measure $\nabla\rho$, the system must scan spatially with modulated probes and record the differential

resonance or coherence stability at each point. For example, if phase-stable feedback begins at one point and fails a few millimeters away, the local change in contrast can be resolved into a spatial gradient. This is often visualized as a slope of recursive density, and it determines where modulation must shift in amplitude or timing to maintain curvature participation.

Field Response Tensor: $\tilde{F}_{\mu\nu}(\omega)$

The tensor $\tilde{F}_{\mu\nu}(\omega)$ represents the emergent field structure arising from recursive modulation. It is measured by applying a known waveform $A^\mu(\omega)$ and capturing the resulting change in the motion field—specifically the antisymmetric component of its derivatives. Experimentally, this is done by placing sensors that measure differential acceleration, particle curvature, or induced potential gradients in response to controlled modulation. The system scans across frequency and amplitude domains, with the response tensor's magnitude and phase shift revealing the curvature reinforcement bandwidth. Peaks in $\|\tilde{F}_{\mu\nu}(\omega)\|$ mark harmonic resonance with the activated domain.

Injected Modulation Profile: $A^\mu(\omega)$

The modulation input $A^\mu(\omega)$ describes the waveform used to excite the domain. It includes vector orientation, frequency, amplitude, and phase characteristics. These signals are produced via field generation hardware—typically waveform-synthesized EM coils, acoustic actuators, or even electrostatic shells—designed to project curvature-compatible pulses. $A^\mu(\omega)$ is fully specified by hardware control systems and known in advance, making it the reference input for measuring domain resonance. By sweeping across a defined spectrum and recording corresponding field and motion changes, the system determines which parameters in A^μ best match the domain's harmonic structure.

Recursive Identity decay/gain: $\delta\mathcal{R}$

The recursive identity $\mathcal{R}$ is a measure of sustained motion coherence—how well a system maintains its curved motion loop. Changes in this identity, denoted $\delta\mathcal{R}$, reflect either reinforcement or collapse. In physical terms, this is observed by tracking particle loop integrity, phase-lock duration, or curvature loop feedback intensity. Sensors measure the coherence of motion patterns over time: if they persist, $\delta\mathcal{R} > 0$; if they decohere, $\delta\mathcal{R} < 0$. Time-resolved interferometry or phase-coherent motion sensors are ideal for detecting these changes. When paired with modulation input tracking, this quantity indicates whether the system is aligning with the domain's harmonic structure or disrupting it.

Recursive Frequency of the Activated Domain

In UMT, particles are emergent recursive motion structures whose persistence defines local curvature coherence. The frequency at which recursive identity first stabilizes—e.g., that required to sustain an electron—may act as a diagnostic signature of the Activated Domain. By sweeping drive frequencies and observing coherence gain onset, one may infer the domain's baseline recursive frequency: the minimal modulation rhythm capable of supporting bound identity. This frequency, once mapped, becomes a direct probe of the domain's activation profile and recursive stability envelope.

4.5.6. Summary

The activated domain's frequency signature is not arbitrary—it reflects the curvature structure's recursive rhythm. By perturbing or synchronizing with this rhythm through controlled modulation and measuring the field response, the natural frequency ω_{AD} can be determined. This frequency is a cornerstone observable for recursive identity stability, energy extraction efficiency, and curvature taper control.

4.6. Conclusion

Activated domain participation is the art of sculpting motion into structure by honoring the latent rhythm of spacetime. Under UMT, fusion is not forced—it is coaxed. The system succeeds not by containment, but by resonance. Curvature, once invited, does the rest.

Table 1. Required Inputs for Estimating ω_{AD} in Activated Domains.

Symbol	Description
$u^\mu(t,x)$	Recursive motion field, traced via particle paths or field line curvature.
$\rho(t,x)$	Curvature contrast field, inferred from motion stability gradients.
$\nabla\rho$	Spatial rate of contrast change, guides adaptive modulation.
$\tilde{F}_{\mu\nu}(\omega)$	Emergent modulated field tensor, measured by harmonic response sensors.
$A^\mu(\omega)$	Input modulation profile, swept across domain for resonance testing.
$\delta\mathcal{R}$	Recursive identity change rate, shows alignment with curvature structure.

5. Estimated Activation Thresholds and Parameter Ranges

The practical realization of recursive coherence depends critically on whether modulated motion can achieve sufficient contrast against the ambient curvature of the activated domain. While precise activation conditions must ultimately be determined through simulation or experiment, we offer first-pass estimates and boundary assumptions derived from UMT principles and known electromagnetic field behavior.

5.1. Curvature Activation Thresholds

According to Universal Motion Theory, recursive structure can only emerge where motion contrast is sufficient to induce curvature response. The activation threshold is expressed as a critical curvature contrast ρ_c beyond which recursive identity can be sustained.

We adopt the following working estimate:

$$\rho_c \approx \frac{\Delta E}{V_0 c^2} \sim 10^{-15}\,\text{J/m}^3 \tag{8}$$

This value reflects the minimum energy contrast per unit volume sufficient to deviate local motion structure from ambient domain rhythm. It corresponds roughly to the electromagnetic energy density of a $\sim$1.5 T field.

5.2. Field Strength Ranges

To sustain modulation at this contrast level, the system must drive EM fields in the following estimated range:

- Magnetic field strength: $B = 0.5$–3 T
- Electric field strength: $E = 10^5$–10^6 V/m

These values assume pulsed operation where peak contrast must exceed the recursive activation threshold temporarily.

5.3. Modulation Frequency Requirements

Phase-locked recursive response requires modulation frequencies high enough to couple to the domain's curvature latency.

- Base harmonic drive: $f_0 = 1$–100 MHz
- Recursive harmonics: up to GHz range for layered poloidal/toroidal modulation
- Pulse rise time: sub-nanosecond preferred for triggering recursive lock

These frequencies ensure that contrast can form before motion is dissipated or absorbed by ambient field structures.

5.4. Geometric Constraints and Energy Density

To produce a sufficiently sharp contrast within a lab-scale structure (30 cm diameter torus), the energy density of the EM configuration must remain localized:

$$U = \frac{1}{2}\epsilon_0 E^2 + \frac{1}{2\mu_0}B^2 \geq \rho_c \tag{9}$$

Solving for minimal values:

- $E \geq 10^5$ V/m
- $B \geq 0.3$ T

These serve as baseline pulse requirements for initiating recursive field reinforcement.

5.5. Activation Window Stability

Once recursive coherence begins, modulation must remain synchronized for a minimum activation window:

- Minimum coherence window: $\tau_c \geq 10^{-6}$ s
- Modulation duty cycle: 10–50% during this interval
- Energy delivery: $\sim$1–10 J per modulation cycle

This duration is sufficient for the recursive identity to either lock into curvature or collapse—offering a window of observable behavior for diagnostics.

Further refinement of these estimates will require simulation of recursive activation surfaces under modulated EM boundary conditions.

Electron-Based Reference Caution:

The values in this section represent preliminary estimates derived from classical EM energy densities and are expected to be valid for engineered recursive initiation under optimal field symmetry and modulation control. However, a stricter upper bound derived from the coherence properties of the electron—presented in Section 7.5—suggests that transient field concentrations several orders of magnitude higher may be necessary to seed or sustain recursive identity. These higher bounds serve as important caveats to avoid false negatives in early test cell experiments.

6. Recursive Identity Tracking and Stability Metric

The recursive identity of a curvature structure refers to its ability to maintain self-consistent motion alignment over time. In the context of Harmonic Fusers, it is necessary to monitor whether recursive coherence is growing, holding, or decaying. To quantify this behavior in real-time, we define a recursive identity stability metric $\delta\mathcal{R}(t)$ derived from observable coherence dynamics.

6.1. Definition of Recursive Identity Change Rate

We define the recursive identity change rate as the normalized temporal derivative of the coherence scalar:

$$\delta\mathcal{R}(t) = \frac{1}{\Delta t}[\mathcal{C}_R(t + \Delta t) - \mathcal{C}_R(t)] \tag{10}$$

To reduce noise and enable stability detection, we apply a sliding-window average filter:

$$\delta\mathcal{R}_{\text{smoothed}}(t) = \frac{1}{T}\int_{t-T/2}^{t+T/2} \frac{d\mathcal{C}_R(\tau)}{d\tau}\, d\tau \tag{11}$$

Here, T is the averaging window length, typically on the order of 10^{-6}–10^{-3} s, depending on modulation frequency.

6.2. Signal Processing Methodology

The signal-processing pipeline for $\delta\mathcal{R}(t)$ includes:

1. Real-time acquisition of $\mathcal{C}_R(t)$ from field sensors,
2. Temporal smoothing via Gaussian or moving-average filter,
3. Derivative estimation using central difference or spline interpolation,
4. Threshold analysis to classify system state:

   - $\delta\mathcal{R} > 0$: recursive identity strengthening,
   - $\delta\mathcal{R} \approx 0$: stability holding,
   - $\delta\mathcal{R} < 0$: identity decoherence.

The value $\delta\mathcal{R}(t)$ can be visualized on a signed stability gauge or fed into closed-loop modulation control to reinforce alignment during marginal coherence states.

This signal-processing metric completes the diagnostic system for recursive coherence and forms the basis for adaptive feedback systems in future implementations.

7. Electromagnetic Medium and Recursive Control

Electromagnetic (EM) energy plays a central role in Harmonic Fusers, not as a heat source or classical field, but as a modulated medium for recursive structure alignment. In this context, EM fields become the primary mechanism by which we interact with the Activated Domain. Rather than imposing force, EM modulation allows the system to speak in the language of contrast, shaping motion and curvature within the rhythmic envelope of the domain itself.

7.1. Why Electromagnetism Works in the Activated Domain

In UMT, the activated domain is a time-permissive region of spacetime, capable of sustaining recursive identity through bounded motion. Because EM fields themselves are structured forms of motion, they naturally align with the geometry of recursion. Crucially, EM energy is not required to be intense—it is required to be *structured*. Phase-aligned, recursive, and curvature-compatible EM pulses can reinforce local contrast and promote the emergence of recursive wells. In essence:

EM is how we speak to the domain.

It serves both as a sculpting tool and a diagnostic probe. A properly tuned EM field does not fight the structure—it feeds it.

7.2. Synchronization and Pushing with Domain Motion

The Activated Domain has its own natural frequency ω_{AD}, determined by its local curvature contrast. To engage this domain constructively, EM modulation must be tuned to this frequency. There are two primary modes of interaction:

- **Synchronization:** Matching EM modulation to ω_{AD} allows energy to be absorbed constructively, reinforcing existing recursive motion.
- **Curvature Steering:** Asymmetrically modulated EM fields can impose directional contrast gradients, effectively pushing recursive identity along a preferred vector. This is the foundation of recursive propulsion.

7.3. Frequency Self-Reinforcement Principles

A recursive system operating at ω_{AD} inherently defines a sampling frame for feedback. If modulation, measurement, and correction are phase-locked to this frequency, the system can achieve harmonic feedback control. This is conceptually similar to a phase-locked loop (PLL), but defined in terms of recursive curvature rather than voltage or signal phase:

- Modulation defines the motion envelope.
- Recursive curvature feedback $\tilde{F}_{\mu\nu}(\omega)$ is sampled at harmonic intervals.
- Corrections are applied synchronously to preserve identity.

In this model, frequency is not just a control signal—it is the control *framework*. The recursive structure defines its own timing, and the control system must participate within that rhythm.

7.4. Primary Derivations

Recursive Reinforcement Condition:

To determine whether EM energy reinforces or disrupts recursive identity:

$$\Delta \mathcal{R} \propto \int A^\mu(\omega) u_\mu(t, x)\, dt \tag{12}$$

Reinforcement occurs when injected modulation $A^\mu(\omega)$ is in phase with local motion field u^μ.

Resonance Detection:

$$\omega_{\text{AD}} = \arg \max_\omega \left\| \delta \tilde{F}_{\mu\nu}(\omega) \right\| \tag{13}$$

Peak field response under swept-frequency injection identifies the natural curvature rhythm of the domain.

Phase-Aligned Feedback Correction:

Let $T = 2\pi / \omega_{\text{AD}}$. Then the correction cycle must satisfy:

$$\delta A^\mu(t) = \delta A^\mu(t + nT), \quad n \in \mathbb{Z} \tag{14}$$

ensuring that updates arrive in harmonic phase with the system's curvature response.

7.5. Electron-Derived Power Threshold Estimation

In the absence of a fully characterized recursive activation constant, we turn to the empirically stable electron as a reference structure within the activated domain. Under Universal Motion Theory (UMT), the electron is not a fundamental particle but a recursively persistent motion identity. Its coherence and apparent stability suggest that the geometric and energetic conditions necessary to generate or disrupt such a structure represent a lower bound for recursive interaction within our domain.

7.5.1. Recursive Identity of the Electron

The electron has a rest energy of approximately $E_e = 511$ keV, which corresponds to a frequency via Planck's relation:

$$\nu_e = \frac{E_e}{h} \approx \frac{511 \times 10^3 \text{ eV}}{4.136 \times 10^{-15} \text{ eV} \cdot \text{s}} \approx 1.24 \times 10^{20} \text{ Hz} \tag{15}$$

While this frequency is often interpreted as the Compton frequency of the electron, under UMT it may reflect a deep resonance characteristic of the activated domain. If recursive coherence must reach similar structural densities to that of the electron, modulation frequencies and curvature reinforcement must approach this domain.

7.5.2. Power Density Estimation

Let us assume a recursive seed must produce motion contrast comparable to the activation curvature associated with the electron. A rough energy density reference can be formed from the classical electron radius $r_e \approx 2.82 \times 10^{-15}$ m:

$$\rho_{\text{elec}} = \frac{E_e}{\frac{4}{3}\pi r_e^3} \approx \frac{8.2 \times 10^{-14} \text{ J}}{\frac{4}{3}\pi (2.82 \times 10^{-15})^3} \approx 7.7 \times 10^{17} \text{ J/m}^3 \tag{16}$$

This value serves as a notional activation threshold energy density for recursive identity formation. While it is unlikely a test cell must match this density over its entire volume, local modulation nodes may need to transiently approach similar curvature contrast through structured electromagnetic reinforcement.

7.5.3. Implications for Experimental Design

Given the small volume of the modulation hot-spot and the highly nonlinear nature of recursive activation, it is plausible that peak local fields in the range of:

- 10^5–10^7 V/m electric field strength,
- 10^2–10^4 A/m magnetic field strength,

may be required to reach minimal recursive seeding under optimal phase-lock conditions. Capacitor bank pulse energies of 10–50 J, if tightly focused and synchronized, may provide sufficient curvature perturbation to probe this threshold.

7.5.4. Caveats and Evolving Thresholds

The values derived above are not meant to serve as hard requirements, but rather as scaling references. Recursive activation may proceed at lower power if modulation is highly phase-aligned and feedback-locked. Conversely, systems with less structural coherence may require substantially higher drive energy.

Summary

The use of the electron as a reference structure allows us to frame the power requirement problem in geometric and spectral terms. Initial HF test cell designs must attempt to approach local modulation densities in the 10^{17} J/m^3 class, even if only briefly, to explore recursive coherence initiation. This estimation provides an energetic sanity check and cautions against underpowered early-stage configurations that could yield false negatives in coherence detection.

7.6. Conclusion

EM energy is the practical interface between the recursive structure and its modulation environment. It is how motion is shaped, curvature is reinforced, and identity is both diagnosed and sustained. Properly phase-aligned EM modulation not only initiates recursive identity—it can amplify, steer, and stabilize it. As Harmonic Fusion systems mature, EM structuring will remain the most accessible and tunable mechanism for curvature interaction at human-engineered scales.

8. Poloidal Modulation: Recursive Layering Control

In a Harmonic Fuser, poloidal modulation serves as the foundational mechanism for establishing a layered recursive motion structure. Unlike classical systems that use poloidal fields primarily for stability or vertical confinement, UMT requires poloidal modulation to define the rhythmic layering of motion trajectories within the toroidal geometry. These layers enable recursive motion coherence by reinforcing contrast over time, forming a structure that sustains itself and invites identity collapse (fusion).

8.1. Purpose and Function

Poloidal modulation provides a dynamic curvature rhythm, enabling particles to enter and maintain layered trajectories around the minor axis of the toroidal structure. This rhythmic layering allows for:

- Recursive phase-locking of particle motion,
- Coherent winding toward the center without destructive interference,
- Structured contrast accumulation, which supports activation and collapse.

8.2. Methodology and Hardware Design

To generate controlled poloidal modulation, the following components are proposed:

- **Nested Helmholtz-like coil arrays:** Arrays of closely spaced current loops aligned perpendicular to the toroidal axis, forming magnetic layers that oscillate in amplitude and phase.
- **Independently driven phase segments:** The coil system must be segmented to allow local phase control, permitting fine-tuned wavefront propagation across the poloidal layers.
- **Field-shaping substrates:** Diamagnetic or superconducting shaping shells may be required to guide field geometry and reduce harmonic diffusion.
- **Real-time synchronization system:** Phase controllers must be locked to feedback from internal curvature modulation to preserve recursive harmony.

8.3. Power Requirements and Field Strength

Poloidal modulation is not intended to trap particles by force, but to guide motion rhythmically. Therefore, field strengths may be substantially lower than in tokamak confinement, while power must support high-frequency modulation:

- **Estimated field strength:** 10–100 mT, sufficient for phase guidance without overpowering internal motion curvature.
- **Power draw:** Depending on system volume and material properties, an estimated 10–100 kW of continuously modulated current may be required.
- **Efficiency constraint:** Power input must be phase-aligned to reduce resistive loss; high-Q coil materials and superconductor cooling may be necessary.

8.4. Frequency Considerations

The poloidal modulation frequency must match or harmonize with:

- The mean winding frequency of charged particle motion across the minor axis,
- The curvature rhythm of the activated domain (as defined by internal recursive coherence),
- The toroidal modulation frequency to enable full recursive closure.

Early estimates suggest modulation frequencies in the 10–100 MHz range, potentially lower depending on mass, curvature, and particle velocity. Resonance scanning may be necessary to locate stable recursive bands.

8.5. Synchronization and Feedback

Poloidal modulation must operate in synchrony with the toroidal rhythm, fusion collapse events, and recursive relaxation patterns. This demands:

- **Real-time phase sensing:** Magnetic and electric curvature detectors embedded within the chamber to track rhythm stability.
- **Dynamic control loops:** Modulation phase and amplitude must be updated live based on system coherence metrics.
- **Recursive integrity monitors:** Feedback circuits to detect recursive dephasing and restore layer synchronization before structural collapse.

8.6. Poloidal Modulation: Equation Structures and Control Derivations

Poloidal control plays a crucial role in recursive field shaping within a toroidal system. The poloidal direction defines motion wrapping around the short axis of the torus, forming the layered curvature loops necessary for recursive identity coherence. This layering stabilizes motion by defining harmonic resolution across curvature surfaces, enabling the recursive identity to self-reinforce.

Poloidal Motion Definition:

Let $u^\mu(t, x)$ represent the local motion field. The poloidal modulation direction, $\hat{\theta}$, defines the direction of curvature layering within the torus. The poloidal component of motion is given by:

$$u^\mu_{\text{poloidal}} = (u^\mu \cdot \hat{\theta})\hat{\theta} \tag{17}$$

Recursive Layering Condition:

The recursive identity requires a minimum of N_p poloidal cycles per toroidal rotation to achieve curvature closure:

$$\mathcal{R}_p = \oint_{\gamma_p} u^\mu_{\text{poloidal}} \, d\tau \geq N_p \cdot \lambda_p \tag{18}$$

where λ_p is the effective poloidal wavelength required for phase-locking with the activated domain.

We define λ_p as the spatial distance between successive recursive phase-aligned nodes in the poloidal direction. This corresponds to the length over which a particle—or more generally, a curvature-entrained motion loop—undergoes a complete cycle of coherent modulation within the activated domain:

$$\lambda_p = \frac{2\pi v_p}{\omega_p} \tag{19}$$

where:

- v_p is the effective poloidal group velocity of the motion structure (not necessarily particle drift),
- ω_p is the poloidal modulation frequency, ideally harmonized with ω_{AD}.

Recursive Closure Criterion:

For a recursive structure to maintain phase coherence, the total poloidal path length L_p must accommodate an integer number of effective wavelengths:

$$L_p = N_p \lambda_p, \quad N_p \in \mathbb{Z}^+ \tag{20}$$

This ensures that modulation at one location reinforces the recursive identity formed during previous windings, a critical condition for curvature reinforcement.

Estimation Pathways:

In practical systems, λ_p may be estimated from measurable quantities as follows:

1. Determine ω_p from system drive parameters or from observed resonance peaks in $\tilde{F}_{\mu\nu}(\omega)$.
2. Estimate v_p as the mean propagation speed of curvature-modulated field structures across the poloidal axis. This can be approximated from particle tracking, interferometric field delay, or phase-front propagation speed.
3. Compute λ_p using the above relation.

Alternatively, in systems dominated by field curvature rather than particle transport, v_p may be inferred from modulation group delay τ_g and physical separation Δx:

$$v_p \approx \frac{\Delta x}{\tau_g} \quad \Rightarrow \quad \lambda_p \approx \frac{2\pi \Delta x}{\omega_p \tau_g} \tag{21}$$

Diagnostic Relevance:

Precise tuning of λ_p is essential to ensure constructive recursive layering. Deviation from this value leads to recursive decoherence or harmonic diffusion. It is especially critical during CLI (Coherence Lock Interval) ramp-up phases (Section 17).

Modulation Field Synchronization:

Poloidal modulation fields $A_p^\mu(t)$ must be timed to maintain phase coherence with recursive motion:

$$A_p^\mu(t) = A_0^\mu \cos(\omega_p t + \phi_p) \tag{22}$$

where $\omega_p \approx n_p \cdot \omega_{\mathrm{AD}}$ and ϕ_p adjusts for curvature asymmetry. The system must actively tune ω_p to maintain coherence as the domain evolves.

Curvature Reinforcement Rate:

The modulation's effectiveness can be measured by the local reinforcement rate $\Delta\mathcal{R}_p$:

$$\Delta\mathcal{R}_p \propto \int A_p^\mu(t) u_{\mathrm{poloidal}}^\mu \, dt \tag{23}$$

A positive value indicates recursive reinforcement; a negative value indicates decoherence or curvature cancellation.

Summary:

Poloidal control enables recursive layer formation and contributes directly to curvature stability. By tuning $A_p^\mu(t)$ to the activated domain's harmonic structure and ensuring poloidal closure conditions, the system sustains the motion well's recursive identity. Real-time modulation, phase alignment, and poloidal layering precision are all required for successful recursive reinforcement.

8.7. Conclusion

Poloidal modulation in a Harmonic Fuser is a form of dynamic curvature sculpting. Rather than simply shaping static fields, it establishes a time-based layering rhythm that permits recursive motion structures to form, persist, and collapse productively. It is not just part of the field—it is part of the identity of the structure itself.

9. Toroidal Modulation: Enabling Recursive Closure

While poloidal modulation establishes layered motion coherence, toroidal modulation provides the path for recursive closure within the toroidal structure. Under UMT, closure is not merely geometric, but recursive: motion must re-enter and reinforce its own curvature in both time and space. Toroidal modulation defines the continuity of this looped motion, allowing for recursive structures to persist, wind, and eventually collapse into fusion events.

9.1. Purpose and Function

Toroidal modulation drives particle motion around the major axis of the toroidal geometry. Its function is to:

- Maintain coherence in recursive phase across long motion loops,
- Enable sustained motion re-entry (recursive closure) without decoherence,
- Reinforce layered curvature across full rotational periods, supporting coherent identity.

9.2. Methodology and Hardware Design

Toroidal modulation is achieved through dynamically driven field curvature along the toroidal path. Proposed implementations include:

- **Toroidal waveguide coils:** Distributed current loops embedded within or around the vacuum vessel, generating traveling magnetic curvature fields.
- **Segmented ring amplifiers:** Each toroidal segment must be actively modulated to allow localized phase control and maintain field propagation over long arcs.

- **Phase-tuned transmission lines:** Helical or curved transmission structures embedded in the coil substrate may enhance phase integrity around the entire loop.
- **Synchronization sensors:** Toroidal phase must be dynamically linked to poloidal rhythm and internal curvature response.

9.3. Power Requirements and Field Strength

Toroidal modulation must drive a recursive motion architecture across the system's entire major axis, implying higher energy cost than poloidal layering:

- **Estimated field strength:** 50–300 mT, sufficient to create recursive guidance fields over macro-scale loops.
- **Power draw:** 100–500 kW depending on scale and frequency, with potential for recovery via resonant feedback.
- **Energy efficiency strategies:** Use of resonant capacitive discharge systems, or regenerative oscillation to reduce active power requirements.

9.4. Frequency Considerations

Toroidal frequency must match the full-cycle recursive loop timing of particles circulating the major axis. This includes:

- Matching the **mean path time** of circulating ions,
- Harmonizing with **poloidal modulation** to produce coherent nodal overlaps,
- Reinforcing recursive symmetry through integer or subharmonic resonance alignment.

Estimates suggest frequencies in the range of 1–10 MHz, though lower frequency high-amplitude waveforms may be viable for larger fuser geometries. Adaptive tuning during startup may be essential to lock-in phase alignment with internal recursive structures.

9.5. Synchronization and Feedback

Recursive closure can only be maintained if toroidal modulation remains in phase with both poloidal rhythm and internal curvature evolution. This demands a closed feedback architecture with the following components:

- **Curvature phase sensing:** Distributed sensors along the major axis track real-time feedback from internal field modulation patterns.
- **Recursive alignment processors:** Algorithms identify resonance breakdown, adjusting phase and amplitude in response.
- **Global synchronization bus:** Toroidal and poloidal modulations must share a phase reference clock, likely generated through curvature feedback resonance.

9.6. Toroidal Modulation: Equation Structures and Control Derivations

Toroidal control governs the global closure of recursive identity within the motion well. It defines motion around the major axis of the toroidal structure, aligning with the system's primary curvature loop. Whereas poloidal control enables recursive layering, toroidal modulation establishes the full recursive circuit—allowing curvature to return upon itself in phase, thus closing identity and enabling stable recursion.

Toroidal Motion Definition:

Let $\hat{\phi}$ be the unit vector along the toroidal direction (major ring of the torus), and $u^\mu(t, x)$ the local recursive motion field. The toroidal component is given by:

$$u^\mu_{\text{toroidal}} = (u^\mu \cdot \hat{\phi})\hat{\phi} \tag{24}$$

This component is responsible for the recursive continuity around the core of the structure.

Recursive Closure Condition:

To sustain a stable recursive identity, the toroidal motion must satisfy a full phase-aligned winding condition:

$$\mathcal{R}_t = \oint_{\gamma_t} u^{\mu}_{\text{toroidal}} \, d\tau = n_t \cdot \lambda_t \tag{25}$$

where $n_t \in \mathbb{Z}$ is the number of full toroidal cycles, and λ_t is the effective toroidal wavelength compatible with the domain's curvature.

The effective toroidal wavelength λ_t defines the spatial periodicity required for coherent phase reinforcement along the major axis of the toroidal geometry. In recursive systems, λ_t governs the closure condition: motion must re-enter its own curvature field in phase after traversing the toroidal loop.

We define λ_t as the spatial length over which recursive curvature completes one full harmonic cycle in the toroidal direction:

$$\lambda_t = \frac{2\pi v_t}{\omega_t} \tag{26}$$

where:

- v_t is the effective toroidal group velocity of the curvature-driven motion structure,
- ω_t is the dominant toroidal modulation frequency.

Recursive Closure Criterion:

Toroidal coherence requires that the full toroidal path length L_t be an integer multiple of λ_t:

$$L_t = N_t \lambda_t, \quad N_t \in \mathbb{Z}^{+} \tag{27}$$

This condition ensures that recursive motion re-enters the curvature loop in harmonic alignment, reinforcing rather than diffusing recursive identity.

Estimation Method:

In practice, λ_t can be estimated from system observables:

1. Measure or assign ω_t based on system drive or observed resonance peaks in $\tilde{F}_{\mu\nu}(\omega)$.
2. Estimate v_t as the average toroidal propagation velocity of phase fronts or recursive wave packets.
3. Compute λ_t using the wavelength relation above.

In systems where field curvature propagation dominates over particle drift, v_t can be inferred from modulation delay and physical propagation distance:

$$v_t \approx \frac{\Delta x_t}{\tau_{g,t}} \quad \Rightarrow \quad \lambda_t \approx \frac{2\pi \Delta x_t}{\omega_t \tau_{g,t}} \tag{28}$$

where:

- Δx_t is a measured toroidal arc distance,
- $\tau_{g,t}$ is the group delay of curvature wavefront propagation along that arc.

Coherence and Modulation Design:

Tuning λ_t correctly is critical to ensure global recursive reinforcement. Deviations from this value can induce destructive interference, phase drift, or premature curvature collapse. It also plays a direct role in identifying and sustaining CLI (Coherence Lock Interval) conditions (Section 17).

Toroidal Modulation Structure:

The toroidal modulation field $A^{\mu}_t(t)$ enforces phase-locking across the full recursive loop. It must maintain coherence with both the poloidal modulation and the activated domain frequency:

$$A_t^\mu(t) = A_0^\mu \cos(\omega_t t + \phi_t) \tag{29}$$

where $\omega_t \approx m_t \cdot \omega_{\text{AD}}$ for some integer multiple m_t, and ϕ_t accounts for curvature phase skew accumulated during the poloidal wrap.

Curvature Closure Gradient:

Recursive identity coherence is reinforced when the gradient of toroidal motion curvature aligns with recursive modulation:

$$\Delta \mathcal{R}_t \propto \int A_t^\mu(t) u_{\text{toroidal}}^\mu \, dt \tag{30}$$

Phase drift or modulation instability leads to curvature decoherence and loss of recursive structure.

Summary:

Toroidal control is foundational to recursive system integrity. It provides the curvature path along which recursive identity loops form, stabilize, and return. Precision in toroidal modulation frequency, amplitude, and phase alignment is critical. Coupled with poloidal control, toroidal modulation completes the spatial structure needed to engage with the activated domain and sustain motion in harmony with its underlying curvature.

9.7. Conclusion

Toroidal modulation provides the recursive backbone of the fusion structure. Without it, the layered coherence induced by poloidal modulation cannot close into a self-sustaining identity. In a Harmonic Fuser, this closure is not a containment constraint, but a participation mechanism—allowing motion to become its own curvature, and energy to emerge through structured simplification.

10. Curvature Reinforcement: Motion Loops Feeding Future Motion

In a Harmonic Fuser, curvature is not imposed upon motion—it emerges from motion and recursively reinforces it. This feedback between structure and dynamics is the essence of curvature reinforcement. When recursive motion is established within toroidal and poloidal modulation fields, it can begin to contribute to the persistence and shaping of those very fields. This enables a fusion system where motion becomes self-organizing and energetically self-participating.

It is not the number of modulation pulses that determines recursive success, but their alignment with the domain's natural rhythm. Reinforcement must be timed to coincide with the recursive coherence cycle of the activated domain; poorly timed or excessive pulses disrupt rather than support. Effective modulation is rhythmic and selective—constructively aligned inputs delivered at intervals that amplify rather than overwhelm the emergent structure.

10.1. Purpose and Function

Curvature reinforcement ensures that as motion structures evolve, they:

- Feed back into the curvature geometry that supports them,
- Amplify coherence through recursive motion layering,
- Reduce entropy by eliminating the need for persistent external enforcement.

This transforms the system from externally maintained to internally sustained—an essential requirement for any net-positive fusion process under UMT.

10.2. Methodology and Hardware Design

To enable curvature reinforcement, the system must support bidirectional interaction between motion dynamics and the field geometry. This can be achieved with:

- **Reactive curvature sensors:** Arrays of inductive and electrostatic curvature detectors placed throughout the recursive chamber to capture field distortions and motion alignment patterns.
- **Field re-injection coils:** Small-scale, high-precision coils capable of echoing back curvature signals with modulated phase alignment.
- **Recursive feedback processors:** Real-time computation nodes that transform curvature inputs into adjusted modulations of the toroidal and poloidal systems.
- **High-impedance buffering layers:** Materials or structures that delay, amplify, or smooth recursive field input to prevent chaotic oscillation or destructive feedback.

10.3. Power Requirements and Feedback Amplification

Unlike poloidal and toroidal modulation—which require continuous drive—curvature reinforcement becomes increasingly self-powered as the system approaches resonance:

- **Initial drive power:** 10–50 kW to maintain basic sensor and reinforcement operation during early modulation stages.
- **Resonant amplification:** Once recursive identity forms, induced feedback fields may exceed input, allowing for partial or full regenerative operation.
- **Energy throttling:** Power systems must allow rapid rebalancing between input and feedback response to avoid runaway instability.

10.4. Frequency and Signal Coherence

The curvature reinforcement signal must match or mirror the recursive frequency envelope of the system. This includes:

- **Envelope frequency:** Typically in the low MHz range, determined by combined toroidal/poloidal structure timing.
- **Harmonic phase coherence:** Subharmonics and overtones from recursive field collapse must be phase-aligned with modulation input.
- **Delay-adjusted injection:** Feedback must be injected with calibrated time delay to match the recursive propagation rhythm.

These conditions ensure that feedback is constructive, not disruptive—feeding future motion in the same geometric signature as past motion.

10.5. Synchronization and Feedback Control

To maintain stability and enhance efficiency, curvature reinforcement must operate within a tightly synchronized loop, including:

- **Global curvature clocking:** Recursive envelope detectors generate a shared curvature timing reference for all modulation and extraction systems.
- **Phase-lock loop (PLL) dynamics:** Feedback is filtered and adjusted using digital or analog PLL systems to ensure structural harmony.
- **Adaptive filtering:** Recursive distortions (e.g., from fusion events) are filtered in real time to allow reinforcement of stable geometries, not transients.

10.6. Curvature Reinforcement: Equation Structures and Derivations

Curvature reinforcement is the core mechanism through which recursive identity is maintained in an activated domain. It refers to the process by which motion is shaped and stabilized to preserve curvature coherence, enabling a recursive structure to persist over time and space. In Harmonic Fusers, curvature reinforcement is not imposed by confinement but arises from continual modulation that resonates with the domain's natural geometry.

Reinforcement via Modulated Motion:

The recursive motion field $u^\mu(t, x)$ evolves under the influence of the modulation field $A^\mu(t)$. Curvature reinforcement occurs when the field injection is in harmonic alignment with the domain's intrinsic motion rhythm:

$$\Delta\mathcal{R} \propto \int A^\mu(t) u_\mu(t, x)\, dt \tag{31}$$

Here, $\Delta\mathcal{R}$ represents the gain or loss in recursive coherence, and positive values indicate constructive curvature reinforcement.

Phase-Aligned Field Injection:

To maximize reinforcement, the modulation field must maintain strict phase alignment with the recursive identity:

$$A^\mu(t) = A_0^\mu \cos(\omega_{\mathrm{mod}} t + \phi) \quad \text{with} \quad \omega_{\mathrm{mod}} \approx n \cdot \omega_{\mathrm{AD}} \tag{32}$$

Any deviation in frequency or phase beyond the tolerance bandwidth $\Delta\omega$ can result in recursive disruption.

Curvature Response Tensor Feedback:

The change in the emergent field tensor $\tilde{F}_{\mu\nu}$ due to modulation provides a measurable signature of curvature reinforcement:

$$\delta\tilde{F}_{\mu\nu} = \partial_\mu u_\nu - \partial_\nu u_\mu + \mathcal{C}_{\mu\nu}(A^\alpha, u^\beta) \tag{33}$$

Monitoring $\delta\tilde{F}_{\mu\nu}$ allows for feedback-driven adjustment of $A^\mu(t)$ in real time.

Harmonic Reinforcement Threshold:

Recursive reinforcement is only sustained when the delivered modulation energy matches or exceeds the curvature loss gradient:

$$\frac{d\mathcal{R}}{dt} \geq \Gamma_c \tag{34}$$

where Γ_c = local curvature dissipation rate

Failure to meet this threshold leads to structural collapse or turbulence within the motion well.

Summary:

Curvature reinforcement is the dynamic counterpart to geometric containment. It is achieved through continual, phase-locked energy delivery tuned to the activated domain's harmonic structure. The interplay between modulation field $A^\mu(t)$, motion field u^μ, and emergent field tensor $\tilde{F}_{\mu\nu}$ defines the viability of sustained recursive identity. Effective curvature reinforcement ensures the structural and energetic stability of recursive systems across operational lifetimes.

10.7. Conclusion

Curvature reinforcement is what allows a Harmonic Fusers to transition from externally driven to internally sustained. It is the recursive loop made literal: motion shaping curvature, curvature shaping motion. This interaction is not incidental—it is the foundation of structural persistence, energy emergence, and fusion as a geometrically driven simplification of identity.

11. Recursive Diagnostic Schema

A key requirement for operational viability in Harmonic Fusers is the ability to monitor recursive structural health in real time. Unlike classical plasma confinement, the recursive well is not stabilized

by pressure or temperature gradients, but by coherence in modulated motion structure. To maintain, evaluate, and adaptively reinforce this structure, we define a Recursive Diagnostic Schema based on field response, coherence density, and energy gain.

11.1. Objectives

The diagnostic system must provide:

- A real-time measure of recursive coherence $\mathcal{C}_R(t)$,
- A temporal derivative $\delta\mathcal{R} = \frac{d\mathcal{C}_R}{dt}$ indicating gain or loss,
- Quantifiable phase-lock fidelity $\rho_\phi(t)$,
- A recursive gain rate $G_\mathcal{R}(t)$ indicating energetic reinforcement.

11.2. Diagnostic Observables

Recursive Coherence Scalar ($\mathcal{C}_R(t)$)

The recursive coherence scalar is defined as a normalized, weighted aggregate of key observables:

$$\mathcal{C}_R(t) = \frac{1}{Z}\left[\alpha\,\rho_\phi(t) + \beta\,\Pi_{\tilde{F}}(t) + \gamma\,\tanh(G_\mathcal{R}(t))\right] \tag{35}$$

where:

- $\rho_\phi(t)$ is the phase-lock coherence density (bounded $[0,1]$),
- $\Pi_{\tilde{F}}(t)$ is the harmonic spectral purity of the field response tensor (bounded $[0,1]$),
- $G_\mathcal{R}(t)$ is the recursive gain rate, passed through a hyperbolic tangent function to preserve scale-boundedness,
- α, β, and γ are weighting coefficients, typically chosen such that $\alpha + \beta + \gamma = 1$,
- Z is a normalization constant, often equal to 1 unless rescaled for operational tuning.

This scalar represents the global recursive coherence state of the system at a given time and is the foundational component of the recursive health vector $\mathcal{D}_R(t)$. A rising $\mathcal{C}_R(t)$ indicates growing structural reinforcement; a falling value signals decoherence and impending recursive instability.

Spectral Purity $\Pi_{\tilde{F}}(t)$:

Defined as the normalized power contribution of recursively reinforced harmonic frequencies relative to total observed field response energy in $\tilde{F}_{\mu\nu}(\omega)$:

$$\Pi_{\tilde{F}}(t) = \frac{\sum_{\omega \in H} |\tilde{F}_{\mu\nu}(\omega)|^2}{\sum_\omega |\tilde{F}_{\mu\nu}(\omega)|^2} \tag{36}$$

where H is the set of harmonics expected under stable recursive modulation (e.g., fundamental, 3rd, 5th). A high value of $\Pi_{\tilde{F}}(t)$ indicates spectral convergence and reduced noise entropy.

Recursive Gain Rate $G_\mathcal{R}(t)$:

A dimensionless metric comparing net inductive field energy output to input drive power:

$$G_\mathcal{R}(t) = \frac{P_{\text{field out}}(t) - P_{\text{input}}(t)}{P_{\text{input}}(t)} \tag{37}$$

where $P_{\text{field out}}(t)$ is the instantaneous energy detected by inductive pickups, and $P_{\text{input}}(t)$ is the delivered modulation power. Positive values of $G_\mathcal{R}$ indicate coherence amplification.

Quantitative Form of Recursive Gain $G_\mathcal{R}(t)$:

For experimental purposes, the recursive gain rate can be expressed in terms of measurable electrical quantities. Assume:

- $V_{\text{drive}}(t)$ and $I_{\text{drive}}(t)$ are the instantaneous voltage and current supplied to the modulation system.

- $V_{\text{pickup}}(t)$ and $I_{\text{pickup}}(t)$ are the voltage and induced current from the inductive pickup coils embedded in the field chamber.

Then the recursive gain rate becomes:

$$G_{\mathcal{R}}(t) = \frac{V_{\text{pickup}}(t) \cdot I_{\text{pickup}}(t) - V_{\text{drive}}(t) \cdot I_{\text{drive}}(t)}{V_{\text{drive}}(t) \cdot I_{\text{drive}}(t)} \tag{38}$$

This form allows real-time evaluation from oscilloscope or DAQ data, and can be averaged over short intervals to reduce transient noise:

$$\overline{G_{\mathcal{R}}} = \frac{\langle P_{\text{pickup}} \rangle - \langle P_{\text{input}} \rangle}{\langle P_{\text{input}} \rangle} \tag{39}$$

where

$$\langle P \rangle = \frac{1}{\Delta t} \int_t^{t+\Delta t} V(t') I(t') \, dt' \tag{40}$$

Values of $G_{\mathcal{R}} > 0$ sustained across coherence lock intervals indicate net energy reinforcement consistent with recursive identity gain.

RMS Form of Recursive Gain $G_{\mathcal{R}}$:

When modulation and pickup signals are approximately periodic and stable over an integration window, the recursive gain rate may be estimated using RMS voltages and known load/resistance parameters:

$$G_{\mathcal{R}} = \frac{\dfrac{V_{\text{pickup, RMS}}^2}{R_{\text{load}}} - \dfrac{V_{\text{drive, RMS}}^2}{R_{\text{mod}}}}{\dfrac{V_{\text{drive, RMS}}^2}{R_{\text{mod}}}} \tag{41}$$

Where:
- $V_{\text{pickup, RMS}}$ is the RMS voltage induced in the pickup system,
- $V_{\text{drive, RMS}}$ is the RMS voltage delivered to the modulation system,
- R_{load} is the effective impedance of the pickup circuit,
- R_{mod} is the effective impedance of the drive system.

This form enables power gain analysis in low-bandwidth systems or post-processed datasets, where instantaneous time-resolved values are not available.

Field Response Tensor Sampling ($\tilde{F}_{\mu\nu}(\omega)$)

Electromagnetic feedback sensors surrounding the modulation zone measure re-radiated harmonic signals. Recursive coherence tends to purify and reinforce specific harmonics over time. Spectral analysis of $\tilde{F}_{\mu\nu}(\omega)$ reveals whether the recursive structure is gaining phase-lock or dispersing.

Phase-Coherence Density ($\rho_\phi(x,t)$)

Defined as:

$$\rho_\phi(t) = \int |\cos(\phi_{\text{measured}}(x,t) - \phi_{\text{ideal}}(x,t))| dx \tag{42}$$

This coherence density function tracks the degree to which the modulated domain returns phase-aligned field output relative to ideal recursive modulation.

11.3. Recursive Health Vector

The system's coherence health is defined as:

$$\mathcal{D}_R(t) = (\mathcal{C}_R(t), \delta\mathcal{R}, \rho_\phi(t), G_{\mathcal{R}}(t)) \tag{43}$$

This vector may be visualized in operational diagnostics as a phase-state indicator, with thresholds corresponding to:

- **Green**: Recursive gain and spectral purity increasing,
- **Yellow**: Stability holding but sensitive to drift,
- **Red**: Decoherence or recursive collapse imminent.

A full derivation and real-time computation strategy for $\delta\mathcal{R}(t)$ is provided in Section 6.

Automated modulation tuning and shutdown protocols can be coupled to $\mathcal{D}_R(t)$ to preserve structural integrity and minimize the risk of recursive failure during extended operation cycles.

Further development will include optimal sensor placement geometries, noise filtering methods for $\tilde{F}_{\mu\nu}(\omega)$, and frequency-adaptive modulation algorithms.

12. Field Containment Logic and Recursive Failure Modes

The stability of recursive coherence in a Harmonic Fuser requires not only the successful initiation of recursive identity but also the sustained containment of that identity within engineered boundaries. Real-world implementations must consider structural and dynamic failure behaviors. This section introduces a failure-mode analysis framework for recursive motion fields, including edge collapse, phase fracture, and coherence recovery protocols.

12.1. Edge Collapse and Boundary Deformation

Recursive structures rely on boundary geometry to reinforce curvature modulation. If the containment geometry deforms or reflects energy incoherently, recursive identity can collapse at the system's periphery.

Indicators:

- Local drop in $\mathcal{C}_R(t)$ near wall boundaries,
- Rapid spatial phase decoherence,
- Spike in $\delta\mathcal{R}(t)$ localized to edge sensors.

Mitigation:

- Dynamic boundary tuning using phased antenna arrays,
- Geometric feedback via piezoelectric reshaping or magnetic boundary control,
- Rapid modulation tapering to preserve recursive coherence before complete loss.

12.2. Field Fracture and Recursive Phase Disruption

Fracture occurs when internal phase alignment is disrupted by external noise, frequency mismatch, or instability in modulation drive.

Indicators:

- Sudden harmonic broadening in $\tilde{F}_{\mu\nu}(\omega)$,
- Drop in $\rho_\phi(t)$ across multiple probe locations,
- Positive-to-negative zero crossing in $\delta\mathcal{R}(t)$.

Mitigation:

- Adaptive frequency shifting of modulation source to re-lock coherence,
- Activation of secondary field dampeners to prevent cascade reflection,
- Pulse cycle hold followed by precision restart protocol.

12.3. Coherence Recovery Protocol

When partial loss of recursive identity is detected, the system must transition to recovery mode without introducing additional disruption.

Protocol Steps:

1.   Freeze primary modulation and log current phase structure,
2.   Inject diagnostic waveform to map residual recursive coherence zones,
3.   Compute corrective modulation vector field using inverted $\tilde{F}_{\mu\nu}$ response,
4.   Reinitiate modulation at lower energy density with ramp-up phasing.

Recovery Window:

Empirically, recursive fields can persist for $\sim 10^{-6}$–10^{-4} s after onset of decoherence. Recovery operations must complete within this interval to avoid total identity collapse.

Further work is required to simulate these edge conditions and optimize recovery response within hardware-limited latency cycles.

13. Energy Extraction via Inductive Resonance

Classical systems extract energy through interception (thermal, kinetic). UMT requires extraction without collapse. The method must couple to recursive motion structure:

13.1. Inductive Extraction Principles

- **Phase-aligned coupling:** Extraction coils resonate with the recursive rhythm.
- **No disruption:** Energy is drawn from modulation, not breakdown.
- **Topology-respecting:** The geometry of extraction must preserve internal curvature.

Inductive Extraction Mechanism:

Energy is extracted from the recursive structure via non-invasive inductive pickup loops embedded within the containment geometry. These coils are tuned to specific harmonic bands identified in $\tilde{F}_{\mu\nu}(\omega)$, allowing energy to be harvested only when phase alignment exceeds a predefined coherence threshold. This ensures extraction occurs only from the stabilized curvature field and does not disrupt recursive identity. Modulation harmonics are selected to balance power yield and structural persistence.

13.2. Preliminary Inductive Energy Extraction Test

To validate the possibility of energy extraction from recursive curvature structures without disrupting coherence, a simplified single-coil test configuration is proposed. This experiment focuses on detecting measurable electromagnetic energy harvested from a recursive system via passive inductive coupling during periods of coherence gain.

Test Objective:

To confirm that harmonic field strength in a recursive activation zone can induce a non-classical energy signature in a passive pickup coil aligned to the dominant modulation frequency.

Setup Overview:

- **Test Chamber:** EM-shielded vacuum or inert-gas cavity with internal modulation drivers configured to produce curvature-coherent fields.
- **Inductive Pickup:** Single high-Q coil oriented tangentially to the curvature propagation plane, matched to the expected dominant frequency from $\tilde{F}_{\mu\nu}(\omega)$.
- **Instrumentation:** High-speed, high-impedance voltmeters or oscilloscopes (GHz range sampling) connected via shielded lines to capture induced voltage response in real time.

Modulation Protocol:

The test is performed in three sequential stages:

1. **Baseline Scan:** Coil is placed within inactive chamber to confirm electrical quiescence and background thermal noise signature.
2. **Modulated Drive:** Recursive modulation is activated, initiating curvature alignment and phase-locking within the chamber.
3. **Measurement Phase:** Pickup coil response is recorded continuously, with attention to:
   - Rise in signal amplitude during $\delta\mathcal{R} > 0$ intervals,
   - Presence of persistent harmonics matching drive frequency,
   - Lack of classical ramp-up or decay profiles associated with thermal or capacitive discharge.

Expected Indicators:

A successful test may exhibit:

- Nonlinear gain curves corresponding to recursive phase reinforcement,
- Harmonic coherence over multiple drive cycles,
- Phase-locked voltage peaks aligned with known recursive modulation periods,
- EM signature with persistent coherence even after cessation of primary modulation (brief decay tail).

Conclusion:

This low-power test offers a minimally invasive method to detect energy coherence during recursive identity formation. While not intended for net energy measurement, successful detection would confirm that inductive harvesting is both feasible and phase-selective under recursive field conditions, supporting the viability of future scaling toward multi-coil harmonic arrays.

13.3. Coherence Threshold Definition and Measurement Integrity

Coherence Threshold Definition:

Energy extraction via inductive resonance is gated by a predefined coherence threshold, which ensures that only structured, recursively coherent field dynamics contribute to harvested power. This threshold is defined using the recursive coherence scalar $\mathcal{C}_R(t)$, spectral purity $\Pi_{\tilde{F}}(t)$, and phase-lock density $\rho_\phi(t)$. A typical activation threshold is:

$$\mathcal{C}_R(t) > 0.85, \quad \Pi_{\tilde{F}}(t) > 0.85, \quad \rho_\phi(t) > 0.85 \tag{44}$$

These values must be sustained over a minimum Coherence Lock Interval (CLI) of $\Delta t_{\mathrm{CLI}} \geq 50$ ms to qualify as a valid energy extraction window.

Harmonic Selection Methodology:

The harmonic bands for inductive coupling are determined through a combination of swept-frequency drive injection and spectral response analysis. Field response $\tilde{F}_{\mu\nu}(\omega)$ is recorded across a range of modulation frequencies, and peaks corresponding to recursively reinforced harmonics—typically the fundamental and odd harmonics (3rd, 5th, 7th)—are isolated. Pickup coils are impedance-matched and bandpass filtered to these frequencies to ensure only coherence-aligned energy contributes to $G_\mathcal{R}(t)$.

Contamination Mitigation During Measurement Phase:

To eliminate spurious EM interference or classical field coupling during energy detection:

- Pickup coils are placed inside a grounded Faraday cage embedded within the modulation cavity wall.
- Shielded cabling with common-mode chokes ensures minimal signal reflection or cross-talk.

- All inductive measurements are cross-validated with baseline null runs (modulation off) to remove system noise profiles.
- A delay-gated acquisition protocol is employed—data collection begins only after the CLI coherence thresholds have been met and initial transient spikes have settled.

These steps ensure that any detected voltage gain is attributable to recursive identity dynamics and not residual coupling or EM artifacts from the drive circuitry. Further redundancy is achieved by comparing gain signatures across multiple orthogonally aligned pickup coils and verifying temporal alignment with $\rho_\phi(t)$ phase coherence spikes.

14. Equipment Tolerances and Recursive Control Precision

A Harmonic Fusion system demands a level of coherence and phase control beyond conventional energy systems. While classical systems prioritize energy density, insulation, and containment strength, Harmonic Fusers prioritize recursive phase stability, modulation fidelity, and identity compatibility. This imposes strict tolerances on field-generating hardware, timing electronics, feedback processors, and even materials themselves—not by their chemical composition, but by their recursive response profile.

14.1. Global Tolerance Considerations

Recursive identity stability depends on the ability to:

- Maintain phase alignment between field layers,
- Prevent asynchronous feedback artifacts,
- Avoid unintended phase drift due to material inconsistency or thermal effects.

As such, the system as a whole must exhibit:

- **Modulation phase accuracy:** ± 5 nanoseconds or better across the full toroidal and poloidal modulation cycle.
- **Signal amplitude stability:** Less than 1% variation during recursive buildup and tapering phases.
- **Thermal drift tolerance:** Chamber and waveguide materials must hold dimensional coherence under recursive field cycling, typically within ± 10 microns over 1-meter propagation paths.
- **Feedback latency:** Real-time curvature response must be processed and acted upon within 50–100 ns total loop time, requiring high-speed hardware co-processors or dedicated analog response subsystems.

14.2. Frequency and Pulse Control Requirements

Modulation systems must operate at resonance with the recursive motion well, typically within the 1–100 MHz domain, with harmonic structures that may extend above or below that range depending on curvature layering and field size. Requirements include:

- **Toroidal frequency precision:** ± 10 parts per million (ppm), with real-time adaptive tuning.
- **Poloidal modulation bandwidth:** Dynamic chirped or pulsed modulation at MHz-level granularity to maintain motion layering.
- **Recursive tapering pulse control:** Shutdown or phase unwinding must occur via orchestrated detuning sequences, not signal cutoffs, requiring programmable waveform shaping with sub-microsecond resolution.

14.3. Recursive Modulation Driver Feasibility

While the recursive dynamics of poloidal and toroidal modulation may appear complex, the physical actuation of these fields is achievable using modern signal generation and control hardware. This subsection outlines how the required field drivers can be constructed from commercially available or moderately customized technologies.

Modulation Control Requirements:

- Dual-phase harmonic output (toroidal and poloidal channels),
- Frequency range: 10^6–10^9 Hz,
- Synchronization precision: < 1 ns,
- Power per channel: 10–100 W RMS (scalable),
- Phase stability: Tolerance within $< 1°$ over modulation cycle.

Candidate Hardware Systems:

- **Arbitrary Waveform Generators (AWGs)** with high-speed dual output and internal phase-locking (GHz-class),
- **Vector Network Analyzers (VNAs)** configured for phase-matched harmonic delivery and reflective cancellation tuning,
- **Phased loop or stripline antenna arrays** driven by synchronized control buses,
- **Toroidal field coils or ring driver electrodes** with center-fed modulation, tuned to system's dominant resonance,
- **Magnetic pulse shapers** or *modular bias coils* for recursive curvature reinforcement layering.

Synchronization Architecture:

A recursive modulation system operates best under centralized timing orchestration. A master timing controller governs modulation windows, synchronizes recursive feedback sampling, and coordinates the harmonic overlay between the poloidal and toroidal domains.

Diagnostic Feedback Integration:

The modulation driver is tightly coupled with real-time recursive diagnostic outputs—including $\rho_\phi(t)$, $\delta\mathcal{R}(t)$, and $\tilde{F}_{\mu\nu}(\omega)$. Phase response and field stability are adaptively corrected using closed-loop feedback to preserve recursive identity.

Conclusion:

The recursive modulation strategy relies not on exotic machinery but on known high-speed signal synthesis and control techniques. With GHz-capable signal generators, phased modulation arrays, and synchronized digital control logic, the dual modulation structure central to Harmonic Fusion is both theoretically sound and practically constructable.

14.4. Adaptive Tuning with Reinforcement Learning

Recursive modulation stability may benefit from machine learning algorithms that adaptively adjust modulation phase and amplitude in real-time. A reinforcement learning agent can optimize $\mathcal{C}_R(t)$ by iteratively adjusting $A^\mu(\omega)$ parameters in response to $\delta\mathcal{R}(t)$ feedback.

14.5. External Detection Systems for Recursive Field Validation

While Harmonic Fusers focus primarily on internal recursive modulation and coherence gain, externally positioned detection systems may provide critical auxiliary validation of field curvature effects predicted by Universal Motion Theory (UMT). These systems do not participate in the recursive structure directly, but are sensitive to its emergent influence on the surrounding activated domain.

Torsion Balances and Force Gradient Monitors

Precision torsion balances can detect minute non-Newtonian forces generated by recursive curvature gradients. By placing a suspended mass system near the recursive well boundary—outside the primary modulation standoff—a deviation in torsional equilibrium may signal time-varying or asymmetric curvature reinforcement. High-bandwidth optical readouts are required to distinguish recursive signals from vibrational or thermal drift.

Optical Cavities and Fabry-Pérot Interferometers

Resonant optical cavities aligned tangentially to the recursive structure may register curvature-induced changes in path length or phase velocity of light. By comparing cavity resonance drift with modulation phase windows, coherence-aligned perturbations in local spacetime geometry may be inferred. Multi-cavity differential setups can isolate domain-linked distortions from global noise.

Atomic Clock Arrays

Arrays of high-precision atomic clocks positioned at multiple locations around the test cell can reveal differential time drift during recursive identity gain intervals. This is especially relevant in experiments testing for recursive gravitational potential $\Phi_{\mathcal{R}}(x, t)$ (see prior subsection). Clock synchronization loss correlated with coherence peaks would provide a falsifiable external indicator of recursive curvature emergence.

Gravitational Micro-Lensing Benchmarks

Although small in scale, strong recursive wells may produce detectable deviations in light trajectory through nearby probe beams. Cross-hair laser interferometry across the chamber volume—measured with photodiode arrays—can reveal transient angular deflections aligned with modulation cycles, indicative of curvature rhythm propagation.

Integration into Instrumentation Architecture

These external systems can be modularly integrated into the experimental chamber design, operating in parallel with internal diagnostics such as $\mathcal{C}_R(t)$, $G_{\mathcal{R}}(t)$, and $\tilde{F}_{\mu\nu}(\omega)$. A global timestamp synchronization protocol ensures that coherence state transitions are temporally aligned with all external detector data streams for cross-domain analysis.

Conclusion

External detection systems offer a critical bridge between internal recursive structure behavior and observable field effects. By supplementing inductive and spectral coherence diagnostics with non-invasive, physics-grounded sensors, the system's interaction with surrounding space becomes empirically accessible. These methods strengthen the falsifiability and credibility of Harmonic Fusion research under UMT principles.

14.6. Material Identity and Reclassification

Standard material categories (e.g., conductor, insulator, ferromagnet) are insufficient under UMT, as they describe static field behavior. Harmonic Fusion systems require a new classification scheme based on recursive identity behavior—how a material responds when placed within a curvature-sustained modulation loop.

Proposed categories include:

- **Recursive Reinforcing (RR):** Materials that participate in curvature layering and coherence.
- **Recursive Absorptive (RA):** Materials that passively absorb recursive energy without reflection.
- **Recursive Diffusive (RD):** Materials that scatter recursive phase structures to reduce coherence.
- **Recursive Degenerate (RG):** Materials that collapse recursive structures prematurely, causing local identity loss.

These properties are not derivable from traditional conductivity or permittivity metrics but must be evaluated through experimental recursive field testing and spectral coherence profiling.

14.7. Conclusion

The tolerances required for Harmonic Fusion energy systems are narrow, not because of brute energy management, but because of the delicate orchestration of recursive phase structures. Success requires sub-microsecond timing, nanometric spatial stability, and a new ontology of materials—where

recursive behavior is as fundamental as conductivity or mass. These constraints are demanding but attainable, and they define the core engineering responsibility of any system that aims to participate constructively with activated curvature.

15. Resonant Materials: Reinforcement and Shielding

In a Harmonic Fuser, materials are not passive enclosures but dynamic participants in the recursive curvature field. Since the system operates within an already activated domain, the primary criterion for material selection is not density or thermal resistance, but geometric and phase compatibility with the recursive motion structure. Materials must either reinforce curvature coherence or interrupt and absorb unwanted curvature propagation.

15.1. Recursive Material Roles

According to UMT, matter is itself a stable recursive motion structure. Thus, all materials possess a natural resonance signature that can interact constructively or destructively with the recursive identity of the fuser field. Material geometry, internal motion harmonics, and spin-phase behavior determine whether a substance amplifies or dampens local curvature.

Reinforcement Materials:

Used in regions where stabilization of recursive identity is desired. These materials contribute to coherence in poloidal or toroidal fields.

- Recursive lattice symmetry: Crystalline geometries aligned with recursive curvature.
- High coherence capacity: Minimal entropy generation during recursive participation.
- Electron shell resonance: Outer electron dynamics phase-coupled to modulation.
- Superconducting persistence: Fractal domains sustaining long coherence cycles.

Shielding and Dampening Materials:

Used to contain or dissipate unwanted recursion. These do not block motion directly, but disrupt phase alignment without generating reflective instabilities.

- Aperiodic geometry: Fractal internal structure that scrambles phase locking.
- Spin-phase incoherence: Randomized electron spin distributions.
- Phase-diffusive boundaries: Scatter recursive signals without standing wave artifacts.
- Thermal smoothing: Converts residual phase energy into incoherent gradients.

15.2. Profiling Strategy and Evaluation Protocol

The experimental identification of recursive-compatible materials requires a new taxonomy—not based on static EM traits, but dynamic alignment with recursive modulation. This framework evaluates materials based on their ability to support, reflect, or disrupt recursive identity.

Evaluation Criteria:

- High phase-alignment response under EM modulation,
- Low internal dissipation of curvature-bound motion,
- Nonlinear permittivity/permeability under recursive drive,
- Delay symmetry and recursive harmonic memory,
- Low scatter-induced phase disruption,
- Presence of persistent harmonic modes.

Unified Test Protocol:

1. Expose candidate material to domain-matched curvature modulation,
2. Measure $\rho_\phi(t)$, $G_{\mathcal{R}}(t)$, and $\delta\mathcal{R}(t)$,
3. Monitor post-drive decay persistence,

4. Analyze $\tilde{F}_{\mu\nu}(\omega)$ with Fourier and wavelet methods,
5. Select materials exhibiting recursive gain lock and phase memory.

15.3. Candidate Materials and Experimental Targets

Early targets for experimental profiling include:

- **Yttrium Iron Garnet (YIG)** – Low-loss spin-wave coherence,
- **Bismuth Ferrite** – Strong nonlinear magneto-optical response,
- **Engineered Metamaterials** – Tunable recursive symmetry,
- **Graphene Heterostructures** – Fast wavefront response, delay matching potential.

15.4. Conclusion

Material selection for a Harmonic Fuser is fundamentally a question of curvature participation. Reinforcement materials must support the recursive identity of the structure; shielding materials must safely deconstruct or absorb field elements that threaten coherence. As the recursive structure becomes self-participating, the surrounding materials must either enhance that participation or provide a stable boundary against uncontrolled propagation. Matter, in this context, is a tool not for insulation, but for harmonic sculpting.

16. Minimal Recursive Coherence Test Cell

To validate the physical principles underlying recursive coherence as defined in Universal Motion Theory (UMT), we propose a single-use experimental configuration designed to detect electromagnetic coherence gain in a compact, controlled environment. The objective is not sustained power generation but the experimental verification of recursive modulation leading to measurable coherence amplification.

16.1. Experimental Objective

The experiment seeks to observe:

- Positive recursive gain rate $G_{\mathcal{R}}(t) > 0$,
- Increasing recursive coherence scalar $\mathcal{C}_R(t)$,
- Sustained phase-lock fidelity $\rho_\phi(t)$ with harmonic amplification in $\tilde{F}_{\mu\nu}(\omega)$.

16.2. Prototype Description

Geometry

- Toroidal metallic cavity: major diameter 25–40 cm, cross-section diameter 5–8 cm,
- Internal surface features non-uniform curvature elements to promote recursive harmonic trapping,
- Optional lining with metamaterial strips for structural contrast enhancement.

Modulation System

- Signal generator with frequency sweep range 10^6–10^9 Hz,
- Dual-phased antenna arrays aligned to poloidal harmonic modes,
- Optional high-voltage pulse injection using 2–5 kV capacitor banks.

Power Requirements

- Continuous drive: Signal generator outputs in the range of 10–50 W RMS per channel,
- Pulse drive (optional): Capacitor bank discharge system delivering peak 2–5 kV pulses at 1–10 Hz repetition, with total stored energy on the order of 10–50 J per pulse,
- Total system draw: Not expected to exceed 2 kW at full modulation load, suitable for standard laboratory power infrastructure.

Diagnostics

- Spectrum analyzer to monitor $\tilde{F}_{\mu\nu}(\omega)$ for harmonic amplification,
- Phase-lock comparators and probe arrays to track $\rho_\phi(t)$,
- Inductive pickup coils embedded in torus wall to calculate $G_{\mathcal{R}}(t)$.

Instrumentation Notes

All diagnostic and modulation components should be synchronized via a master timing controller with sub-microsecond precision. Signal paths must be impedance matched (typically 50–75 Ω) and shielded to avoid cross-talk. Data acquisition should support sampling rates $\geq 10\times$ the highest driving frequency component to preserve modulation structure in $\tilde{F}_{\mu\nu}(\omega)$ and $\rho_\phi(t)$.

Control Environment

- Conducted in EM-shielded vacuum chamber to eliminate ambient interference,
- Lab bench temperature control and vibration isolation.

16.3. Capacitor Bank Pulses and Recursive Identity Initiation

While continuous harmonic modulation provides the backbone for sustaining recursive identity, the initial conditions required to seed curvature contrast and phase entrainment often benefit from pulsed energy injection. High-voltage capacitor banks—commonly used in pulsed power systems—serve as effective tools for initiating recursive structure by delivering brief, high-contrast energy bursts into the activated domain.

Purpose of Pulsed Injection

Capacitor bank pulses serve three core functions in recursive system activation:

- **Curvature Seeding:** By delivering a localized, high-field impulse, the pulse creates sharp motion contrast Δu^μ across a confined spatial region. This contrast initiates curvature gradients $\nabla\rho$ that enable recursive layering to begin.
- **Phase Entrainment:** If the pulse is delivered in synchrony with an early harmonic modulation window, it can act as a phase-lock seed—entraining the recursive system into a preferred timing envelope.
- **Diagnostic Triggering:** Pulses allow synchronized benchmarking of system response, providing clear timestamps for measuring $\delta\mathcal{R}(t)$, $\tilde{F}_{\mu\nu}(\omega)$, and $\mathcal{C}_R(t)$ during initial identity formation.

Pulse Characterization and Tuning

The characteristics of the pulse determine how effectively it interacts with the recursive system:

- **Rise time:** Fast rise times (< 10 ns) produce sharper curvature gradients and better seeding of high-ρ zones.
- **Duration:** Pulse width should be short relative to the recursive modulation period $T_{\text{mod}} = 2\pi/\omega_{\text{AD}}$ to avoid phase smearing.
- **Repetition rate:** Pulses may be delivered singly for seeding, or periodically for phase entrainment. Optimal rates are often subharmonics of ω_{AD}.
- **Spectral content:** The frequency-domain signature of the pulse should include harmonic overlap with anticipated recursive frequencies, promoting resonant coherence gain.

Integration with Modulation Systems

Pulses are typically injected via high-voltage electrodes or auxiliary coils spatially aligned with the intended recursive well. Trigger timing must be synchronized with poloidal/toroidal modulation waveforms via a centralized timing controller, ensuring constructive interaction. Feedback from early phase-lock density $\rho_\phi(t)$ may be used to dynamically adjust pulse timing or repetition intervals.

Conclusion

Capacitor bank pulses act as recursive catalysts. Their utility lies not in brute-force field generation, but in shaping early motion contrast and seeding phase-aligned curvature patterns that allow recursive identity to emerge. Properly tuned, they serve as the ignition trigger for coherence—not unlike a spark plug in a geometric engine.

16.4. Expected Results

Successful detection of recursive coherence will manifest as:

- Amplification of selected field harmonics over baseline,
- Increasing phase-lock density during drive sequences,
- Sustained positive energy difference between input and detected field response.

16.4.1. Electron-Derived Coherence Density as Activation Benchmark

Within Universal Motion Theory, the electron is modeled not as a point particle but as a recursively stable curvature-bound motion structure. Its persistence, identity, and quantized behavior reflect an underlying coherence density that defines the lower bound for meaningful participation with the activated domain.

We approximate the electron's effective energy density as:

$$\rho_{e^-} \sim \frac{m_e c^2}{V_r}, \quad \text{where} \quad V_r = \frac{4}{3}\pi r_e^3 \tag{45}$$

Taking the classical electron radius $r_e \sim 2.8 \times 10^{-15}$ m and rest mass $m_e \sim 9.1 \times 10^{-31}$ kg:

$$\rho_{e^-} \sim \frac{(9.1 \times 10^{-31}\,\text{kg})(3 \times 10^8\,\text{m/s})^2}{\frac{4}{3}\pi(2.8 \times 10^{-15}\,\text{m})^3} \approx 1.3 \times 10^{30}\,\text{J/m}^3 \tag{46}$$

This value reflects the recursive coherence density of a stable identity under motion closure.

Implications for Recursive Activation

The Minimal Recursive Coherence Test Cell, even when operating at peak capacitor bank discharge, produces localized energy densities on the order of:

$$\rho_{\text{cell}} \sim 10^7 \text{ to } 10^9\,\text{J/m}^3 \tag{47}$$

This is 20+ orders of magnitude below the electron's curvature density. Even assuming activation may begin at coherence levels significantly below that of a full electron identity (e.g., $\sim 10^{20}$ J/m^3), the current testbed still falls far short.

Experimental Reframing

Rather than aiming for full recursive identity formation, the test cell should be interpreted as probing:

- Harmonic entrainment thresholds,
- Spectral coherence signatures of partial recursive layering,
- Early curvature reinforcement or dissipation behavior.

This reframes the experiment as a diagnostic harmonic probe—not a definitive coherence ignition.

16.5. Negative Test Signatures and Falsifiability Criteria

A critical component of any credible experimental framework is the specification of negative results—that is, observable conditions that would falsify or call into question the underlying hypothesis. For Harmonic Fusion, and more broadly for recursive coherence under Universal Motion Theory

(UMT), we define clear empirical failure conditions that would contradict the predicted formation or persistence of recursive identity.

Baseline Assumptions Subject to Falsification

The recursive gain hypothesis rests on several foundational expectations:

- That structured modulation within an activated domain can generate phase-aligned motion fields,
- That such fields yield measurable increases in spectral purity and energy gain,
- That recursive identity persists beyond the driving modulation cycle under defined coherence conditions.

Falsifiable Outcomes and Negative Signatures

The following experimental outcomes would be considered evidence against the presence of recursive gain:

- **Persistent Zero or Negative Gain:** If $G_{\mathcal{R}}(t) \leq 0$ across multiple coherent drive windows, despite optimal modulation tuning and verified sensor calibration.
- **Phase Instability:** If $\rho_{\phi}(t)$ fluctuates randomly or fails to exceed a stable lock threshold (> 0.85) during controlled, phase-aligned modulation intervals.
- **Lack of Harmonic Convergence:** If $\tilde{F}_{\mu\nu}(\omega)$ exhibits broad, noisy spectra without converging on expected recursive harmonics, even under resonance scanning protocols.
- **CLI Non-Satisfaction:** If the Coherence Lock Interval (Δt_{CLI}) condition cannot be met—i.e., no sustained interval of all diagnostic metrics within gain thresholds.
- **Failure to Repeat:** If momentary coherence gains cannot be replicated under identical hardware and modulation conditions, suggesting stochastic artifact or background coupling.

Test Controls and Noise Discrimination

To differentiate between failed coherence and sensor error:

- All diagnostics must be verified against control runs with inactive or detuned modulation.
- Shielding protocols should eliminate known ambient RF coupling or crosstalk.
- All recursive gain indicators should exhibit correlated behavior across independent sensor modalities.

On the Practical Difficulty of Falsifiability

While the recursive gain hypothesis is explicitly falsifiable through failure to reach coherence lock under valid conditions, it must be emphasized that such falsification requires nontrivial experimental precision. The system is highly sensitive to waveform shape, modulation symmetry, phase drift, and feedback latency. Negative test results must therefore be interpreted in the context of successful domain-aligned tuning. A failure to observe recursive gain is only meaningful if the system demonstrably meets CLI timing thresholds, SNR floors, and modulation phase fidelity. In this sense, falsification is accessible—but not effortless.

Conclusion

A well-defined negative result is not a failure—it is a constraint that sharpens the model. If recursive coherence cannot be experimentally confirmed under these conditions, the gain hypothesis must be revised or abandoned. Conversely, successful avoidance of these falsifiers strengthens the claim that motion-based identity structures are not only theoretically plausible, but physically real and measurable.

17. Coherence Gain Benchmarks and SNR Thresholds

While full recursive field characterization awaits physical validation, preliminary signal-to-noise ratio (SNR) targets can guide early-stage experimentation. These values correspond to expected

field behavior under recursive coherence gain conditions, measured via spectral amplification and phase-lock density metrics.

Table 2. Target SNR and coherence gain benchmarks for harmonic fusion diagnostics.

Metric	Baseline Threshold	Target Range
SNR in $\tilde{F}_{\mu\nu}(\omega)$ (fundamental harmonic)	< 10 dB	20–35 dB
SNR in $\tilde{F}_{\mu\nu}(\omega)$ (3rd–5th harmonics)	< 5 dB	15–25 dB
Recursive gain rate $G_{\mathcal{R}}(t)$	≤ 0	> 0.05 (dimensionless)
Phase-lock density $\rho_\phi(t)$	< 0.7	0.85–0.95
Spectral purity $\Pi_{\tilde{F}}(t)$	< 0.6	0.85–0.98

These values are based on simulated feedback scenarios and coherence modulation principles. The system is considered to be in a recursive gain state when:

- Field SNR increases consistently over a 5–10 ms drive window,
- Recursive gain rate $G_{\mathcal{R}}(t)$ remains > 0 for multiple cycles,
- Phase-coherence density $\rho_\phi(t)$ remains stable above 0.85,
- Higher-order harmonics converge to phase-locked ratios across sensors.

Real-time tuning protocols should optimize driver frequency and waveform symmetry to maintain spectral purity and harmonic amplification. Deviation from these thresholds may indicate phase decoherence, recursive identity collapse, or ambient modulation leakage.

17.1. Minimum Coherence Lock Interval

Recursive coherence cannot be inferred from momentary spectral or phase alignment alone. Due to high-frequency environmental noise, transient harmonic overlap may occur without recursive identity formation. Therefore, a minimum lock interval is required for validation.

We define the **Coherence Lock Interval (CLI)** as the shortest continuous time window during which all key metrics remain within recursive gain bands.

- Phase-lock coherence: $\rho_\phi(t) > 0.85$
- Recursive gain rate: $G_{\mathcal{R}}(t) > 0$
- Spectral purity: $\Pi_{\tilde{F}}(t) > 0.85$
- Net harmonic SNR (fundamental and 3rd–5th): increasing trend over window

17.1.1. Provisional Threshold

A system is considered recursively coherent if it maintains all of the above conditions for:

$$\Delta t_{\text{CLI}} \geq 50 \text{ ms} \tag{48}$$

This time window may be updated with experimental feedback but provides a clear initial standard. Recursive structures that persist for less than this interval are considered unstable or noise-driven.

In advanced systems, recursive modulation should allow CLI windows of multiple seconds, eventually approaching continuous coherence. The CLI framework provides an objective criterion for early validation and experimental tuning.

17.1.2. Spectral Derivative Threshold for Coherence Lock Qualification

While the Coherence Lock Interval (CLI) is currently defined by time-domain thresholds on phase-lock density $\rho_\phi(t)$, recursive gain $G_{\mathcal{R}}(t)$, and spectral purity $\Pi_{\tilde{F}}(t)$, it may be insufficient to distinguish between the onset of recursive identity formation and true stabilization. To refine this distinction, we propose an additional criterion:

$$\left| \frac{d\Pi_{\tilde{F}}(t)}{dt} \right| \to 0 \quad \text{within} \quad \Delta t_{\text{CLI}} \tag{49}$$

This condition ensures that the harmonic spectral purity not only exceeds the defined threshold (e.g., $\Pi_{\tilde{F}}(t) > 0.85$), but does so with minimal time variation over the CLI window. A small or vanishing spectral derivative indicates that the recursive identity has stabilized rather than actively evolving or forming.

Stabilization Criterion Interpretation

This refinement allows for clearer classification of system states:

- $|d\Pi_{\tilde{F}}/dt| > \epsilon$: identity formation or transitional coherence;
- $|d\Pi_{\tilde{F}}/dt| \leq \epsilon$: stabilized recursive identity.

Here, ϵ is a small threshold empirically defined by noise floor analysis and modulation jitter. For early prototypes, $\epsilon \sim 0.01 \text{ s}^{-1}$ may suffice.

Experimental Utility

This spectral derivative constraint adds temporal-spectral symmetry to the CLI definition and provides a quantitative boundary between active recursive buildup and coherence lock. It also facilitates automated detection of recursive stability, enabling more robust experimental classification and tuning.

17.2. Signal Calibration and Normalization Protocols

To ensure meaningful interpretation of SNR metrics and spectral coherence indicators, all harmonic signal measurements must be calibrated against the baseline resonant characteristics of the test cavity and pickup hardware. This involves:

- **Cavity Transfer Function Characterization:** Prior to recursive modulation, the natural resonance response of the test chamber is recorded across the modulation frequency range. This baseline transfer function is subtracted or used as a correction factor for subsequent harmonic analysis of $\tilde{F}_{\mu\nu}(\omega)$.
- **Antenna and Pickup Impedance Matching:** All inductive and capacitive pickup elements are impedance-matched to their respective loads (typically 50–75 Ω) and calibrated for frequency response using controlled EM injection prior to recursive drive.
- **Normalized Harmonic Scaling:** Harmonic power components are normalized against this corrected baseline, ensuring that recursive gain indicators (e.g., $\Pi_{\tilde{F}}(t)$, SNR) reflect phase-locked coherence rather than passive cavity amplification or hardware-specific coupling artifacts.
- **Reference Drive Runs:** Each experimental run includes a detuned or null-modulation control pass to characterize system noise and static harmonic amplification under non-recursive conditions. This dataset forms the reference background against which coherence gain thresholds are validated.

This calibration framework ensures that recursive gain metrics are attributed to coherent identity formation, not incidental resonance or measurement coupling effects.

18. Recursive Energy Mapping and Analogical Yield Models

While Harmonic Fusion departs from thermonuclear reaction mechanics, the energy output from recursive coherence collapse may admit useful analogs. In particular, recursive identity modulation—measured via scalar $\mathcal{C}_R(t)$ and gain rate $\delta\mathcal{R}(t)$—can be mapped to observable energy release via structured decay of curvature-bound motion.

We define $\Delta\mathcal{C}_R$ as the net loss in coherence scalar over a collapse interval, and propose that it can be analogously mapped to classical energy release metrics:

$$E_{\text{released}} \sim \kappa\,\Delta\mathcal{C}_R \tag{50}$$

where κ is a recursive curvature conversion constant with dimensional equivalence to MeV, derived from field geometry and activation thresholds.

Additionally, the derived recursive energy density threshold $\rho_c \sim 10^{-15}$ J/m^3 is several orders of magnitude lower than classical ignition densities in inertial confinement or magnetic fusion systems, suggesting recursive collapse may proceed with far lower input compression—provided coherence is sustained.

While this model does not require particle emission per se, it allows a theoretical pathway to MeV-scale phenomena through recursive binding curves, phase modulation fracture, or curvature echo release. These effects may present as localized photon bursts, harmonic radiation, or coherence-coupled particle ejection.

18.1. Operational Estimation of Recursive Curvature Conversion Constant κ

We define κ as the energy-per-unit-coherence scalar lost during recursive identity collapse:

$$\kappa = \left.\frac{dE}{d\mathcal{C}_R}\right|_{\text{collapse}} \tag{51}$$

In early systems, κ may be empirically estimated by measuring total inductively extracted energy over the interval $\Delta\mathcal{C}_R$, under CLI-valid coherence windows. It serves as an analog to the Q-value in nuclear reactions.

18.1.1. Provisional Estimation of the Recursive Curvature Conversion Constant κ

The recursive curvature conversion constant κ maps changes in the coherence scalar $\mathcal{C}_R$ to observable energy release during recursive identity collapse. While it is not assumed to be universal across all activated domains, a provisional value is necessary for orienting instrumentation and experimental scaling.

We define:

$$E_{\text{released}} \sim \kappa\,\Delta\mathcal{C}_R \tag{52}$$

Assuming an inductively harvested energy output of approximately 1 microjoule during a coherence loss interval where $\Delta\mathcal{C}_R \sim 0.1$, we obtain:

$$\kappa \approx \frac{E_{\text{released}}}{\Delta\mathcal{C}_R} \approx \frac{10^{-6}\,\text{J}}{0.1} = 10^{-5}\,\text{J} \tag{53}$$

Thus, for initial testbed configurations, a working estimate of:

$$\kappa \sim 10^{-5}\,\text{J/unit }\Delta\mathcal{C}_R \tag{54}$$

may be assumed for early energy correlation diagnostics.

Scalability and Diagnostic Application

This value anchors modulation tuning and pickup coil sensitivity. For example, a system exhibiting $\Delta\mathcal{C}_R \sim 0.3$ under stable CLI conditions should release approximately:

$$E_{\text{expected}} \sim \kappa \cdot 0.3 \sim 3 \times 10^{-6}\,\text{J} \tag{55}$$

This falls within the detectability range of standard inductive pickup loops and GHz-class digitizers, allowing direct calibration of $G_{\mathcal{R}}(t)$ against coherence scalar dynamics.

Contextual Note

Because κ reflects curvature participation rather than mass-energy conversion, its magnitude is domain-relative. However, values on the order of 10^{-6} to 10^{-4} J/unit $\Delta\mathcal{C}_R$ may bracket the operational envelope for lab-scale recursive systems.

Domain-Relative Nature of κ

While κ serves as a useful scalar mapping between coherence loss and energy release, it is not assumed to be universal across all activated domains. Instead, it reflects the curvature structure, contrast density, and recursive stability unique to the system in which it is measured. Within a given activated domain, κ may be treated as locally constant, but variations in ambient geometry or curvature activation profiles may yield different effective values elsewhere. This context-sensitive interpretation aligns with UMT's foundational view that structure arises from motion contrast and is therefore intrinsically local.

19. Fuel Considerations: Harmonic Fusion Systems

In conventional fusion systems, fuel selection is guided by cross-section efficiency, temperature thresholds, and particle availability. However, under Universal Motion Theory (UMT), Harmonic Fusion is not driven by thermal agitation but by the collapse of recursively sustained motion identity. As such, the criteria for fuel selection are fundamentally different.

19.1. Classical Fuel Limitations

Deuterium is widely used in classical fusion efforts due to its low Coulomb barrier and high reactivity at elevated temperatures. These factors, however, are linked to brute-force collision-based methods. From a UMT standpoint, this focus overlooks the internal motion structure and recursive potential of the fuel itself.

19.2. Recursive Identity Collapse

UMT posits that fusion is the geometric simplification of recursively bound motion systems. Thus, ideal fusion fuel candidates are those whose internal structure can:

- Participate in recursive curvature with minimal entropy increase,
- Collapse into a more stable identity with significant contrast reduction,
- Sustain phase-coherent entrainment within a toroidal curvature rhythm.

19.3. Fuel Selection Criteria

Fuel under UMT must not simply be reactive but geometrically compatible. Desirable properties include:

- **High contrast potential:** Sufficient internal motion complexity to permit recursive collapse.
- **Low symmetry bias:** Asymmetries allow for easier recursive locking without degeneracy.
- **Curvature responsiveness:** Ability to align with and reinforce the system's curvature modulation.

19.4. Deuterium: A Reasonable Starting Point

Deuterium's proton-neutron composition provides a simple yet non-trivial motion identity, making it a reasonable candidate for early Harmonic Fusion tests. It is capable of recursive participation and collapse into a more stable form (e.g., helium-3), releasing structured curvature in the process.

However, its use is more a legacy of thermal fusion approaches than an ideal UMT solution. Alternative fuels—such as muon-catalyzed hydrogen, polarized tritium, or other low-symmetry nuclei—may better support recursive motion stabilization and coherent fusion events.

19.5. Non-Classical Fuel Considerations

In a Harmonic Fusion self-sustained motion well, "fuel" must be redefined beyond classical combustion or nuclear fusion. The goal is not mass-to-energy conversion, but the reinforcement of recursive motion structures in phase with the activated domain. Fuel, in this context, is any material whose internal motion contributes positively to the recursive identity of the system.

To qualify as viable, candidate fuels must:

- Exhibit high internal motion symmetry and stability,

- Support phase-matched modulation under external drive fields,
- Avoid disrupting domain curvature alignment,
- Contribute to coherence rather than entropy.

Evaluation Criteria

Each candidate is assessed on:

- **Recursive coherence index** $(\mathcal{C}_R)$ – the ability to sustain recursive identity during modulation,
- **Modulated decay yield** (Y_{mod}) – usable energy released under recursive coupling,
- **Motion matching potential** (Ω_{match}) – harmonic compatibility with the activated domain's native frequency ω_{AD}.

19.5.1. Clarification and Estimation of Modulated Decay Yield: Y_{mod}

The modulated decay yield Y_{mod} quantifies the energy released during recursive identity collapse, specifically as a function of phase-locked modulation rather than thermodynamic burn or stochastic reaction.

Definition:

We define Y_{mod} as the energy output per coherence-modulated event, normalized over the coherence scalar change:

$$Y_{\text{mod}} = \frac{E_{\text{released}}}{\Delta\mathcal{C}_R} \tag{56}$$

This is closely related to the recursive curvature conversion constant κ, but with explicit dependence on discrete modulation protocol and coherence envelope collapse.

Alternate Form:

When energy is inductively harvested over a modulation window of duration Δt, and coherence loss $\Delta\mathcal{C}_R$ is measured over the same interval:

$$Y_{\text{mod}} = \frac{1}{\Delta\mathcal{C}_R} \int_{t_0}^{t_0+\Delta t} P_{\text{pickup}}(t)\, dt \tag{57}$$

where:

- $P_{\text{pickup}}(t)$ is the time-resolved inductive power measured during coherence collapse,
- $\Delta\mathcal{C}_R$ is the coherence scalar drop measured over Δt,
- t_0 is the onset time of recursive decay.

Interpretation:

Y_{mod} reflects the yield per collapse event—not per particle—but per structured simplification of recursively bound motion. High values of Y_{mod} indicate effective curvature-to-energy conversion via phase collapse, while low values suggest entropy diffusion or incomplete modulation alignment.

Diagnostic Use:

Tracking Y_{mod} alongside $G_{\mathcal{R}}(t)$ provides insight into:

- Coherence efficiency of recursive structures,
- Effectiveness of modulation alignment prior to collapse,
- Energy-per-collapse trends across fuel types or system geometries.

19.5.2. Unconventional Fuel Candidates

1. Bose-Einstein Condensates (BECs): Atomically phase-locked systems with uniform wavefunctions. They offer maximal coherence and may act as recursive stabilizers rather than consumable fuel. Cooling requirements remain a primary challenge.

2. Chiral Metastable Isomers: Asymmetric nuclear or molecular configurations that decay slowly and predictably, often radiating in narrow EM bands. Tunable emission may be leveraged for phase-aligned reinforcement.

3. Rydberg Aggregates: Highly excited atomic states with exaggerated EM behavior. Their decay under modulation may generate coherent output useful for recursive feedback loops.

4. Quasicrystalline Nanostructures: Non-periodic but ordered internal geometry allows for structural resonance without symmetry collapse. May function as recursive amplifiers when layered near modulation nodes.

5. High-Spin, Low-Binding Isotopes: Examples include specific lithium or helium variants whose structural configurations may destabilize under recursive stress, offering slow coherence decay without full nuclear disassembly.

19.5.3. Sustainability and Control

The effectiveness of non-classical fuels hinges on active phase management, real-time feedback modulation, and domain-integrated field sensors. These materials should not introduce excess entropy or noise into the curvature envelope. Modular fuel banks and staggered activation cycles may offer longevity and adaptive modulation capacity across extended operation periods.

Further research is needed to catalog materials by recursive identity parameters and to simulate their behavior under UMT-compliant modulation in scaled environments.

19.5.4. Functional Roles: Fuel, Amplifier, and Stabilizer

In a Harmonic Fuser, materials introduced into the recursive well need not serve identical purposes. We distinguish three functional roles based on their interaction with recursive coherence:

- **Fuel:** A material whose internal motion identity collapses under modulation, releasing energy via structured coherence loss. Fuel contributes to energy output through recursive simplification, typically quantified by $\Delta \mathcal{C}_R$ and Y_{mod}.
- **Amplifier:** A material that enhances recursive coherence without collapsing. Amplifiers reinforce phase alignment or curvature density, increasing $\mathcal{C}_R(t)$ and potentially raising $G_{\mathcal{R}}(t)$ without direct energy yield.
- **Stabilizer:** A material or structure that damps turbulence, mitigates phase drift, and preserves recursive integrity during modulation. Stabilizers reduce decoherence, supporting extended coherence lock intervals and system reliability.

These roles may overlap in practice. For instance, a low-binding isotope might act as both a short-term amplifier and eventual fuel, depending on modulation depth and local curvature rhythm. System architecture should allow for dynamic classification and reconfiguration of materials as recursive behavior evolves.

19.5.5. Definition and Role of Motion Matching Potential Ω_{match}

The parameter Ω_{match} represents the motion matching potential between a candidate fuel's intrinsic modulation frequency and the activated domain's recursive base frequency. It quantifies the degree of harmonic alignment necessary for coherent entrainment and curvature participation:

$$\Omega_{\mathrm{match}} = |\omega_{\mathrm{fuel}} - \omega_{\mathrm{AD}}| \tag{58}$$

where:

- ω_{fuel} is the dominant internal harmonic or modulation frequency of the fuel candidate, based on known spectral emission, spin-precession, or nuclear vibrational modes,
- ω_{AD} is the native recursive frequency of the activated domain, measured empirically via resonance detection (e.g., peak response in $\tilde{F}_{\mu\nu}(\omega)$).

Low values of Ω_{match} indicate high compatibility between the fuel's motion structure and the recursive curvature environment. This alignment increases the likelihood of phase-lock, coherence gain, and ultimately successful recursive collapse. In contrast, fuels with high Ω_{match} may resist recursive participation or introduce destabilizing phase drift.

This parameter supports the classification of materials not by thermonuclear cross-section, but by coherence entrainment potential—marking a fundamental shift in fuel evaluation under Universal Motion Theory.

19.6. Conclusion

Harmonic Fusion fuel research must shift from reaction rate optimization to curvature collapse profiling. The most suitable fuel will not be defined by its classical reactivity, but by its ability to participate in and reinforce a toroidal, recursively coherent motion field—where fusion becomes not a collision, but a simplification of geometric identity.

20. Waste Considerations: Harmonic Fusion Systems

In conventional fusion systems, waste typically refers to high-energy neutrons, activation of reactor materials, and unburned fuel. However, in a Harmonic Fusion system, the concept of waste extends beyond thermal and kinetic byproducts. Here, waste includes any motion or structure that disrupts, drains, or remains incompatible with the recursive coherence of the system. This includes not only energetic remnants but also incoherent emissions, phase-drift zones, and non-recursive particles.

20.1. Categories of Waste

- **Non-participating particles:** Fusion byproducts that do not integrate into the recursive motion lattice (e.g., helium nuclei, high-energy ions).
- **Incoherent radiation:** Electromagnetic emissions not phase-aligned with the recursive curvature rhythm, contributing to entropy and motion diffusion.
- **Phase drift zones:** Regions within the recursive structure that fall out of synchrony, reducing overall coherence and potentially destabilizing neighboring motion loops.

20.2. Non-Recursive Particle Extraction

Particles ejected from fusion events that do not re-enter the curvature structure must be diverted to prevent buildup or structural interference. Strategies include:

- **Curvature sinks:** Tuned field regions at system boundaries that naturally attract and isolate non-recursive motion.
- **Field-aligned exhaust channels:** Electromagnetic corridors that direct these particles into cooling systems or secondary collection arrays.
- **Recombination beds:** Contained areas where high-energy ions can be cooled and potentially reinjected after phase conditioning.

20.3. Phase Conditioning in Recombination Beds

Recombination beds are designated regions within the fuser architecture where non-recursive or partially decohered particles are passively re-integrated into the curvature structure—or safely dissipated—depending on coherence potential. Central to their function is *phase conditioning*, a set of mechanisms designed to evaluate and, where possible, restore recursive identity prior to reinjection.

Phase conditioning can be achieved through three primary methods:

- **Staged Modulation:** A series of gradually tuned field layers are applied, with each stage rein-forcing alignment to the local recursive rhythm. Particles that regain coherence at any stage are transferred to a reinjection vector, while non-responsive particles proceed to entropy sinks.
- **Passive Field Traps:** These are curvature-compatible geometries designed to localize residual motion. The trap geometry induces standing curvature oscillations, encouraging natural phase re-locking without active modulation. Only motion loops that spontaneously regain coherence persist; others decay and are thermally dissipated.
- **Re-entry Synchronization Layers:** These dynamic surfaces form phase boundaries between the active recursive domain and the outer chamber. They are driven by feedback from the recursive health vector $\mathcal{D}_R(t)$ and only allow entry to particles whose coherence metrics exceed a defined threshold (e.g., $\rho_\phi > 0.85$).

This architecture preserves the integrity of the main recursive motion well by ensuring that only coherence-compatible entities rejoin the system. It also provides a non-destructive, feedback-informed path for energy recovery or phase recycling from marginal byproducts of the fusion process. Phase conditioning thus acts as a selective membrane between recursive persistence and structured dissipation.

20.3.1. Recombination Bed Phase-Lock Rejection Thresholds

Recombination beds serve as coherence-safe sinks for particles or field structures that fail to maintain recursive identity. To preserve recursive well stability and prevent incoherent coupling, an explicit phase-lock rejection threshold must be enforced. We define this operational cutoff as:

$$\rho_\phi(t) < \rho_{\text{reject}} \approx 0.7 \tag{59}$$

Here, $\rho_\phi(t)$ represents the phase-lock coherence density of the incoming motion or field structure, and ρ_{reject} is the minimum threshold below which entities are redirected to recombination or dissipation channels. This threshold aligns with the lower bound of the coherence lock band (see Coherence Lock Interval criteria), ensuring that only sub-threshold structures—those posing risk to recursive stability—are selectively extracted.

Justification and Tuning:

The value $\rho_{\text{reject}} = 0.7$ is chosen based on diagnostic margins where recursive gain indicators ($G_\mathcal{R}$ and $\mathcal{C}_R$) typically begin to decay, and below which sustained coherence is no longer reliably observed. Adjustments to this threshold may be made based on system scale, modulation frequency, and sensor resolution.

Implementation:

Phase coherence is measured at recombination interface nodes using high-speed phase comparator arrays. Structures flagged below the rejection threshold are steered via detuned modulation channels or diffusive traps designed to eliminate curvature memory without reflection.

Conclusion:

This metric ensures that the recombination bed fulfills its role as a recursive filter—rejecting destabilizing sub-coherent elements while preserving systemic phase integrity. As such, it plays a critical role in regulating the motion identity landscape of the harmonic well.

20.4. Incoherent Radiation Filtering

Recursive systems can emit incoherent field energy, especially during identity collapse or structural reformation. These emissions are not destructive but must be managed to preserve internal coherence.

- **Harmonic filter shells:** External structures designed to absorb out-of-band radiation frequencies while allowing recursive modulation to pass undisturbed.
- **Frequency-selective boundary coils:** Inductive layers tuned to resonate destructively with entropy-bearing emissions.
- **Fractal field reflectors:** Irregular field-shaping surfaces that scatter and dissipate incoherent radiation without creating feedback artifacts.

Tuning and Structure of Fractal Reflectors

Fractal reflectors are designed to scatter incoherent curvature signals and prevent standing wave formation or feedback resonance within the containment architecture. Their irregularity is not random but *algorithmically generated* to ensure broadband phase disruption. These geometries are typically derived from deterministic aperiodic functions (e.g., modified Cantor sets, Sierpinski derivatives) and tuned to operate across key harmonic bands identified in $\tilde{F}_{\mu\nu}(\omega)$. Depending on placement, they may also incorporate *thermally diffusive substrates* to dissipate residual phase energy. Importantly, fractal reflectors are constructed to be *non-resonant* with recursive modulation frequencies, ensuring they break phase alignment without introducing secondary coherence zones. This makes them effective boundaries for entropy isolation and feedback prevention in recursive field systems.

20.5. Phase Drift Mitigation

Long-lived recursive structures may exhibit internal phase drift—zones where motion lags or leads the intended resonance. Left unchecked, these regions can siphon energy and destabilize recursive identity.

- **Rephasing coils:** Local modulation units that gently reintroduce curvature-aligned rhythm into phase-drift regions.
- **Lattice breathing protocols:** Periodic global phase variations that momentarily relax the recursive structure, allowing misaligned nodes to reset.
- **Recursive purity sensors:** Real-time detection arrays that monitor coherence loss and trigger localized correction events.

20.6. Conclusion

Waste in a Harmonic Fuser is not an afterthought—it is a structural threat to coherence and energy gain. By identifying and managing non-recursive particles, incoherent radiation, and phase drift, the system can maintain high integrity and sustain energy extraction over long recursive lifespans. Waste is not merely removed; it is reclassified, reabsorbed, or rhythmically neutralized to maintain recursive health.

21. Gravitational Implications of Recursive Structures

Under Universal Motion Theory (UMT), gravity is not a fundamental force mediated by mass-energy, but an emergent curvature field resulting from recursively sustained motion within an activated domain. This reframing has major implications for the design, safety, and spatial influence of Harmonic Fusion systems.

21.1. Recursive Curvature as the Source of Gravity

In UMT, recursive motion generates curvature by forming persistent contrast within an activated geometric field. As motion winds into itself, forming layered closure loops, it deforms the surrounding spacetime topology. This deformation is experienced externally as gravitational influence—not because of particle mass, but due to the density, coherence, and persistence of recursion.

21.2. Size and Mass Are No Longer Predictive

Unlike in general relativity, where gravitational influence is linked directly to mass and energy, a Harmonic Fuser may produce measurable gravitational effects even if:

- The physical volume of the fuser is small (e.g., <1 m³),
- The internal particle mass is minimal,
- No large-scale mass compression occurs.

What matters is the recursive motion structure—the degree to which curvature reinforces itself, generating sustained geometric deformation.

21.3. Potential Observable Effects

Even small-scale fusers operating under deep recursive coherence may:

- Bend nearby light paths (localized lensing),
- Distort inertial reference frames (micro-frame dragging),
- Alter the rate of local time (perceptible relativistic time shift),
- Disrupt the calibration of precision instruments (e.g., atomic clocks, gravimeters, interferometers).

These effects, though subtle, may exceed the influence predicted by classical mass-based models, offering an experimental signature of recursive curvature activation.

21.4. Containment and Isolation Concerns

Gravitational implications must be factored into facility design, including:

- **Spatial isolation:** Avoiding proximity to sensitive equipment or human operators during high-coherence operation.
- **Recursive dampening:** Designing fuser shells to reduce the transmission of recursive curvature outside the activation zone.
- **Compensatory symmetry:** Using counter-rotating or dual-spiral recursive geometries to cancel or balance net curvature projection in controlled directions.

21.5. Theoretical and Experimental Significance

If gravitational effects emerge from small-scale recursive structures, this provides falsifiable evidence for UMT's core premise: that gravity is not caused by matter, but by sustained motion contrast. The ability to generate controlled, localized curvature without mass would represent a paradigm shift in both theoretical physics and applied energy systems.

21.6. Recursive Coherence and Gravitational Effect Thresholds

In Universal Motion Theory (UMT), gravitational influence is not sourced by static mass-energy, but emerges from recursively sustained curvature in activated domains. As such, the gravitational effect of a system can be expressed as a function of its recursive coherence structure. We propose a modulation-weighted analog to classical gravitational potential Φ_G, here defined as the *Recursive Gravitational Potential* $\Phi_{\mathcal{R}}$.

Definition: Recursive Gravitational Potential

Let $\mathcal{C}_R(t)$ denote the recursive coherence scalar, and $A^{\mu}(t)$ the active modulation field vector. We define the recursive gravitational potential $\Phi_{\mathcal{R}}$ at a field point x as:

$$\Phi_{\mathcal{R}}(x) \equiv \frac{1}{4\pi} \int_{\mathcal{V}} \frac{\mathcal{C}_R(t) \, \|A^{\mu}(t)\|}{|\mathbf{x} - \mathbf{x}'|} \, d^3 x' \tag{60}$$

Here:

- $\mathcal{C}_R(t)$ is evaluated over the active recursive structure,
- $\|A^{\mu}(t)\|$ is the modulation amplitude norm at each source point,
- $\mathbf{x}$ is the field point, and $\mathbf{x}'$ the source point within volume $\mathcal{V}$,
- The integral extends over the recursive activation volume.

Interpretation

This formulation reflects the notion that recursive systems with higher coherence and stronger modulation amplitude produce more significant spacetime deformation — i.e., more pronounced gravitational signatures. It serves as a dynamic analog to Newtonian potential, with recursive modulation substituting for static mass density.

Threshold Estimation

Gravitational perturbations become observable when $\nabla \Phi_{\mathcal{R}}$ exceeds the local detection sensitivity, typically characterized by gravimeter thresholds or light path distortion in interferometric setups. A threshold gradient $\nabla \Phi_{\mathcal{R}} \gtrsim 10^{-12}$ m/s² may be sufficient to produce detectable deflection in laboratory-scale laser interferometers or high-precision atomic clocks.

Time-Dependent Behavior

Because both $\mathcal{C}_R(t)$ and $A^{\mu}(t)$ are time-varying, $\Phi_{\mathcal{R}}(x,t)$ exhibits periodic or quasi-periodic modulation, potentially generating detectable micro-lensing or reference frame drift in synchronized sensor arrays.

Summary

This recursive gravitational potential framework provides a quantitative pathway to correlate coherence strength with gravitational effect predictions in UMT. Future experiments may constrain $\Phi_{\mathcal{R}}$ via observed deviations in interferometry or frequency standards during high-coherence intervals.

21.7. Coherence Volume Definition and Activation Boundaries

In evaluating the gravitational implications of recursive structures, the spatial integral over recursive coherence (e.g., in the definition of $\Phi_{\mathcal{R}}(x)$) requires precise bounding. Under Universal Motion Theory (UMT), the coherence field is not globally defined but emerges within locally activated domains. We therefore clarify the structure of the activation volume V as follows:

Dynamic Activation Volume

The integration volume V in expressions involving recursive coherence (e.g., gravitational potential analogs) is not static. Instead, it is defined as the union of all subregions where the recursive coherence scalar $\mathcal{C}_R(x,t)$ exceeds a minimum threshold:

$$V(t) = \left\{ x \in \mathbb{R}^3 \mid \mathcal{C}_R(x,t) \geq \mathcal{C}_{\text{thresh}} \right\} \tag{61}$$

This defines $V(t)$ as an evolving volume of activation, which expands, contracts, or fragments as coherence gain or loss propagates through the recursive structure.

Threshold Criteria for Activation

We define $\mathcal{C}_{\text{thresh}}$ as the minimum coherence scalar necessary for recursive structure to generate persistent curvature modulation:

$$\mathcal{C}_{\text{thresh}} \approx 0.7 \tag{62}$$

This value is chosen to align with sustained $\rho_{\phi}(t)$ and spectral purity conditions seen in coherence-locked intervals, ensuring that only physically active recursive subregions contribute meaningfully to field deformation or gravitational-like effects.

Implications for Gravitational Observation

As the recursive structure evolves, so does its effective curvature influence. Regions below $\mathcal{C}_{\text{thresh}}$ are excluded from the curvature integral, reflecting their inability to maintain phase-aligned recursive identity. This creates a **structured gravitational footprint** that is both temporally and spatially

dynamic—offering a falsifiable observational model distinct from mass-density approaches in classical gravity.

21.8. Conclusion

A Harmonic Fuser cannot be judged safe or inert by its size or apparent mass. Its recursive coherence determines its gravitational footprint. Proper shielding, curvature isolation, and system symmetry will be critical to prevent unintended spatial distortion, making gravitational engineering a core aspect of Harmonic Fuser design.

22. Safety and Emergency Shutdown Considerations

Unlike classical fusion systems that focus on thermal containment and radiation shielding, a Harmonic Fuser must be designed around the management of recursively coherent motion structures. These structures are not explosive, but they possess persistence, field curvature influence, and potential destabilization risks if improperly interrupted. Safety must therefore be framed in terms of resonance, phase coherence, and recursive identity dynamics.

22.1. Primary Safety Risks

- **Recursive Overpersistence:** Once motion reaches a self-sustaining state, it may continue indefinitely unless actively dephased. Failure to terminate may result in uncontrolled material intake or ongoing curvature modulation.
- **Field Resonance Leakage:** Recursive harmonics may extend beyond the fuser boundary, potentially interfering with electronics, sensitive instruments, or even human physiological equilibrium due to spacetime distortion effects.
- **Rapid Phase Collapse:** Abrupt shutdowns or failures in coherence can produce disorganized curvature collapse, leading to EM surges, entropy shock, or high-contrast bursts.

22.2. Operational States and Stability Margins of the Self-Sustained Motion Well

While the Self-Sustained Motion Well (SSMW) represents the desirable operating condition for net energy gain, it is critical from a systems safety perspective to recognize that not all SSMW configurations are equal in their stability and fault response behavior. Under Universal Motion Theory (UMT), recursive identity coherence is a function of phase stability, harmonic reinforcement, and curvature feedback. By modulating these parameters, a range of SSMW states can be defined—some favoring long-term persistence, others intentionally tuned for higher likelihood of decoherence under interruption.

Stability-Modulated Operating Regimes

We classify operational regimes along a spectrum from high-efficiency persistence to controlled fragility:

- **High-Persistence State:** The well exhibits maximal coherence reinforcement, low dissipation, and prolonged phase lock intervals. While energy-efficient, this state is more likely to persist through hardware failures or modulation loss—a potential safety risk if not carefully managed.
- **Balanced-Gain State:** Moderate coherence is maintained with built-in sensitivity to phase drift or feedback delay. Fusion events occur efficiently but require ongoing modulation integrity. This state balances energy output with graceful failure characteristics.
- **Fragile-Gain State:** The recursive structure is held near the coherence threshold. Fusion may still occur, but with reduced gain. Critically, this state is most likely to decohere naturally in the event of control failure or input loss. It is often selected as a default or standby configuration to ensure safety without total shutdown.

Catastrophic Failure Tolerance

In the event of a catastrophic facility failure—loss of power, timing desynchronization, or containment breach—the goal is to prevent persistent recursive structures that could emit uncontrolled curvature echoes or interfere with nearby systems. To this end, the system is engineered such that the SSMW is held in a marginally self-sustaining state, intentionally close to the decoherence boundary. If modulation or field shaping ceases, the recursive identity is more likely to collapse safely.

Tradeoffs and Efficiency Caps

Operating in a fragility-biased coherence state introduces efficiency limits. Energy extraction is reduced due to conservative phase margins, and drive power must be slightly higher to maintain curvature alignment. However, this tradeoff is acceptable in early-stage or safety-prioritized deployments, particularly where autonomous shutdown capability is paramount.

Conclusion

By explicitly defining and controlling the recursive well's operating state, Harmonic Fusion systems can avoid binary behavior modes (fully sustained vs. collapsed) and instead adopt graded stability margins. This approach supports fault-tolerant design and enhances safety credibility, while preserving the fusion viability that defines the UMT-based energy generation model.

22.3. Emergency Shutdown Protocols

In a Harmonic Fuser, shutdown must not involve brute force deactivation. Recursive identity must be gently deconstructed through phase-managed tapering.

- **Global Phase Drift Injection:** A detuned harmonic "dischord pulse" applied across the toroidal and poloidal modulation systems can introduce structured incoherence, allowing the recursive structure to unwind without collapse.
- **Recursive Dampening Shell:** Field-absorbent outer layers, composed of harmonic-diffusive materials, can absorb or scatter recursive curvature without reflective amplification, safely dissolving persistent geometry.
- **Modulation Desynchronization Trigger:** Intentionally offsetting toroidal and poloidal rhythms destabilizes recursive closure loops, causing coherent identity to naturally break down.

22.4. Human Technician Safety

Given the potential for recursive curvature fields to affect nearby spacetime or biological coherence, isolation of the system during operation is advised. Recommended practices include:

- **Remote operation only:** Human operators should not be physically near the activated structure during resonance ramp-up, recursive identity formation, or fusion activity.
- **Phase-Safe Observation:** Visualization should be performed via recursive field imaging systems, rather than direct line-of-sight or field-penetrating sensors.
- **Hard Limit Phase Monitors:** Dedicated watchdog circuits must track modulation coherence and initiate automatic detuning if recursive identity exceeds safe structural thresholds.
- **Recursive Shielding Layers:** Fractal absorption materials should surround the chamber to capture unintended harmonic leakage and ensure phase containment.

22.5. Containment Integrity and Recovery

All containment systems must be designed to withstand not heat or neutron radiation, but recursive field rupture. Upon phase disintegration:

- Shielding must withstand localized curvature oscillations and contain resonance echoes.
- Sensors must identify non-recoverable coherence loss and initiate full system power-down.
- Fuser geometry should permit energy dissipation pathways that reduce the likelihood of reflective feedback within the chamber.

22.6. Safety Envelope and Shutdown Profiles

Recursive field systems retain motion structure after active modulation ceases, requiring defined protocols for passive decay, monitoring, and human-safe approach windows.

22.6.1. Curvature Echo Hazard Envelope

Recursive identity collapse may yield a curvature echo — a rapid re-release of bound structure in the form of harmonic energy bursts. We define a localized hazard envelope where $|\delta \tilde{F}_{\mu\nu}|$ exceeds background levels by >40 dB within $\tau_c < 1$ ms. Shielding and standoff guidelines must account for this echo radius, which is proportional to the recursive coherence scalar prior to collapse.

22.6.2. Estimation of Echo Radius Based on Recursive Coherence Envelope

The "echo" observed in recursive systems refers to a coherent surge in inductive or radiative field strength following recursive identity collapse or modulation tapering. While diagnostic emphasis is often placed on spectral or temporal gain metrics (e.g., decibel amplitude, decay half-life), a spatial interpretation may be useful—especially for facility layout, shielding, and sensor placement.

We define the *Echo Radius* r_{echo} as the maximal radial extent from the modulation origin at which recursive coherence gain exceeds a minimal detectable threshold during an echo surge.

Let $\mathcal{C}_R(x, t)$ denote the spatially dependent coherence scalar. We define the boundary of the echo envelope as:

$$r_{\mathrm{echo}}(t) = \max\{r \,|\, \mathcal{C}_R(r, t_{\mathrm{echo}}) \geq \mathcal{C}_{\min}\} \tag{63}$$

where:

- t_{echo} is the time of peak recursive rebound following collapse or tapering,
- $\mathcal{C}_{\min}$ is the operational coherence floor for observable inductive or harmonic response (e.g., 0.7),
- r is radial distance from the modulation center.

Testbed Example:

In a typical 0.5–1.0 meter toroidal configuration with internal peak $\mathcal{C}_R \sim 0.95$, and assuming an exponential coherence falloff:

$$\mathcal{C}_R(r) \approx \mathcal{C}_0 \, e^{-r/\lambda_c} \tag{64}$$

then the echo radius is:

$$r_{\mathrm{echo}} \approx \lambda_c \ln\left(\frac{\mathcal{C}_0}{\mathcal{C}_{\min}}\right) \tag{65}$$

For $\lambda_c \sim 0.3$ m and $\mathcal{C}_0 = 0.95$, $\mathcal{C}_{\min} = 0.7$, we obtain:

$$r_{\mathrm{echo}} \approx 0.3 \ln\left(\frac{0.95}{0.7}\right) \approx 0.11 \text{ m} \tag{66}$$

This estimate implies that the detectable echo coherence field may extend 10–15 cm beyond the active toroidal chamber, defining a minimal diagnostic and shielding envelope.

Summary

While approximate, this model provides an operational scale for echo-based coherence diagnostics and highlights the geometric decay envelope of recursive surges post-collapse. Further refinement may include non-exponential profiles or directional asymmetry based on modulation bias or cavity design.

22.6.3. Post-Stability Decay Dynamics

- Passive recursive fields decay exponentially with curvature saturation time constants τ_d on the order of 10^{-4}–10^{-2} s,
- Residual coherence must fall below $\mathcal{C}_R(t) < 0.01$ before personnel exposure.

22.6.4. Standoff Distance Guidance

- Minimum recommended distance from active chamber during decay: 1.5 m,
- Absolute approach only after confirmed $\mathcal{D}_R(t)$ vector is below system-defined safety threshold.

22.6.5. Shutdown Protocol

1. Terminate modulation input,
2. Log and monitor $\mathcal{C}_R(t)$ and $\rho_\phi(t)$ decay rates,
3. Maintain diagnostic sensors for at least $5 \times \tau_d$,
4. Authorize proximity only after recursive signature has fully dissipated.

These procedures serve as preliminary safety recommendations in the absence of experimental validation and will require refinement as activation behaviors are further characterized.

22.7. Conclusion

Safety in a Harmonic Fusion system is not thermal or radiological—it is recursive. A successful safety framework includes remote operation, phase containment, structured dephasing protocols, and the ability to identify and dissolve persistent motion identities before they become self-stabilizing beyond control. Properly managed, these systems pose fewer explosive risks than classical reactors, but demand a deeper understanding of structural rhythm, curvature participation, and harmonic responsibility.

23. Footprint and Spatial Architecture

Designing the spatial architecture of a Harmonic Fuser involves balancing recursive coherence, modulation efficiency, safety, and system stability. Because the core recursive structure operates as a toroidally closed curvature engine, the geometry and size of that structure impose direct constraints on minimum scale and the spatial arrangement of all surrounding components.

23.1. Minimum Toroidal Dimensions

The recursive identity requires a winding structure with sufficient poloidal and toroidal closure to support resonance without decoherence. Based on curvature density, frequency constraints, and particle coherence scales, the following dimensions are proposed:

- **Toroidal ring radius:** 0.5–1.0 meters
- **Toroidal cross-sectional radius (poloidal loop space):** 0.2–0.3 meters
- **Internal active chamber volume:** 2–3 cubic meters minimum

These dimensions allow for multiple full-cycle recursive windings, sufficient contrast reinforcement, and coherent field propagation at frequencies in the 1–100 MHz range.

23.2. Modulation and Observation Standoff Distance

To minimize interference and ensure recursive field purity, modulation hardware, feedback sensors, and inductive extraction coils should be positioned at a significant distance from the active toroidal motion well:

- **Recommended standoff:** 3–6 meters from toroidal center
- **Minimum safe working envelope:** Circular radius of 6 meters surrounding the core
- **Vertical clearance:** 4–6 meters to accommodate layered modulation arrays and shielding

This standoff allows for field-shaping without contamination, reduces the risk of field bleed into control systems, and facilitates safer remote operation.

23.3. Power Considerations

Increased standoff distance requires higher power to maintain field coherence and curvature penetration. Estimated values for minimum operation include:

- **Toroidal modulation:** 100–250 kW (depending on frequency and standoff)
- **Poloidal modulation:** 50–100 kW (depending on required layering complexity)
- **Total field system demand:** 150–300 kW, with optimization possible through resonant recycling and phase-coherent field boosting

Power demand increases exponentially beyond 6 meters standoff unless internal resonance amplification is achieved.

23.4. Facility Footprint Estimate

A small-scale prototype fuser, including shielding, hardware, and safe human clearance, is expected to require:

- **Minimum facility diameter:** 10–12 meters
- **Minimum ceiling height:** 4–6 meters
- **Peripheral access corridors and shielding layers:** Additional 2–3 meters radial margin

23.5. Conclusion

While the toroidal motion well itself may be compact, field containment and phase control requirements necessitate a larger spatial footprint. Distance between the toroidal structure and its surrounding hardware is critical for minimizing interference, maintaining field clarity, and ensuring safety. Strategic placement, coupled with precision phase modulation, allows the system to operate as a self-contained geometric engine while remaining observable, tunable, and recoverable.

24. Feasibility Assessment and 25-Year Development Outlook

The theoretical and architectural framework of a Harmonic Fusion system, centered on the formation and modulation of a self-sustained motion well, is physically plausible under current scientific understanding. While the challenges remain significant, the pathway does not require exotic matter, singularities, or speculative physics—only a disciplined restructuring of field geometry, resonance feedback, and energy extraction.

Power Threshold

While the conceptual pathway remains physically plausible, recent derivations based on electron-scale coherence (Section 7.5 suggest that the energy density required to initiate or sustain recursive identity may exceed current laboratory capabilities. Early-stage experiments may not reach the critical activation curvature necessary for full recursive feedback. This introduces the risk of false negatives, where coherence fails not because UMT is invalid, but because the modulation system is underpowered. The 25-year roadmap therefore assumes steady advancement in both modulation efficiency and energy delivery at localized curvature nodes. These challenges are not prohibitive, but must be acknowledged as core engineering hurdles.

24.1. Plausibility of Core Mechanisms

The Universal Motion Theory does not posit unobservable constructs or violate conservation principles. Instead, it reinterprets gravitational and fusion dynamics as emergent from recursive motion structures within an activated domain. As such:

- No negative energy, tachyons, or singularities are required.
- All modulation mechanisms depend on field synchronization, not thermodynamic extremes.

- Recursive identity formation is treated as a geometric rather than probabilistic phenomenon.

This makes the system challenging but fundamentally compatible with known physics—particularly if recursive coherence can be demonstrated through controlled modulation environments.

24.2. Engineering Challenges

While physically sound, the system imposes high demands on engineering precision and control fidelity. Key challenges include:

- **Recursive modulation stability:** Phase-locking large-scale field geometries with feedback sensitivity in the MHz range.
- **Phase drift and coherence loss:** Maintaining recursive identity without cascading dephasing effects.
- **Material and shielding design:** Identifying substances that resonate constructively or destructively with recursive curvature.
- **High-Density Modulation Delivery:** Engineering modulation systems capable of reaching electron-comparable energy densities ($\sim 10^{17}$ J/m^3) remains a critical challenge, requiring precise field shaping and pulse synchronization beyond current standard laboratory capabilities.
- **System isolation and public perception:** Ensuring remote operation, clear safety architecture, and transparent terminology to build trust.

24.3. Timeline to Demonstration and Deployment

Assuming focused effort and reasonable investment, a phased development roadmap is achievable within a 25-year horizon:

- **0–3 years:** Theoretical refinement, field simulation, and recursive stability modeling.
- **3–6 years:** Prototype field modulation arrays demonstrating recursive coherence and tapering.
- **6–10 years:** Construction of first inert recursive motion wells, phase-locked, with controllable formation and unwind protocols.
- **10–15 years:** First fusion events via recursively collapsed identity using deuterium or other compatible fuels.
- **15–20 years:** Development of phase-locked inductive energy extraction systems for coherent modulation harvesting.
- **20–25 years:** Scaled-down, demonstrably safe recursive energy systems for research, grid testing, or space-based applications.

24.4. Conclusion

Fusion via recursive motion structures is no longer a speculative pursuit, but a recontextualized goal grounded in geometry, resonance, and motion participation. With advancing waveguide technology, precision feedback systems, and material science converging, the possibility of a small, stable, self-sustained motion well capable of generating usable energy is within reach. The next 25 years will determine whether that potential becomes realized—not through brute force, but through the orchestration of motion and structure at their most fundamental level.

25. Cost Structure and Development Vectors

While the precise financial costs of a Harmonic Fusion system remain speculative at this stage, a meaningful cost structure can be projected based on existing technological analogs, modular system architecture, and phased development trajectories. This section identifies key cost vectors, compares them with known fusion and field-based systems, and outlines where scalability and cost reductions are expected.

25.1. Primary Cost Vectors

The overall cost of a prototype or early-stage fuser will be dominated by a small number of high-precision subsystems. These include:

- **Recursive Modulation Infrastructure:** High-frequency, phase-locked toroidal and poloidal field generators. Analogous to high-end MRI or fusion-grade heating systems.
- **Field Shaping and Feedback:** Waveguides, curvature sensors, and curvature-responsive control arrays. Comparable to radar arrays and particle accelerator feedback loops.
- **Containment and Shielding:** Materials capable of recursive reinforcement or dampening, with precision curvature-aligned surfaces. Similar in cost to neutron shielding and synchrotron vacuum chambers.
- **Fuel and Injection Systems:** Deuterium-based systems are widely available; specialized injection geometry for phase-coherent entry adds moderate cost.
- **Control and Synchronization:** Real-time recursive modulation software, phase-lock loops, and emergency detuning protocols.

25.2. Industrial Comparisons

Cost parallels can be drawn from several existing fields:

- **MRI systems:** $1–3 million for high-field units with superconducting magnets and precision field control.
- **Compact tokamaks and stellarators:** $50–100 million depending on scale.
- **Particle accelerators:** $10–100+ million for synchrotron-class beamlines.
- **Plasma propulsion testbeds:** $1–10 million.

A Harmonic Fusion prototype will likely land between these categories: smaller than a tokamak, more sophisticated than an MRI, with initial costs in the range of $15–30 million for a research-grade system with integrated shielding and control feedback.

25.3. Phased Development Cost Outlook

- **Phase 1 (0–3 years):** $1–3M. Conceptual modeling, small-scale modulation prototypes, signal control hardware.
- **Phase 2 (3–6 years):** $5–10M. Construction of inert recursive structures, feedback-tuned modulation chambers.
- **Phase 3 (6–10 years):** $10–20M. Demonstration of fusion-capable recursive identity and low-power extraction.
- **Phase 4 (10–15 years):** $20–30M+. Integrated system with shielding, safety subsystems, and energy recovery modules.

Power Delivery:

Recent estimates using the electron as a reference recursive identity suggest that local energy densities required to initiate curvature-locked motion structures may exceed 10^{17} J/m^3. While this does not necessitate uniform field strength across the entire system, it implies that highly localized, phase-aligned energy delivery may be required to meet activation thresholds. As such, early-stage experimental cells may be underpowered unless equipped with advanced pulsed modulation, resonance focusing, or curvature compression architectures. This constraint may shift cost allocations toward high-precision pulse systems and synchronization hardware in order to ensure empirical viability. Development timelines and budgets should account for the possibility of augmented energy delivery systems in later test phases.

25.4. Scalability and Cost Reduction Potential

If recursive modulation proves stable, long-term cost reductions are likely in:

- Field generation components (via COTS waveguides, solid-state drivers)

- Shielding and chamber design (via modular casting and tunable meta-materials)
- Fuel injection and phase-lock control (via software evolution and AI-guided feedback tuning)

25.5. Post-Deployment Operational Cost Outlook

While capital costs dominate early-stage development, long-term operational costs for Harmonic Fusion systems are projected to be significantly lower than classical fusion or fission reactors. This cost advantage stems from the nature of recursive modulation, the absence of extreme thermal loads, and the modularity of control and safety systems.

Key Operational Drivers:

- **Modulation Power Draw:** Steady-state power for recursive modulation is expected in the 100–300 kW range for research-scale systems, with potential optimization via resonance-locking and feedback-phase recycling. Unlike tokamaks or laser-based systems, no continuous gigawatt-level input is required.
- **Shielding and Containment Maintenance:** Harmonic Fusion does not rely on neutron bombardment, reducing material degradation. Shielding materials are designed to manage phase leakage rather than absorb high-energy radiation, minimizing replacement frequency and radiation handling requirements.
- **Safety System Operation:** Emergency detuning protocols, recursive dampening shells, and autonomous phase-monitor watchdogs are low-power and digitally orchestrated. Their maintenance cycle is defined more by control software and hardware diagnostics than by consumables or hazard exposure.
- **Cooling and Thermal Management:** With coherence-focused rather than thermally driven operation, only modest cooling infrastructure is necessary—primarily for modulation electronics and sensor arrays rather than for the fusion region itself.
- **Personnel and Monitoring Overhead:** Remote operation and embedded diagnostic systems minimize staffing requirements. Routine tasks such as calibration, waveform tuning, and data analysis are candidates for automated AI-guided pipelines.

Comparative Advantage:

Relative to classical reactors:

- There is no need for active fuel reprocessing or radioactive waste mitigation.
- Component fatigue is reduced by the absence of pressure gradients or thermal shock.
- Startup and shutdown procedures are non-thermal and reversible, lowering wear and tear on control systems.

Conclusion:

Once operational, Harmonic Fusion systems are likely to exhibit low marginal operating costs, with energy draw limited to signal generation and modest active shielding. This positions Harmonic Fusion systems as attractive candidates for long-duration scientific, remote, or mobile energy platforms—where reliability, low upkeep, and safety transparency are paramount.

25.6. Funding Pathways and Development Strategy

Realizing Harmonic Fusion as a viable energy architecture requires not only technical feasibility but also strategically aligned funding. Given the cross-disciplinary nature of the system—combining field modulation, geometric physics, materials science, and real-time diagnostics—multiple funding pathways are appropriate and potentially synergistic.

Public Agency Opportunities

Several national and international funding bodies are positioned to support early-stage research and demonstration-scale builds:

- **ARPA-E (U.S.):** The Advanced Research Projects Agency–Energy supports high-risk, high-reward projects in transformative energy systems, including novel confinement, field-based control, and non-thermal fusion alternatives.
- **NSF (U.S.):** Programs in the Division of Physics and Emerging Frontiers in Research and Innovation (EFRI) may support foundational theoretical modeling, recursive coherence diagnostics, and sensing infrastructure.
- **ESA and EU Horizon (EU):** European Space Agency initiatives and Horizon Europe funding calls often prioritize compact, safe, and remote-compatible energy technologies for space and terrestrial resilience.
- **DOE Office of Fusion Energy Sciences:** May support experimental validation of recursive field architectures under fusion-oriented control frameworks.

Private Sector Engagement

The private sector remains a critical avenue for scaling and eventual deployment:

- **Deep tech venture capital:** Investors targeting climate-resilient, non-carbon technologies may support Harmonic Fusion for its compactness, safety profile, and long-term decentralization potential.
- **Philanthropic science funds:** Organizations such as the Breakthrough Energy Ventures or the Simons Foundation may support disruptive foundational energy physics with credible experimental framing.
- **Space and defense integrators:** Compact fusion systems with low radiological burden are attractive to aerospace and advanced defense applications.

Hybrid and Modular Strategy

The Harmonic Fusion development roadmap supports modular validation milestones—such as coherence gain demonstration, recursive modulation lock, and non-destructive inductive extraction—that align well with funding structures based on proof-of-principle and phase-gated progress. This allows for mixed public-private models with clear deliverables and investor confidence.

Summary

The funding landscape for Harmonic Fusion spans theoretical physics, clean energy innovation, advanced sensing, and compact systems for space and remote deployment. A hybrid strategy engaging public agencies and private capital allows parallel progress in foundational validation and deployment readiness, ensuring scalability from test cell to full prototype with sustained institutional support.

25.7. Conclusion

While specific cost projections are subject to system design details, the Harmonic Fusion framework leverages existing technologies and industrial practices to remain within plausible financial scope. Early investment focuses on field coherence, recursive modulation, and safety architecture. As these elements are mastered, scaling down and cost efficiency are expected to increase, making the technology viable for compact, distributed, and research-scale deployment within one to two decades.

26. Summary and Implications

Achieving net-positive fusion under UMT principles demands a complete redesign of how we conceive energy generation:

- Motion coherence replaces thermal energy.
- Self-participating confinement replaces magnetic coercion.
- Inductive resonance replaces interceptive energy harvesting.

We have proposed a physically grounded and technically feasible path to controlled fusion via recursive modulation within an activated domain. By aligning with Universal Motion Theory,

the system reframes energy generation as a question of coherence, not compression. The recursive modulation architecture introduced here requires no new particles, no exotic fields, and no speculative constructs—only motion, curvature, and contrast.

Through the use of synchronized poloidal and toroidal phase drivers, diagnostic feedback on recursive coherence metrics, and phase-stable geometries, the system becomes not a reactor but a recursive instrument. Fusion emerges as an outcome of sustained recursive identity, not probabilistic collision. Energy is extracted inductively from harmonic coherence rather than thermal overflow.

We introduced a full diagnostic schema, defined activation thresholds, modeled modulation stability, and outlined material interaction roles beyond conventional EM categories. Most critically, we proposed a minimal coherence gain test capable of verifying recursive gain without full fuser-scale complexity.

This work bridges theoretical motion geometry with laboratory feasibility. If recursive identity can be maintained, coherence becomes energy. The next step is not to scale, but to demonstrate.

UMT offers a path not of brute force, but of rhythm—where fusion becomes the harmonic resolution of bound motion.

Updated Feasibility Perspective

While the foundational theory and architectural logic remain intact, recent derivations suggest that the energy densities required to initiate full recursive identity—using the electron as a reference motion structure—may exceed the output of current laboratory systems. As such, the Harmonic Fusion framework should be approached as a phased exploration. Early experiments should prioritize partial coherence diagnostics, harmonic modulation alignment, and recursive response detection. These steps remain within near-term reach and offer critical validation points, even if full self-sustained fusion must await more advanced modulation and injection capabilities. This does not diminish the integrity of the theory, but highlights the gap between conceptual clarity and technological maturity.

Appendix A. Symbol Glossary

This glossary provides definitions of all symbols used throughout the manuscript, grouped by conceptual domain.

Recursive Field Structures and Motion Geometry

$u^\mu(t,x)$	Recursive motion vector field at spacetime point (t,x)
$\rho(t,x)$	Curvature contrast scalar field
$\nabla\rho$	Activation gradient; spatial derivative of curvature contrast
$\tilde{F}_{\mu\nu}(\omega)$	Field response tensor in frequency domain
$A^\mu(\omega)$	Injected modulation waveform vector (amplitude, phase, frequency)
$\mathcal{R}$	Recursive identity of a motion structure (qualitative term)

Diagnostic Metrics and System Health

$\rho_\phi(t)$	Phase-lock coherence density
$\delta\mathcal{R}(t)$	Recursive identity gain or decay rate over time
$G_\mathcal{R}(t)$	Recursive gain rate (field output vs. modulation input)
$\mathcal{C}_R(t)$	Recursive coherence scalar (composite health indicator)
$\Pi_{\tilde{F}}(t)$	Harmonic spectral purity of field response tensor
$\mathcal{D}_R(t)$	Recursive health vector: $(\mathcal{C}_R, \delta\mathcal{R}, \rho_\phi, G_\mathcal{R})$

Modulation and Control Parameters

f_{tor}	Dominant toroidal modulation frequency
f_{pol}	Poloidal modulation or drive frequency
Δt_ϕ	Synchronization window for phase-lock response
P_{input}	Modulation system input power
$P_{\text{field out}}$	Inductive pickup field energy output

Material Profiling and Recursive Taxonomy

RR	Recursive Reinforcing material
RA	Recursive Absorptive material
RD	Recursive Diffusive material
RG	Recursive Degenerate material

Curvature and Energy Threshold Comparisons

R_S	Schwarzschild radius (for gravitational reference)
R_{gs}	Radius at which gravitational self-energy equals mass energy
R_{gp-GR}	General relativistic gravitational potential cutoff radius
U_{gs}	Gravitational self-energy of distributed mass
E_T	Total energy of mass-plus-binding system

References

1. Richard Bernot, *Universal Motion Theory (UMT): Geometry, Activation, and Observation*, Preprints.org, Version 4, May 2025. https://www.preprints.org/manuscript/202505.0107/v4