Article

Real-Time Demand Side Management Algorithm Using Stochastic Optimization

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Abstract: A Demand-side management technique are deployed along with battery energy-storage systems (BESSs) to lower the electricity cost by mitigating the peak load of a building. Most of the existing methods rely on manual operation of the BESS, or even an elaborate building energy-management system resorting to a deterministic method that is susceptible to unforeseen growth in demand. In this study we propose a real-time optimal operating strategy for BESS based on density demand forecast and stochastic optimization. This method takes into consideration uncertainties in demand when accounting for an optimal BESS schedule, making it robust compared to the deterministic case. The proposed method is verified and tested against existing algorithms. Data obtained from a real site in South Korea is used for verification and testing. The results show that the proposed method is effective, even for the cases where the forecasted demand deviates from the observed demand.

Keywords: demand-side management, peak demand control, dynamic-interval density forecast, stochastic optimization, dimension reduction, battery energy-storage system (BESS)

1. Introduction

Uneven energy consumption degrades power quality and translates into high energy cost. Therefore, grid operators put much effort toward reducing peak demand through various methods, such as financial incentives. This objective is known as demand-side management (DSM)[1]. DSM is deployed on the consumer side, as well, to mitigate the peak, thereby lowering the electricity cost. Recently, building energy-management systems (BEMS) have been widely deployed for DSM along with a battery energy-storage system (BESS). In many cases, however, the operation of the BESS is determined manually. Even for an elaborate BESS, the operation strategy is intuitively designed and mostly relies on a deterministic method.

In [2], the authors suggested a typical deterministic approach. A peaking interval is foretold empirically, and the BESS is charged to its full capacity prior to this interval. The BESS is then evenly discharged during the defined period. The wider the peaking interval, the higher is the probability of covering all possible peak occurrences. However, the performance of the peak cut would be less effective as the interval becomes wider due to the energy limit of the BESS. A narrow peaking interval has a high probability of missing the peak, but the discharge effect of the BESS is much denser, and thus, the peak can be cut more deeply as long as the actual peak falls within the foretold interval. In both cases, however, the peak cut performance is generally poor because the interval is fixed as that determined during the offline analysis.

Another prevalent method used by industrial energy consumers is to monitor demand and discharge BESS at its full rate when a peak occurs. The advantage of this method is that the discharge interval can be dynamically adjusted depending on the monitored demand value. Nevertheless, this method could lead to an unintended result, as the amount of discharge energy might often be more than necessary, causing an early depletion of the BESS. To tackle this problem, it is important to

46 know with some certainty when the peak will occur as well as its value. A demand forecast can
47 alleviate this problem,[3]–[7] . sss
48   Research has shown that BESS can effectively restrict the power demand from exceeding the
49 predetermined value and suppress the voltage imbalance factor within the recommended value
50 [8]–[10]. The research in [11] aims to reduce the electricity cost based on time-of-use (TOU) charges
51 and peak power demand charges as issued by grid companies. The BESS is developed to reduce the
52 peak demand and, consequently, the electricity bill for customers. With the use of BESS, the stress of
53 utility companies can be reduced during high peak power demands.
54   The above works use a deterministic approach to DSM [7], [11]–[15]. This is an inadequate
55 representation of real-life occurrences of demand. Electric power demands recorded under practical
56 applications are time-series data with uncertainties and are mostly correlated. A single point out of
57 the sample forecasts the future value of demand at a specific time based on historic data. On the
58 other hand, the density forecast gives a forecast at a certain probability value, because in reality, it is
59 difficult to forecast the demand with certainty at a certain time in the future. Density forecast models
60 are useful not only in forecasting the future behaviour, but also in determining optimal operation
61 and control policies [16]. Most DSM approaches do not take into consideration the stochastic nature
62 of demand.
63   This paper proposes a solution to DSM via an optimal BESS schedule that takes into
64 consideration uncertainties in demand. The approach employs dynamic-interval density forecast
65 (DIDF) to forecast the demand distribution profile a day ahead multiple times in a day horizon.
66 Although the method and subsequent accuracy of the forecast greatly affects the performance of
67 DSM, the specific method is beyond the scope of this study; the authors are preparing this topic for a
68 separate work. In this paper, only the concept and format of DIDF are presented for application to
69 the dynamic scheduling of a BESS. To this end, a dimension-reduction method, termed piecewise
70 peak approximation (PPA), is developed to reduce the dimension of the demand probability
71 distribution (DPD) obtained from DIDF for a faster computational time. The method captures the
72 stochastic nature in demand by using stochastic optimization [17] to provide a robust BESS schedule
73 while satisfying the technical constraint of maximizing BESS efficiency and life cycle. The proposed
74 method is then applied to an actual environment in South Korea to verify the performance.
75   The rest of this paper is organized as follows. Section II describes the proposed approach to
76 DSM via stochastic optimization. Section III discusses the problem formulation. Section IV
77 elaborates on a case study and experimental evaluation of the proposed approach using data from a
78 real site in South Korea. Finally, Section V provides a summary of this paper with spotlights on the
79 main concepts and conclusions.

80 **2. Proposed Approach: DSM Via Stochastic Optimization**

81   This paper proposes a DSM solution made up of three modules. I. Dynamic-interval density
82 forecast module, II. Dimensionality Reduction module, III. Stochastic optimization module

83 *2.1. Dynamic-Interval Density Forecast*

84   A density forecast is generated a day in advance based on empirical data as a probability
85 distribution at each time instance in a day horizon. It is important to capture the uncertainties in
86 demand. Most day-ahead forecast algorithms forecast a single value for each time instance in a day
87 horizon, as shown in Figure 1(a). The problem with this approach is that, in practical applications,
88 electric demand has uncertainties that need to be accounted for, as shown in Figure 1(b). When a
89 deterministic forecast is used for DSM, it is expected that the forecasted demand will be equal to
90 observed demand. When this is the case, the resulting BESS scheduled after design optimization is
91 able to resolve the peak, as shown in Figure 2(a). On the other hand, when the observed demand
92 deviates significantly from the forecasted demand, the BESS is unable to resolve the peak, as shown
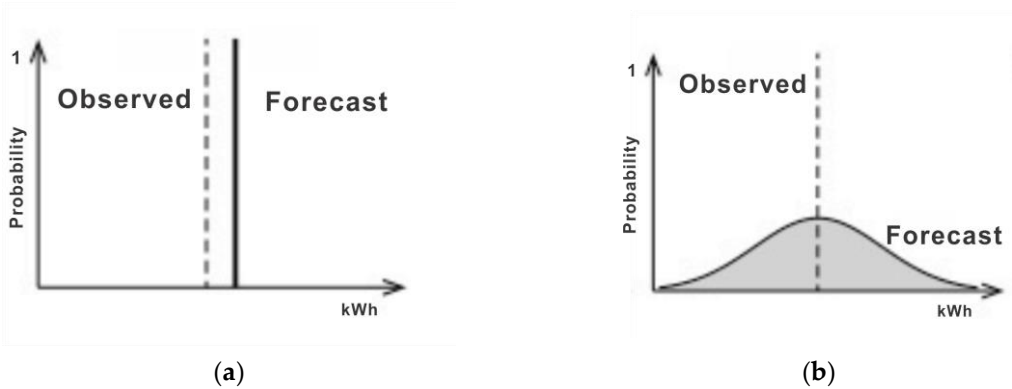
(**a**)   (**b**)

93   Figure 1: Comparison between (a) deterministic and (b) probabilistic forecast models

(**a**)   (**b**)
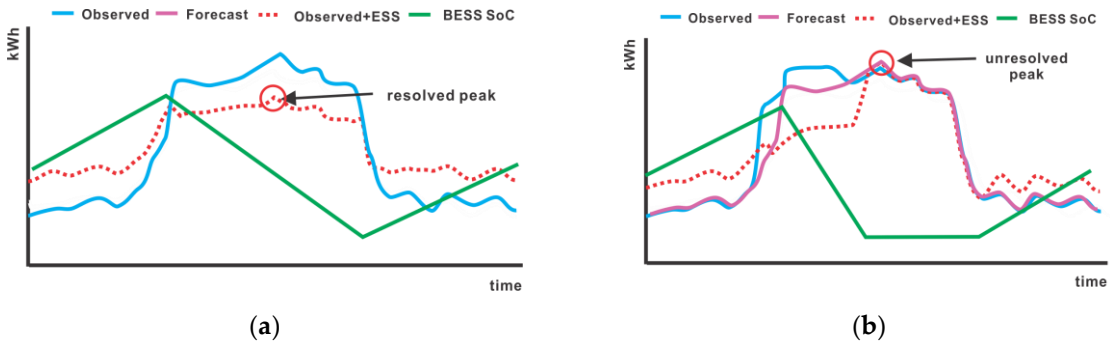
94   Figure 2: Deterministic forecast and BESS schedule analysis (a) when forecast coincides with
95   observed (b) when observed deviates from forecast

96   in Figure 2(b). Electric demand is a random variable that depends on many factors like weather,
97   special events, and socioeconomic factors. The density forecast provides a good description of the
98   uncertainty associated with a forecast and provides a forecast of probability distribution of demand
99   at each time instance in the day horizon, as seen in Figure 3(a). We refer this as demand probability
100   distribution (DPD) profile. The details of the forecast methods are out of the scope of this paper and
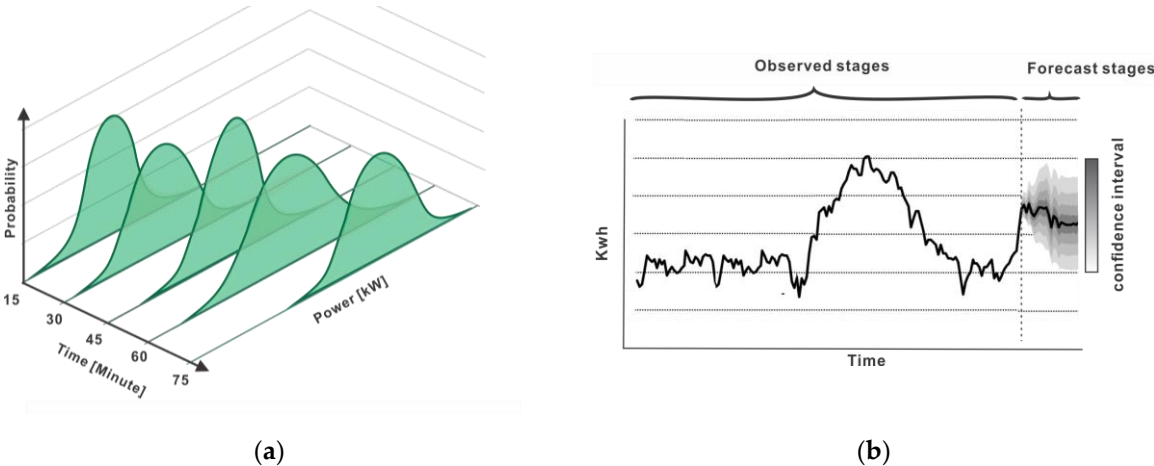101   it is to be considered in authors' another work.

(**a**)   (**b**)

102   Figure 3: (a)Demand forecast as a probability distribution (DPD), (b) Demand distribution forecast
103   with confidence interval

104   As depicted in Figure 3(b), the probability distribution is generally narrow at the beginning of
105   the forecast stages and becomes wider as it gets farther from the current moment. This phenomenon
106   calls for re-forecasting to restore confidence in the forecast. In dynamic-interval forecasting, the
107   forecast is performed multiple times in a day horizon in other to restore confidence in the forecast.

108   The notion is to forecast at wider intervals during the demand off-peak period and narrow intervals
109   during demand peak periods. DIDF helps track the forecasted distribution with high accuracy
110   because the confidence interval of the forecast is improved in the next forecast interval.

111   *2.2. Dimensionality Reduction module*

112   Because of the stochastic nature of the input data, many demand profile scenarios are possible.
113   For example, given demand distribution samples at 15-min intervals in a day horizon, there are n=96
114   sample points, where n is the number of demand distributions in a day horizon. The number of
115   possible demand profile scenarios that can arise from this setup is a^n, where a is the number of
116   samples in each demand distribution. If there are a=5 samples in each demand distribution, the
117   number of possible demand profile scenarios can be evaluated as 5^{96}, which is not feasible for
118   real-time optimization even with a high-performance computer. A Monte Carlo simulation can be
119   used to select plausible scenarios to follow the original demand distribution for a representational
120   selection. However, the number of scenarios to select is a trade-off between accuracy and
121   computational complexity. In real-time applications, time is of the essence; therefore, using dense or
122   high-dimensional data will affect the execution time. From this perspective, it is prudent to perform
123   dimensionality reduction of the data with high fidelity.
124   2.2.1. Time-Of-Use (TOU) Partitioning
125   This paper proposes a method to reduce the dimension of DPD to improve the computational
126   time of the optimization algorithm. This is achieved by reducing the n samples in DPD to m samples.
127   The value of m is influenced by partitions of the contracted TOU price in a day horizon. In Figure 4, a
128   TOU policy of the Korean electric power company (KEPCO) is illustrated. Each partition has a
129   different pricing policy with periods from late morning to afternoon tagged as peak times (red band
130   and yellow), which have a higher price compared to that of early mornings and late evenings (green
131   band). The partitions also vary depending on the current season [18]. A typical day horizon can be
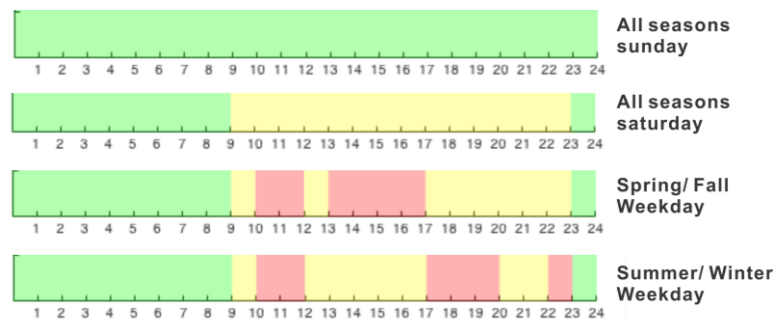132   partitioned into $f = \{1, 3, 7, 8\}$, as shown in Figure 4.

Figure 4: KEPCO TOU daily partitions

133   The value of f depends on the day of week and season. $f = 1$ represents the number of partitions
134   for Sundays in all seasons, $f = 3$ represents the number of partitions for Saturdays in all seasons,
135    $f = 7$ represents the number of partitions for weekdays in spring or fall, and $f = 8$ represents
136   the number of partitions for weekdays in winter or summer [18]. As established above, the
137   maximum number of partitions possible in a day is $w = 8$. The value of the reduced dimension m is
138   a trade-off between accuracy and computation speed. The minimum value that m can take is $m = 8$.
139   When $f < w = m$ or $f \le w < m$ a parameter c is introduced to pad f to reach m. c can be
140   evaluated using (1).

$$c = \begin{cases} w - f, f < w = m \\ m - f, f \le w < m \end{cases}$$

(1)

141   2.2.2. Piecewise Peak Approximation

142   Given a probability distribution forecast of demand, referred to as DPD, $X = \{d_1, d_2, ..., d_n\}$,
143   where d_i is the probability distribution forecasted at the *i*-th time instance, piecewise peak
144   approximation (PPA) is performed after DPD is marked into *m* partitions following TOU. PPA is
145   achieved by approximating all distributions that fall within a partition as a single distribution. The
146   most common measure of central tendency used for such approximations is the average, as used in
147   the deterministic case in [19] and [20]. This idea is also applicable in a stochastic case. However, since
148   the peaking value is of the essence, using the average of demand distributions that fall in a partition
149   could compromise the peak information. To carry the peaking feature, the distributions in a partition
150   are approximated as the distribution with the maximum peak propensity, as illustrated in Figure
151   5(a) and Figure 5(b). The PPA produces a reduced demand probability distribution (RDPD)
152   represented as $H = \{<\hat{d}_1, r_1 >, <\hat{d}_2, r_2 >, ..., <\hat{d}_m, r_m >\}$, where $\hat{d}_k$ is the distribution with the
153   maximum peak propensity in the *k*-th partition, r_k marks the beginning of the *(k+1)-th* partition and
154   end of the *k*-th partition, with $k = 1, 2, ..., m$. r_k corresponds to potential points where TOU
155   pricing changes occur. Preserving these price-change points during dimensionality reduction makes
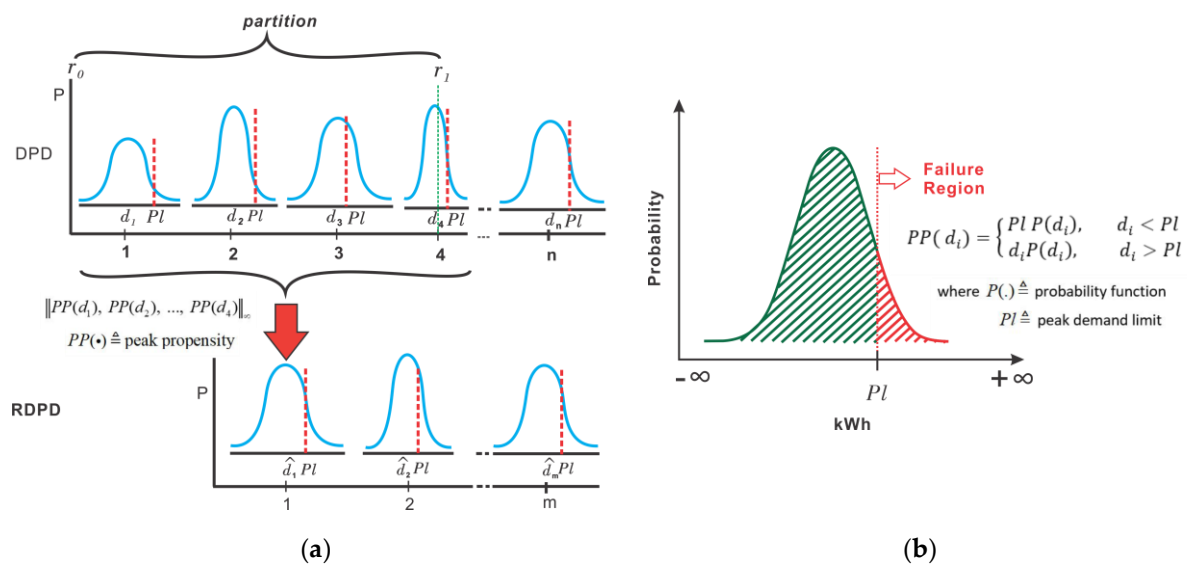156   it convenient to apply the right TOU price during optimization.

(a)   (b)

157   Figure 5: (a) Converting distributions in a partition distribution to a single distribution using PPA
158   (b) Peak propensity or failure region of demand distribution

159   Algorithm 1 describes the PPA process.

Algorithm 1: PPA(X)

---
begin

1. $q = TOU\_band(X)$

2. $c = (w - f)1\{w = m\} + (m - f)1\{m > w\}$

3.   **for** i=1 to c

4. $Z = \max\_sub\_divide(q)$

5.   **endfor**

6.   **for each** partition in Z,k

7. $H_k = \max\_peak\_propensity(Z(k), Z(k-1), X)$

```
8.        r_k = Z(k)

9.    endfor


end
```

160   *2.2. Stochastic Optimization*

161   Stochastic programming is an approach for modelling optimization problems that involve
162   uncertainty. Whereas deterministic optimization problems are formulated with known parameters,
163   real world problems almost invariably include parameters which are unknown at the time a decision
164   should be made. When the parameters are uncertain, but assumed to lie in some given set of possible
165   values, one might seek a solution that is feasible for all possible parameter choices and optimizes a
166   given objective function[17].
167   Stochastic optimization approaches the demand side management (DSM) problem by
168   optimizing (minimizing) the total cost on average, $\min_{x \in X} E[f(D, x)]$, where x is the decision
169   variable and D is demand as a random variable. Stochastic optimization evaluates the best cost and
170   controls the peak demand for a given objective under demand uncertainties.

171   **3. Problem Formulation**

172   The objective of the proposed approach is to provide demand side management considering
173   demand uncertainties. The algorithm performs probability distribution forecast at set intervals using
174   empirical data. The demand probability distribution(DPD) produce after the forecast is
175   dimensionally reduced for faster computation via piecewise peak approximation (PPA). The reduce
176   demand probability distribution (RDPD) is used as input to the stochastic optimization in
177   conjunction with energy tariff and parameter constraints which seeks a robust BESS schedule with a
178   given objective while satisfying BESS's technical and efficiency constraints, as shown in Figure 6.
179   The objective function of the stochastic optimization is divided into two parts:
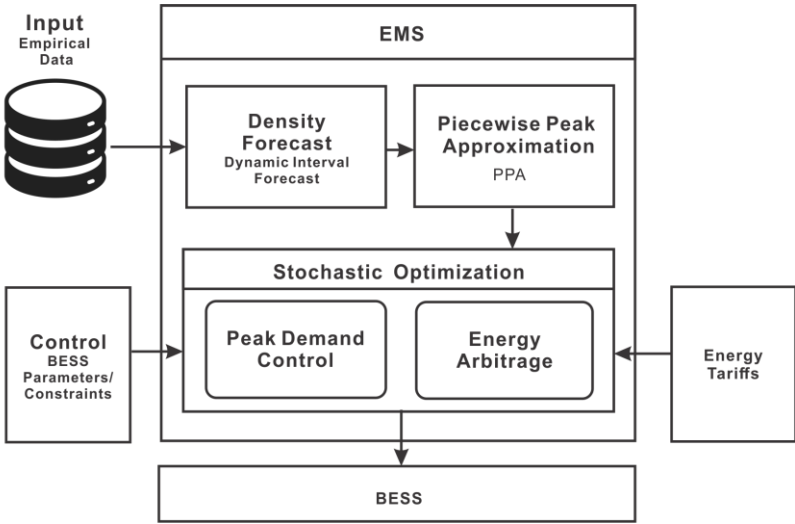

180   Figure 6: Proposed system architecture

181   1.   Energy Cost (TOU): this is computed at every time interval
182   2.   Demand (Peak) Cost: this is evaluated at the end of every month

183   *3.2. Energy Cost*

184   The energy cost represents the amount of energy used within a period multiplied by the TOU
185   energy price. In a distribution sense, the energy cost is the total expected demand multiplied by the
186   TOU energy price, which can be evaluated using (2).

$$\text{Cos}\,t^{TOU} = \sum_{k=1}^{m} g_k \times C_k^{TOU} \tag{2}$$

$$g_k = E[\hat{d}_k + e_k] \tag{3}$$

187   where $\hat{d}_k$ is the k-th distribution in RDPD, e_k is the BESS schedule provided at the k-th instance by
188   the optimization algorithm, C_k^{TOU} is the TOU energy price at the kth instance, g_k is the expected
189   demand of the k-th distribution in RDPD, and $\text{Cos}\,t^{TOU}$ is the total expected cost of energy in a
190   day.

191   *3.2. Demand Cost*

192   The demand cost is the maximum 15-min average power over a month multiplied by the
193   demand price. This is evaluated using (4). The demand cost and energy cost must be unified.
194   Normally, the demand cost is evaluated monthly, whereas the energy cost is calculated at a unit time
195   interval. Because of this difference in units, the demand cost needs to be evaluated correctly at unit
196   time intervals such that the accumulated demand cost over a month is equal to the monthly demand
197   cost, as expressed by (8). The unified daily demand cost can be evaluated using (9).

$$\text{Cos}\,t^D = D_{\max} \times C^D \tag{4}$$

$$D_{max} = \| H_1^{\max}, H_2^{\max}, ..., H_q^{\max} \|_\infty \tag{5}$$

$$H_l^{\max} = \| h_{l1}, h_{l2}, ..., h_{lm} \|_\infty \tag{6}$$

$$h_{lk} = \begin{cases} Pl \times P(\hat{d}_{lk} + e_k), & (\hat{d}_{lk} + e_k) < Pl \\ (\hat{d}_{lk} + e_k) \times P(\hat{d}_{lk}), & (\hat{d}_{lk} + e_k) > Pl \end{cases} \tag{7}$$

$$\text{Cos}\,t^D = \sum_{l=1}^{q} \| \{h_{lk}\}_{k=1}^{m} \times C^U \|_\infty \equiv D_{\max} \times C^D \tag{8}$$

$$\text{Cos}\,t^d = \| \{h_{lk}\}_{k=1}^{m} \times C^U \|_\infty \tag{9}$$

$$C^U = \left(\frac{C^D}{q} \right) / m \tag{10}$$

$$q = \begin{cases} 28, & \text{Feb} \\ 29, & \text{Feb(leap year)} \\ 30, & \text{Sept, Apr, Jun, Nov} \\ 31, & \text{Otherwise} \end{cases}, \tag{11}$$

198   where C^D is demand price for a month, $H_l^{\max}$ is the maximum demand on the l-th day, $D_{\max}$ is
199   maximum demand for a month, h_{lk} is the peak demand distribution at instance k on the l-th day,
200   $\hat{d}_{lk}$ is the demand distribution at an instance k in RDPD on l-th day, Pl is the peak demand limit, P(.)

201 is a probability function, C^U is the unified demand price at any instance in a day, $\text{Cos}\,t^D$ is the
202 monthly demand cost, $\text{Cos}\,t^d$ is the unified daily demand cost, q is the number of days in a month,
203 with $l = 1, 2, ..., q$.

204   By KEPCO policy, the demand value used to evaluate demand cost is obtained using (7); thus, if
205 the current recorded demand is greater than the Pl, the recorded demand value is used in calculating
206 the cost. If the recorded demand is less than the Pl, the value of the Pl is used to compute the cost.
207 This is evaluated to achieve peak demand control.

208 *3.3. Optimization*

209   The objective function of the stochastic optimization is formulated as the ensemble of energy
210 cost and demand cost (EC) (12). The design optimization algorithm provides BESS control schedule
211 candidates at each iteration of the optimization process, $u_x = e_1,\ e_2,...,e_m$, based on conditions
212 established as constraints to the objective function, where u_x is the x-th BESS control schedule, e_k is
213 the BESS value scheduled at the kth instance in u_x, $x = 1, 2, ..., s$, s is the number of iterations via the
214 optimization algorithm.

215   For each u_x, the ensemble of energy cost and demand cost is evaluated, this is evaluated as the
216 minimum of both parameters. This is repeated for each iteration of the BESS control sequences until
217 the one with the least cost on average is found. The objective function for the stochastic optimization
218 is formulated as (14).

$$EC = f(H, u_x) \tag{12}$$

$$f(H, u_x) = \min(\sum_{k=1}^{m} \text{Cos}\,t_k^{TOU}, \text{Cos}\,t^d) \tag{13}$$

$$\arg\min_{u_x} f(H, u_x) \tag{14}$$

219 An inequality constraint is imposed on the objective function such that the state of the charge (SOC)
220 of the BESS at the beginning of a day should be the same as that at the end of the day (15).
221 Furthermore, the SOC of the BESS should be in the range of soc_{max} and soc_{min}, thus maximum and
222 minimum SOC, respectively as expressed by (16).

$$soc_0 = soc_{final} \tag{15}$$

$$soc_{min} \leq soc_k \leq soc_{max} \tag{16}$$

$$soc_k = soc_{k-1} + e_k \frac{\gamma}{S_{BESS}} \tag{17}$$

$$\gamma = eff^{ch}, \gamma = \frac{1}{eff^{dch}}, \tag{18}$$

223 where soc_k is the SOC at instance k; soc_0 and soc_{final} are the initial and final SOC respectively,
224 γ is the efficiency of BESS, eff^{ch} and eff^{dch} are the charge and discharge efficiency respectively.
225 The constraints guarantee that the optimization returns feasible solutions.

226

227 **4. Case Study**

228   In this section, the proposed approach is implemented with a case study and simulated for
229 results. For the case study, 2016 and 2017 data from a real-site in South Korean was obtained. The
230 data is recorded at an interval of 15 min in a day horizon, because of KEPCO's policy of recording
231 peak demand in 15-min intervals. The 2016 data is used for the daily interval forecast for 2017. The
232 2017 forecast data is used to implement the DSM algorithm, and the observed data is used for testing
233 and result analysis.

234   By convenience, a density forecast of 250 elements per each distribution is used.
235 Dynamic-interval density forecast (DIDF) is performed following TOU partitions in a day horizon to
236 obtain demand probability distribution (DPD). DPD of n dimensional space is reduced to m
237 dimensional space which is referred to as a reduced reduce demand probability distribution (RDPD)
238 via PPA for stochastic optimization. During peak times, the forecast is performed after every 15-min
239 interval, whereas at off-peak times, the forecast is made on the order of hour intervals, followed by 2
240 hours, 3 hours, etc., depending on the size of the off-peak interval. Stochastic optimization is
241 performed using RDPD. Particle-swarm optimization (PSO) [21] with a swarm size of 500, inertia of
242 0.6, and 200 iteration is used to implement the stochastic optimization procedure using the
243 parameters in Table I at intervals following DIDF. TOU pricing is based on data from KEPCO [18].

244   Table 1 shows the parameters used for the case study. The simulation was realized in MATLAB
245 2014 on an Intel i5 processor with 16 GB of RAM. On average, it takes 55 s to complete a single run of
246 the stochastic optimization.

247   Table 1. Simulation parameters

Parameters	Symbols	Symbols
Peak demand limit	Pl	6610 kW
BESS capacity	S_{BESS}	500 kWh
BESS efficiency	γ	90%
Initial SOC	soc_0	0.2
Maximum/Minimum SOC	soc_{max} / soc_{min}	0.9/0.2
Number of sample points	m	24
Number of distributions in a day,	n	96
Number of samples in a distribution	a	250

248

249   Figure 7 and Figure 8 present the results of the robust BESS schedule as applied to the expected
250 demand. The results also show a comparison of the expected demand under the BESS schedule as
251 well as when the BESS is absent. Each figure presents the expected demand, SOC of BESS as well as
252 the cost for expected demand when the BESS schedule is applied and when it is not. At the
253 beginning of the day, BESS starts operation from the minimum SOC value, and the same value is
254 maintained at the end of the day. The optimal BESS schedule obtained after stochastic optimization
255 is verified against the most probable demand of the distribution. Figure 7(a) presents a stochastic
256 optimization algorithm considering only energy arbitrage. It can be observed that the BESS
257 discharges heavily during the critical TOU periods (peak times), indicated by the red band, because
258 the TOU price is high during this period. As such, it discharges prior to charging to full capacity
259 during the off-peak period, in which TOU price is cheaper. Figure 7(b) shows the result where the
260 algorithm considers only the peak demand cost. Figure 8 presents the results where the algorithm
261 considers both the peak demand cost and energy arbitrage. In Figure 7(b) and Figure 8, the BESS
262 schedule discharges heavily during the peak periods from 10 am to 2 pm to resolve the demand peak
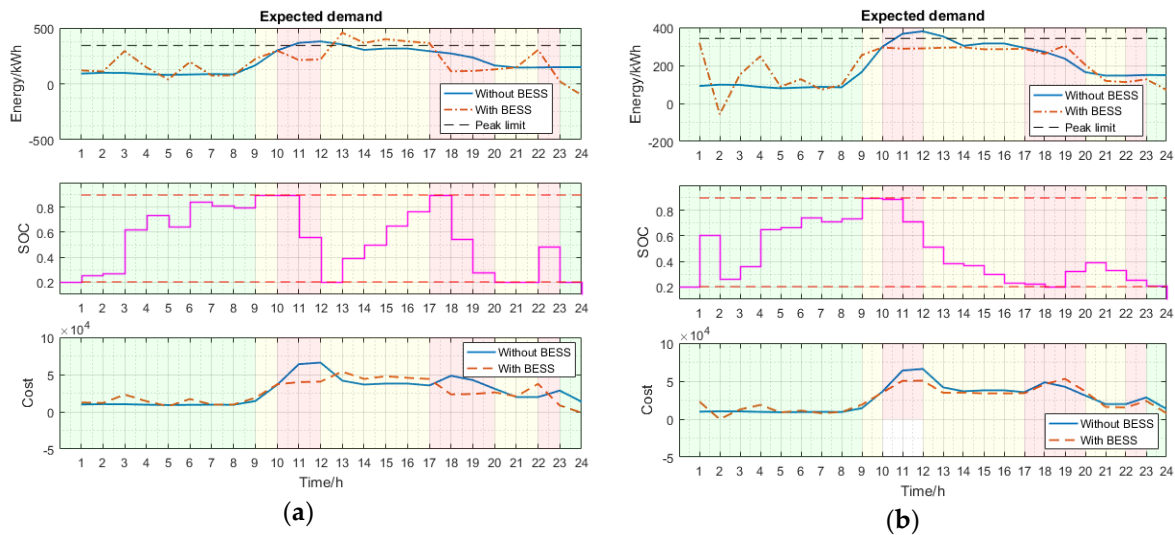263 exceeding the peak limit.

Figure 7: (a) DSM algorithm results considering only energy arbitrage (b) DSM algorithm results considering only peak demand control
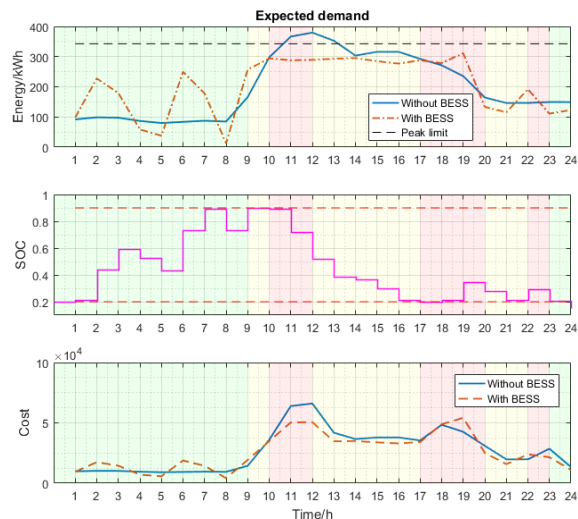

Figure 8. DSM algorithm results considering energy arbitrage and peak demand control

From Table II, it can be observed that implementing the algorithm considering only energy arbitrage cost performs poorly in terms of peak reduction, but it is the best in terms of cost reduction. This is because it seeks only to reduce cost and not peak demand. With a previous peak value of 1763 kW, the algorithm causes a new peak of 2072 kW, representing a 18% increment in peak. In contrast, it provides the best yearly cost reduction of ₩35,296,338 in 2017. When the algorithm features only peak control, it is able to reduce the peak from 1763 kW to 1330 kW, which is a peak reduction of 26% and a yearly cost reduction of ₩2,937,306.

An ensemble of energy arbitrage and peak control seeks to harness the benefit of the two algorithms; as such, the results show a reduction of 1308 kW in peak, representing a 26% decrease and a yearly cost reduction of ₩9,636,600.

Although implementing energy arbitrage alone provides the best energy cost, it also results in the worst peak control. The peak control case also has a good peak demand reduction, but also the worst yearly cost reduction. A combination of the two presents a compromise between these two factors to achieve a better cost and the best cost reduction.

281   Table 2. Simulation results

Parameter		Value
Original Peak (Without BESS)		1763 kW
New Peak (With BESS)	Energy arbitrage	2072 kW
	Peak Control	1330 kW
	Ensemble	1308 kW
Peak Reduction	Energy arbitrage	-18 %
	Peak Control	25 %
	Ensemble	26 %
Original Cost (Without BESS)		₩ 235,084,438
Yearly Cost Reduction (With BESS)	Energy arbitrage	₩ 35,296,338
	Peak Control	₩ 2,937,306
	Ensemble	₩ 9,636,600
Yearly Cost Reduction	Energy arbitrage	15 %
	Peak Control	1 %
	Ensemble	4%

282   **5. Discussion**

283   The proposed demand side management algorithm is compared with a deterministic
284   optimization (DO) method using a deterministic day ahead forecast which is predominantly
285   proposed in other research. The deterministic approach forecasts a day ahead demand profile which
286   is used to evaluate an optimal BESS schedule for the next day, as shown in Figure 9(a).

(**a**)   (**b**)
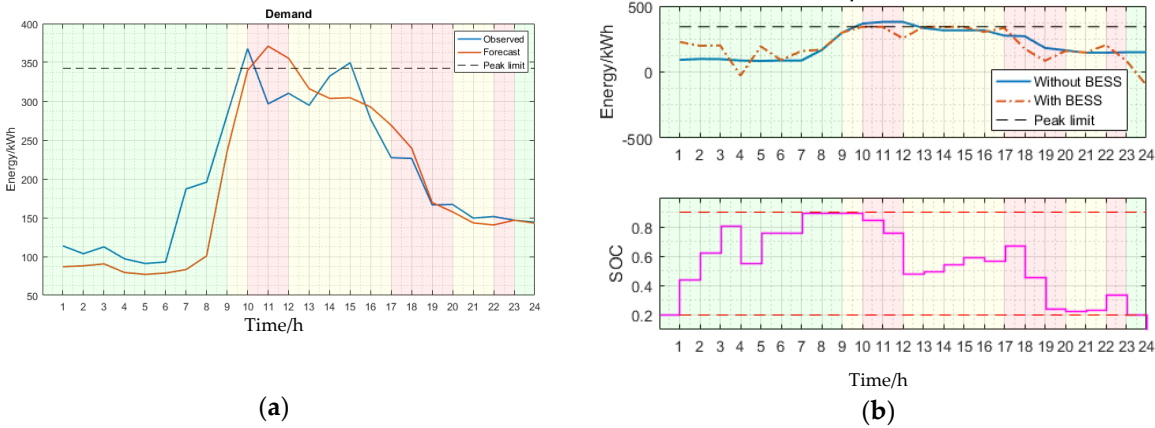
287   Figure 9. (a) Day ahead forecast and observed demand, (b) BESS schedule on forecasted demand
288   using DO

289   Figure 10(b) shows the forecasted demand and the effect of the subsequent BESS schedule that
290   was generated from the optimization algorithm. From the figure it can be observed that although the
291   peak demand is reduced, the reduction strictly follows the peak limit. The peak is reduced from
292   1518kW to 1370kW representing a 9.8% reduction.

293   Figure 10(a) shows the results of the BESS schedule obtained from the optimization algorithm
294   as applied to the observed demand. It can be observed that the BESS schedule generated fails to
295   reduce the peak demand because of inaccuracies in the forecast as compared to the observed
296   demand. The BESS schedule rather increases the peak from 1563kW to 1624kW, representing a 3.8
297   increase in peak demand.

298   Figure 10(b) show the results when the proposed real-time demand side management solution
299   is applied to the observed demand. It can be observed that the real time algorithms perform better
300   since the dynamic interval density forecast, reforecast the demand at set intervals to correct the

301 deviation in forecast. The approaches is able to reduce the peak demand from 1563kW to 1236kW
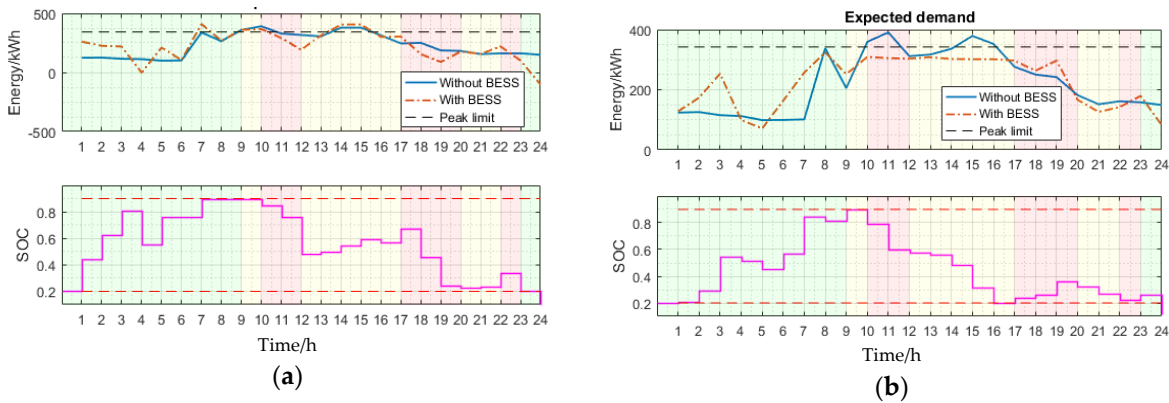302 representing a 20.9% reduction.

Figure 11. (a) BESS schedule on observed demand using DO (b) BESS schedule on observed demand using proposed approach.

6. Conclusion

306   This paper has proposed a DSM solution that incorporates a dynamic interval density forecast
307 with a piecewise peak approximation for stochastic optimization.

308   The DSM solution has been verified using demand data from a real industrial site in South
309 Korea. The results show that energy arbitrage alone cannot reduce the peak demand. In the case
310 where the algorithm implements only energy arbitrage, a peak increase of 18% was incurred. When
311 the algorithm implements an ensemble of energy arbitrage and peak demand cost, the peak demand
312 is reduced by 26%. Unlike the deterministic case, where the forecast is performed once in a day
313 horizon, the proposed solution performs the forecast at set intervals in a day horizon to restore
314 confidence in the forecast should it deviate. This ensures a much more accurate forecast and a robust
315 BESS schedule. For verification the proposed demand side management algorithm is compared to a
316 deterministic algorithm, the proposed method achieves 20.9% in peak reduction while the
317 deterministic case achieves 9.8%. This real-time algorithm is applicable to industrial or commercial
318 settings.

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